

# Model Architecture Comparison

Inputs  
( $u$ ,  $P_{gen}$ ,  $P_{load}$ )

**Physics Baseline**



$$\dot{x} = \eta_i \cdot u \cdot \{u > 0\} - (1/\eta_{ou}) \cdot u \cdot \{u < 0\} - d(t)$$
$$\dot{x} = -\alpha x + \beta \cdot P_{gen} - \beta \cdot P_{load} + \gamma x$$

Outputs  
( $x$ ,  $\dot{x}$ )



Inputs  
( $u$ ,  $P_{gen}$ ,  $P_{load}$ )

**Universal Differential Equation (UDE)**



$$\dot{x} = \eta_i \cdot u \cdot \{u > 0\} - (1/\eta_{ou}) \cdot u \cdot \{u < 0\} - d(t)$$
$$\dot{x} = -\alpha x + f_{\theta}(P_{gen}) - \beta \cdot P_{load} + \gamma x$$

Outputs  
( $x$ ,  $\dot{x}$ )



$P_{gen}$

**Neural Residual**  
 $f_{\theta}(P_{gen})$

Inputs  
( $u$ ,  $P_{gen}$ ,  $P_{load}$ )

**Bayesian Neural ODE (BNODE)**



$$\dot{x} = f_{\theta}(x, \dot{x}, u, d)$$
$$\dot{x} = f_{\theta}(x, \dot{x}, P_{gen}, P_{load})$$

Outputs + UQ  
( $x$ ,  $\dot{x}$ ,  $\sigma$ )



$\sigma$

**Uncertainty Quantification**  
NUTS