

# 000 001 002 003 LOCALITY-ATTENDING VISION TRANSFORMER 004 005 006 007

008 **Anonymous authors**  
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## ABSTRACT

026 Vision transformers have demonstrated remarkable success in classification by  
 027 leveraging global self-attention to capture long-range dependencies. However,  
 028 this same mechanism can obscure fine-grained spatial details crucial for tasks  
 029 such as segmentation. In this work, we seek to enhance the segmentation per-  
 030 formance of vision transformers after being trained using the usual image-level  
 031 classification objective. More specifically, we present a simple yet effective add-  
 032 on for vision transformers that improve their performance on segmentation tasks  
 033 while retaining their image-level recognition capabilities. In our approach, we  
 034 modulate the self-attention with a learnable Gaussian kernel that biases the at-  
 035 tention toward neighboring patches. We further refine the patch representations  
 036 to learn better embeddings at patch positions. These modifications ensure mean-  
 037 ingful representations at spatial positions and encourage tokens to focus on lo-  
 038 cal surroundings, while still preserving the model’s ability to incorporate global  
 039 information. Experiments demonstrate the effectiveness of our modifications,  
 040 evidenced by substantial segmentation gains on three benchmarks (*e.g.*, over  
 041 6% and 4% on ADE20K for ViT Tiny and Base), without changing the train-  
 042 ing regime or sacrificing classification performance. The code is available at  
 043 <https://anonymous.4open.science/r/LocAtViTRepo/>.  
 044

## 1 INTRODUCTION

045 Vision transformers (ViT, Dosovitskiy et al., 2021) have emerged as powerful visual backbones by  
 046 modeling images as sequences of patch tokens, processed with self-attention. Unlike convolutional  
 047 neural networks (CNN, LeCun et al., 2015), which aggregate local information in a restricted recep-  
 048 tive field, ViTs can capture long-range dependencies at any layer. This global attention mechanism  
 049 has proven highly effective for image classification, enabling ViT models to surpass CNN perfor-  
 050 mance when sufficient data is available (Touvron et al., 2021a). A key factor behind this success is  
 051 the ability to integrate global context that leads to more uniform and holistic representations across  
 052 layers, which enhances the recognition of high-level image semantics (Raghu et al., 2021).

053 The same global focus that makes ViTs excel in classification, however, poses challenges for dense  
 054 prediction tasks such as semantic segmentation. These tasks require precise localization and fine-  
 055 grained spatial detail, properties that convolutional inductive biases naturally encourage but vanilla  
 056 ViTs lack (Hassani et al., 2023). As a result, the design of spatial attention and feature hierarchy  
 057 has been found critical for adapting transformers to dense tasks (Wang et al., 2021; Liu et al., 2021).  
 058 Still, a tension remains between capturing global context and preserving local detail. Global atten-  
 059 tion can dilute local cues, whereas purely local schemes may miss long-range dependencies needed  
 060 for holistic understanding. Besides, the classification objective used by models often neglects the  
 061 necessities of dense prediction, motivating a need for a “segmentation-in-mind” pretraining. **Empirically,**  
 062 **we show in Appendix G that, in a ViT trained for classification, patch tokens progressively**  
 063 **lose distinct local structure and become increasingly aligned with the [CLS] token.**

064 More recently, foundation models trained at large-scale (Radford et al., 2021; Oquab et al., 2023),  
 065 which learn versatile visual representations, have seen broad adoption in a breadth of visual tasks.  
 066 Despite the availability of more intricate designs, these models still mostly adopt vanilla ViT due to  
 067 its simplicity and ease of integration. This widespread reliance underscores the practical value of  
 068 enhancing ViT’s capabilities rather than pursuing more complex new designs. A prominent example  
 069 is CLIP (Radford et al., 2021), which couples a ViT-based image encoder with a text encoder to align  
 070 image-text representations, enabling zero-shot classification and open-vocabulary recognition. Such

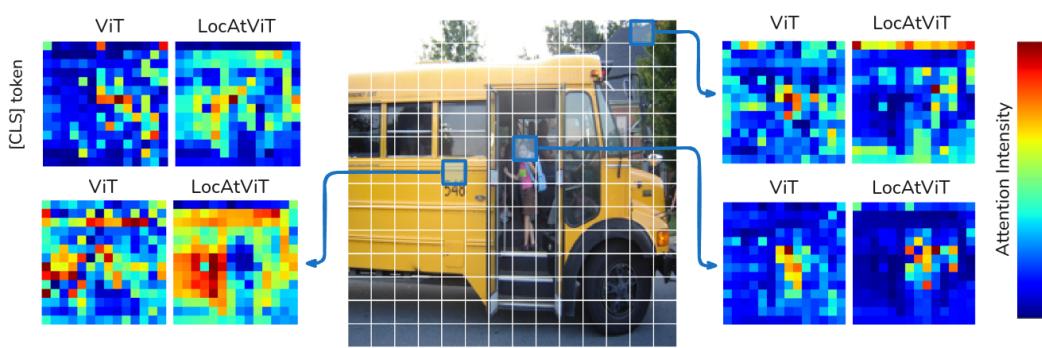


Figure 1: **Qualitative evaluation on the attention maps.** The final attention map of ViT and LocAtViT for the [CLS] token and three patches are illustrated for an image with label *school bus*.

representations can be repurposed for dense predictions, for instance, by comparing local features to text prompts, but this adaptation is non-trivial. Furthermore, recent studies try to harness CLIP’s knowledge for segmentation without any task-specific training (Zhou et al., 2022; Wang et al., 2024; Hajimiri et al., 2025). However, as CLIP and similar models are not trained for quality local representations, their features often lack the spatial granularity needed for precise dense prediction.

**Contributions.** In this paper, we propose a modular *Locality-Attending* (LocAt) add-on, which incorporates two ideas: (i) We modulate the attention logits with a learnable Gaussian kernel centered on each query token’s location, ensuring that patches closer to the query receive higher attention. This acts as an explicit inductive bias encouraging each token to attend to its local neighborhood while still allowing global interactions. We denote the resulting self-attention module as the *Gaussian-Augmented* (GAug) attention (Sec. 4.1). (ii) We enhance patch representations for segmentation by introducing minor changes prior to the classification head, preserving the meaningfulness of spatial tokens, that are most important for dense prediction. We term this procedure as *Patch Representation Refinement* (PRR) that addresses the gradient flow issue in ViTs for segmentation, which is overlooked in the literature (see Sec. 4.2). Hence, LocAt refers to the combination of GAug and PRR. Figure 2 demonstrates that it improves different baselines, yielding significant segmentation performance gains (arrows pointing upward), while preserving or improving classification accuracy (no arrow pointing to the left). The proposed add-on also enhances the quality of attention maps, as illustrated in Fig. 1. LocAt is a lightweight and objective-agnostic add-on, also compatible with self-supervised pretraining. Importantly, the minimal architectural changes required to integrate LocAt make it readily applicable to any ViT with marginal changes, facilitating its usage in foundation models. To the best of our knowledge, we are the first to offer this perspective on ViT pretraining: designing pretraining with downstream dense prediction in mind, while being faithful to vanilla ViT’s training regime and architecture.

## 2 RELATED WORK

**Hierarchical ViT backbones for dense prediction.** While the original ViT targets image classification and produces low-resolution features with weak locality priors (Dosovitskiy et al., 2021), dense prediction has motivated backbones that retain or recover spatial detail across stages. Some works use pyramid and token-merging designs to introduce multi-scale features and lightweight decoders for segmentation (Wang et al., 2021; Xie et al., 2021), while others build parallel branches for local and global processing (Chu et al., 2021). These works show that topology substantially

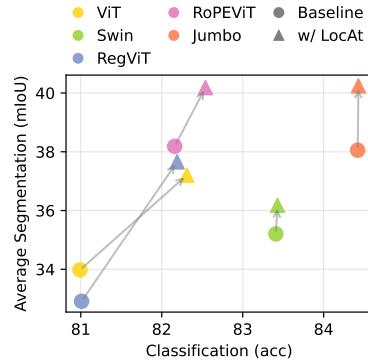


Figure 2: **LocAt considerably enhances different baselines** in segmentation, while preserving or even improving classification.

108 helps dense tasks. However, they typically require non-trivial architectural changes (new stages or  
 109 merging blocks) and may rely on local window attention that limits full-image interaction.  
 110

111 **Convolution-based hybrids.** Another line injects convolutional priors either inside attention or in  
 112 the feed-forward network to encourage local bias while keeping global modeling. Works use con-  
 113 volutional projections (Wu et al., 2021a), add gated positional self-attention to softly bias toward  
 114 convolutional behavior (d’Ascoli et al., 2021), couple local convolutional features with global rep-  
 115 resentations (Peng et al., 2021), or add convolutions in the feed-forward network (Li et al., 2021).  
 116 These hybrid models add extra modules that require tuning, and they can reduce plug-and-play  
 117 compatibility with off-the-shelf ViTs, as they often introduce branches or replace core components.  
 118 Besides, convolution offers a spatially-shared kernel which is independent of patch information.

119 **Locality mechanisms inside attention.** Orthogonal to backbone design, many papers modify the  
 120 attention pattern itself to introduce locality. Many of the works use fixed or structured windows (Liu  
 121 et al., 2021; Dong et al., 2021; Yang et al., 2021). Other ideas include utilizing sliding or dilated  
 122 neighborhoods to expand receptive fields efficiently (Hassani et al., 2023; Hassani & Shi, 2023),  
 123 sampling content-relevant keys (Xia et al., 2023), selecting regions using dynamic sparse rout-  
 124 ing (Zhu et al., 2023), or using explicit global-local mixers to balance context with locality (Ding  
 125 et al., 2022; Tu et al., 2022; Chen et al., 2022; Hatamizadeh et al., 2023). Most of these approaches  
 126 restrict or mask interactions (using windows or patterns) or add mixing subsystems that complicate  
 127 design, impeding their widespread adoption.

128 **Positional encodings that strengthen locality.** Beyond absolute embeddings, relative positional  
 129 encoding (RPE), and rotary positional encodings (RoPE) improve spatial awareness in ViTs (Shaw  
 130 et al., 2018; Liu et al., 2021; Wu et al., 2021b; Su et al., 2021; Heo et al., 2024). These approaches  
 131 are orthogonal to attention locality, and we briefly mentioned them to emphasize that they encode  
 132 locality as well. Our work complements rather than replaces them, as we show in the experiments.  
 133

134 **Improving token representation.** Recent work on *register tokens* augments ViTs with dedicated  
 135 auxiliary tokens that absorb non-informative computation and yield smoother feature maps helpful  
 136 for dense prediction (Dariset et al., 2024). Unlike this approach, we do not require auxiliary tokens,  
 137 and we also address the issue of gradient flow to spatial patch outputs, overlooked in the prior work.  
 138 [CaiT \(Touvron et al., 2021b\) introduces class-attention layers that specialize the last blocks to re-](#)  
 139 [fining only the class token, while keeping patch tokens fixed in those layers, leading to suboptimal](#)  
 140 [dense prediction performance. Token-labeling methods \(Jiang et al., 2021\) require a modified train-](#)  
 141 [ing regime and assign patch-level pseudo-labels from an external teacher. Finally, pooling heads](#)  
 142 [such as global average pooling \(GAP\) and multihead attention pooling \(MAP\) \(Zhai et al., 2022\)](#)  
 143 [aim to produce a stronger pooled representation for classification by aggregating patch tokens, while](#)  
 144 [our work is explicitly designed for segmentation-in-mind training with an emphasis on improving](#)  
 145 [the spatial token representations themselves rather than only the pooled vector.](#)

146 **Foundation models for dense prediction.** Large pre-trained foundation models, such as  
 147 CLIP (Radford et al., 2021), demonstrate impressive zero-shot generalization on image-level recog-  
 148 nition by leveraging ViT backbones. The preference for the standard ViT backbone can be attributed  
 149 to its strong global attention, predictable scaling behavior with data and model size, and a uniform  
 150 architecture that avoids the need for complex stage-wise tuning as the model grows (Zhai et al.,  
 151 2022; Alabdulmohsin et al., 2023). However, despite excelling on image-level benchmarks, such  
 152 models remain less effective for dense prediction because their representations are predominantly  
 153 global and task-agnostic (Shao et al., 2024). As a result, additional adaptation or decoding layers  
 154 are usually required to repurpose them for segmentation or detection (Li et al., 2022; Xu et al.,  
 155 2023; Luo et al., 2023). While these adaptations yield improvements, they do not fully address  
 156 the core issue: foundation-model ViTs—trained with classification objectives—tend to emphasize  
 157 global semantics over local detail (Liang et al., 2023).

158 A ViT backbone that natively preserves both local detail and global context could enable foundation  
 159 models to excel at dense prediction without extra adaptation layers or specialized fine-tuning. In  
 160 this work, we take a step in that direction by refining the ViT backbone itself. Our approach aims to  
 161 potentially bridge the gap between the powerful image-level understanding and the requirements of  
 pixel-level prediction tasks.

Mechanism family	Intact backbone	Locality type	Easily applied on ViT	Query adaptive
<b>Conv-based hybrids</b>	✗	Fixed spatial kernels, shared across patches.	✗	✗
<b>Local window/block attention</b>	✗	Hard locality within windows, limited cross-window links.	✗	Partial
<b>Positional encodings</b>	✓	Implicit spatial bias, no explicit distance decay.	✓	✗
<b>Gaussian-Augmented (ours)</b>	✓	Soft, continuous decay over patch distances.	✓	✓

Table 1: **Qualitative comparison of locality mechanisms in ViT architectures.** Further details are provided in Appendix E.

### 3 PRELIMINARIES

Each ViT layer  $l$  takes a sequence of tokens  $\mathbf{x}^{(l-1)} \in \mathbb{R}^{(1+hw) \times C}$  as input, containing a [CLS] token and  $hw$  spatial patch tokens. Each token is a  $C$ -dimensional vector, and  $h$  and  $w$  denote the number of patches in each column and row.  $\mathbf{x}^{(0)}$  is the partitioned and flattened input after adding the positional embeddings. At each layer  $l$ , the following operations are applied, where LN, attn, and MLP denote layer normalization, self-attention, and feed-forward network, respectively:

$$\mathbf{x}' = \mathbf{x}^{(l-1)} + \text{attn}\left(\text{LN}(\mathbf{x}^{(l-1)})\right), \quad (1)$$

$$\mathbf{x}^{(l)} = \mathbf{x}' + \text{MLP}\left(\text{LN}(\mathbf{x}')\right). \quad (2)$$

Each self-attention module (attn) consists of two sets of weight matrices:  $\mathbf{W}^{qkv} \in \mathbb{R}^{C \times d \times 3}$  to compute  $d$ -dimensional query, key, and value matrices (*i.e.*,  $\mathbf{q}, \mathbf{k}, \mathbf{v} \in \mathbb{R}^{(1+hw) \times d}$ ) based on the input, and  $\mathbf{W}^o \in \mathbb{R}^{d \times C}$  for the final projection. After obtaining  $\mathbf{q}$ ,  $\mathbf{k}$ , and  $\mathbf{v}$ , we calculate:

$$\mathbf{A} = \text{softmax}\left(\mathbf{q}\mathbf{k}^\top / \sqrt{d}\right) \mathbf{v}. \quad (3)$$

Matrix  $\mathbf{A} \in \mathbb{R}^{(1+hw) \times d}$  is then transformed by  $\mathbf{W}^o$  to form the output of the layer. The *attention logits* of a patch  $p$  are represented by the  $p^{\text{th}}$  row of  $\mathbf{q}\mathbf{k}^\top / \sqrt{d}$ . Note that for simplicity, we present the formulation of a single-head self-attention.

### 4 METHOD

We now present **LocAtViT**, which enhances ViT with two modular components, GAug attention (Sec. 4.1) and PRR (Sec. 4.2), and is trained with the same classification objective as ViT.

#### 4.1 GAUSSIAN-AUGMENTED ATTENTION

We aim to introduce explicit local attention into layers of vision transformer (for all tokens but [CLS]) via adding a patch-specific Gaussian kernel to attention logits. We first discuss the altered self-attention formulation, followed by details on computation of the kernel, and then the final form of the attention. Table 1 compares our approach to multiple related work categories, and motivates our choice of a Gaussian kernel as a simple, query-adaptive locality bias that can be added on top of vanilla self-attention without modifying the ViT architecture or training objective.

**Modified self-attention.** At every layer’s self-attention, we add a *supplement* matrix  $\mathbf{S}$  to the attention logits, aiming to emphasize the attention of each patch to its surrounding. With this addition, the self-attention formulation of Eq. (3) is modified as follows, which is also depicted in Fig. 3a:

$$\mathbf{A} = \text{softmax}\left(\frac{\mathbf{q}\mathbf{k}^\top}{\sqrt{d}} + \mathbf{S}\right) \mathbf{v}. \quad (4)$$

We construct  $\mathbf{S}$  so that a patch  $p$  attends more to its immediate surroundings, with increment gradually decreasing with distance from  $p$ . A natural choice for such a distance-based locality prior is an unnormalized Gaussian centered at  $p$ . A Gaussian kernel provides a smooth, monotone decay of influence with distance, controlled by a variance parameter  $\sigma^2$  (in the isotropic case). This gives an interpretable handle on the effective receptive field: small  $\sigma$  yields a sharp, highly local focus, whereas large  $\sigma$  approaches a nearly uniform weighting over patches (more information in Appendix F). We parameterize the variance of the Gaussian kernel for each patch by a 2D vector, stored in the  $p^{\text{th}}$  row of  $\Sigma \in \mathbb{R}_+^{hw \times 2}$ , controlling the attention span along both axes for each patch. Since patches might have different needs in how far they should attend to their neighbors, we compute the variances based on the query matrix derived from the input, using a learnable weight matrix  $\mathbf{W}^\sigma \in \mathbb{R}^{d \times 2}$  (with  $f$  being a scaled sigmoid function ensuring positive, bounded values):

$$\Sigma = f(\mathbf{q}\mathbf{W}^\sigma), \quad (5)$$

**Gaussian kernel.** For a patch grid of size  $h \times w$ , we denote the set of coordinate vectors:

$$\mathbf{P} = [i \quad j]_{i \in \{1, 2, \dots, h\}, j \in \{1, 2, \dots, w\}}, \quad (6)$$

in an  $hw \times 2$  matrix. The  $hw \times hw \times 2$  pairwise squared difference  $\mathbf{D}$  is computed as:

$$\mathbf{D}_{ptm} = (\mathbf{P}_{pm} - \mathbf{P}_{tm})^2, \quad \text{for } m \in \{1, 2\}, \quad (7)$$

where  $p$  and  $t$  denote indices of source and target patch, and  $m$  indexes the coordinate dimensions. Given  $\Sigma$ , the elements in the Gaussian kernel matrix  $\mathbf{G} \in \mathbb{R}_+^{(hw+1) \times (hw+1)}$  are calculated as:

$$\mathbf{G}_{pt} = \exp\left(-\frac{1}{2} \sum_{m=1}^2 \frac{\mathbf{D}_{ptm}}{\Sigma_{pm}}\right), \quad (8)$$

which determines the addition to attention logits from patch  $p$  to  $t$ . We construct the Gaussian kernel only over spatial tokens. Since [CLS] has no spatial coordinates, entries involving [CLS] are zero and only the patch-patch attention logits are augmented. By pre-computing  $\mathbf{D}$ , i.e., the numerator, we can efficiently compute  $\mathbf{G}$  during training.

**Supplement matrix.** Based on Eq. (8), each entry in  $\mathbf{G}$  lies in  $[0, 1]$ . Directly setting  $\mathbf{S} = \mathbf{G}$  in Eq. (4) causes a scale mismatch between  $\mathbf{S}$  and the attention logits. To mitigate this discrepancy, we assume a learnable weight matrix  $\mathbf{W}^\alpha \in \mathbb{R}^{d \times 1}$  that computes the desired scaling for each patch, based on its  $\mathbf{q}$  vector. Entries in  $\alpha$  scale rows of the Gaussian kernel, more specifically:

$$\alpha = \text{softplus}(\mathbf{q}\mathbf{W}^\alpha) \in \mathbb{R}_+^{hw}, \quad (9)$$

$$\mathbf{S} = \text{diag}(\alpha) \mathbf{G}, \quad (10)$$

in which softplus ensures positive coefficients. Intuitively,  $\alpha$  acts as a per-query, row-wise balancing factor between the original attention logits and the Gaussian locality prior. For tokens where the network predicts small values of  $\alpha$ , the contribution of  $\mathbf{S}$  is negligible and the behavior approaches standard global self-attention (weak locality), whereas larger values of  $\alpha$  yield a stronger local bias. This makes our approach a soft, data-dependent locality mechanism rather than a hard constraint. We empirically analyze the effect of this scaling, as well as parameter-free alternatives, in Appendix D.3 and D.4. We refer to our modified self-attention as *Gaussian-Augmented* (GAug) attention. Figure 3b illustrates the generation process of the supplement matrix.

## 4.2 PATCH REPRESENTATION REFINEMENT

**Problem statement.** In a classification task using ViT, only the [CLS] token’s output of the model is used for computing the loss. While effective for classification, this approach has fundamental limitations for dense prediction from a gradient flow perspective. More concretely, the patch positions’ outputs receive no *direct* supervision, i.e., it is not important to the model what ViT’s final outputs are at those positions. However, these output representations are crucial for further dense prediction. This is problematic because the fine-grained spatial information carried by individual patch tokens is not effectively learned at the final layer.

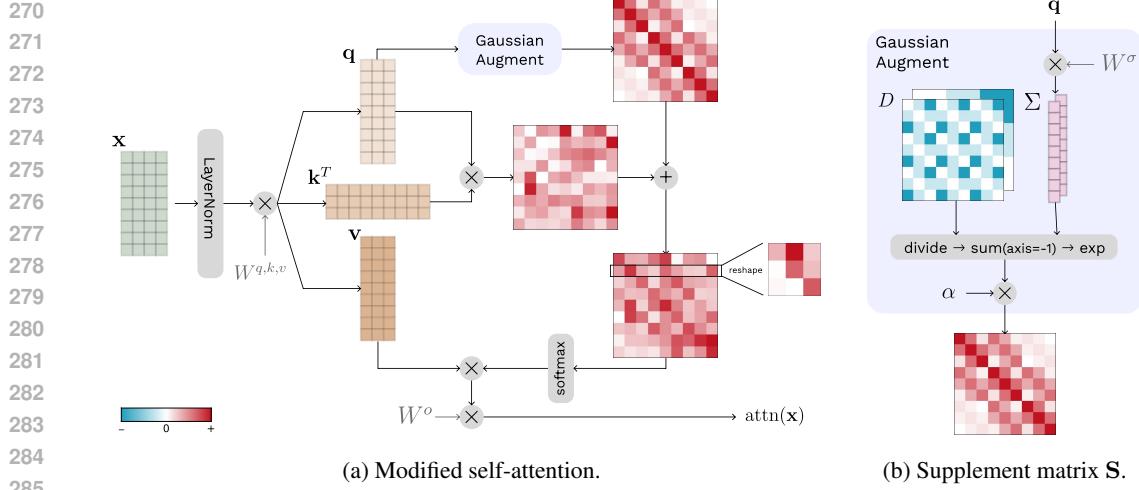


Figure 3: **Illustration of the Gaussian-Augmented attention** for a  $3 \times 3$  grid. For simplicity, the [CLS] token is not shown. (a) The Gaussian addition, i.e.,  $S$  in Eq. (4), is obtained based on  $q$  and is added to the attention logits. The  $p$ -th row in the attention logits matrix presents the attention of patch  $p$  to all patch tokens. The reshaped matrix illustrates that with the GAug add-on, both local and global attentions are integrated. (b) The supplement matrix  $S$  encourages attending to the locality and is computed using the pairwise squared difference tensor  $D$  from Eq. (7). For simplicity, we fix the Gaussian variances and scaling coefficients to one for all patches in this visualization.

Some subsequent methods, such as Swin (Liu et al., 2021), remove the [CLS] token and use global average pooling (GAP) before the classification head. However, this forces an undesirable behavior from a dense prediction standpoint, i.e., a *uniform gradient flow* across all positions. For example, in an image of a bird with other objects in the background, GAP compels the model to match all patch representations—including background regions—with the classifier’s prototype of bird. The uniform gradient flow means that all patch tokens receive equal importance, regardless of their relevance, potentially leading to representations particularly suboptimal for tasks like segmentation. Moreover, GAP has been shown to reduce localization in higher layers (Raghu et al., 2021).

**Proposed solution.** To encourage meaningful patch representations at the final layer’s output,  $x^{(l)}$ , we propose the following operation before the classification head:

$$x^+ = \text{softmax} \left( \frac{x^{(l)} x^{(l)\top}}{\sqrt{d}} \right) x^{(l)}, \quad (11)$$

which acts like a *parameter-free* self-attention. This operation, which introduces no new parameter, aggregates information from all patch positions in a non-uniform manner, thereby preserving their unique contributions and ensuring diverse gradient flow across patch locations. The resulting representation at the [CLS] token,  $x_0^+$ , is then passed to the classification head. We refer to this strategy as *Patch Representation Refinement* (PRR). PRR can be seen as an alternative to GAP, suitable for segmentation-in-mind pretraining.

Our components share the common objective of making ViT representations more suitable for dense prediction, and they act at different stages. GAug operates inside the backbone, modifying self-attention to bias information exchange toward local neighborhoods so that patch tokens can better encode fine spatial details. PRR, in contrast, acts right before the classification head and changes how tokens are aggregated to explicitly route supervision and gradients to patch outputs. In practice, each module can be attached independently to a ViT backbone (see ablations in Sec. 5.4). However, they are coupled through the gradient path: with standard [CLS] classification, adding GAug in the last block has little effect, because its parameters receive no gradient from the loss, whereas PRR routes gradients to those GAug parameters so they can be effectively learned.

324    **5 EXPERIMENTS**  
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326    **5.1 EXPERIMENTAL SETUP**  
 327

328    **Datasets.** For the main experiments, where we assess both classification and segmentation performance,  
 329    we first train models on ImageNet-1K (Deng et al., 2009; Russakovsky et al., 2015),  
 330    which contains 1.28M training images from 1,000 classes. Then, we further utilize these models  
 331    for training on segmentation datasets: ADE20K (Zhou et al., 2019), PASCAL Context (Mottaghi  
 332    et al., 2014), and COCO Stuff (Caesar et al., 2018; Lin et al., 2014), which contain 150, 59, and 171  
 333    semantic categories, respectively. ADE20K and COCO Stuff images are resized to  $512 \times 512$  and  
 334    PASCAL Context images to  $480 \times 480$ . Furthermore, we also assess classification performance on  
 335    smaller scale datasets: CIFAR-100 (Krizhevsky & Hinton, 2009) and mini-ImageNet (Vinyals et al.,  
 336    2016), a subset of ImageNet-1K, consisting of 100 classes with 500 training and 100 validation  
 337    examples each. In all classification experiments, images are resized to  $224 \times 224$ .  
 338

339    **Implementation details.** Our method is implemented using the PyTorch Image Models  
 340    (`timm`) (Wightman, 2019) library. We train models on ImageNet-1K for 300 epochs, with initial  
 341    learning rate (LR) 0.001, and on CIFAR-100 and mini-ImageNet for 600 epochs, with LR 0.0005.  
 342    Global batch size is set to 1024, linear warm-up to 20 epochs, and we use AdamW (Kingma & Ba,  
 343    2014; Loshchilov & Hutter, 2019) optimizer with a weight decay of 0.05. As in Ding et al. (2022), a  
 344    simple triangular learning rate scheduler (Smith & Topin, 2018) is applied, and the stochastic depth  
 345    drop rates (Huang et al., 2016) for the Tiny, Small, and Base backbones are set to 0.1, 0.2, and  
 346    0.4, respectively. We follow Liu et al. (2021) for data augmentation and use RandAugment (Cubuk  
 347    et al., 2020), Mixup (Zhang et al., 2018), Cutmix (Yun et al., 2019), and random erasing (Zhong  
 348    et al., 2020). The sigmoid function  $f$  in Eq. (5) is scaled to have a maximum of  $\max(h, w)$ , and  
 shifted to satisfy  $f(0) = 1$ .

349    For semantic segmentation, we utilize the MMSegmentation toolbox (OpenMMLab, 2020) and em-  
 350    ploy a simple 1-layer MLP on top of the frozen classification-trained models. This configuration en-  
 351    sures that segmentation performance mainly reflects the discriminative power of the classifica-  
 352    tion-trained backbone in dense prediction. This setup aligns with our goal of isolating and assessing  
 353    patch representation quality under a low-tuning regime ([more information in Appendix J](#)). Training  
 354    on segmentation datasets is performed over 20K iterations with a batch size of 32.

355    **5.2 MAIN RESULTS**  
 356

357    **Segmentation performance.** The LocAt add-on can be applied on several ViT-based models, and  
 358    Tab. 2 evaluates its effect, in terms of classification performance on ImageNet-1K, as well as seg-  
 359    mentation performance on three benchmarks, when applied to five models: ViT (Dosovitskiy et al.,  
 360    2021), Swin Transformer (Liu et al., 2021), ViTs with registers (denoted as RegViT, we use 4 regis-  
 361    ter, Darct et al., 2024), Rotary Position Embedding for ViTs (denoted as RoPEViT, Heo et al.,  
 362    2024), and the recent Jumbo (Fuller et al., 2025). Comparing each baseline with its enhanced  
 363    counterpart (gray row below), proves LocAt’s addition is useful in improving the segmentation  
 364    performance of all. For instance, LocAtViT Tiny achieves a substantial improvement of **+6.17%**,  
 365    **+4.86%**, and **+5.86%**, over ViT on ADE20K, PASCAL Context, and COCO Stuff, respectively.  
 366    Importantly, LocAt-enhanced models’ superior segmentation performance is achieved without com-  
 367    promising classification performance; in fact, they deliver comparable or even improved accuracy  
 368    across different models (*e.g.*, LocAtViT outperforms ViT by **+1.55%** in Tiny backbone).

369    LocAt improves baselines that are architecturally close to ViT significantly, *e.g.*, RoPEViT, and  
 370    interestingly, it brings improvements over Swin as well. We believe this is not trivial as the add-  
 371    on was designed for ViT’s architecture, in which there exists a [CLS] token and the attention  
 372    width is not limited, while in Swin the windowed attention mechanism severely affects the extent to  
 373    which LocAt can play a role. Furthermore, our add-on incurs a negligible increase in computational  
 374    efficiency in terms of number of FLOPs over the corresponding counterparts (measured at  $224 \times 224$   
 375    using Sovrasov, 2018-2024). Additional experiments are presented in Appendix B.

376    **Classification performance.** In addition to the ImageNet-1K classification results in Tab. 2, Tab. 3  
 377    investigates LocAt’s classification effectiveness on small-scale datasets: mini-ImageNet (Vinyals

Table 2: **Segmentation performance** of models and their counterparts with our LocAt extension (in gray), along with their **classification performance** on ImageNet-1K, which the models are initially trained on. Results demonstrate that (i) LocAt substantially boosts segmentation performance (*our primary focus*), while preserving or even improving the classification performance, and (ii) this effect holds for a variety of methods, for different backbone sizes. Furthermore, (iii) the segmentation gains appear not only in weaker baselines, but also in strong, high-performing models, where classification improvements are harder to achieve.

	Method	Segmentation mIoU (%)			Top-1 (%) ImageNet	#Params (M)	FLOPs (G)
		ADE	P-Context	C-Stuff			
Tiny	ViT	17.30	33.71	20.29	72.39	6	1.26
	+ LocAt	23.47 <sub>+6.17</sub>	38.57 <sub>+4.86</sub>	26.15 <sub>+5.86</sub>	73.94 <sub>+1.55</sub>	6	1.27
	Swin	25.58	36.78	28.34	81.18	28	4.50
	+ LocAt	26.52 <sub>+0.94</sub>	37.65 <sub>+0.87</sub>	29.09 <sub>+0.75</sub>	81.43 <sub>+0.25</sub>	28	4.51
	RegViT	15.98	33.45	19.58	72.90	6	1.29
	+ LocAt	24.39 <sub>+8.41</sub>	39.90 <sub>+6.45</sub>	27.38 <sub>+7.80</sub>	74.08 <sub>+1.18</sub>	6	1.30
	RoPEViT	19.17	38.16	22.75	73.60	6	1.26
	+ LocAt	24.48 <sub>+5.31</sub>	40.79 <sub>+2.63</sub>	27.98 <sub>+5.23</sub>	74.34 <sub>+0.74</sub>	6	1.27
	Jumbo	20.33	36.36	22.13	78.71	9	1.40
	+ LocAt	21.62 <sub>+1.29</sub>	37.22 <sub>+0.86</sub>	23.87 <sub>+1.74</sub>	78.78 <sub>+0.07</sub>	9	1.42
Base	ViT	28.40	43.10	30.43	80.99	86	17.58
	+ LocAt	32.64 <sub>+4.24</sub>	45.35 <sub>+2.25</sub>	33.62 <sub>+3.19</sub>	82.31 <sub>+1.32</sub>	86	17.64
	Swin	31.90	40.11	33.60	83.41	88	15.46
	+ LocAt	32.89 <sub>+0.99</sub>	41.44 <sub>+1.33</sub>	34.20 <sub>+0.60</sub>	83.43 <sub>+0.02</sub>	88	15.47
	RegViT	27.93	41.81	28.99	81.01	86	17.95
	+ LocAt	32.71 <sub>+4.78</sub>	46.14 <sub>+4.33</sub>	34.12 <sub>+5.13</sub>	82.19 <sub>+1.18</sub>	86	18.02
	RoPEViT	31.38	48.83	34.35	82.16	86	17.58
	+ LocAt	34.94 <sub>+3.56</sub>	49.24 <sub>+0.41</sub>	36.37 <sub>+2.02</sub>	82.54 <sub>+0.38</sub>	86	17.64
	Jumbo	32.20	47.31	34.65	84.42	130	19.74
	+ LocAt	35.69 <sub>+3.49</sub>	49.20 <sub>+1.89</sub>	35.84 <sub>+1.19</sub>	84.43 <sub>+0.01</sub>	130	19.81

Table 3: **Classification top-1 accuracy** of ViT and LocAtViT for different backbone sizes, on mini-ImageNet and CIFAR-100, showcasing LocAt’s effectiveness on small-scale datasets.

Size	mini-ImageNet		CIFAR-100	
	ViT	LocAtViT	ViT	LocAtViT
Tiny	74.94	78.47 <sub>+3.53</sub>	73.84	80.43 <sub>+6.59</sub>
Small	78.98	84.30 <sub>+5.32</sub>	76.33	81.13 <sub>+4.80</sub>
Base	79.91	84.86 <sub>+4.95</sub>	76.90	82.20 <sub>+5.30</sub>

Table 4: **Self-supervised performance of LocAtViT used in DINO**, showcasing LocAt’s effectiveness in the self-supervised regime.

Experiment	ViT-S/16	LocAtViT-S/16
Linear classification	65.52	67.65 <sub>+2.13</sub>
10-NN	61.69	63.96 <sub>+2.27</sub>
Nearest 20-NN	61.53	63.74 <sub>+2.21</sub>
neighbor 100-NN	59.30	61.19 <sub>+1.89</sub>
200-NN	57.90	59.78 <sub>+1.88</sub>

et al., 2016) and CIFAR-100 (Krizhevsky & Hinton, 2009). Although designed to enhance segmentation, these results demonstrate LocAt’s classification effectiveness even when trained on small-scale datasets. LocAt improves ViT’s performance by 3-6% on mini-ImageNet and 4-7% on CIFAR-100, while only introducing 2,340 new parameters (0.003% increase for Base). Please note that segmentation results are not included for models trained on these datasets since, due to their scale and number of classes, representations are not expected to generalize well to segmentation benchmarks.

**Foundation models.** In the previous sections, we described our interest in improving ViT’s segmentation capabilities without changing their training scheme. Our experiments support that our minor modifications lead to better dense prediction performance, while performing on par or superior to the vanilla models in classification. One reason for our interest in the mentioned problem is that ViTs have been widely used across computer vision foundation models and are the go-to choice for many of the recent methods (Radford et al., 2021; Kirillov et al., 2023; Caron et al., 2021; Oquab et al., 2023). One of the popular models that yields versatile image representations and transfers well to different computer vision tasks is DINO (Caron et al., 2021), which is trained in a self-supervised

Table 5: **Hummingbird dense NN retrieval (mIoU %)** on PASCAL VOC and ADE20K.

Method	Tiny				Base			
	PASCAL		ADE20K		PASCAL		ADE20K	
	Vanilla	+ LocAt						
ViT	39.2	<b>50.3</b>	12.0	<b>15.2</b>	55.8	<b>58.7</b>	19.5	<b>21.5</b>
Swin	45.2	<b>45.3</b>	16.1	<b>16.3</b>	57.6	<b>62.8</b>	23.3	<b>24.6</b>
RegViT	39.4	<b>52.3</b>	12.5	<b>15.9</b>	55.5	<b>60.3</b>	19.4	<b>22.8</b>
RoPEViT	50.7	<b>54.7</b>	16.0	<b>17.5</b>	61.0	<b>61.4</b>	22.4	<b>23.7</b>
Jumbo	40.0	<b>45.5</b>	13.3	<b>14.5</b>	58.5	<b>63.8</b>	21.6	<b>23.7</b>

manner and can serve as a general-purpose backbone. Two of the main evaluation protocols used by Caron et al. (2021) are learning a linear classifier on top of the frozen backbone and nearest neighbor classification ( $k$ -NN) on top of the features.

We train DINO ViT-S/16 and DINO LocAtViT-S/16 on ImageNet-1K for 50 epochs using the setting provided in the official repository, and evaluate them on the mentioned tasks. Table 4 demonstrates that replacing ViT with LocAtViT in DINO actually improves its performance on both linear and  $k$ -NN classification. We report the  $k$ -NN performance on  $k \in \{10, 20, 100, 200\}$  as advised by Caron et al. (2021). These findings reveal our objective-agnostic modifications’ effectiveness in the self-supervised regime and the potential of our method on backbones that learn general-purpose representations. While interesting, further investigation on larger foundation models is beyond our computational reach and lies outside the scope of this work.

**Hummingbird evaluation.** To further assess whether LocAt improves quality of image features, we evaluate our models using Hummingbird (Balažević et al., 2023), a protocol proposed for evaluating *in-context scene understanding* in a purely frozen-feature regime. We use the implementation by Pariza et al. (2024) and follow its dense nearest-neighbor (NN) retrieval setup. Table 5 shows that LocAt consistently improves NN retrieval performance relative to the corresponding vanilla backbones on PASCAL VOC (Everingham et al., 2010) and ADE20K, across architectures, suggesting that LocAt enhances spatial representations, even without any task-specific fine-tuning or decoder.

### 5.3 QUALITATIVE ANALYSIS

An interesting implication of our proposed modifications is the refinement of ViT’s patch outputs, which makes it more suitable for use cases on dense prediction tasks. Figure 1 offers a visual comparison of attention maps from a vanilla ViT and our LocAtViT, both trained for classification, for an image labeled as *school bus*. From the [CLS] token’s attention, we observe that ViT’s focus is broadly dispersed, whereas LocAtViT shows more concentrated and coherent activation on key features of the bus. Furthermore, we present the attention maps of three patch tokens to other patches. For instance, a patch on the bus side attends to nearly the entire bus in LocAtViT, whereas ViT’s map is harder to interpret. A patch covering the child’s face generates meaningful attention in both models, but ViT seems to highlight unrelated regions more. Interestingly, for a patch near the top-right corner, LocAtViT not only focuses on some tree patches, but also extends attention to the sky and road, all corresponding to the image background. Despite being trained solely for classification, LocAtViT exhibits an improved ability to detect some scene structures, suggesting that our proposed local interactions can enrich the model’s contextual understanding without sacrificing global attention. Further qualitative examples are presented in Appendix C.

### 5.4 ABLATION STUDY

In this section, we provide an ablation study on the architectural choices we made. We also provide ablation study on the self-attention module’s design in the Appendix D, and we compare PRR to pooling heads and class-attention in Appendix H and I.

**Effect of GAug and PRR.** Part ① of Tab. 6 ablates on GAug and PRR defined in Secs. 4.1 and 4.2. Results demonstrate that both GAug and PRR indeed enhance the performance of the model in both classification and segmentation, and their combination pushes the performance even further.

486  
 487 Table 6: **Ablations on model’s architecture.** We report segmentation performance (mIoU %) over  
 488 three benchmarks and classification accuracy (top-1 %) on ImageNet-1K. PE and GAP stand for  
 489 positional embeddings and global average pooling.

490 Method	Tiny				Base			
	ADE	P-Context	C-Stuff	ImageNet	ADE	P-Context	C-Stuff	ImageNet
492 ViT	17.30	33.71	20.29	72.39	28.40	43.10	30.43	80.99
493 ① ViT + GAug	18.98	34.97	21.51	73.16	30.26	44.36	32.21	82.00
494 ViT + PRR	21.60	37.93	25.85	73.71	29.89	44.03	32.16	82.19
495 LocAtViT	23.47	38.57	26.15	73.94	32.64	45.35	33.62	82.31
496 ② ViT - PE	15.13	31.94	19.35	69.36	24.59	40.18	28.79	79.39
497 LocAtViT - PE	22.69	38.15	26.05	73.10	29.73	44.69	32.17	82.17
498 ③ ViT	17.30	33.71	20.29	72.39	28.40	43.10	30.43	80.99
499 ViT + GAP	19.65	34.94	22.86	72.50	27.99	41.97	29.88	81.84
500 ViT + PRR	21.60	37.93	25.85	73.71	29.89	44.03	32.16	82.19

501  
 502 **Effect of positional embeddings.** Part ② of Tab. 6 evaluates the impact of the default absolute  
 503 positional embeddings (PE) on our proposed LocAt add-on. For both backbone sizes, LocAtViT  
 504 without PE not only outperforms ViT without PE, but also surpasses ViT with PE. This indicates  
 505 that LocAt captures the spatial information embedded into PE and more, with much fewer learnable  
 506 parameters. It is worth noting that our approach is not an alternative to positional encoding and we  
 507 did not intend to propose a new PE method. Therefore, these results are included just to demonstrate  
 508 empirically that LocAt indeed captures the spatial information that the default PE captures, which  
 509 is the agent for capturing locality in vanilla ViT. We have shown in Tab. 2 that LocAt is applicable  
 510 alongside other, newer positional encoding approaches, such as RoPE, as well.

511  
 512 **Comparison between PRR and GAP.** As discussed in Sec. 4.2, PRR addresses patch locations’  
 513 gradient flow issues while overcoming GAP’s limitations in segmentation. Part ③ of Tab. 6 com-  
 514 pares how vanilla ViT performs when equipped with PRR versus GAP. PRR shows superior seg-  
 515 mentation performance and interestingly, it improves classification accuracy more than GAP. Moreover,  
 516 although GAP helps ViT in classification, it hurts the segmentation performance in the Base back-  
 517 bone, which is in line with the discussions in Sec. 4.2 about GAP’s problems in segmentation.

## 520 6 CONCLUSION

521  
 522 **Summary.** We present the *Locality-Attending Vision Transformer*, a modular framework that en-  
 523 hances vision transformers for dense prediction while preserving image-level capabilities and inte-  
 524 grating seamlessly into existing ViTs. This introduces a segmentation-in-mind pretraining perspec-  
 525 tive: by adding *GAug* attention, our method biases self-attention toward local regions to capture  
 526 fine-grained spatial details, while *PRR* ensures meaningful gradient flow to patch tokens, strength-  
 527 ening representations for dense prediction. Extensive experiments across multiple ViT baselines  
 528 show that LocAt delivers superior segmentation performance without compromising classification  
 529 accuracy. Our objective is not to surpass state-of-the-art architectures, but to improve classifica-  
 530 tion-trained ViT backbones for segmentation with a method largely orthogonal to prior advancements,  
 531 motivated by the trend of them being widely used, e.g., by foundation models. Consistent with Heo  
 532 et al. (2024), we therefore emphasize comparisons between baselines and their LocAt-enhanced  
 533 counterparts. We hope that these lightweight modifications will be adopted in ViT-based foundation  
 534 models.

535  
 536 **Limitations.** We evaluated our method on multiple classification and segmentation datasets. How-  
 537 ever, these datasets all only contain natural images, and we have left evaluation on other domains  
 538 such as medical imaging or remote sensing as future work. Furthermore, while we have demon-  
 539 strated the effectiveness of LocAtViT used in a small foundation model, evaluation on large founda-  
 540 tion models, such as CLIP, has been out of our computational reach.

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756  
 757           **LOCALITY-ATTENDING VISION TRANSFORMER**  
 758           **APPENDIX**

760  
 761           **A TECHNICAL DETAILS**

763           **A.1 CODE**

766           Our code is anonymously and publicly available at <https://anonymous.4open.science/r/LocAtViTRepo/>. The README.md file provides guidelines on how to set up the environment, train the models, and perform different evaluations. For ViT (Dosovitskiy et al., 2021), Swin Transformer (Liu et al., 2021), RegViT (Darcel et al., 2024), and RoPEViT (Heo et al., 2024), we used the implementation provided by Wightman (2019), and for Jumbo (Fuller et al., 2025) we used their official repository. All of these models are reproduced. Jumbo is a new work the repository is incomplete, hence, we used the available code and implemented some of the components based on the paper.

774           **A.2 COMPUTE RESOURCES**

776           Our experiments were conducted using NVIDIA RTX A6000 48GB, V100 32GB, and A100 40GB  
 777           GPUs. The Tiny, Small, and Base backbones of LocAtViT require 15GB, 29GB, and 29GB of GPU  
 778           memory with a local batch size of 512, 512, and 256, respectively.

780           **A.3 LLM USAGE**

783           We used LLMs to aid or polish writing. Adhering to ICLR’s author guideline, we include additional  
 784           information here. We used LLMs to generate codes for plotting figures, tables, and other code or  
 785           LaTeX related issues. We also used LLMs to improve the writing, polish, or shorten the paragraphs,  
 786           while double checking the output.

787           **B LOCATViT COMPARISON WITH RELATED WORK**

790           In Tab. 2, we included five baseline methods and implemented LocAt for each. Table 7 compares  
 791           LocAtViT to multiple related works from Sec. 2: CvT-21 (Wu et al., 2021a), Conformer (Peng et al.,  
 792           2021), ConViT (d’Ascoli et al., 2021), Twins (Chu et al., 2023; 2021), DaViT (Ding et al., 2022),  
 793           and GCViT (Hatamizadeh et al., 2023). We utilized the publicly available code and checkpoints,  
 794           and evaluated the models on our segmentation pipeline, as described in Sec. 5. Although LocAtViT  
 795           does not achieve the best classification performance, LocAt helps ViT outperform methods like  
 796           Twins across all three segmentation benchmarks.

797  
 798           **Table 7: Segmentation and classification performance** of the Base backbone of related works and  
 799           the proposed LocAtViT.

Method	Segmentation mIoU (%)			Top-1 (%) ImageNet
	ADE	P-Context	C-Stuff	
CvT-21	21.40	40.91	29.29	82.50
Conformer	22.11	40.03	26.37	83.83
ConViT	23.08	44.82	25.20	82.30
Twins	30.47	44.55	32.27	82.71
DaViT	30.68	44.87	32.38	<b>84.64</b>
GCViT	30.91	44.71	32.77	84.47
LocAtViT	<b>32.64</b>	<b>45.35</b>	<b>33.62</b>	82.31

810  
811    **C ADDITIONAL QUALITATIVE EXPERIMENTS**

812    Figure 4 provides three additional images from the mini-ImageNet dataset, alongside the attention  
813    maps of the [CLS] token and several patches for ViT and LocAtViT.  
814

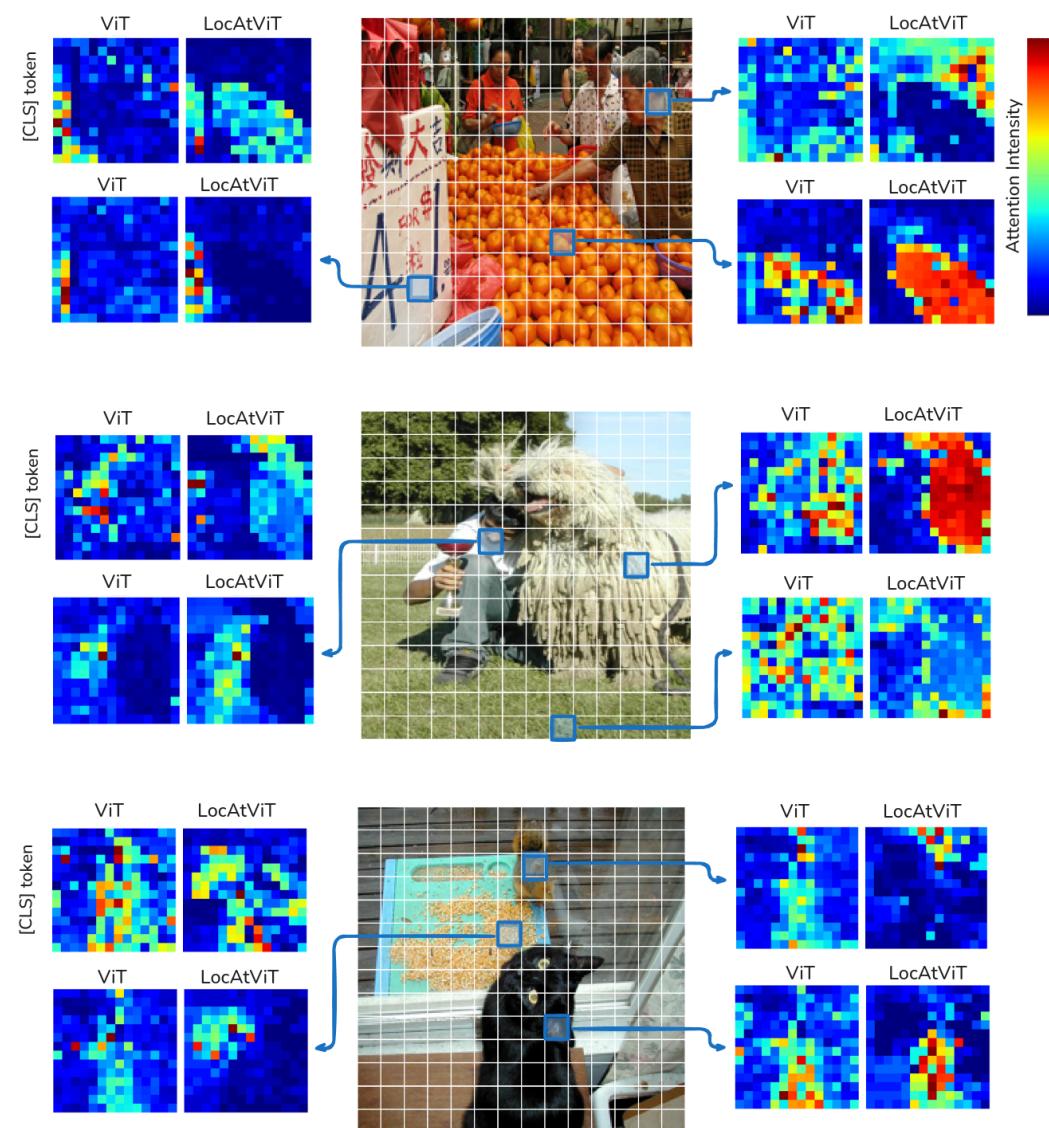


Figure 4: **Qualitative evaluation on the attention maps.** The final attention map of ViT and LocAtViT for the [CLS] token and three different patches are illustrated for three different images from mini-ImageNet with labels: *orange*, *Komondor*, and *corn*.

856    **D ABLATION STUDY ON SELF-ATTENTION**  
857

858    In this section, we perform ablations on the design choices inside the GAug self-attention module.  
859

860    **D.1 GAUSSIAN BASED ON INPUT**  
861

862    In the original ViT, a query vector intuitively determines the information a patch should be looking  
863    for. Since the Gaussian variance controls how far a patch attends to its surroundings, we compute  $\Sigma$   
based on the query matrix in Eq. (5). Table 8 compares this approach to computing  $\Sigma$  based on  $x$ ,

864  
 865   Table 8: **Ablations on GAug attention components.**  $\Delta\#Params$  shows the difference in the number  
 866   of the parameters of each model compared to LocAtViT (first row). Experiments are conducted on  
 867   mini-ImageNet.

	Tiny	Base	$\Delta\#Params$
LocAtViT (Sec. 4)	78.47	84.86	-
Gaussian from $\mathbf{x}$	79.10	85.18	+18,504, +329,868
Isotropic Gaussian	78.71	84.66	-780
Fixed $\sigma = 1$	75.20	82.81	-2,340
width $\sigma = 5$	76.41	82.65	-2,340
$\sigma = 10$	75.53	82.42	-2,340
No scaling	76.26	83.07	-780
Auto $\alpha$	78.48	84.54	-780

878  
 879   the self-attention input. While the latter improves performance, it significantly increases the number  
 880   of parameters.  
 881

## 882   D.2 VARIANCE MATRIX

884   To comply with a more general setting, we assigned separate variances for each image axis. An  
 885   alternative is to use a single variance per patch, forming an isotropic Gaussian kernel. This simplifies  
 886   Eq. (8) to:  
 887

$$888 \quad \mathbf{G}_{pt} = \exp\left(-\frac{\sum_{m=1}^2 \mathbf{D}_{ptm}}{2\sigma_p^2}\right). \quad (12)$$

890   The result of this modification is referred to as *Isotropic Gaussian* in Tab. 8. This table also com-  
 891   pares this approach with another experiment where the Gaussian kernel width is fixed different  
 892   constant values, instead of being patch-specific and query-based. These results indicate that an  
 893   isotropic Gaussian kernel performs comparably, but a fixed kernel width substantially diminishes  
 894   performance, demonstrating the importance of our dynamic input-dependent kernel width.  
 895

## 896   D.3 NO SUPPLEMENT MATRIX SCALING

898   In Sec. 4.1, we introduced a learnable scaling vector  $\alpha$  to match the scale of the supplement matrix  
 899    $\mathbf{S}$  to that of the attention logits. To isolate its effect, Tab. 8 reports a variant (*No  $\alpha$* ) in which the  
 900   supplement matrix in Eq. (10) is not scaled, *i.e.*, we set  $\mathbf{S} = \mathbf{G}$  (equivalently,  $\alpha = 1$ ) and directly  
 901   add the raw Gaussian kernel to the logits. **This no-scaling configuration corresponds to a harder**  
 902   **use of the locality term and consistently reduces accuracy, confirming that unscaled addition of  $\mathbf{G}$**   
 903   **is suboptimal and that the learnable scaling is important for balancing global attention with the**  
 904   **Gaussian prior.**

## 905   D.4 AUTOMATIC SCALING OF THE SUPPLEMENT MATRIX

907   As mentioned, we motivated the need for scaling the supplement matrix before adding it to the  
 908   attention logits in Sec. 4.1. We now propose a parameter-free, input-dependent scheme, *Auto  $\alpha$* ,  
 909   that automatically matches the scale of  $\mathbf{S}$  to that of the original attention logits. Concretely, let  
 910    $N = 1 + hw$ ,  $\mathbf{q}, \mathbf{k} \in \mathbb{R}^{N \times d}$ , and define the row-wise  $\ell_2$ -norm vectors:  
 911

$$912 \quad \mathbf{r} = [\|\mathbf{q}_1\|_2, \dots, \|\mathbf{q}_n\|_2]^\top, \quad (13)$$

$$913 \quad \mathbf{u} = [\|\mathbf{k}_1\|_2, \dots, \|\mathbf{k}_n\|_2]^\top. \quad (14)$$

915   Then the standard attention logits satisfy:

$$917 \quad \frac{\mathbf{q}\mathbf{k}^\top}{\sqrt{d}} = \left(\frac{\mathbf{r}\mathbf{u}^\top}{\sqrt{d}}\right) \circ \cos(\mathbf{q}, \mathbf{k}), \quad (15)$$

918 where  $\circ$  denotes the Hadamard product, and  $\cos(\mathbf{q}, \mathbf{k}) \in \mathbb{R}^{N \times N}$  has entries  $\cos(\mathbf{q}_i, \mathbf{k}_j)$ . Hence, if  
 919 we set

$$\alpha = \frac{\mathbf{r}\mathbf{u}^\top}{\sqrt{d}} \in \mathbb{R}^{N \times N}, \quad (16)$$

922 then the modified logits in Eq. (4) can be rewritten as  
 923

$$\frac{\mathbf{q}\mathbf{k}^\top}{\sqrt{d}} + \mathbf{S} = \alpha \circ (\cos(\mathbf{q}, \mathbf{k}) + \mathbf{G}), \quad (17)$$

926 where both terms inside the parentheses are bounded (in  $[-1, 1]$  and  $[0, 1]$ , respectively), ensuring  
 927 that  $\mathbf{S}$  scales comparably to the original logits.  
 928

929 However, using  $\alpha \circ \mathbf{G}$  would independently scale each entry of  $\mathbf{G}$ , destroying the Gaussian kernel  
 930 structure (each row of  $\mathbf{G}$  is a kernel centered at one patch). To preserve each kernel’s shape, we  
 931 average  $\alpha$  across columns:

$$\bar{\alpha}_i = \frac{1}{N} \sum_{j=1}^N \alpha_{ij}, \quad \bar{\alpha} = [\bar{\alpha}_1, \dots, \bar{\alpha}_n]^\top \in \mathbb{R}^N, \quad (18)$$

935 and then form:

$$\mathbf{S} = \text{diag}(\bar{\alpha}) \mathbf{G}, \quad (19)$$

937 similar to Eq. (10). This row-wise scaling applies a single factor to each Gaussian kernel, preserving  
 938 its shape while matching its magnitude to the attention logits.  
 939

940 Auto  $\alpha$  performs close to learnable  $\alpha$  in the original LocAtViT, with slightly fewer parameters. We  
 941 nevertheless keep the learnable  $\alpha$  in our main model for simplicity of formulation and to give the  
 942 network maximal flexibility in attenuating or amplifying locality where beneficial.  
 943

## E QUALITATIVE COMPARISON OF LOCALITY MECHANISMS IN ViT ARCHITECTURES.

947 In Table 1 we provided a summarized qualitative comparison of locality mechanisms in ViT archi-  
 948 tectures, which highlights the benefits of the proposed method. In this section, we provide further  
 949 details on the following properties considered in the table: **easily applicable on ViT architecture**,  
 950 and **query-adaptive locality**.

951 **Easily applicable on ViT architectures.** *Convolution-based hybrids* are not easily applicable, since  
 952 they require convolutional stems or intermediate convolutional stages that alter the backbone design.  
 953 *Local window or block attention* also needs architectural changes, such as window partitioning and  
 954 shifted windows, which makes them less straightforward to integrate into a standard ViT. *Positional  
 955 encodings*, by contrast, are trivially applicable, as they can be added to the attention mechanism  
 956 without modifying the backbone. Our *Gaussian-Augmented attention* is similarly easy to apply,  
 957 since it simply adds a Gaussian bias term to the attention logits and does not require structural  
 958 changes.

959 **Query-adaptive locality.** *Convolution-based hybrids* do not provide query-adaptive locality, as  
 960 convolutional kernels are fixed after training and shared across spatial positions. *Local window or  
 961 block attention* offers partial adaptivity, where attention weights are content-based, but restricted to  
 962 a fixed window, so queries cannot flexibly extend beyond that boundary. *Positional encodings* are  
 963 not query-adaptive, since they impose a static positional bias that does not depend on the query.  
 964 In contrast, our *Gaussian-Augmented attention* is fully query-adaptive: Gaussian parameters are  
 965 predicted from each query, allowing the locality radius and decay to vary dynamically depending on  
 966 the query content.

## F ABLATION STUDY ON ALTERNATIVE DISTANCE-BASED KERNELS

970 In the main paper we model locality with a Gaussian kernel added to the attention logits (Sec. 4.1).  
 971 The choice of a Gaussian is motivated by the desire for a smooth, distance-based attenuation function  
 972 with a scale parameter that controls the effective receptive field, and that can be predicted from

972  
973  
974  
975  
Table 9: **Effect of different distance-based attenuation kernels.** Segmentation performance  
976 (mIoU %) over three benchmarks and classification accuracy (top-1 %) on ImageNet-1K are re-  
977 ported.  
978  
979  
980  
981

Kernel	Tiny				Base			
	ADE	P-Context	C-Stuff	ImageNet	ADE	P-Context	C-Stuff	ImageNet
No (ViT)	17.30	33.71	20.29	72.39	28.40	43.10	30.43	80.99
Gaussian	23.47	38.57	26.15	73.94	32.64	45.35	33.62	82.31
Inv-dist	22.18	38.16	25.25	74.00	28.42	43.48	30.82	81.94
Laplace	21.67	37.80	25.56	74.01	29.74	44.10	31.95	82.24

982  
983 each query token. Nevertheless, other monotone distance-based kernels are also reasonable, and we  
984 compare with two other kernels in what follows.  
985

986 Let  $r_{pt} = \|P_p - P_t\|_2$  denote the Euclidean distance between patches  $p$  and  $t$  in the spatial grid. We  
987 construct two alternative kernels by predicting scale parameters  $\gamma$  and  $\lambda$  from the queries:

$$988 \quad L_{pt} = \exp(-\gamma_p r_{pt}), \quad (20)$$

989 denoting the Laplace kernel, and the inverse-distance kernel denoted as:  
990

$$991 \quad I_{pt} = \frac{1}{1 + r_{pt}/\lambda_p}. \quad (21)$$

992 In both cases, the resulting kernel matrix replaces  $G$  in Eq. (10), and the rest of the GAug formulation  
993 (including the scaling with  $\alpha$ ) is kept unchanged.  
994

995 Table 9 compares performance of different choices of the kernel. All three locality-augmented  
996 variants improve over the baseline ViT, confirming that introducing a smooth distance-based prior is  
997 beneficial. Among them, the Gaussian kernel delivers the strongest segmentation gains on all three  
998 benchmarks, while remaining competitive in ImageNet-1K accuracy compared to the Laplace and  
999 inverse-distance kernels. This supports the choice of a Gaussian kernel in the main LocAtViT model  
1000 as a simple yet effective way to inject adaptive locality into attention.  
1001

## 1002 G LOCAL FEATURE ANALYSIS ACROSS LAYERS

1003 In the main paper, we argue that the global attention mechanism of vanilla ViT tends to obscure  
1004 fine-grained local information that is important for dense prediction. Here, we provide a quantitative  
1005 analysis of how local patch features evolve across layers in a standard ViT and in our LocAtViT. We  
1006 focus on Base models of ViT and LocAtViT trained on ImageNet-1K and evaluate features on the  
1007 ImageNet-1K validation set.  
1008

1009 **Locality score.** For each layer  $l$  and each spatial patch token, we compute a locality score defined  
1010 as the cosine similarity between that patch and its 8 immediate neighbors in the surrounding  $3 \times 3$   
1011 window. We then average this score over all spatial locations and all validation images. Intuitively,  
1012 a higher locality score indicates that nearby patches share more similar representations, which is  
1013 desirable as long as representations do not collapse globally. Figure 5a reports this locality score  
1014 per layer. After the third layer, LocAtViT consistently achieves a higher locality score than vanilla  
1015 ViT, indicating that its patch features remain more coherent with their spatial neighbors as depth  
1016 increases.  
1017

1018 **Patch- [CLS] similarity.** High neighbor similarity alone does not guarantee that meaningful local  
1019 structure is preserved: if all patch tokens collapse to the same global representation, their mutual  
1020 similarity (including to neighbors) will also be high. To distinguish this degenerate case from  
1021 genuine locality, we additionally measure, for each layer  $l$ , the cosine similarity between every patch  
1022 token and the [CLS] token, again averaged over all patches and validation images. Figure 5b  
1023 shows that in vanilla ViT this patch- [CLS] similarity steadily increases with depth and peaks in  
1024 the final layers, revealing a progressive pull of patch features toward a shared global representation  
1025 dominated by the [CLS] token. In contrast, LocAtViT maintains substantially lower patch- [CLS]  
similarity across layers, while still achieving a higher locality score.  
1026

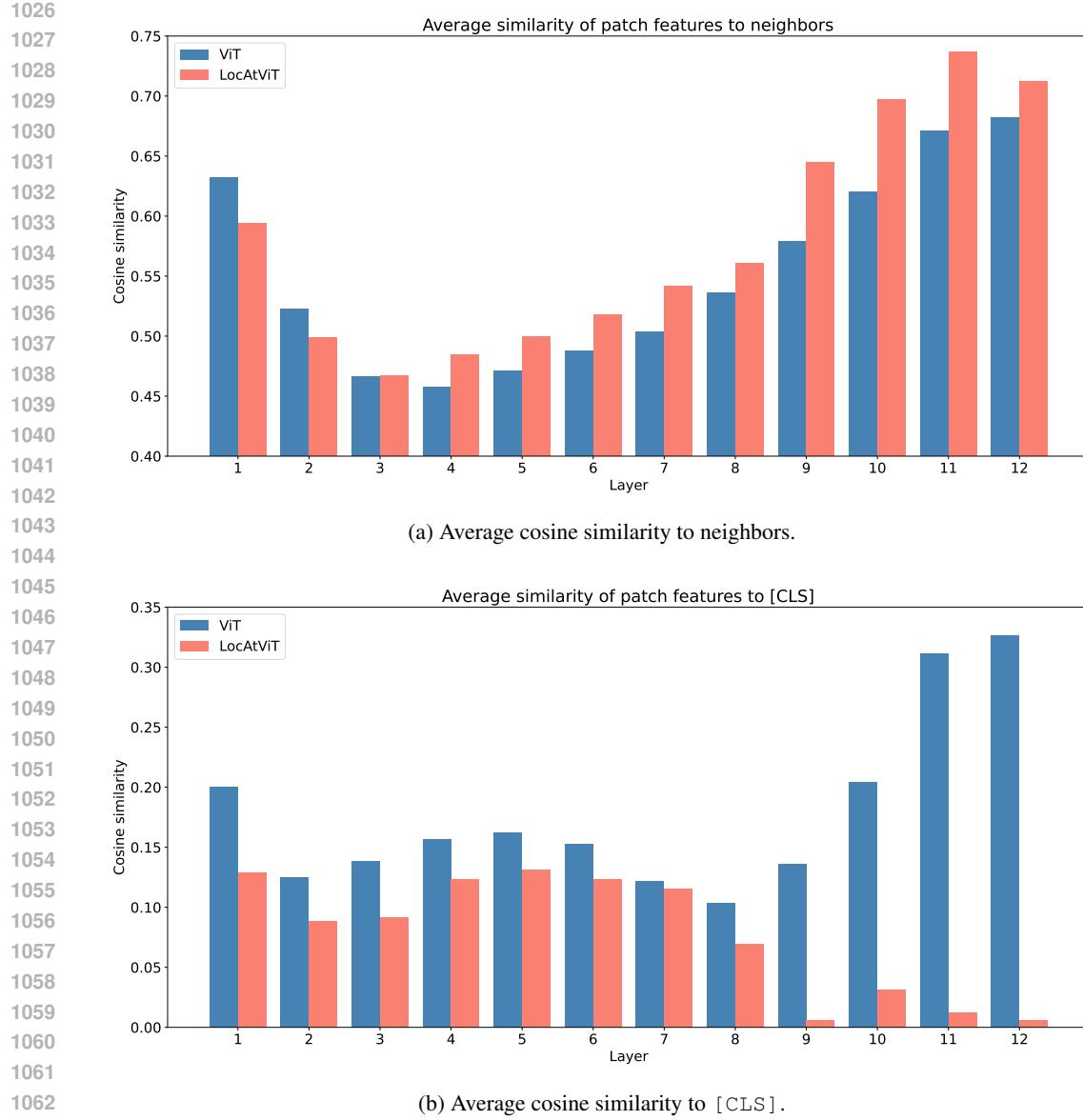


Figure 5: **Degradation of local features in vanilla ViT.** Features in ViT collapse to the global information in the last layers while in LocAtViT, patch features encode local information.

**Discussion.** Taken together, these two measurements show that, in vanilla ViT, patch tokens gradually lose distinct local information and become dominated by global [CLS]-like content as depth grows. LocAtViT, on the other hand, preserves strong locality in patch features without collapsing them onto the [CLS] token. This behavior aligns with our design goal: to enhance the preservation of local structure while retaining the benefits of global attention, thereby producing representations that are better suited for dense prediction.

## H COMPARISON WITH CLASSIFIER-SIDE REFINEMENT METHODS

We compared PRR to GAP in Sec. 5.4. To further isolate the classifier-side refinement, we compare PRR against several standard pooling heads: max pooling, AvgMax (average + max pooling), and multihead attention pooling (MAP). Table 10 reports the performance of these pooling mechanisms with comparable capacity with ViT Tiny backbone size (6M). PRR achieves the best performance

1080 across segmentation and classification among the pooling heads, indicating the effectiveness of ex-  
 1081 plicitly refining patch representations.  
 1082

1083  
 1084 Table 10: **Comparison of PRR with standard pooling heads.** on a Tiny backbone. We report  
 1085 segmentation performance (mIoU %) over three benchmarks and classification accuracy (top-1 %)  
 1086 on ImageNet-1K.

Pooling	ADE	P-Context	C-Stuff	ImageNet
GAP	19.7	34.9	22.9	72.5
Max	19.2	34.7	23.3	71.9
AvgMax	20.1	35.6	24.2	72.3
MAP	20.2	36.3	23.1	73.0
PRR	21.6	37.9	25.9	73.7

## I COMPARISON TO CAIT AND CLASS-ATTENTION

1099 CaiT (Touvron et al., 2021b) introduces dedicated class-attention layers in the last blocks that pro-  
 1100 cess only the class token, while patch tokens remain fixed, and are primarily designed to stabilize  
 1101 optimization and improve classification in very deep transformers. Table 11 compares ViT+PRR  
 1102 Tiny and Base to CaiT backbone of similar size in both classification and segmentation. For a fair  
 1103 comparison, CaiT models are trained with the same data, augmentations, and optimization settings,  
 1104 and we evaluate all models in our segmentation pipeline as described in Sec. 5. In this setting,  
 1105 PRR consistently outperforms CaiT on both ImageNet-1K classification and all three segmentation  
 1106 benchmarks. We attribute this gap to a structural difference in how the final layers are used. In  
 1107 CaiT, the last class-attention blocks exclusively update the class token while keeping patch tokens  
 1108 fixed, so a fraction of the backbone capacity is devoted solely to refining a shallow class embedding.  
 1109 In our ViT+PRR design, all blocks maintain full self-attention among patch and class tokens, and  
 1110 PRR then applies one additional parameter-free self-attention over all tokens. This symmetric use  
 1111 of capacity allows the final layers to refine patch features and the class token jointly, which appears  
 1112 better aligned with the demands of dense prediction while remaining superior in classification.

1113 Table 11: Comparison between PRR and CaiT at similar parameter budgets (*i.e.*, 6M and 86M  
 1114 parameters for Tiny and Base). We report mIoU (%) on three segmentation benchmarks and top-1  
 1115 accuracy (%) on ImageNet-1K.

Method	Tiny				Base			
	ADE	P-Context	C-Stuff	ImageNet	ADE	P-Context	C-Stuff	ImageNet
ViT+PRR	21.6	37.9	25.9	73.7	29.9	44.0	32.2	82.2
CaiT	16.9	30.2	18.7	69.6	27.8	41.9	30.1	79.1

## J FULL FINE-TUNING ON ADE20K

1126 The segmentation results in Tab. 2 use a simple MLP decoder on top of a frozen backbone in order  
 1127 to keep the head lightweight and make performance primarily reflect the backbone representations.  
 1128 We adopt this pipeline deliberately to isolate the effect of the backbone representations: a strong  
 1129 decoder and long full fine-tuning can partially mask differences between pretraining strategies. To  
 1130 check that the gains of LocAt also hold under a standard segmentation protocol, we additionally  
 1131 attach a UperNet (Xiao et al., 2018) decoder to ViT and LocAtViT and fine-tune *all* parameters on  
 1132 ADE20K for 50K iterations. As shown in Tab. 12, LocAt improves mIoU over ViT in both Tiny and  
 1133 Base backbone sizes, confirming that the locality bias introduced by GAug and PRR yields more  
 effective representations even when the entire network is trained end-to-end for segmentation.

1134 Table 12: **End-to-end ADE20K fine-tuning with a standard UpNet decoder.** We report  
 1135 mIoU (%) after fine-tuning all parameters for 50K iterations.  
 1136

	Tiny	Base
ViT	35.7	41.2
ViT + LocAt	<b>36.9</b>	<b>45.2</b>

## K COCO DETECTION AND INSTANCE SEGMENTATION

To further assess the generality of LocAt beyond semantic segmentation, we conduct experiments on COCO 2017 object detection and instance segmentation using a Mask R-CNN (He et al., 2017) head. We use Swin Tiny backbone and evaluate two training regimes: (*i*) full end-to-end fine-tuning (FT), and (*ii*) frozen-backbone training where only the detection head is updated. Both settings follow a standard  $1 \times$  schedule. Table 13 reports bounding-box AP and mask AP. LocAt improves performance in both FT and frozen settings, confirming that the locality-preserving representations produced by GAug and PRR benefit spatial localization tasks as well.

1151 Table 13: **COCO 2017 object detection and instance segmentation** using a Mask R-CNN head.  
 1152 We report bounding-box AP ( $AP^b$ ) and mask AP ( $AP^m$ ) under both full fine-tuning (FT) and frozen-  
 1153 backbone settings.  
 1154

		AP <sup>b</sup>	AP <sup>b</sup> <sub>50</sub>	AP <sup>b</sup> <sub>75</sub>	AP <sup>m</sup>	AP <sup>m</sup> <sub>50</sub>	AP <sup>m</sup> <sub>75</sub>
FT	Swin	42.3	65.0	46.0	38.9	61.9	41.7
	Swin + LocAt	42.8	65.4	46.7	39.3	62.5	42.0
Frozen	Swin	28.9	52.9	28.1	29.3	50.7	30.3
	Swin + LocAt	29.7	54.2	28.7	30.0	51.6	30.9

## L STABILITY OF LEARNED STANDARD DEVIATIONS

The per-patch Gaussian variances are predicted from the queries through a bounded nonlinearity in Eq. (5), ensuring numerical stability; however, in principle these values could collapse to the lower or upper end of the admissible range. Figure 6 analyzes the mean and percentile ranges of the learned standard deviations across layers for a LocAtViT Base model trained on ImageNet-1K. We find that the predicted variances remain well inside the allowed interval and do not cluster near the bounds. Instead, they form non-trivial depth-dependent patterns: early layers tend to use narrower kernels, whereas deeper layers gradually broaden their spatial extent. These observations indicate that GAug learns meaningful locality scales rather than degenerately switching the Gaussian bias “off” (very small variance) or “fully on” (maximal variance) everywhere.

## M HIGHER RESOLUTION OVERHEAD

We quantify the overhead introduced by LocAt when moving from the common  $224 \times 224$  training resolution to a higher  $512 \times 512$  setting, and report in Tab. 14, wall-clock time and peak GPU memory usage for one epoch of training on mini-ImageNet using a single A100 GPU with batch size 16.

## N FAILURE MODES AND LIMITATIONS OF THE GAUSSIAN BIAS

Our design goal for the Gaussian augmentation is to gently bias attention toward local structure, rather than to hard-enforce locality. Empirically, across the backbones and tasks reported in the main paper, we observe performance gain when adding GAug and PRR. However, the magnitude of the gains depends on the underlying attention topology. The largest improvements appear on backbones with unrestricted patch-patch attention (*e.g.*, ViT, RegViT, RoPEViT, Jumbo), whereas

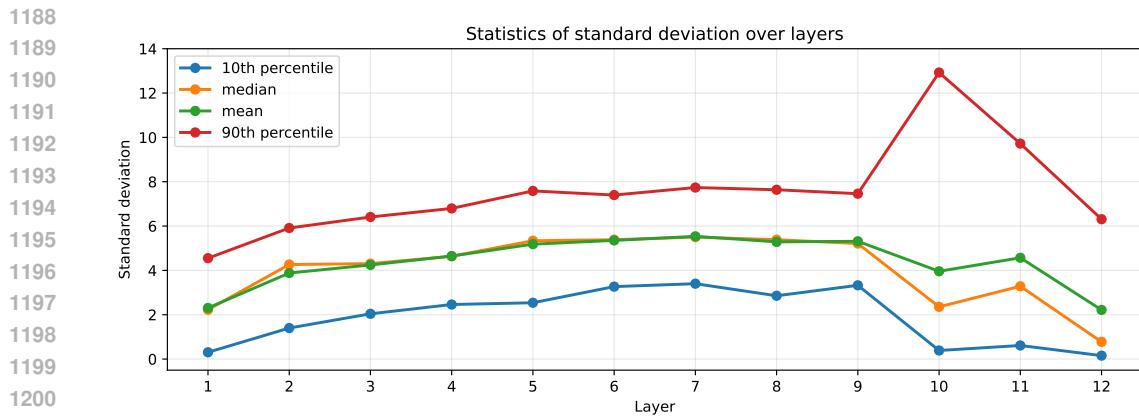


Figure 6: Standard deviation of GAug’s Gaussian over layers

Table 14: Training wall-clock (minutes per epoch) and peak memory usage (GB) on mini-ImageNet for Tiny and Base backbones under different input resolutions. Batch size is 16 and all experiments use a single A100 GPU.

	Size	Image side	Wall-clock time (m)	Memory (GB)
Tiny		224	2.0	1.2
		512	6.1	6.7
Base		224	3.1	4.1
		512	21.1	25.0

the gains on a windowed-attention backbone such as Swin are noticeably smaller. This suggests that GAug is most effective when attention is globally connected and locality is not already hard-coded by the architecture.

To further probe this limitation, we also applied our approach on top of GCViT (Hatamizadeh et al., 2023), a stronger windowed-attention model with attention confined to small grids. In this setting we did not obtain improvements in the performance. We attribute this negative result to the fact that when attention is restricted to narrow windows, the additional Gaussian bias has little room to meaningfully reshape the locality pattern. In contrast, even for powerful unrestricted-attention models such as Jumbo, there remains enough flexibility for GAug and PRR to provide noticeable benefits.