## Preuve

## April 11, 2017

## Abstract

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$$\begin{split} & [\nabla_x \frac{1}{2} ||Ax - b||_2^2]_j = [\nabla_x \frac{1}{2} (Ax - b).(Ax - b)]_j \\ & [\nabla_x \frac{1}{2} ||Ax - b||_2^2]_j = [\nabla_x \frac{1}{2} (\sum_{i=1}^n (\sum_{k=1}^p A_{i,k} x_k)^2 - 2b_i (\sum_{k=1}^p A_{i,k} x_k) + b_i^2)]_j \\ & [\nabla_x \frac{1}{2} ||Ax - b||_2^2]_j = \frac{\partial_{\frac{1}{2}} (\sum_{i=1}^n (\sum_{k=1}^p A_{i,k} x_k)^2 - 2b_i (\sum_{k=1}^p A_{i,k} x_k) + b_i^2)}{\partial x_j} \\ & [\nabla_x \frac{1}{2} ||Ax - b||_2^2]_j = \frac{1}{2} (\sum_{i=1}^n 2(\sum_{k=1}^p A_{i,k} x_k) A_{i,j} - 2b_i A_{i,j}) \\ & [\nabla_x \frac{1}{2} ||Ax - b||_2^2]_j = (\sum_{i=1}^n (\sum_{k=1}^p A_{i,k} x_k) A_{i,j} - b_i A_{i,j}) \\ & [\nabla_x \frac{1}{2} ||Ax - b||_2^2]_j = (\sum_{i=1}^n A_{i,j} (\sum_{k=1}^p A_{i,k} x_k) - b_i) \\ & [\nabla_x \frac{1}{2} ||Ax - b||_2^2]_j = \sum_{i=1}^n A_{j,i}^T [Ax - b]_i \\ & [\nabla_x \frac{1}{2} ||Ax - b||_2^2]_j = [A^T (Ax - b)]_j \end{split}$$