C for Science - Practical Exercise #5

- 1. Create the program that is appended to the end of this document.
 - (a) Configure your compiler to compile in "Release" (optimised) mode. How long does this take to multiply the two large matrices?
 - (b) Identify the appropriate location and insert: #pragma omp parallel for private(j,k)
 - (c) Configure your compiler to use OpenMP. How long does it take now?
 - (d) What significance does private(j,k) have?
 - (e) Why not use three #pragma omp parallel for lines, one for each for loop?

[P. T. O.]

The Newton-Raphson method can be used to compute the root of function which we know the derivative of. Given F(x) we find x^* such that $F(x^*) = 0$. The algorithm starts with an initial guess, x_0 , for the root and calculated an improved guess from the formula:

$$x_{n+1} = x_n - \frac{F(x_n)}{F'(x_n)}, \quad n = 0, 1, \dots$$
 (1)

Iteration stops when a termination criterion is met, some common ones include:

- A maximum number of iterations has been reached (we don't want to wait forever!).
- $F(x_n)$ is "close" to zero.
- $|x_{n+1} x_n|$ is "small".

(also note that we really need $F'(x_n) \neq 0$).

2. Place the following at the top of your program:

(this is a function pointer to a function which takes in one double and returns one double).

3. Write a C function to carry out Newton iteration following the prototype:

where,

- f is the F(x) function we are trying to solve.
- df corresponds to the derivative of the target function, i.e. F'(x).
- max_its is the maximum number of iterations that are allowed.
- tol is the algorithm tolerance, if either $|F(x_n)| < \text{tol}$ or $|x_{n+1} x_n| < \text{tol}$, iteration should stop.
- \mathbf{x} is a pointer to an initial guess, when the Newton iteration has finished, this should be set to x_{n+1} .
- Newton should return the number of iterations carried out.
- 4. Write a main function to
 - (a) prompt the user for an initial guess, maximum number of iterations and a tolerance.
 - (b) Call the Newton function to compute the answer.
 - (c) Print out: x_{n+1} and $F(x_{n+1})$.
- 5. Test the program with the case $F(x) = x^2 2$ at first, with an initial guess of $x_0 = 1$:
 - (a) What is the lowest tolerance setting you can use before the method fails to converge (using fewer than 10 iterations)?
- 6. Test your solver on the Bessel function (present in GSL and other libraries). Take $F(x) = J_0(x)$, $F'(x) = -J_1(x)$ and try an $x_0 = 2$.

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
void multiplyMatrix(double ** matrixA, double ** matrixB, double ** matrixC,
      int rowsA, int colsA, int colsB)
}
   int i,j,k;
   for (i = 0; i < rowsA; i++)
      for (j = 0; j < colsB; j++)
         matrixC[i][j] = 0;
         for (k = 0; k < colsA; k++)
            matrixC[i][j] += matrixA[i][k] * matrixB[k][j];
      }
}
void randomMatrix(double ** matrix, int rows, int cols)
   int i, j;
   for (i = 0; i < rows; i++)
      for (j = 0; j < cols; j++)
         matrix[i][j] = (double)rand()/RAND_MAX;
}
double ** allocMatrix(int rows, int cols)
   double ** matrix;
   int i;
   matrix = (double **) malloc (rows*sizeof(double *));
   if (!matrix) return NULL;
   matrix[0] = (double *) malloc (rows*cols*sizeof(double));
   if (!matrix[0])
   {
      free(matrix);
      return NULL;
   }
   for (i = 1; i < rows; i++)
      matrix[i] = matrix[i-1] + cols;
   return matrix;
}
void freeMatrix(double ** matrix)
   free(matrix[0]);
   free(matrix);
}
int main(void)
{
   double ** matrixA, ** matrixB, ** matrixC, ticks;
   int size = 1600;
```

```
matrixA = allocMatrix(size,size); randomMatrix(matrixA, size, size);
matrixB = allocMatrix(size,size); randomMatrix(matrixB, size, size);
matrixC = allocMatrix(size,size);

printf("Two random matrices generated, now multiplying...\n\n");
ticks = clock();
multiplyMatrix(matrixA, matrixB, matrixC, size, size, size);
printf("Multiplication of two square matrices of size %d took %g seconds\n",
size,(clock() - ticks)/CLOCKS_PER_SEC);

freeMatrix(matrixA);
freeMatrix(matrixB);
freeMatrix(matrixC);

return 0;
}
```