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STAT 5000LAB #3
FALL 2024 DUE TUE SEP 17TH NAME: SAM OLSON
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Directions: Complete the exercises below. When you are finished, turn in any required files online in Canvas, then check-in with the Lab TA for dismissal.

Introduction to Confidence Intervals in SAS

The same SAS code that conducts the two-sample t-test in SAS will also provide a corresponding confidence interval. As an example, consider the observational study on texting speeds from last time:

For a school statistics poster competition in 2006, students timed 15 randomly selected teenagers from the school and 15 randomly selected staff from the school over the age of 30 on how long it took each person to text the following sentence on their phone: "the quick brown fox jumps over the lazy dog." Each subject had the sentence in front of them while they were typing. The text message had to be typed with no errors, no abbreviations, and no use of the phone directory. Time was measured using a stop watch to within 0.01 seconds. Participants were timed using two phones - their own phone and a "control" phone, which was the same for all participants. We would like to determine if teenagers were faster "texters," on average, than adults. The data are located in the smsspeed.csv file and the full SAS program in smsspeed_Lab3.sas within our course's shared folder in SAS Studio.

• First, load in the dataset:

• Then, use the proc ttest command to conduct a test and obtain the corresponding confidence interval for the difference in mean speed between the teenagers and adults. Use the class option to specify the category variable and the var option to specify the response variable.

```
title1 'T-test for Difference in Mean Times - Own Phone';
proc ttest data=SMS;
    class AgeGroup;
    var Own;
run;
```

You'll find the corresponding 95% confidence interval in the columns of the output table for 95% CL Mean and then look at the row for Diff (1-2) Pooled.

• You can change the confidence level using the alpha= parameter. For example, a 99% confidence interval can be obtained by:

```
proc ttest data=SMS alpha=0.01;
    class AgeGroup;
    var Own;
run;
```

Sample Size Simulations in SAS

In lecture, we looked at an example of a randomized experiment to determine which of two treatments was the most effective at reducing bone loss in elderly women. In this experiment, we will assume equal sample sizes, equal population variances, and normally distributed response variables in both samples. We will also assume an estimate of the pooled sample variance for the response variable is available from previous studies, denoted as S_p^2 . The SAS code to calculate sample sizes is provided in the power_Lab3.sas file in the course's shared folder in SAS Studio.

• Suppose our research question is to determine whether or not the two treatment means are different. We will use a hypothesis test with Type I error rate of α and will want the power to detect a difference of δ units between the treatment means to be $1 - \beta$.

In lecture, our example used $\alpha = 0.05$ (alpha), $1 - \beta = 0.8$ (power), $\delta = 4$ (meandiff), and $S_p^2 = 25$ (take the square root and enter as stddev). The code that produced the result of 26 subjects in each treatment group (specified using a period for npergroup, meaning this is what you want SAS to solve for) is given below.

```
proc power;
    twosamplemeans test=diff
alpha = 0.05
    meandiff = 4.0
    stddev= 5
    npergroup = .
    power = 0.80;
run;
```

• Then, use SAS to help you determine the effect of changes to the values of α , $1-\beta$, δ , and S_p^2 on the sample size (n). To make it easier to study these changes, you can modify the SAS code to study the sample size for multiple values of an input value at the same time. For example, to study the effect of increasing power $1-\beta$, you can change the power command to

```
power = 0.80 to 0.95 by 0.05;
```

or you can list values to study, like

```
power = 0.80, 0.9, 0.95, 0.99;
```

• Instead of the analysis above, suppose our research question is to estimate the difference between the two treatment means using a $100(1-\alpha)\%$ confidence with width of no more than δ units.

In lecture, our example used $\alpha = 0.05$, $\delta = 4$, and $S_p^2 = 25$. From the calculation, we obtained a sample size of 50 from each sample. The code that produced this result is given below.

```
proc power;
    twosamplemeans test=diff
alpha = 0.05
    meandiff = 4.0
    stddev= 5
    npergroup = .
    power = 0.975;
run;
```

Note: For sample size determinations using the confidence interval method, the value of power should always be set to the confidence level, $1 - (\alpha/2)$.

Assignment

- 1. Conduct the t-test for the SMS speed example in SAS and complete the following exercises:
 - 1. Using the formula from the notes, calculate by hand a 95% confidence interval for the difference in the two treatment means. Use $t_{28,0.975} = 2.0484$.

Formula:

95% Confidence Interval =
$$(\bar{Y_1} - \bar{Y_2}) \pm t_{28,0.975} S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$$

Where:

$$S_p = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}$$

Calculation

```
# Load Data
library(readr)
smsspeed_1 <- read_csv("C:/Users/samue/OneDrive/Desktop/Iowa_State_PS/STAT 5000/Labs/Lab 3/smsspeed-1.c</pre>
## Rows: 30 Columns: 4
## Delimiter: ","
## chr (1): AgeGroup
## dbl (3): Age, Own Phone, Control
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
      filter, lag
## The following objects are masked from 'package:base':
##
##
      intersect, setdiff, setequal, union
data1 <- smsspeed_1 %>%
 filter(smsspeed_1$AgeGroup == "Over30")
data2 <- smsspeed_1 %>%
 filter(smsspeed_1$AgeGroup == "Teens")
sampleMean1 <- mean(data1$`Own Phone`)</pre>
sampleMean2 <- mean(data2$`Own Phone`)</pre>
difference <- sampleMean1 - sampleMean2</pre>
difference
```

[1] 44.012

```
\#Step 2: Finding standard deviation
s1 <- sd(data1$`Own Phone`)</pre>
s2 <- sd(data2$`Own Phone`)</pre>
#Step 3: Finding sample size
n1 <- length(data1$`Own Phone`)</pre>
n2 <- length(data2$`Own Phone`)</pre>
numerator (n1-1)*(s1^2) + (n2-1)*(s2^2)
denom \leftarrow n1 + n2 - 2
pooled <- sqrt( numerator / denom )</pre>
sqrtFactor <- sqrt(1/n1 + 1/n2)</pre>
tStatDf <- 2.0484
rightSide <- tStatDf*pooled*sqrtFactor</pre>
pooled
## [1] 18.51069
rightSide
## [1] 13.84544
lb <- difference - rightSide</pre>
ub <- difference + rightSide</pre>
lb
## [1] 30.16656
## [1] 57.85744
```

This gives a 95% Confidence Interval for the Difference to be between (30.167, 57.857).

2. Provide a screenshot of the SAS output and use it to verify your calculation.

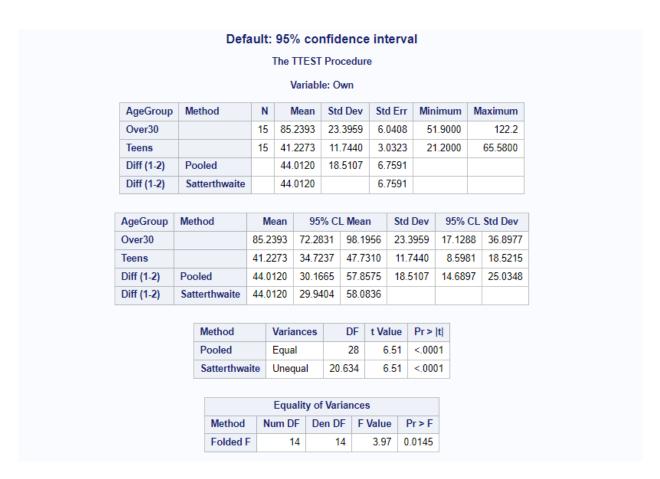


Figure 1: 95% Confidence Interval SAS

3. Interpret the confidence interval in the context of the problem.

A 95% Confidence Interval can be interpreted as a calculated range within which we can be 95% certain the true effect (true difference between two groups) lies.

Within the context of this particular question, it can be interpreted as: We are 95% Confident that the true difference between people Over 30 and Teens texting speeds is between 30.167 and 57.857 seconds; or is would take people Over 30 30.167 to 57.857 more seconds to type a specified message compared to Teens (within the context of being 95% confident).

This may also be interpreted as a commentary on the procedure of calculating the Confidence Interval: If we repeated this procedure of experimentation and calculation and constructed their respective 95% confidence intervals, these confidence intervals would contain the true difference between Over 30 and Teens texting times 95% of the time.

- 2. Use SAS to explore sample size determinations for the bone loss example using the **hypothesis testing method** and complete the following exercises:
 - 1. Explore the effect of changing just the significance level For $\alpha = 0.01, 0.05, 0.1$, what are the resulting sample sizes? Summarize your findings in one concise sentence.

	Fixed	l Scenario Ele	ments	
	Distrib	ution	Normal	
	Method	I	Exact	
	Mean D	ifference	4	
	Standa	rd Deviation	5	
	Nomina	al Power	8.0	
	Numbe	r of Sides	2	
	Null Dif	Null Difference		
	Com	puted N per G	Froup	
Index	Alpha	Actual Power	er N per	Group
1	0.01	0.81	0	39
	0.05	0.80	7	26
2	0.05	0.00	1	20

Figure 2: Alpha

For greater significance levels we calculate needing an increasing number of sampels per Group, and the amount these sample sizes increase by is non-linear, i.e. each decrease of 0.01 in α (greater significant level) requires a larger number of samples to be added per Group compared to its prior significance level.

2. Explore the effect of changing just the power - For $1 - \beta = 0.99, 0.95, 0.9, 0.8, 0.7$, what are the resulting sample sizes? Summarize your findings in one concise sentence.

	Two	The POW o-Sample t Tes			rence
		Fixed Sce			
		Distribution	Distribution		ıl
		Method		Exac	t
		Alpha		0.0	5
		Mean Differe	ence	4	4
		Standard De	eviation	į	5
		Number of Sides		- 2	2
		Null Difference		(0
		Compute	d N per (Group	
Index	No	minal Power	Actual	Power	N per Group
1		0.99		0.991	59
2		0.95		0.952	42
3		0.90		0.902	34
4		0.80		0.807	26
5		0.70		0.716	21

Figure 3: Beta

When changing just the power in relation to the estimated sample size, we see that greater power (smaller β) requires larger sample sizes, and the increase in sample sizes between power levels becomes larger and larger for smaller and smaller β 's.

3. Explore the effect of changing just the true effect size - For $\delta = 1, 2, 3, 4, 5, 6$, what are the resulting sample sizes? Summarize your findings in one concise sentence.

Tv	The POWER Procedure Two-Sample t Test for Mean Difference				
	Fixed 9	Fixed Scenario Elements			
	Distribut	Distribution			
	Method		E	xact	
	Alpha		(0.05	
	Standard	Deviation		5	
	Nominal	Power		8.0	
	Number	Number of Sides		2	
	Null Diffe	Null Difference		0	
	Comp	uted N per (Grou	р	
Index	Mean Diff	Actual Po	wer	N pe	er Group
1	1	0.	801		394
2	2	0.	804		100
3	3	0.804		45	
4	4	0.	807		26
5	5	0.	807		17
6	6	0.	802		12

Figure 4: Effect Size

We require significantly larger sample sizes to detect smaller effect sizes, i.e. the larger the effect size, the smaller the estimated sample size required, holding all else equal.

4. Explore the effect of changing just the estimated population variance - For $S_p^2=1,4,9,16,25,36$, what are the resulting sample sizes? Summarize your findings in one concise sentence.

Tw	o-Sample	t Test for M	ean [Differ	ence
	Fixed	Fixed Scenario Elements			
	Distrib	Distribution		mal	
	Method	i	Б	cact	
	Alpha		0	.05	
	Mean E	Difference		4	
	Nomina	al Power		8.0	
	Numbe	r of Sides		2	
	Null Di	fference		0	
	Comp	outed N per	Grou	ıp	
Index	Std Dev	Actual Po	wer	N p	er Group
1	1	0.	948		3
2	2	0.	876		6
3	3	0.	805		10
4	4	0.	807		17
5	5	0.	807		26
6	6	0	808		37

Figure 5: 95% Confidence Interval SAS

As the estimated population variance increases, we estimate needing increasing larger sample sizes, and the rate at which this increased sample size is estimated is increasing, e.g. the difference between 5 and 6 Std Dev is larger than the difference between 1 and 2 Std Dev.

- 3. Use SAS to explore sample size determinations for the bone loss example using the **confidence interval method** and complete the following exercises:
 - 1. Explore the effect of changing just the significance level For $\alpha=0.01,0.05,0.1$, what are the resulting sample sizes? Summarize your findings in one concise sentence.

The POWER Procedure Two-Sample t Test for Mean Difference

Fixed Scenario Elements		
Distribution Norma		
Method	Exact	
Mean Difference 4		
Standard Deviation	5	
Number of Sides	2	
Null Difference	0	

Computed N per Group				
Index	Alpha	Nominal Power	Actual Power	N per Group
1	0.01	0.995	0.995	85
2	0.01	0.975	0.975	66
3	0.01	0.950	0.952	58
4	0.05	0.995	0.995	66
5	0.05	0.975	0.977	50
6	0.05	0.950	0.952	42
7	0.10	0.995	0.995	57
8	0.10	0.975	0.977	42
9	0.10	0.950	0.952	35

Consistent with the findings of Q2, albeit for a difference method: Higher significance levels (lower α) require significantly larger sample sizes per group.

2. Explore the effect of changing just the true effect size - For $\delta = 1, 2, 3, 4, 5, 6$, what are the resulting sample sizes? Summarize your findings in one concise sentence.

The POWER Procedure				
Two-Sample t Test for Mean Difference				

Fixed Scenario Elements		
Distribution	Normal	
Method	Exact	
Alpha	0.05	
Standard Deviation	5	
Nominal Power	0.975	
Number of Sides	2	
Null Difference	0	

Computed N per Group					
Index	Mean Diff	Actual Power	N per Group		
1	1	0.975	770		
2	2	0.976	194		
3	3	0.976	87		
4	4	0.977	50		
5	5	0.976	32		
6	6	0.978	23		

Consistent with the findings of Q2, 3. albeit for a difference method: We require much larger sample sizes per Group for smaller differences between groups, and smaller sample sizes per Group for larger differences between groups.

3. Explore the effect of changing just the estimated population variance - For $S_p^2=1,4,9,16,25,36$, what are the resulting sample sizes? Summarize your findings in one concise sentence.

Two-	Sample t Test for Mean Differ	ence
	Fixed Scenario Elements	

Fixed Scenario Elements		
Distribution	Normal	
Method	Exact	
Alpha	0.05	
Mean Difference	4	
Nominal Power	0.975	
Number of Sides	2	
Null Difference	0	

Computed N per Group					
Index	Std Dev	Actual Power	N per Group		
1	1	0.996	4		
2	2	0.978	9		
3	3	0.979	19		
4	4	0.976	32		
5	5	0.977	50		
6	6	0.976	71		

Consistent with the findings of Q2, 4. albeit for a difference method: Increasing estimated population variance results in much larger estimations for sample sizes, and the rate of increase for these samples grows larger as the variance increases.

4. Think about how the sample size determination using the confidence interval method relates to the **standard error method**. Summarize your findings in one concise sentence.

These two methods are related in that both methods require and take as input the **pooled estimate of** the population variance to estimate the required sample size.

Total: 50 points # correct: %: