

## Statistics 520, Fall 2025

### Assignment 1

For each of the following situations, define random variables that might be appropriate for conducting an analysis. If distributions are to be assigned to these variables, what should be the support of those distributions? Would it be reasonable to consider the variables to be independent? In some cases there may not be a single correct answer. While it is certainly reasonable to be thinking about some type of model you are **not** being asked to identify a model structure that you would use to address the objectives identified. You are only being asked to define appropriate random variables (and perhaps covariates), identify what support a distribution assigned to them should have, and make a preliminary assessment about an assumption of independence. **Do not suggest a model, you will loose points if you do.**

1. (20 pt.) As part of its Long Term Resource Monitoring Program, the USGS Upper Midwest Environmental Sciences Center located in LaCrosse, Wisconsin has sampled sediment from the Upper Mississippi River from about 120 sites at each of six reaches (or stretches) of the river, from 1992 to 2004. In each stretch of the river, samples were taken from a number of primary habitat categories used as strata in a sampling design. Those categories were Backwater, Impounded Water, Side Channel, and Main Channel Border. Sampling locations were selected separately each year so that repeated sampling of the same location over time did not occur. The sediment samples are brought back to the laboratory, run through a sieve, and the types and numbers of invertebrates are recorded, as is the specific predominant sediment type of sand, silt, or clay (there are actually 6 categories, but 3 is enough to get the idea). Water depth is also measured at the time each sample is collected.

The USGS would like to use these data to address a number of questions

related to the status of mayflies (*Ephemeroptera*) in the river. Mayflies form the basis for a number of aquatic food chains and are also generally considered an indicator of water quality (rather, their absence is considered an indicator of a lack of water quality). There are any number of objectives that might be identified for this study. Here, we will be concerned with only two. Restrict your answer to issues that are relevant for these two objectives.

- (a) Is the presence/absence of mayflies at sampling locations related to the primary habitat category and/or the specific sediment type?
  - (b) Has the abundance of mayflies exhibited a systematic change over the period 1992 to 2004?
2. (10 pt.) A study was conducted at the College of Veterinary Medicine at ISU to examine the efficacy of a vaccine for Porcine Reproductive and Respiratory Syndrome (PRRS) virus. This virus infects sows but affects piglets. In the study, 12 pregnant adult sows were given the vaccine and another 12 were not. Both groups were “challenged” (i.e., exposed to the virus). Sows were housed separately. The number of piglets born normal, born weak, and born stillborn were recorded for each sow. The objective of analysis was to determine whether the vaccine was effective in reducing the effects of the PRSS virus.
  3. (10 pt.) A problem considered by Dr. Dixon about 15 years ago was the topic of a seminar he presented to the department. This problem involved the capture of insects by a predatory plant species, a member of the family of pitcher plants *Sarraceniaceae*. These plants have a long central tube with a hood-shaped part at the upper end. The tube has hair-like structures that point downward. Insects that enter the tube are not able to move back up because of these hairs, and eventually are digested by enzymes in the plant. Insects that do not enter the tube may obtain nectar from the plant without

becoming plant food. A primary prey species of the pitcher plant species involved in this study are a certain type of small wasp. The study was designed to determine how effective these plants are at capturing wasps.

The study consisted of two parts. The first part involved *direct* observation of the plants for several hundred hours. The data recorded were the number of wasps visiting the plants and the number of these that were captured by the plants. There were a total of 376 “plant-hours” of observation, 157 visits, and 2 captures. The second part of the study involved cleaning out a number of plants, leaving the study site, and returning about 2 weeks later (it takes the plants longer than 2 weeks to totally digest a wasp that is captured). The data recorded in this part of the study were the number of wasps captured by the plants over a period of 2 weeks, which was equivalent to 1416 “plant-hours”. There were a total of 6 wasps captured in this *indirect* observation portion of the study.

Our concern here is not with the actual numbers that resulted from this study, but rather with defining random variables that might be used in a statistical analysis. The focus of the seminar by Dr. Dixon was how information from the indirect observation part of the study could be combined with information from the direct observation part of the study to improve estimation of the rate of visits by wasps and the probability of capture given a visit, which were the objectives of the study.