

```

In [473]: from sirf.STIR import (ImageData, AcquisitionData, SPECTDetector, AcquisitionModelUsingMatrix, make_PoissonLogLikelihood, OSMAPOSReconstructor, SeparableGaussianImageFilter, MessageRedirector, )

In [134]: current_directory = os.getcwd()
current_directory

Out[134]: '/home/sam/working/STIR_users_MIC2823'

In [78]: msg = MessageRedirector()
AcquisitionData.set_storage_scheme('memory')

In [47]: # CT2020 parameters
totalActivity = 258.423 # MBq
time_per_projection = 43 # seconds
photon_units_per_mv = 1000 # photons per mv
photopeak_energy = 208 # keV
window_lower = 187.56 # keV
window_upper = 229.31 # keV
source_type = 'Lu177'
collimator = 'na-megp'
num_energy_spectra_channels = 300

# OSEM parameters
iterations = 5
subsets = 12

In [154]: template_image = ImageData(os.path.join(os.getcwd(), "data/Lu177/SPECT_NEMA_Lu177_template.hv"))
mu_map = ImageData(os.path.join(os.getcwd(), "data/Lu177/registered_CTAC.hv"))

measured_data = AcquisitionData(os.path.join(os.getcwd(), "data/Lu177/SPECTCT_NEMA_128_EM001_DS_en_1_Lu177_SC.hdr"))

In [49]: mu_map_stir = mu_map.clone()
mu_map_stir.fill(np.flip(mu_map_stir.as_array(), axis=2))

Out[49]: <sirf.STIR.ImageData at 0x7f8972eef850>

In [50]: axial_slice = 65
coronal_slice = 82
vmax = 0.15

fig, ax = plt.subplots(2, 2, figsize=(10, 9))
ax[0,0].imshow(mu_map.as_array()[axial_slice, :, :], cmap='tab20b', vmax=vmax)
ax[0,0].set_title('SIMIND mu-map \n (transverse slice (axial_slice))')
fig.colorbar(ax[0,0], ax=ax[0,0], shrink=0.7)
ax[0,1].imshow(mu_map_stir.as_array()[axial_slice, :, :], cmap='tab20b', vmax=vmax)
ax[0,1].set_title('STIR mu-map \n (transverse slice (axial_slice))')
fig.colorbar(ax[0,1], ax=ax[0,1], shrink=0.7)
ax[1,0].imshow(mu_map.as_array()[coronal_slice, :, :], cmap='tab20b', vmax=vmax)
ax[1,0].set_title('SIMIND mu-map \n (coronal slice (coronal_slice))')
fig.colorbar(ax[1,0], ax=ax[1,0], shrink=0.7)
ax[1,1].imshow(mu_map_stir.as_array()[coronal_slice, :, :], cmap='tab20b', vmax=vmax)
ax[1,1].set_title('STIR mu-map \n (coronal slice (axial_slice))')
fig.colorbar(ax[1,1], ax=ax[1,1], shrink=0.7)

Out[50]: <matplotlib.colorbar.Colorbar at 0x7f8972cda4d0>

SIMIND mu-map
(transverse slice 65)

STIR mu-map
(transverse slice 65)

SIMIND mu-map
(coronal slice 82)

STIR mu-map
(coronal slice 82)

In [155]: acq_matrix = SPECTUMatrix()
acq_matrix.set_attenuation_image(mu_map_stir)
acq_matrix.set_keep_all_views_in_cache(True)
acq_matrix.set_resolution_model(1.0304, 0.02148, False)
acq_model = AcquisitionModelUsingMatrix(acq_matrix)
acq_model.set_up(measured_data, template_image)

In [156]: def divide(a,b, eps=1e-8):
    return (a/eps)/(b/eps)

def osem(acq_model, acq_data, current_image, sensitivity_image, scatter):
    fm = acq_model.forward(current_image) + scatter
    bpg = acq_model.backward(fm, acq_data, fm)
    return divide(current_image + bpg, sensitivity_image)

def run_osem(acq_model, acq_data, initial_image, iterations, scatter = 0):
    current_image = initial_image.clone()
    sensitivity_images = []
    one_sino = acq_data.get_uniform_copy(1)
    for s in range(iterations):
        for s in range(subsets):
            acq_model.subset_num = s
            if len(sensitivity_images) < subsets:
                sensitivity_images.append(acq_model.backward(one_sino))
            current_image = osem_step(acq_model, acq_data, current_image, sensitivity_images[s], scatter)
            print("Completed iteration [%s] of [%s] iterations, subset [%s] of [%s] subsets")
        return current_image

In [157]: acq_model.no_subsets = subsets

osem_reconstruction = run_osem(acq_model, measured_data, template_image.get_uniform_copy(1), iterations, subsets)

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In [34]: from matplotlib.colors import LogNorm

# round osen_max up to the nearest power of 10
osen_max = 10 ** np.ceil(np.log10(osen_reconstruction.max()))

# Lm177 [85, 40-104, 32-96]

slice = 66
vmin = 0.1

# same as above but highlight lower values with inverse log scale
ax = plt.subplot(1, 3, figsize=(12, 5))
ax0 = ax[0].imshow(osen_reconstruction.as_array()[slice, 40:104, 32:96], norm=LogNorm(vmin=vmin, vmax=osen_max))
```

```

ax[0].set_title('OSEM - no scatter correction')
ax[1].set_title('OSEM - no scatter correction with simind_scatter_correction.as_array()[slice, 40:104, 32:96]')
ax[2].set_title('OSEM - simind scatter correction')
ax[3].set_title('OSEM - simind scatter correction with tew_scatter_correction.as_array()[slice, 40:104, 32:96], normLogLQn')
ax[2].set_title('OSEM - TEW scatter correction')

fig.colorbar(ax0, ax=ax[0], shrink=0.6)
fig.colorbar(ax1, ax=ax[1], shrink=0.6)
fig.colorbar(ax3, ax=ax[2], shrink=0.6)

# draw spheres on images to show where the spheres are
# sphere diams are 60, 37, 28, 22, 17, 13 mm
from matplotlib.patches import Circle

# sphere centres in pixels - Lu177
centres = [(19.5, 42), (42.5, 41.5), (31, 22), (42.5, 28.5), (20, 28.5), (31, 48)]

# sphere radii in pixels
pixel_size = template_image.voxel_sizes()[0] # assume isotropic voxels (which we know they are)
diams = [60, 37, 28, 22, 17, 13]
radii = [d / pixel_size / 2 for d in diams]

for i, a in enumerate(ax):
    for c, r in zip(centres, radii):
        circ = Circle(c, r, color='r', fill=False)
        a.add_patch(circ)

# remove ticks
for a in ax:
    a.set_xticks([])
    a.set_yticks([])

```

OSEM - no scatter correction

OSEM - simind scatter correction

OSEM - TEW scatter correction

```

In [506]: # round osem_max up to the nearest power of 10
osem_max = 10 ** np.ceil(np.log10(osem_reconstruction.max()))

slice = 66
vmin = 0.1

# same as above but highlight lower values with inverse log scale
fig, ax = plt.subplots(1, 3, figsize=(12, 5))
ax0 = ax[0].imshow(osem_reconstruction.as_array()[slice])
ax[0].set_title('OSEM - no scatter correction')
ax1 = ax[1].imshow(osem_reconstruction_with_simind_scatter_correction.as_array()[slice])
ax[1].set_title('OSEM - simind scatter correction')
ax3 = ax[2].imshow(osem_reconstruction_with_tew_scatter_correction.as_array()[slice])
ax[2].set_title('OSEM - TEW scatter correction')
fig.colorbar(ax0, ax=ax[0], shrink=0.6)
fig.colorbar(ax1, ax=ax[1], shrink=0.6)
fig.colorbar(ax3, ax=ax[2], shrink=0.6)

# draw spheres on images to show where the spheres are
# sphere diams are 60, 37, 28, 22, 17, 13 mm
from matplotlib.patches import Circle

centres2 = [(c[0]*32, c[1]*40) for c in centres]
centres_bg = (32*32, 40*32)
radii2 = radii.copy()
radius_bg = 5

for i, a in enumerate(ax):
    for c, r in zip(centres2, radii2):
        circ = Circle(c, r*1.5, color='r', fill=False)
        a.add_patch(circ)
        circ = Circle(centres_bg, radius_bg, color='b', fill=False)
        a.add_patch(circ)

```

```
# remove ticks
for a in ax:
    a.set_xticks([])
    a.set_yticks([])
```

OSEM - no scatter correction

OSEM - simind scatter correction

OSEM - TEW scatter correction

```
In [474]: # some functions for calculating metrics

def sphere_mask(arr_shape, center, radius):
    z, y, x = np.ogrid[:arr_shape[0], :arr_shape[1], :arr_shape[2]]
```

```

dist_sq = (x - center[2])**2 + (y - center[1])**2 + (z - center[0])**2
return dist_sq <= radius**2

def mean_activity_conc.in_sphere(arr, center, radius, voxel_size, calibration_factor):
    mask = sphere_mask(arr.shape, center, radius)
    mean_count_per_vox = np.mean(arr[mask])
    return mean_count_per_vox * ((voxel_size/10)**3) / calibration_factor

def total_activity_conc.in_sphere(arr, center, radius, calibration_factor):
    mask = sphere_mask(arr.shape, center, radius)
    counts = np.sum(arr[mask])
    return counts / calibration_factor

def standard_deviation.in_sphere(arr, center, radius, voxel_size, calibration_factor):
    mask = sphere_mask(arr.shape, center, radius)
    std_count_per_vox = np.std(arr[mask])
    return std_count_per_vox * ((voxel_size/10)**3) / calibration_factor

def SNR(arr, center, radius, voxel_size, calibration_factor):
    signal = mean_activity_conc.in_sphere(arr, center, radius, voxel_size, calibration_factor)
    noise_std = standard_deviation.in_sphere(arr, center, radius, voxel_size, calibration_factor)
    return signal / noise_std

def CNR(arr, center_obj, radius_obj, center_bg, radius_bg, voxel_size, calibration_factor):
    signal_obj = mean_activity_conc.in_sphere(arr, center_obj, radius_obj, voxel_size, calibration_factor)
    signal_bg = mean_activity_conc.in_sphere(arr, center_bg, radius_bg, voxel_size, calibration_factor)
    noise_std_bg = standard_deviation.in_sphere(arr, center_bg, radius_bg, voxel_size, calibration_factor)
    return (signal_obj - signal_bg) / noise_std_bg

calibration_factor = 0.0472 # Counts per second per MBq = counts / acquisition time / activity
calibration_factor *= (time_per_projection * measured_data.dimensions()[12]) # counts per MBq
activity_concentration = 1 - 111 # MBq/ml
activity_concentration_voxel = activity_concentration * template_image.voxel_sizes[0] * template_image.voxel_sizes[1] * template_image.voxel_sizes[2]

radii_150percent = [r * 1.5 for r in radii] # to include spillover
radii_75percent = [r * 0.75 for r in radii]
radii_50percent = [r * 0.5 for r in radii]

centres_3d = [(slice, c[1]+40, c[0]+32) for c in centres] # centres for full 3D array
center_bg_3d = (slice, 40+39.5, 32+32) # centre for full 3D

expected_sphere_activity = activity_concentration * 4/3 * np.pi * (d/2/10)**3 for d in diams

In [47]: def calculate_metrics(arr, center, radius, voxel_sizes, calibration_factor, bg_center, bg_radius):
    voxel_volume = voxel_sizes[0] * voxel_sizes[1] * voxel_sizes[2] # m^3
    voxel_size_mm = np.mean(voxel_sizes) # assuming voxels are approximately cubic

    total_activity = total_activity_conc.in_sphere(arr, center, radius, calibration_factor)
    activity_conc = mean_activity_conc.in_sphere(arr, center, radius, voxel_size_mm, calibration_factor)
    snr = SNR(arr, center, radius, voxel_size_mm, calibration_factor)
    cnr = CNR(arr, center, radius, bg_center, bg_radius, voxel_size_mm, calibration_factor)

    return total_activity, activity_conc, snr, cnr

/tmp/ipykernel_2692758/3259244286.py:26: RuntimeWarning: divide by zero encountered in scalar divide
    return signal / noise_std
Expected sphere activity (MBq):
[182.19989875359364, 42.72668898519332, 18.516889898863544, 8.981775697561378, 4.144202193852766, 1.85328827593
6244]
Metrics
Total Activity, Activity Concentration, SNR, CNR
Metrics for original radii (Total Activity, Activity Concentration, SNR, CNR):
[1.4249688811111111, 0.0001111111111111111, 0.0001111111111111111, 0.0001111111111111111] (33 32681232842295 1 185062

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16351199293, 2.93197589231681, 58.89755823725282), (13.1094941680494, 0.704903811, 0.132782011586384, 2.5167172789792174,
164 (54.62819503292612), (4.59481186892762, 0.950383628113456, 0.394344, 0.8948382529047, 0.657436075151406), (1.66702
165 432.8381418, 0.689892146639338, 2.785120974317535, 3.517523473946673), (0.19112216666666347, 0.1195112933692
166 3838, 1.4126289331489969, 7.15571536643886))
167
168 Metrics for 75% radii:
169 (0.884498945283899, 1.859608258452321, 0.689845509465768, 0.2705337678933), (1.574908153115146, 1.47958463516
170 223797, 5.088325983299597, 79.852801881364944), (0.7744724290928116, 1.3766591486888, 0.6165776696997856, 81.6880
171 566531), (1.0951091350583838, 1.5569161367738274, 4.43433380361073, 88.11885896466576), (0.74204117525056
172 6, 8.85944156665287, 3.9088789013247083, 63.63867326247697), (0.1047931438882878, 0.1735922146459288, 1.68
173 39510221232468, 10.23911659210721)
174
175 Metrics for 50% radii:
176 (20.5645937805950646, 1.9688561813939376, 0.4803835215546766, 155.1629972443276), (5.2758088798866645, 1.69747
177 90092769, 7.110436193710002, 0.24384092781102), (2.677295124732992, 1.6816614027612392, 5.86473297762013,
178 0.7137980632479958), (1.267304378825871, 1.223232908753365, 0.611919011434276, 0.291912015301183), (0.1737
179 1183261896, 1.06062595987803, 15.591988957056677, 33.1139318764139), (0.02557806275368043, 0.296263231033
180 33647, 19.546525759318847)]
181
182 Total activity for 15% radii:
183 [24.1914670865342, 49.799704384349634, 20.17952291368373, 0.9197765650451443, 3.63333275433737, 0.27537872155
184 66855]
185
186 reconstructions = {
187     'OSEM': osem_reconstruction.as_array(),
188     'OSEM with Sinned Scatter': osem_reconstruction_with_sinned_scatter_correction.as_array(),
189     'OSEM with Tiew Scatter': osem_reconstruction_with_tiew_scatter_correction.as_array()
190 }
191
192 # Lists of metrics and radii
193 radii_list = [radii, radii_75percent, radii_50percent, radii_15percent]
194 radii_names = ['Original', '75%', '50%', '15%']
195
196 # Initialize event list for storing dataframes
197 dfts = []

```

```
# Iterate for each radii
for rad, rad_name in zip(radii_list, radii_names):

    # Create a temporary dictionary to build dataframe
    data = {}

    for recon_name, recon_data in reconstructions.items():

        # Check if rad_name is 150% for special case (only Total Activity)
        if rad_name == "150%":
            activity_list = [total_activity_in_sphere(recon_data, c, r, calibration_factor) for c, r in zip(ces,
                                                            data[recon_name]) + activity_list]
        else:
            activity_concentration_list = []
            snr_list = []
            cr_list = []

            for c, r in zip(centres_3d, rad):
                activity_concentration = mean_activity_conc_in_sphere(recon_data, c, r, template_image_voxel_snr)
                snr = activity_concentration / standard_deviation_in_sphere(recon_data, c, r, template_image_voxel_snr)
                bg_std = standard_deviation_in_sphere(recon_data, centre_bg_3d, r, template_image_voxel_sizes)
                nc = (activity_concentration - mean_activity_conc_in_sphere(recon_data, centre_bg_3d, r, template_image_voxel_sizes)) / bg_std
                activity_concentration_list.append(activity_concentration)
                snr_list.append(snr)
                cr_list.append(cr)
```

```

        cnr_list.append(cnr)

        # We store each metric as a separate column in the dictionary
        data[["recon_name", "Activity Concentration"]] = activity_concentration_list
        data[["recon_name", "SNR"]] = snr_list
        data[["recon_name", "CNR"]] = cnr_list

        # Convert dictionary to DataFrame with sphere diameters as the index and append to list
        df = pd.DataFrame(data, index=diams) # Set sphere diameters as the index
        df.index.name = "MEMA sphere diameter" # Set the index title
        dfs.append(df)

    # At this point, dfs contains the four DataFrames. You can access each one by indexing the list.
    original_df, severity5_df, fifty_df, one_fifty_df = dfs

    /tmp/ipykernel_269275/3757504864.py:35: RuntimeWarning: divide by zero encountered in scalar divide
      snr = activity_concentration / standard_deviation_in_sphere(recon.data, c, r, template_image.voxel_sizes())
[8], calibration_factor)

```



NEMA sphere diameter			OSEM with Simind Scatter	OSEM with TEW Scatter
60	242.691467		175.641681	200.189378
37	49.799703		37.372329	43.167686
28	20.179523		15.984001	17.881021
22	8.919776		7.073645	7.999460
17	3.613333		2.491531	3.040209
13	0.275379		0.135469	0.170369

original_df									
In [502]:									
Out[502]:									
NEMA sphere diameter									
	OSEM - Activity Concentration	OSEM - SNR	OSEM - CNR	OSEM with Simind Scatter - Activity Concentration	OSEM with Simind Scatter - SNR	OSEM with Simind Scatter - CNR	OSEM with TEW Scatter - Activity Concentration	OSEM with TEW Scatter - SNR	OSEM with TEW Scatter - CNR
60	1.517551	3.118323	62.640410	1.247191	2.707297	287.085257	1.330680	2.914540	115.867997
37	1.185002	2.931828	58.897558	1.004254	2.582313	855.213126	1.075202	2.782764	153.171514
28	1.032983	2.516713	54.628150	0.900085	2.267638	761.574056	0.954874	2.422586	144.914152
22	0.960384	2.094010	56.987436	0.848574	2.782032	601.932388	0.852051	2.967017	160.470624
17	0.689593	2.785126	51.751235	0.567389	1.966738	312.119226	0.632058	2.552387	148.833649
13	0.118511	1.410269	7.155715	0.061081	0.861318	44.549969	0.079185	1.023473	19.979077

seventy_five_df									
In [504]:									
Out[504]:									
NEMA sphere diameter									
	OSEM - Activity Concentration	OSEM - SNR	OSEM - CNR	OSEM with Simind Scatter - Activity Concentration	OSEM with Simind Scatter - SNR	OSEM with Simind Scatter - CNR	OSEM with TEW Scatter - Activity Concentration	OSEM with TEW Scatter - SNR	OSEM with TEW Scatter - CNR
60	1.859690	6.808646	92.270534	1.562564	5.751009	1079.620464	1.639753	6.110158	242.318050
37	1.497658	5.088326	79.862580	1.302519	4.606647	1102.498270	1.366953	4.802178	207.713416
28	1.376659	4.684777	81.680056	1.227521	4.384244	870.115249	1.286546	4.538594	231.795008
22	1.156017	4.434034	88.118051	1.049813	4.109932	578.262517	1.087210	4.214877	256.821606
17	0.859484	3.900879	63.638673	0.734412	2.843879	645.908800	0.793706	3.665015	207.338718
13	0.173398	1.683951	10.239116	0.111628	1.185797	107.119389	0.130204	1.382025	23.483998

fifty_df									
In [505]:									
Out[505]:									
NEMA sphere diameter									
	OSEM - Activity Concentration	OSEM - SNR	OSEM - CNR	OSEM with Simind Scatter - Activity Concentration	OSEM with Simind Scatter - SNR	OSEM with Simind Scatter - CNR	OSEM with TEW Scatter - Activity Concentration	OSEM with TEW Scatter - SNR	OSEM with TEW Scatter - CNR
60	1.968056	8.480383	105.162997	1.665876	7.197411	1433.575653	1.727400	7.271773	264.502421
37	1.697473	7.210498	96.243840	1.409663	6.443198	961.380652	1.544167	6.619438	280.798782
28	1.601661	5.864733	133.073900	1.410632	5.195520	736.619666	1.504947	5.535437	300.824155
22	1.223233	6.911991	91.291912	1.087273	7.330899	808.646878	1.147791	6.314268	300.185761
17	1.006026	15.591989	73.311932	0.986193	17.852331	957.900355	0.937909	14.350916	178.067026
13	0.296262	inf	19.546257	0.250783	inf	242.472378	0.252186	inf	46.828638