

Exam.	Back		
Level	BE	Full Marks	80
Programme	BCT	Pass Marks	32
Year / Part	IV / I	Time	3 hrs.

Subject: - Digital Signal Analysis and Processing (CT704)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Define Energy and Power type discrete time signal. Check whether signal $x[n] = e^{j(\pi n/3 + \pi/4)}$ is periodic or not. If it is periodic, state its periodic time. [2+2]
2. Find the output of LTI system having impulse response $h[n] = (1/2)^n \{u[n+2] - u[n-2]\}$ and input signal $x[n] = \{2, 1, 0.5, -1\}$. Also check the answer. [3+2]
3. State and explain the properties of a Region of Convergence (ROC). Find the inverse z-transform of $X(z) = z^2 \left[1 - \frac{3}{2}z^{-1} \right] (1+z^{-1})(1-z^{-1})$ [3+3]
4. Plot the pole-zero in z-plane and Draw Magnitude Response (not to the scale) of the system described by difference equation $y[n] - 0.4y[n-1] + 0.2y[n-2] = x[n] + 0.5x[n-1] + 0.6x[n-2] + 0.8x[n-3]$ [3+7]
5. Draw the direct form and Lattice structure of a filter with system function $H(z) = 1 + 0.7z^{-1} + 1.2z^{-2} - z^{-3}$. [3+7]
6. Why Kaiser window is better than other fixed windows in FIR filter design? Find out first six coefficients of impulse response of a low pass FIR filter having Pass band edge frequency $\omega_p = 0.2\pi$, Stop band edge frequency $\omega_s = 0.5\pi$ and Stop band attenuation $\alpha_s = 41\text{dB}$ using any appropriate window function. [2+6]
7. What is an optimum filter? Show mathematical expression of the Remez exchange algorithm for FIR filter design with flow chart. [1+6]
8. Design a low pass discrete IIR filter by Bilinear Transformation method to an approximate Butterworth filter having specifications as below: [15]

Pass bandedge frequency (ω_p) = 0.27π radians
 Stop bandedge frequency (ω_s) = 0.58π radians
 Passband ripple (δ_p) = 0.11
 Stopband ripple (δ_s) = 0.21, Consider sampling frequency 0.5 Hz.
9. Compute the 8-point DFT of the sequence $x[n] = \left\{ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, 0, 0, 0, 0 \right\}$ using Decimation in Frequency Fast Fourier Transform (DIF-FFT) algorithm. [7]
10. What is a zero padding? If $X_1(k)$ and $X_2(k)$ are DFT of sequence $x_1[n] = \{1, 2, 0, 1, -2\}$ and $x_2[n] = \{1, 0, 1, 1, 2\}$ respectively then find the sequence $x_3[n]$; If DFT of $x_3[n]$ is given by $X_3(k) = X_1(k), X_2(k)$. [1+7]

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1. Plot the sequence $x[n] = u[n] - u[n-3] + 5\delta[n-4] = nu[n-6]$. List out the properties of LTI system. [3+2]
2. Determine whether the following system are: [3+3]
 - $y[n] = y[n-4] + x[n-4]$ is Time-invariant or not
 - $y[n] = x^2[n]$ is Linear or Non-linear
3. Define a ROC. What are the properties of ROC of z-transform? Find the inverse Z-transform of $X(z) = (2z^2 + 2z^2 + 3z + 5)/(z^2 - 0.1z - 0.2)$, ROC: $|z| < 0.4$. [1+3+5]
4. The poles of a system are located at: $0.45-0.77i$ and $-2 \pm 0.3i$. Map the poles and zero in the z-plane and plot the magnitude response of the system. [2+8]
5. Obtain the Direct Form I and Direct Form II realization of the following system. [5]

$$3y[n] + y[n-1] + 2y[n-4] = 2x[n] + x[n-3]$$
6. Determine the lattice coefficients corresponding to the FIR filter with the system function: [5]

$$H(z) = A_3(z) = 1 + \frac{52}{96}z^{-1} + \frac{25}{40}z^{-2} + \frac{1}{3}z^{-3}$$
7. Design a digital low-pass filter with the following specification: [12]
 - Pass-band magnitude constant to 0.7 dB below the frequency of 0.15π
 - Stop-band attenuation at least 14 dB for the frequencies between 0.6π to π

Use Butter worth approximation as a prototype and use impulse invariance method to obtain the digital filter.
8. Design a FIR linear phase filter using Kaiser window that meets the following specifications: [9+3]

$$|H(e^{jw})| \leq 0.01, 0 \leq |w| \leq 0.25\pi$$

$$0.95 \leq |H(e^{jw})| \leq 1.05, 0.35\pi \leq |w| \leq 0.6\pi$$

$$|H(e^{jw})| \leq 0.01, 0.65\pi \leq |w| \leq \pi$$

Also determine the minimum length ($M+1$) of the impulse response and Kaiser window parameter β .
9. Why do we need DFT? Draw the butterfly structure to compute the DFT of the following signal using Radix-2 DIFFFT algorithm, and compute $X(2)$ and $X(1)$ only $x[n] = \{1.5, -1, 1.8, 0.6, 3, 1.7\}$ [3+7]
10. Define zero padding. Find the linear convolution through circular convolution with padding of zeros for the following sequences: $x[n] = \{1, 1, 1, 1\}$ and $h[n] = \{2, 3\}$. [1+5]

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1. Explain the process of calculating fourier series coefficients. [3]
2. Determine the system output $y(n)$ of the following signals: $h(n) = \{1,1,1\}$ and $x(n) = \{1,1,1,1\}$ [6]
3. Define a ROC. Find inverse Z-transform of $X(z) = z/\{(z-0.4)(z+1.5)^2\}$, ROC: $|z| < 0.4$ [1+5]
4. State linear constant coefficient difference equation and corresponding system function.
Determine the output sequence of the system with impulse response $h[n] = (1/2)^n u[n]$ when the input signal is $x[n] = 10 - 5\sin(\pi n/2) + 20\cos\pi n$ $-\infty < n < \infty$. [3+7]
5. The system function of a filter is $H(z) = 2 + 1.8z^{-1} - 1.6z^{-2} + z^{-3}$. Draw the Direct Form and Lattice Structure implementation of the above filter. [3+7]
6. Explain in detail about how rectangular window is used in FIR filter design. How Gibb's oscillations arise in this process. [6]
7. Explain about Remaz exchange algorithm with suitable derivation and flow chart. [9]
8. Using bilinear transformation, design a butterworth low pass filter which satisfies the following Magnitude Response. [12]

$$0.89125 \leq |H(e^{j\omega})| \leq 1 \quad \text{for } 0 \leq \omega \leq 0.2\pi$$

$$|H(e^{j\omega})| \leq 0.17783 \quad \text{for } 0.3\pi \leq \omega \leq \pi$$
9. Explain briefly about bilinear transformation method of IIR filter design. [3]
10. Why do we need DFT? Find 8-point DFT of sequence $x[n] = \{1, -1, 2, 2, 1, 1, 2, 2\}$ using Fast Fourier Transform algorithm. [2+6]
11. Find $x_3[n]$ if DFT of $x_3[n]$ is given by $X_3(k) = X_1(k)X_2(k)$ where $X_1(k)$ and $X_2(k)$ are 5-point DFT of $x_1[n] = \{1, -2, 2, 1, 4\}$ and $x_2[n] = \{2, 1, -3, -1\}$ respectively. [7]

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1. Define and plot a discrete time unit step signal. Explain its relation with unit impulse signal. [1+2]
2. Calculate $y[n]$, if $x[n]$ is $x[-2] = 0.5$, $x[0] = 1$, $x[1] = 0.75$, $x[3] = 0.5$ and $n[n]$ is $n[0] = 1$, $n[1] = 0.75$ and $n[2] = 0.5$ and verify your result. [6]
3. Define a ROC. Find inverse Z-transform of $X(z) = (2z^3 + 2z^2 + 3z + 5) / (z^2 - 0.1z - 0.2)$, ROC: $|z| < 0.4$ [1+5]
4. Define the difference equation with example. The Poles of a system are located at:- $0.45 + 0.77i$ and $2 \pm 0.7i$ and zeros at: $1.2 \pm 0.43i$. Plot the magnitude response of this system. [2+8]
5. Draw the Lattice Structure from the following system function: [10]

$$\frac{1 + \frac{1}{3}z^{-1} + \frac{9}{8}z^{-2} + \frac{4}{3}z^{-3} + z^{-4}}{1 + \frac{2}{3}z^{-1} + \frac{5}{8}z^{-2} + \frac{2}{3}z^{-3} + z^{-4}}$$

6. Design a digital Butterworth low pass filter satisfying the constraints

$$\begin{cases} 0.707 \leq |H(e^{jw})| \leq 1 & 0 \leq w \leq \frac{\pi}{2} \\ |H(e^{jw})| \leq 0.2 & \frac{3\pi}{4} \leq w \leq \pi \end{cases}$$

- With $T = 1\text{sec}$ using bilinear transformation method. Realize the filter using the most convenient realization form. [11+4]

7. Design an FIR linear phase filter using Kaiser window to meet the following specifications: [8]

$$0.98 \leq |H(e^{jw})| \leq 1.02, \text{ for } 0 \geq w \geq 0.9\pi$$

$$|H(e^{jw})| \leq 0.01, \text{ for } 0.14\pi \leq w \leq \pi$$

8. Draw the Howchart of Remez-Exchange theorem and explain it. [7]
9. Why we need FFT? Find 8-point DFT of sequence $x[n] = \{1, -1, 3, 2, 1, 1, 3, -2\}$ using Decimation in frequency Fast Fourier Transform (DIFFFT) algorithm. [2+6]
10. Find $x_3[n]$ if DFT of $x_3[n]$ is given by $X_3(k) = X_1(k) X_2(k)$ where $X_1(k)$ and $X_2(k)$ are 5-point DFT of $x_1[n] = \{1, -2, 5, 1, 2\}$ and $x_2[n] = \{1, 2, -3, -2\}$ respectively. [7]

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1. Define energy and power signal. Check the signal $x[n] = u[n]$ and $x[n] = \delta[n]$ is Energy or Power type. [2+3]
2. Find the output of LTI system having impulse response $h[n] = (1/3)^n \{u[n+1]-u[n-2]\}$ and input signal $x[n] = \{2,1,0.5,3\}$. [5]
3. State the properties of region of convergence (ROC). Drive the convolution property of Z-transform. [3+3]
4. Find the output of LTI System having impulse response $h[n] = (1/2)^n u[n]$ and input signal $x[n] = 5e^{j\pi n/3}$ for $-\infty < n < \infty$. [4]
5. Plot Magnitude Response (not to the scale) of the system described by difference equation.
 $y[n]-0.5y[n-1]+0.3y[n-2]=x[n]+0.7x[n-1]$ [6]
6. Determine the Direct Form II realization of the following system
 $y(n) = -0.1y(n-1) + 0.72y(n-2) + 0.7x(n) - 0.252x(n-2)$ [4]
7. Compute the lattice coefficients and draw the lattice structure of following FIR system
 $H(z) = 1 + 2z^{-1} - 3z^{-2} + 4z^{-3}$ [6]
8. Draw the flowchart of Remez-Exchange theorem and explain it. Design an FIR linear phase filter using Kaiser window to meet the following specifications:
 $0.99 \leq |H(e^{jw})| \leq 1.01$, for $0 \geq w \geq 0.19\pi$ [6+8]
 $|H(e^{jw})| \leq 0.01$, for $0.21\pi \leq w \leq \pi$
9. Design a low pass digital filter by Bilinear Transformation method to an approximate Butterworth filter, if passband edge frequency is 0.25π radians and maximum deviation of 1 dB below 0 dB gain in the passband. The maximum gain of -15 dB and frequency is 0.45π radians in stopband, Consider sampling frequency 1Hz. [15]
10. Find 8-point DFT of sequence $x[n] = \{1,1,0,1,0,1,2\}$ using Decimation in Time Fast Fourier Transform (DITFFT) algorithm. [7]
11. Why we need DFT? If $X_1(k)$ and $X_2(k)$ are DFT of sequence $x_1[n] = \{1,2,4\}$ and $x_2[n] = \{-1,2,3,1\}$ respectively, then find the sequence $x_3[n]$, if DFT of $x_3[n]$ is given by $X_3(k) = X_1(k)X_2(k)$. [2+6]

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1. How fourier series coefficients are calculated? Explain. [4]
2. Find the output of LTI system having impulse response $h[n]$ with $h[-2] = 1$, $h[0] = 2$, $h[1] = 3$ and input signal $x[n]$ with $x[0] = 1/2$, $x[2] = 2$, $x[3] = 3$. Also check the answer. [3+2]
3. Explain the properties of Region of Convergence with examples. [6]
4. Describe stability and causality characteristics of LTI system in terms of Impulse Response and ROC of its transfer function with suitable examples. [4]
5. Plot the pole-zero in z-plane and Draw Magnitude Response (not to the scale) of the system described by difference equation. [2+4]

$$y[n] - 0.4y[n-1] + 0.1y[n-2] = x[n] + 0.6x[n-1]$$
6. Determine the Direct Form I and Direct Form II realization of the following system. [5]

$$y(n) = -0.1y(n-1) + 0.2y(n-2) + 3x(n) + 3.6x(n-2) + 0.6x(n-3)$$
7. Compute the lattice coefficients and draw the lattice structure of following FIR system. [5]

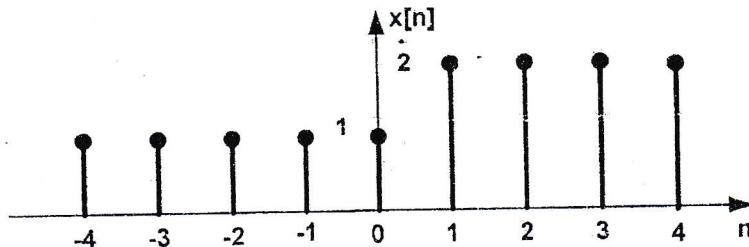
$$H(z) = 1 + 2z^{-1} + z^{-2}$$
8. Describe how digital FIR filter can be design by window method. Why Kaiser window is better than other fixed windows in FIR filter design? [5+3]
9. What is an optimum filter? Show mathematical expression of Remez exchange algorithm for FIR filter design. [1+6]
10. Explain about the advantages of selecting bilinear transformation method over impulse invariance method (IIM). Design a digital low pass Butterworth filter using impulse invariant transformation with pass band and stop band frequencies 200Hz and 500Hz respectively. The pass band and stop band attenuation are -5dB and -12dB respectively. The sampling frequency is 5kHz. Use IIM method. [3+12]
11. Find the FFT of the signal $x[n]\{1,1,2,4,3,1,2,1\}$ using DIT-FFT algorithm. [8]
12. Compute Circular Convolution of $h(n) = \{1, 2, 1, -1, 1\}$ and $x[n] = \{1, 2, 3, 1\}$. [7]

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1. Find the odd and even part of the following signal: [4+5]



A discrete time LTI system has input signal and impulse response as,

$x[n] = \begin{cases} 1 & -1 \leq n \leq 1 \\ 0 & \text{elsewhere} \end{cases}$ and $h[n] = \begin{cases} 1 & -1 \leq n \leq 1 \\ 0 & \text{elsewhere} \end{cases}$ Find the output of the system using graphical method,

2. Find the inverse z transform of: [6]

$$X(Z) = (1+2z^{-1}+z^{-2})/(1+1.5z^{-1}+0.5z^{-2}), |z| > 1$$

using partial fraction method.

3. Why do we need difference equation? State linear constant coefficient difference equation and corresponding system function. [2+3+5]

Consider an LTI system with impulse response $h[n]=(1/2)^n u[n]$. Determine $y[n]$, if the input is $x[n] = Ae^{jn\pi}$

4. If a 3 stage lattice filter for all pole polynomial has coefficients. [5]

$$K_1 = \frac{1}{4}, K_2 = \frac{1}{2} \text{ and } K_3 = \frac{1}{3} \text{ Obtain the system function of this filter.}$$

5. What is the importance of quantization in Digital Signal Processing? Which one is better rounding or truncation? Explain about limit cycles in recursive system? Define dead band. [1+1+2+1]

6. Explain in detail about how rectangular window is used in FIR filter design. How Gibb's oscillations arise in this process. [6]

7. What is a Remez exchange algorithm? Derive its equation and draw its flow chart. [9]

8. Design a low pass digital filter by Bilinear Transformation method to an approximate Butter worth filter it passband frequency is 0.2π radians and maximum deviation of 1 db below 0 dB gain in the pass band. The maximum gain of -15 db and frequency is 0.4π radians in stop band, consider sampling frequency 1 Hz. [15]

9. A system has input signal $x[n] = \{1,2,3,4\}$ and impulse response $h[n] = \{1,3,5,7\}$ and the DFT of $x[n]$ is $X[k]$ and the DFT of $h[n]$ is $H[k]$. Find the output of the system $y[n]$ if $G[k] = X[k].H[k]$ [7]

10. Find DFT for $\{1, 1, 2, 0, 1, 2, 0, 1\}$ using FFT DIT butterfly algorithm and plot the spectrum. [6+2]

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1. Find the even and odd part of signal $x[n]$, [3]

$$x[n] = \begin{cases} 1 & \text{for } -4 \leq n \leq 0 \\ 2 & \text{for } 1 \leq n \leq 4 \end{cases}$$

2. A discrete time LTI system has impulse response $h(n) = \{1, 3, 2, -1, 1\}$ for $-1 \leq n \leq 3$.

Determine the system output $y(n)$ if the input $x(n)$ is given by $x(n) = 2\delta(n) - \delta(n-1)$. [6]

3. Define ROC. Find inverse Z-transform of [1+5]

$$X(z) = 1/\{(z - 0.5)(z + 2)\}, \text{ if}$$

- i) ROC: $0.5 < |z| < 2$
- ii) ROC: $|z| < 0.5$
- iii) ROC: $|z| > 2$

4. The poles of a system are located at: $0.45+0.77i$ and $-2 \pm 0.3i$ and zeroes at: $1.2 \pm 3i$. Map the poles and zero in the z-plane and plot the magnitude response of the system. [2+8]

5. Compute Lattice coefficients and draw lattice structure for given IIR system $H(z) = 1/(1-0.01z^{-1} - 0.23z^{-2} + 0.5z^{-3})$. Also check the stability of given system. [4+2+1]

6. What is limit cycle effect in recursive system? Describe with one example showing how it occurs. [3]

7. Design a low pass FIR filter having Pass band edge frequency $\omega_p = 0.3\pi$, Stop band edge frequency $\omega_s = 0.5\pi$ and Stop band attenuation $\alpha_s = 40$ dB using any appropriate window function. [8]

8. What is optimum filter? Show mathematical expression of Remez exchange algorithm for FIR filter design. [1+6]

9. What is the advantage of bilinear transformation? Design a low pass discrete time Butterworth filter applying bilinear transformation having specifications as follows: [2+9+4]

Pass band frequency (ω_p) = 0.25π radians

Stop band frequency (ω_s) = 0.55π radians

Pass band ripple (δ_p) = 0.11

and stop band ripple (δ_s) = 0.21

Consider sampling frequency 0.5 Hz.

Also, convert the obtained digital low-pass filter to high-pass filter with new pass band frequency (ω'_p) = 0.45π using digital domain transformation.

10. Why do we need Discrete Fourier Transform (DFT) although we have Discrete-time Fourier Transform (DTFT)? Find circular convolution between $x[n] = \{1, 2\}$ and $y[n] = u[n] - u[n-4]\$. [2+5]

11. How fast is FFT? Draw the butterfly diagram and compute the value of $X(7)$ using 8 pt DIT-FFT for the following sequences: [2+6]

$$x(n) = \{1, 0, 0, 0, 0, 0, 0, 0\}$$

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1. Find the even and odd part of signal $x[n]$, [3]

$$x[n] = \begin{cases} 1 & \text{for } -4 \leq n \leq 0 \\ 2 & \text{for } 1 \leq n \leq 4 \end{cases}$$

2. Illustrate the significance of convolution summation in digital signal analysis. Compute the convolution of the following signals: $h(n) = \{1, 0, 1\}$ and $x(n) = \{1, -2, -2, 3, 4\}$ [2+4]

3. Define Region of Convergence. Find inverse Z - transform of $X(z) = z / \{(z-1)(z-2)^2\}$, ROC: $|z| < 1$ [1+5]

4. Given $H(z)$ for a system with the following difference equation:
 $y(n) = x(n) + x(n-2)$ [2+6+2]

Plot its poles and zeros in Z plane. Determine its magnitude response. Also, determine whether system is causal and stable.

5. Draw lattice structure for given pole - zero system [6]

$$H(z) = (0.5 + 2z^{-1} + 0.6z^{-2}) / (1 - 0.3z^{-1} + 0.4z^{-2})$$

6. What do you mean by Limit Cycle? How it occurs in recursive system? [1+3]

7. What is the condition satisfied by Linear phase FIR filter? Show that the filter with $h(n) = \{-1, 0, 1\}$ is a linear phase filter. [2+4]

8. Use Hanning window method to design a digital low-pass FIR filter with pass-band edge frequency (w_p) = 0.25π , stop-band edge frequency (w_s) = 0.35π where main lobe width of Hanning window is $8\pi/M$, M is the filter length. [9]

9. Why Spectral Transformation is required? [2]

10. Design a low-pass digital filter by impulse invariance method to an approximate Butterworth filter, if passband edge frequency is 0.2π radians and maximum deviation of 0.5 dB below 0 dB gain in the passband. The maximum gain of -15 dB and frequency is 0.35π radian in stopband, consider sampling frequency 1Hz. [13]

11. Why do we need Discrete Fourier Transform (DFT) although we have Discrete-time Fourier Transform (DTFT)? Find circular convolution between

$$x[n] = \{1, 2\} \text{ and } y[n] = u[n] - u[n-4].$$

12. How fast is FFT? Draw the butterfly diagram and compute the value of $x(7)$ using 8 pt DIT-FFT for the following sequences: [2+6]

$$x(n) = \{1, 0, 0, 0, 0, 0, 0, 0\}$$

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1. Determine which of the following signals are periodic and compute their fundamental period: [3]
 - $\cos(\pi n^2/8)$
 - $\cos(n/2) \cos(\pi n/4)$
2. Find output, $y(n)$ when: $h(n) = \{5,4,3,2\}$ and $x(n) = \{1,0,3,2\}$ [6]
3. List out the properties of Region of Convergence. Find the Z-transform and locate the ROC of the signal. [2+4]

$$x[n] = \left(-\frac{1}{3}\right)^n u[n] - \left(\frac{1}{3}\right)^n u[-n-1]$$
4. Find the output of LTI System having impulse response [4]

$$h[n] = (1/3)^n u[n]$$
 and input signal $x[n] = 5e^{j\pi n/2}$ for $-\infty < n < \infty$.
5. Plot Magnitude Response (not to the scale) of the system described by difference equation. $y[n] - 0.3 y[n-1] + 0.225 y[n-2] = x[n] + 0.5x[n-1]$ [6]
6. Determine the Cascade Form realization of the following system. [4]

$$y[n] - \frac{3}{4}y[n-1] + \frac{1}{8}y[n-2] - x[n] - 2x[n-1] = 0$$
7. Compute the lattice coefficients and draw the lattice structure of following FIR system [6]

$$H(z) = 1 + 3.1z^{-1} + 5.5z^{-2} + 4.2z^{-3} + 2.3z^{-4}$$
8. Describe how FIR filter can be designed by window method. Discuss the characteristics of different type of window function. [4+4]
9. What is an optimum filter? Show mathematical expression of Remez exchange algorithm for FIR filter design. [1+6]
10. Using bilinear transformation method, design a digital filter using Butterworth approximation which satisfies the following conditions: [10]

$$0.8 \leq |He^{jw}| \leq 1 \quad \text{for } 0 \leq w \leq 0.2\pi$$

$$|He^{jw}| \leq 0.2 \quad \text{for } 0.6\pi \leq w \leq \pi$$
11. A digital LPF with cut off frequency $w_c = 0.2575 \pi$ is given as $H(Z) = \frac{0.1 + 0.4z^{-1}}{1 - 0.6z^{-1} + 0.1z^{-2}}$ Design a digital high pass filter with $w'_c = 0.3567\pi$. [5]
12. Define Padding zones. Find 8-point DFT of sequence. [1+6]

$$x[n] = \{1,1,0,0,1,1,2\}$$
 using Decimation in Time Fast Fourier Transform (DITFFT) algorithm.
13. Why we need DFT? State and prove Circular Convolution property of DFT. [2+2+4]

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BCT	Pass Marks	32
Year / Part	IV / I	Time	3 hrs.

Subject: - Digital Signal Analysis and Processing (CT704)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Define Energy and Power type signal with suitable example. Check the signal $x[n] = \cos(2\pi n/5) + \sin(\pi n/3)$ is periodic or not. [2+2]
2. Define LTI system. Find the output of LTI system having impulse response $h[n] = 2u[n] - 2u[n-4]$ and input signal $x[n] = (1/3)^n u[n]$. [1+4]
3. State the properties of region of convergence (ROC)? Derive the time shifting property of Z-transform. [3+3]
4. Why do we need Difference Equation? Draw Pole-zero in Z-Plane and plot magnitude response (not to the scale) of the system described by difference equation $y[n] - 0.4y[n-1] + 0.2y[n-2] = x[n] + 0.1x[n-1] - 0.06x[n-2]$ [2+2+6]
5. Determine the Direct Form II realization of the following system $y(n) = -0.1y(n-1) + 0.72y(n-2) + 0.7x(n) - 0.252x(n-2)$ [4]
6. Compute the lattice coefficients and draw the lattice structure of following FIR system $H(z) = 1 + 2z^{-1} - 3z^{-2} + 4z^{-3}$ [6]
7. Design a digital FIR filter for the design of the low pass filter having $\omega_p = 0.3\pi$, $\omega_s = 0.5\pi$, $\alpha_s = 40$ dB using suitable window function. [8]
8. What is optimum filter? Describe Remez exchange algorithm for FIR filter design with flow chart. [1+6]
9. What is the advantage of bilinear transformation? Design a low pass discrete time Butterworth filter applying bilinear transformation having specifications as follows: [2+9+4]

Pass band frequency (ω_p) = 0.25π radians
 Stop band frequency (ω_s) = 0.55π radians
 Pass band ripple (δ_p) = 0.11
 And stop band ripple (δ_s) = 0.21

Consider sampling frequency 0.5Hz

Also, convert the obtained digital low-pass filter to high-pass filter with new pass band frequency (ω'_p) = 0.45π using digital domain transformation.

10. Why do we need FFT? Find 8-point DFT of sequence $x[n] = \{1, 1, 2, 2, 1, 1, 2, 1\}$ using Decimation in frequency FFT (DIFT) algorithm. [2+7]
11. Find $x_3[n]$ if DFT of $x_3[n]$ is given by $X_3(k) = X_1(k) X_2(k)$ where $X_1(k)$ and $X_2(k)$ are 4-point DFT of $x_1[n] = \{1, 2, -2\}$ and $x_2[n] = \{1, 2, 3, -1\}$ respectively. [6]