

## DOUBT SESSION

## Ques 1. Search in Rotated Sorted Array

<https://leetcode.com/problems/search-in-rotated-sorted-array/description/>

There is an integer array `nums` sorted in ascending order (with distinct values).

Prior to being passed to your function, `nums` is possibly left rotated at an unknown index `k` ( $1 \leq k < \text{nums.length}$ ) such that the resulting array is `[nums[k], nums[k+1], ..., nums[n-1], nums[0], nums[1], ..., nums[k-1]]` (0-indexed). For example, `[0,1,2,4,5,6,7]` might be left rotated by 3 indices and become `[4,5,6,7,0,1,2]`.

Given the array `nums` after the possible rotation and an integer `target`, return the index of `target` if it is in `nums`, or `-1` if it is not in `nums`.

You must write an algorithm with  $O(\log n)$  runtime complexity.

Example:

`[1 2 3 4 5]`

↓ Rotate

`[2 3 4 5 1]`

↓

`[3 4 5 1 2]`

If `target = 5` in the final rotated array then we will return the index of 5. [Ans = 2]

The Brute Force solution can be easily solved in linear time,  $O(N)$ .

Approach for optimised solution using Binary Search:

Given a `X`, we have to design a check function such that:

Partitioning space around `x`.

→ `X` ←

If I am at any idx here then I am told to move right for ans

Here, the check fn should direct to the left

1. Find index of smallest element (`i`)
2. `[i → n]` : increasing array
3. `[0 → i-1]` : increasing

individual B.S

```
int helper1(vector<int>&a)
{
    int low=0,high=a.size()-1,ans=0;
    while(low<=high)
    {
        int mid=(low+high)>>1;
        if(a[mid]>=a[0])low=mid+1;
        else
        {
            ans=mid;
            high=mid-1;
        }
    }
    return ans;
}

int binary_search(int l, int r,vector<int>&a,int t)
{
    int low=l,high=r;
    while(low<=high)
    {
        int mid=(low+high)>>1;
        if(a[mid]==t)return mid;
        if(a[mid]>t)high=mid-1;
        else low=mid+1;
    }
    return -1;
}

int search(vector<int>& nums, int target) {
    int smallest=helper1(nums);
    int ans1=binary_search(0,smallest-1,nums,target);
    int ans2=binary_search(smallest,nums.size()-1,nums,target);
    if(ans1!=-1)return ans1;
    if(ans2!=-1)return ans2;
    return -1;
}
```

## Ques 2. Strange Number

<https://www.codechef.com/APRIL20B/problems/STRNO>

When Varsha was travelling home, she saw a mysterious villa. Varsha is curious about this strange villa and wants to explore it. When she reached the entry gate, the guard gave her a problem to solve and said that he would allow her to enter the villa only if she solved it.

The guard gave Varsha two integers `X` and `K`. Varsha needs to determine whether there is an integer `A` such that it has exactly `X` positive integer divisors and exactly `K` of them are prime numbers.

Varsha found this problem really hard to solve. Can you help her?

Suppose we have a number, i.e.,  $p_1^{\alpha_1} p_2^{\alpha_2} p_3^{\alpha_3} p_4^{\alpha_4} = A$

We know that,

$$(\alpha_1 + 1)(\alpha_2 + 1)(\alpha_3 + 1)(\alpha_4 + 1) = X$$

If we somehow make the above four different values and if  $K=4$

then our answer will be yes otherwise

No. (like for  $K=3, 5$ ).

→ Suppose  $x=20$

So, how can we write 20:



$$2 * 10 = x \quad \text{--- ①}$$

$$2 * 5 * 2 = x \quad \text{--- ②}$$

x can be written in 2 diff ways  
so can we say that in ①,  
 $x = 2 * 10$

$$= (1+1) * (9+1) \quad \text{--- ③}$$

So if we have 2 prime numbers  
 $p_1^{\alpha_1} p_2^{\alpha_2} = A$  and I have such  
values of  $\alpha_1, \alpha_2$  such that  
 $(\alpha_1 + 1) * (\alpha_2 + 1) = x$

Comparing this with ③  
we can say that there will  
some prime numbers whose  
value will be 1, 9 which will  
be equal to some A  
 $A = p_1^1 p_2^9$

Now,

$$\rightarrow x = 20$$

$$= 2 * 2 * 5 \quad (\text{Most Broken})$$

$$= (1+1) * (1+1) * (4+1)$$

$$A = p_1^1 p_2^1 p_3^4$$

If  $x=20, k=3$ , then answer = Yes.

$\rightarrow$  If  $k=2$ , then we won't have  
to look for most broken form  
but simply can use  $2 * 10$  or  $4 * 5$ .

```
ostream& operator<<(ostream& os)
void solve()
{
    int x, k;
    cin >> x >> k;
    map<int, int> mp;
    int i = 2;
    int xx = x;
    int mx = 0;
    while (i <= x)
    {
        while (x % i == 0)
        {
            x /= i;
            mx++;
        }
        i++;
    }
    if (mx < k) cout << "no\n";
    else cout << "yes";
    cout << endl;
}
```