

# DOUBT SESSION

## Ques 1. Search in Rotated Sorted Array

<https://leetcode.com/problems/search-in-rotated-sorted-array/>

There is an integer array `nums` sorted in ascending order (with **distinct** values).

Prior to being passed to your function, `nums` is **possibly left rotated** at an unknown index `k` ( $1 \leq k < \text{nums.length}$ ) such that the resulting array is `[nums[k], nums[k+1], \dots, nums[n-1], nums[0], nums[1], \dots, nums[k-1]]` (**0-indexed**). For example, `[0, 1, 2, 4, 5, 6, 7]` might be left rotated by `3` indices and become `[4, 5, 6, 7, 0, 1, 2]`.

Given the array `nums` after the possible rotation and an integer `target`, return the `index of target` if it is in `nums`, or `-1` if it is not in `nums`.

You must write an algorithm with  $O(\log n)$  runtime complexity.

Example :

$[1 \ 2 \ 3 \ 4 \ 5]$   
↓ Rotate

$[2 \ 3 \ 4 \ 5 \ 1]$   
↓  
 $\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ 3 & 4 & 5 & 1 & 2 \end{matrix}$

If `target = 5` in the final rotated array then we will return the index of 5. [Ans = 2]

The Brute Force solution can be easily solved in linear time,  $O(N)$ .

Approach for optimised solution using Binary Search :

Given a  $X$ , we have to design a check function such that :

Partitioning Space around  $X$ .

$\xrightarrow{\hspace{1cm}}$   $X$   $\xleftarrow{\hspace{1cm}}$

If I am at any idx here then I am told to move right for ans

Here, the check fn should direct to the left

1. Find index of smallest element ( $i$ )
  2.  $[i \rightarrow n]$  : increasing array
  3.  $[0 \rightarrow i-1]$  : increasing
- individual B.S

```

int helper1(vector<int>&a)
{
    int low=0,high=a.size()-1,ans=-1;
    while(low<=high)
    {
        int mid=(low+high)>>1;
        if(a[mid]>=a[0]) low=mid+1;
        else
        {
            ans=mid;
            high=mid-1;
        }
    }
    return ans;
}
int binary_search(int l, int r,vector<int>&a,int t)
{
    int low=l,high=r;
    while(low<=high)
    {
        int mid=(low+high)>>1;
        if(a[mid]==t) return mid;
        if(a[mid]>t) high=mid-1;
        else low=mid+1;
    }
    return -1;
}
int search(vector<int>& nums, int target) {
    int smallest=helper1(nums);
    int ans1=binary_search(0,smallest-1,nums,target);
    int ans2=binary_search(smallest,nums.size()-1,nums,target);
    if(ans1!=-1) return ans1;
    if(ans2!=-1) return ans2;
    return -1;
}

```

## Ques 2. Strange Number

<https://www.codechef.com/APRIL20B/problems/STRNO>

When Varsha was travelling home, she saw a mysterious villa. Varsha is curious about this strange villa and wants to explore it. When she reached the entry gate, the guard gave her a problem to solve and said that he would allow her to enter the villa only if she solved it.

The guard gave Varsha two integers  $X$  and  $K$ . Varsha needs to determine whether there is an integer  $A$  such that it has exactly  $X$  positive integer divisors and exactly  $K$  of them are prime numbers.

Varsha found this problem really hard to solve. Can you help her?

Suppose we have a number, i.e,

$$p_1^{\alpha_1} p_2^{\alpha_2} p_3^{\alpha_3} p_4^{\alpha_4} = A$$

We know that,

$$(\alpha_1+1)(\alpha_2+1)(\alpha_3+1)(\alpha_4+1) = X$$

If we somehow make the above four different values and if  $K=4$  then our answer will be yes otherwise

No. (like for  $K=3, 5$ )

→ Suppose  $X=20$

So, how can we write 20?



$$2^{10} = x \quad \text{--- (1)}$$

$$2^5 \cdot 2 = x \quad \text{--- (2)}$$

$x$  can be written in 2 diff ways  
so can we say that in (1),

$$x = 2^{10} \\ = (1+1) * (9+1) \quad \text{--- (3)}$$

So if we have 2 prime numbers  $P_1^{\alpha_1} P_2^{\alpha_2} = A$  and I have such values of  $\alpha_1, \alpha_2$  such that  $(\alpha_1+1) * (\alpha_2+1) = x$

Comparing this with (3)  
we can say that there will be some prime number whose value will be 1, 9 which will be equal to some  $A$

$$A = P_1^1 P_2^9$$

Now,

$$\rightarrow x = 20$$

$$= 2^2 \cdot 5 \quad (\text{Most Broken})$$

$$= (1+1) * (1+1) * (4+1)$$

$$A = P_1^1 P_2^1 P_3^4$$

If  $x=20, k=3$ , then answer = Yes.

$\rightarrow$  If  $k=2$ , then we won't have to look for most broken form but simply can use  $2^{10}$  or  $4 \cdot 5$ .

```
ostream& operator<<(ostream& os)
void solve()
{
    int x, k;
    cin >> x >> k;
    map<int, int> mp;
    int i = 2;
    int xx = x;
    int mx = 0;
    while (i <= x)
    {
        while (x % i == 0)
        {
            x /= i;
            mx++;
        }
        i++;
    }
    if (mx < k) cout << "no\n";
    else cout << "yes";
    cout << endl;
}
```