

## Backtracking

## Mixed Drill

Framework : L C C M D

A func<sup>n</sup> calling itself

Rec / Backtracking using recursion

implmenting built-in functions

[Brute Force]

Explore everything valid

- Q: Given  $N \times N$  board. You have to place each knight in each row such that no two knights attack each other.

Abt :-

for ( $k_1 = 0$ ;  $k_1 < n$ ;  $k_1++$ )

    for ( $k_2 = 0$ ;  $k_2 < n$ ;  $k_2++$ )

        for ( $k_3 = 0$ ;  $k_3 < n$ ;  $k_3++$ )

            if  $\left[ \begin{array}{l} \text{abs}(k_1 - k_2) \neq 2 \& \& \\ \text{abs}(k_1 - k_3) \neq 1 \& \& \text{abs}(k_2 - k_3) \neq 2 \end{array} \right]$

                valid configuration.

inc  $n \rightarrow$  so inc loops too.

Variably nest loops  $\rightarrow$  can be done by using backtracking.

It is nothing but a variable

size nesting of for loops as required.

• 5 things to decide whenever you are writing Backtracking Problem

$\rightarrow$  level  $\rightarrow$  places where you need to decide  $\rightarrow$  per row where would be the knight

$\rightarrow$  choice  $\rightarrow$  choices are the place you are deciding  $\rightarrow$  which column for this row

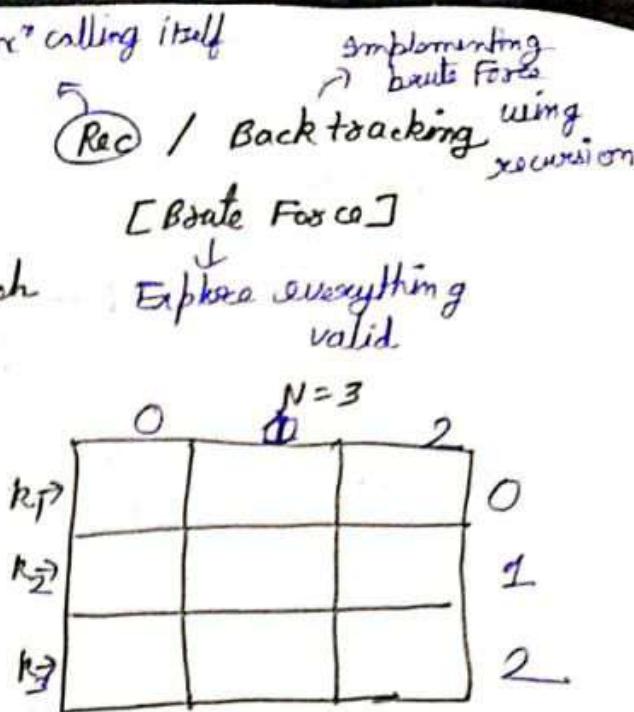
$\rightarrow$  check  $\rightarrow$  if that is even valid  $\rightarrow$  No 2 knights attack

make the choice

Move  $\rightarrow$  Place knight, recurse & revert  $\rightarrow$  Place knight

Decide (because)  $\rightarrow$  • correctness check  
• print/collect/count  
• return

$\rightarrow$  point all configurations



$\text{choice} = [0, 1, 2]$

	0	1	2
→ 0	k	-	-
→ 1	R		
→ 2	R		

~~rec (row)~~  
~~for (col: choices)~~  
~~if (check (row, col)) {~~

Decide

For the ~~prev-loop~~, one level loop, the  
 Two level loops are running, for  
 the ~~prev-loop~~, one level loop once that  
 is over when it comes back, the one level  
 loop goes one step forward and goes  
 to the second level loop again

↓  
what Backtracking concept

Pseudocode :-

~~rec (row) → level~~  
~~if (row == N) {~~  
~~print (board);~~  
~~return;~~  
~~}~~  
~~for (col: choices)~~  
~~if (check (row, col)) {~~  
~~board [row] [col] = 'k'~~  
~~rec (row + 1);~~  
~~board [row] [col] = ' ';~~  
~~}~~

```
int n;
char board[15][15];
void reset(){
    for(int i=0;i<n;i++){
        for(int j=0;j<n;j++){
            board[i][j]=' ';
        }
    }
}
void printer(){
    for(int i=0;i<n;i++){
        for(int j=0;j<n;j++){
            cout<<board[i][j];
        }
        cout<<endl;
    }
    cout<<endl;
}
```

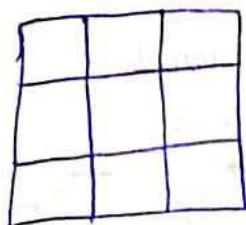
```
bool inside(int row,int col){
    if(row<n&&col<n&&row>=0&&col>=0) return 1;
    return 0;
}
int dx[]={-1,-2,-2,-1};
int dy[]={-2,-1,1,2};

int can_place(int row,int col){
    for(int k=0;k<4;k++){
        if(inside(row+dx[k],col+dy[k]) && board[row+dx[k]][col+dy[k]]=='K'){
            return 0;
        }
    }
    return 1;
}
```

```
// L - Level
void rec(int level){
    cout<<level<<endl;
    printer();
    // D - Decide
    if(level==n){
        return;
    }
    // C - Choices
    for(int col=0;col<n;col++){
        // C - Check
        if(can_place(level,col)){
            // M - Move
            // placing
            board[level][col]='K';
            // recurse.
            rec(level+1);
            // revert
            board[level][col]='.';
        }
    }
}
```

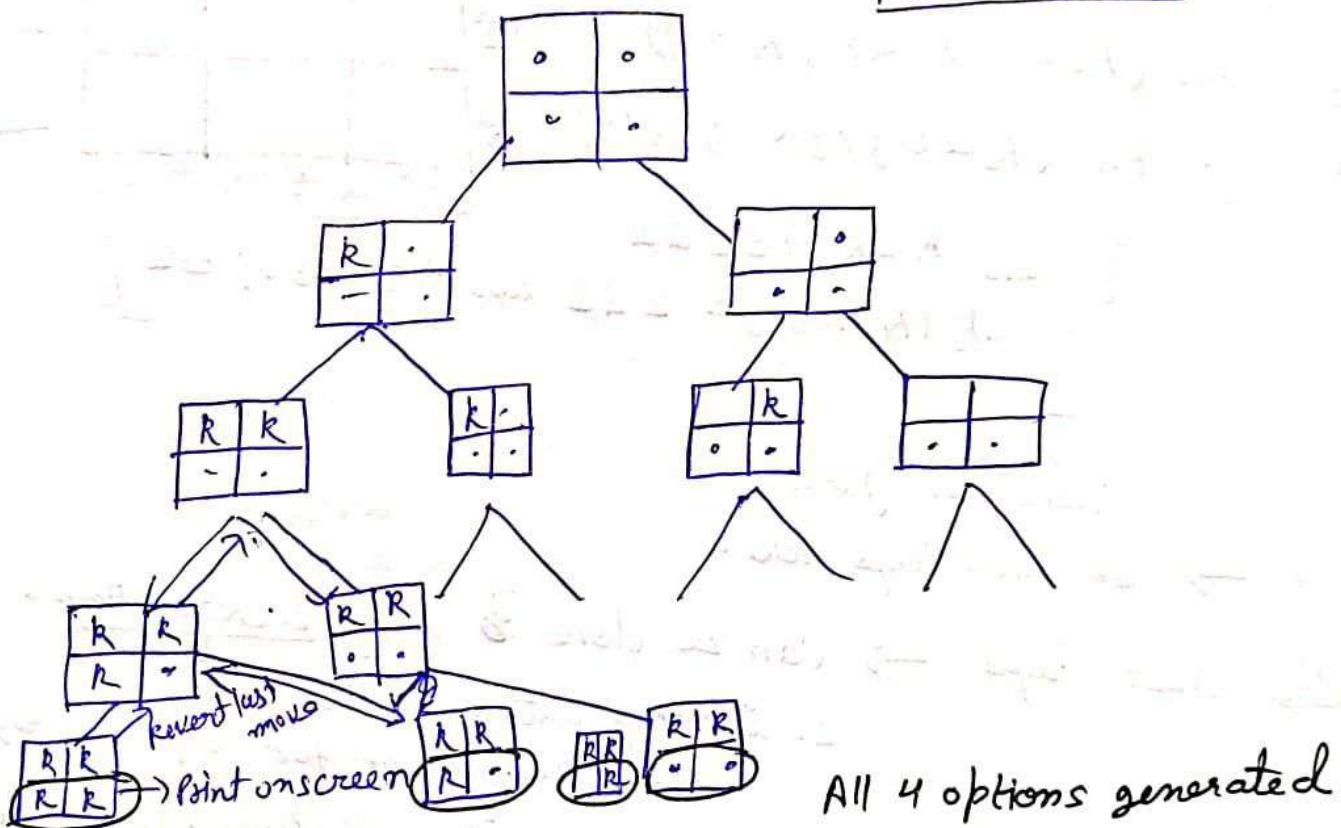
```
void solve(){
    cin>>n;
    rec(0);
}
```

Q: Any cells can have knight or not. Generate all poss configurations where no two knights are attacking each other.



level → cell  
 choice → Place a knight or not ( $2^{N^2}$ )  
 check → check safe  
 Moves → Place, exchange, revert  
 Decide → ✅

Recursion Tree



```
#include<bits/stdc++.h>
using namespace std;

int n;
// DS to store configuration.
char board[15][15];
void reset(){
    for(int i=0;i<n;i++){
        for(int j=0;j<n;j++){
            board[i][j]='.';
        }
    }
}
void printer(){
    for(int i=0;i<n;i++){
        for(int j=0;j<n;j++){
            cout<<board[i][j];
        }
        cout<<endl;
    }
    cout<<endl;
}

bool inside(int row,int col){
    if(row<n&&col<n&&row>=0&&col>=0) return 1;
    return 0;
}
int dx[]={-1,-2,-2,-1};
int dy[]={-2,-1,1,2};

int can_place(int row,int col){
    for(int k=0;k<4;k++){
        if(inside(row+dx[k],col+dy[k]) && board[row+dx[k]][col+dy[k]]=='K'){
            return 0;
        }
    }
    return 1;
}
```

```

// L - Level
void rec(int row,int col){
    // D - Decide
    if(row==n){
        printer();
        return;
    }
    // C - Choices
    // Place
    {
        // C - Check
        if(can_place(row,col)){
            // M - Move
            // placing
            board[row][col]='K';
            // recurse.
            if(col==n-1)rec(row+1,0);
            else rec(row,col+1);
            // revert
            board[row][col]='.';
        }
    }
    // Don't Place
    {
        // M - Move
        // recurse.
        if(col==n-1)rec(row+1,0);
        else rec(row,col+1);
    }
}

void solve(){
    cin>>n;
    reset();
    rec(0,0);
}

```

~~Q.~~  $\text{Arr} \rightarrow [3 \ 2 \ 5]$

Print all permutations of array.

① All elements are distinct

② There can be repeats

① Data structure

Brute Force :-

(By loops)

② LCM &

$[0 \ 0 \ 1 \ 2]$

Level  $\rightarrow$  self index

0  $\rightarrow$  for (int o = ...)

choice  $\rightarrow$  which original

1  $\rightarrow$  for (ind = 1 ...)

Mark check  $\rightarrow$  already taken

2  $\rightarrow$  for (ind 2 ...)

Move  $\rightarrow$  Place, exec, revert

[ind i != idj]

Decide  $\rightarrow$  Print

```

#include<bits/stdc++.h>
using namespace std;

int n;
// DS to store configuration.
int arr[15];
int perm[15];

map<int,int> freq;

// L - Level
void rec(int idx){
    // decide
    if(idx==n){
        for(int i=0;i<n;i++)cout<<perm[i]<<" ";
        cout<<endl;
        return;
    }
    // C
    auto temp = freq;
    for(auto v:temp){
        // Check
        if(v.second>0){
            // Move
            freq[v.first]--;
            perm[idx]=v.first;

            rec(idx+1);

            perm[idx]=-1;
            freq[v.first]++;
        }
    }
}
void solve(){
    cin>>n;
    for(int i=0;i<n;i++){
        cin>>arr[i];
        freq[arr[i]]++;
    }

    rec(0);
}

```