

- N.W: Find count of # of subarray with # of distinct ele == k .
- ① Find count of # of subarray with # of distinct element  $\geq k$  .
  - ② Find sum of length of all subarray with # of distinct element  $\geq k$  .

① Hint :-

Let  $F(\text{arr}, k)$  : No. of subarray with  $\leq k$  distinct elements .

$F(\text{arr}, k-1)$  : No. of subarray with  $\leq (k-1)$  distinct elements .

Count of subarrays with exactly  $k$  distinct elements

$$\Rightarrow F(\text{arr}, k) - F(\text{arr}, k-1)$$

Variation : Find the max length of a subarray with exactly  $k$  distinct elements .

→ similar to Type 1 Form of pointer q2 .

→ Before taking max length , check if freq == distinct -

```
while(tail<n){  
    while(head+1<n && check(arr[head+1])<=k)  
    {  
        head++;  
        // insert head.  
        insert(arr[head]);  
    }  
    // update answer  
    if(distinct==k)  
        ans = max(ans, head-tail+1);  
  
    // remove element from tail  
    if(tail<=head){  
        // remove from DS.  
        erase(arr[tail]);  
        tail++;  
    }else{  
        tail++;  
        head = tail-1;  
    }  
}
```

Test Case 1

Input

Enter input

Output

Click on Run to

Desired Output (Optimal)

Enter desired output

Test Case 2

Input

Enter input

Output

Click on Run to

Add Test Case

② If no. of distinct elements  $> k \rightarrow$  holds for subarray  $(L, R)$   
Then, it does not necessarily hold for  $(L+1, R)$ .

Approach :-

1. Partition the array using two pointers.
2.  $(n-1-\text{head}) =$  No. of subarrays ending after head
3. Count subarrays with  $\leq k$  distinct & subtract from total.

Part 2 : Find the sum of length of these subarrays.

$$\text{len} = \text{tail} - \text{head} + 1$$

$$\text{ans} + = \text{len} \left( \frac{\text{len}+1}{2} \right)$$

Form 2: Two pointers with opp. direction

→ 2sum  
→ 3sum

Q10 Find max value of  $\underbrace{[\min(\text{arr}[i], \text{arr}[j]) * (j-i)]}_{\text{min}}$   $\boxed{0 \leq i < j \leq n}$   $\overbrace{\text{len(gap)}}$

$N = 7$

$\text{arr} = \boxed{3 \ 5 \ 8 \ 3 \ 2 \ 7 \ 1}$

$N \leq 10^5$   
 $\text{arr}[i] \leq 10^9$

Logic :-

- 1) start i at the left end, j at the right end.
- 2) While length dec, inc min to get better result.
- 3) Move pointer with the smaller value.

Leetcode Problem No: 11 → similar

```
int maxArea(vector<int>& height) {  
    int i = 0, j = height.size() - 1, ans = 0;  
    while (i < j) {  
        ans = max(ans, min(height[i], height[j]) * (j - i));  
        if (height[i] < height[j]) i++;  
        else j--;  
    }  
    return ans;  
}
```

Form 3: Is  $S$  a subsequence of  $T$ ?

Exa:  $T = a c d b a c d a b$       ( $\text{size} = N$ )  
 $S = c b a d b$       ( $\text{size} = M$ )

Approach:-

- Two pointers - one for each sequence
- If match - move both pointers.
  - If mismatch - move pointer in  $T$  only.

T.C :  $O(n+m)$

Other Applications of Form 3 :-

1. Merge sort  
→ compare smallest elements from two lists and pick smaller one.
2. Intersection of 2 sorted lists  
→ If same, add to ans and move both.  
→ If different, move ptr of with smaller value.

```
bool isSubsequence(string s, string t) {  
    int i = 0, j = 0;  
    while(i < s.length() && j < t.length()){  
        if(s[i] == t[j]){  
            i++;  
            j++;  
        }else{  
            j++;  
        }  
    }  
    if(i == s.length()) return true;  
    else return false;  
}
```