

July 26, 2025

Doubt Session

Ques 1. Diversify the Array

<https://maang.in/problems/Diversify-the-Array-97>

Description

Only K changes can be done!

You have been given an array A. The diversity of the array A is defined as the number of pairs $i, j, i < j$ such that $A_i \neq A_j$.

You want to maximize the diversity of the array. For that, you are allowed to make at most K operations on it, in any of which, you can select a particular element and change its value to any integer in the range 1 to 10^9 , both inclusive. Find out the maximum diversity of the array that you can obtain.

$i < j$

$a[i] \neq a[j]$

→ decrease duplicates and increase diversity.

Ex 1: 123, already 3 different elements resulting in max. diversity

$$\text{So } {}^3C_2 = 3 \underline{\text{Ans}}$$

Ex 2: 1 1 2 2 K=2 changes allowed

$\{1:2, 2:2\}$ we can use this to diversify the array

$$\text{So, } {}^4C_2 = 6 \underline{\text{Ans}}$$

Ex 3: 2 3 3 2 4 4 , K=2

$\{2:2, 3:2, 4:2\}$ Out of 6 elements, convert K elements.

→ Only 3 unique elements

→ We can make 2 out of 3 duplicates into different number to increase diversity

→ Resulting in 5 unique, 1 duplicate.

$$\text{Overall pair } {}^5C_2 = \frac{5 \times 4}{2} = 10 \text{ pairs}$$

4 non equal $\leftarrow \textcircled{5} \rightarrow$ 1 leftover duplicate

This can pair up with the alr. existing duplicate, Hence Ans = $10 + 4 = 14 \underline{\text{Ans}}$

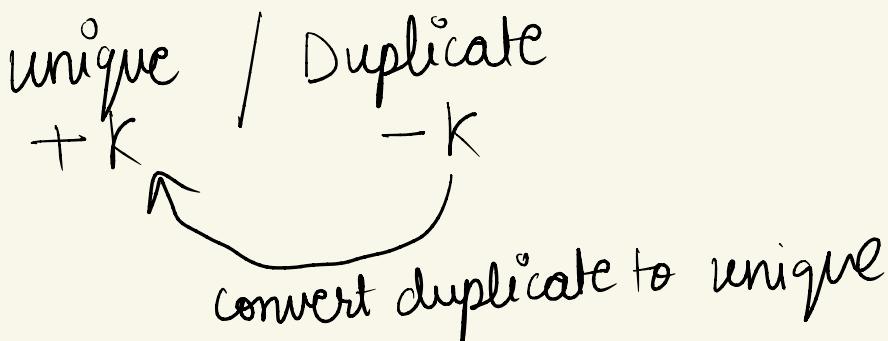


Generalising :

Total el = 18
 1 2 5 3
 ↓ ↓ ↓ ↓
 2 3 6 7

(2,2), (3,3) (4,4) cannot contribute to the diversity → Maximise unique element

Out of K operations, we can decrease K from existing duplicates and add to unique.



$$\Rightarrow {}^n C_2 - d$$

$$\text{Total pair} = {}^{18} C_2$$

K=3

1	2	5	3	4	7	8
↓	↓	↓	↓	↓	↓	↓
2	3	6	7	1	1	1
1	1					

Newly introduced

(just take randomly)

$$(K-1) \binom{K-1}{=3-1} \binom{K-1}{=2-2} \binom{K-1}{=2-2}$$

Instead of reducing each duplicate, we can reduce the duplicate all at once too like

1	2	5	3	4
↓	↓	↓	↓	↑
2	3	6	7	3

Subtracted from most occurring (increases diversity most)

Now,

$$\text{Ans} = {}^{18} C_2 - {}^2 C_2 - {}^3 C_2 - {}^4 C_2 - {}^6 C_2$$

Subtracting the duplicate pairs from total number of pair

- Maintain priority queue of pairs for maintaining frequency.
 $\text{pq_top}()$ → second will give us access to the most occurring element which has highest frequency.
- Reduce this freq by $\text{freq} - k$
- If we still have k left, continue to remove for other pairs.

Ques 2. Height of N soldiers

<https://maang.in/problems/Height-of-Soldiers-88>

There are N soldiers standing in a row, numbered 1 through N . The height of i -th soldier is H_i . For each non-empty contiguous segment of the line, strength is defined as the minimum height of the soldier in that segment.

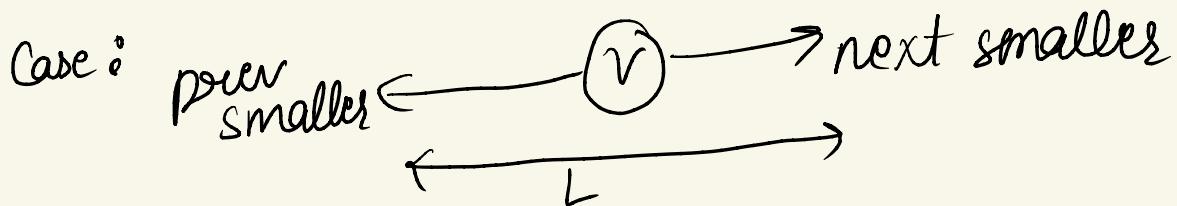
You have to tell the maximum strength for each x size group, for all groups of size x between 1 to N .

Example 1 2 3 4 6 3 2

Imagine
subarray is ending here.

We can try to think like where will 3 contribute as max element.

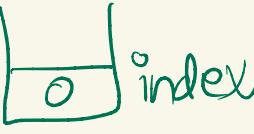
For each element, we can assume that its contributing as max and we will try to figure out no. of subarrays that will have the i -th element as max.



smallest element \circlearrowleft V \circlearrowright of L_3 of $L-13$ of $L-23$ --- 1



Ex1 $O(N)$ 0 1 5 2 3 9 6 5

\rightarrow for 1
 $\{1:1\}$ 

\rightarrow for 5

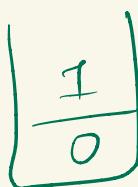
Can 5 replace 1 on stack?

5 can def contribute

to min element of subarray w

size = 1

$\{1:5\}$



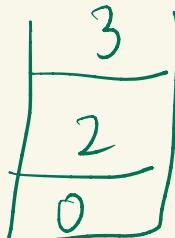
\rightarrow for 2

$\{1:5\} 9$


 pop on comparison with incoming idx
 as 5 > 2.
 pop idx_1 as $5 > 2$.

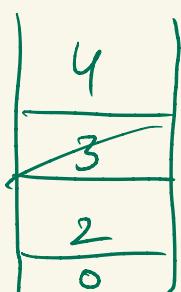
\rightarrow for 9

$\{1:9$
 $2:2\}$



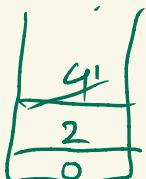
\rightarrow for 6

$\{1:9$
 $2:6$
 $4:2\}$



\rightarrow for 3

$\{1:9, 2:6,$
 $4:2, 3:3\}$
 $5:2\}$

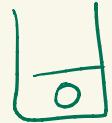


Ex2

2 5 1 3 2

\rightarrow for 2

$\{1:2\}$



\rightarrow for 5

$\{1:2\} 5$

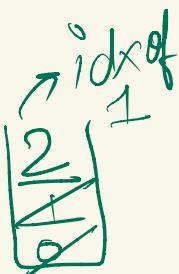


2:2

\rightarrow for 1, $i=2$

$\{1:5$
 $2:2$

$3:1$

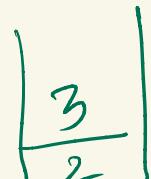


1 is dominating as max when compared with $a[1]$ and $a[0]$.

1 will be min in this window.

\rightarrow for 3

$\{1:5, 2:2,$
 $3:1, 4:1\}$



\rightarrow for 2

$\{1:5, 2:2,$
 $3:1, 4:1, 5:1\}$



2 won't be able to extend till $a[2]$, can only do that till $a[3]$.