

1. D-Enough Array [AtCoder] : Two Pointer Problem



$$\text{ans} = (\# \text{ of subarr } (\text{sum} \leq k))$$
$$\left[ \frac{n(n+1)}{2} - f(k) \right]$$

Ans

Total - smaller than  $k$  through variable window

Pseudocode :-

$\text{sum} = 0, \text{head} = -1, \text{tail} = 0$

while ( $\text{tail} < n$ )

    while ( $(\text{head} + 1 < n) \&& (\text{arr}(\text{head} + 1) + \text{sum}) \leq k$ )

$\text{head}++;$

$\text{sum} += \text{arr}[\text{head}]$

$\text{ans} -= \text{head} - \text{tail} + 1$

    if ( $\text{tail} < \text{head}$ ) {

~~sum -= arr[head]~~

$\text{tail}++;$

}

else {

$\text{tail}++;$

~~sum~~

~~head~~ =  $\text{tail} - 1$

}

2. Hamburgers [Codeforces # - 371C]  
Min/Max → BS / Greedy / DP

$$\begin{array}{c} \text{Ham} \\ \times \text{Burgers} \\ \hline \end{array} \begin{array}{l} (\text{in Burgers } (n_B)) \times P_B \\ (\text{in sausage } (n_s)) \times P_S \\ (\text{in cheese } (n_c)) \times P_C \\ \hline \text{Total} \quad \leq 8 \end{array}$$

```
#include<bits/stdc++.h>
using namespace std;

#define endl '\n'
using lli = long long int;
lli nb_have, ns_have, nc_have;
lli pb_price, ps_price, pc_price;
lli budget;
lli req_b = 0, req_s = 0, req_c = 0;
bool check(lli num_hamburgers) {
    lli total_b_needed = num_hamburgers * req_b;
    lli total_s_needed = num_hamburgers * req_s;
    lli total_c_needed = num_hamburgers * req_c;

    lli buy_b = max(0LL, total_b_needed - nb_have);
    lli buy_s = max(0LL, total_s_needed - ns_have);
    lli buy_c = max(0LL, total_c_needed - nc_have);
    lli total_cost = buy_b * pb_price + buy_s * ps_price + buy_c * pc_price;
    return total_cost <= budget;
}

void solve() {
    string recipe;
    cin >> recipe;
    cin >> nb_have >> ns_have >> nc_have;
    cin >> pb_price >> ps_price >> pc_price;
    cin >> budget;

    for (char c : recipe) {
        if (c == 'B') req_b++;
        else if (c == 'S') req_s++;
        else req_c++;
    }
    lli low = 0;
    lli high = 2e14;
    lli ans = 0;

    while (low <= high) {
        lli mid = low + (high - low) / 2;
        if (check(mid)) {
            ans = mid;
            low = mid + 1;
        } else {
            high = mid - 1;
        }
    }
    cout << ans << endl;
}
```

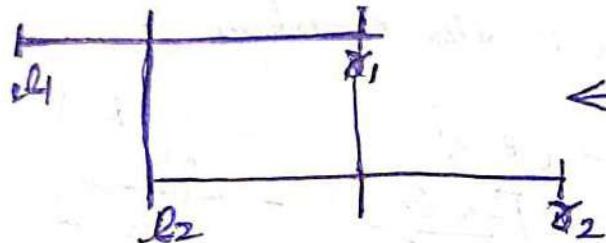
3: The meeting place cannot be changed [Codeforces - 780B]

Binary Search

↳ Binary search on  $\text{Ans}$

$$x - vt \quad v \quad x \quad x + vt$$

$i^{th}$  friend can be anywhere  
in  $[x_i - v_i * t, x_i + v_i * t]$ .



Intersection  
 $\left[ \max(l_1, l_2), \min(r_1, r_2) \right]$

All friends can only meet if the intersection of intervals is non-empty.  
If time  $t$  is enough so any time ( $> t$ ) is also enough. So the predicate  
"can\_meet( $t$ )" is monotonic  $\Rightarrow$  we can do binary search on time.

```
bool check(double time) {
    double max_left_bound = 0.0;
    double min_right_bound = 1e10;

    for (int i = 0; i < n; i++) {
        max_left_bound = max(max_left_bound, (double)x[i] - (double)v[i] * time);
        min_right_bound = min(min_right_bound, (double)x[i] + (double)v[i] * time);
    }

    return max_left_bound <= min_right_bound;
}

void solve() {
    cin >> n;
    x.resize(n);
    v.resize(n);

    for (int i = 0; i < n; i++) cin >> x[i];
    for (int i = 0; i < n; i++) cin >> v[i];

    double low = 0.0;
    double high = 1e9 + 7;

    for(int i = 0; i < 100; i++) {
        double mid = low + (high - low) / 2.0;
        if (check(mid)) {
            high = mid;
        } else {
            low = mid;
        }
    }

    cout << fixed << setprecision(12) << high << endl;
}
```

4. Quiz Master  $\rightarrow$  Two pointers or binary search
1. Sort the students by smartness  $\rightarrow [a_1, a_2, \dots, a_n]$
  2.  $\min \text{smartness} = a[L]$
  3.  $\max \text{ " } = a[R]$
- Goal = minimize the gap ( $a[R] - a[L]$ )
- Sort smartness, then use sliding window to find smallest interval  $[L, R]$  where student covers all topics.