

## Doubt class

### ① Power of 2

M-1:-

1 → 1

2 → 10

4 → 100

8 → 1000

16 → 10000

subtracting 1  
from each →

0 → 0

1 → 1

3 → 11

7 → 111

15 → 1111

Exa:  $4 \& 3 \Rightarrow$

$$\begin{array}{r} 100 \\ 011 \\ \hline 000 \end{array}$$

∴ 4 is a power of 2.

gf  $[n \& (n-1)] == 0 \Rightarrow$  then that particular no is power of 2

→ Powers of 2 have only one '1' in binary.

→ subtracting 1 flips all the bits after that 1.

→ Adding AND-ing them becomes zero.

Exa: 9 & 8

1000

1001

1000

$\Rightarrow \neq 0$

give

∴ Not a power of 2.

T.C: O(1)

```

M-2: while (n%2 == 0)
      m = m/2;

```

$T.C : O(\log N)$

```

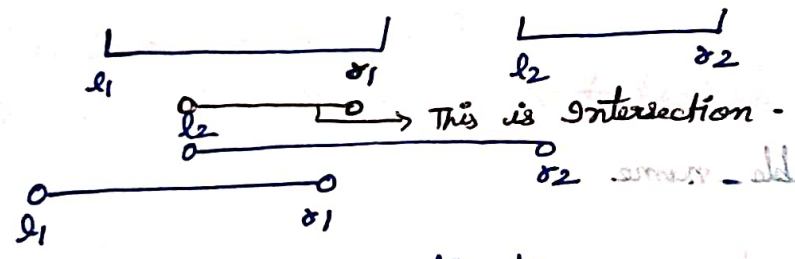
if (n == 1) return 1;
return 0;

```

M-3: if  $((n/2) \% 2 == 0) \rightarrow$  This is wrong approach

M-4: If the binary representation of the number has only one '1', then it is a power of 2.

2. Two Intervals :-



$l_2 = \max(l_1, l_2) \rightarrow$  starting pt  
 $r_1 = \min(r_1, r_2) \rightarrow$  Ending pt

if (starting  $\leq$  ending)  
     intersection exist

else  
     intersection does not exist

3 GCD

M-1: Use in-built STL func<sup>n</sup> :-  $\text{gcd}(a, b)$

M-2: Use Euclidean GCD Algorithm

4 Lucky Numbers :-

$\rightarrow$  A no. consisting only of 4 & 7

Traverse every digit of the no. using modulo 10 and check if the digits are 4 & 7 only and stop if any other no. found.

Code :-

```
int lucky (int x) {  
    while (x) {  
        int digit = x % 10;  
        if (digit != 4 && digit != 7) return 0;  
        x /= 10;  
    }  
    return 1;  
}
```

```
void solve (int a, int b) {  
    int a, b;  
    cin >> a >> b;  
    for (int i = a; i <= b; i++) {  
        if (lucky(i)) {  
            cout << i << " ";  
        }  
    }  
}
```

5. Sum of odd no. b/w X & Y :-

If X is even  $\rightarrow$  start = X + 1  
If X is odd  $\rightarrow$  start = X + 2

Y  $\begin{cases} \rightarrow$  Even  $\rightarrow$  Ending = Y - 1  
 $\rightarrow$  odd  $\rightarrow$  Ending = Y - 2 \end{cases}

$\rightarrow$  start  $\leq$  Ending

$$S_n = \frac{n}{2} (a + l) \rightarrow AP$$

Code :-

```
int x, y;  
cin >> x >> y;  
int starting = min(x, y); ending = max(x, y);  
if (x % 2) starting += 2;  
else starting += 1;  
if (y % 2) ending -= 2;  
else ending -= 1;
```

**T.C :  $O(1)$**



if (starting <= ending) {

int m = ((ending - starting) / 2) + 1;

int ans = (m \* (starting + ending)) / 2;

cout << ans << endl;

}  
else {

cout << 0 << endl;

}

}

6. Three Numbers ; -

$$X + Y + Z = S$$

$$0 \leq x, y, z \leq k$$

$$X + Y = S - Z$$

$$X + Y = T$$

Range of T:  $S - K \leq T \leq S \approx 0 \leq T \leq 2K$

Exa:  $K = 8$

$8 \text{ sol}^n$

$$X + Y = 7$$

- 0 + 7
- 1 + 6
- 2 + 5
- 3 + 4
- 4 + 3
- 5 + 2
- 6 + 1
- 7 + 0

$$X + Y = 3$$

- 0 + 3
- 1 + 2
- 2 + 1
- 3 + 0

$\rightarrow 4 \text{ sol}^n$

$$X + Y = 10$$

- 8 + 2
- 7 + 3
- 6 + 4
- 5 + 5
- 4 + 6
- 3 + 7
- 2 + 8

$\rightarrow 7 \text{ sol}^n$

$$X + Y = 15$$

- 8 + 7
- 7 + 8

$\rightarrow 2 \text{ sol}^n$

sum  $\leq T \leq k$

$\hookrightarrow$  Then we are getting  $T+1 \text{ sol}^n$

When  $\text{sum}(T) > k \Rightarrow$  starting:  $x \leq k$ ,  $\text{diff} = T - k$

No. of  $\text{sol}^n = k - \text{diff} + 1$

Exa:-  $T = 10, k = 8$

$\text{diff} = 10 - 8 = 2$

No. of  $\text{sol}^n = 8 - 2 + 1 = 7$

Code :-

```
void solve () {
```

```
    int k, s;
```

```
    cin >> k >> s;
```

```
    /*
```

```
    x+y+z=s;
```

```
    0 <= s <= 3k
```

```
    x+y = s-z;
```

```
    x+y = T
```

```
    max(0, s-k) <= s-z <= s
```

```
    */
```

```
    int ans = 0;
```

```
    for (int i = max((int)0, s-k); i <= s; i++) {
```

```
        if (i <= k) {
```

```
            ans += i+1;
```

```
        }
```

```
        else if (i <= 2*k) {
```

```
            int d = i-k;
```

```
            ans += (k-d+1);
```

```
        }
```

```
    }
```

```
    cout << ans << endl;
```

```
}
```

T.C :  $O(K)$

7. Another pyramid Problem :-

code :-

```
void solve () {
```

```
    int n;
```

```
    cin >> n;
```

```
    int row = n;
```

```
    int col = (2*n)-1
```

```
    for (int i=1; i <= row; i++) {
```

```
        for (int blank=0; blank < n-i; blank++) {
```

```
            cout << " "; }
```

```
        for (int num=1; num <= i; num++) cout << num << " ";
```

```
        for (int num=i-1; num >= 1; num--) cout << num << " ";
```

```
        for (int blank=0; blank < n-i; blank++) {
```

```
            cout << " "; }
```

```
        cout << endl;
```

row = n

col =  $(2 * n) - 1$

space to print for every row =  $n - i$