

Backtracking Mixed Drill

Framework: L C C M D

A func calling itself

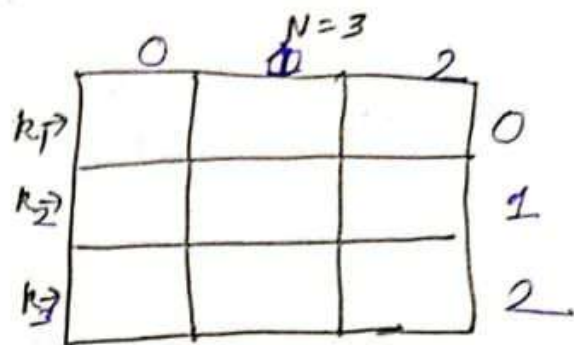
Implementing brute force

Rec / Backtracking using recursion

[Brute Force]

↓
Explore everything valid

Q: Given $N \times N$ board. You have to place each knight in each row such that no two knights attack each other.



Appd:-
levels of loops.
for ($k_1 = 0; k_1 < n; k_1++$)
for ($k_2 = 0; k_2 < n; k_2++$)
for ($k_3 = 0; k_3 < n; k_3++$)

if $\left[\begin{array}{l} \text{abs}(k_1 - k_2) \neq 2 \ \&\& \\ \text{abs}(k_1 - k_3) \neq 1 \ \&\& \text{abs}(k_2 - k_3) \neq 2 \end{array} \right]$

valid configuration.

inc n \rightarrow so inc loops too.

variably nest loops \rightarrow can be done to using backtracking.

It is nthing but a variable size nesting of for loops as required.

• 5 things to decide whenever you are writing Backtracking Problem

\rightarrow level \rightarrow Places where you need to decide \rightarrow per row where would be the knight.

\rightarrow choice \rightarrow choices are the place you are deciding \rightarrow which column for this row

\rightarrow check \rightarrow No if that is even valid \rightarrow No 2 knights attack

Move \rightarrow make the choice Place knight, recurse & revert \rightarrow Place knight

Decide (base case) \rightarrow • correctness check \rightarrow print all configuration
• print/collect/count
• return

choice = [0, 1, 2]

	0	1	2
→ 0	k	-	-
→ 1	k		
→ 2	k		

rec (row)
~~for (col: choices)~~
~~if (check (row, col)) {~~

For the prev. loop, one level loop, the two level loops are summing, for the prev loop, one level loop once that is over when it comes back, the one level loop goes one step forward and goes to the second level loop again.

↓
Backtracking concept

Pseudocode :-

rec (row) → level
 if (row == N) {
 print (board);
 return;
 }
 for (col: choices)
 if (check (row, col)) {
 board [row] [col] = 'k'
 rec (row + 1);
 board [row] [col] = ' ';
 }
 }
 Move →

```
int n;  
char board[15][15];  
void reset(){  
    for(int i=0;i<n;i++){  
        for(int j=0;j<n;j++){  
            board[i][j]=' '  
        }  
    }  
}  
void printer(){  
    for(int i=0;i<n;i++){  
        for(int j=0;j<n;j++){  
            cout<<board[i][j];  
        }  
        cout<<endl;  
    }  
    cout<<endl;  
}
```

```
bool inside(int row,int col){
    if(row<n&&col<n&&row>=0&&col>=0)return 1;
    return 0;
}
int dx[]={-1,-2,-2,-1};
int dy[]={-2,-1,1,2};

int can_place(int row,int col){
    for(int k=0;k<4;k++){
        if(inside(row+dx[k],col+dy[k]) && board[row+dx[k]][col+dy[k]]=='K'){
            return 0;
        }
    }
    return 1;
}
```

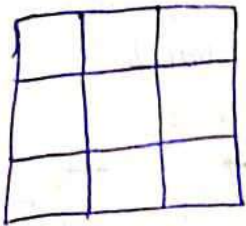
```

// L - Level
void rec(int level){
    cout<<level<<endl;
    printer();
    // D - Decide
    if(level==n){
        return;
    }
    // C - Choices
    for(int col=0;col<n;col++){
        // C - Check
        if(can_place(level,col)){
            // M - Move
            // placing
            board[level][col]='K';
            // recurse.
            rec(level+1);
            // revert
            board[level][col]='.';
        }
    }
}

```

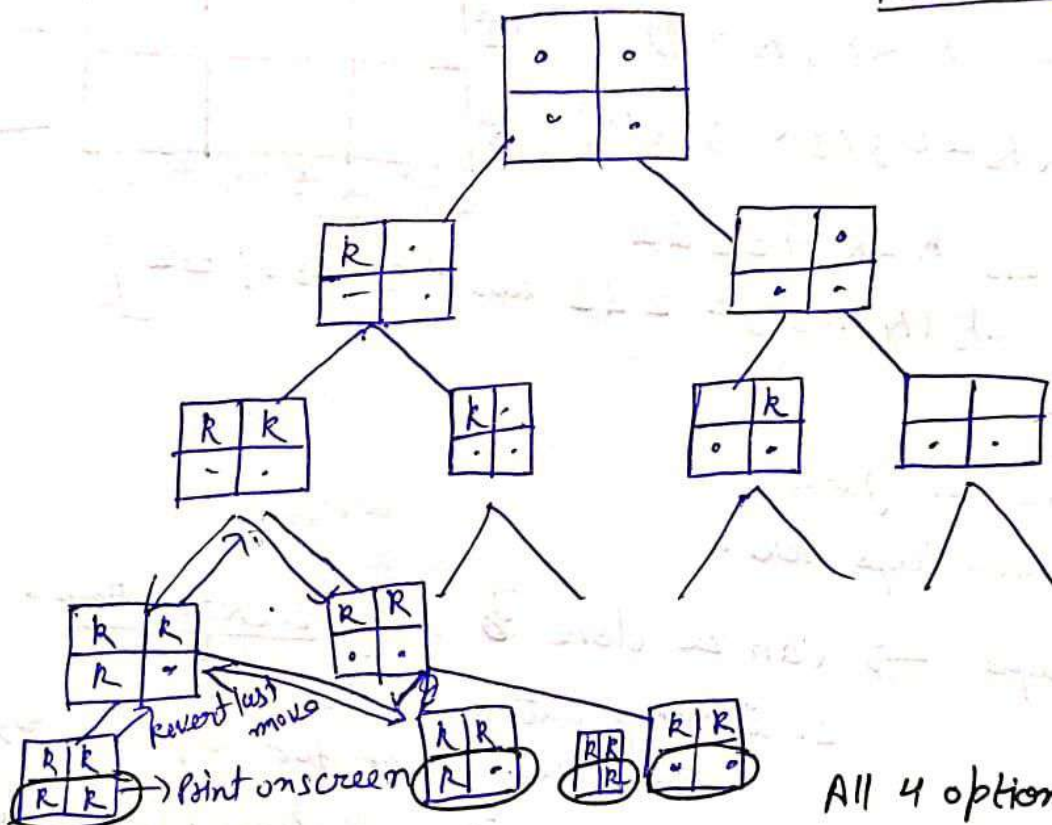
```
void solve(){  
    cin>>n;  
    rec(0);  
}
```


Q. Any cells can have knight or not. Generate all psbl configurations where no two knights are attacking each other.



level \rightarrow cell
 choice \rightarrow Place a knight or not (2^{N^2}) cells
 check \rightarrow check safe per square two choices
 Moves \rightarrow Place, recurse, revert
 Decide \rightarrow ✓

Recursion Tree



All 4 options generated

```

#include<bits/stdc++.h>
using namespace std;

int n;
// DS to store configuration.
char board[15][15];
void reset(){
    for(int i=0;i<n;i++){
        for(int j=0;j<n;j++){
            board[i][j]='.';
        }
    }
}
void printer(){
    for(int i=0;i<n;i++){
        for(int j=0;j<n;j++){
            cout<<board[i][j];
        }
        cout<<endl;
    }
    cout<<endl;
}

bool inside(int row,int col){
    if(row<n&&col<n&&row>=0&&col>=0)return 1;
    return 0;
}
int dx[]={-1,-2,-2,-1};
int dy[]={-2,-1,1,2};

int can_place(int row,int col){
    for(int k=0;k<4;k++){
        if(inside(row+dx[k],col+dy[k]) && board[row+dx[k]][col+dy[k]]=='K'){
            return 0;
        }
    }
    return 1;
}

```



```

// L - Level
void rec(int row,int col){
    // D - Decide
    if(row==n){
        printer();
        return;
    }
    // C - Choices
    // Place
    {
        // C - Check
        if(can_place(row,col)){
            // M - Move
            // placing
            board[row][col]='K';
            // recurse.
            if(col==n-1)rec(row+1,0);
            else rec(row,col+1);
            // revert
            board[row][col]='.';
        }
    }
    // Don't Place
    {
        // M - Move
        // recurse.
        if(col==n-1)rec(row+1,0);
        else rec(row,col+1);
    }
}

void solve(){
    cin>>n;
    reset();
    rec(0,0);
}

```

Q. Arr $\rightarrow [3 \ 2 \ 5]$

Print all permutations of array.

① All elements are distinct

② There can be repeats

Brute Force :-

(By loops)

① Data structure

② LCCMS

$[\underline{0} \ \underline{1} \ \underline{2}]$
0 1 2

Level \rightarrow sub index

choice \rightarrow which original

Move check \rightarrow already taken

Move \rightarrow Places, swap, revert

Decide \rightarrow Print

0 \rightarrow for (ind 0 = ...)

1 \rightarrow for (ind = 1-...)

2 \rightarrow for (ind 2-...)

[ind i \neq idj]

```

#include<bits/stdc++.h>
using namespace std;

int n;
// DS to store configuration.
int arr[15];
int perm[15];

map<int,int> freq;

// L - Level
void rec(int idx){
    // decide
    if(idx==n){
        for(int i=0;i<n;i++)cout<<perm[i]<<" ";
        cout<<endl;
        return;
    }
    // C
    auto temp = freq;
    for(auto v:temp){
        // Check
        if(v.second>0){
            // Move
            freq[v.first]--;
            perm[idx]=v.first;

            rec(idx+1);

            perm[idx]=-1;
            freq[v.first]++;
        }
    }
}

void solve(){
    cin>>n;
    for(int i=0;i<n;i++){
        cin>>arr[i];
        freq[arr[i]]++;
    }

    rec(0);
}

```