

- N.W. ① Find count of # of subarray with # of distinct ele == k.
- ② Find sum of length of all subarray with # of distinct element $\geq k$.

① Hint :-

Let $F(arr, k)$: No. of subarray with $\leq k$ distinct elements.

$F(arr, k-1)$: No. of subarrays with $\leq (k-1)$ distinct elements.

Count of subarrays with exactly k distinct elements

$$\Rightarrow F(arr, k) - F(arr, k-1)$$

Variation : Find the max length of a subarray with exactly k distinct elements.

→ similar to Type 1 Form of pointer q2.

→ Before taking max length, check if freq == distinct.

```

while(tail<n){
    while(head+1<n && check(arr[head+1])<=k)
    {
        head++;
        // insert head.
        insert(arr[head]);
    }
    // update answer
    if(distinct==k)
        ans = max(ans, head-tail+1);

    // remove element from tail
    if(tail<=head){
        // remove from DS.
        erase(arr[tail]);
        tail++;
    }else{
        tail++;
        head = tail-1;
    }
}

```

Test Case 1

Input

Enter input

Output

Click on Run to

Desired Output (Optional)

Enter desired output

Test Case 2

Input

Enter input

Output

Click on Run to

Add Test Case

② If no. of distinct elements $> k \rightarrow$ holds for subarray (L, R)
Then, it does not necessarily hold for $(L+1, R)$.

Approach :-

1. Partition the array using two pointers.
2. $(n-1-\text{head}) = \text{No. of subarrays ending after head}$
3. Count subarrays with $\leq k$ distinct & subtract from total.

Part 2 : Find the sum of length of these subarrays.

$$\text{len} = \text{tail} - \text{head} + 1$$

$$\text{ans} += \text{len} \left(\frac{\text{len} + 1}{2} \right)$$

Form 2: Two pointers with opp. direction

→ 2sum
→ 3sum

Q1: Find max value of $[\min(\text{arr}[i], \text{arr}[j]) * (j-i)]$

$N = 7$

arr =

3	5	8	3	2	7	1
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$0 \leq i < j \leq n$

$N \leq 10^5$
 $\text{arr}[i] \leq 10^9$

Logic :-

- 1) start i at the left end, j at the right end.
- 2) While length dec, inc min to get better result.
- 3) Move pointer with the smaller value.

leetcode Problem NO: 11 \rightarrow similar

```
int maxArea(vector<int>& height) {  
    int i = 0, j = height.size() - 1, ans = 0;  
    while (i < j) {  
        ans = max(ans, min(height[i], height[j]) * (j - i));  
        if (height[i] < height[j]) i++;  
        else j--;  
    }  
    return ans;  
}
```

Form 3: Is S a subsequence of T ?

Exa: $T = a c d b a c d a b$ (size = N)
 $S = c b a d b$ (size = M)

Approach:-

Two pointers - one for each sequence

- If match - move both pointers.
- If mismatch - move pointer in T only.

T.C: $O(n+m)$

Other Applications of Form 3:-

1. Merge sort

→ Compare smallest elements from two lists and pick smaller one.

2. Intersection of 2 sorted lists

→ If same, add to ans and move both.

→ If different, move ptr with smaller value.

```
bool isSubsequence(string s, string t) {  
    int i = 0, j = 0;  
    while(i < s.length() && j < t.length()){  
        if(s[i] == t[j]){  
            i++;  
            j++;  
        }else{  
            j++;  
        }  
    }  
    if(i == s.length()) return true;  
    else return false;  
}
```