

7.4 Logistic Regression - Model Evaluation

Tuesday, 08 November 2022 17:39

| Summary | <ul style="list-style-type: none">Measures to evaluate the performance of the model | | | | | | | | | | | | | | | | | | | | | | | | |
|--|--|-------------|----|-------------|--|-------|--|--|---|---|--|----------|---|----|---|----|---|---|---|----|--|--|----|----|----|
| | <h2>Evaluation of the Model</h2> <p>How do we judge whether this logistic regression model is a good?</p> <ul style="list-style-type: none">Typical statistical indicators: (generally based on the Log-likelihood) – deviance, R^2, and information criteria (Akaike, and Baye's).Some of them have a threshold (often χ^2 based statistic) or sometime it is higher-the-better type (e.g. R^2).Other performance indicators: (generally based on correct identification) – Accuracy, Precision, Recall.Obviously, they are all large-the-better type performance indicators. | | | | | | | | | | | | | | | | | | | | | | | | |
| <ul style="list-style-type: none">What measures do we use in Logistic Regression to evaluate the performance of the model? | <h2>Evaluation of the Model</h2> <ul style="list-style-type: none">Accuracy: Measure of the total number of predictions a model gets right, including both True Positives and True Negatives.Recall: Indicates the percentage of the response values (that we are interested in) were actually captured by the model.Precision: Measures the percentage of the predicted response values (that we are interested in) that were correct. | | | | | | | | | | | | | | | | | | | | | | | | |
| <ul style="list-style-type: none">To understand the formulae better, see 7.6 page. | <h2>Evaluation of the Model</h2> <p>For the student placement example, the response variable was binary (and we were interested in the chances of student getting placed, $Y = 1$).</p> <p>The performance measures can be interpreted as:</p> <ul style="list-style-type: none">Accuracy: The ratio of the number of times predicted and actual Y values matched (for both $Y = 0$ and $Y = 1$) to the total observations in the sample.Recall: The ratio of the number of times the prediction for Y was 1, to the total number of instances in the sample where Y was actually 1.Precision: The ratio of the number of times the actual Y was 1, to the total number of instances where the prediction for Y was 1.For better understanding, refer here.We want these values as large as possible to conclude that the model is good. | | | | | | | | | | | | | | | | | | | | | | | | |
| | <table><tr><td></td><td></td><th colspan="2">Predicted Y</th><th>Total</th></tr><tr><td></td><td></td><th>0</th><th>1</th><td></td></tr><tr><th rowspan="2">Actual Y</th><th>0</th><td>14</td><td>2</td><td>16</td></tr><tr><th>1</th><td>3</td><td>8</td><td>11</td></tr><tr><td></td><td></td><td>17</td><td>10</td><td>27</td></tr></table> | | | Predicted Y | | Total | | | 0 | 1 | | Actual Y | 0 | 14 | 2 | 16 | 1 | 3 | 8 | 11 | | | 17 | 10 | 27 |
| | | Predicted Y | | Total | | | | | | | | | | | | | | | | | | | | | |
| | | 0 | 1 | | | | | | | | | | | | | | | | | | | | | | |
| Actual Y | 0 | 14 | 2 | 16 | | | | | | | | | | | | | | | | | | | | | |
| | 1 | 3 | 8 | 11 | | | | | | | | | | | | | | | | | | | | | |
| | | 17 | 10 | 27 | | | | | | | | | | | | | | | | | | | | | |
| | <p>At Cut off = 0.5, we get these values of the performance indicators:</p> <p>Accuracy 81.48%</p> <p>Recall 72.73%</p> <p>Precision 80.00%</p> | | | | | | | | | | | | | | | | | | | | | | | | |

| | | Predicted Y | | Total |
|----------|---|-------------|----|-------|
| | | 0 | 1 | |
| Actual Y | 0 | 14 | 2 | 16 |
| | 1 | 3 | 8 | 11 |
| | | 17 | 10 | 27 |

$$\text{Accuracy} = \frac{14+8}{27}$$

| | | Predicted Y | | Total |
|----------|---|-------------|----|-------|
| | | 0 | 1 | |
| Actual Y | 0 | 14 | 2 | 16 |
| | 1 | 3 | 8 | 11 |
| | | 17 | 10 | 27 |

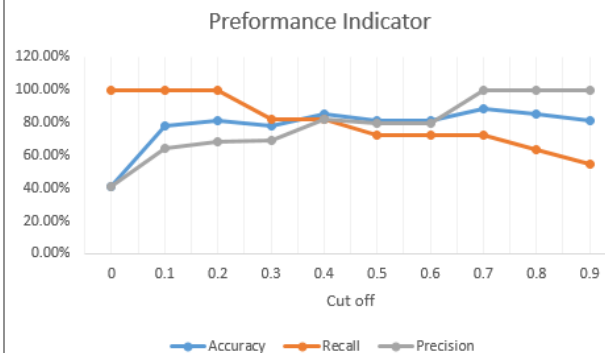
$$\text{Recall} = \frac{8}{11}$$

| | | Predicted Y | | Total |
|----------|---|-------------|----|-------|
| | | 0 | 1 | |
| Actual Y | 0 | 14 | 2 | 16 |
| | 1 | 3 | 8 | 11 |
| | | 17 | 10 | 27 |

$$\text{Precision} = \frac{8}{10}$$

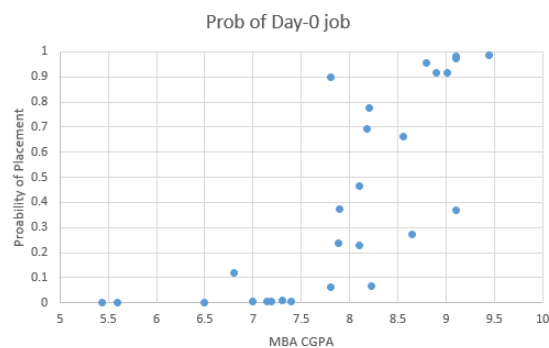
So, to predict the appropriate cut-off, we try different numbers and observe which cut off gives us the best values of the performance indicators

| Cut off | Accuracy | Recall | Precision |
|---------|----------|---------|-----------|
| 0 | 40.74% | 100.00% | 40.74% |
| 0.1 | 77.78% | 100.00% | 64.71% |
| 0.2 | 81.48% | 100.00% | 68.75% |
| 0.3 | 77.78% | 81.82% | 69.23% |
| 0.4 | 85.19% | 81.82% | 81.82% |
| 0.5 | 81.48% | 72.73% | 80.00% |
| 0.6 | 81.48% | 72.73% | 80.00% |
| 0.7 | 88.89% | 72.73% | 100.00% |
| 0.8 | 85.19% | 63.64% | 100.00% |
| 0.9 | 81.48% | 54.55% | 100.00% |



It seems that 0.4 is the best cut-off choice for the given data.

Here probability vs. MBA CGPA graph is plotted.



It tells something I don't have the energy to care about.

Something about since b_1 is some value that's why we're seeing this kind of graph.