



CS 445 – Data Structures – Assignment#4¹

Due: Friday April 13th @ 11:59pm

All source files plus a completed Assignment Information Sheet zipped into a single .zip file and submitted properly to CourseWeb.

Late submission: Sunday April. 15th @ 11:59pm with 10% penalty per late day

OVERVIEW

Purpose: Now that we have looked at Merge Sort and Quick Sort (and discussed a couple Quick Sort variations), we'd like to empirically verify what we have discussed about their relative efficiencies. We will do this by timing the algorithms as well as counting the number of comparisons and data movements of each sort in different situations on different size arrays. We will then tabulate our results and compare the algorithms' performances. We hope to see differences in the relationships between the performance metrics and array sizes for the different algorithms, and possibly come to some conclusions about which versions are best in given situations and overall.

DETAILS

You will test 9 different sorting algorithms:

- 1) QS1: Simple Quick Sort with A[last] as the pivot (in file Quick.java)
- 2) QS2: Median of 3 Quick Sort as given in TextMergeQuick.java (base case array size < 5)
- 3) QS3: Median of 3 Quick Sort as given in TextMergeQuick.java but with base case array size < 20
- 4) QS4: Median of 3 Quick Sort as given in TextMergeQuick.java, but with base case array size < 100
- 5) QS5: Random Pivot Quick Sort with base case array size < 5
- 6) QS6: Iterative Quick Sort developed by converting the recursive Quick Sort into iterative using an explicit stack per the instructions in Notes on converting recursion to iteration [Notes on converting recursion to iteration](#).
- 7) MS1: Recursive Merge Sort as given in TextMergeQuick.java
- 8) MS2: Iterative Merge Sort as given in TextMergeQuick.java

¹ Assignment adapted from Dr. John Ramirez's CS 445 class.

- 9) MS3: Iterative Merge Sort developed by converting the recursive Merge Sort into iterative using an explicit stack per the instructions in Notes on converting recursion to iteration [Notes on converting recursion to iteration](#).

The code for six algorithms (1-4 and 7-8) is already completely written – you only have to change the base case value in the Median of 3 Quick Sort from a constant to a variable so that you can give it different values during your program execution. You **must write** the other three algorithms (5-6 and 9) so that it works correctly. Random Pivot Quick Sort is actually very similar to the simple Quick Sort, except that you choose the pivot index as a random integer between first and last (inclusive) rather than choosing it as A[last].

Your primary task in this assignment is to write a **main program** that will enable the user to time all 9 of the algorithms under different circumstances, and then to tabulate and analyze the resulting data.

INPUT AND VARIABLE SETUP

Your program should allow the following to be input from the user:

- 1) The size of the arrays to be tested.
- 2) The number of trials for each test. The overall performance for the test will be the average of the performance for each of the trials. For random data, each trial should have different numbers in the array, but the data for a given trial should be **the same random data for all 9 algorithms**. In other words, consider, for example, an array called A1, algorithms QS1 and QS2, and trials T1 and T2. If A1 is filled with random numbers for QS1 in trial T1, then those same numbers (in the same initial positions) should be used for QS2 in trial T1. However, different random numbers should be generated for trial T2, again using the same numbers for both QS1 and QS2.
- 3) The name of the file your results will be output to.

For each algorithm your program should iterate through 3 initial setups of the data:

- a) Random – in this case you will fill the arrays with random integers. To make your assessments more accurate, each of your algorithms should utilize the same random data, as mentioned above. This can be accomplished in several ways but you will lose credit if the data is not the same.
- b) Already sorted (low to high) – in this case simply fill the arrays with successive integers starting at 1.
- c) Already reverse sorted (high to low) – in this case simply fill the arrays with decreasing integers starting at the array length.

Timing and Measurement: You will time your algorithms using the predefined method

`System.nanoTime()`

This method returns the time elapsed on the system timer in nanoseconds. You will time one trial in the following fashion:

```

long start = System.nanoTime();

// Execute the sorting method here (array should ALREADY be filled before timing starts)

long finish = System.nanoTime();

long delta = finish – start;

```

Since you are performing multiple trials, for a given algorithm you will add the times for the trials together, then divide by the number of trials to get the average time per trial. You may also want to divide by 1 billion to get your final results in seconds rather than nanoseconds.

You will also need to measure the number of comparisons and the number of data movements of the algorithms. You will need to instrument your code to add performance counters to the sorting algorithms. Every time a comparison is made, you would need to increment a comparison counter. Every time an assignment is made using the array the data moves counter has to be incremented. **You may find the instructions and supplied code for Lab 9 useful in this regard.**

Since you are performing multiple trials, for a given algorithm you will add up the counters for the trials together, then divide by the number of trials to get the average per trial.

OUTPUT

For each of the variations in the run, your program must output its results to the file named by the user. Note that since you have 3 data setups and 9 algorithms, **each overall execution of your main program should produce 27 different results.** Each result should look something like the following example:

```

Algorithm: Simple Quick Sort
Array Size: 25000
Order: Random
Number of trials: 10
Average time: 0.0038441037 sec
Average number of comparisons: 579427.2 comparisons
Average number of data moves: 279606.6 data moves

```

Trace Output Mode: In order for your TA to be able to test the correctness of your sorting algorithms and main program logic, you are required to have a Trace Output Mode for your program. This mode should be automatically set when the Array Size is ≤ 20 . In Trace Output Mode, your program should output all of the following to standard output (i.e., the display) for **EACH** trial of **EACH** algorithm:

```

Algorithm being used

Array Size

```

Data configuration (sorted, reverse sorted, random)

Initial data in array prior to sorting

Data in array after sorting

The evaluation of the correctness of your algorithms and data processing will be heavily based on the Trace Output Mode for your program. If you do not implement this or it does not work correctly, you will likely lose a lot of credit.

Note: Be sure that Trace Output Mode is OFF for arrays larger than 20.

RUNS

The goal is to see how the performance of the algorithms changes as the size of the arrays increases. Use **10 trials** for all of your runs.

Size = 25000, Filename = test25k.txt

Size = 50000, Filename = test50k.txt

Size = 100000, Filename = test100k.txt

Note: Only do the first 3 sizes above for the Simple Quick Sort. Even with these it may take a while for the simple Quick Sort algorithm and you will have to increase the stack size of the JRE to accommodate the execution – see below. For the sizes below you will only have 24 results.

Size = 200000, Filename = test200k.txt

Size = 400000, Filename = test400k.txt

Size = 800000, Filename = test800k.txt

Size = 1600000, Filename = test1600k.txt

Size = 3200000, Filename = test3200k.txt

An example run may appear as shown below:

```
assig4> java -Xss10m Assig4
Enter array size: 25000
Enter number of trials: 10
Enter file name: test25k.txt
```

An example output file is test25k.txt, which you can find on CourseWeb.

RESULTS

After you have finished all of your runs, tabulate your results in an Excel spreadsheet. Use a different worksheet for each initial ordering (random, sorted, reverse sorted). In each worksheet, make three tables (one for time, a second for number of comparisons, and a third for number of data moves) of your results with the array sizes as the columns and the algorithms as the rows. Also make a graph for each of your tables so that you can visualize the growth of the run-time and performance metrics for each algorithm.

You must also **write a brief summary/discussion of your results**. Based on your tables, indicate the best algorithm for each of the initial data orderings. Based on your overall results (for all data orderings), speculate on what you think the best of the 9 algorithms is for general purpose use. Your write-up should be well written and justified by your results. Your write-up can be embedded in your spreadsheet or submitted as a separate document (e.g., a Word document).

SUBMISSION REQUIREMENTS

Submit all of your Java source files, as usual, but **also submit all output files and your Excel file (and Word file)**. As usual, put all of these files into a **single .zip file** for submission. Also, as usual, your program must be able to be compiled and executed on the command line directly from your submission without any IDEs or additional files.

If you cannot get the program working as specified, clearly indicate any changes you made and clearly indicate why, so that the TA can best give you partial credit. You will lose some credit for not getting it to work properly, but getting the main program to work with modifications is better than not getting it to work at all. A template for the Assignment Information Sheet can be found in the assignment's CourseWeb folder. You do not have to use this template but your sheet should contain the same information.

ADDITIONAL REQUIREMENTS, HINTS AND HELP

- For help with generating random integers, see the Random class in the Java API and specifically the nextInt() method.
- To make your results more accurate, **do not run anything else on your machine while you are doing your runs**. Don't worry about system processes that are running – just make sure you don't run any other applications.
- To make your results consistent, **do all of your runs on the same machine under the same (if possible) circumstances**.
- Note that for smaller arrays and in some cases even for larger arrays the time for a given trial may be very small – perhaps even negligible.

- Be sure to time only the actual sorting procedure – do not time loading the data into the array or any I/O, such as printing to the screen or reading from the keyboard; this is very slow and will skew the timing greatly).
- As we discussed, in some cases a recursive algorithm makes so many calls that it uses up all of the memory in the run-time stack, causing the JRE to crash. To prevent this problem we can invoke the Java interpreter with a flag to indicate the size of the run-time stack. This can be done in the following way:

```
prompt> java -Xss<size> MainClassName
```
- You may have to experiment with the value for <size> to avoid getting a `StackOverflowError`, but in my runs using 10M worked. If you think about how these algorithms execute, you will see that we only have to worry about the stack size for the Simple Quick Sort algorithm in the cases of the sorted and reverse sorted data.

Extra CREDIT

- For comparison purposes, add some additional sorting algorithms to your tests to see how they compare. For example, you could include Shellsort or Insertionsort.

RUBRICS

Please check the grading rubric on CourseWeb.