## Farnsworth Knitted Thesis Code

#### 2025-05-03

```
library(readxl)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
library(tidyr)
library(lubridate)
##
## Attaching package: 'lubridate'
## The following objects are masked from 'package:base':
##
       date, intersect, setdiff, union
library(quadprog)
library(ggplot2)
library(knitr)
library(kableExtra)
## Warning in attr(.knitEnv$meta, "knit_meta_id"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
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## See help("Deprecated")
##
## Attaching package: 'kableExtra'
## The following object is masked from 'package:dplyr':
##
       group_rows
library(showtext)
## Loading required package: sysfonts
## Loading required package: showtextdb
library(zoo)
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
library(sysfonts)
library(future)
library(future.apply)
library(patchwork)
library(lmtest)
library(sandwich)
library(gridExtra)
##
## Attaching package: 'gridExtra'
## The following object is masked from 'package:dplyr':
##
```

```
##
       combine
library(grid)
showtext_auto()
font_add_google("Merriweather", "latexfont")
df <- read_xlsx("~/Downloads/FarnsworthCrashData (1).xlsx")</pre>
# CALCULATE ATT
# Format columns
df <- df %>%
 rename_all(tolower) %>%
 mutate(
    month num = match(tolower(month), tolower(month.abb)),
    year = suppressWarnings(as.numeric(year))) %>%
 filter(!is.na(year), !is.na(month_num)) %>%
  mutate(
    date = make_date(year, month_num, 1),
    crash_rate = crashes / vmt)
# Set pre- and post- periods
policy_start <- as.Date("2021-02-01")</pre>
df_pre <- df %>% filter(date < policy_start)</pre>
df_post <- df %>% filter(date >= policy_start)
# Pivot wide in the pre-period to prepare for the matrix minimization problem
df pre wide <- df pre %>%
  select(date, state, crash_rate) %>%
 pivot_wider(names_from = state, values_from = crash_rate, values_fn = sum)
# Set treated versus untreated states
treated state <- "Oregon"</pre>
all_states <- setdiff(colnames(df_pre_wide), "date")</pre>
donor_states <- setdiff(all_states, treated_state)</pre>
# Set y_o as the outcome vector for the treated unit in the pre-period
y_o <- df_pre_wide[[treated_state]]</pre>
\# Set Y_d as the matrix of outcome vectors for donor states in the pre-period
Y_d <- df_pre_wide[, donor_states] %>% as.matrix()
# Define function for synthetic control
scm_fit <- function(y, Y) {</pre>
 Dmat <- 2 * t(Y) %*% Y
 dvec <- 2 * t(Y) %*% y
 Amat <- cbind(rep(1, ncol(Y)), diag(ncol(Y)))
 bvec <- c(1, rep(0, ncol(Y)))</pre>
  sol <- solve.QP(Dmat, dvec, Amat, bvec, meq = meq)</pre>
  sol$solution}
# Minimize the squared error between Oregon and the donor states in the pre-period
w_hat <- scm_fit(y_o, Y_d)</pre>
# Display donor weights
```

```
weights_df <- data.frame(donor = donor_states,</pre>
  weight = round(w_hat, 4)) %>%
  arrange(desc(weight))
  kable(weights_df, caption = "Donor Weights") %>%
  kable_styling(latex_options = c("striped", "hold_position"))
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```
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```

Table 1: Donor Weights

donor	weight
Washington	0.4805
California	0.2593
Wyoming	0.1263
Idaho	0.0660
Colorado	0.0471
Utah	0.0208
Arizona	0.0000
Wisconsin	0.0000
North Carolina	0.0000
South Dakota	0.0000
North Carolina	0.0000

```
# Create synthetic Oregon from donor states and flag post-policy months
df_wide_all <- df %>%
  select(date, state, crash_rate) %>%
 pivot_wider(names_from = state, values_from = crash_rate, values_fn = sum) %>%
 mutate(synthetic = rowSums(across(all_of(donor_states), ~ .x * w_hat[which(donor_states == cur_column
   post = date >= ymd("2020-11-01"))
# Apply scalar correction to match Oregon's level
c <- mean(df_wide_all$Oregon[!df_wide_all$post], na.rm = TRUE) /</pre>
     mean(df_wide_all$synthetic[!df_wide_all$post], na.rm = TRUE)
# Caclulate the estimated difference between Oregon and synthetic control at each time point
df_wide_all <- df_wide_all %>%
 mutate(
    synthetic_scaled = synthetic * c,
    gap = Oregon - synthetic_scaled)
# Compute average treatment gap before and after policy
att_summary <- df_wide_all %>%
  group_by(post) %>%
  summarise(avg_gap = mean(gap, na.rm = TRUE), .groups = "drop")
# Calculate ATT as the post-period average gap minus pre-period average gap
att <- diff(att_summary$avg_gap)</pre>
print(att)
## [1] -0.07996006
# Calculate pre-treatment MSPE
pre_mspe <- df_wide_all %>%
 filter(!post) %>%
  summarise(
   mspe = mean((Oregon - synthetic_scaled)^2, na.rm = TRUE),
   rmse = sqrt(mspe),
```

```
mae = mean(abs(Oregon - synthetic_scaled), na.rm = TRUE))
# Create a table to display the pre-treatment fit metrics
fit_metrics_table <- tibble(</pre>
  Metric = c("Mean Squared Prediction Error (MSPE)",
             "Root Mean Squared Error (RMSE)",
             "Mean Absolute Error (MAE)"),
  Value = c(round(pre mspe$mspe, 6), round(pre mspe$mse, 6), round(pre mspe$mae, 6)))
kable(fit metrics table, caption = "Pre-Treatment Fit Quality Metrics") %>%
kable_styling(latex_options = c("striped", "hold_position"))
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```

Table 2: Pre-Treatment Fit Quality Metrics

Metric	Value
Mean Squared Prediction Error (MSPE)	0.010199
Root Mean Squared Error (RMSE)	0.100990
Mean Absolute Error (MAE)	0.081102

```
# PLACEBO TESTS
# Create storage for placebo ATT estimates
placebo att <- c()
# Loop through each donor state and treat it as if it were "treated"
for (state in donor_states) {
# Construct synthetic control for placebo state
y_placebo <- df_pre_wide[[state]]</pre>
Y_d_placebo <- df_pre_wide[, setdiff(donor_states, state)] %>% as.matrix()
# Estimate weights using earlier function
w_placebo <- tryCatch({</pre>
    scm_fit(y_placebo, Y_d_placebo)
  }, error = function(e) return(NULL))
# Create synthetic control for placebo-treated state
if (!is.null(w_placebo)) {
  synth_placebo <- as.matrix(df_wide_all[, setdiff(donor_states, state)]) %*% w_placebo</pre>
  gap_placebo <- df_wide_all[[state]] - synth_placebo</pre>
 post_period <- df_wide_all$date >= as.Date("2021-02-01")
# Compute placebo ATT and store it
  placebo_ATT <- mean(gap_placebo[post_period], na.rm = TRUE)</pre>
 placebo_att <- c(placebo_att, placebo_ATT)}}</pre>
# Compute p-value by calculating share of placebo ATTs as extreme as Oregon's
placebo_p_value <- mean(abs(placebo_att) >= abs(att))
# Compute standard error using standard deviation of placebo ATTs
se_placebo <- sd(placebo_att, na.rm = TRUE)</pre>
print(placebo_p_value)
```

```
## [1] 0.4
print(se_placebo)
## [1] 0.3554559
# Compute pre- and post-treatment MSPEs for Oregon
oregon pre mspe <- mean((df wide all$Oregon[!df wide all$post] -
                         df_wide_all$synthetic_scaled[!df_wide_all$post])^2, na.rm = TRUE)
oregon_post_mspe <- mean((df_wide_all$Oregon[df_wide_all$post] -</pre>
                          df_wide_all$synthetic_scaled[df_wide_all$post])^2, na.rm = TRUE)
oregon_mspe_ratio <- oregon_post_mspe / oregon_pre_mspe</pre>
# Calculate MSPE ratios for all placebo states
placebo_mspe_ratios <- c()</pre>
placebo_pre_mspes <- c()</pre>
state_names <- c()</pre>
# Repeat synthetic control estimation for each placebo
for (state in donor_states) {
  y_placebo <- df_pre_wide[[state]]</pre>
 Y_d_placebo <- df_pre_wide[, setdiff(donor_states, state)] %>% as.matrix()
  w_placebo <- tryCatch({</pre>
    scm fit(y placebo, Y d placebo)
  }, error = function(e) return(NULL))
  if (!is.null(w_placebo)) {
    synth_placebo <- as.matrix(df_wide_all[, setdiff(donor_states, state)]) %*% w_placebo
# Compute pre- and post-MSPEs
    pre_mspe <- mean((df_wide_all[[state]][!df_wide_all$post] -</pre>
                       synth_placebo[!df_wide_all$post])^2, na.rm = TRUE)
    post_mspe <- mean((df_wide_all[[state]][df_wide_all$post] -</pre>
                        synth_placebo[df_wide_all$post])^2, na.rm = TRUE)
# Store MSPE ratio if valid
    if (pre_mspe > 0) {
      mspe_ratio <- post_mspe / pre_mspe</pre>
      placebo_mspe_ratios <- c(placebo_mspe_ratios, mspe_ratio)</pre>
      placebo_pre_mspes <- c(placebo_pre_mspes, pre_mspe)</pre>
      state names <- c(state names, state)}}}</pre>
# Create MSPE ratio comparison table
mspe_ratio_df <- data.frame(</pre>
 State = c("Oregon", state_names),
  Pre_MSPE = c(oregon_pre_mspe, placebo_pre_mspes),
 MSPE_Ratio = c(oregon_mspe_ratio, placebo_mspe_ratios)) %>%
  arrange(desc(MSPE_Ratio))
# Display MSPE ratio table and Oregon's implied p-value
kable(mspe_ratio_df, caption = "MSPE Ratio Comparison (Post/Pre)") %>%
kable_styling(latex_options = c("striped", "hold_position"))
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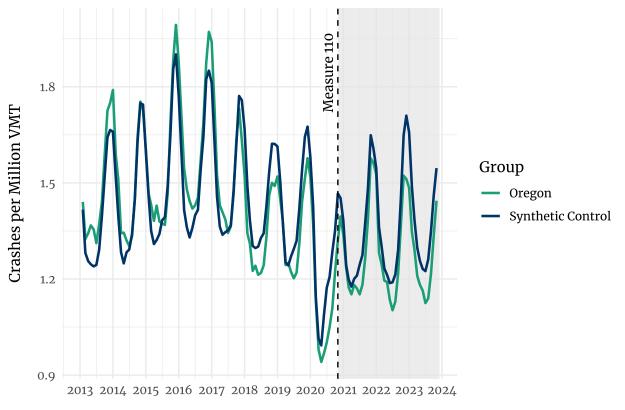
Table 3: MSPE Ratio Comparison (Post/Pre)

State	Pre_MSPE	MSPE_Ratio
North Carolina	0.0526758	4.7819119
Colorado	0.0633336	1.9632051
Wyoming	0.0223791	1.5847923
Oregon	0.0101989	1.0263402
California	0.9557949	1.0042035
Wisconsin	0.0431936	0.9798528
Washington	0.0348025	0.8948216
Idaho	0.0397932	0.8627429
South Dakota	0.0528337	0.8326771
Utah	0.0266501	0.7714646
Arizona	0.0196941	0.6356507

```
# CREATE PLOT
# Prepare plot data by selecting Oregon and synthetic control crash rates, reshaping to long format
df_plot <- df_wide_all %>%
  select(date, Oregon, synthetic_scaled) %>%
  pivot_longer(cols = c("Oregon", "synthetic_scaled"), names_to = "series", values_to = "crash_rate") %
  filter(!is.na(crash_rate)) %>%
  group_by(series) %>%
  mutate(smoothed_rate = zoo::rollmean(crash_rate, k = 3, fill = NA, align = "center")) %>%
  ungroup() %>%
  mutate(series = recode(series, synthetic_scaled = "Synthetic Control"))
# Plot crash rates over time with treatment date and shaded post-treatment region
ggplot(df_plot, aes(x = date, y = smoothed_rate, color = series)) +
  annotate("rect", xmin = as.Date("2020-11-01"), xmax = max(df_plot$date),
           ymin = -Inf, ymax = Inf, fill = "gray90", alpha = 0.7) +
  geom_line(size = 0.9) +
  geom_vline(xintercept = as.Date("2020-11-01"), linetype = "dashed") +
  annotate("text", x = as.Date("2020-11-01"),
           y = max(df_plot$smoothed_rate, na.rm = TRUE),
           label = "Measure 110", angle = 90, vjust = -0.5, hjust = 1.1,
           size = 3.5, family = "latexfont") +
  scale_y_continuous(name = "Crashes per Million VMT") +
  scale_x_date(date_breaks = "1 year", date_labels = "%Y") +
  scale_color_manual(values = c("Oregon" = "#1b9e77", "Synthetic Control" = "#003366")) +
  labs(x = "Year", color = "Group") +
  theme_minimal(base_family = "latexfont") +
   axis.title.x = element text(margin = margin(t = 10)),
   axis.title.y = element_text(margin = margin(r = 10)),
   plot.title = element_text(hjust = 0.5, size = 14, face = "bold")
 )
## Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.
## i Please use `linewidth` instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
```

## generated.

## Warning: Removed 4 rows containing missing values or values outside the scale range
## (`geom\_line()`).



#### Year

```
# Save file to folder
ggsave("images/synthdid_plot_scaled.pdf", width = 8, height = 4, dpi = 300)
```

```
# SENSITIVITY ANALYSIS
# Define donor subsets
subset_list <- list(</pre>
                       = c("Washington", "Idaho", "California"),
  Neighbors
  Exclude_Washington = setdiff(donor_states, "Washington"))
# Prepare storage
subset results <- list()</pre>
weights_by_subset <- list()</pre>
se_by_subset <- list()</pre>
pval_by_subset <- list()</pre>
# Loop over each donor subset
for (label in names(subset_list)) {
  donors_subset <- subset_list[[label]]</pre>
  y_oregon <- df_pre_wide$Oregon</pre>
  Y_subset <- df_pre_wide[, donors_subset] %>% as.matrix()
```

```
w_subset <- tryCatch(scm_fit(y_oregon, Y_subset), error = function(e) NULL)</pre>
  if (is.null(w_subset)) next
# Construct synthetic series and gap
  synth_all <- as.matrix(df_wide_all[, donors_subset]) %*% w_subset</pre>
              <- df_wide_all$Oregon - synth_all</pre>
 post_period <- df_wide_all$date >= as.Date("2020-11-01")
# Compute raw ATT
  ATT_raw <- mean(gap[post_period], na.rm = TRUE)
# compute placebo ATTs for the subset
  placebo ATT subset <- c()</pre>
  for (pseudo_treated in donors_subset) {
    Y_pseudo <- df_pre_wide[, setdiff(donors_subset, pseudo_treated)] %>% as.matrix()
    w_pseudo <- tryCatch(scm_fit(df_pre_wide[[pseudo_treated]], Y_pseudo),</pre>
                          error = function(e) NULL)
    if (is.null(w_pseudo)) next
    synth_pseudo <- as.matrix(df_wide_all[, setdiff(donors_subset, pseudo_treated)]) %*% w_pseudo
    gap_pseudo <- df_wide_all[[pseudo_treated]] - synth_pseudo</pre>
    placebo_ATT_subset <- c(placebo_ATT_subset,</pre>
                             mean(gap_pseudo[post_period], na.rm = TRUE))}
# Correct ATT bias
  bias subset <- mean(placebo ATT subset, na.rm = TRUE)</pre>
  ATT corrected subset <- ATT raw - bias subset
  se_corrected_subset <- sd(placebo_ATT_subset - bias_subset, na.rm = TRUE)</pre>
  pval_corrected_subset <- mean(</pre>
    abs(placebo_ATT_subset - bias_subset) >= abs(ATT_corrected_subset),
    na.rm = TRUE)
# Store results
  subset_results[[label]] <- ATT_corrected_subset</pre>
  weights_by_subset[[label]] <- setNames(round(w_subset, 4), donors_subset)</pre>
  se_by_subset[[label]] <- se_corrected_subset</pre>
  pval_by_subset[[label]] <- pval_corrected_subset}</pre>
# Combine into tables
subset_df <- tibble(</pre>
  Subset
            = names(subset results),
 ATT_Estimate = unlist(subset_results),
Std_Error = unlist(se_by_subset),
  Empirical_p_value= unlist(pval_by_subset))
weight_long <- bind_rows(</pre>
  lapply(names(weights_by_subset), function(label) {
   tibble(
      Subset = label,
      Donor = names(weights_by_subset[[label]]),
      Weight = weights_by_subset[[label]])}))
# Display
kable(subset_df, caption = "Bias-Corrected Sensitivity Analysis by Donor Subset") %>%
```

## kable\_styling("striped", "hold\_position")

```
## Warning in attr(x, "align"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
## See help("Deprecated")
## Warning in attr(.knitEnv$meta, "knit_meta_id"): 'xfun::attr()' is deprecated.
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## See help("Deprecated")
## Warning in attr(x, "align"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
## See help("Deprecated")
## Warning in attr(x, "format"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
```

#### ## See help("Deprecated")

Table 4: Bias-Corrected Sensitivity Analysis by Donor Subset

Subset	ATT_Estimate	Std_Error	Empirical_p_value
Neighbors	0.0978369	0.6871422	1
${\bf Exclude\_Washington}$	0.0120047	0.3828464	1

```
kable(weight_long, caption = "Donor Weights by Subset") %>%
  kable_styling("striped", "hold_position")
```

```
## Warning in attr(x, "align"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
## See help("Deprecated")
## Warning in attr(.knitEnv$meta, "knit_meta_id"): 'xfun::attr()' is deprecated.
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## See help("Deprecated")
```

```
## Warning in attr(.knitEnv$meta, "knit_meta_id"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
## See help("Deprecated")
## Warning in attr(x, "align"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
## See help("Deprecated")
## Warning in attr(x, "format"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
## See help("Deprecated")
```

Table 5: Donor Weights by Subset

Subset	Donor	Weight
Neighbors	Washington	0.6149
Neighbors	Idaho	0.1131
Neighbors	California	0.2721
Exclude_Washington	Idaho	0.2619
Exclude_Washington	Utah	0.0000
Exclude_Washington Exclude_Washington Exclude_Washington Exclude_Washington	Colorado California Arizona Wisconsin	0.0867 0.1499 0.2182 0.0000
Exclude_Washington Exclude_Washington Exclude_Washington	North Carolina Wyoming South Dakota	0.0000 0.2833 0.0000

```
# PSEUDO-TREATMENT TEST
# Set cutoff for pseudo-treatment dates after 2015 so we have at least two years to create a synthetic
pseudo_periods <- df_pre$date[df_pre$date >= as.Date("2015-01-01")]
n_placebo_draws <- 50</pre>
# Loop over each pseudo-treatment date and estimate synthetic control gaps
pseudo_results_nested <- lapply(pseudo_periods, function(pseudo_date) {</pre>
# Filter training data before the pseudo-treatment date
 df_train <- df_pre %>% filter(date < pseudo_date)</pre>
# Pivot training data to wide format
  df_train_wide <- df_train %>%
    select(date, state, crash_rate) %>%
    pivot_wider(names_from = state, values_from = crash_rate, values_fn = sum)
  if (nrow(df_train_wide) <= 2) {</pre>
    return(list(ATT = NA, SE = NA, p_value = NA))}
# Construct synthetic Oregon from pre-pseudo data
  y_oregon <- df_train_wide$Oregon</pre>
  Y_d_oregon <- df_train_wide[, donor_states] %>% as.matrix()
# Estimate weights using earlier function
 w_hat_oregon <- tryCatch({</pre>
```

```
scm_fit(y_oregon, Y_d_oregon)
  }, error = function(e) NULL)
# Transform dataset to apply synthetic control across full period
  df_all_wide <- df_pre %>%
    select(date, state, crash_rate) %>%
    pivot_wider(names_from = state, values_from = crash_rate, values_fn = sum)
# Create synthetic control before pseudo-treatment date
  synthetic_series_oregon <- rowSums(as.matrix(df_all_wide[, donor_states]) *</pre>
                                    matrix(rep(w_hat_oregon, each = nrow(df_all_wide)), ncol = length(do:
# Scale so fake synthetic control matches fake treated unit
scalar_oregon <- mean(df_all_wide$Oregon[df_all_wide$date < pseudo_date], na.rm = TRUE) /</pre>
                 mean(synthetic_series_oregon[df_all_wide$date < pseudo_date], na.rm = TRUE)</pre>
synthetic_series_oregon_scaled <- synthetic_series_oregon * scalar_oregon</pre>
# Compute the gap between actual and synthetic Oregon
df_all_wide <- df_all_wide %>%
  mutate(
    synthetic_pseudo = synthetic_series_oregon_scaled,
    gap_pseudo = Oregon - synthetic_pseudo,
    post_pseudo = date >= pseudo_date)
# Compute pseudo ATT
  att_summary_pseudo <- df_all_wide %>%
    group_by(post_pseudo) %>%
    summarise(
      avg_gap = mean(gap_pseudo, na.rm = TRUE),
      .groups = "drop")
  if (nrow(att_summary_pseudo) != 2) {
    return(list(ATT = NA, SE = NA, p_value = NA))}
  att_oregon <- diff(att_summary_pseudo$avg_gap)</pre>
# Calculate SEs for pseudo treatment estimates using placebo-based inference
# Create empty vector to store placebo ATTs
 placebo_att_list <- c()</pre>
# Loop over each donor state
 for (draw in 1:n_placebo_draws) {
    fake_treated <- sample(donor_states, 1)</pre>
# Construct synthetic control for placebo state
    Y_d_fake <- df_train_wide[, setdiff(donor_states, fake_treated)] %>% as.matrix()
    y_fake <- df_train_wide[[fake_treated]]</pre>
# Estimate weights using earlier function
  w_hat_fake <- tryCatch({</pre>
    scm_fit(y_fake, Y_d_fake)
  }, error = function(e) NULL)
```

```
# Create synthetic control for placebo-treated state
  synthetic_series_fake <- rowSums(as.matrix(df_all_wide[, setdiff(donor_states, fake_treated)]) *</pre>
    matrix(rep(w_hat_fake, each = nrow(df_all_wide)), ncol = length(setdiff(donor_states, fake_treated)
# Scale each placebo's synthetic control to match its own pre-period mean
  post_fake <- df_all_wide$date >= pseudo_date
  scalar_fake <- mean(df_all_wide[[fake_treated]][!post_fake], na.rm = TRUE) /</pre>
               mean(synthetic_series_fake[!post_fake], na.rm = TRUE)
  synthetic_series_fake_scaled <- synthetic_series_fake * scalar_fake</pre>
# Compute and store placebo ATT for this draw
  gap_fake <- df_all_wide[[fake_treated]] - synthetic_series_fake_scaled</pre>
  placebo_ATT <- mean(gap_fake[post_fake], na.rm = TRUE) - mean(gap_fake[!post_fake], na.rm = TRUE)</pre>
  placebo_att_list <- c(placebo_att_list, placebo_ATT)}</pre>
# Compute SE using distribution of placebo estimates
  se_pseudo <- sd(placebo_att_list, na.rm = TRUE)</pre>
  if (!is.na(att_oregon) & !is.na(se_pseudo) & se_pseudo > 0) {
    z_val <- att_oregon / se_pseudo</pre>
    p_val <- 2 * pnorm(-abs(z_val))</pre>
 } else {
    p_val <- NA}</pre>
# Return ATT, SE, and p-value as list for this pseudo-treatment period
  list(ATT = att_oregon, SE = se_pseudo, p_value = p_val)})
# Merge results across all pseudo-treatment dates into a dataframe
pseudo_results_nested_df <- data.frame(</pre>
  Pseudo_Treatment_Date = pseudo_periods,
  ATT = sapply(pseudo_results_nested, `[[`, "ATT"),
  SE = sapply(pseudo_results_nested, `[[`, "SE"),
  p_value = sapply(pseudo_results_nested, `[[`, "p_value"))
# Correct ATT's bias
bias_estimate <- mean(pseudo_results_nested_df$ATT, na.rm = TRUE)</pre>
att_bias_corrected <- att - bias_estimate</pre>
print(bias_estimate)
## [1] -0.1232997
print(att bias corrected)
## [1] 0.04333967
# Display results
kable(pseudo_results_nested_df, caption = "Nested Parallel Pseudo-Treatment Test Results") %>%
 kable_styling(bootstrap_options = c("striped", "hold_position"))
## Warning in attr(x, "align"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
## See help("Deprecated")
## Warning in attr(.knitEnv$meta, "knit_meta_id"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
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```

```
## Use 'xfun::attr2()' instead.
## See help("Deprecated")
## Warning in attr(.knitEnv$meta, "knit_meta_id"): 'xfun::attr()' is deprecated.
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## Use 'xfun::attr2()' instead.
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## Use 'xfun::attr2()' instead.
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## See help("Deprecated")
## Warning in attr(x, "format"): 'xfun::attr()' is deprecated.
## Use 'xfun::attr2()' instead.
## See help("Deprecated")
```

Table 6: Nested Parallel Pseudo-Treatment Test Results

Pseudo_Treatment_Date	ATT	SE	p_value
2015-01-01	-0.0827550	0.1627413	0.6110983
2015-02-01	-0.0706487	0.1637458	0.6661385
2015-03-01	-0.0757093	0.1884103	0.6878075
2015-04-01	-0.0732283	0.1770219	0.6791171
2015-05-01	-0.0859242	0.1585736	0.5879172

2015-06-01	-0.0858965	0.1345224	0.5231294
2015-07-01	-0.0891618	0.1404061	0.5254103
2015-08-01	-0.0954612	0.1670356	0.5676594
2015-09-01	-0.0942475	0.1704264	0.5802568
2015-10-01	-0.0976868	0.2092531	0.6406175
2015-11-01	-0.0949838	0.1637562	0.5618931
2015-12-01	-0.0936220	0.1847434	0.6123176
2016-01-01	-0.0981282	0.1604705	0.5408667
2016-02-01 2016-03-01	-0.1026357 -0.1098459	0.1884116 $0.1401633$	0.5859312 $0.4332164$
2016-04-01	-0.1125975	0.1245931	0.3661433
2016-05-01 2016-06-01	-0.1271328 -0.1298673	0.1558954 $0.1785972$	0.4147860 $0.4671327$
2016-00-01 2016-07-01	-0.1298073	0.1785972 $0.1670893$	0.4071327 $0.4264823$
2016-08-01	-0.1350954	0.1070893	0.4204023 $0.4345480$
2016-09-01 2016-10-01	-0.1353912 -0.1388422	0.1610854 $0.1822714$	0.4006318 $0.4462192$
2016-10-01	-0.1388422	0.1822714 $0.1899659$	0.4402192 $0.4591789$
2016-12-01	-0.1432327	0.1994012	0.4725639
2017-01-01	-0.1454488	0.1955731	0.4570547
2017-02-01	-0.1550669	0.1605314	0.3340642
2017-02-01	-0.1578954	0.1752808	0.3676873
2017-04-01	-0.1591483	0.2180138	0.4653953
2017-05-01	-0.1648333	0.2005028	0.4110200
2017-06-01	-0.1647402	0.1989160	0.4075631
2017-07-01	-0.1662160	0.1888377	0.3787479
2017-08-01	-0.1682317	0.2109204	0.4250982
2017-09-01	-0.1707842	0.1738409	0.3258947
2017-10-01	-0.1744075	0.1864221	0.3495040
2017-11-01	-0.1704315	0.2017590	0.3982625
2017-12-01	-0.1687330	0.1883158	0.3702470
2018-01-01	-0.1511033	0.1747993	0.3873468
2018-02-01	-0.1407953	0.1868888	0.4512313
2018-03-01	-0.1373423	0.1734883	0.4285641
2018-04-01	-0.1315467	0.2075634	0.5262332
2018-05-01	-0.1332178	0.2022406	0.5100823
2018-06-01	-0.1301488	0.1506565	0.3876551
2018-07-01 2018-08-01	-0.1311230 -0.1278244	0.1886679 $0.1952637$	$0.4870591 \\ 0.5127097$
2018-09-01	-0.1219431	0.1952037 $0.2182920$	0.5127097 $0.5764185$
2018-10-01	-0.1233561	0.1865990	0.5085636 $0.5884278$
2018-11-01 2018-12-01	-0.1216885 -0.1231813	0.2248845 $0.2098372$	0.5664276 $0.5571818$
2019-01-01	-0.1231313	0.2098372 $0.1818236$	0.3371818 $0.4955580$
2019-02-01	-0.1150870	0.1859132	0.5358924
2019-03-01	-0.1207534	0.1790284	0.4999981
2019-03-01	-0.1210245	0.1790284 $0.1910577$	0.4999931 $0.5264434$
2019-05-01	-0.1279102	0.2304936	0.5789355
2019-06-01	-0.1320526	0.1739349	0.4477287
2019-07-01	-0.1377227	0.2006557	0.4924840

2019-08-01	-0.1354053	0.2262569	0.5495342
2019-09-01	-0.1310543	0.2398062	0.5847217
2019-10-01	-0.1360527	0.2761552	0.6222476
2019-11-01	-0.1247594	0.2934737	0.6707545
2019-12-01	-0.1190971	0.2362134	0.6141260
2020-01-01	-0.1145537	0.2409321	0.6344588
2020-02-01	-0.1166256	0.3052027	0.7023685
2020-03-01	-0.1269430	0.2446045	0.6037799
2020-04-01	-0.1322853	0.2686923	0.6224860
2020-05-01	-0.1517854	0.2636377	0.5647943
2020-06-01	-0.1579029	0.3101533	0.6106735
2020-07-01	-0.1493356	0.1954311	0.4447873
2020-08-01	-0.1369775	0.2376456	0.5643487
2020-09-01	-0.1147620	0.2546726	0.6522593
2020-10-01	-0.1100578	0.3001318	0.7138440
2020-11-01	-0.0643787	0.2715289	0.8125816
2020-12-01	-0.0592107	0.2113203 $0.2137676$	0.7817906
2021-01-01	0.0435573	0.1936818	0.8220640
2015-01-01	-0.0827550	0.1616487	0.6086906
2015-02-01	-0.0706487	0.1583792	0.6555442
2015-03-01	-0.0757093	0.1548251	0.6248424
2015-03-01	-0.0732283	0.1348231 $0.1750776$	0.0240424 $0.6757556$
2015-05-01	-0.0859242	0.1750770 $0.1529873$	0.5743597
2015-06-01	-0.0858965	0.1880101	0.6477634
2015-07-01	-0.0891618	0.1732959	0.6068982
2015-08-01	-0.0954612	0.1835729	0.6030511
2015-09-01	-0.0942475	0.1910798	0.6218457
2015-10-01 2015-11-01	-0.0976868 -0.0949838	0.1477640 $0.1859832$	0.5085481 $0.6095528$
2015-11-01	-0.0936220	0.1822659	0.6093328 $0.6074923$
2016-01-01	-0.0981282	0.1868488	0.5994620
2016-02-01	-0.1026357	0.1799241	0.5683802
2016-03-01	-0.1098459	0.1625379	0.4991567
2016-04-01	-0.1125975	0.1816332	0.5353126
2016-05-01	-0.1271328	0.2114145	0.5476111
2016-06-01	-0.1298673	0.1768074	0.4626362
2016-07-01	-0.1328737	0.1881390	0.4800309
2016-08-01	-0.1350954	0.1919016	0.4814437
2016-09-01	-0.1353912	0.1777588	0.4462648
2016-10-01	-0.1388422	0.1864003	0.4563563
2016-11-01	-0.1406127	0.2067760	0.4964890
2016-12-01	-0.1432327	0.1926425	0.4571697
2017-01-01	-0.1454488	0.2080361	0.4844574
2017-02-01	-0.1550669	0.1919185	0.4191003
2017-03-01	-0.1578954	0.1861300	0.3962671
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2017-11-01	-0.1704315	0.1984586	0.3904641
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2018-09-01	-0.1219431	0.2046272	0.5512232
2018-10-01	-0.1233561	0.1959448	0.5289922
2018-11-01	-0.1216885	0.1791512	0.4969792
2018-12-01	-0.1231813	0.1976447	0.5331227
2019-01-01	-0.1239120	0.1963689	0.5280298
2019-02-01	-0.1150870	0.1565901	0.4623656
2019-03-01	-0.1207534	0.1881884	0.5210926
2019-04-01	-0.1210245	0.2483991	0.6261040
2019-05-01	-0.1279102	0.2261594	0.5716824
2019-06-01	-0.1320526	0.2017963	0.5128634
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2020-07-01	-0.1493356	0.2465032	0.5446368
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2021-01-01 2015-01-01 2015-02-01 2015-03-01 2015-04-01	0.0435573 -0.0827550 -0.0706487 -0.0757093 -0.0732283	$\begin{array}{c} 0.1644157 \\ 0.1506287 \\ 0.1468817 \\ 0.1713525 \\ 0.1469130 \end{array}$	$\begin{array}{c} 0.7910696 \\ 0.5827328 \\ 0.6305231 \\ 0.6586095 \\ 0.6181692 \end{array}$
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2017-09-01	-0.1707842	0.1301632	0.3311550 $0.4126541$
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2017-08-01 2017-09-01	-0.1682317 -0.1707842	0.1746863 $0.2101729$	0.3355222 $0.4164538$
2017-10-01	-0.1707842 -0.1744075	0.2101729 0.2030433	0.4104538 $0.3903587$
2017-10-01	-0.1744075	0.2030433 $0.1997218$	0.3903387 $0.3934682$
2017-12-01	-0.1687330	0.1831773	0.3569742
2018-01-01	-0.1511033	0.1902329	0.4270170
2018-02-01	-0.1407953	0.1752531	0.4217537
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2018-05-01	-0.1332178	0.2074980	0.5208602
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2018-07-01	-0.1311230	0.1867801	0.4826678
2018-08-01	-0.1278244	0.1851947	0.4900582
2018-09-01	-0.1219431	0.2105205	0.5624234
2018-10-01	-0.1233561	0.2350147	0.5996618
2018-11-01	-0.1216885	0.1950105	0.5326209
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2019-02-01	-0.1150870	0.1802591	0.5231788
2019-03-01	-0.1207534	0.2016986	0.5493848
2019-04-01	-0.1210245	0.1797274	0.5007069
2019-05-01	-0.1279102	0.2258684	0.5711871
2019-06-01 2019-07-01	-0.1320526 -0.1377227	0.2373408 $0.2188608$	0.5779485 $0.5291717$
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2019-09-01	-0.1310543	0.2247663	0.5598468
2019-10-01 2019-11-01	-0.1360527 -0.1247594	0.2363578 $0.2561831$	0.5648709 $0.6262631$
2019-11-01 2019-12-01	-0.1247594 -0.1190971	0.2501851 $0.1928445$	0.0202031 $0.5368516$
2020-01-01	-0.1145537	0.2567215	0.6554400
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2020-04-01	-0.1517854	0.2642822	0.5657439
2020-06-01 2020-07-01	-0.1579029 -0.1493356	$0.2792609 \\ 0.2134317$	0.5717804 $0.4841221$
2020-07-01	-0.1369775	0.2134517 $0.2571610$	0.4841221 $0.5942739$
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2020-10-01	-0.1100578	0.2235080	0.6224286
2020-11-01	-0.0643787	0.2910552	0.8249440
2020-11-01	-0.0592107	0.2068899	0.7747293
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2015-02-01	-0.0706487	0.1325264	0.5939701
2015-03-01	-0.0757093	0.1734060	0.6624004
2015-04-01	-0.0732283	0.1726938	0.6715399
2015-05-01	-0.0859242	0.1605477	0.5925157
2015-06-01	-0.0858965	0.1463622	0.5572871
2015-07-01	-0.0891618	0.1466681	0.5432435
2015-08-01	-0.0954612	0.1632354	0.5586775
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2015-11-01	-0.0949838	0.1778031	0.5931977
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2016-07-01	-0.1328737	0.1764469	0.4514187
2016-08-01	-0.1350954	0.1781404	0.4482329
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2016-10-01	-0.1388422	0.1643547	0.3982384
2016-11-01	-0.1406127	0.1790590	0.4322853
2016-12-01	-0.1432327	0.2014514	0.4770822
2017-01-01	-0.1454488	0.1752385	0.4065361
2017-02-01	-0.1550669	0.1897868	0.4138951
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2019-08-01 2019-09-01	-0.1354053 -0.1310543	0.1938393 $0.2592765$	0.4848369 $0.6132347$
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2015-02-01	-0.0706487	0.1845057	0.7017879
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2017-06-01 2017-07-01	-0.1647402	0.1675148 $0.2163187$	0.3253927 $0.4422585$
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2017-09-01	-0.1002317	0.1904033 $0.1812979$	0.3461882
2017-10-01	-0.1744075	0.2164551	0.4203901
2017-11-01	-0.1704315	0.1676593	0.3093747
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2018-11-01	-0.1216885	0.1827869	0.5055773
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2019-05-01	-0.1279102	0.2268668	0.5728821
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2019-07-01	-0.1377227	0.2337229	0.5556892
2019-08-01	-0.1354053	0.2297496	0.5556195
2019-09-01	-0.1310543	0.1895306	0.4892716
2019-10-01	-0.1360527	0.2571383	0.5967338
2019-11-01	-0.1247594	0.2606908	0.6322428
2019-12-01	-0.1190971	0.2099807	0.5705912
2020-01-01	-0.1145537	0.2381233	0.6304677
2020-02-01	-0.1166256	0.2439721	0.6326298
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2020-04-01	-0.1322853	0.2769471	0.6328954
2020-05-01	-0.1517854	0.2933275	0.6048346
2020-06-01	-0.1579029	0.2277819	0.4881718
2020-07-01	-0.1493356	0.2481516	0.5473127
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2017-12-01	-0.1687330	0.1733983	0.3305060
2018-01-01 2018-02-01	-0.1511033 -0.1407953	0.1680464 $0.2064123$	0.3685589 $0.4951713$
2018-03-01	-0.1373423	0.1533969	0.3706058
2018-04-01	-0.1315467	0.1944081	0.4986265
2018-05-01 2018-06-01	-0.1332178 -0.1301488	0.1892424 $0.1883618$	0.4814618 $0.4895962$
2018-07-01	-0.1311230	0.1874381	0.4893902 $0.4842061$
2018-08-01 2018-09-01	-0.1278244 -0.1219431	0.1768081 $0.1921036$	0.4697074 $0.5255734$
2018-10-01	-0.1233561	0.1921030 $0.2086865$	0.5255754 $0.5544485$
2018-11-01	-0.1216885	0.1690696	0.4716765
2018-12-01	-0.1231813	0.1687485	0.4654086

2019-01-01	-0.1239120	0.1905475	0.5155019
2019-02-01	-0.1150870	0.1718613	0.5030806
2019-03-01	-0.1207534	0.2016243	0.5492375
2019-04-01	-0.1210245	0.1968911	0.5387680
2019-05-01	-0.1279102	0.2093707	0.5412479
2019-06-01	-0.1320526	0.1955264	0.4994411
2019-07-01	-0.1377227	0.2074623	0.5067899
2019-08-01	-0.1354053	0.2415349	0.5750678
2019-09-01	-0.1310543	0.3029081	0.6652663
2019-10-01	-0.1360527	0.2655855	0.6084589
2019-11-01	-0.1247594	0.2811455	0.6572205
2019-12-01	-0.1190971	0.1668682	0.4754006
2020-01-01	-0.1145537	0.2220454	0.6059227
2020-02-01	-0.1166256	0.2555009	0.6480600
2020-03-01	-0.1269430	0.2290421	0.5794183
2020-04-01	-0.1322853	0.2282352	0.5621837
2020-05-01	-0.1517854	0.2896005	0.6001950
2020-06-01	-0.1579029	0.2598309	0.5433771
2020-07-01	-0.1493356	0.2528648	0.5548053
2020-08-01	-0.1369775	0.2263482	0.5450707
2020-09-01	-0.1147620	0.2508799	0.6473563
2020-09-01 2020-10-01	-0.1147020	0.2644277	0.6473503 $0.6772552$
2020-10-01	-0.1100378	0.2044277 $0.2771725$	0.0772332 $0.8163288$
2020-11-01	-0.0592107	0.2016001	0.3103233 $0.7689843$
2021-01-01	0.0435573	0.2010001 $0.1790100$	0.8077549
2015-01-01	-0.0827550	0.1141649	0.4685302
2015-02-01	-0.0706487	0.1741502	0.6849799
2015-03-01	-0.0757093	0.1501313	0.6140593
2015-04-01	-0.0732283	0.1948468	0.7070469
2015-05-01	-0.0859242	0.1645316	0.6015067
2015-06-01	-0.0858965	0.1875746	0.6470011
2015-07-01	-0.0891618	0.1132648	0.4311662
2015-08-01	-0.0954612	0.2062818	0.6435287
2015-09-01	-0.0942475	0.1647839	0.5673586
2015-10-01	-0.0976868	0.1853557	0.5981774
2015-11-01	-0.0949838	0.1918589	0.6205499
2015-12-01	-0.0936220	0.1920250	0.6258677
2016-01-01	-0.0981282	0.1729861	0.5705371
2016-02-01	-0.1026357	0.1460931	0.4823449
2016-03-01	-0.1098459	0.1789255	0.5392683
2016-04-01	-0.1125975	0.1577903	0.4754812
2016-05-01	-0.1271328	0.1569702	0.4179881
2016-06-01	-0.1298673	0.1190913	0.2754992
2016-07-01	-0.1328737	0.2086740	0.5242861
2016-08-01	-0.1350954	0.1649214	0.4127009
2016-09-01	-0.1353912	0.1831143	0.4596757
2016-09-01 2016-10-01	-0.1353912 -0.1388422	0.1831143 $0.1498115$	0.4596757 $0.3540412$
2016-10-01 2016-11-01	-0.1388422 -0.1406127	0.1498115 $0.2128900$	0.5040412 $0.5089363$
2016-11-01 2016-12-01	-0.1400127 -0.1432327	0.2128900 $0.1861997$	0.5089505 $0.4417496$
2017-01-01	-0.1452527 -0.1454488	0.1752439	0.4417490 $0.4065506$
2011-01-01	-0.1404400	0.1102403	0.4000000

2017-02-01	-0.1550669	0.1976587	0.4327359
2017-03-01	-0.1578954	0.1814452	0.3841858
2017-04-01	-0.1591483	0.1896684	0.4014207
2017-05-01	-0.1648333	0.1985610	0.4064599
2017-06-01	-0.1647402	0.1770944	0.3522473
2017-07-01	-0.1662160	0.1974719	0.3999448
2017-08-01	-0.1682317	0.2058261	0.3333440 $0.4137292$
2017-09-01	-0.1707842	0.2068356	0.4089742
2017-10-01	-0.1744075	0.2158502	0.4190890
2017-11-01	-0.1704315	0.1970593	0.3871077
2017-12-01	-0.1687330	0.2015816	0.4025668
2018-01-01	-0.1511033	0.2513515 $0.1553555$	0.3307378
2018-02-01	-0.1407953	0.1826644	0.4408335
2018-03-01	-0.1373423	0.1711815	0.4223683
2018-04-01	-0.1315467	0.1912854	0.4916425
2018-05-01	-0.1332178	0.1998807	0.5051001
2018-06-01	-0.1301488	0.1652766	0.4310124
2018-07-01	-0.1311230	0.1587849	0.4089231
2018-08-01	-0.1278244	0.1764356	0.4687700
2018-09-01	-0.1219431	0.2108573	0.5630478
2018-10-01	-0.1233561	0.2247100	0.5830349
2018-11-01	-0.1216885	0.2181362	0.5769429
2018-12-01	-0.1231813	0.1987695	0.5354426
2019-01-01	-0.1239120	0.2084160	0.5521500
2019-02-01	-0.1150870	0.1906592	0.5460919
2019-03-01	-0.1207534	0.2149396	0.5742513
2019-04-01	-0.1210245	0.2263284	0.5928370
2019-05-01	-0.1279102	0.2276119	0.5741390
2019-06-01	-0.1320526	0.1943997	0.4969580
2019-07-01	-0.1377227	0.2459657	0.5755295
2019-08-01	-0.1354053	0.2253752	0.5479736
2019-09-01	-0.1310543	0.2298392	0.5685420
2019-10-01	-0.1360527	0.2301902	0.5544906
2019-11-01	-0.1247594	0.2465137	0.6127897
2019-12-01	-0.1190971	0.2720599	0.6615599
2020-01-01	-0.1145537	0.2717610	0.6733727
2020-02-01	-0.1166256	0.2014077	0.5625538
2020-03-01	-0.1269430	0.2554056	0.6191713
2020-04-01	-0.1322853	0.2603156	0.6113321
2020-05-01	-0.1517854	0.2810443	0.5891443
2020-06-01	-0.1579029	0.2732184	0.5633070
2020-07-01	-0.1493356	0.2412659	0.5359381
2020-08-01	-0.1369775	0.2521498	0.5869654
2020-09-01	-0.1147620	0.2621207	0.6615158
2020-10-01	-0.1100578	0.2807695	0.6950682
2020-11-01	-0.0643787	0.2624791	0.8062461
2020-12-01	-0.0592107	0.2320325	0.7985819
2021-01-01	0.0435573	0.1742916	0.8026565

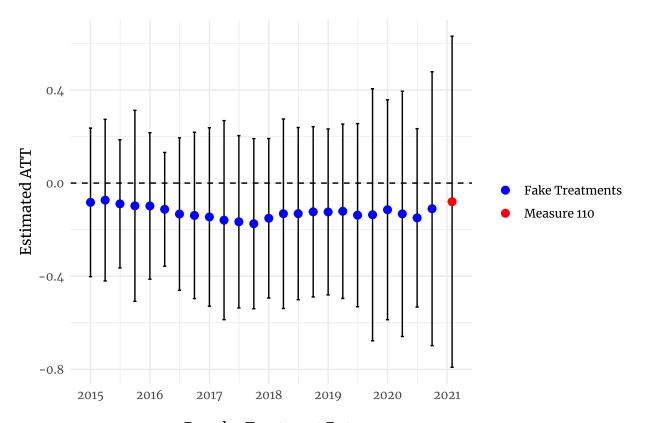
```
# Keep only one pseudo-treatment per month to prevent overplotting
pseudo_results_filtered <- pseudo_results_nested_df %>%
  mutate(month = lubridate::floor date(Pseudo Treatment Date, "3 months")) %>%
  group_by(month) %>%
  slice(1) %>%
  ungroup()
pseudo_results_filtered <- pseudo_results_filtered %>%
  slice_head(n = nrow(.) - 1)
\# Plot pseudo-treatment ATT over time
ggplot(pseudo_results_filtered, aes(x = month, y = ATT)) +
  geom_errorbar(aes(ymin = ATT - 1.96 * SE, ymax = ATT + 1.96 * SE), width = 20, color = "black") +
  geom_point(color = "blue") +
  geom_hline(yintercept = 0, linetype = "dashed") +
  geom_vline(xintercept = att_bias_corrected, color = "red", linetype = "solid") +
  scale_x_date(
    date_breaks = "1 year",
    date_labels = "%Y") +
    x = "Pseudo-Treatment Date",
    y = "Estimated ATT") +
  theme_minimal(base_family = "latexfont") +
  theme(axis.title.x = element_text(margin = margin(t = 15)))
    0.50
    0.25
Estimated ATT
    0.00
   -0.25
   -0.50
   -0.75
                        2016
                                                 2018
                                                              2019
           2015
                                     2017
                                                                           2020
                                                                                        2021
```

## Pseudo-Treatment Date

```
# Report the proportion of pseudo-treatments with p < 0.05

n_significant_nested <- sum(pseudo_results_nested_df$p_value < 0.05, na.rm = TRUE)
```

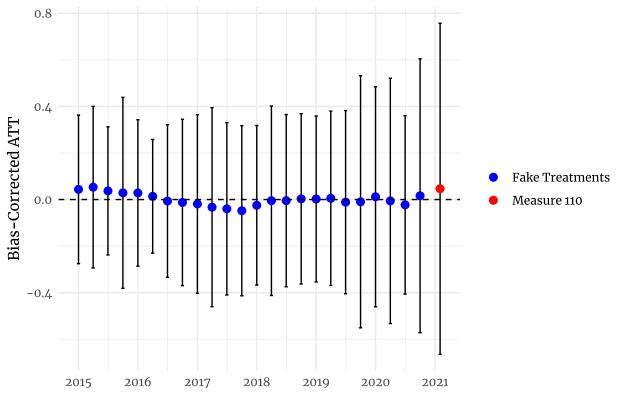
```
n_total_nested <- nrow(pseudo_results_nested_df)</pre>
cat("\nOut of", n_total_nested, "pseudo-treatments,", n_significant_nested,
    "had p < 0.05 (", round(100 * n_significant_nested/n_total_nested, 2), "%).\n")
##
## Out of 803 pseudo-treatments, 0 had p < 0.05 ( 0 \% ).
# Save file to folder
ggsave("images/pseudo_treatment.pdf", width = 8, height = 4, dpi = 300)
# PLOT PSEUDO TREATMENT RESULTS WITH OREGON
# Define the real treatment result
true_treatment_date <- as.Date("2021-02-01")</pre>
att_or <- -0.07996006
se_or <- 0.3626841
# Append Oregon result to filtered pseudo results
pseudo_results_filtered <- pseudo_results_filtered %>%
  mutate(is_real = FALSE) %>%
  bind_rows(
   data.frame(
      month = true treatment date,
     ATT = att_or,
     SE = se or,
      is_real = TRUE))
# Plot pseudo-treatment ATT over time
ggplot(pseudo_results_filtered, aes(x = month, y = ATT, color = is_real)) +
  geom_errorbar(aes(ymin = ATT - 1.96 * SE, ymax = ATT + 1.96 * SE), width = 20, color = "black") +
  geom_point(size = 2.5) +
  scale_color_manual(
   values = c("FALSE" = "blue", "TRUE" = "red"),
   labels = c("FALSE" = "Fake Treatments", "TRUE" = "Measure 110"),
   name = NULL
  ) +
  geom_hline(yintercept = 0, linetype = "dashed") +
  scale_x_date(date_breaks = "1 year", date_labels = "%Y") +
  labs(
   x = "Pseudo-Treatment Date",
   y = "Estimated ATT",
  theme_minimal(base_family = "latexfont") +
   axis.title.x = element_text(margin = margin(t = 15)),
   legend.position = "right" # you can also try "top", "bottom", or "left"
```



## Pseudo-Treatment Date

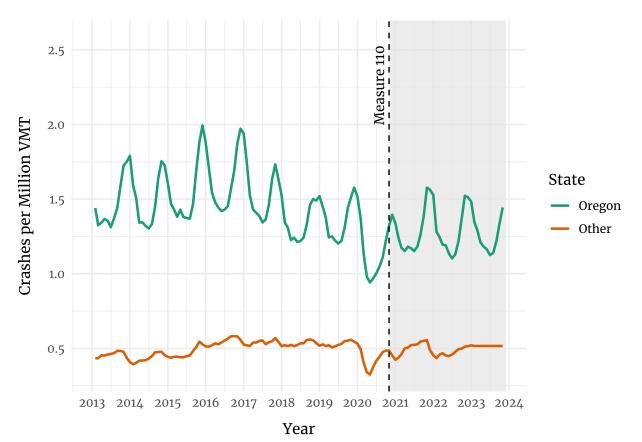
```
# Report the proportion of pseudo-treatments with p < 0.05
n_significant_nested <- sum(pseudo_results_nested_df$p_value < 0.05, na.rm = TRUE)
n_total_nested <- nrow(pseudo_results_nested_df)</pre>
cat("\nOut of", n_total_nested, "pseudo-treatments,", n_significant_nested,
    "had p < 0.05 (", round(100 * n_significant_nested/n_total_nested, 2), "%).\n")
##
## Out of 803 pseudo-treatments, 0 had p < 0.05 ( 0 \% ).
# Save file to folder
ggsave("images/pseudo_treatment.pdf", width = 8, height = 4, dpi = 300)
# PLOT PSEUDO TREATMENT RESULTS WITH OREGON, CORRECT FOR BIAS
# Compute average placebo ATT (drift)
bias_drift <- mean(pseudo_results_filtered$ATT[!pseudo_results_filtered$is_real], na.rm = TRUE)
# Apply correction to ATT and compute new y-axis values
pseudo_results_filtered <- pseudo_results_filtered %>%
  mutate(
    ATT_corrected = ATT - bias_drift,
   ymin_corrected = ATT_corrected - 1.96 * SE,
   ymax_corrected = ATT_corrected + 1.96 * SE)
# Plot pseudo-treatment ATT over time
ggplot(pseudo_results_filtered, aes(x = month, y = ATT_corrected, color = is_real)) +
  geom_errorbar(aes(ymin = ymin_corrected, ymax = ymax_corrected), width = 20, color = "black") +
  geom_point(size = 2.5) +
```

```
scale_color_manual(
  values = c("FALSE" = "blue", "TRUE" = "red"),
  labels = c("FALSE" = "Fake Treatments", "TRUE" = "Measure 110"),
  name = NULL
) +
geom_hline(yintercept = 0, linetype = "dashed") +
scale_x_date(date_breaks = "1 year", date_labels = "%Y") +
labs(
  x = "Pseudo-Treatment Date",
  y = "Bias-Corrected ATT",
) +
theme_minimal(base_family = "latexfont") +
theme(
  axis.title.x = element_text(margin = margin(t = 15)),
  legend.position = "right"
)
```



## Pseudo-Treatment Date

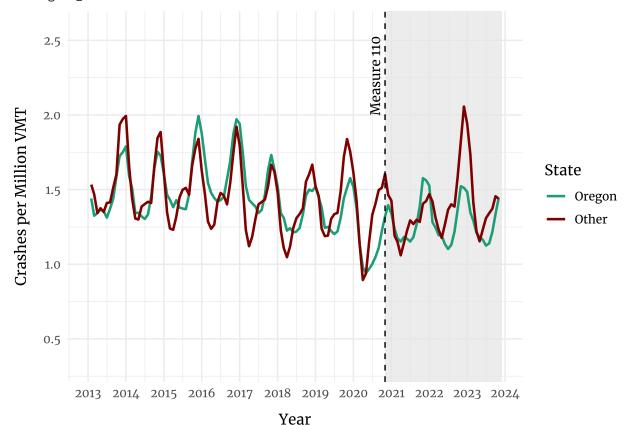
```
# PLOT DONOR STATES AGAINST OREGON
# Compute shared y-axis limits
df ca <- df wide all %>% select(date, Oregon, California)
df_wy <- df_wide_all %>% select(date, Oregon, Wyoming)
df_wa <- df_wide_all %>% select(date, Oregon, Washington)
smooth_df <- function(df, other) {</pre>
 df %>%
   rename(Other = !!sym(other)) %>%
   pivot_longer(c("Oregon","Other"), names_to="series", values_to="crash_rate") %>%
    group_by(series) %>%
   mutate(smoothed_rate = zoo::rollmean(crash_rate, 3, fill=NA, align="center")) %>%
   ungroup()}
sm_ca <- smooth_df(df_ca, "California")</pre>
sm_wy <- smooth_df(df_wy, "Wyoming")</pre>
sm_wa <- smooth_df(df_wa, "Washington")</pre>
global_ylim <- range(</pre>
  c(sm_ca$smoothed_rate, sm_wy$smoothed_rate, sm_wa$smoothed_rate),
 na.rm = TRUE)
# Oregon vs. California
ggplot(sm_ca, aes(date, smoothed_rate, color = series)) +
  annotate("rect",
   xmin = as.Date("2020-11-01"), xmax = max(sm ca$date),
   ymin = -Inf, ymax = Inf, fill = "gray90", alpha = 0.7
  ) +
  geom_line(size = 0.9) +
  geom_vline(xintercept = as.Date("2020-11-01"), linetype = "dashed") +
  annotate("text",
   x = as.Date("2020-11-01"), y = global_ylim[2],
   label = "Measure 110", angle = 90, vjust = -0.5, hjust = 1.1,
   size = 3.5, family = "latexfont"
  ) +
  scale_y_continuous("Crashes per Million VMT", limits = global_ylim) +
  scale_x_date(date_breaks = "1 year", date_labels = "%Y") +
  scale color manual(
   values = c("Oregon" = "#1b9e77", "Other" = "#d95f02"),
   labels = c("Oregon", "California", color = "State")
  ) +
  labs(x = "Year", color = "State") +
  theme minimal(base family = "latexfont") +
  theme(legend.position = "right",
        axis.title.x = element_text(margin = margin(t = 10)),
        axis.title.y = element_text(margin = margin(r = 10)))
```



```
ggsave("images/Oregon_vs_California.pdf", width = 6, height = 4, dpi = 300)
```

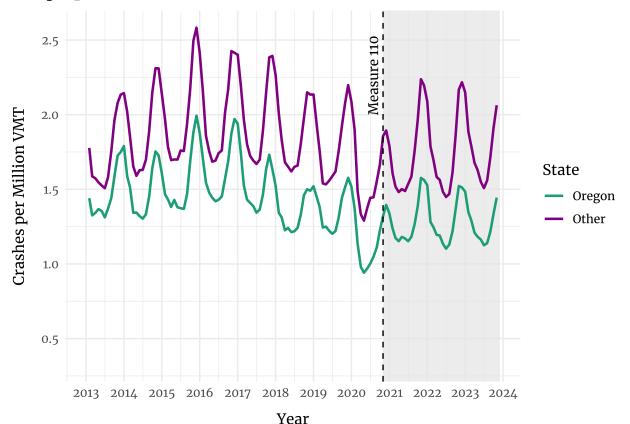
```
# Oregon vs. Wyoming
ggplot(sm_wy, aes(date, smoothed_rate, color = series)) +
  annotate("rect",
   xmin = as.Date("2020-11-01"), xmax = max(sm_wy$date),
   ymin = -Inf, ymax = Inf, fill = "gray90", alpha = 0.7
  ) +
  geom_line(size = 0.9) +
  geom_vline(xintercept = as.Date("2020-11-01"), linetype = "dashed") +
  annotate("text",
   x = as.Date("2020-11-01"), y = global_ylim[2],
   label = "Measure 110", angle = 90, vjust = -0.5, hjust = 1.1,
   size = 3.5, family = "latexfont"
  scale y continuous("Crashes per Million VMT", limits = global ylim) +
  scale_x_date(date_breaks = "1 year", date_labels = "%Y") +
  scale_color_manual(
   values = c("Oregon" = "#1b9e77", "Other" = "#800000"),
   labels = c("Oregon", "Wyoming", color = "State")
  ) +
  labs(x = "Year", color = "State") +
  theme_minimal(base_family = "latexfont") +
  theme(legend.position = "right",
        axis.title.x = element_text(margin = margin(t = 10)),
```

```
axis.title.y = element_text(margin = margin(r = 10)),
plot.title = element_text(hjust = 0.5, size = 14, face = "bold"))
```



ggsave("images/Oregon\_vs\_Wyoming.pdf", width = 6, height = 4, dpi = 300)

```
# Oregon vs. Washington
ggplot(sm_wa, aes(date, smoothed_rate, color = series)) +
  annotate("rect",
   xmin = as.Date("2020-11-01"), xmax = max(sm wa$date),
   ymin = -Inf, ymax = Inf, fill = "gray90", alpha = 0.7
  ) +
  geom_line(size = 0.9) +
  geom_vline(xintercept = as.Date("2020-11-01"), linetype = "dashed") +
  annotate ("text",
   x = as.Date("2020-11-01"), y = global_ylim[2],
   label = "Measure 110", angle = 90, vjust = -0.5, hjust = 1.1,
   size = 3.5, family = "latexfont"
  ) +
  scale_y_continuous("Crashes per Million VMT", limits = global_ylim) +
  scale_x_date(date_breaks = "1 year", date_labels = "%Y") +
  scale_color_manual(
   values = c("Oregon" = "#1b9e77", "Other" = "#800080"),
```



```
ggsave("images/Oregon_vs_Washington.pdf", width = 6, height = 4, dpi = 300)
```

## Warning: Removed 4 rows containing missing values or values outside the scale range ## (`geom\_line()`).

```
# REGRESSION ESTIMATE

# Run DID regression

lm.DID <- lm(crash_rate ~ treated*post + vmt + month_num + pop_density + factor(state), data = df)

clustered_se <- vcovCL(lm.DID, cluster = ~state)

coeftest(lm.DID, vcov = clustered_se)

##

## t test of coefficients:
##

## Estimate Std. Error t value Pr(>|t|)
```

1.9522e+00 6.6338e-01 2.9429 0.003304 \*\*

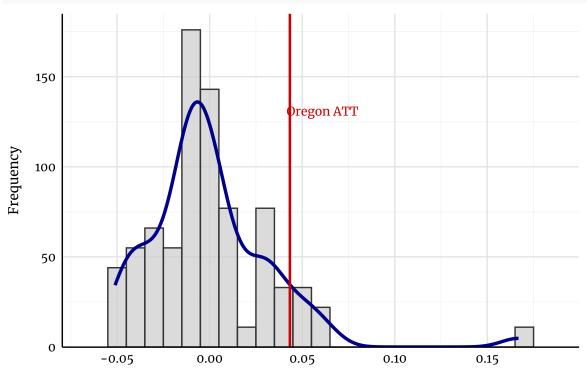
## (Intercept)

```
-6.3107e-01 5.8426e-01 -1.0801 0.280271
## treated
## postTRUE
                              -1.1608e-01 3.9157e-02 -2.9644 0.003083 **
## vmt
                              -6.4267e-05 5.4155e-05 -1.1867 0.235538
                               2.9107e-02 5.3226e-03 5.4686 5.344e-08 ***
## month_num
## pop density
                              1.7527e-04 8.3580e-03 0.0210 0.983272
## factor(state)California
                              1.0383e-01 2.0681e+00 0.0502 0.959968
## factor(state)Colorado
                             2.8119e-01 1.0754e-01 2.6147 0.009024 **
## factor(state)Idaho -5.7660e-01 4.4719e-01 -1.2894 0.197470
## factor(state)North Carolina 7.6267e-01 4.5912e-01 1.6611 0.096902 .
## factor(state)Oregon 9.9692e-02 3.4569e-01 0.2884 0.773096
## factor(state)South Dakota 4.5305e-01 4.5397e-02 9.9797 < 2.2e-16 ***
                              -5.8953e-02 2.9091e-01 -0.2027 0.839436
## factor(state)Utah
## factor(state)Washington 2.8243e-02 3.5052e-01 0.0806 0.935791
## factor(state)Wisconsin
                             2.3468e-01 3.7564e-01 0.6248 0.532229
## treated:postTRUE
                               3.2211e-02 6.0684e-02 0.5308 0.595635
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# PLOT PSEUDO TREATMENT DISTRIBUTION
# Extract placebo ATTs and estimate bias
placebo_atts <- na.omit(pseudo_results_nested_df$ATT)</pre>
bin_width <- 0.01
n_placebos <- length(placebo_atts)</pre>
bias_estimate <- mean(placebo_atts)</pre>
att_bias_corrected <- att_or - bias_estimate</pre>
# Bias-correct placebo ATTs
placebo_atts_corrected <- placebo_atts - bias_estimate</pre>
# Calculate test p-value
p_value <- mean(abs(placebo_atts_corrected) >= abs(att_bias_corrected))
# Build histogram
hist_counts <- hist(placebo_atts_corrected, plot = FALSE, breaks = seq(
  min(placebo_atts_corrected) - bin_width,
 max(placebo_atts_corrected) + bin_width,
 by = bin_width))$counts
# Placebo ATT distribution dataframe
placebo_df <- data.frame(value = placebo_atts_corrected)</pre>
# Theme
publication_theme <- theme_minimal() +</pre>
  theme(
   text = element_text(family = "latexfont", color = "black"),
   plot.title = element_text(size = 11, face = "bold", hjust = 0),
   plot.subtitle = element_text(size = 10, hjust = 0, margin = margin(b = 10)),
   axis.title.x = element_text(size = 10, margin = margin(t = 10)),
   axis.title.y = element_text(size = 10, margin = margin(r = 10)),
   axis.text = element_text(size = 9, color = "black"),
   legend.position = "none",
   panel.grid.major = element_line(color = "gray90"),
```

```
panel.grid.minor = element_line(color = "gray95"),
    plot.margin = margin(20, 20, 20, 20),
    plot.caption = element_text(size = 8, hjust = 0, margin = margin(t = 15)),
    panel.border = element_blank(),
    axis.line = element_line(color = "black", size = 0.5))
## Warning: The `size` argument of `element_line()` is deprecated as of ggplot2 3.4.0.
## i Please use the `linewidth` argument instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
# Main histogram + density + Oregon ATT
main_plot <- ggplot(placebo_df, aes(x = value)) +</pre>
  geom histogram(
    binwidth = bin_width,
    fill = "gray80",
    color = "gray20",
    alpha = 0.7) +
  geom_density(
    aes(y = ..density.. * n_placebos * bin_width),
    color = "darkblue",
    size = 1.2,
    adjust = 1.7) +
  geom_vline(
    xintercept = att_bias_corrected,
    color = "red3",
    linetype = "solid",
    size = 0.9) +
  annotate("text",
    x = att_bias_corrected+0.037,
    y = max(hist_counts) * 0.85,
    label = "Oregon ATT",
    color = "red3",
    size = 3.2,
   hjust = 1,
   family = "latexfont") +
  labs(
    x = "Bias-Corrected ATT from Pseudo-Treatments",
    y = "Frequency") +
  publication_theme +
  scale x continuous(
    expand = c(0.02, 0.02),
    breaks = scales::pretty_breaks(n = 8)) +
  scale_y_continuous(
    expand = c(0, 0.1),
    breaks = scales::pretty_breaks(n = 6)) +
  coord_cartesian(ylim = c(0, max(hist_counts) * 1.2))
# Save + print
ggsave("images/synthetic_did_results.pdf", plot = main_plot, width = 8, height = 5, dpi = 300)
## Warning: The dot-dot notation (`..density..`) was deprecated in ggplot2 3.4.0.
## i Please use `after_stat(density)` instead.
```

## This warning is displayed once every 8 hours.
## Call `lifecycle::last\_lifecycle\_warnings()` to see where this warning was
## generated.

# print(main\_plot)



Bias-Corrected ATT from Pseudo-Treatments