

Sec. 1.1

T A R C D

T, F, D, D
T, F, T, F

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- a) I didn't buy a lottery ticket this week.
- b) I bought a lottery ticket or I won the million dollar jackpot.
- c) If I buy a lottery ticket this week, then I will win the million dollar jackpot.
- d) I bought a lottery ticket and I won the million dollar jackpot.
- e) I will win the million dollar jackpot if and only if I buy a lottery ticket.
- f) If I do not buy a lottery ticket, I will not win the million dollar jackpot.
- g) I did not buy a lottery ticket this week, and I did not win the million dollar jackpot.
- h) I did not buy a lottery ticket this week, or I bought a ticket and won the million dollar jackpot.

19.

- a) F
- b) T
- c) T
- d) T

29.

- a) If you wash the bosses car, then you will get promoted.
- b) If there are winds from the south, then will be stronger.

29.

a)

(ohv, I will ski tomorrow if it snows today.

ihv, if it doesn't snow today, I won't ski tomorrow

(ohc, I won't ski tomorrow if it doesn't snow today.

b)

(ohv, If there is going to be a quiz, I will come to class

ihv, I will not come to class if there is not going to be a quiz

(ohc, If there is not going to be a quiz, I will not come to class

c)

(ohv, If a positive integer has no divisors other than 1 and itself, it is a prime

ihv, A positive integer is not a prime if it has divisors other than 1 and itself.

(ohc, If a positive integer has divisors other than 1 and itself, it is not a prime.

31.

a) 2^2

b) 2^4

b)
c) 2^6

d) 2^4

34.

a)

P	$\sim P$	$P \rightarrow \sim P$
T	F	F
F	T	F

b)

P	$\sim P$	$P \wedge \sim P$
T	F	F
F	T	F

c)

P	q	$P \vee q$	$P \oplus (P \vee q)$
T	T	T	F
T	F	T	F
F	T	T	T
F	F	F	F

d)

p	q	$p \wedge q$	$p \vee q$	$(p \wedge q) \rightarrow (p \vee q)$
T	T	T	T	T
T	F	F	T	F
F	T	F	T	F
F	F	F	F	T

e)

p	q	$\sim p$	$q \rightarrow \sim p$	$p \leftrightarrow q$	$((q \rightarrow \sim p) \leftrightarrow (p \leftrightarrow q))$
T	T	F	F	T	F
T	F	F	T	F	F
F	T	T	T	F	F
F	F	T	T	T	T

f)

p	q	$\sim q$	$p \leftrightarrow q$	$p \leftrightarrow \sim q$	$(p \leftrightarrow q) \oplus (p \leftrightarrow \sim q)$
T	T	F	T	F	T
T	F	T	F	T	T
F	T	F	T	T	T
F	F	T	F	T	T

{p, 1}

1.

a)

p	$p \wedge 1$
T	T
F	F

F	F	
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b) $P \mid P \vee F$

T	T
F	F

c) $P \mid P \wedge F$

T	F
F	F

d) $P \mid P \vee T$

T	T
F	T

e) $P \mid P \vee P$

T	T
F	F

f) $P \mid P \wedge P$

T	T
F	F

8

a) Kame will not take a job in industry and go to graduate school.

b) Yoshiko doesn't know Java or C++ (U/U)

c) Tom () is not young or

(then)

d) Rita will hit more to
Oregon and Washington.

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a) $p \wedge q \rightarrow p$

$p \mid q$	$p \wedge q$	$p \wedge q \rightarrow p$
T T	T	T
T F	F	T
F T	F	T
F F	F	T

$\therefore p \wedge q \rightarrow p$ always T

b) $p \rightarrow p \vee q$

$p \mid q$	$p \vee q$	$p \rightarrow p \vee q$
T T	T	T
T F	T	T
F T	T	T
F F	F	T

$\therefore p \rightarrow p \vee q$ always T

c) $\sim p \rightarrow (p \rightarrow q)$

$p \mid q$	$\sim p$	$p \rightarrow q$	$\sim p \rightarrow (p \rightarrow q)$
T T	F	T	T
T F	F	F	T
F T	T	T	T
F F	T	F	T

F	T	T	T
F	F	T	T

$\therefore \neg p \rightarrow (p \rightarrow q)$ always \top

d) $p \wedge q \rightarrow (p \rightarrow q)$

p	p	$p \wedge q$	$p \rightarrow q$	$p \wedge q \rightarrow (p \rightarrow q)$
T	T	T	T	T
T	F	F	F	T
F	T	F	T	T
F	F	F	T	T

$\therefore p \wedge q \rightarrow (p \rightarrow q)$ always \top

e) $\neg(p \rightarrow q) \rightarrow p$

p	q	$\neg(p \rightarrow q)$	$\neg(p \rightarrow q) \rightarrow p$
T	T	F	T
T	F	T	T
F	T	F	T
F	F	F	T

$\therefore \neg(p \rightarrow q) \rightarrow p$ always \top

f) $\neg(p \rightarrow q) \rightarrow \neg q$

p	q	$\neg(p \rightarrow q)$	$\neg q$	$\neg(p \rightarrow q) \rightarrow \neg q$
T	T	F	F	T
T	F	T	T	T
F	T	F	F	T
F	F	F	T	T

$\therefore \neg(p \rightarrow q) \rightarrow \neg q$ a tautology