STATISTICAL METHODOLOGIES

# FREQUENCY DISTRIBUTION



1. Such things as test scores, class rank, weight, and income, are called variables. Income, for instance, is called a variable because different income values are possible. In general, things that vary in value from case to case or time to time are called

#### 

#### VARIABLES

2. The number of times a particular value of a variable occurs is referred to as the frequency of that value. If 17 students receive a score of 70 on a test, then the score of 70 has a \_\_\_\_\_\_\_ of 17.

## 

## FREQUENCY

3. A distribution is a series of separate values such as scores which are ordered to magnitude. A group of ordered scores can make up a distribution. For example, a group of scores ranging from the lowest to the highest score is a \_\_\_\_\_\_ (see table).

# Scores 13 11 11 9 9 8 5

DISTRIBUTION

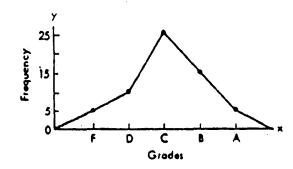
4. A set of ordered scores and their corresponding frequencies is called a frequency distribution. This can be represented in table or graph form. The table below shows the number of times a score occurs in its group. This table is a frequency

Scores	Frequency
13	Ĭ
11	11
9	111
8	1
- 5	I

# <u>ტეგატიიტინი პიტიტიტიტიტიტიტიტიტი</u>

#### DISTRIBUTION

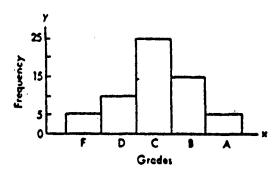
5. Frequency distributions can also be graphically illustrated. The two most common graphs used to illustrate frequency distributions are the frequency polygon and the histogram. If scores and their frequencies are illustrated with points connected by lines, it is called a frequency polygon. Because the illustration below shows the frequency of particular scores by the height of points that are connected by lines, it is called a frequency



<del>aanaadaaaaaaaaaaaaaa</del>aa

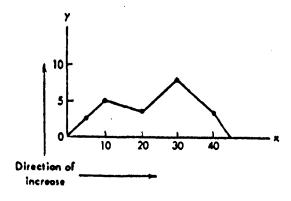
POLYCON

6. In a histogram frequency distribution, the scores and their frequencies are designated by the use of rectangular boxes. In the frequency distribution below, the height of the rectangular boxes indicates the frequency of students that received that particular score. It is called a



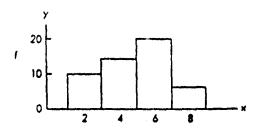
#### PISTOGRAM

7. It is the accepted practice for the vertical side of a graph, called the ordinate axis, to be used to designate the frequency. The horizontal side, called the abscissa axis, is used for the scores. Direction of increase is upward for the frequency on the ordinate axis. Direction of increase for the variable is from left to right on the \_\_\_\_\_\_ axis.



ABSCHIA

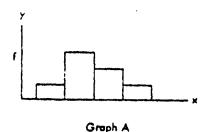
8. On this graph the f, which designates the frequency, is the \_\_\_\_\_ axis, and the x, designating the variable, is the \_\_\_\_\_ axis.

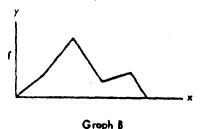


#### ORDINATE

## **ABSCISSA**

9. The two most common graphs used to illustrate frequency distributions are the frequency polygon and the \_\_\_\_\_\_ Graph A. is a \_\_\_\_\_ Graph B. is a \_\_\_\_\_





<del>nuaduancoc</del>nosconosco<del>nocococ</del>ocon

HISTUCRAM

MISTOCRAM

# AVERAGES

#### CENTRAL

11. In statistics there are several "averages" or measures of \_\_\_\_\_\_\_ in common use. Three of these are (a) the mean, (b) the median, and (c) the mode.

#### 

#### CENTRAL TENDENCY

12. The mean is generally the most familiar and most useful to us... The mean is computed by dividing the sum of the scores by the total number of scores. The formula for the mean would be

$$Mean = \frac{sum of the scores}{?}.$$

#### TOTAL NUMBER OF SCORES

- 13. Instead of stating that the mean is the sum of the scores divided by the total number of scores, it is easier to use the following symbols:
  - a. Mcan =  $\overline{X}$  read "X bar") or M. (The symbols  $\overline{X}$  or M are used when referring to the mean of a sample from the total population.)

b. Sum of the scores =  $\Sigma X$  ( $\Sigma = \text{sum}$ ; X = each score).

c. Total number of scores = N.

Thus the formula for the mean would be X = ?/?

14. Compute the mean  $(\overline{X} = \Sigma X/N)$  from the given information:

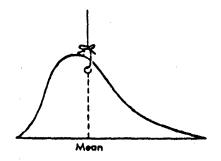
Sum of scores (XX): 7

Number of scores (N): 4

$$X = \frac{2}{3} = \frac{2}{3}$$

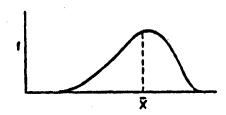
$$20/4 = 5$$

15. Finding the arithmetic mean of a distribution is analogous to finding the center of moment, or the balance point, in a solid block. If a distribution were suspended by the mean it would hang level or balanced. The mean, whose symbol is \_\_\_\_\_\_ is the center of moment in a frequency distribution.



X on M

16. Thus, if extremely high or extremely low scores are added to a distribution, the mean tends to shift toward those scores. If the center of balance of the distribution is shifted to one side or the other of the curve, the curve becomes "skewed." The following curve has a few extremely low scores. Consequently, this distribution is

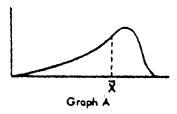


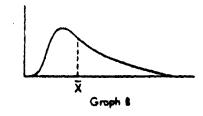
7.	Extreme scores,	either	high	or lo	ow,	tend	to	
	a distribution.							

STEEN STEEN

18. If a distribution is massed so that the greatest number of scores is at the right end of the curve and a few scores are scattered at the left end, the curve is said to be negatively skewed. If the massing of scores is at the left end of the curve with the tail extending to the right end, then the curve is positively skewed.

Graph A illustrates \_\_\_\_\_\_ skewness. Graph B illustrates \_\_\_\_\_ skewness.

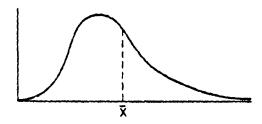




# PERSONAL PARTIES OF THE PROPERTY OF THE PERSONAL PROPERTY OF THE PERSON

# 

This graph's tail is extending to the right because of a few extremely high scores, therefore, it is \_\_\_\_\_\_ skewed.



A curve is symmetrical when one half of the curve is a reproduction of the other half. If you folded a frequency polygon at the mean and the two halves were similar, then the frequency distribution represented by the polygon would be said to be

# 

#### SYMMETRICAL

21. According to the formula for computing the mean (X = XX/N), we can define the mean as the arithmetic average of the scores in a distribution. If we added extreme scores to one end of a previously symmetrical curve, the mean would shift towards those extreme scores. Would the curve be symmetrical or not symmetrical?

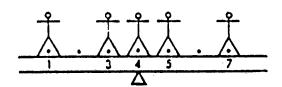
ROBERTO CONTROL CONTRO

22. Regardless of whether the curve is symmetrical or asymmetrical, the mean is always the center of balance. Does this imply that the mean is centrally located in asymmetrical curves?

NO

23. Let us illustrate this point by placing a distribution along an interval scale such as that below. Each figure represents one person. The scale would obviously balance if a fulcrum were

under the middle number, 4. Calculate the mean by the formula  $X = \Sigma X/N$  to verify this. Was this distribution symmetrical?



## <del>00000000000000000000000000000000</del>

X = 20/5 = 4

# 

TE

L	•			of 7 had gotten 12, what would b			
	balance po	oint of	the scale	below.	is the fulc	rum centrall	y lo
	<u>.</u>	ŢŢ	-	•		<u>,</u>	

-5

pulcrum should be under number 5

<del>აგგაიტეცი</del>ებიტებილ<mark>ების გაგ</mark>ები

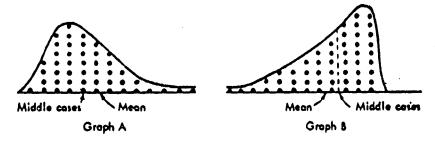
NO

20

25. What would be the mean for the above distribution if the person who scored 12 had instead scored 22?

7

26. When a curve is positively skewed (see graph A) the mean is located to the \_\_\_\_\_\_ (right or left) of most of the cases. When a curve is negatively skewed (see graph B) the mean is located to the \_\_\_\_\_ of most of the cases. (Each dot is one case.)



RICHT

LEFT

27. If the measures 2, 2, 3, 3, 15 were a frequency distribution, the curve would be \_\_\_\_\_\_ skewed.

POSITIVELY

<b>28</b> .	The preceding distribution of 2, 2, 3, 3, 15 has a mean of 5. What will the mean be if 10 points are added to the score of 15 (making it a score of 25)?
	5 <i>000</i> 000000000000000000000000000000000
29.	We saw that by adding 10 points to the score of 15, the mean of the distribution 2, 2, 3, 3, 15 was raised by 2 points. The reason for this is that the mean is an arithmetic average and each score contributes to its value. When 10 was added it was averaged or distributed equally among the five scores. This has the same effect as adding a constant of 2 points to each score (10 points/5 scores = 2 points per score). When 2 points are added to each score, the mean is raised by points (from 5 to 7).
	<del>იიაიიია</del> იიიიიი <del>იაიიიიიიი</del> ი <del>იაიი</del>
	2
30.	When a constant is added to each score of a distribution, that constant is added to the previous mean to find the new mean. If each score of a distribution is multiplied by a constant, the new mean is found by multiplying the old mean by that
	<del>000<b>000000000000000000000000</b>0000</del>
	CONSTANT
31.	The distribution 0, 2, 2, 3, 13 has a mean of 4. What would the mean be if each score was multiplied by a constant of 2?

# MEDIAN

32. By adding or substituting an extreme score to a distribution, the mean no longer represents a centrally located score but represents a measure that is more typical of the extreme score.

This causes us to rely on another measure of central tendency which is called the median or the middle score. The median is abbreviated Md or Mdn. The measure of central tendency that is less affected by the addition of an extreme score is the

# <del>pac<mark>ae co co co</mark> co co</del>

#### MEDIAN

33. The median is a point on a scale of measurement above which are exactly half the cases and below which are the other half of the cases. The student should note that the median is defined as a point and not as a specific measurement, e.g., a score or a case. From the distribution 4, 6, 8, 10, 12, it is easy to see that 8 is the middle score. The score of 8 is at the point where there are two scores above and two scores below, hence, 3 is the median. What is the median of 11, 11, 14, 19, 19?

14

34. To obtain the median, the measures are arranged in ascending order from the lowest to the highest measure. Then by count-

ing up this scale, the point is selected where there are an equa number of cases above this point and an equal number of case
below this point. The value of this point is the middle or the
case.
9 <del>9000</del> 09 <del>0000000000000000</del> 0
MEDIAN

35. The median of the distribution 3, 2, 0, 1, 6 can be found by first arranging the measures from the lowest to the \_\_\_\_\_\_ number (0, 1, 2, 3, 6). Then we find the middle score or case, which is \_\_\_\_\_, and that is the median.

HICHEST

2

38. It is not too difficult to determine the median of a distribution with an odd number of cases—if providing the score at the midpoint has a frequency of 1. In the distribution 3, 5, 7, 9, 11, 13, 13, the median score, which is \_\_\_\_\_\_\_ has a frequency of 1. The score of 13 has a frequency of \_\_\_\_\_\_

9

<del>99999999999999999999999</del>

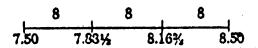
9

37. A distribution whose midpoint score has a frequency greater than 1 (e.g., 5, 6, 9, 9, 9, 11) presents a special problem. To overcome this, the student needs to know what is meant by "the interval of a score." For our purposes, the interval of a score ranges from 5 unit below a given score up to 5 unit above a given score. For example, the score of 9 includes all values within the limits of 8.5 up to 9.5. The exact midpoint of the interval whose lower and upper limits are 8.5 and 9.5, respectively, is 9. The score of 17 would represent the interval from 16.5 up to

# 

17.5

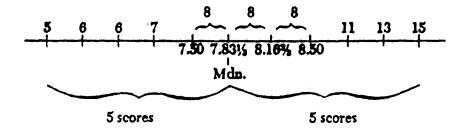
38. In the distribution of 5, 6, 6, 7, 8, 8, 8, 11, 13, 15, the score of 8 has a frequency of \_\_\_\_\_\_\_ The score of 8 has an interval range from 7.5 up to \_\_\_\_\_\_ It is assumed that the unit of three scores (8, 8, 8) is spread equally through the interval of 7.5 to 8.5. Each 8 occupies 1/2 (0.331/2) of a unit. For example:



3

R.5

39. The midpoint of the distribution 5, 6, 6, 7, 8, 8, 8, 11, 13, 15, where half the scores are on one side and half the scores are on the other, is between the fifth and \_\_\_\_\_\_\_ score. Below the interval 7.5 to 8.5 there are four scores, consequently the fifth score extends ½ of the way into the three score unit. Thus, the point between the fifth score and the sixth, which is the \_\_\_\_\_\_ is found by adding ½ of the unit to 7.5 (7.5 + .33½ = 7.83½). Note the illustration:

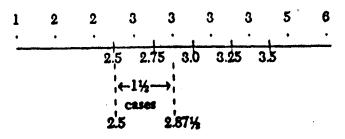


**concens**e en concense en conc

SIXTU

#### MIDPOINT OR MEDIAN

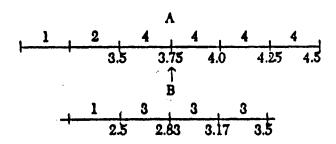
40. The distribution 1, 2, 2, 3, 3, 3, 3, 5, 6 has nine cases. The median of these nine cases is a point which has 4.5 cases below it and cases above it. This midpoint falls within a four-case unit. Below the lower limit of 3 (which is 2.5) there are three cases; therefore by extending one and one-half cases into the interval of 2.5 to 3.5 we can locate the median. Each 3 accounts for one-fourth of the four-case unit, hence one and one-half cases is equal to % plus % of a unit (0.25 + 0.12%). The



4.5

2,871/<sub>2</sub>

41. The same principle applies to distributions with even numbers of cases except that the median falls midway between the two middle cases. For example in distribution A, shown below, the arrow indicates the median. Draw an arrow to indicate the median of distribution B.



2,83

42. The distribution 40, 43, 44, 45, 48, 53, 56, 60 has eight cases. The median is a point midway between the fourth and

45.0		oted in the ill Md			18.0
<del>-+-</del>	45.5	46.0 46.	47.0 5	47.5	-+-
	000000	coocoquesa	00000000	000000	
		FIFT	TILE .	•	
	00000	0000000000	) <b>0 0 0 0 0 0 0 0</b> 0	000000	
		47.	5		
				~ —	
case. The limit of 1	upper lin	tween the nit of 12 is	and a	midway b	nd the lower etween these
case. The limit of 1 two limits	upper lin	nit of 12 is	and a	midway b	and the lower etween these the median
case. The limit of 1 two limit	upper lin  14 is  s is the po	nit of 12 is	and a	midway b	nd the lower etween these
case. The limit of 1 two limit Note the	upper lin  14 is  s is the po  illustration	nit of 12 is	and a	midway be which is	and the lower etween these s the median
case. The limit of 1 two limit Note the	upper lin  14 is  s is the po  illustration	nit of 12 is wint on:	and 1	midway be which is	and the lower etween these s the median
case. The limit of 1 two limit. Note the	upper lin 14 is s is the po illustratio	nit of 12 is on:	and 1	nidway be , which is 14.0	and the lowe etween these the median
case. The limit of 1 two limit. Note the	upper lin 14 is s is the po illustratio	nit of 12 is on:  12.5	13.5	nidway be , which is 14.0	and the lowe etween these the median
case. The limit of 1 two limit. Note the	upper lin 14 is s is the po illustratio	nit of 12 is on:  12.5  13	13.5 .0	nidway bo , which is	and the lowe etween these the median
case. The limit of 1 two limit. Note the	upper lin 14 is s is the po illustratio	nit of 12 is on:  12.5  13	13.5 .0	nidway bo , which is	nd the low etween the sthe media
case. The limit of 1 two limit. Note the	upper lin 14 is s is the po illustratio	nit of 12 is on:  12.5  13	13.5 .0	nidway be which is	nd the lowe etween thes s the mediar

**????????????????????????????????** 

44.	The values of the median as a method for obtaining the most typical measure of central tendency is a skewed distribution becomes even greater the more extreme the end score is. For example, the median of 0, 6, 9, 10, 10 is The contract of the left of
	mean of this distribution is 7 (i.e., 35/5). If one of the 10's substituted by the extreme number 55 (the new distribution would be 0, 6, 9, 10, 55), the median remains
,	but the mean is now
	9

45. The mean and median will both be affected if the score of 55 is added to the distribution 0, 6, 9, 10, 10. The new distribution would be 0, 6, 9, 10, 10, 55. The mean is 90/6 = 15. The addition of the extreme score shifted the value of the mean 8 points to the right. How far to the right was the median shifted?

Which measure of central tendency was affected the least?

**¢¢¢¢¢¢¢¢¢¢¢¢¢¢¢**¢¢¢¢¢°°

5 or one-half of a point

ACDIAN

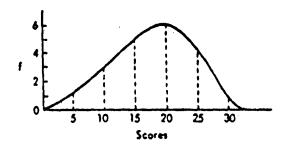
46. When we want to minimize the effect of one or more extreme
scores, we should use the to represent the
average score of the distribution.
\$\frac{\partial \text{constraints}}{\text{constraints}} \text{constraints} constrai
MEDIAN
47. The median, for both odd and even number of cases, is the point
on a distribution where there are an equal number of cases
above and that point.
990900000000000000000000000000
BELOW
MODE
MODE
46 4 432.1
48. A third measure of central tendency is the mode. It may be defined as the one value or score which occurs with the most
frequency. The mode of the series 2, 3, 4, 4, 4, 5, 5 is 4. The
mode of the series 7, 8, 10, 10, 10, 11, 11 is
The median is
<del>0000000000000000000000000000000000000</del>
10
00000000000000000000000000000000000000
**************************************

49. Is it possible for a distribution to have a median and a mode of the same value? \_\_\_\_\_\_ (yes or no)

ტიტიტიტიტიტიტიტ<del>იტიტიტიტიტი</del>

TE

50. The mode is used as a simple, inspectional "average" to show, in a hurry, the center of concentration of a frequency distribution. What is the mode or the rough average of the frequency polygon shows below?

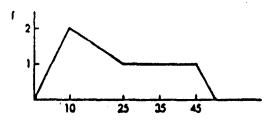


*₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲₲* 

20

51. The mode is not generally used unless there are a large number of cases in a distribution. When the number of cases in a distribution is small, there is a good possibility of several scores having the same frequency. The frequency polygon shown below is an extreme example. It is evident that the mode is 10 but it does not give a close approximation of the average case. The mean is 25 (IX/N = 125/5). The cases, in ascending order, are

10, 10, 25, 35, 45, with the number 25 at the midpoint; thus is the median.



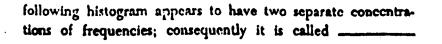
2!

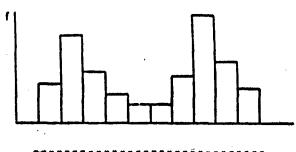
MODE

53. The mode is used also to be sure that the average you obtain exists in actuality. In finding the average size of automobile tire that is purchased, the mean or median size might be a tire that doesn't exist. Therefore, one would want to know the size of tire bought most often. This would be the \_\_\_\_\_\_.

MODE

54. In addition to serving as a measure of central tendency, the concept of modality is useful in describing the shape of some distributions. If a histogram or a frequency distribution has two peaks, it is referred to as a bimodal distribution. If a distribution has some than two peaks, it is called multimodal. The

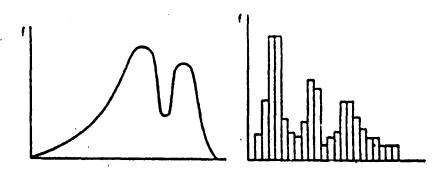




BIMODAL

55. The distribution of the frequency polygon illustrated below is

\_\_\_\_\_\_ The distribution of the histogram is \_\_\_\_\_\_ the frequency pologon is negatively skewed, whereas the histogram is \_\_\_\_\_ skewed.



**ᲝᲛᲛᲠᲛᲝᲛᲐᲛᲛᲠᲔᲑᲐᲛᲛᲝᲛ**Მ**ᲠᲛᲑᲐᲑᲑᲐᲛᲑ**Მ

BEMODAL

MULTIMODAL

POSTTIVELY

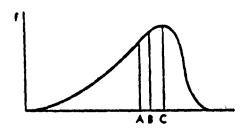
56. The score which occurs with the most frequency is the mode; hence the node is totally uninfluenced by extreme scores. The mean is greatly influenced by extreme scores. On the basis of these two statements and the preceding exercises on the median, it is evident that line A is the mode (it is totally uninfluenced by the extreme scores). Line B is not affected as much as line C, thus it must be the \_\_\_\_\_\_\_ Line C is the \_\_\_\_\_\_\_; it was influenced the most by the extreme scores.

57. The frequency distribution below is \_\_\_\_\_\_skewed.

Line A is the \_\_\_\_\_ Line B is the \_\_\_\_\_

Line C is the \_\_\_\_\_ The mean of a negatively showed distribution is located left of the center. The

me in of a positively skewed distribution is located \_\_\_\_\_\_\_ of the center.



##CATIVELY

MEAN

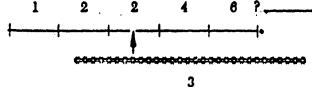
<del>\$60000000000000000000000000000</del>

MEDIAN

MODE

RICHT

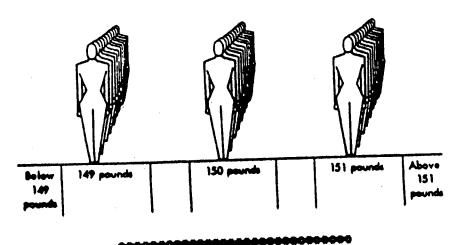
58, What are the mean, median, and mode of the distribu



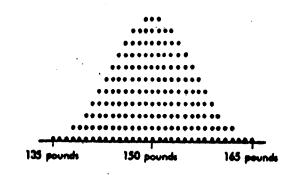
3

<b>59</b> .	The mean, median, and mode have been discussed as averages						
	It should now be evident why these three statistical tools are						
	called measures of						

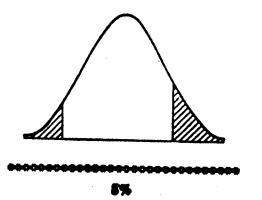
# THE NORMAL CURVE



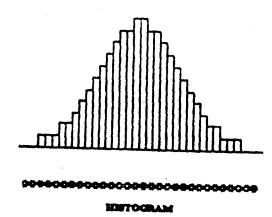
61. From an airplane, the place where this odd event was occurring might look like the diagram below. Each dot represents a



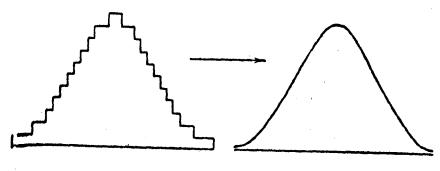
# PERSON OR STUDENT



#3. If each column of students is represented by a rectangular box, we have our old friend the



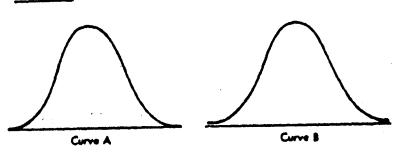
134. If we have a very large number of people and use very small weight categories, the irregular step-like curve would become smooth and continuous. The resulting figure approaches a special type of curve called the normal curve. In frequency distributions normality is not associated with small groups of people but rather with very \_\_\_\_\_\_ groups of people.



LABOR

135: In a normal curve (which by definition describes an infinite number of cases) the tails of the curve never touch the baseline.

Which curve below could be a true normal curve?



# 

E

66. It has been found that quantitative data gathered from highfrequency random measurements of natural phenomena and of many mental and social traits, even though not precisely normal in distribution, can be closely described by the normal

# <del>ຬຐຨຨຌຐຐຐຨຌຨຌຨຨຩຨຨ</del>ຨຩຬຓຓຨຨຨຨຨຨຨຨ

#### CURVE

67. The distributions of such diverse properties as achievement test scores, I. Q., and height and weight of people form approximately \_\_\_\_\_\_

# <del>00000000000000000000000000000</del>

### NORMAL CURVES

68. The end points of a normal curve remain open and recede indefinitely so as never to touch the abscissa or base line because the number of cases has to be

# 

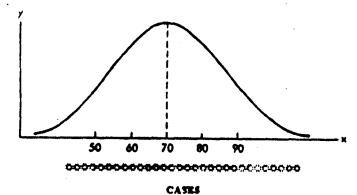
DOPINITE

69. When a line approaches infinitely close to another line but does not touch that line, the lines are said to be asymptotic. The end points of a normal curve are \_\_\_\_\_\_ to the base line.

# <del>100400000000000000000000000000000</del>

#### ASTMPTOTIC

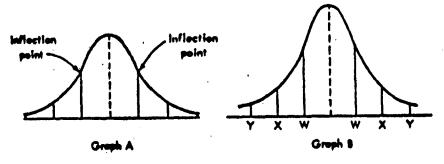
- 70. The bell-shaped curve illustrated below approximates what the statisticians call a normal curve. Note the following properties:
  - a. It is symmetrical.
  - b. The mean, median, and mode have the same value (in this instance, 70).
  - c. There are thus an equal number of scores on either side of the mean (central axis).
  - d. It is composed of infinitely large numbers of
  - e. The end points of the curve are \_\_\_\_\_\_ to the abscissa (base line).



## ASTMPTOTIC

71. Another identifying characteristic of the normal curve is its mathematical construction. There are two points on the normal

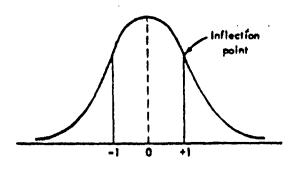
curve where the curve changes direction from convex to concave. These points are points of inflection (see graph A). Are the inflection points on graph B at line W, line X, or line Y?



# <del>qqquqqqqqqqqqqqqqqqqqqqqqqq</del>

#### LINE W

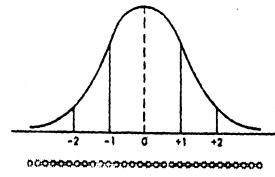
72. By the methods of calculus it can be shown that a line drawn perpendicular from the point of inflection to the abscissa is one unit of distance or deviation from the central axis. If one uses this distance as a standard, a uniform method of dividing the base line into equal segments can be established. If the central axis is designated as zero, the line one unit of distance to the right would be plus and the line one unit of distance to the left would be



**0000000000000000000000000000**00000

MINUS

73. Mathematically, the lines -1 and +1 are situated one unit of distance or deviation from the central axis or values (the mean, median, and mode). These two lines are designated as ±1 (read as plus and minus one). Two units of distance or deviation from the central axis are labeled as +2 and \_



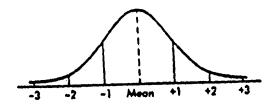
74. Using the unit of distance established by constructing a perpendicular line from the point of inflection to the abscissa as a standard, we can divide the base line into several equal segments. Since the normal curve is asymptotic with respect to the abscissa, one could divide the base line into equal parts indefinitely. All segments would be a uniform or standard distance. The unit of distance was established by constructing a perpendicular line from the point of \_\_\_\_\_\_ to the abscissa.

# *იტები და გაციანი და გაციანი და გაციანი და გაციაციაციაციაციაცია გაციანი და გაცია*

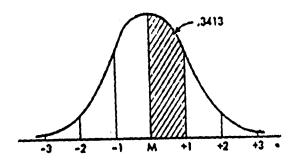
#### INFLECTION

75. The proportion of cases beyond ±3 units from the center of the normal curve is so small that they are generally ignored. It is thus common practice to illustrate only those cases contained between the arbitrary limits of +3 and \_\_\_ units of deviation.

76. Notice that in the graph below each divided segment is equal to the distance from (or the deviation from) the mean to the perpendicular line drawn from the \_\_\_\_\_ point.

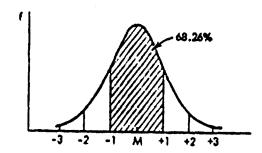


77. The total area under the normal curve may be set to equal 1 or unity. Between the mean and +1 unit of deviation above (to the right of) the mean is .3413 (about 1/3) of the total area, i.e., from the mean to +1 unit of deviation lies 34.13% of the total cases. Since -1 unit of deviation is proportionate to +1 unit of deviation, \_\_\_\_\_\_s of the total cases lie between -1 unit of deviation and the mean.

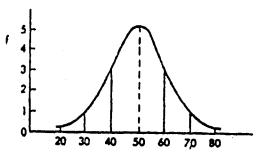


ტენი მის ან ან ან ან ანი მის ა 34.13%

78. Because of the massing of scores around the central values, a little more than % (2  $\times$  34.13% = 68.26%) of the total frequencies are between +1 and -1 deviations. If a normal distribution has a total frequency of 1000 scores, approximately 341 scores (34.13% × 1000) are located between the mean and -1 unit of deviation and approximately 341 scores are located between the mean and +1 unit of deviation. How many scores are located between -1 deviation and +1 unit of deviation?



683 (682.6)



<del>0304000003300000000000000000000</del>

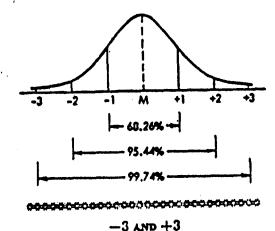
6S.26% on 68%

<del>6939999999999999999999</del>

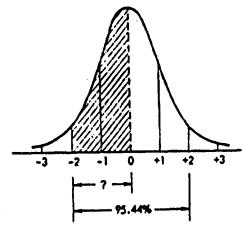
60

80. Although the normal curve extends indefinitely to the left and to the right, the end neints of the curve approach the base line as

closely that over 95.44% (see graph below) of the area or frequencies are neluded between the limits -2 and +2 and 99.74% of the passes are included between the limits - and + \_\_\_\_\_



81. The percentage of cases contained between the mean (central axis) of a normal curve and +3 units of deviation is 49.87% (one-half of 99.74%). The percentage of cases between the central axis (the mean) of a normal curve and -2 units of deviation is



47.73%

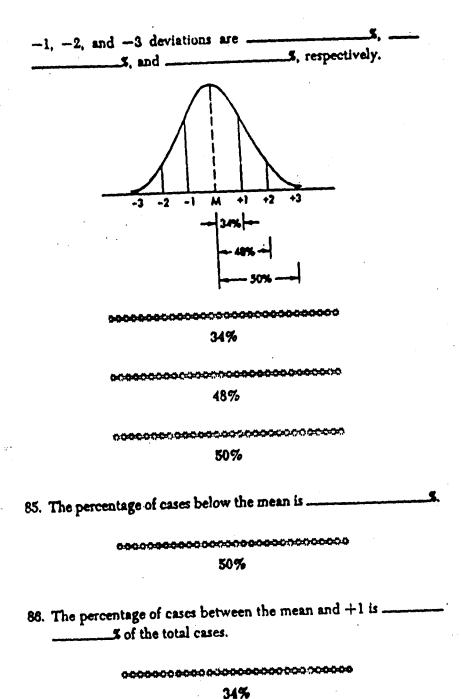
82. As we stated before, for practical purposes the limits of the frequencies of the normal curve rarely exceed those of ±3 units of deviation from the mean. The approximate twenty six hundredths of one percent (.0026) of the total cases existing outside the limits of ±3 are so slight in amount that the unity of the curve is generally assumed to be unaffected. Approximately thirteen hundredths of one percent (.0018) of the total cases extend beyond +3 and approximately hundredths of one percent of the total cases extend beyond -3.

# TERRITEIN

83. Though the percentage of cases is very small and insignificant at a considerable distance from the mean (beyond ±3) the proportion of frequencies approaches zero but never equals zero. The reason is that the normal curve is \_\_\_\_\_\_ with respect to the abscissa or base line.

# ASYMPTOTIC

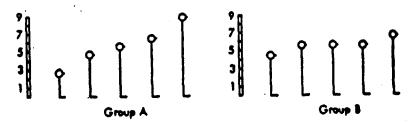
84. Since the proportion of the total cases that exist beyond the limits of ±3 is so slight, it may be plausible to treat data as if 100% of the total cases fall within ±3 deviations. If one makes this assumption, the percentage of cases is rounded off to the nearest whole percent. Thus (note graph below) the percentages of cases from the mean to +1, +2, and +3 are 34%, 48%, and 50%, respectively. The percentages of cases from the mean to



	•
3-1%) of the	ntage of cases below +1 deviation is 84% (50% plus total cases and the percentage of cases above +1 s% of the total cases. The per
centage of	cases below -1 deviation is
	<del>000000</del> 000000000000000000000000000000
	16% (100% — 84%)
	999999999999999999999999
	16% (50% — 34%)
centage of	to the scores on the graph below, about what per- cases lie below 43? Between
43 and 57?	Below 57? Between
Above 57?	Below 29?
ä	29 36 43 50 57  ***********************************
	<del>2000000000000000000000000000000000000</del>
	# /7

# VARIABILITY

89. Descriptions of groups by frequency distributions, central tendency, and normality have been discussed. Another way of describing a group is to have some index of how much variety exists. Consider the height of the two groups of people below. Both groups have a mean and median of 6 feet but the most variable is group



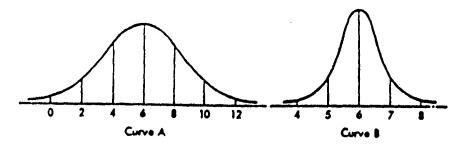
<del>ροσουμαρουκτουοοσομουσουνου</del>σος **σκ**ουν **Λ** 

90. One common measure of variability is the range. The range of a set of scores is the distance between the midpoints of the lowest and highest scores. To find the range, subtract the lowest score from the highest score. The range of group A whose heights are 3, 5, 6, 7, 9 is 9 minus 3 or 6. The range for less variable group B whose heights in fect are 5, 6, 6, 7 is \_\_\_\_\_\_

2 (or 7 minus 5)

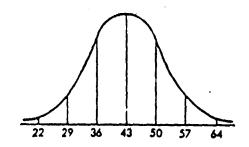
91. If the normal curves below, in which the vertical deviation lines are one standard unit apart, represent large populations,

which curve represents the most variable group?



curve A

92. The distance from one deviation line to another is the other major index of variability. It is called a standard deviation. In the diagram below, 29 differs from 43 by two



STANDARD DEVIATIONS

93. When members of a group deviate very little from each other, the standard deviations are very small. The reverse is true for

highly variable groups. Consequently, the variability or diversit of two groups can be compared by the relative size of their

# \_<del>ტენტებებატიდინის განტები</del>

#### STANDARD DEVIATIONS

94. The capital letters S.D. are used when referring to the standar deviation of a sample of a population. It is common practic to symbolize the standard deviation by the small Greek letter sigma (\sigma) when referring to the population values. To abbreviate a sample's standard deviation, one could use the capital letter.

To abbreviate the standard deviation for population, use the small Greek letter.

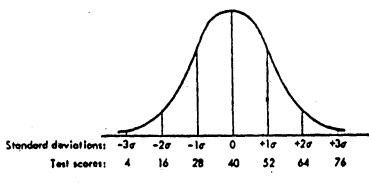
# 

S.D.

# <del>86088696262696969696969</del>

O OR SIGMA

95. Suppose that a population of scores is distributed so that tile mean is 40 and the distance of 12 points is 10 (read as our standard deviation). The students one standard deviation about the mean received the score of



<del>000000000000000000000000000</del>

52

96. What is the difference, in score points, between the scores of +1\sigma and -2\sigma of the above illustration? 

 $36 (3 \times 12)$ 

97. The standard deviation is a kind of average of all the deviations from the mean score. The amount a score (X) deviates from the mean (X) is symbolized by the small letter x, that is, X - X = x. Give the symbols for the following:

Raw score

Mean \_\_\_\_

Deviation \_\_\_\_

**შანიტები და გადიტი მინიტი გატატიტიტი** 

98. To calculate a standard deviation, the deviations from the mean have to be squared. To square a number, you multiply it by itself, For example, 5 squared, or  $5^2$ , =  $5 \times 5 = 25$ ;  $2^2 =$ \_\_\_\_\_

<del>შიინის და განამის და განამის და გაცი</del>ი

99. A minus times a minus equals a plus, therefore, (-4)<sup>s</sup> or  $-4 \times -4 = 16$ , Complete the following:

 $(-3)^{5} + (-1)^{2} + (-1)^{3} + 5^{3} =$ 

100. The opposite of squaring a number is taking a square root. The square root of 25 or  $\sqrt{25} = 5$ ;  $\sqrt{16} =$ 

101. When some arithmetic occurs inside a square-root sign, work the arithmetic before taking the square root.

$$\sqrt{1+3} = \sqrt{4} = 2$$

$$\sqrt{\frac{5^2+7}{2}} = \sqrt{\frac{32}{2}} = \sqrt{16} = \frac{2}{\sqrt{4}} = \sqrt{\frac{2}{4}} = \sqrt{\frac{2}{4}$$

Note: When we take the square root of a number, both positive and negative roots occur; but we are concerned only with the positive roots.

 $\sqrt{36/4} = \sqrt{9} = 3$ 

102. Squaring, dividing and taking the square root are used in solving the formula for the standard deviation: S.D. =  $\sqrt{\Sigma r^2/N}$ . The symbol V directs a person to take the square

103

The formula for the standard deviation,  $\sqrt{\Sigma x^2/N}$ , can be executed in six steps:

- 1. Compute the mean (X).
- 2. Subtract the mean from each score to find the deviations from the mean  $(X \overline{X} = x)$ .
- 3. Square each deviation from the mean (x2).
- 4. Add the squares of the deviations ( $\Sigma x^2$ ).
- 5. Divide the  $\Sigma x^2$  by  $N(\Sigma x^2/N)$ .
- 6. Take the square root of  $\Sigma x^2/N$  ( $\sqrt{\Sigma x^2/N}$ ).

The steps above illustrate why the standard deviation is defined as the square root of the average of the squared deviations from the

# 

#### MEAN

104. To see how to calculate a standard deviation, let's assume a distribution of 0, 2, 2, 8. The mean (X) is 3.

$$X - X$$
 or x (deviations) = (0-3), (2-3), (2-3), (8-3)  
= -3, -1, -1,

 $x^2$  (squared deviations) = 9, 1, 1, \_\_\_\_

Ex2 (sum of squared

$$deviations) = 9 + 1 + 1 + \dots = \dots$$

<del>000000000000000000000000000</del>

5

25

<del>09000000000000000000000000000</del>0

$$25 = 38$$

105. We have found the sum of the squared deviations ( $\Sigma x^2$ ) to be 36. With an N of 4, the average of the squared deviations from the mean is  $\Sigma x^2/N = 36/4 = 9$ . The square root of the average of the squared deviations from the mean equals 1 standard deviation. That is, S.D. =  $\sqrt{\Sigma x^2/N} = \sqrt{36/4} =$ 

# 

3

106. Calculate the standard deviation for the distribution 1, 2,

a. 
$$X=4$$

b. 
$$(X - \overline{X})$$
 or  $x = (1-4), (3-1), (-1), (-1), (-1)$ 

e. 
$$\Sigma x^3/N =$$

f. S.D. = 
$$\sqrt{\Sigma r/N} = -$$

# 

2

107. Subtracting a constant from or adding a constant to all the raw scores of a distribution does not change the value of the stand-

	the standard deviation of 50-50, 52-50, 52-50, 58-50 or 0, 2, 2, 8 is
	Note: The formula used here for computing standard deviations is based directly on the definition of standard deviation. This formula was chosen because it best helps one understand the basic concept of standard deviation. If you have to calculate standard deviations of various data, consult a statistical methods book for the standard deviation formula most appropriate to your data.
	<del>0000000000000000000000000000000000000</del>
108.	The range is easier to understand and easier to calculate than the standard deviation but it has some serious disadvantages. Not much else can be done with the range. The standard deviation (and its square called the variance) is the basis of a whole branch of statistics. The measure of variation having the greater versatility is the
	<del>000000000000000000000000000000000</del>
	STANDARD DEVIATION
109.	The size of the range depends a good deal upon the size of the sample. There is more chance of simultaneously drawing a very high score and a very low score when the sample is larger. Consequently, range generally increases with an increase in the size of the
	*********

ard deviation. If the standard deviation of 50, 52, 52, 58 is 3.

110. Because all the scores are used in computing the standard deviation while only two scores (the highest and lowest) are used in computing the range, the standard deviation is much more stable than the range. The most stable measure of variability is the

# 

111. For example, a sample of 20 scores could be drawn at random from a population of 200 scores. The standard deviation and the range could now be calculated and the 20 scores returned to the population pile. If this process were repeated many times, the standard deviations would vary in size much less than would the \_\_\_\_\_\_.

RANCE

# INTERPRETING TEST SCORES

112. The number of correct answers that a person acquires on a test is called his raw score. Assuming that each question on a test counted one point, a raw score of 12 would mean that an individual answered \_\_\_\_\_\_ questions of the test correctly.

# NOMINAL, ORDINAL, AND INTERVAL SCALES

Often the methods used in analyzing or interpreting experimental data differ according to the measurement scale used. The nominal scale merely names categories, such as male-female, or successfailure, or Democrat-Republican-Independent. There may be any number of categories, but every item must be uniquely classified as belonging to one or another of them. If numbers are assigned, such as 1 = male and 2 = female, the numbers have no meaning as an actual numerical measure; in other words, it makes no sense to talk about 1.5 as being half-male and half-female. The ordinal scale is a (ranking) measure, such as private-corporal-sergeant, or first-second-third place in a race, or A-B-C-D-E in a grading scale. There still may be categories named, but with ordinal measure the categories now are ranked as being "better" or "worse," "higher" or "lower," etc. The interval scale is a true numerical measurement scale in which numerical differences have meaning, such as degrees for temperature, pounds for weight, feet for height, or counting measure for the number of redheads in a class. Sometimes it is difficult to classify certain observations as to measurement scale, and sometimes the classification will vary according to the context of the experiment. For example, the group assignment of children to reading groups would be nominal if the choice of any particular child for Group A, Group B, and so on wore made arbitrarily. However, if the children were assigned according to their reading ability, it would be ordinal, since it would rank them. If, after the children are assigned, we wished to count the number of children in each group, our counts would involve the interval scale.