

A Search for Higgs Decay to Pseudoscalar Higgs-like Particles at  
CMS

Samuel Higginbotham

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# Abstract

The Higgs boson was added to the Standard Model (SM) ten years ago, and since then, physicists have been using the Higgs as an integral part of research. Using the Higgs boson to probe for new physics phenomena is part of the high energy experimental frontier. At CERN, the Compact Muon Solenoid (CMS) gathers data from proton-proton collisions to push this frontier further. In this dissertation, a search is conducted for exotic decays of the Standard Model (SM) Higgs Boson,  $H$ , decaying to a pair of pseudoscalars,  $a$ , which then decay to pairs of muons and tau leptons. This search supports many beyond Standard Model (BSM) theories which could solve the  $\mu$  coupling problem in Super Symmetry and fit into Axion-like Models (Peccei-Quinn) and Grand Unified Theories (GUTs). Due to the model independent nature of this search, the SM is also tested. Pseudoscalar masses between 20 and 60 GeV are investigated using the full Run II dataset collected at CMS corresponding to a luminosity of  $137 \text{ fb}^{-1}$ . The existence of the pseudoscalar Higgs is primarily motivated by Two Higgs Doublet Models with the extension of a Singlet (2HDM+S). Upper limits on the branching fraction are set.

# Acknowledgements

thank

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# Chapter 1

## Introduction

### 1.1 The Standard Model and beyond

Comprising 18 particles and numerous interactions between their fields, the Standard Model provides a description of the fundamental interactions of nature. The Standard Model (SM) which is consistent with all empirical evidence is the leading theory of the universe.

Rather than providing a detailed description of the SM, the purpose of this introduction is to frame the analysis from a theoretical perspective. A table listing components of the SM appears below in figure 1.1.

Particles are represented by fields and interact within the theory. The simplest SM interactions of these fields are found by looking at the Dirac Lagrangian and then establishing  $U(1)$  interactions that have a conserved quantity (charge). Noether originally proved that local transformation symmetries imply conserved currents which has extensive implications for particle physics and theories that predict quantum numbers and conserved quantities, such as charge in the  $U(1)$  group [1].

After analyzing the  $U(1)$  group, one typically extends the theory to include more fields and structures through higher dimensional groups. The gauge principle will be examined for  $U(1)$  and then expanding to  $SU(2)$  before taking the product of these groups to form the Weinberg-Salam Model.

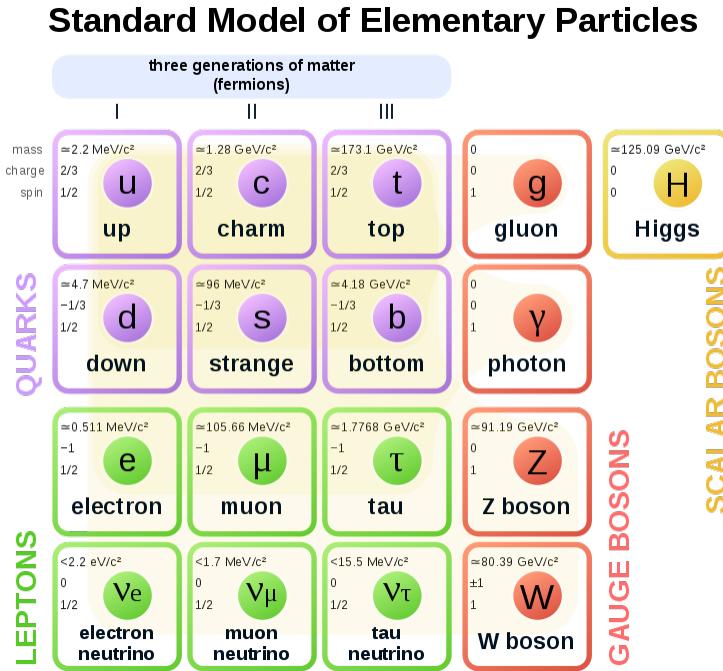


Figure 1.1: Standard Model particles

## 1.2 Gauge Principle, Yang Mills Theories, and the Weinberg-Salam Model

The gauge principle sets the stage for interactions between particle-fields in a theory. Much like in differential geometry and general relativity, there is a cost to interacting or changing through the action of a transformation. Consider the covariant derivative on a vector field  $V(x)$ .

$$\mathcal{D}_\mu V(x) \equiv \lim_{\Delta x^\mu \rightarrow 0} \frac{V_{||}(x + \Delta x) - V(x)}{\Delta x^\mu} \quad (1.1)$$

How the field changes under the transformation will determine the nature of the field. The connection terms that link the field follow from the transformation. A unitary operator can capture the parallel component in the covariant derivative. This operator carries the field and the *local* transformation law depending on the symmetries and complexity of the math structure that the unitary operator carries.

$$V_{\parallel}(x + \Delta x) = U(x + \Delta x)V(x + \Delta x) \quad (1.2)$$

After expanding the unitary operator, one can find the terms and phases that are carried under this transformation. For the  $U(1)$  group, these steps give the electromagnetic field tensor and charge

conservation. One defines the transformation and field, then works out the form of the covariant derivative and examines how the gauge field transforms [2]. To put it generally

$$\Psi' = U(\vec{x})\Psi \text{ particle under local transformation} \quad (1.3)$$

$$\mathcal{D}^\mu = \partial^\mu + igB^\mu \text{ covariant derivative} \quad (1.4)$$

$$B'^\mu = UB^\mu U^{-1} + \frac{i}{g}(\partial^\mu U)U^{-1} \text{ gauge field transform.} \quad (1.5)$$

For  $U(1)$  with a unitary transformation of the form  $U(x) = \exp \frac{ie}{2}Y \cdot \beta(x)$

$$\Psi'(x) = (1 + \frac{ie}{2}Y \cdot \beta(x))\Psi \text{ particle field with local transformation} \quad (1.6)$$

$$\mathcal{D}_\mu = \partial_\mu + ieA_\mu \text{ covariant derivative} \quad (1.7)$$

$$A^\mu \rightarrow A^\mu + \frac{1}{e}(\partial^\mu \beta) \text{ gauge field transform.} \quad (1.8)$$

Notably, the commutator between the covariant derivatives yields the practical field that it carries. For the  $U(1)$  case, it is the electromagnetic field tensor.

$$[\mathcal{D}^\mu, \mathcal{D}^\nu] \Psi = ieF^{\mu\nu}\Psi \quad (1.9)$$

These relations are important when higher dimensional groups and more complex particle fields are considered. Yang-Mills theories take these components and analyze them under groups like  $SU(2)$  or other special unitary groups. When one considers a local  $SU(2)$  transformation, the terms that show up are more rich than  $U(1)$ .

For  $SU(2)$  with a unitary transformation of the form  $U(x) = \exp \frac{ig}{2}\boldsymbol{\tau} \cdot \boldsymbol{\alpha}(x)$

$$\Psi'(x) = (1 + \frac{ig}{2}\boldsymbol{\tau} \cdot \boldsymbol{\alpha})\Psi \text{ particle field with local transformation} \quad (1.10)$$

$$\mathcal{D}_\mu = \partial_\mu - \frac{i}{2}g\boldsymbol{\tau} \cdot \mathbf{W}_\mu(x) \text{ covariant derivative} \quad (1.11)$$

$$\boldsymbol{\tau} \cdot \mathbf{W}_\mu \rightarrow \boldsymbol{\tau} \cdot \mathbf{W}_\mu + \frac{1}{g}\boldsymbol{\tau} \cdot (\partial_\mu \boldsymbol{\alpha}) - \boldsymbol{\tau} \cdot (\boldsymbol{\alpha} \times \mathbf{W}_\mu) \text{ gauge field transform.} \quad (1.12)$$

Now if we consider  $SU(2) \times U(1)$  and build states out of that and add a scalar field, the structure is there for the Weinberg-Salam Model.

### 1.3 The Higgs Mechanism

As mentioned in the previous section, taking the  $SU(2) \times U(1)$  groups with an additional scalar field and defining their local transformations give way to the interactions within the electroweak Weinberg-Salam model. The fields transform the same way as before; however, Higgs and others thought of adding a scalar field to the theory. In order to see the interactions with the scalar field, we need to see how it transforms.

$$\begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_3 + i\phi_4 \\ \phi_3 - i\phi_4 \end{pmatrix} \quad (1.13)$$

This scalar field transforms in the following way under  $U(1)$  and  $SU(2)$  transformations

$$\begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \rightarrow \begin{pmatrix} e^{ig\frac{\beta}{2}} & 0 \\ 0 & e^{ig\frac{\beta}{2}} \end{pmatrix} \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \quad U(1) \quad (1.14)$$

$$\begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \rightarrow e^{\frac{ig}{2}\tau \cdot \alpha} \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \quad SU(2) \quad (1.15)$$

$$\mathcal{D}_\mu \phi = \partial_\mu \phi - \frac{i}{2} g \tau \cdot \mathbf{W}_\mu \phi - \frac{i}{2} g' B_\mu \phi, \quad (1.16)$$

yielding the Higgs field Lagrangian component

$$\mathcal{L} = (\mathcal{D}^\mu \phi)^\dagger (\mathcal{D}_\mu \phi) + \frac{m_h^2}{2} \phi^\dagger \phi - \frac{\lambda}{4} (\phi^\dagger \phi)^2. \quad (1.17)$$

The Higgs potential contains the typical “Mexican hat” shape. The kinetic term holds interesting interactions and implications for the gauge bosons in the theory. All together the Weinberg-Salam model with the Higgs field is (with  $L$  and  $R$  being lefthanded and righthanded fermion fields) [3]

$$\mathcal{L} = \bar{L} i \gamma^\mu \mathcal{D}_\mu L + \bar{R} i \gamma^\mu \mathcal{D}_\mu R + (\mathcal{D}^\mu \phi)^\dagger (\mathcal{D}_\mu \phi) \quad (1.18)$$

$$\begin{aligned} &+ \frac{m_h^2}{2} \phi^\dagger \phi - \frac{\lambda}{4} (\phi^\dagger \phi)^2 - G_e (\bar{L} \phi R + \bar{R} \phi^\dagger L) \\ &- \frac{1}{4} G_{\mu\nu}^{(W)} \cdot G^{(W)\mu\nu} - \frac{1}{4} F_{\mu\nu}^{(B)} F^{(B)\mu\nu}. \end{aligned} \quad (1.19)$$

The Weinberg-Salam Model has major implications: the terms  $L$  and  $R$  along with their hermitian conjugates form an interaction with the Higgs field giving these fermions mass. This equation, along with the shape of the Higgs potential, imply spontaneous symmetry breaking and interactions that produce massive vector gauge bosons and massless photons.

## 1.4 Higgs Doublet Models

The Standard Model can naturally be extended by giving more complexity to the fields. Suppose that there were multiple scalar fields instead of just the single Higgs field  $\phi$ . Then one can consider adding another component, thus making it a doublet. Adding the doublet, and working out the relations for the field, creates the most general two-Higgs doublet model (2HDM) with the Higgs potential shown in equation 1.20 [4].

$$\begin{aligned} V = & m_1^2 |H_1|^2 + m_2^2 |H_2|^2 + \frac{\lambda_1}{2} |H_1|^2 + \frac{\lambda_2}{2} |H_2|^2 \\ & + \lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1^\dagger H_2|^2 \\ & + \frac{\lambda_5}{2} \left( (H_1 H_2)^2 + c.c. \right) + m_{12}^2 (H_1 H_2 + c.c.) \\ & + \left( \lambda_6 |H_1|^2 (H_1 H_2) + c.c. \right) \\ & + \left( \lambda_7 |H_2|^2 (H_1 H_2) + c.c. \right) \end{aligned} \quad (1.20)$$

Expanding around the minimum of the potential yields two doublets with vacuum expectation values  $v_1$  and  $v_2$ . They are usually mixed under a rotation parameter  $\tan \beta = v_1/v_2$ . After one carries out the interactions with the SM gauge bosons which consume the complex field components and a neutral pseudoscalar combination of scalar Higgs field components, the surviving three real degrees of freedom yield one neutral pseudoscalar mass eigenstate along with two neutral scalar mass eigenstates.  $A$  denotes the pseudoscalar,  $h$  the lighter neutral SM like Higgs, and  $H^0$  the remaining scalar. As with the notation for fields that interact with the potential, the rotation matrix that mixes these scalars into the components that interact under the potential is parametrized by the continuous parameter  $\alpha$

$$\begin{pmatrix} h \\ H^0 \end{pmatrix} = \begin{pmatrix} -\sin \alpha & \cos \alpha \\ \cos \alpha & \sin \alpha \end{pmatrix} \begin{pmatrix} H_{1,R}^0 \\ H_{2,R}^0 \end{pmatrix} \quad (1.21)$$

In the literature this parameter is important because  $\tan \beta$  and  $\alpha$  set the possible couplings to SM particles. Next, if a complex scalar singlet is added, couplings to SM fermions and bosons are supported [5].

$$S = \frac{1}{\sqrt{2}} (S_R + iS_I) \quad (1.22)$$

The scalar singlet doesn't have Yukawa couplings, but rather couples to  $H_{1,2}$ . Through its mixing with  $H_{1,2}$  the singlet can couple to SM fermions.

A possible coupling that preserves the SM Higgs by keeping  $\theta_a$  small could be defined as

$$a \equiv \cos \theta_a S_i + \sin \theta_a A, \quad \theta_a \ll 1 \quad (1.23)$$

This allows for decays like  $h \rightarrow aa \rightarrow X\bar{X}YY$ , where  $X$  and  $Y$  are SM fermions or bosons. Looking into the phase space where the mixing is small frames the Higgs pseudoscalar analysis in a region with little SM resonance—making it also a general search for any beyond SM (BSM) phenomena. There are terms in the effective Lagrangian that support the  $h \rightarrow aa$  decays:

$$\begin{aligned} \mathcal{L} &\subset g_{hAA} hAA + \lambda_S |S^2|^2 \\ &\subset g_{hAA} \sin^2 \theta_a haa + 4\lambda_S v_s \sin \zeta_1 \cos^2 \theta_a haa \end{aligned} \quad (1.24)$$

here  $\zeta$  is just the angle that mixes the singlet with the SM Higgs (needed because of the added state). These interactions give rise to different scenarios that favor certain SM fermions and bosons. According the literature, four distinct scenarios are typically entertained. The scenarios, supported by the effective Lagrangian 1.24, yield branching fractions as a function of  $a$ -mass and  $\tan \beta$ . These are enumerated below:

- Type I: Fermions couple only to the  $H_2$  field and are independent of  $\tan \beta$ , pseudoscalar coupling are proportional to the SM Higgs (final state of the fermions) represented in figure 1.2.
- Type II: Down-type fermions are particularly favored supporting more NMSSM models and is dependent on  $\tan \beta$  represented in figure 1.3.
- Type III: Branching ratios are directly dependent on  $\tan \beta$  and are emphasized when more than one lepton is considered.  $\tau^+ \tau^-$  can dominate in this scenario represented in figure 1.4.
- Type IV: Dependent on  $\tan \beta$ , for  $\tan \beta < 1$ , branching ratios for  $b\bar{b}$ ,  $c\bar{c}$ , and  $\tau^+ \tau^-$  are similar (supports  $2b2\tau$ ) represented in figure 1.5.

## 1.5 Previous and present searches in 2HDM+S models

As shown in the previous section, the Higgs couples to all massive SM particles and also to new particles provided that the new particles have mass. BSM theories contain ample room for the

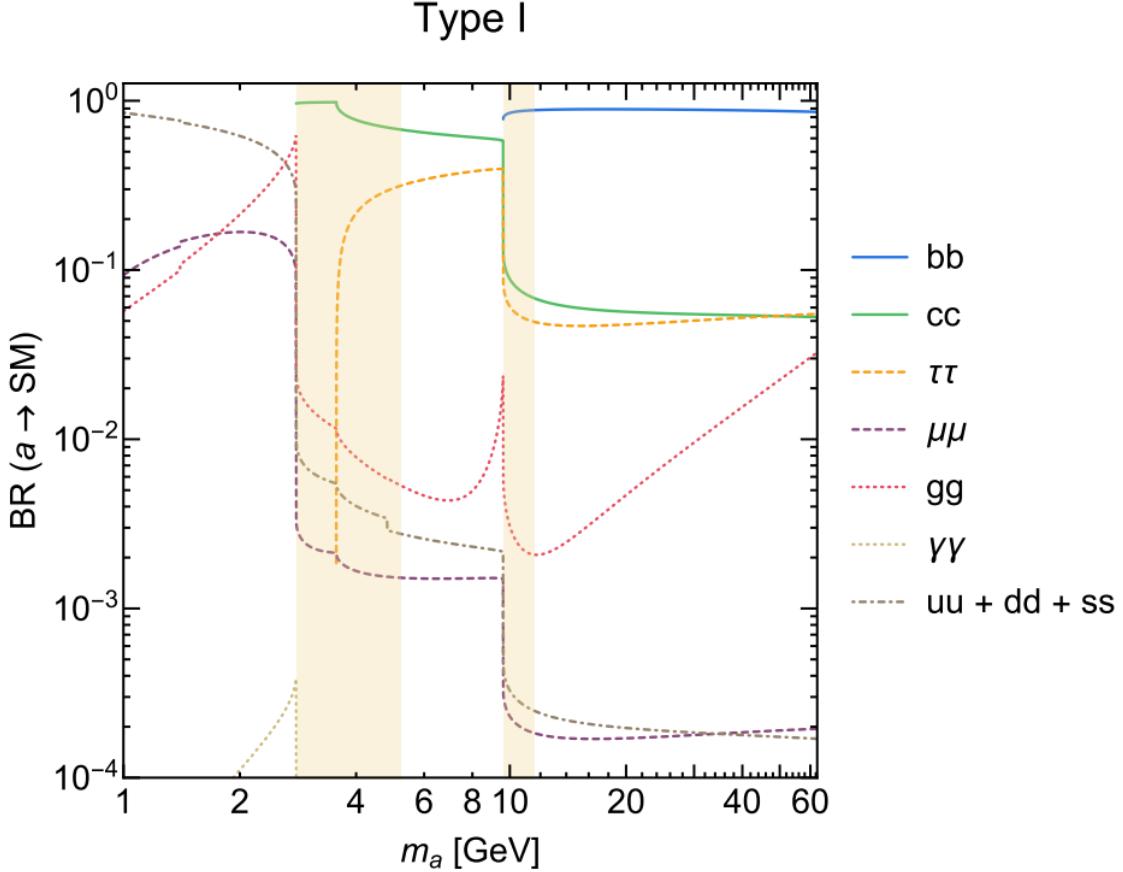


Figure 1.2: Type I 2HDM+S scenario branching fractions [4]

Higgs to couple to new particles, making the Higgs an excellent window to investigate any physics beyond the SM. Notably, the two Higgs doublet model (2HDM) with its extension of a scalar singlet is considered (2HDM+S). These types of BSM theories can solve the  $\mu$  coupling problem in Super Symmetry (SUSY), while maintaining general support of SUSY (Holomorphy), Axion-like Models (Peccei-Quinn), electroweak baryogenesis and several Grand Unified Theories (GUTs) [4].

A representative diagram showing the physics process and the branching ratio as a function of  $\tan\beta$  is shown in figure 1.6. This pseudoscalar Higgs search for “resolved”  $a$  particles in the range of 20 to 60 GeV is a good search for new physics. In 2016 this general search was carried out with  $35.9 \text{ fb}^{-1}$  of data, and new competitive limits were set in reference [6].

Given the potential for improvements in the limits for different 2HDM+S types, extending this search using the full RunII dataset is motivated.

The branching ratios change based on the function of  $\tan\beta$  depending on the type of model under investigation. In particular, we look at types I-IV. Type III is expected to be most sensitive

as it maintains a larger branching ratio compared to other decay modes over the range of the pseudoscalar masses when focusing on the final state of two muons and two tau leptons. In addition to the search for this model, any deviation from the SM prediction in the effective mass range would also be found.

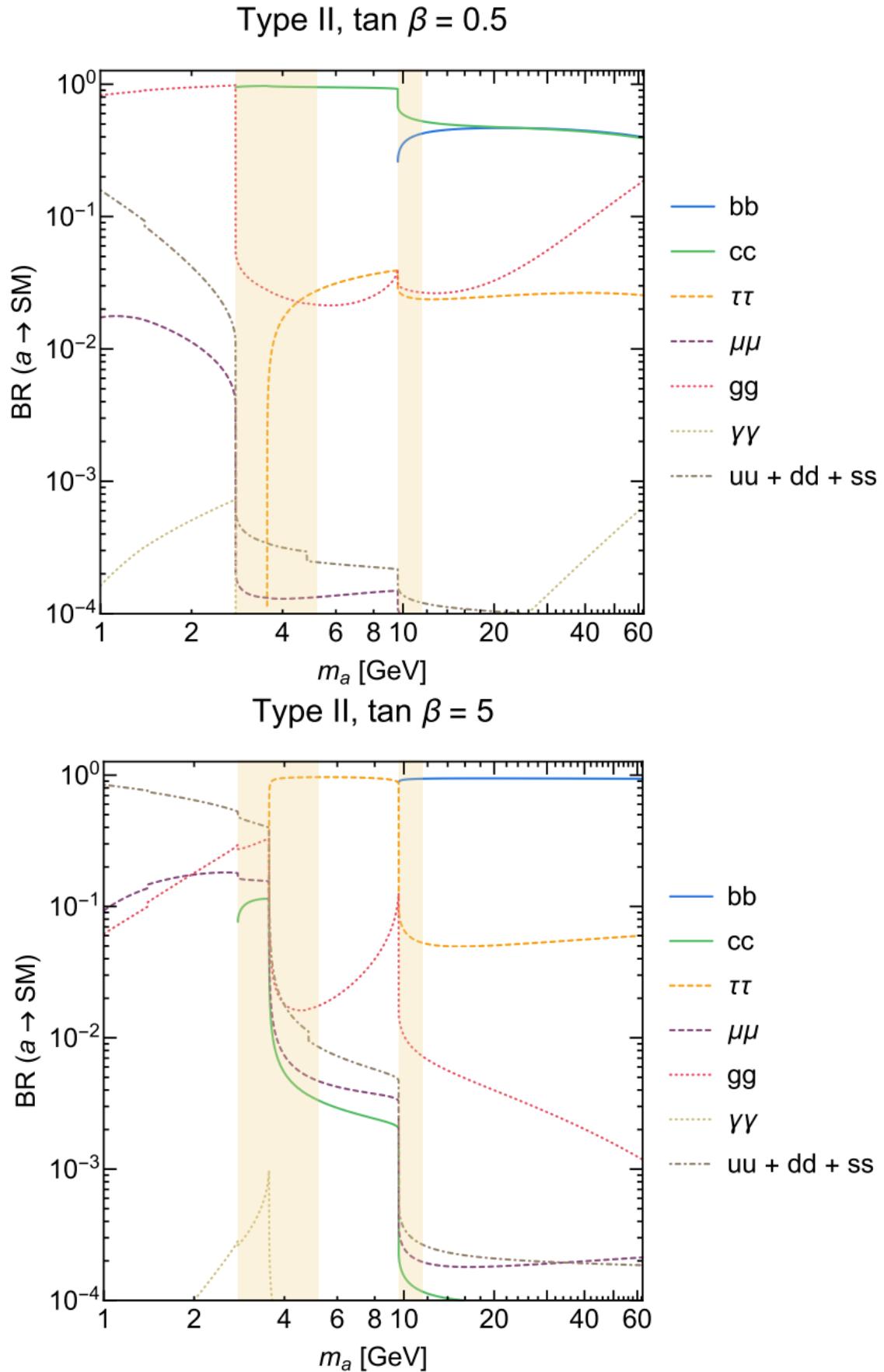


Figure 1.3: Type II 2HDM+S scenario branching fractions [4]

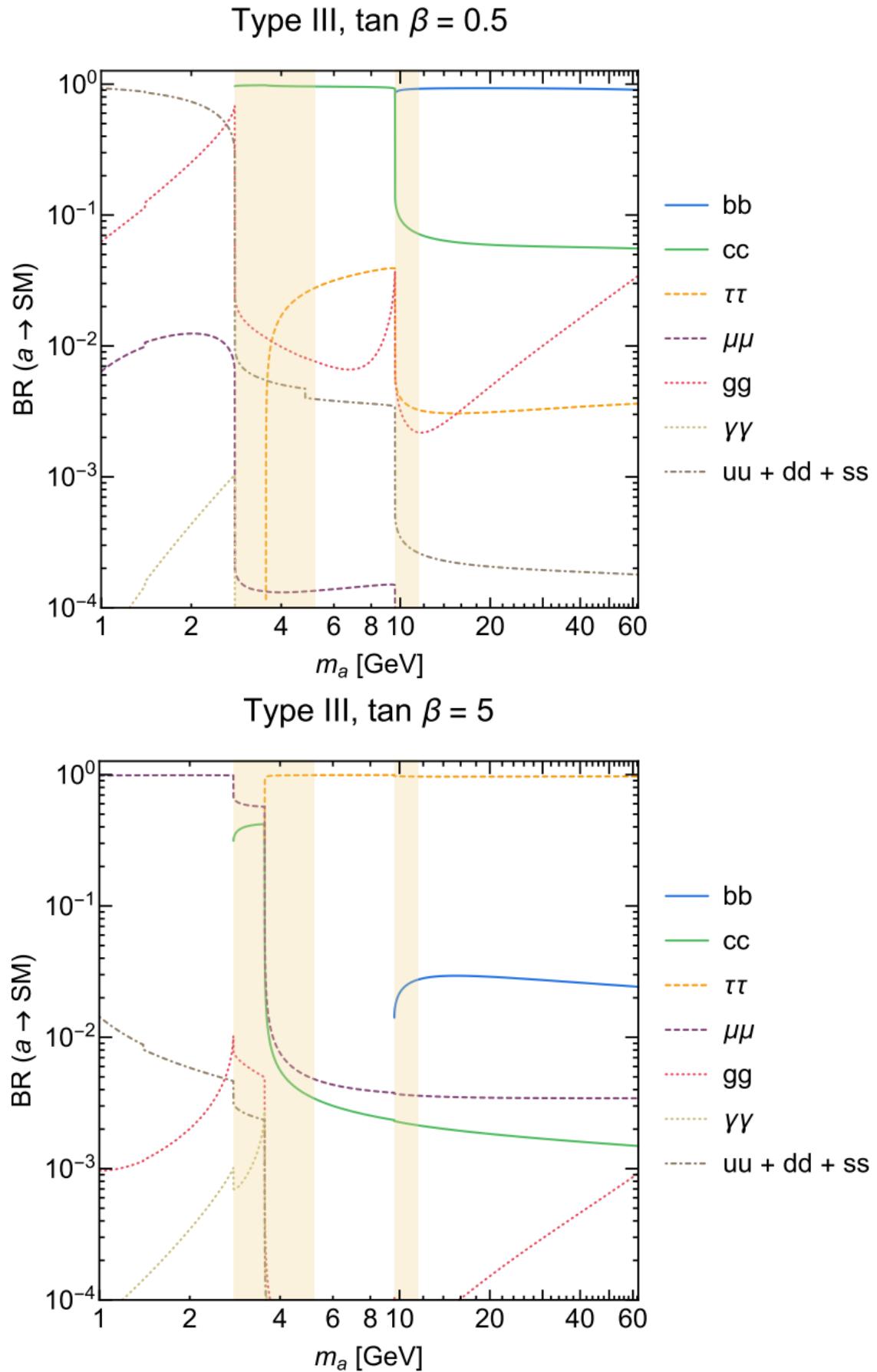


Figure 1.4: Type III 2HDM+S scenario branching fractions [4]

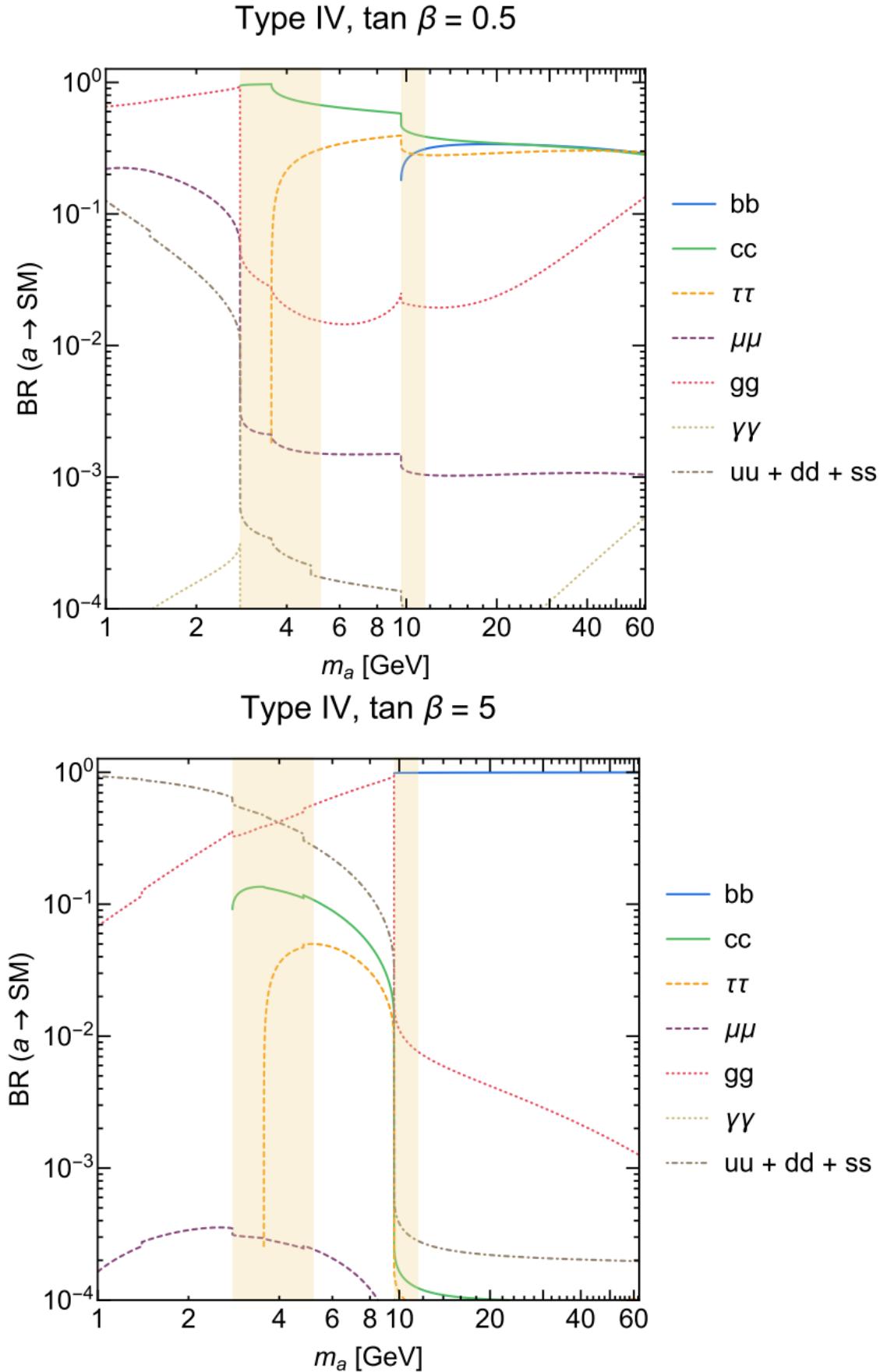


Figure 1.5: Type IV 2HDM+S scenario branching fractions [4]

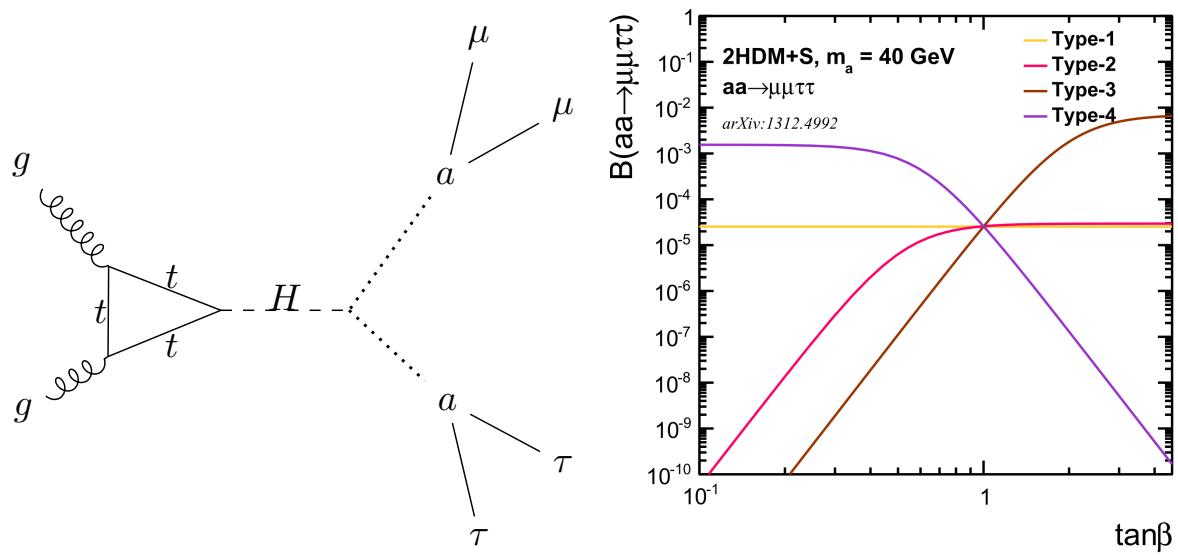


Figure 1.6: Diagram of Higgs decay to pseudoscalar  $a$  particles (Left) and branching ratios for pseudoscalar production in different  $\tan\beta$  scenarios and different 2HDM+S Types (right)

## Chapter 2

# CERN, The LHC, and The CMS Detector

### 2.1 CERN and the Large Hadron Collider

The *organisation européenne pour la recherche nucléaire* or CERN conducts the world's frontier particle physics experiments. Scientists at CERN represent numerous countries who work together for a greater understand of the universe. CERN hosts the Large Hadron Collider (LHC), currently the largest particle collider in the world. The LHC is 27 km in circumference and holds eight experimental caverns 150 meters underneath the earth. Accelerator physicists and engineers strive to provide high energy collisions along these eight sites. More than 1500 superconducting magnets are used to steer and focus the accelerating protons. The beams are brought into collision at four caverns where the experiments are sited. The LHC is capable of colliding both protons and heavy ions. The Compact Muon Solenoid (CMS) is the general purpose detector located at collision point 5(P5) in Cessy, France [7].

### 2.2 The Compact Muon Solenoid detector

At around 14,000 tons, the CMS detector may not seem like it would be compact; however, it is quite dense. As shown in the diagram 2.2, the detector contains many subdetectors housed within a powerful solenoid magnet. At a diameter of 6 meters, a combined weight of 12,500 ton,

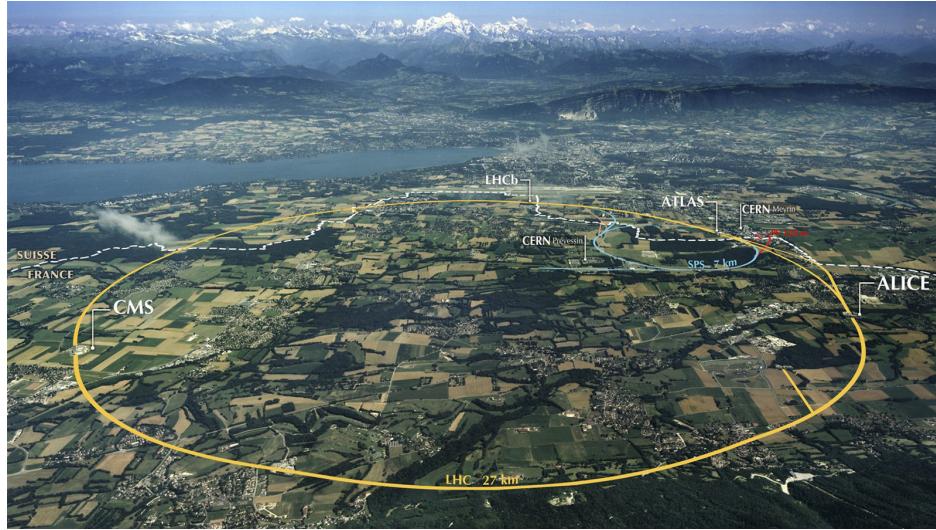


Figure 2.1: Overview of the Large Hadron Collider spanning Switzerland and France - Maximilien Brice, CERN

and a field of 3.8 Tesla, the solenoid is the central feature of the Compact Muon Solenoid (CMS). Within the solenoid volume, there is the silicon pixel and strip tracker, a lead tungstate crystal

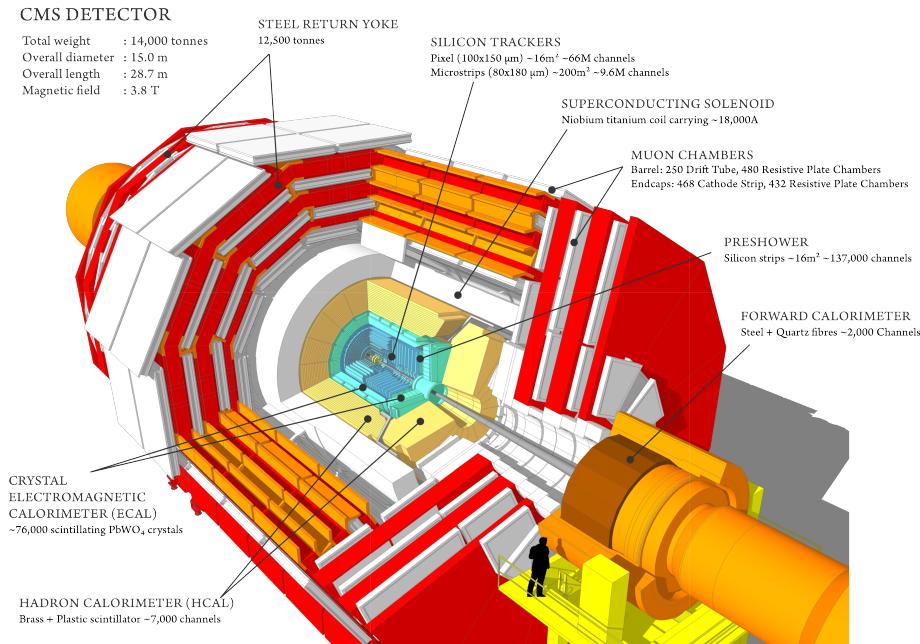


Figure 2.2: The CMS detector full 3D image with all subsystems labeled

electromagnetic calorimeter (ECAL), and a brass plus scintillator hadron calorimeter (HCAL). Each tracker and calorimeter comprises a barrel and two endcap sections. Forward calorimeters

extend the pseudorapidity ( $\eta$ ) coverage provided by the barrel and endcap detectors. Gas-ionization chambers are embedded in the steel flux-return yoke outside the solenoid and are used to primarily detect muons.

A coordinate system centered on the nominal collision point is adopted. The  $y$ -axis points vertically outward toward the sky, the  $x$ -axis tangent to the Earth, and the  $z$ -axis along the direction of the beam pipe. The azimuthal angle  $\phi$  and the radial coordinate  $r$  in the  $x$  and  $y$  plane, and the polar angle  $\theta$  measured from the  $z$  axis are typically used to denote space points. Often pseudorapidity, defined by

$$\eta = -\ln \tan(\theta/2) \quad (2.1)$$

is used to describe the angular distance from the beam pipe. A more detailed description of the CMS detector can be found in Reference [8].

## 2.3 Subdetector Systems

Several subdetector systems play an important role in the identification of the muons, electrons, and tau leptons that are used in the analysis. All subdetector systems are important to event reconstruction in CMS with several detectors identifying the particles that are used in this analysis. These are the tracker system, electromagnetic calorimeter, the hadronic calorimeter, and muon system.

### 2.3.1 Tracker

The tracker comprises several groups of silicon detectors. Going outward from the beam pipe, there is the pixel detector and then the silicon tracker. A silicon detector works by sensing the ionization trail left by an energetic charged particle. Typically, multiple band gaps are created through the process of lithography which adds artificial impurities of p-type (holes) or n-type (electrons). This process is known as “doping”. When a minimum ionizing particle (MIP) disturbs the latent charge—set by the bias voltage on the sensor—there is a current generated in the n and p type components which is given by the Shockley equation.

$$\mathcal{J}_{n,p} = \frac{q_0 D_{n,p} d_{n,p}}{L_{n,p}} \left( e^{\frac{q_0 V}{k_B T}} - 1 \right) \quad (2.2)$$

For reference:  $L_{n,p}$  is the diffusion length,  $D_{n,p}$  the diffusion coefficients,  $d_{n,p}$  the charge/hole density,  $V$  the bias voltage,  $q_0$  the standard charge unit,  $k_B$  the Boltzmann constant, and  $T$  the temperature. This current is sensed by the electrodes etched onto the silicon substrate. A graphical display of surface current using simulation as a function of time is shown in figure 2.3.1. A wealth of silicon information can be found in reference [9].

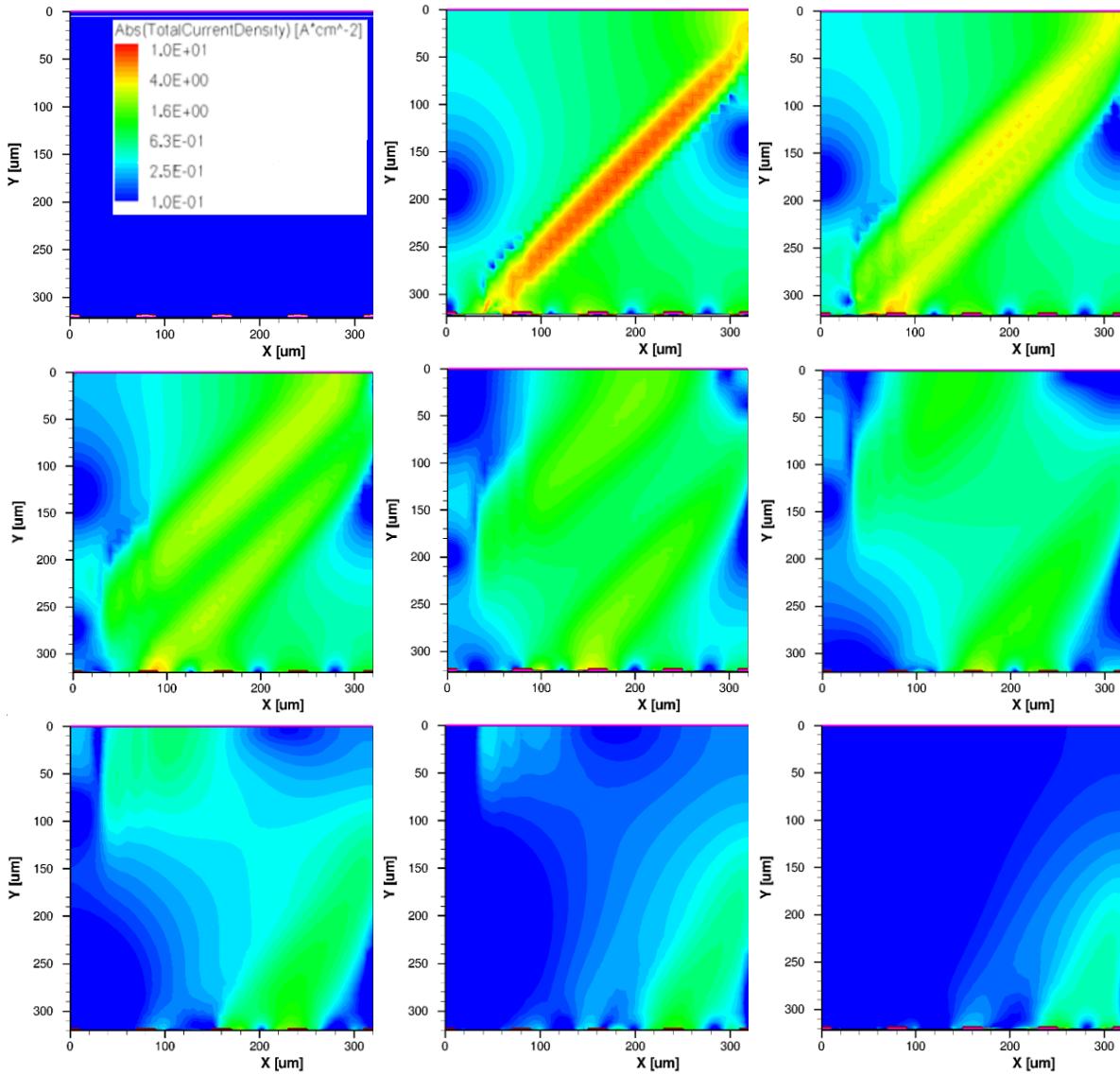


Figure 2.3: Simulation of a MIP traveling across a silicon strip sensor at  $45^\circ$  over time from 0.0, 1.1, 1.5, 2, 3, 4, 5, 6, 7 nanoseconds. The induced surface current dissipates and would be collected by the channels of the silicon module [9].

## Pixel Detector

The pixel detector contains the Barrel Pixels (BPIX) and the Forward Pixels (FPIX). Similar  $2 \times 8$  silicon detector modules make up both the BPIX and FPIX systems.

In 2016, the phase I FPIX was constructed and tested. At Purdue University, an Aerotech robotic gantry control system was used to join a hybrid flex circuit to a bump-bonded silicon pixel module. After wirebonding, the gantry system encapsulated the wirebonds for protection from corrosion and magnetic field resonance. Purdue was one of the manufacturing sites alongside University Nebraska-Lincoln.

Using LabVIEW, we developed a state machine to assemble and encapsulate these pixel modules. A pattern recognition and linear algebra suite were developed to perform precise operations at a 50 micron resolution. An example of a post encapsulated token bit manager—which resides on top of the high density interconnect of a completely assembly module—is shown in figure 2.3.1.

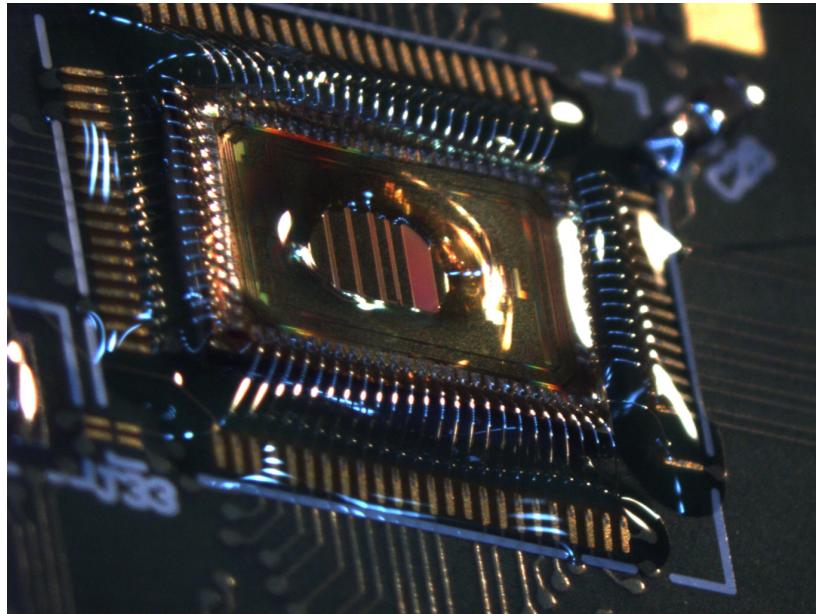


Figure 2.4: Encapsulated token bit manager of a forward pixel module currently installed in CMS

In 2017, this system was installed in CMS, increasing the number of disks to three and the number of barrel layers to four. The design of CMS is such that the inner subdetector systems may be taken out of the solenoid and serviced. These forward disks, which are especially important for the reconstruction of boosted charged particles, are located in high regions of  $\eta$  and are overlapped for improved hermeticity.

## Silicon Tracker

The silicon tracker comprises larger silicon modules by area than the pixel system and is located further from the beam pipe. A representative layout of the silicon tracker and the pixel system can be found in figure 2.3.1 [8].

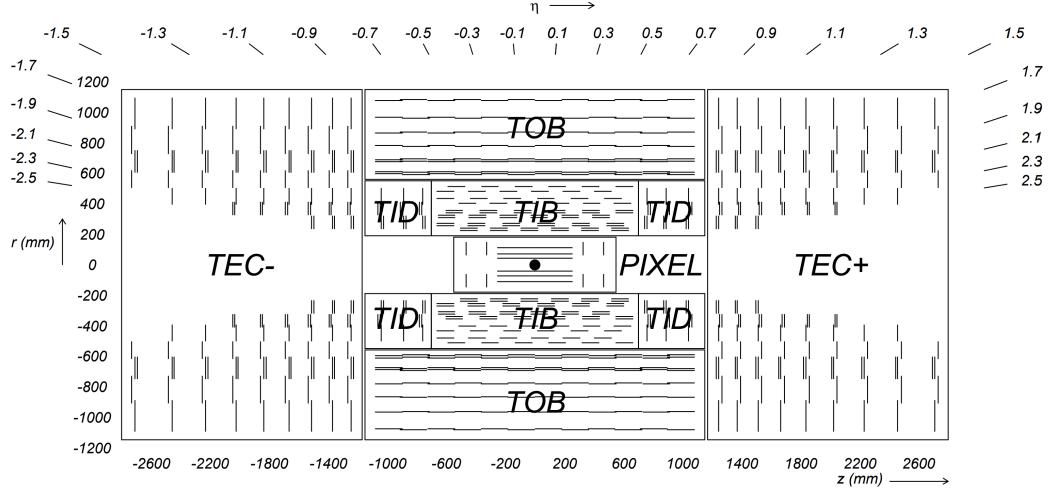


Figure 2.5: The silicon tracker system, consisting of the inner pixel system (BPIX and FPIX), The Tracker End Caps (TEC), Tracker Inner Detector(TID), Tracker Inner Barrel (TIB), and the Tracker Outer Barrel (TOB) by position in  $r$ ,  $z$  , and  $\eta$  [8]

### 2.3.2 Electromagnetic Calorimeter (ECAL)

The principal components of the ECAL are the 76200 lead tungstate ( $\text{PbWO}_4$ ) crystals, which scintillate and absorb energy from incoming particles. These detector components are also separated in barrel and endcap regions. A photomultiplier is attached to each the crystal to detect its light signal. The relative energy resolution is

$$\left(\frac{\sigma}{E}\right)^2 = \left(\frac{2.8\%}{\sqrt{E}}\right)^2 + \left(\frac{0.12}{E}\right)^2 + (0.3\%)^2$$

The first, second, and third terms in equation 2.3.2 reflect the stochastic, noise, and constant terms respectively as determined in a calibration run with a 440 nm blue laser [8, 9].

### 2.3.3 Hadronic Calorimeter (HCAL)

The Hadronic Calorimeter is the primary subdetector to identify “jets”, which are collimated collections of hadrons. Brass plates interwoven with plastic scintillators are used to induce particle

showers. Light signals from the scintillators are propagated through wavelength shifting fibers, and read out through an optical decoding unit before ultimately landing at a hybrid photodiode. There are barrel (HB) and endcap (HE) sections inside the solenoid. The hadronic outer (H0) and super forward detector (HF) sit outside the solenoid. An overview of the HCAL system is shown in figure 2.6 [8, 9].

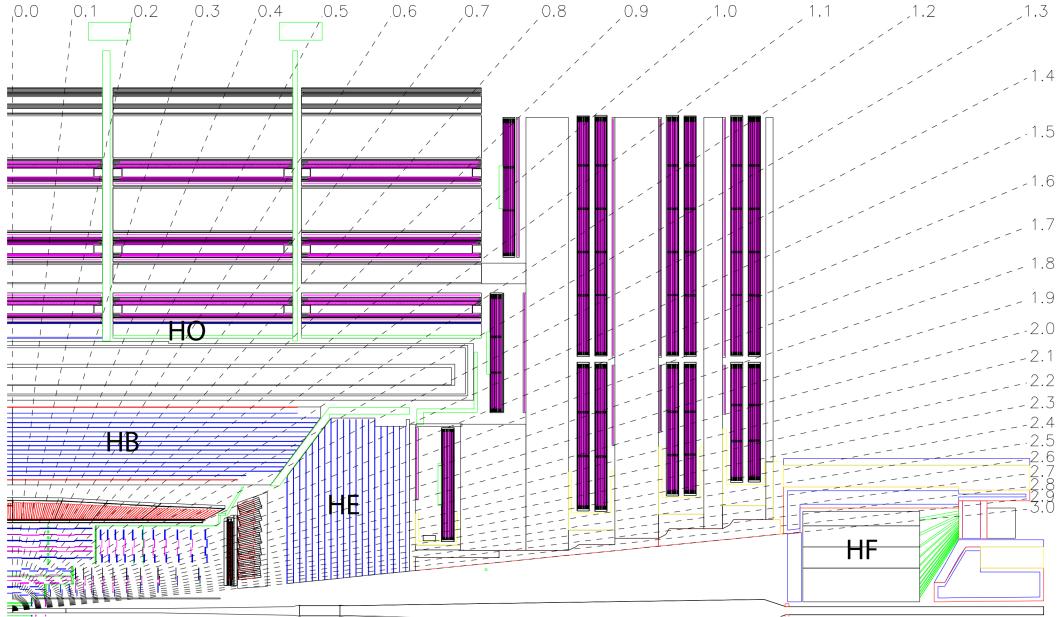


Figure 2.6: Overview of the HCAL system from the  $z, \eta$  plane showing the hadron barrel (HB), encap (HE), outer (HO), and the forward (HF) subsystems [8]

### 2.3.4 Muon System

The muon system comprises drift tubes (DT) which cover a pseudorapidity region ( $|\eta| < 1.2$ ) split into four stations interleaved in the flux return plates. In the higher  $|\eta|$  endcap regions, cathode strip chambers (CSC), which provide fast response time, fine segmentation, and radiation resistance, are used. In both high and low regions resistive plate chambers (RPC) are used [10]. For a visual representation of a cross section of the muon system, please refer to figure 2.3.4. Notably, the track of the muon is bent inside the solenoid by the Lorentz force, and then reverses after it exits.

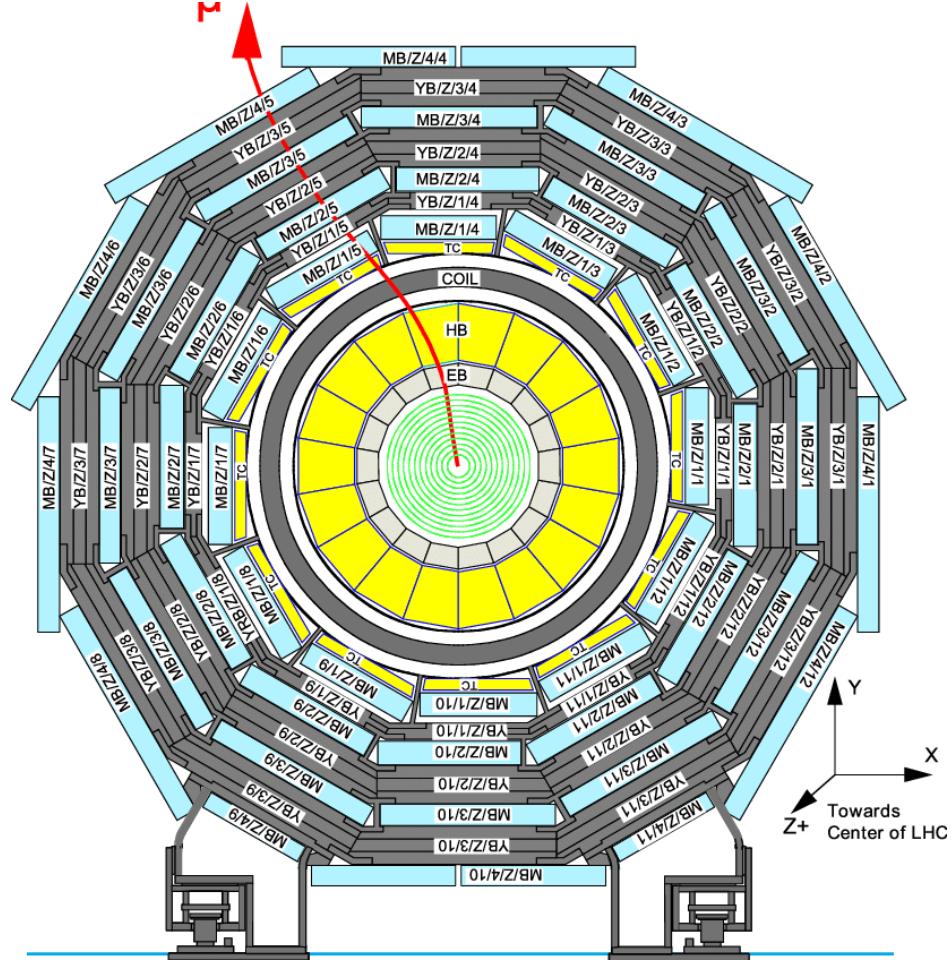


Figure 2.7: Muon system involving multiple subdetector systems: tracker, solenoid, and the muon gas chambers around the iron yoke (grey) - Maximilien Brice, CERN

## 2.4 Level 1 Trigger System and High Level Trigger

Particle collisions happen at a rate of 40 MHz, resulting in about 20 minimum bias events at each bunch crossing. The bandwidth that would be needed to record all these collisions is prohibitively high [7, 11]. The Level 1 trigger (L1) and High Level Trigger (HLT) work to reduce these rates by selecting events of interest.

The L1 trigger system, which comprises many subsystems, can process data at the beam collision rate. Algorithms are in place that take input from the calorimeters, the muon systems, and other detectors in the form of “trigger primitives”, and use pattern recognition, along with fast summing techniques, to trigger on events. Many of these algorithms are run on Field Programmable Gate Arrays (FPGAs). After 144 beam crossings, the Global Trigger (GT) initiates readout for events

of interest at the front end electronics. The L1 system also outputs physics objects to seed the reconstruction algorithms used by the HLT [11]. The HLT maximum input rate is 100 kHz and the output rate is on the order of kHz. It is constrained by the processing power available, the data recording and transfer rate of Tier 0 (T0), and the prompt reconstruction algorithms. Late in Run II, “Scouting” and “Parking” data were used to make more efficient use of the available bandwidth. Scouting reduces the event size by saving only objects reconstructed by the HLT. Parking reduces the immediate load on the T0 system by postponing prompt reconstruction to when CMS is not running [12].

## 2.5 Particle flow algorithm

The event data model requires the association of higher level physics objects—like leptons—with energy deposits and tracks in the detector. The particle flow algorithm at CMS has the goal of associating these primary detector signatures with these particles so a direct comparison to Monte Carlo (MC) simulation can be done. The list of particle objects includes jets, missing transverse energy, taus, charged-leptons, photons, and bottom quark jets among others. To outline the algorithm: charged particle tracks reconstructed in the tracker, energy clusters from the ECAL, HCAL, preshower detector (ES), and forward calorimeter (HF) are topologically linked into blocks. The linking is done through many associations of energy deposits and tracks in  $\phi, \eta$  space. These blocks are then interpreted as particles. Further details can be found in reference [13].

## 2.6 Computational Infrastructure

Over 200 peta-bytes of information have been gathered in Run II. A schematic overview of the computing infrastructure can be found in figure 2.8 [14].

The T0 facility, which comprises 32,000 24-core processors, is where higher level reconstruction of physics objects is done. The data is stored and processed at many different sites, organized by tiers. There is one Tier-0, seven Tier-1, about one-hundred fifty Tier-2, and numerous Tier-3 centers. The sum of these tiers is the “grid” or the Worldwide LHC Computing Grid (WLCG), which in total combines 900 000 CPUs from over 170 sites in 42 countries. Tools like `XrootD` and `Rucio` allow physicists from around the world to access centrally supported data. An abundance

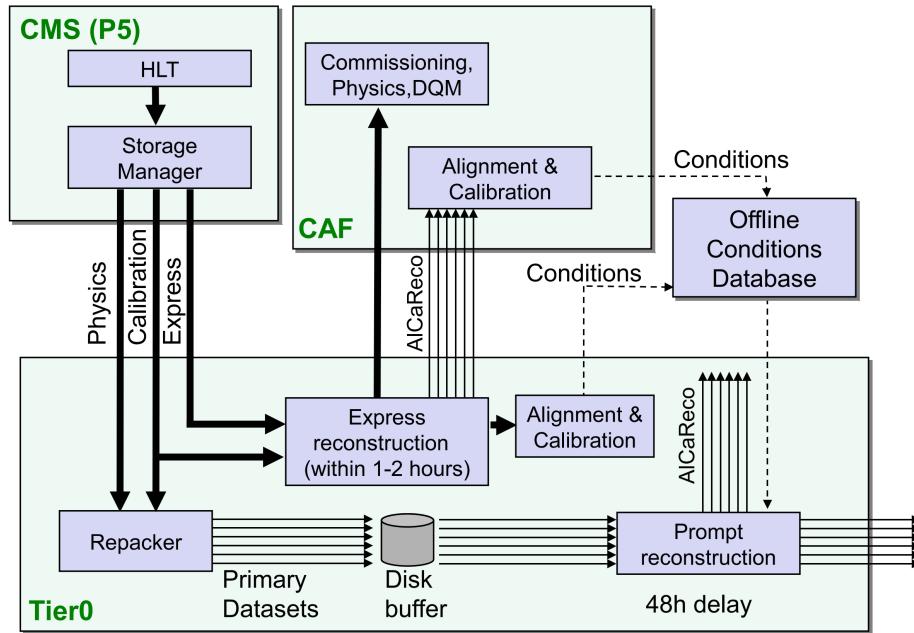


Figure 2.8: Schematic overview of T0 computing: data can be available from different sections allowing for data quality monitoring and also storage to several databases [14].

of up to date information can be found <https://home.cern/science/computing/grid>.

# Chapter 3

## Luminosity

### 3.1 Luminosity at the LHC

Luminosity sets the scale for the number of events recorded at the LHC. It is how bright the beam is and dictates how many interactions can be expected over a data taking period. Therefore, it is important for all physics analyses to use the correct luminosity, and its measured error, to obtain an accurate result. The number of expected events for any given process is the luminosity  $\mathcal{L}$  times the cross section  $\sigma$ .

$$N_{\text{event}} = \mathcal{L}\sigma_{\text{event}} \quad (3.1)$$

$$\mathcal{L} = \frac{N_b^2 n_b f_{\text{LHC}} \gamma_r}{4\pi \epsilon_n \beta^*} \left( 1 / \sqrt{1 + \left( \frac{\theta_c \sigma_z}{2\sigma^*} \right)^2} \right) \quad (3.2)$$

$N_b$  is the number of particles in the bunch crossing,  $n_b$  the number of bunches,  $f_{\text{LHC}}$  the revolution frequency of the LHC,  $\gamma_r$  the relativistic factor,  $\epsilon_n$  the normalized beam emittance,  $\beta^*$  the beta function at the collision point (related to the crossing angle),  $\theta_c$  is the full crossing angle,  $\sigma_z$  the RMS bunch length and  $\sigma^*$  the transverse RMS beam size at the interaction point.

### 3.2 Luminometers

Several subsystems are used to measure luminosity at CMS. Particularly the Pixel Luminosity Telescope, HF with summed transverse energy (ET) and occupancy (OC), BCM1F, and Tracker/Pixel based luminosity detectors to name several. In this section, the tracker based luminosity will be

the focus. The pixel system is integral in the reconstruction of events for physics analysis and in measuring the luminosity.

There was validation of the new pixel detector in early 2017, from the BPIX and FPIX upgrades mentioned in section 2.3.1. The Lumi-POG—Luminosity physics object group—commissioned luminosity measurement using the clusters from the new pixel detector in an automated workflow. We measure the luminosity by counting pixel clusters in a low channel occupancy setting and scaling it by a visual cross section determined in a separate analysis. Using the relation in equation 3.3, the instantaneous luminosity can be obtained once the number of clusters and the visible cross section  $\sigma_{\text{cluster}}$  are measured.

$$\langle N_{\text{cluster}} \rangle \equiv \frac{\sigma_{\text{cluster}}}{f_{\text{LHC}}} \mathcal{L}_{\text{SBIL}} \quad (3.3)$$

$\mathcal{L}_{\text{SBIL}}$  is the instantaneous luminosity of a single bunch crossing—the aggregate collection of protons that are in the beam typically 3564 total bunches during standard pp-collisions.  $\sigma_{\text{cluster}}$  is the cross section that is measured in a separate analysis involving Van-de-Meer scans (beam dynamic scans). More details can be found here [15].

### 3.2.1 Tracker luminosity

For the pixel luminosity, a two component correction is applied on the fly to correct for self-radiative effects on the pixel modules under particle fluence and for inefficiencies. One detail that is important in estimating the luminosity from the pixel detector is ensuring that the data that is taken and analyzed has consistent performance. Several times in a year, the Lumi-POG and Beam Radiation Instrumentation Luminosity (BRIL) groups analyze the performance of each subdetector used to measure luminosity and certify the data once the analysis is complete. In 2017 and 2018 data taking campaigns, the luminosity from the pixel detector was vetted by looking at relative module performance over the runs of data taking for those years. If the modules didn't have consistent performance, they were removed from the final result.

Even though up to half of the modules were vetoed after this procedure, there was plenty of statistics due to the gathering of many pixel clusters per event. This module veto decision was made by taking the total clusters in each module and scaling them so that the overall total clusters are one. Then, on a per-module basis, the performance relative to the total clusters was compared. This helped the analyzer look at consistent performance and manage a list of passing modules used

in a final luminosity measurement using the pixel detector.

For Run III data taking, integration of the cluster counting procedure was included at the HLT. A data compression of  $10^3$  was made by taking the low level data from the silicon pixels and storing them in a simple data container, which saved a peta-byte of data. Online luminosity using these data containers and methods are being investigated as more CMS-physicists are interested in using the central tracking system for luminosity measurements.

# Chapter 4

## Lepton Identification and Object Selection

### 4.1 Lepton identification

The following three sections briefly describe how certain subsystems of the CMS detector work together to identify muons, electrons, and tau leptons.

#### 4.1.1 Muon identification systems

As CMS implies in its name, muons are certainly a focal point in particle detection. Looking at muons that come from the interaction vertex—prompt muons—the tracker plays an important role in identifying charged particle tracks. The tracker system works in conjunction with the gas chambers to reconstruct muons, and the solenoid bends the charged particle’s tracks allowing the momentum to be measured for an accurate mass resolution. By design, muons should be the only particle that should reach the gas chambers, making for great muon efficiency. During reconstruction, muons are identified and are ultimately divided into four working points (very loose, loose, medium, tight). These points are defined on their efficiencies and depend on the  $\chi^2$  of the track and momentum of the candidate muon [16, 17].

### 4.1.2 Electron identification systems

The main subdetector involved with electron identification is the ECAL. To identify electrons, a cluster of energy in the ECAL is associated with a track that is constructed in the silicon detector system. The tracks are identified in the typical fashion by using the Kalman Filter tracking technique to pick good quality tracks, then the tracks are refitted using a Gaussian Sum Filter. These tracks would then be associated with an ECAL super cluster by requiring matching in  $\eta$ ,  $\phi$  space

$$|\Delta\eta| = |\eta_{\text{SC}} - \eta_{\text{in}}^{\text{extrap}}| < 0.02 \quad (4.1)$$

$$|\Delta\phi| = |\phi_{\text{SC}} - \phi_{\text{in}}^{\text{extrap}}| < 0.15 \quad (4.2)$$

This method has an overall efficiency of about 93% [18].

### 4.1.3 Tau identification systems

Tau leptons decay in many different ways. It is the heaviest lepton, so heavy that it can decay to intermediate mesons. The  $\rho$ ,  $a$ , and  $\pi$  mesons are several possible mesons that the tau can decay to. Therefore, when it comes to tau identification, many algorithms are needed to properly identify them using information across the detector. Tau leptons decay both hadronically and leptonically as shown in the table below 4.1.

Table 4.1: Possible hadronic tau decays,  $h$  doesn't indicate a Higgs particle but a hadronic prong [19]

Decay Modes	Resonance	$\mathcal{B}(\%)$
Leptonic Decay		35.2
$\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau$		17.8
$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$		17.4
Hadronic Decay		64.8
$\tau^- \rightarrow h^- \nu_\tau$		11.5
$\tau^- \rightarrow h^- \pi^0 \nu_\tau$	$\rho(770)$	25.9
$\tau^- \rightarrow h^- \pi^0 \pi^0 \nu_\tau$	$a_1(1260)$	9.5
$\tau^- \rightarrow h^- h^+ h^- \nu_\tau$	$a_1(1260)$	9.8
$\tau^- \rightarrow h^- h^+ h^- \pi^0 \nu_\tau$		4.8
Other		3.3

The Hadron Plus Strips (HPS) combines the use of the tracker system and the electromagnetic calorimeter (ECAL) for hadronic tau identification [20].

## 4.2 Data and simulation

For this analysis, muons are paramount, so there must be a certain number of muons triggered for the event to be selected. Two final states contain electrons, so datasets containing electrons are also used. The single muon, double muon, and electron plus photon datasets are used depending on the year. These datasets contain the triggers that are the most important for object selection. Single muon triggers that contain isolated muons at 22, 24, and 27 GeV thresholds are implemented, along with double muon triggers with good reconstructed muons that have 17 GeV threshold. More information on triggers and selection is given in the event selection section 5.2.1.

The simulation used to compare to data typically use MadGraph5@NLO along with PYTHIA 8 for hadronization. These CMS centrally-generated samples are then digitized using GEANT4 to the same format as real data events collected and processed at CMS high level trigger. These raw data formats are then reconstructed to physics objects—such as tracks and higher level objects like muons and leptons. A direct comparison between data and simulation can be made after calibrating simulation in control regions.

Data taken from CMS during the entire Run II period was examined, corresponding to 137  $\text{fb}^{-1}$  of integrated luminosity. The list for data and simulation Monte Carlo(MC) is exhaustive and listed in the appendix A.

For the MC production of the signal samples, to reflect the 2HDM modeling, events were generated at tree level for a pseudoscalar Higgs like boson between the masses of 15 and 60 GeV in intervals of 5 GeV with the parent Higgs produced through gluon fusion. These masses are sufficient for the parametric modeling described in the fit to obtain a more precise peak resolution 7.3. Privately produced samples were used for 2017 and 2018. The scripts and conditions used are located here: <https://github.com/samhiggle/iDM-analysis-AODproducer/tree/haa>. The NMSSMHE $t$  model was used to simulate the events. Parameters and information can be seen in the package: <https://cms-project-generators.web.cern.ch/cms-project-generators/>.

## 4.3 Physics object selection

Baseline selections are recommended by the various Physics Object Groups (POGs) for object selection. Ultimately, these take the form of cuts for leptons based primarily on kinematic variables

like the momentum. Based on the final state, selections are made to identify muons, electrons, and tau leptons. These three leptons form the objects under selection. All leptons under consideration must pass trigger requirements that depend on momentum of the lepton. Special triggers are used for the different final states depending on the number of muons in the event. A precise description of the triggers used are given later in section 5.2.1. Identifying unique particles in object selection is critical, particularly differentiating between lepton candidates that come from the interaction vertex (prompt) and those that appear from decays down the line (nonprompt). Relative isolation is typically defined in order to ensure there is no overlap between candidate leptons. More details on this variable and it's usage in the Particle Flow algorithm can be found here [21].

$$I^\ell \equiv \frac{\sum_{\text{charged}} p_T + \max(0, \sum_{\text{neutral}} p_T - \frac{1}{2} \sum_{\text{charged}} p_T)}{p_T^\ell}. \quad (4.3)$$

$\sum_{\text{charged}} p_T$  is the scalar sum of the transverse momenta of the charged particles originating from the primary vertex and contained in a cone of size  $\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} = 0.4$  (0.3) centered on the muon (electron) direction. The sum  $\sum_{\text{neutral}} p_T$  is a similar quantity for neutral particles.

As mentioned in the instrumentation and detector section, the muon identification system uses the tracker to identify charged tracks and the muon chambers identify the particles later in their trajectory after they exit the solenoid. Typically “good” muons are those that are both associated with a track and their subsequent identification in the drift tubes or the CSC chambers. The average muon lifetime is  $2.2 \mu\text{s}$  so they travel quite far from the interaction point the subdetectors. The physics object group’s recommendations are followed, which select muons with  $p_T > 15 \text{ GeV}$  and  $|\eta| < 2.4$  in addition to selecting only “good” muons. Electrons originating from the tau decay are reconstructed in by track association in tandem with energy deposition in the Electronic Calorimeter (ECAL). To clarify selection in the calorimeter systems, events are vetoed for candidate electrons that also show a substantial energy deposition in the HCAL. The hits and track quality from two separate algorithms, along with the geometrical and energy matching from the ECAL are used in a Multivariate Analysis (MVA) technique like Boosted Decision Trees (BDTs) to select good electrons for analysis [18]. To identify  $\tau_h$  candidates, the hadron-plus-strips (HPS) algorithm is used to identify the major modes of the hadronic tau decay [20]. Typically events with hadronic prong are considered in combination with a number of neutral pions and missing transverse energy from the neutrinos. Pions almost always decay to photons, so an algorithm is considered that

joins the identification of charged hadrons and neutral pions. The HPS algorithm combines inner track information, hits in the HCAL, and pion association in the ECAL by deposits in a  $\eta, \phi$  strip region to identify hadronic tau leptons. The  $\tau_h$  is matched to  $h^\pm, h^\pm\pi^0, h^\pm h^\mp h^\pm$ , or  $h^\pm h^\mp h^\pm\pi^0$  depending on the overall charge vs neutral constituents [22, 23]. In addition to HPS algorithms, a Deep Neural Network (DNN) was constructed to further aid in identification by discriminate between genuine tau leptons and those that originate from quark or gluon jets, electrons, or muons. In the DNN, the tau four-momentum and charge, the number of charged and neutral particles used to reconstruct the tau candidate, the isolation variables, the compatibility of the leading tau track with coming from the primary vertex, the properties of a secondary vertex in case of a multiprong tau decay, observables related to the  $\eta$  and  $\phi$  distributions of energy reconstructed in the ECAL strips, observables related to the compatibility of the tau candidate with being an electron, and the estimated pileup density in the event are all used. In total, 47 high-level input variables are incorporated [24]. In practice, the DNN has discriminators for muons, electrons, and jets that fake genuine taus and have efficiencies that go from 40% to 90% in a 10% granularity of the discriminating variable. The medium working point is used for each of these discriminators. All leptons also have a momentum threshold and isolation requirements to place them in a kinematic region where good agreement between data and MC is expected in control regions.

Table 4.2:  $t\bar{t}$  baseline cuts and identification for lepton selection

lepton	baseline cuts
Muon	$\delta Z < 0.2, \delta xy < 0.045, p_T > 5.0 GeV, \text{Iso.} \leq 0.2, \eta \geq 2.4$
Electron	$\delta Z < 0.2, \delta xy < 0.045, p_T > 7.0 GeV, \text{Iso.} \leq 0.15, \eta \geq 2.5$
Tau	$\delta Z < 0.2, \delta xy < 0.045, p_T > 18.5 GeV, \text{Iso.} \leq 0.2, \eta \geq 2.3, \text{Med. DNN}$

## 4.4 Corrections to simulations

For accurate results that reflect true experimental data, many corrections to MC samples are made. In general, in compliance with CMS’s Physics Object Groups (POGs), standard techniques are applied to ensure proper simulation. Of critical importance is the corrections to energy scales for the leptons in the analysis. These corrections will affect the nominal energy recorded for the event as well as the rates in which objects are identified. In order to protect against bias and to

investigate systematic errors, corrections that could effect the results are considered in the overall error in the statistical inference model.

#### 4.4.1 Muon energy scale

Corrections to the muon's energy scale are computed for the muons that pass selection for the analysis. Medium muon ID with track based isolation that pass the isolated single muon triggers at 22 GeV, 24 GeV, and 27GeV are then rescaled for pileup, efficiency, di-lepton  $P_T$  and EWK re-weighting of based on accurate gauge boson measurements. After selection, the scale factors for energy corrections are measured and parametrized in  $\phi$  and  $\eta$  in multiplicative and additive corrections

$$\rho^{\text{cor}} = \kappa(\eta, \phi)\rho + Q\lambda(\eta, \phi) \quad (4.4)$$

. The correction coefficients  $\kappa$ , and  $\lambda$  are measured in a tag and probe method and  $\rho$ ,  $Q$  related to the energy scale.

In practice, these are just scale factors applied to the energy scale in certain eta phi regions.

Table 4.3: Measured energy scale correction for genuine across all years.

Correction (%)	
$\eta$ region	scale factor
0 – 1.2	0.4
1.2 – 2.1	0.9
> 2.1	2.7

#### 4.4.2 Electron energy scale

Genuine electron energy scale and resolution requires corrections to be applied to MC in order to match data [25]. These corrections are provided directly by the E/Gamma POG, and applied to genuine electrons coming from tau lepton decays for the channels  $\mu\mu e\mu$  and  $\mu\mu e\tau$ .

The energy shift is split depending on the  $\eta$  of the electron shown in table 4.4.

Table 4.4: Measured energy scale correction for genuine across all years.

Correction (%)	
$\eta$ region	scale factor
0 – 1.2	1.0
1.2 – 2.1	1.0
> 2.1	2.0

#### 4.4.3 $\tau$ energy scale

There is a central energy shift based on the type of tau decay. Due to the electroweak interactions,  $\tau$  leptons decay hadronically and leptonically. Figure 4.1 shows the typical tau decay leptonically or hadronically.

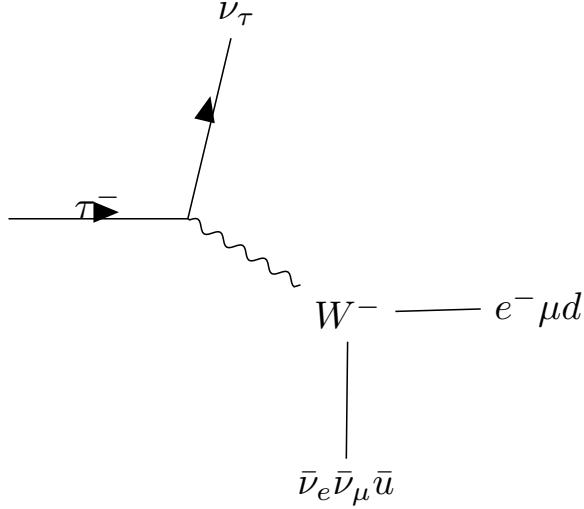


Figure 4.1: diagram depicting the possible decays of the tau lepton: 65% of the time hadronically and 18% to tau neutrino and electron with antineutrino (17% for muon)

When the tau decays hadronically, many different intermediate mesons are produced and each type of decay has a different signature particularly when they hadronize and deposit the energy within HCAL. The Tau-POG has measured the central value systematic deviation as a form of scalar factor that is applied for an accurate result of measuring the tau's energy. This is split by the prongs (charged hadrons) and  $\pi^0$  s.

The deviation in the model is measured by between the difference in data and MC for different values of hadronic tau energy. The uncertainty is measured for each decay mode considered in the

Table 4.5: Measured  $\tau_h$  energy scale correction for genuine  $\tau_h$ 's across all years.

Decay mode	Correction (%)		
	2016	2017	2018
$h^\pm$	-0.6	0.7	-1.3
$h^\pm\pi^0$	-0.5	-0.2	-0.5
$h^\pm h^\pm h^\pm$	0.0	0.1	-1.2

analysis. Figures 4.2 shows the differences in data and MC for the 1 prong +  $\pi_0$  decay mode as a function of tau energy; all other tau decay modes are also measured.

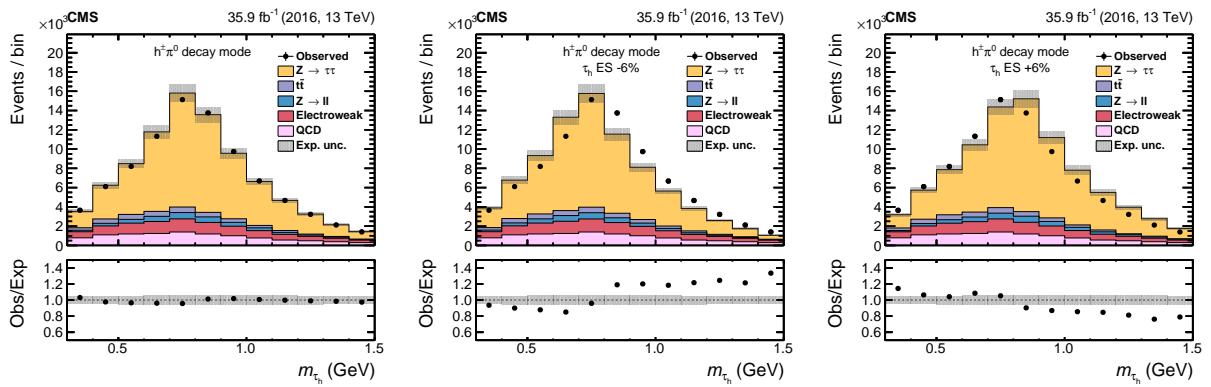


Figure 4.2: Tau mass distributions considering the nominal  $\tau_h$  energy scale in simulation (left), or the  $\tau_h$  energy scale shifted by -6% (left) or +6% (right), in the  $\mu\tau_h$  final state, for the 1 prong +  $\pi^0$  decay mode.

#### 4.4.4 $\tau_h$ ID efficiency

Genuine  $\tau_h$  identification efficiency can be different in Data and MC [26]. To correct for this difference, measurements are made using genuine Z+jets production (Drell-Yan) to two  $\tau$  leptons, one decays leptonically and the other hadronically. The invariant mass of the system is used as an observable. Naturally, this region has far more statistics than the control and signal regions in the pseudoscalar analysis. To measure the identification efficiency precisely, it is done in the inclusive regions with an emphasis of simulation containing real taus. This measurement is done by the Tau POG, and the scale factors are provided to CMS. For the  $\mu\mu e\tau_h$  and  $\mu\mu\mu\tau_h$  channels, scale factors are binned in 3 different  $p_T$  bins: 30–35, 35–40, and 40+ GeV. In the  $\tau_h\tau_h$  final state, the efficiencies are also binned by decay mode.

These efficiencies, while used in the primary event and the parameter of interest in the fit, they

are not considered in the systematic model as they are expected to have very little impact on fit and limits based on the 2016 result.

#### 4.4.5 $e \rightarrow \tau_h$ and $\mu \rightarrow \tau_h$ misidentification rate

The efficiency of the discriminators against electrons or muons misidentified as  $\tau_h$  candidates can also be different between simulation and data. These data/MC scale factors are binned by barrel/endcap region of the measured  $\eta(\tau_h)$ , and by  $\tau_h$  decay mode. They depend on the discriminators against electrons and muons used in the DNN. Scale factors are measured to correct this difference and are applied to  $e \rightarrow \tau_h$  or  $\mu \rightarrow \tau_h$  in MC. Full information on misidentification measurements and application in analyses can be found in reference [26].

The misidentification scale factors are derived by pass and fail regions. The regions are set up by selecting events where a reconstructed  $\tau_h$  passes the DNN working point and also fails the DNN discriminant against muons or electrons. The regions considered are QCD multijet, W+jets, and Z+jets—similar to the fake rate calculation like in chapter 6. QCD multijet is estimated from same sign lepton region within data. W+Jets normalization is carefully selection from a region with high transverse mass. The visible mass distributions of the events in these regions are fit and the overall signal yield remains constant in the pass and fail regions. The normalization of  $Z \rightarrow ee$  background is allowed to vary in this muon faking tau measurement. The expected impact on the systematic model from these anti-lepton discriminators are expected to be very small so they are not included in the uncertainty model.

#### 4.4.6 Pileup Re-weighting

MC events are re-weighted using a minimum bias cross section equal to the luminosity for the corresponding year. This pileup re-weighting is to rescale the events for effective number of primary interactions during collisions. During Run II, pileup or the number of primary vertices in a crossing or underlying event could reach close to 100 and in Run III this will exceed 200.

#### 4.4.7 Electron and muon identification efficiency

Scale factors derived within the HTT group are applied for muons [27], and the EGamma POG scale factors are applied for electrons [28]. The scale factors for muons with  $5 < p_T < 9$  GeV and

$9 < p_T < 10$  GeV, are computed privately as there are no official numbers, and were approved by the MuonPOG in the 2016 analysis.

#### 4.4.8 Generator event weights and luminosity

Generator weights are applied on an event-by-event basis. Samples produced with the aMCatNLO generator contain both positive and negative event weights. The presence of negative event weights reduces the effective yield of the samples. The event weights for simulation are scaled to the expected yields for each sample. The number of generated events in each sample is used, however in the aMCatNLO sample, this sum of generated events is weighted by the generator weights, effectively making the aMCatNLO samples smaller when weighting for luminosity and cross section.

To correct for differences between leading order and next to leading order cross sections, scale factors called K-factors are used. They are applied to W+Jets and Drell-Yan samples in order to correct between purely generated events and reconstructed event yields. For Drell-Yan a factor of 1.1637 is used and for W+Jets a factor of 1.221 is used.

#### 4.4.9 Offline Muon Selection

Due to the selection of muons at 5 GeV, which is below the trigger threshold, scale factors were measured in the barrel and endcap using the tag and probe technique in the 2016 analysis. These factors are used to correct for low  $p_T$  muon selection, in addition to the Muon POG’s recommendation, to support correct simulation of data.

Table 4.6: Scale factors to correct for Offline muon selection being less than the online trigger threshold.

	Barrel	Endcap
Muons with $5 < pT < 9$ GeV	0.956	0.930
Muons with $9 < pT < 10$ GeV	0.916	0.897

#### 4.4.10 Visualizing the Corrections

The energy scales for the various leptons used in the analysis are not only changed in the nominal case, but their uncertainty is measured and then propagated to the fit model via changes in the normalization for the distribution. To visualize this and provide a cross check distributions for

the  $\tau$ ,  $\mu$ , and  $e$  energy scales are cross checked in the parameter of interest ( the mass of the di-muon system from the leading  $p_T$  pseudoscalar  $a$  particle). These systematics for  $\mu\mu\tau\tau$  channel are visualized here in figure 4.3.

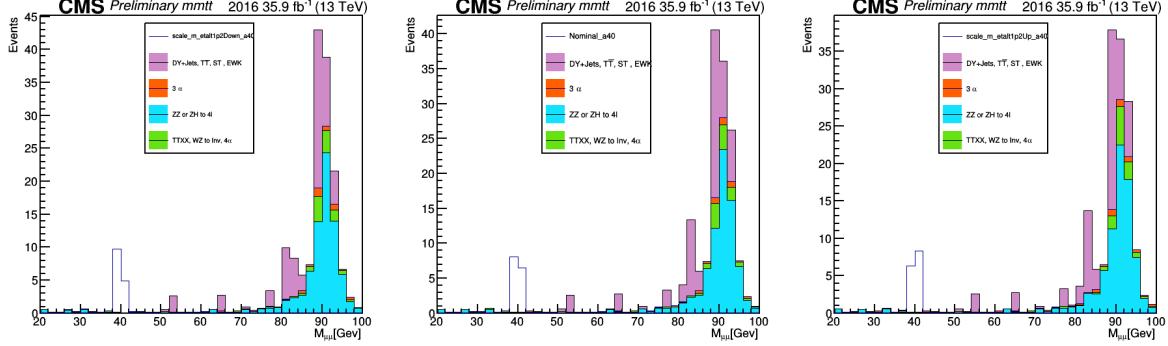


Figure 4.3: Systematic Shift in the Uncertainty Model for 2016  $\mu\mu\tau\tau$  for the muon energy scale shift down (left), nominal (mid), and up (right), no data is shown on this plot as it directly reflects the signal region without the extraction cuts

In the end, the uncertainty considered in the fit model would then be the percent yield up and down as a flat error (log-normal) that affects the normalization of the template. Because the model is so statistically limited, the log-normal is sufficient in capturing the changes in the distributions over the fit range.

# Chapter 5

## Event Selection

### 5.1 Framing an analysis at CERN

In order to conduct a concrete hypothesis test, two perspectives are taken. The null hypothesis is the SM, which will comprise all possible events that are categorized as *background*. The alternative hypothesis is the SM with the addition of the *signal*, ie ...  $H \rightarrow aa \rightarrow \mu\mu\tau\tau$ .

### 5.2 Defining signal and control regions

To optimize the analysis, regions of the data and simulation are cut away in order to increase the number of signal events relative to background events. This process is known as “making cuts”. In order to not bias the result, regions are setup to investigate the agreement of simulation with data (the control region) and to conduct the statistical hypothesis test (signal region). When the data and MC simulation agreement are reasonable in the control region, then the statistical test can be made in the signal region.

#### 5.2.1 Triggers for event selection

The trigger requirements are inclusive, selecting events that pass single muon and double muon triggers. Events that are triggered by the single muon triggers criteria contain muons that are isolated with either 22, 24, and 27 GeV muons. Double muon triggers have a 17 GeV threshold for the leading muon and 8 GeV for the subleading muon. Triple muon triggers are used for the

channels that have three muons in the final state and have a descending threshold of 12, 10, and 5 GeV. In addition, to properly select objects that coincide with the trigger additional trigger matching is conducted. The lepton is matched to the seed and filter bit that is generated at the L1 system. Trigger filter bit matching ensures that the objects and events that are counted are genuine.

### 5.2.2 Optimizing lepton pair selection

A simple selection algorithm was used to identify good lepton pairs that come from the pseudoscalar  $a$ . Standard working point cuts are made, and two oppositely charged, isolated muons with the largest scalar summed  $p_T$  are chosen to form the first decay products of the  $a$ . Two opposite charged  $\tau$  leptons with the largest scalar summed  $p_T$  are chosen for the second  $a$ . This approach increased the signal acceptance compared to choosing mass window cuts to form the  $a$  pairs. The following table reflects the pair matching efficiency study done with the preliminary dataset from 2016: . The dip in efficiency may be explained by the boosted or resolved  $a$  particles and their

Table 5.1: Lepton Pair Matching Efficiency

$a$ - Mass	15	20	25	30	35	40	45	50	55	60
Efficiency	0.87	0.82	0.79	0.79	0.79	0.80	0.80	0.83	0.85	0.87

decay products, assuming a Higgs particle is produced at rest. If the  $a$  mass is low then it is more relativistic, resulting in collimated leptons. If the  $a$  has a higher mass, then it is produced closer to rest and the leptons are identified back to back. It is possible that particle flow and association has a more difficult time in identifying decay products of the  $a$  particles in between the mass extremes.

### 5.2.3 Optimizing final state event selection

After picking the leading prompt muons from the  $a$  decay, the next step is to identify the other  $a$  decay by using various leptons in the final state. The final state comprises four leptons two muons coming from the leading  $a$  and two tau leptons coming from the subleading  $a$ . These  $\tau$  leptons can decay leptonically or hadronically, and this analysis counts all possibilities for the tau decay. Therefore, event selection is driven to find two prompt muons and all decay products of the tau leptons. There are four final states in total:  $\mu\mu e\mu$ ,  $\mu\mu e\tau$ ,  $\mu\mu\mu\tau$ , and  $\mu\mu\tau\tau$ . For notation, when

the final state is listed with a tau, such as  $\mu\mu\mu\tau$  the  $\tau$  is presumed to decay hadronically. The third muon in this context would also be coming from a leptonically decaying  $\tau$ . In addition to the kinematic requirements listed in 4.3, several cuts are made to select final state events. The following list contains cuts common to all channels:

- leading muons must have opposite charge coming from the  $a$
- tau decay products must have opposite charge coming from the other  $a$
- no b-quark tag jets
- signal extraction cuts (not shown in data MC control plots used in statistical test)
  - invariant mass of the 4 lepton system  $M_{4l} < 120 GeV$
  - $M_{\mu\mu} > M_{\tau\tau}$  (to account for energy loss from neutrinos).

Table 5.2: additional final state selection cuts

finalstate	cuts
$\mu\mu e\mu$	Iso. $\mu$ from $\tau \leq 0.2$ , Iso. $e$ from $\tau \leq 0.15$
$\mu\mu e\tau$	$\tau_h$ DNN against $\mu$ and $e$
$\mu\mu\mu\tau$	$\tau_h$ DNN against $\mu$ and $e$ , Iso. $\mu$ from $\tau \leq 0.15$
$\mu\mu\tau\tau$	$\tau_h$ DNN against $\mu$ and $e$

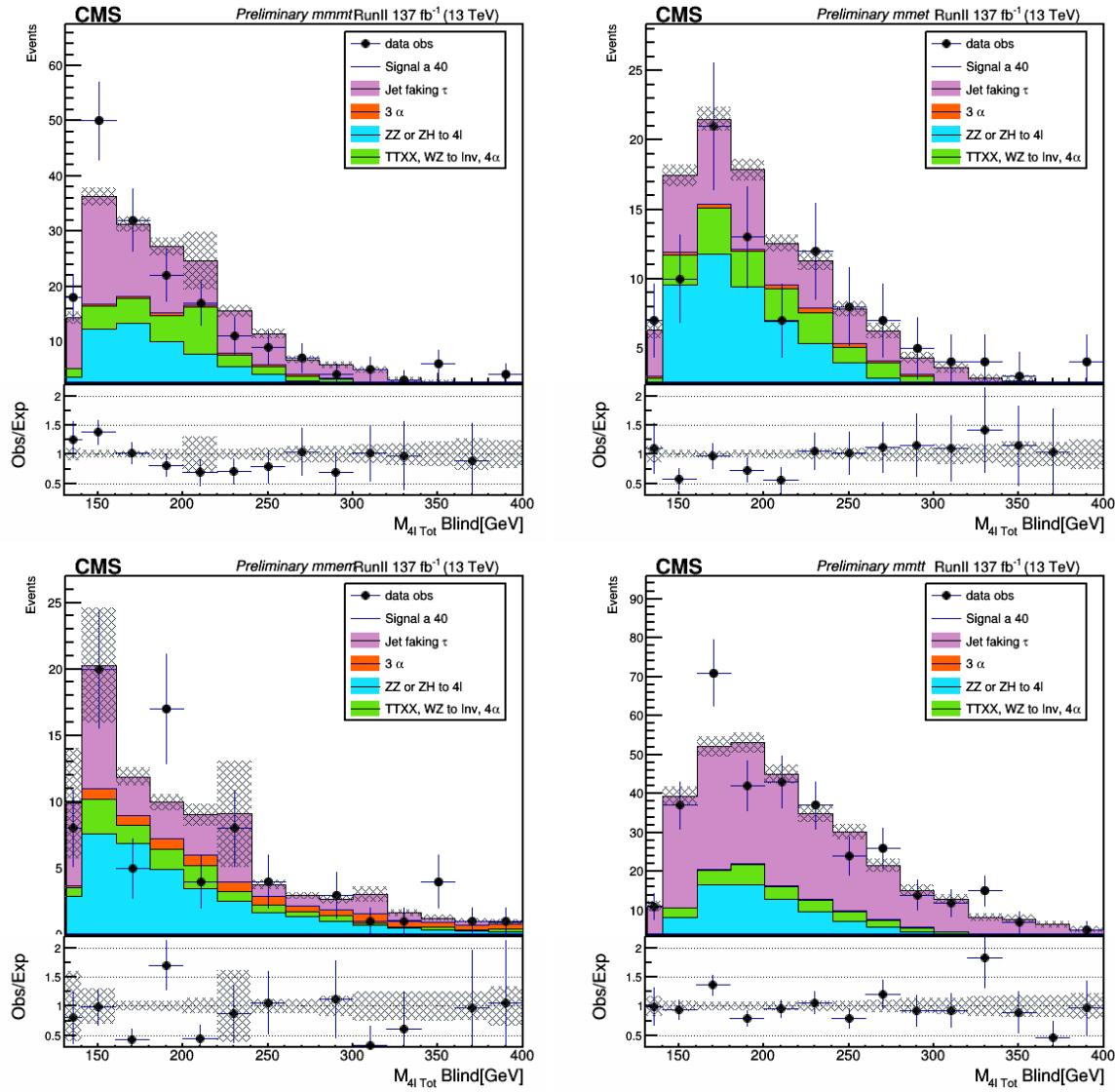


Figure 5.1: Invariant mass of the four lepton system for 2018 data in all Channels

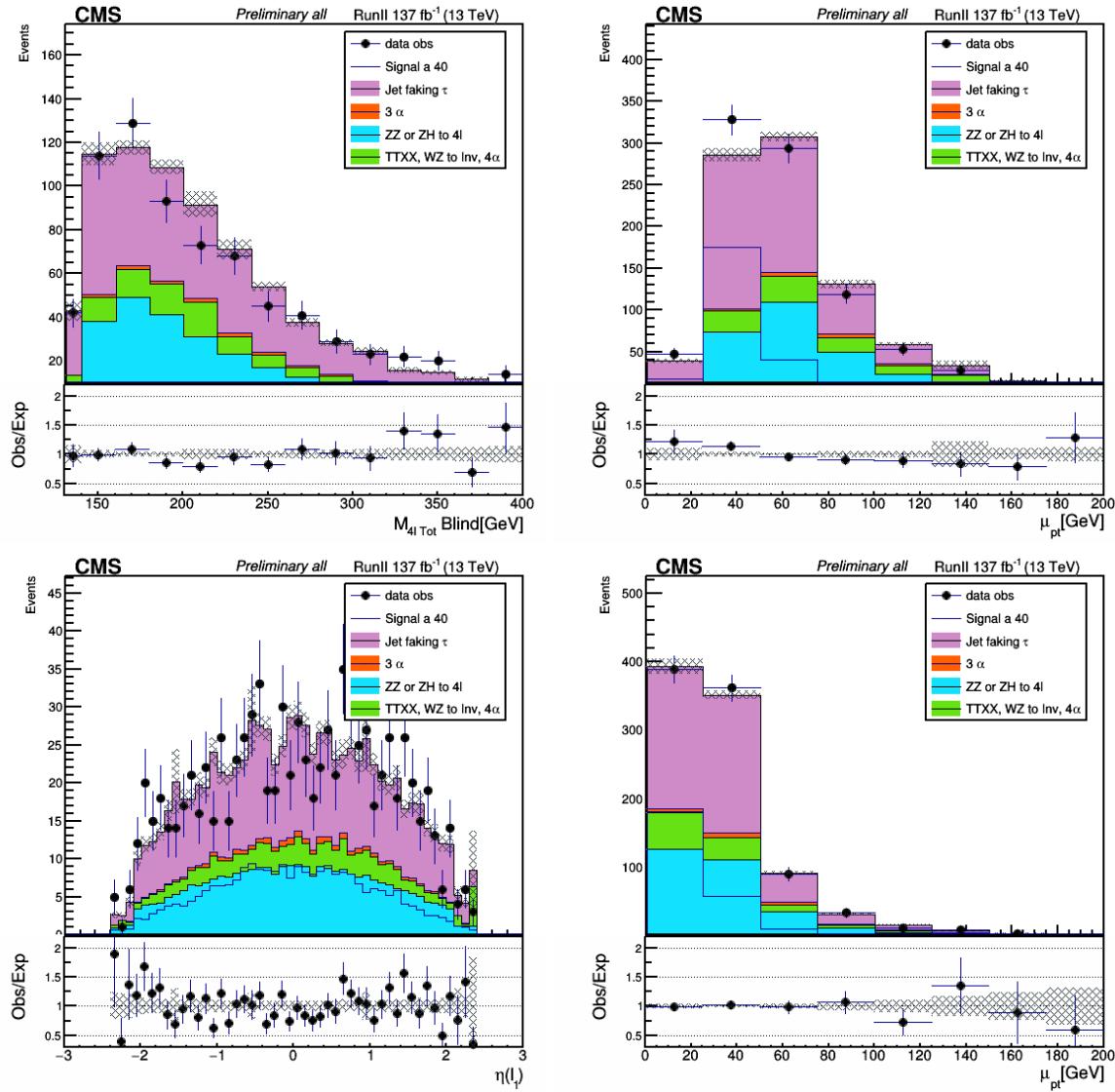


Figure 5.2: Several data-MC control plots for full RunII data in all Channels

# Chapter 6

## Background Estimation

Due to the stringent cuts in the signal region and absence of resonance, Monte Carlo (MC) simulation suffers from low statistics for some background processes. Therefore in addition to the Monte Carlo (MC) simulation, a data driven method is used to estimate a significant portion of background that simulation alone is not sufficient to measure. Tau leptons decay hadronically about 65% of the time forming intermediate mesons. The clusters of hadrons that these decays produce are jets; therefore, jets coming from other processes effectively fake the hadronic  $\tau$  signature. This is a non trivial fake rate to measure and account for in analyses.

In order to conduct the data driven method, a proportion is made to extract the jet faking tau background. Generally, this proportion is constructed using a region orthogonal to the statistical hypothesis test. For example this could be sign inversion on the lepton pair used in the final state. In this orthogonal region and in the signal region, tight and loose identification criteria are made to extrapolate the scale factor that estimate the tau's fake rate. The tight identification should be excellent at selecting true genuine tau leptons and the loose identification more inclusive to all tau leptons even those that are fake. The shape of the kinematic distributions should not change between the tight and loose regions for this method to hold true. Therefore, using the orthogonal regions—same sign and opposite sign—along with the loose signal region one can extrapolate the number of events in the tight signal region. Due to the four regions, the method is also referred to as the “ABCD” method.

## 6.1 Brief outline of the fake rate method

The fake rate function in the same sign (SS) region is *known*. Events passing loose identification in the opposite sign (OS) region is *known*. Events passing in the signal region is *unknown*. Assuming the shapes are similar and that the loose and tight identification is not dependent on the sign of the leptons. Then one can make the equivalence statement:

$$\frac{\text{Events}_{\text{SS Tight}}}{\text{Events}_{\text{SS Loose}}} \doteq \frac{\text{Events}_{\text{OS Tight}}}{\text{Events}_{\text{OS Loose}}} \quad (6.1)$$

To make the expression more precise, the fake rate function is typically parametrized in lepton candidate transverse momentum. Also, prompt MC is subtracted from data, which is motivated by estimating the true jet faking taus background (non-prompt taus). If MC is matched to prompt then it is unlikely a jet faking tau, so they are removed.

$$f(pt) = \frac{\text{Data Events S.S. Tight} - \text{Prompt MC Background}}{\text{Data Events S.S. Loose} - \text{Prompt MC Background}} \quad (6.2)$$

After the measurement is made for each tau candidate, then the fake rate is applied as an event weight to the opposite sign loose region in order to extrapolate to the signal region. So isolating the events in the signal region and flipping the relation in equation 6.1, one obtains the result for each lepton candidate in the final state:

$$\text{Events}_{\text{OS Tight}} = f(pt) \cdot \text{Events}_{\text{OS Loose}} \quad (6.3)$$

## 6.2 Measurement of the Fake Rate

To measure the fake rate, multiple categories are considered and motivated through the production processes which produce jets. As outlined in the SM Higgs decays to tau leptons analysis and its supporting document on fake rate measurements, several regions are used to determine the fake rate [27]. The separate jet “enriched” background regions are considered for each final state

- QCD multijet targeting the majority of jet $\rightarrow \tau_h$  fake events in the  $\tau_h \tau_h$  final state,
- W+jets targeting jets mostly in the e $\tau_h$  and  $\mu\tau_h$  final states,
- t $\bar{t}$  events targeting fully-hadronic or semi-leptonic decays.

These are then measured as a function of  $p_T$  of the object and then for final states involving hadronic tau leptons these are further split into subcategories depending on the decay mode.

In the QCD multijet region, there is no way to estimate it with pure MC simulation. Therefore, in order to estimate the QCD contribution all MC simulation events are subtracted before the measurements. Then the remaining fake rate measurement in the determination region is assumed to be from QCD.

In the W+Jets region, similarly all MC is subtracted except for the W+Jets simulation. Note that QCD contamination is minimal because of the dominance of the W boson resonance.

In the  $t\bar{t}$  region it is the same as the W+Jets regions, except the subtraction is  $t\bar{t}$ ; however, there is also an isolation region that is used because the fake rate for this process is expected to be very small and actually calculable using MC, so in addition to the genuine  $t\bar{t}$  events, the fraction of jets faking hadronic taus are also included in the subtraction.

To parameterize the fake rates as a smooth function in  $p_T$ , a line is fitted to each distribution. In addition to measuring the rate for each “enriched” background region, they are further split by final state or lepton candidate composition.

W+jets with no jets and one jet, QCD multi-jet with no jets, one jet, and more jets, and  $t\bar{t}$  make up the total number of background categories that are measured. Only plots pertaining to the  $\mu\mu e\tau$  and  $\mu\mu\mu\tau$  channels are created.

At high hadronic tau  $p_T$  (greater than 100 GeV), negative fake rates are possible because of low statistics and the linear fit model extrapolation, so if the candidate tau has a  $p_T$  of greater than 100 GeV then the rate at 100 GeV is applied.

In order to combine these “enriched” background regions and use it in an “ABCD” approach, the fraction of events for each of the background regions are combined in an overall fake rate that is still parametrized by  $p_T$  and category.

So the following steps are done for each final state to measure the fake rate:

1. Determine fake rate scale factor parametrized in candidate lepton  $p_T$  in the QCD, W+jets, and  $t\bar{t}$  regions
2. Make corrections based on the other lepton in the channel for closure
3. Make corrections based on the differences between the first step and the signal region

4. Determine the fraction of QCD, W+jets, and  $t\bar{t}$  events in the signal region.

To help in the presentation of the measurement regions, a table listing the enriched background and targeted final state along with the cuts and the anti-isolation requirement (the non-orthogonal condition in the ABCD method) will be presented. As indicated in the tables below,  $\mu\tau$  and  $e\tau$  final states share the same categories. For the  $\tau\tau$  channel, only the QCD “enriched” background category is considered. For the  $e\mu$  final state, the fake rate measurements from the  $\mu\tau$  and  $e\tau$  channels are used for the corresponding lepton.

Table 6.1: QCD “enriched” background category cuts for each channel, baseline selection cuts for events are made by default as listed in section 5 without the signal extraction cuts

final state	measurement cuts for QCD	anti-isolation criteria
$\mu\tau$	SS leptons Isolation $\mu \in (0.02, 0.15)$	$\tau$ VVVLoose DNN but fails Med. DNN
$e\tau$	SS leptons Isolation $e \in (0.02, 0.15)$	$\tau$ VVVLoose DNN but fails Med. DNN
$\tau\tau$	SS leptons subleading $\tau$ pass Med. DNN and leading VVVLoose DNN	leading $\tau$ fails Med DNN

Table 6.2: W+jets “enriched” background category cuts for each channel, baseline selection cuts for events are made by default as listed in section 5 without the signal extraction cuts

final state	measurement cuts for W+jets	anti-isolation criteria
$\mu\tau$	SS leptons $m_T$ between $\mu$ and $p_T^{\text{miss}} > 70$ GeV	$\tau$ VVVLoose DNN but fails Med. DNN
$e\tau$	SS leptons $m_T$ between $e$ and $p_T^{\text{miss}} > 70$ GeV	$\tau$ VVVLoose DNN but fails Med. DNN

Table 6.3:  $t\bar{t}$  “enriched” background category cuts for each channel, baseline selection cuts for events are made by default as listed in section 5 without the signal extraction cuts

final state	measurement cuts for W+jets	anti-isolation criteria
$\mu\tau$	SS leptons number of b-tag jets $\geq 1$	$\tau$ VVVLoose DNN but fails Med. DNN
$e\tau$	SS leptons number of b-tag jets $\geq 1$	$\tau$ VVVLoose DNN but fails Med. DNN

Fake factor measurements for the  $\mu\mu\mu\tau$  channel in the QCD region for 2017 is included in figure 6.1. The rest of the measurements are included in the Appendix B. For a more detailed description of the data driven background method along with the measurements for the closure and extra correction terms regard reference [27].

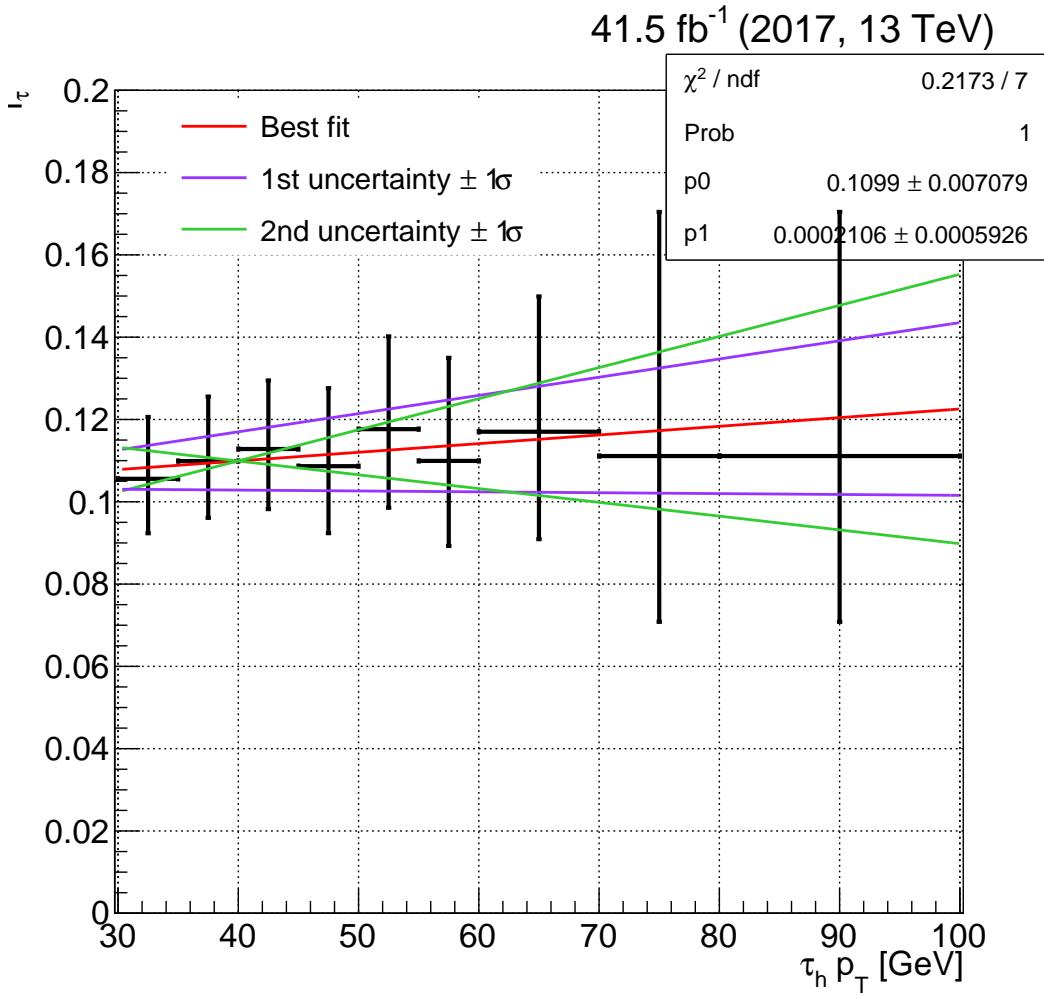


Figure 6.1: Fake factors determined in the QCD multijet determination region with 0 jet in the  $\tau_h$  final state in 2017. They are fitted with linear functions as a function of the  $\tau_h$   $p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

### 6.3 Application of the Fake Rate Method

After the jet faking tau rate is measured, it is then applied to events that are identified as loose. Since the final state involves two tau leptons, this procedure is applied to each tau lepton in the final state thus requiring application of the fake rate to four different possibilities. Each lepton candidate may be identify as loose or equivalently, failing the tight identification. The fake rate is then applied depending on the identification for each lepton candidate and in the case the event fails both candidate requirements then a minus sign is included to avoid the case of double counting. The final weight is then applied depending on the pass and fail criteria of each lepton candidate. The weight is effectively a transfer factor that is created using the fake rate measured earlier.j

- If event fails identification for  $\tau$  1:

$$w_1(pt) = \frac{f_1(pt)}{1 - f_1(pt)} \quad (6.4)$$

- If event fails identification for  $\tau$  2:

$$w_2(pt) = \frac{f_2(pt)}{1 - f_2(pt)} \quad (6.5)$$

- If event fails identification for both:

$$w_{12}(pt) = -\frac{f_1(pt)}{1 - f_1(pt)} \cdot \frac{f_2(pt)}{1 - f_2(pt)} \quad (6.6)$$

The weight is the ratio of tight events to loose events that explicitly fail the tight requirement.

To illustrate the different regions please consider the diagram outlining the different regions in the “ABCD” method 6.2.

This fake factor methodology has been used by other analyses such as the standard model Higgs measurement with an associated Z boson [29].

For a closure test, the same criteria are applied to the selection of the tight same sign region. The vast majority of the background should be jets faking taus in that case. Indeed it is shown in figure 6.3.

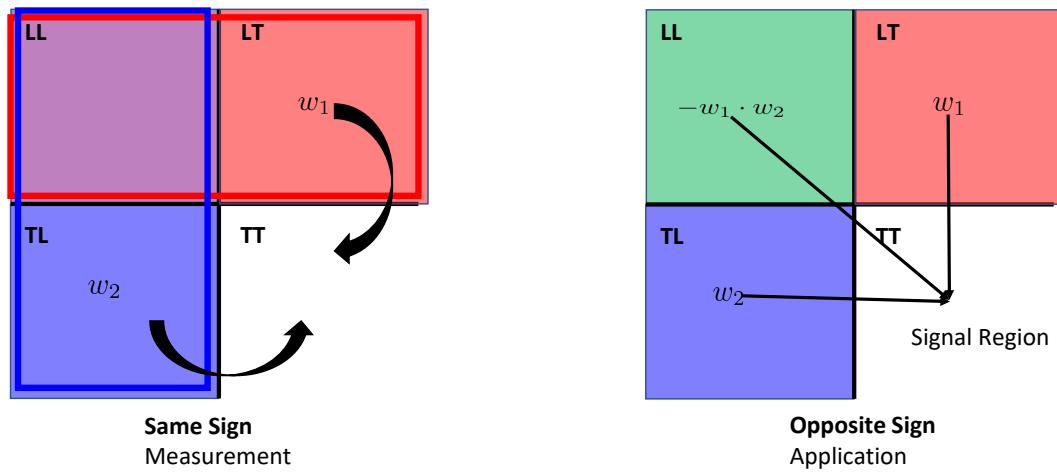


Figure 6.2: Diagram depicting the measurement and application regions, this “ABCD” method is multiplied by each of the  $\tau$  leptons in the final state

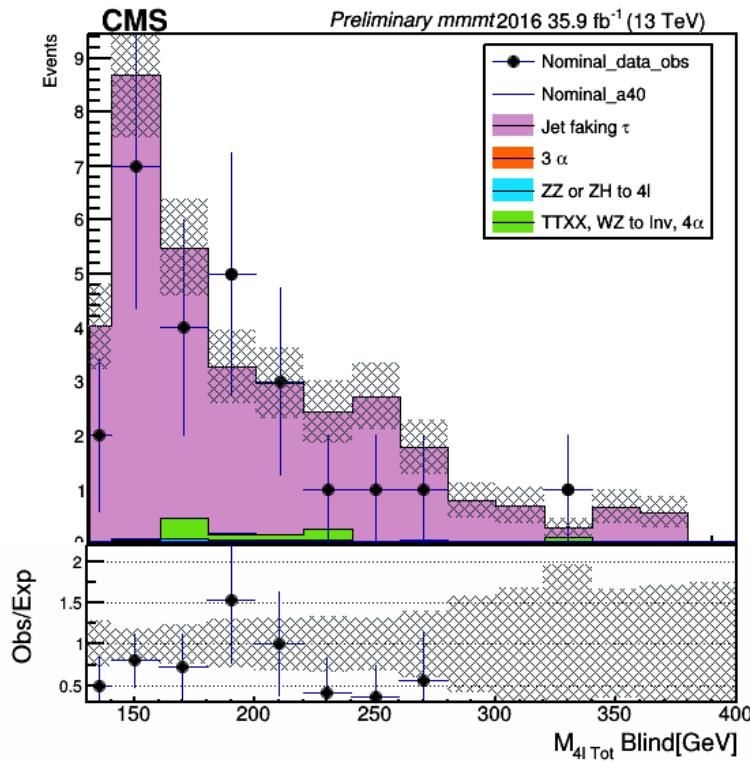


Figure 6.3: Validation of the fake factor method, fake factors are applied to the same sign tight region

# Chapter 7

## Statistical Inference Modeling

### 7.1 Statistical Inference at CERN

In order to conduct a hypothesis test, a test statistic is needed. In high energy particle physics this is typically constructed through the *profile likelihood ratio* and then a confidence level is set using the test statistic [30]. The construction of a likelihood is required along with the test statistic from the likelihood and a way to calculate a confidence level. To start, a binned histogram containing a distribution from a kinematic variable is chosen—like the mass of the parent particle—to be used in the hypothesis test. To construct the likelihood, the typical approach is to assume a Poisson distribution for the events in the  $i^{th}$  bin of the kinematic variable and then “smear” it by multiplying it with a Gaussian that is also dependent on the events. The Poisson distribution represents the true number of events one would expect and the Gaussian represents the systematic error—also denoted as nuisance parameters—that are endemic to the model. The events are split, into signal and background by construction. Because the amount of signal events isn’t known and is the subject of the search, they are allowed to vary by a coefficient denoted as  $\mu$  - the signal strength. For an upper limit, the signal strength is changed until the cumulative distribution function of the likelihood reaches the desired confidence or  $p$ -value.

$$\mathcal{L}(\text{data}|\mu, \theta) = \text{Poisson}(\text{data}, \mu \cdot s(\theta) + b(\theta)) \cdot p(\tilde{\theta}|\theta) \quad (7.1)$$

For binned  $n_i$  events in bin label  $i$ :

$$\text{Poisson}(\text{data}, \mu \cdot s(\theta) + b(\theta)) = \prod_i \frac{(\mu s_i + b_i)^{n_i}}{n_i!} e^{-\mu s_i - b_i} \quad (7.2)$$

. For reference:  $s$  and  $b$  demarcate the signal and background events respectively,  $i$  the bin number,  $n$  the total number of expected events, and  $\theta$  the Gaussian nuisance parameter.

In the case of this analysis, a slightly different likelihood is considered. A shape-based approach is studied, which uses probability density functions over the entirety of the fit variable. The fit variable is often called the parameter of interest (POI). Multiple PDFs can be combined in this scenario, but the important difference is the absence of any binning. Therefore a good fit is required. The construction of the likelihood for the unbinned parametric shape is then:

$$\text{Poisson}(\text{data}, \mu \cdot s(\theta) + b(\theta)) = k^{-1} \prod_i (\mu S f_s(x_i) + B f_b(x_i)) e^{-\mu S - B} \quad (7.3)$$

. Where  $k$  is the number of events,  $S$  and  $B$  the total event rate,  $f_s(x_i)$  and  $f_b(x_i)$  the probability density function, and  $i$  the number of different categories. A Bernstein polynomial would capture the slow changing background and the Voigtian captures the sharp peaking dimuon mass signal. Therefore in the pseudoscalar analysis, a product of Bernstein polynomials for  $f_b(x_i)$  and Voigtian functions for  $f_s(x_i)$  are used.

To outline the typical approach in the profile likelihood method, the follow steps are done in an effort to set the limit

1. To form the test statistic, the *profile likelihood ratio* is used

$$\tilde{q}_\mu = -2 \ln \frac{\mathcal{L}(\mathbf{D}|\mu, \hat{\theta}_\mu)}{\mathcal{L}_{\max}(\mathbf{D}|\hat{\mu}, \hat{\theta})} \quad 0 \leq \hat{\mu} \leq \mu \quad (7.4)$$

Where  $\hat{\mu}$  and  $\hat{\theta}$  are the maximum likelihood estimators,  $\hat{\theta}$  the optimized value of the estimator, and  $\mathbf{D}$  is the input dataset typically chosen as simulation for expected limits and real data for the observation.

2. Find the *observed* value of the test statistic  $\tilde{q}_\mu^{obs}$  for given signal strength  $\mu$ .
3. Find values of the nuisance parameters that best describe the experimentally observed data by maximizing the likelihood.
4. Generate toy MC pseudo data to construct probability density functions for signal and background  $f(\tilde{q}_\mu|\mu, \hat{\theta}_\mu)$  and  $f(\tilde{q}_\mu|0, \hat{\theta}_\mu)$  for background only hypothesis. These pdfs are the pdfs of the test statistic under the assumption of a signal strength.

5. Define  $p$ -values to be associated with the actual observation for both  $s + b$  and  $b$  only hypotheses

$$p_\mu = P(\tilde{q}_\mu \geq \tilde{q}_\mu^{obs} | s + b) = \int_{\tilde{q}_\mu^{obs}}^{\infty} f(\tilde{q}_\mu | \mu, \hat{\theta}_\mu^{obs}) d\tilde{q}_\mu \quad (7.5)$$

$$1 - p_b = P(\tilde{q}_\mu \geq \tilde{q}_b^{obs} | b) = \int_{\tilde{q}_b^{obs}}^{\infty} f(\tilde{q}_\mu | \mu = 0, \hat{\theta}_b^{obs}) d\tilde{q}_\mu \quad (7.6)$$

. Then take the ratio to form the confidence levels (CLs)

$$CL_s(\mu) = \frac{p_\mu}{1 - p_b} \quad (7.7)$$

- .
6. Let  $\alpha$  be the measure of confidence, then for  $\mu = 1$  if  $CL_s \leq \alpha$  then the signal hypothesis is rejected in favor of the background only hypothesis
7. Further, to quote a 95% confidence level on  $\mu$ , we need to adjust the signal strength ( $\mu$ ) , until  $CL_s = 0.05$

## 7.2 Worked Example for Low Stat Analyses

Order of magnitude estimates for low stat analyses like the Higgs decay to pseudoscalars can be obtained by considering a very simple statistical inference model.

Suppose there are  $N$  events

$$N = B \cdot \sigma \cdot A \cdot \mathcal{L} \quad (7.8)$$

where  $B$  is the branching fraction for the physics process,  $A$  is the signal acceptance,  $\sigma$  is the cross section, and  $\mathcal{L}$  is the luminosity. As outlined in the previous section, suppose that the number of expected events follows a Poisson distribution. In the case of a background model predicting 0 average events, the upper 95% bound would be 3.7 events.

Inverting the relation

$$B = \frac{N}{\sigma \cdot A \cdot \mathcal{L}} \quad (7.9)$$

Selecting the signal acceptance from the pseudoscalar analysis (2016  $\mu\mu\mu\tau$ )

$$A = \frac{\text{events pass all cuts}}{\text{starting events}} = \frac{1293}{250000} \approx 0.005 \quad (7.10)$$

and taking the cross section for gluon gluon fusion production of the Higgs  $\sigma = 48\text{pb}$  along with the luminosity for 2016  $\mathcal{L} = 35,900\text{pb}^{-1}$

Then the upper 95% CL limit on the branching fraction is

$$B = \frac{N}{\sigma \cdot A \cdot \mathcal{L}} = 0.00043 = 4.3 \times 10^{-4} \quad (7.11)$$

### 7.3 Fit model for pseudoscalar Higgs search

After the signal extraction cuts are applied, an unbinned parametric likelihood fit was done with various shapes depending on the background and signal categorization. There is one signal distribution depending on the hypothesized  $a$  mass, and two background distributions that are considered in the final fit. The two contributing background distributions originate from “Irreducible” events coming from two Z bosons (ZZ) and from “Reducible” events coming from jets faking tau leptons (FF).

For the signal, a Voigtian function is used to fit the pseudoscalar  $a$  mass spectrum in a small window - 2GeV - of the hypothesized  $a$  mass for the sample as in figure 7.2. The Voigtian shape was chosen to reflect the narrow simulated peak that is statistically smeared by experimental measurement. The Voigtian function is a Gaussian convoluted with a Lorentzian function, so in addition to the Gaussian parameters there is one extra degree of freedom which is associated with the Lorentzian. The Lorentzian controls the sharpness of the distribution. For the signal MC, the standard deviation of the distributions tends to increase as the mass approaches 60 GeV. To compare the signal MC distributions, they are all plotted in figure 7.1.

Shapes from the signal samples in intervals of 5 GeV across the whole fit range 20-60 GeV are interpolated using spline functions for the fit parameters, thus precise limits can be obtained at the 1 GeV granularity. The interpolated model describes the signal samples well and produces similar results for the distributions at the 5 GeV granularity. A spline function is created for the mean, standard deviation, normalization, and the Lorentzian. A first order polynomial is used to fit the mean and a third order polynomial is used to fit the standard deviation, normalization, and Lorentzian. An example of such functions are shown in figure 7.3. The bands that envelope the spline indicate the spread and the accepted error on the spline in the statistical inference model.

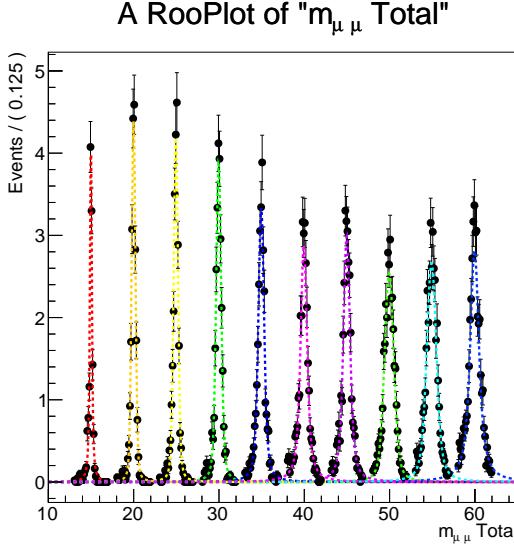


Figure 7.1: Signal fit using a Voigtian function

For the irreducible background coming from  $ZZ \rightarrow 4l$ , a Bernstein polynomial is used to fit the shape over the entire  $a$  mass range in figure 7.7. Depending on the final state and shape, the degree of the polynomial is chosen by best fit. A Fischer F-test was conducted and there doesn't seem to be enough statistics in the bins to provide an accurate difference in the log-likelihood in order to recommend a particularly higher order polynomial over other orders. Thus for  $\mu\mu\tau\tau$  and  $\mu\mu e\tau$ , a 1st order polynomial is used. For the channels that do have more events like  $\mu\mu\mu\tau$  and  $\mu\mu e\mu$ —albeit even for a lower number of integrated events—a quadratic function is used. The true values of the error estimation on the parameters are taken from the fit itself and can be seen in the plots like figure 7.7. The error on these shape parameters are shown in the impacts which demonstrate how the fit parameters effect the overall statistical inference model C.1.

For the jet faking tau background, a Bernstein polynomial is also used to fit the shape over the entire  $a$  mass range in figure 7.8. Similar to the ZZ or irreducible background, the jet faking tau background polynomial degree is chosen by best fit.

The rest of the channels and years are shown in the appendix D.

In order to measure the systematic effects on the final distribution and the fits, changes in the fit templates are done and propagated to the fit model in the form of rate parameters. These rate parameters differ slightly between the signal and background distributions. For background, the error in the fit parameters is directly included in the uncertainty model.

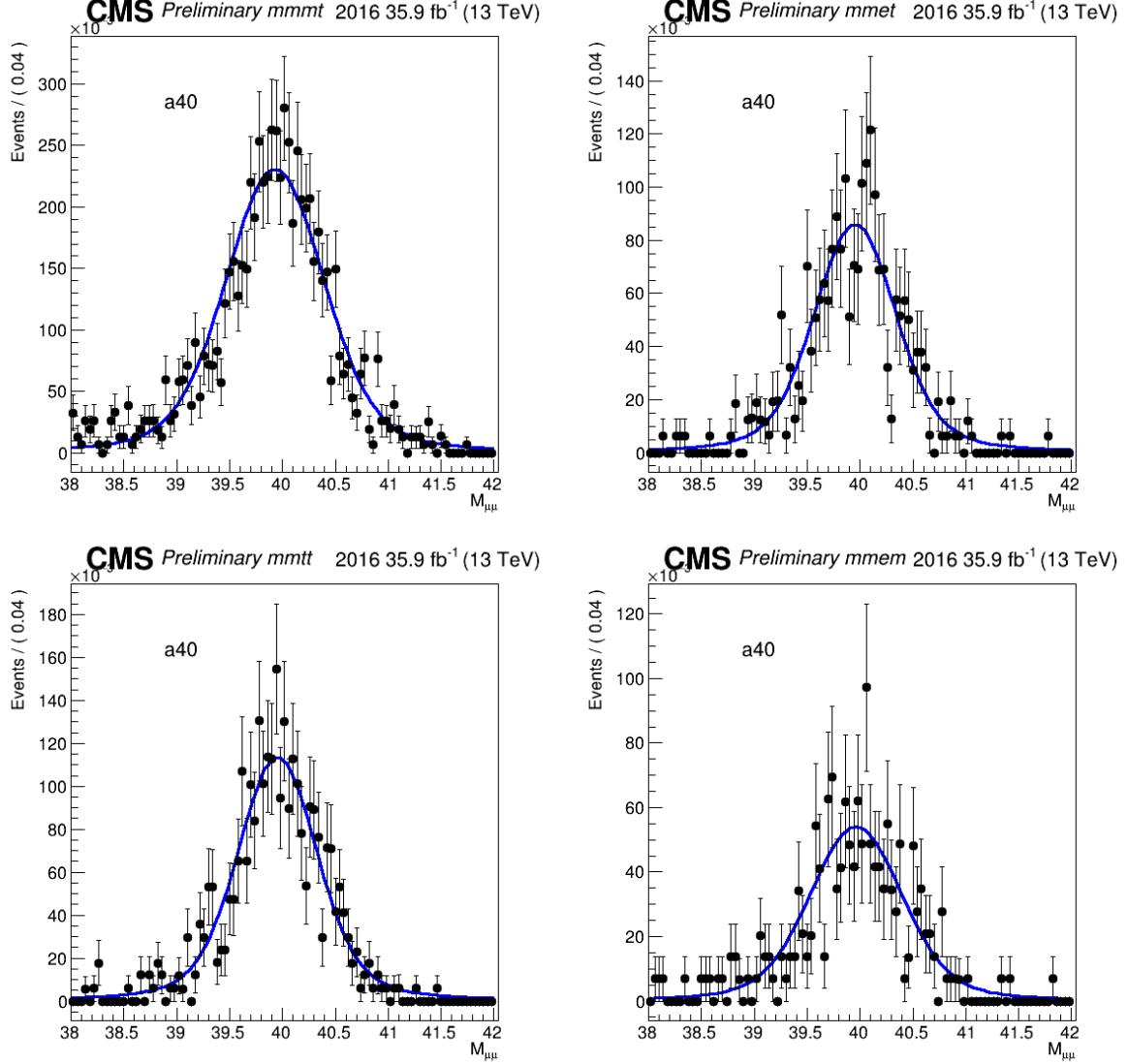


Figure 7.2: Signal fits using a Voigtian function for a-mass at 40GeV

The uncertainty of the spline function affects the uncertainty for the signal, so it is included in the fit model. As mentioned in the fit model section 7.3 and shown in figure 7.3, the magnitude of this uncertainty is estimated from the fit of the parameters for the spline. Overall, a 10% uncertainty is used for the lorentzian (alpha) and 20% for the standard deviation (sigma) and 0.5% for the mean (mean). Although the mean is measured very precisely, the energy scale shifts from the leptons are included in this number. At the section highlighting the uncertainties 4.4, one can see the bin-shift from the energy scale. The bin-shift indicates the amount the mean of the distribution is affected from the energy scale shift. The shift should fit within the envelope of the

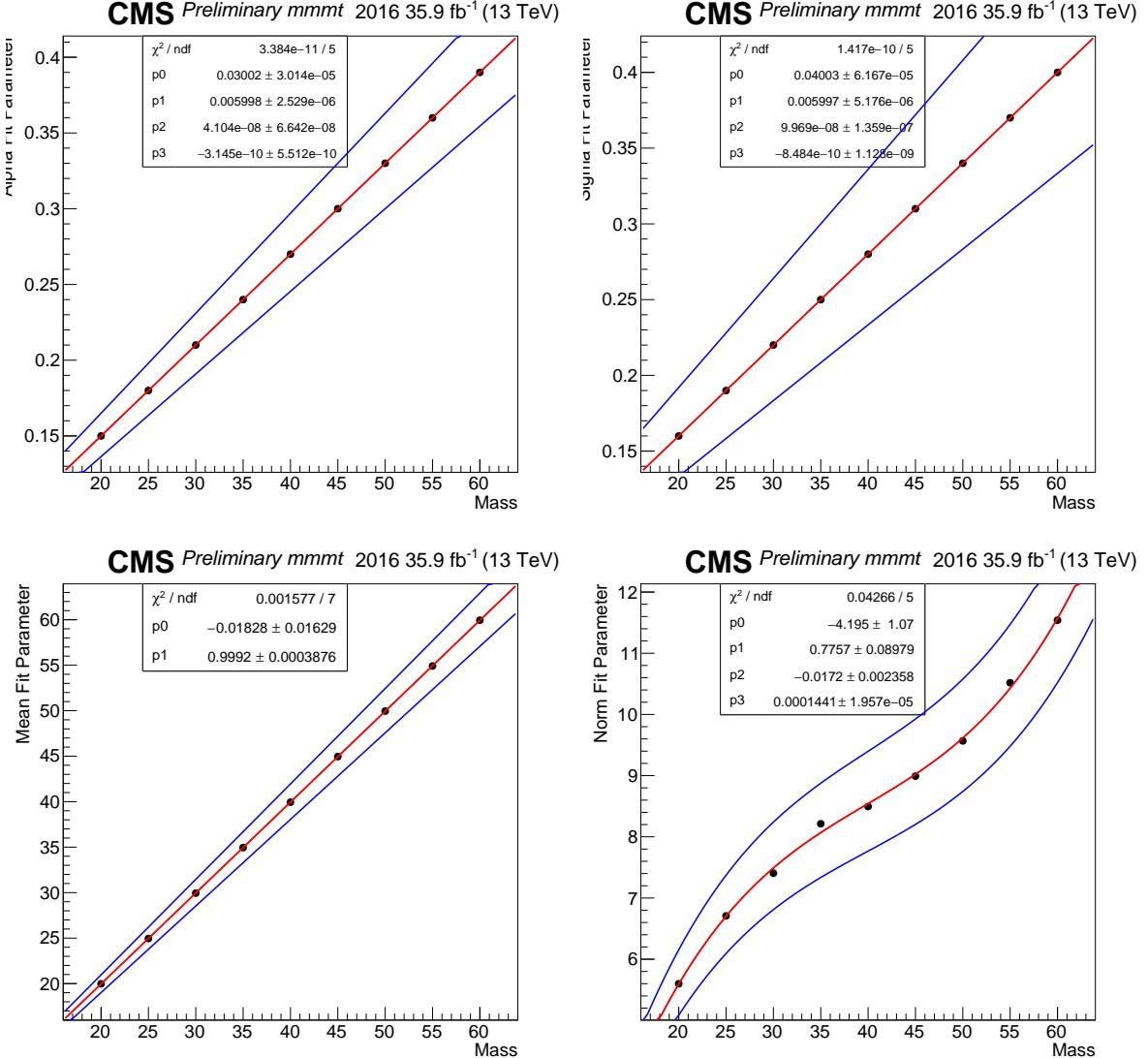


Figure 7.3: Spline functions for 2016 mmmmt a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

percentage on the parameter.

For the other systematic uncertainties that are not based on parametric shapes, like the energy scale of the leptons, a log-normal deviation to the normalization is used. The extent to which these systematics effect the search is calculated through the concept of the “impact”. An impact is a way to see how that systematic uncertainty impacts the overall statistical model. To measure an impact for a particular systematic uncertainty, it is allowed to vary within the fit range while the rest of the parameters in the likelihood function are frozen. The corresponding difference in the signal strength is measured. In order to read the impact plots and to understand what the impacts represent in

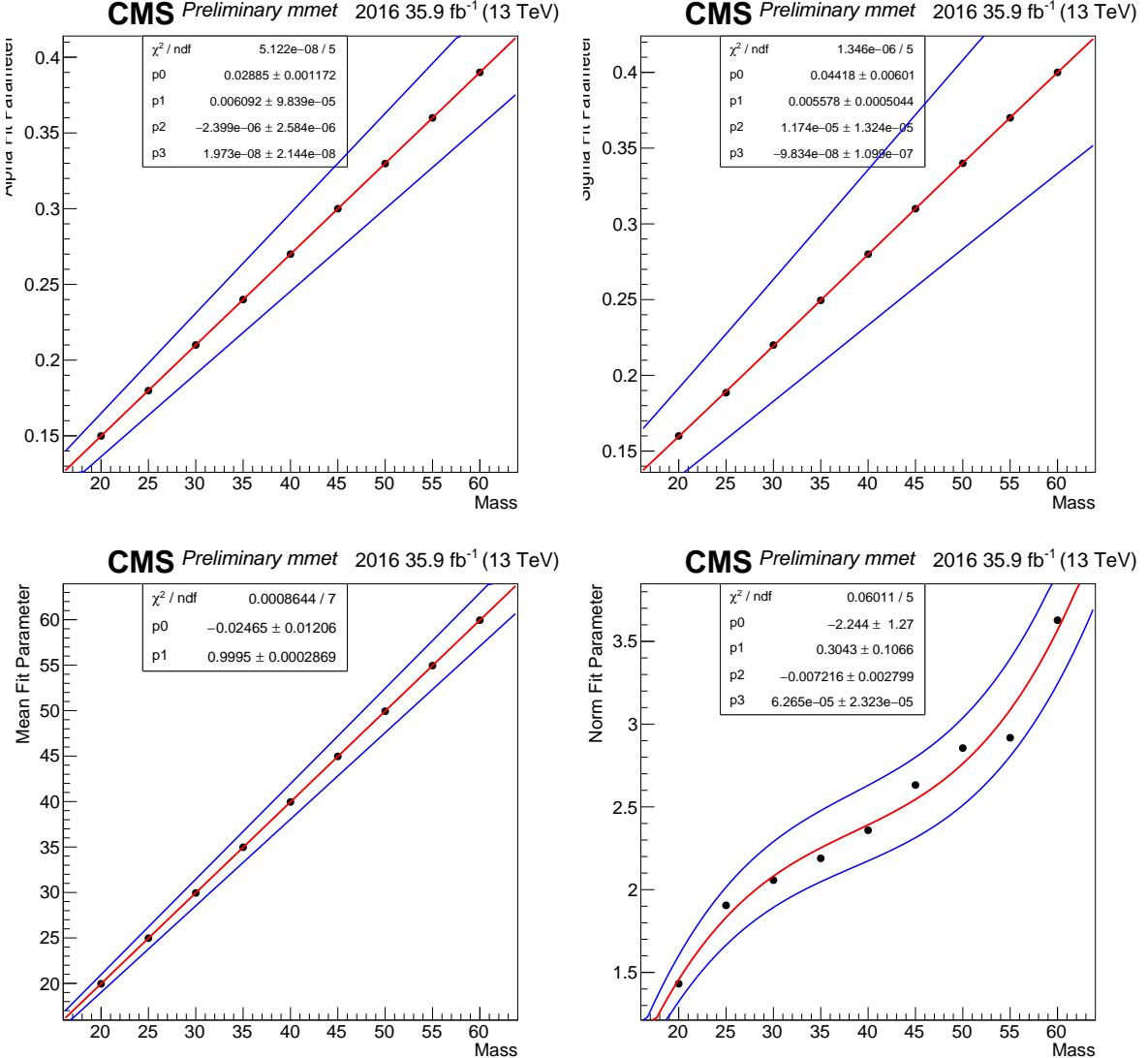


Figure 7.4: Spline functions for 2016 mmet a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

the fit model please look at table 7.1: Each impact has a corresponding nomenclature, range of variation, and effect on the POI. The nomenclature is listed in 7.1 and the variation and effect on the POI is seen in the plots 7.9.

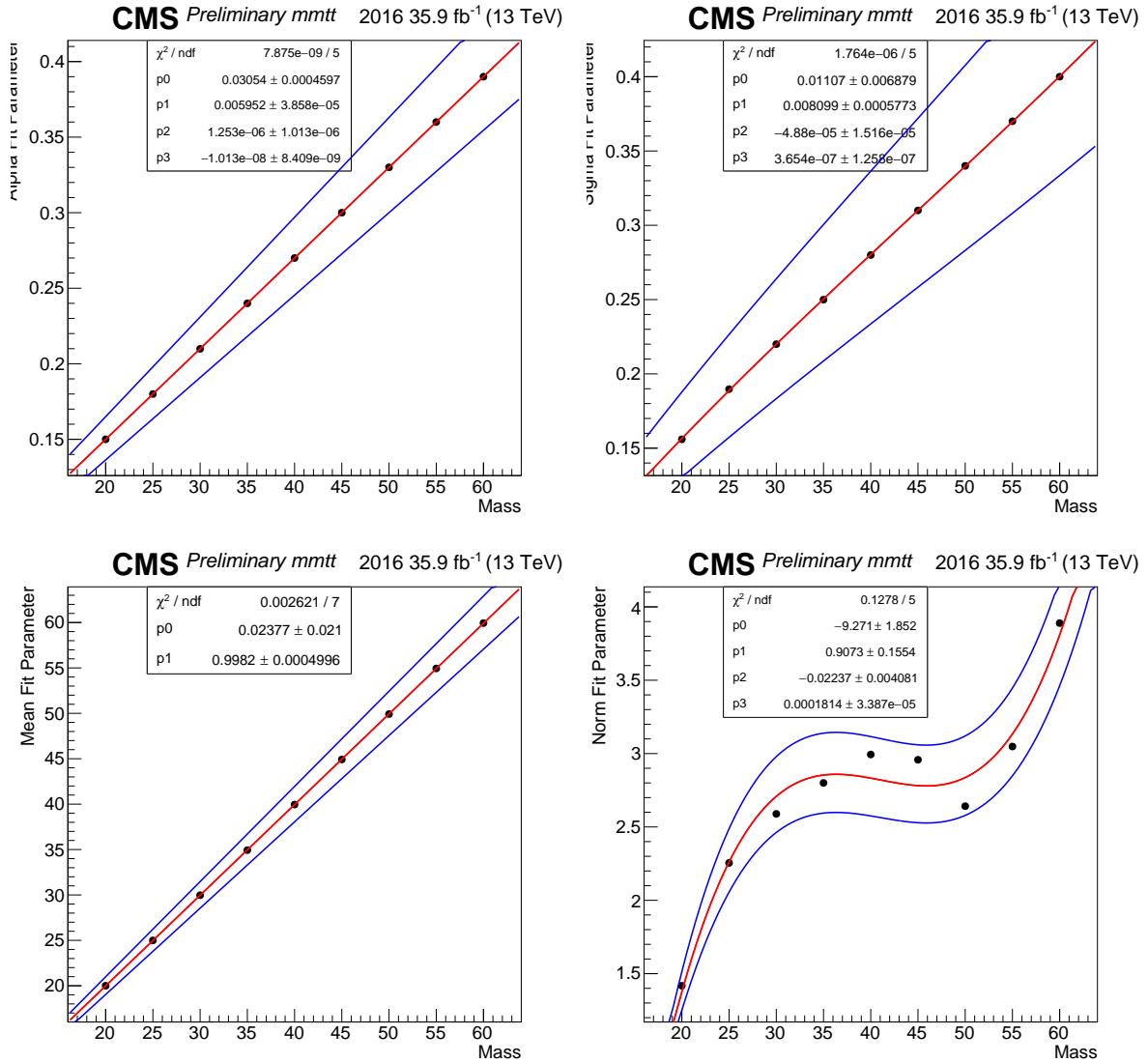


Figure 7.5: Spline functions for 2016 mm tt a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

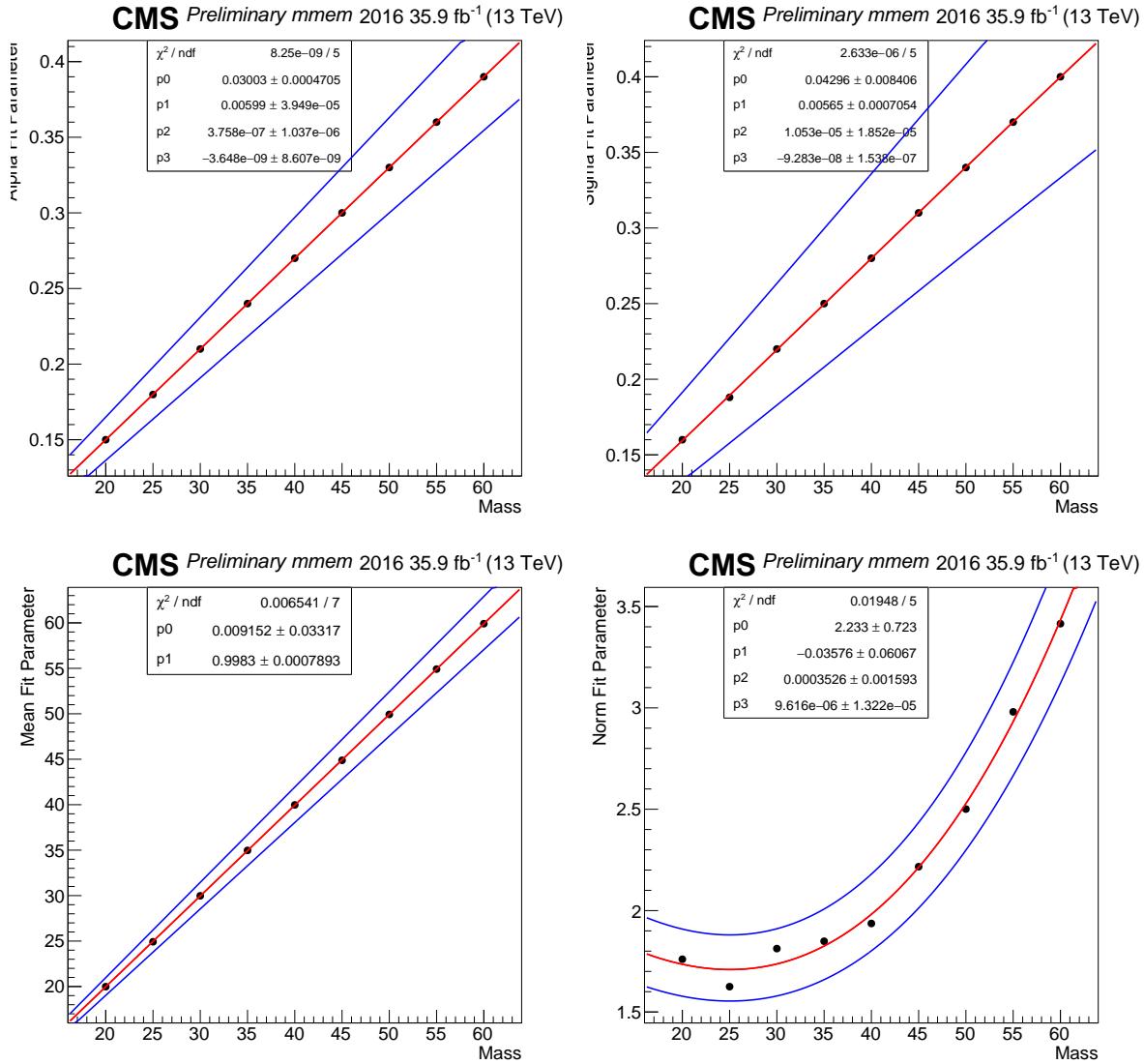


Figure 7.6: Spline functions for 2016 mmem a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

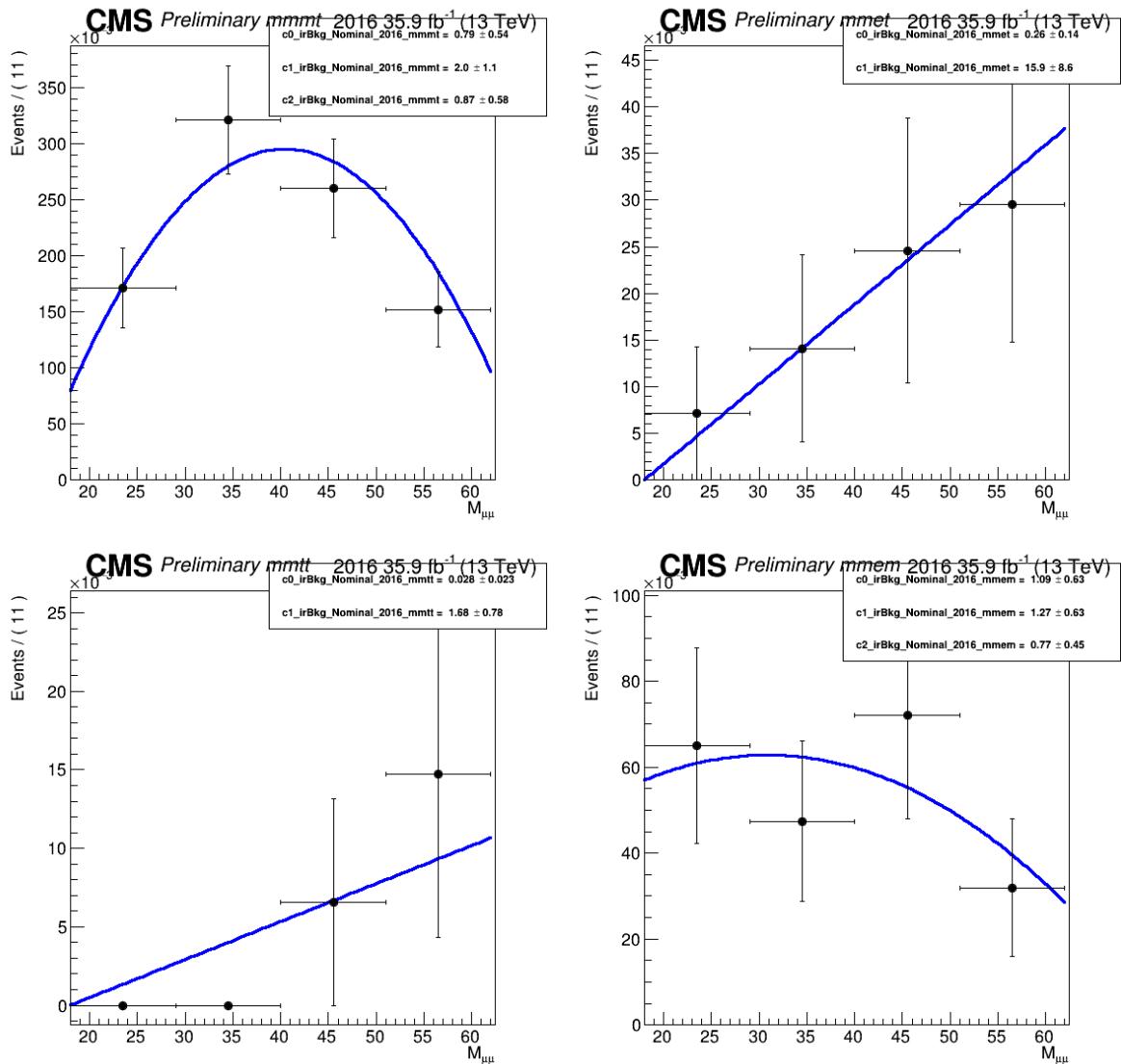


Figure 7.7: Irreducible background fit using Bernstein polynomials

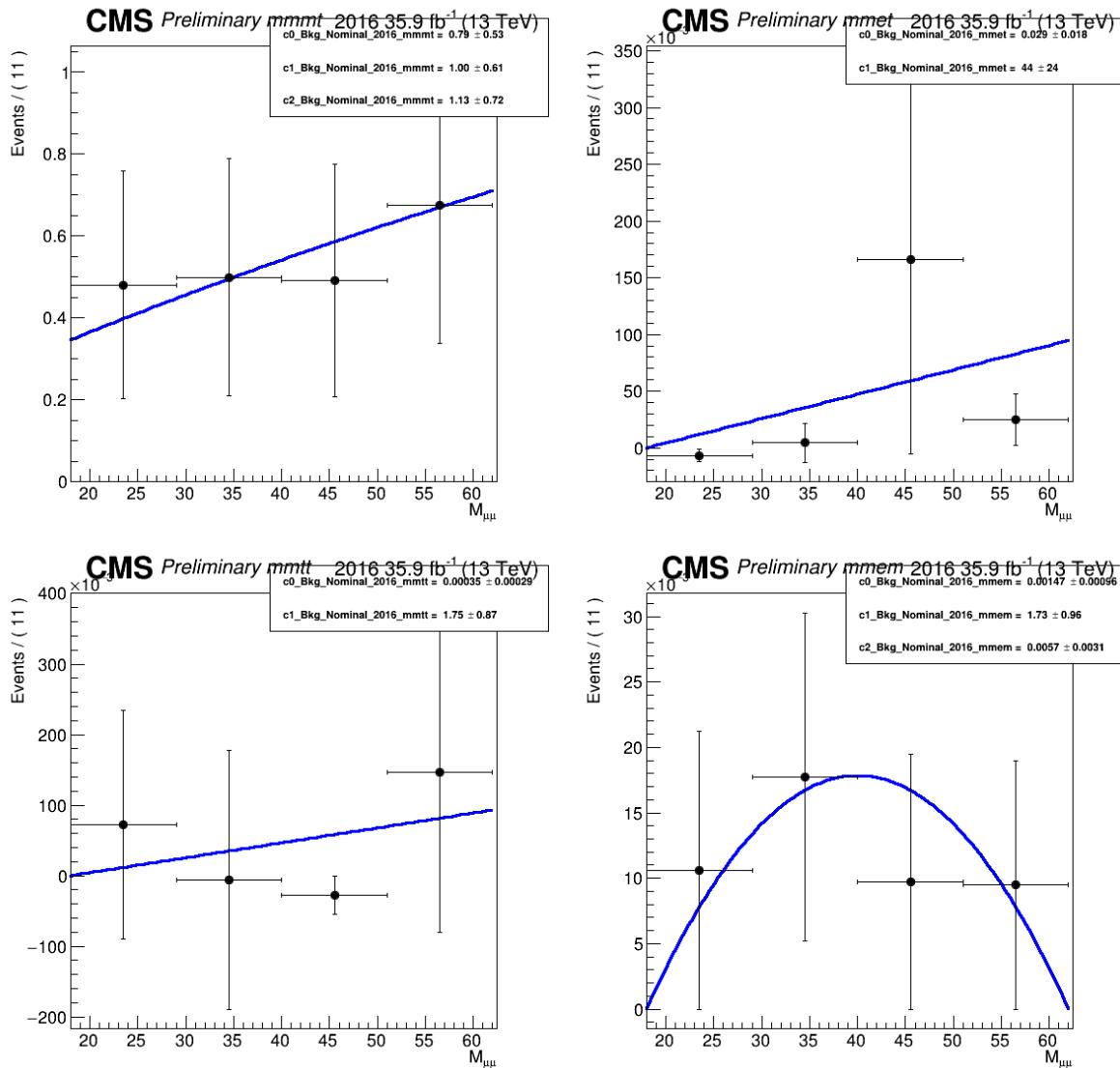


Figure 7.8: Reducible background fit using Bernstein polynomials

Table 7.1: List of uncertainties with the corresponding name and description. The name directly refers to the variable in the impact plots 7.9.

Name of Uncertainty	Description	Magnitude
scale	e, $\mu$ , and $\tau$ (split by decay mode) energy scales	% channel dependent
c0_, c1_, ... cN_	Coefficients of the Bkg (datadriven) or irBkg (ZZ) parametric shape	% channel dependent
lumi	luminosity uncertainty	(1.6% )
intAlpha	alpha interpolated spline function shape uncertainty	(10%)
intSigma	sigma interpolated spline function shape uncertainty	(20%)
intMean	mean interpolated spline function shape uncertainty energy scale shift uncertainties for signal included	(5%)

Systematic impact distributions, sometimes referred to as pull distributions, is listed in figure 7.9. The rest of the channels and years are located in the appendix C.

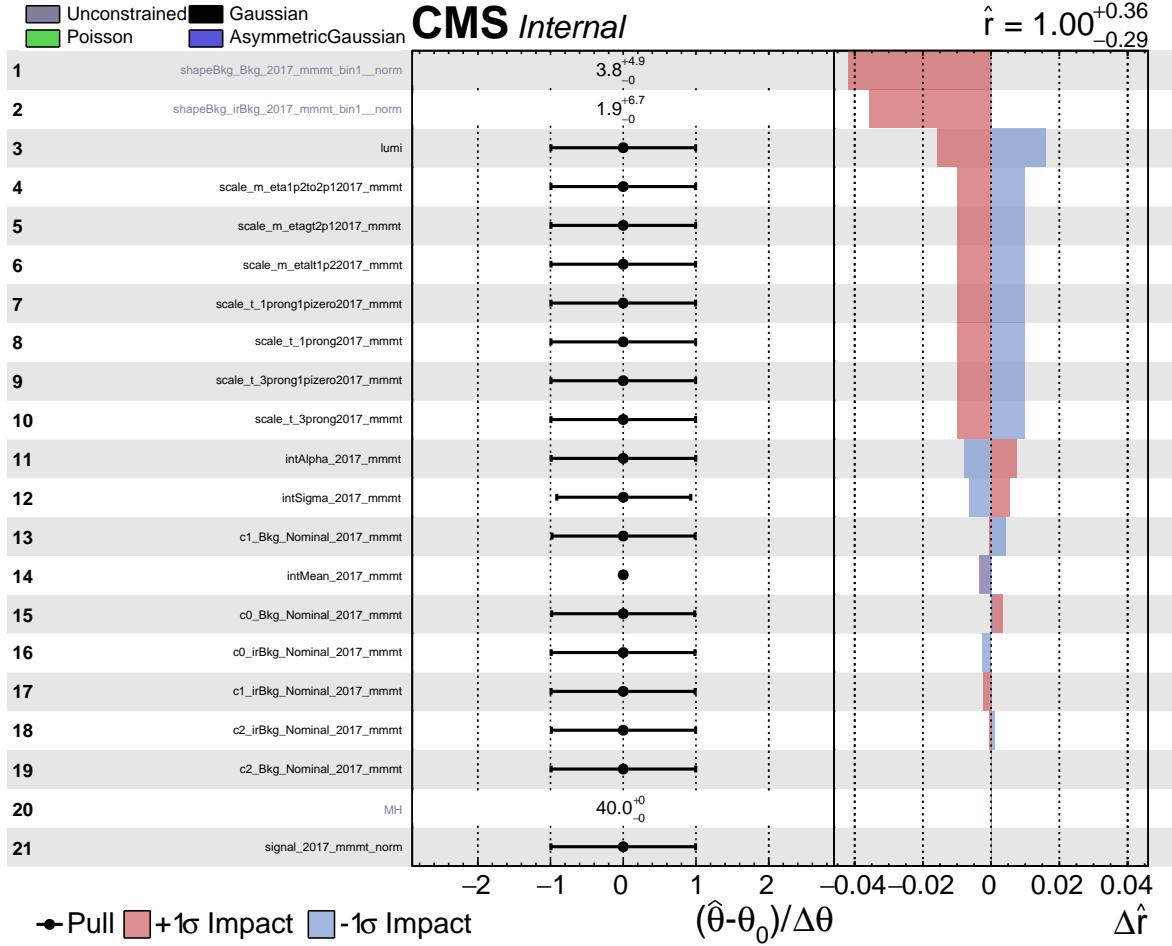


Figure 7.9: Expected systematic impacts for the fit model  $\mu\mu\tau$ , as normalization impacts (shapeBkg\_Bkg and shapeBkg\_irBkg), these are expected to be one-sided, and—as mentioned in the fit model 7.1—the mean is precisely measured and is expected to be constrained less than one for most channels

# Chapter 8

## Conclusions

### 8.1 Results

After the final event selection, including the signal extraction cuts listed in section 5.2.2, the statistical hypothesis test can be made. The final number of events listed in each category for the full Run II dataset is shown in the table 8.1 below

Table 8.1: Expected event yields of signal and background categories across all years pertaining to  $137 \text{ fb}^{-1}$ .

Signal $m_a = 40 \text{ GeV}$	Background	
	Data Driven (FF)	Irreducible (ZZ)
6.54	23.61	6.33

As discussed in the previous section 7.3, the shapes that were created are used in an upper limit for each mass point. Initial values of the signal distributions are selected to make sure that the signal strength modifier ( $\mu$ ) in the limit is of order unity. The range of masses in the limit is between 20 GeV and 60 GeV to ensure compatibility with  $h \rightarrow aa$  combination limits for more exotic Higgs models—like those at lower  $a$  mass. In order to estimate the upper limit at 95% CL on the branching fraction, a simple Poisson model can be used. For a statistically limited search, we can estimate the background yield as no events. The estimated upper limit on the branching fraction calculated earlier is:

$$B = \frac{N}{\sigma \cdot A \cdot \mathcal{L}} = 0.00043 \quad (8.1)$$

. This limit is set by adjusting the signal strength (event yield) until a p-value of 5% is reached on the joint likelihood function for the fit model. The event yield is normalized with a branching fraction, which was assumed to be  $\sigma_{SM}(h) \times 0.01\%$ . Multiplying the CL by 0.01% returns the limit on  $\frac{\sigma_h}{\sigma_{SM}} B(h \rightarrow aa \rightarrow 2\mu 2\tau)$ . Preliminary limits are set using the asymptotic limit method [30] for each mass point.

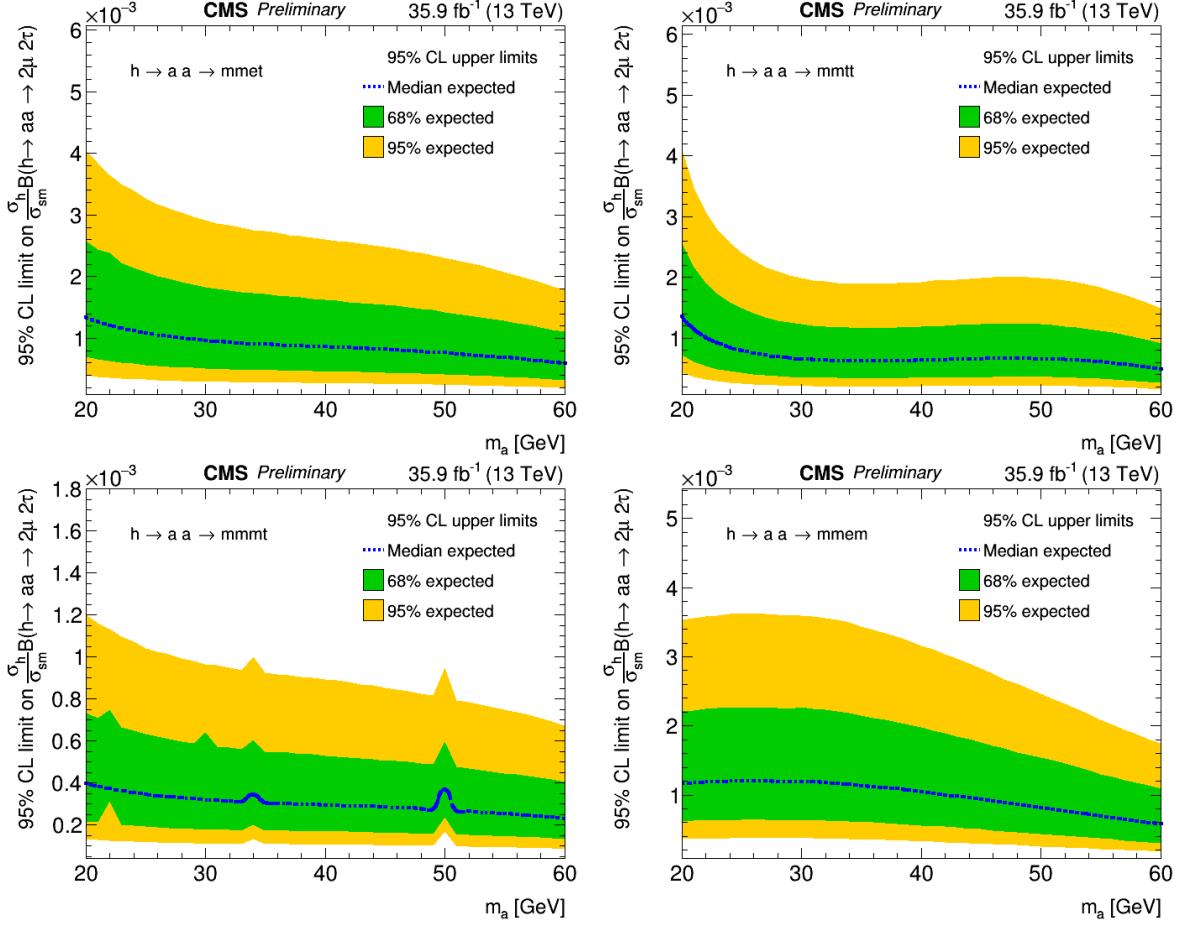


Figure 8.1: Asymptotic CL Limits on the branching fraction times ratio of the SM cross section for 2016

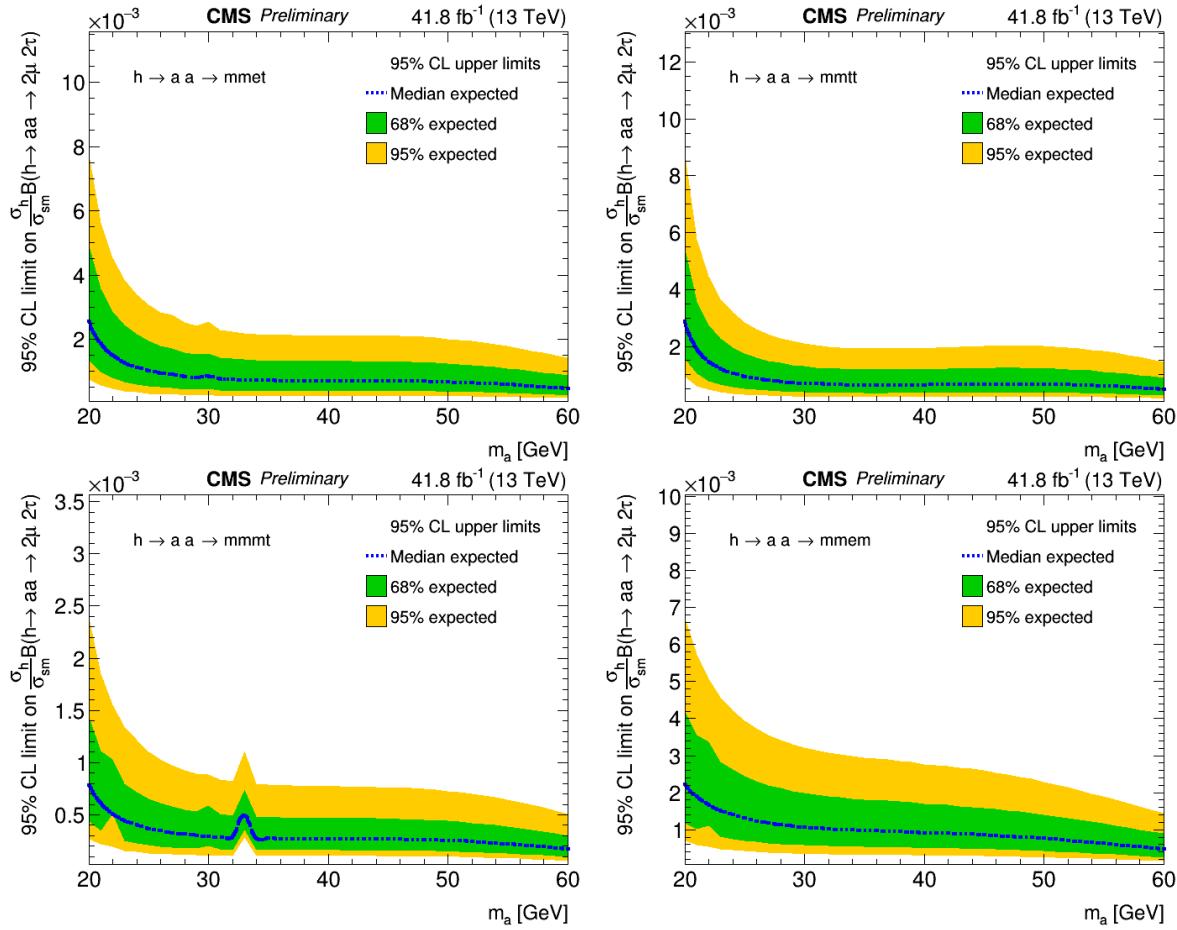


Figure 8.2: Asymptotic CL Limits on the branching fraction times ratio of the SM cross section for 2017

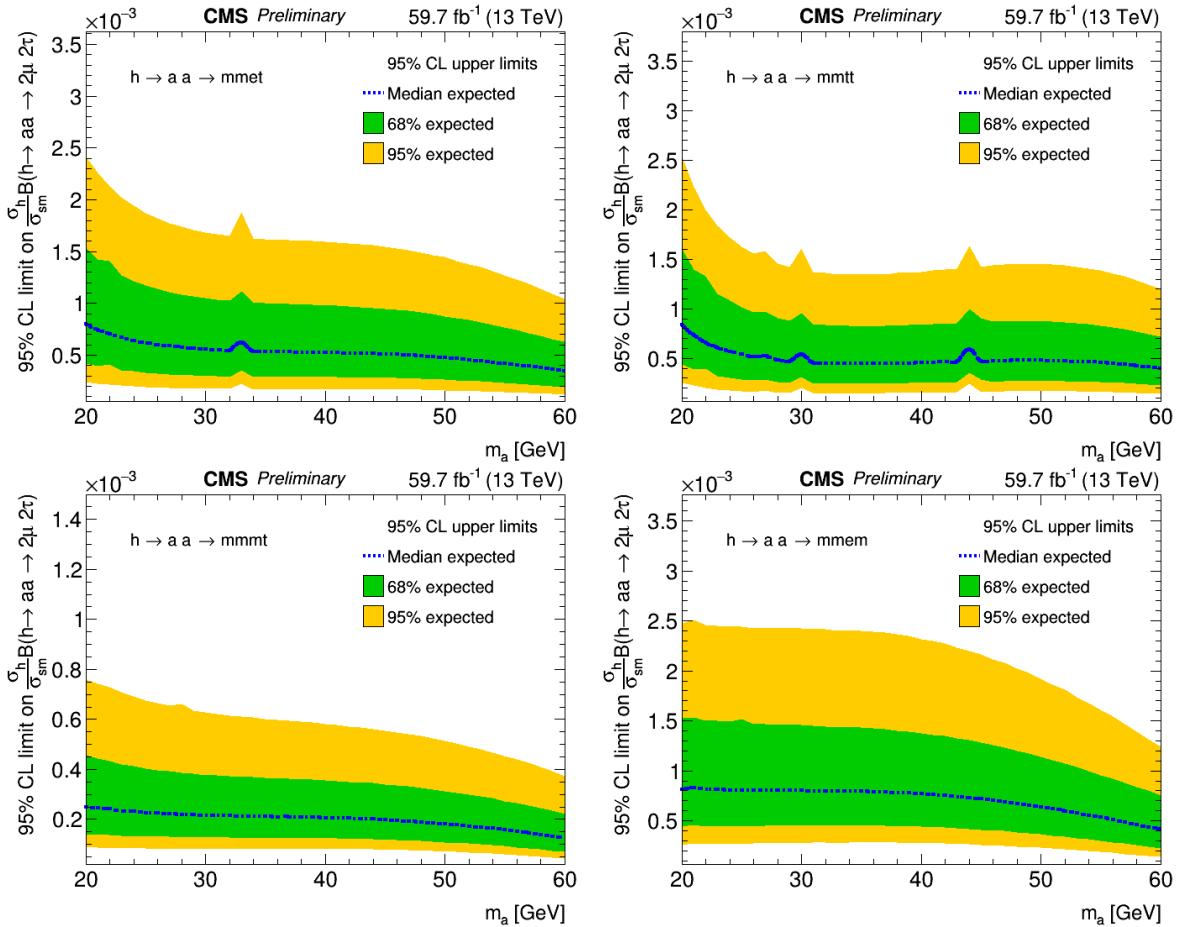


Figure 8.3: Asymptotic CL Limits on the branching fraction times ratio of the SM cross section for 2018

All of the years and channels are then added together to form the combined result and the model 2HDM+S interpretations for different scenarios. Type III, where coupling to  $\tau$  leptons is favored, is expected to be the most stringent scenario for this final state. More parameter space in theory is excluded at the upper 95% level in regions of lower values on the limit (regions in blue) in figure 8.5. Type I excludes mostly high mass particles and isn't depended on  $\tan \beta$ . Type II and III exclude more at high  $\tan \beta$  region as opposed to Type IV which excludes at low  $\tan \beta$ .

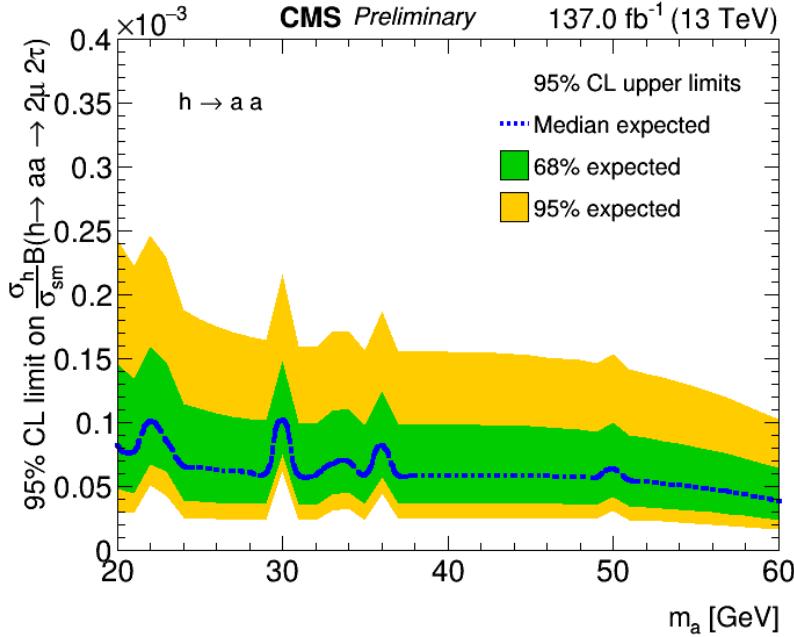


Figure 8.4: Asymptotic CL Limits on the branching fraction times ratio of the SM cross section for the full Run II dataset 137fb<sup>-1</sup>

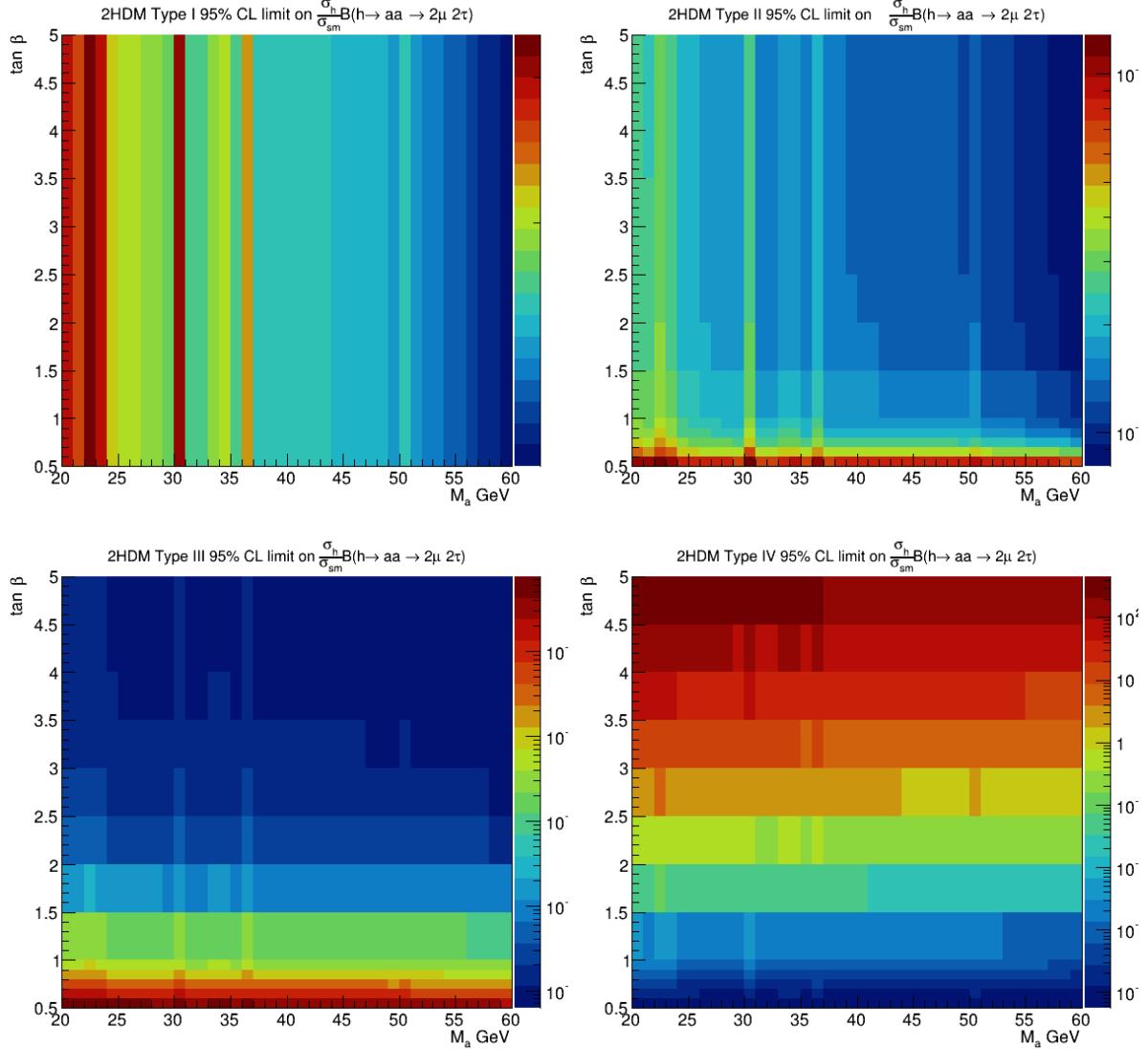


Figure 8.5: upper 95% CL limits on the branch fraction of  $h \rightarrow aa$  times the ratio of the SM cross sections for the full Run II dataset ( $137\text{fb}^{-1}$ ) for different 2HDM+S model specific scenarios.

## 8.2 Conclusion

An overview of the Large Hadron Collider, CERN, CMS, luminosity operations, and an analysis focusing on the search for a BSM processes involving an exotic Higgs-like particle was presented. Using the full Run II dataset collected at CMS corresponding to an integrated luminosity of  $137\text{fb}^{-1}$ , the search for the SM Higgs Boson,  $h$ , decaying to a pair of pseudoscalars,  $a$ , which then decay to pairs of muons and tau leptons was completed. Expected upper 95% confidence level limits are set to about  $10^{-4}$  after addition of all final decay modes. These results are independent of separate 2HDM+S models and is considered a generic search that applies to multiple MSSM scenarios along with any BSM physics within the search window. It has been an honor of a lifetime to work alongside CMS, Purdue University, and Princeton Univsersity to deliever this analysis and years of service work!

## Appendix A

# Data and Simulation Samples

### A.1 Data and Simulation Used for Analysis

The full Run II dataset was used corresponding to  $137\text{fb}^{-1}$ .

Table A.1: List of data sets included in the analysis for the 2016 data taking period.

Data set
/SingleMuon/Run2016B_ver2-Nano250ct2019_ver2-v1/NANOAOD
/SingleMuon/Run2016B_ver1-Nano250ct2019_ver1-v1/NANOAOD
/SingleMuon/Run2016G-Nano250ct2019-v1/NANOAOD
/SingleMuon/Run2016F-Nano250ct2019-v1/NANOAOD
/SingleMuon/Run2016E-Nano250ct2019-v1/NANOAOD
/SingleMuon/Run2016D-Nano250ct2019-v1/NANOAOD
/SingleMuon/Run2016C-Nano250ct2019-v1/NANOAOD
/SingleMuon/Run2016H-Nano250ct2019-v1/NANOAOD
/DoubleMuon/Run2016H-Nano250ct2019-v1/NANOAOD
/DoubleMuon/Run2016G-Nano250ct2019-v1/NANOAOD
/DoubleMuon/Run2016F-Nano250ct2019-v1/NANOAOD
/DoubleMuon/Run2016B_ver2-Nano250ct2019_ver2-v1/NANOAOD
/DoubleMuon/Run2016B_ver1-Nano250ct2019_ver1-v1/NANOAOD
/DoubleMuon/Run2016E-Nano250ct2019-v1/NANOAOD
/DoubleMuon/Run2016D-Nano250ct2019-v1/NANOAOD
/DoubleMuon/Run2016C-Nano250ct2019-v1/NANOAOD

Table A.2: List of data sets included in the analysis for the 2017 data taking period.

Data set
/DoubleMuon/Run2017B-02Apr2020-v1/NANO AOD
/DoubleMuon/Run2017C-02Apr2020-v1/NANO AOD
/DoubleMuon/Run2017D-02Apr2020-v1/NANO AOD
/DoubleMuon/Run2017E-02Apr2020-v1/NANO AOD
/DoubleMuon/Run2017F-02Apr2020-v1/NANO AOD
/MuonEG/Run2017B-02Apr2020-v1/NANO AOD
/MuonEG/Run2017C-02Apr2020-v1/NANO AOD
/MuonEG/Run2017D-02Apr2020-v1/NANO AOD
/MuonEG/Run2017E-02Apr2020-v1/NANO AOD
/MuonEG/Run2017F-02Apr2020-v1/NANO AOD
/SingleMuon/Run2017B-02Apr2020-v1/NANO AOD
/SingleMuon/Run2017C-02Apr2020-v1/NANO AOD
/SingleMuon/Run2017D-02Apr2020-v1/NANO AOD
/SingleMuon/Run2017E-02Apr2020-v1/NANO AOD
/SingleMuon/Run2017F-02Apr2020-v1/NANO AOD
/DoubleEG/Run2017B-02Apr2020-v1/NANO AOD
/DoubleEG/Run2017C-02Apr2020-v1/NANO AOD
/DoubleEG/Run2017D-02Apr2020-v1/NANO AOD
/DoubleEG/Run2017E-02Apr2020-v1/NANO AOD
/DoubleEG/Run2017F-02Apr2020-v1/NANO AOD
/SingleElectron/Run2017B-02Apr2020-v1/NANO AOD
/SingleElectron/Run2017C-02Apr2020-v1/NANO AOD
/SingleElectron/Run2017D-02Apr2020-v1/NANO AOD
/SingleElectron/Run2017E-02Apr2020-v1/NANO AOD
/SingleElectron/Run2017F-02Apr2020-v1/NANO AOD

Table A.3: List of data sets included in the analysis for the 2018 data taking period.

Data set
/SingleMuon/Run2018A-02Apr2020-v1/NANO AOD
/SingleMuon/Run2018B-02Apr2020-v1/NANO AOD
/SingleMuon/Run2018C-02Apr2020-v1/NANO AOD
/SingleMuon/Run2018D-02Apr2020-v1/NANO AOD
/DoubleMuon/Run2018A-02Apr2020-v1/NANO AOD
/DoubleMuon/Run2018B-02Apr2020-v1/NANO AOD
/DoubleMuon/Run2018C-02Apr2020-v1/NANO AOD
/DoubleMuon/Run2018D-02Apr2020-v1/NANO AOD
/DoubleMuonLowMass/Run2018A-02Apr2020-v1/NANO AOD
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/DoubleMuonLowMass/Run2018C-02Apr2020-v1/NANO AOD
/DoubleMuonLowMass/Run2018D-02Apr2020-v1/NANO AOD
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/EGamma/Run2018B-02Apr2020-v1/NANO AOD
/EGamma/Run2018C-02Apr2020-v1/NANO AOD
/EGamma/Run2018D-02Apr2020-v1/NANO AOD

Table A.4: List of data sets included in the analysis for the 2016 data taking period.

Table A.5: List of data sets included in the analysis for the 2017 data taking period.

Table A.6: List of data sets included in the analysis for the 2018 data taking period.

Monte Carlo Datasets for 2018
/DY1JetsToLL_M-50_TuneCP5_13TeV-madgraphMLM-pythia8/RunIIAutumn18NanoAODv7-Nano02Apr2020_102X_upgrade2018_realistic_v21-v1/NANOAODSIM
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## Appendix B

# Fake Rate Measurements

These figures show the rest of the datadriven background estimation on the rate at which jets fake tau leptons in QCD, ttbar, and W+jet regions. The y-axis can be interpreted as the percent fake rate.

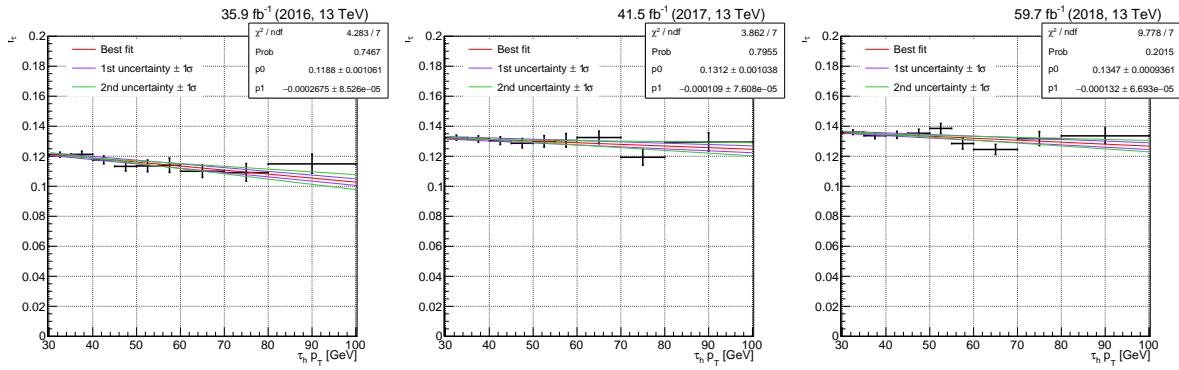


Figure B.1: Fake factors determined in the W+jets determination region with 0 jet in the  $e\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

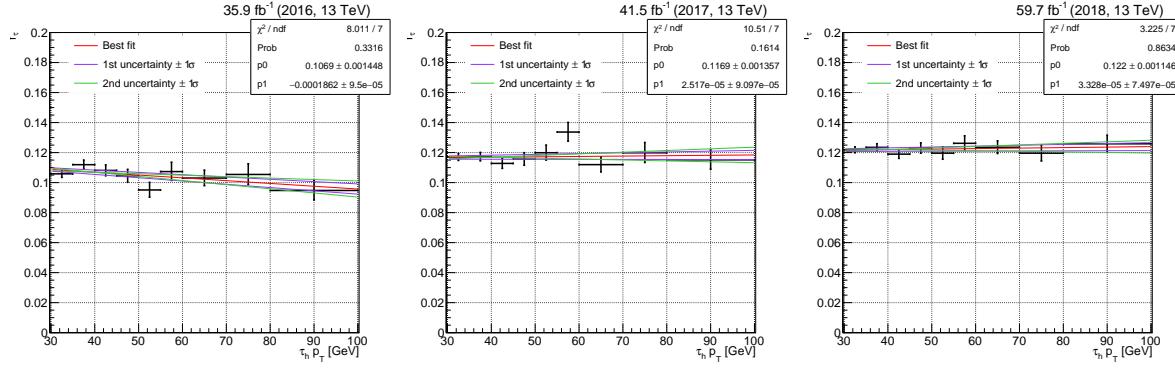


Figure B.2: Fake factors determined in the W+jets determination region with one jet in the  $e\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

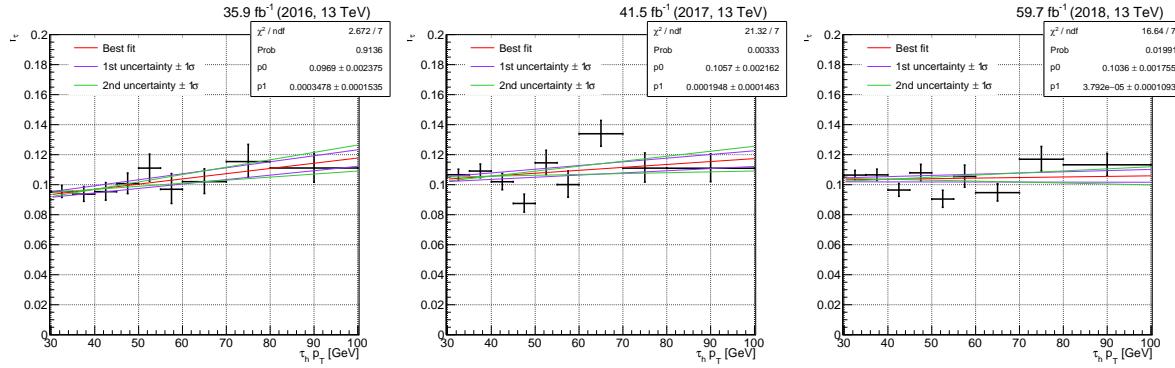


Figure B.3: Fake factors determined in the W+jets determination region with at least two jets in the  $e\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

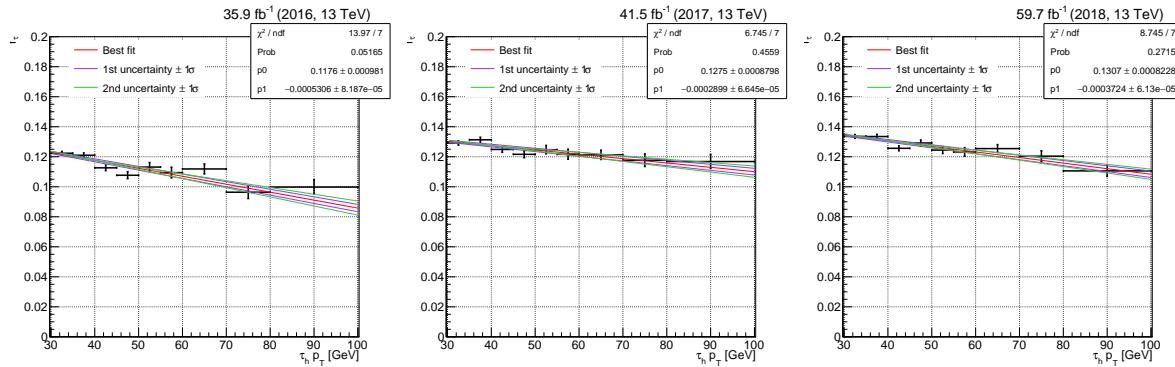


Figure B.4: Fake factors determined in the W+jets determination region with 0 jet in the  $\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

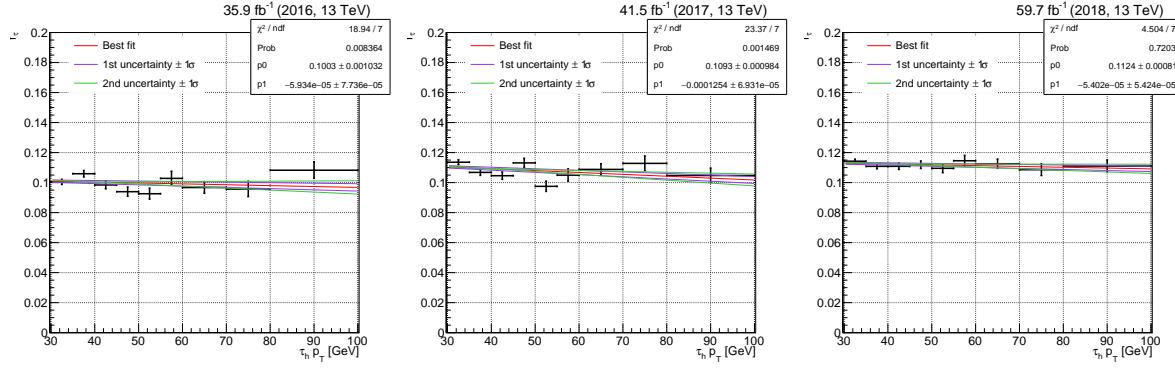


Figure B.5: Fake factors determined in the W+jets determination region with one jet in the  $\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

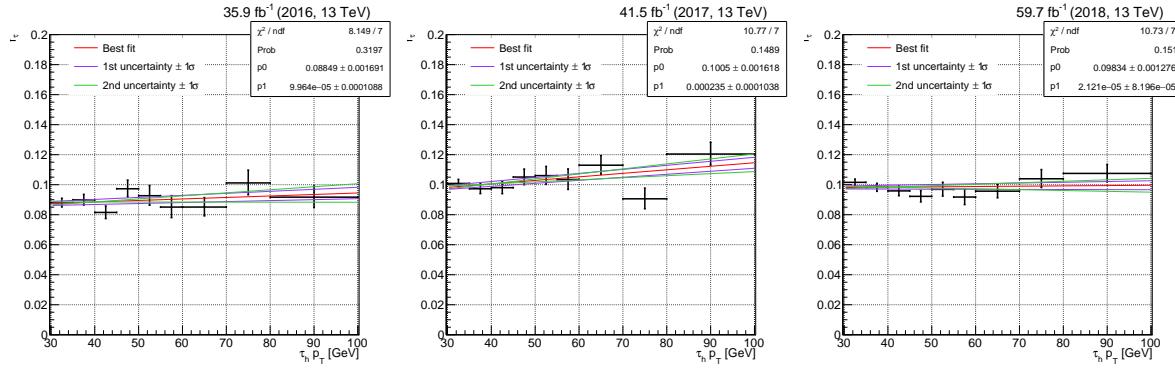


Figure B.6: Fake factors determined in the W+jets determination region with at least two jets in the  $\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

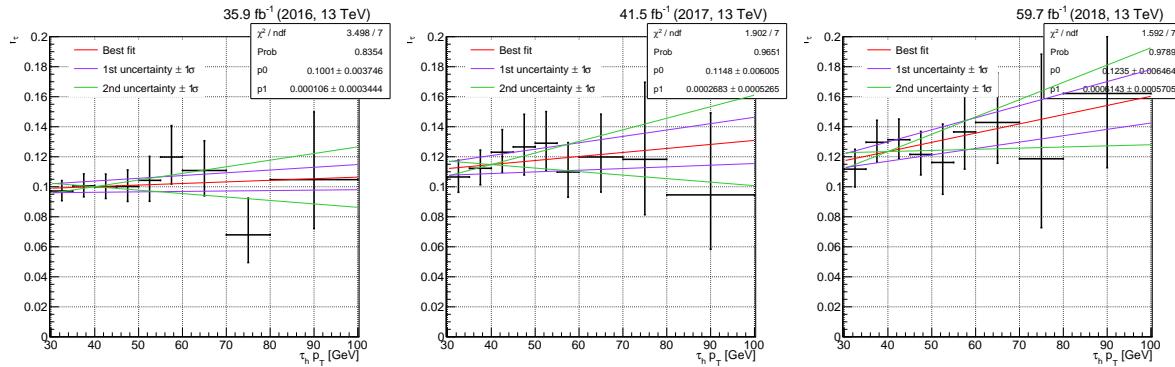


Figure B.7: Fake factors determined in the QCD multijet determination region with 0 jet in the  $e\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

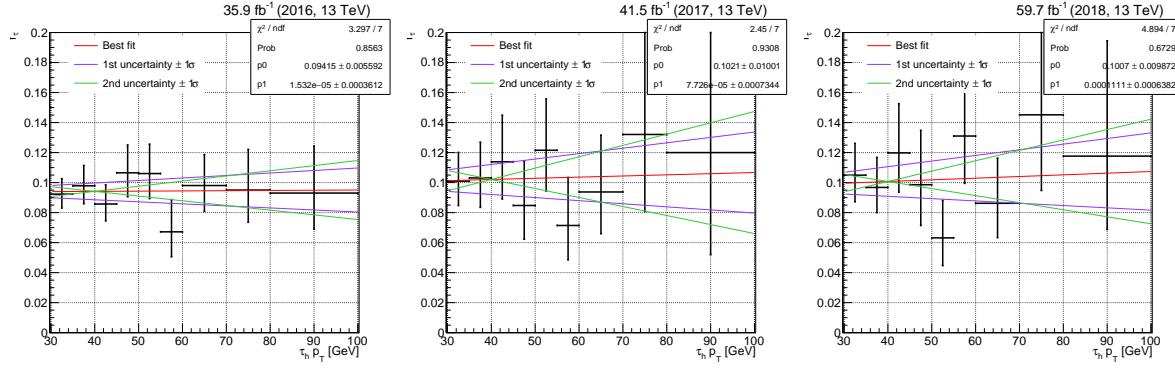


Figure B.8: Fake factors determined in the QCD multijet determination region with one jet in the  $e\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

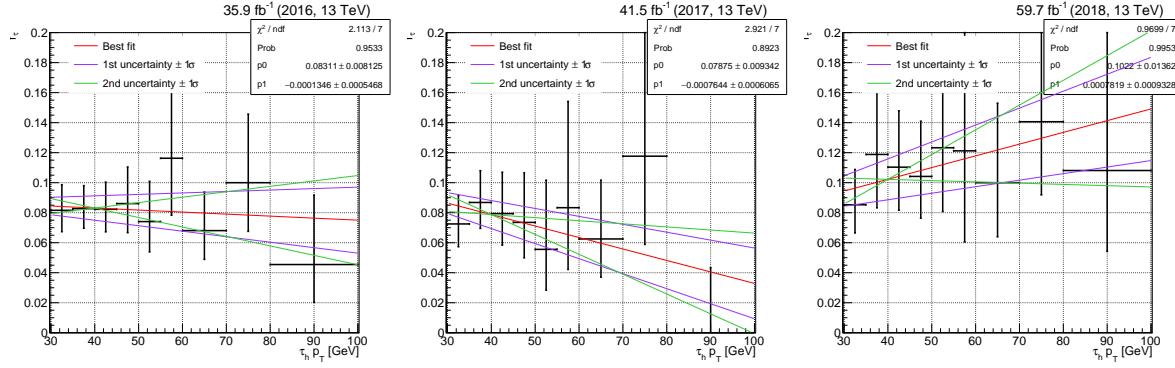


Figure B.9: Fake factors determined in the QCD multijet determination region with at least two jets in the  $e\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

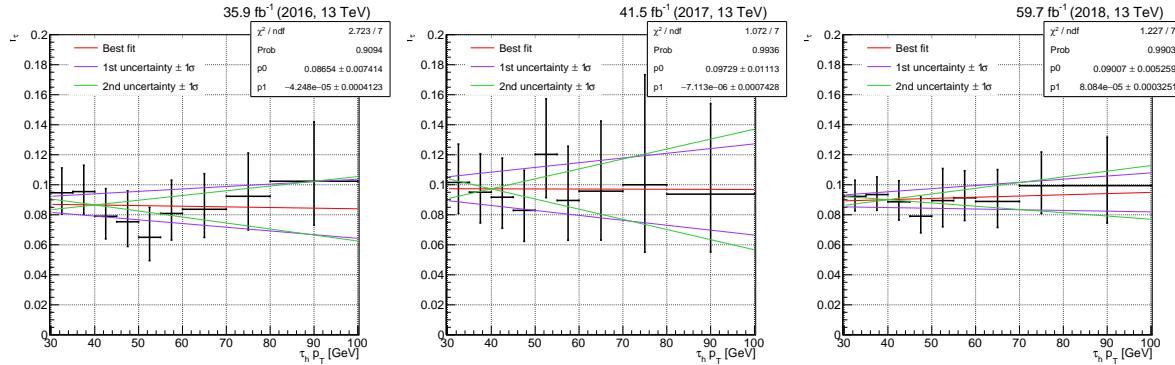


Figure B.10: Fake factors determined in the QCD multijet determination region with one jet in the  $\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

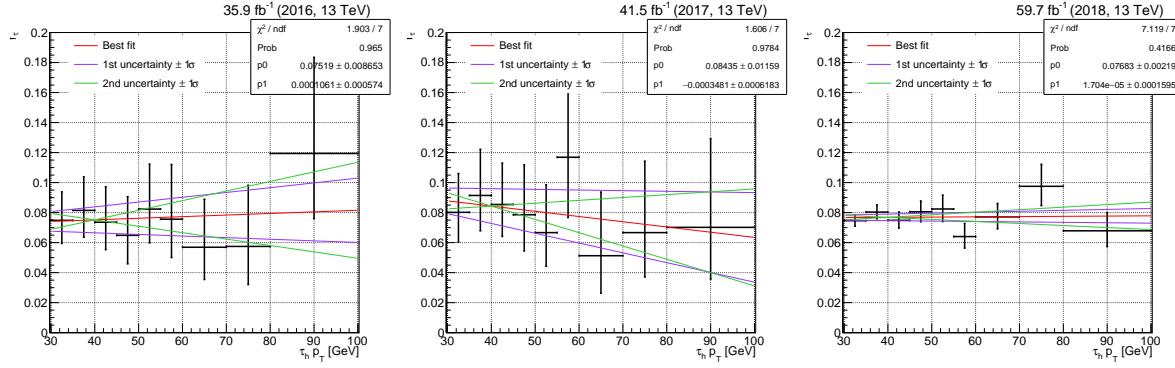


Figure B.11: Fake factors determined in the QCD multijet determination region with at least two jets in the  $\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h$   $p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

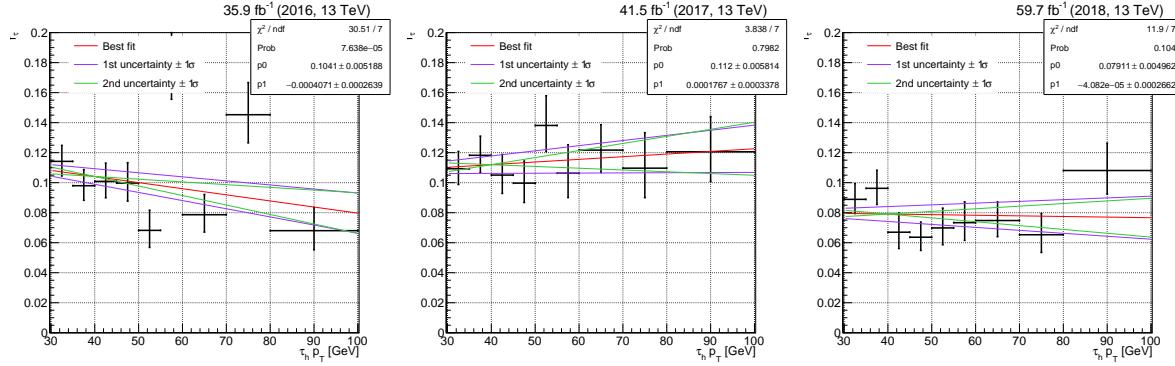


Figure B.12: Fake factors determined in the  $t\bar{t}$  determination region in data in the  $e\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h$   $p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

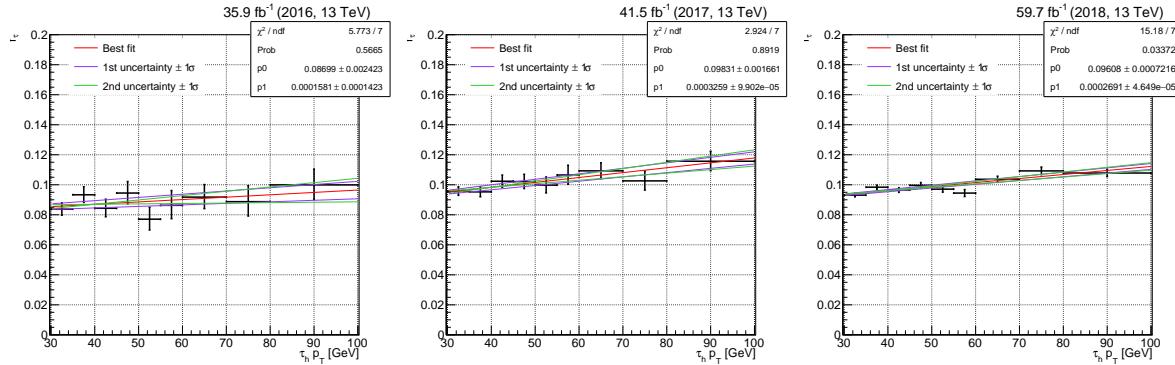


Figure B.13: Fake factors determined in the  $t\bar{t}$  simulation in the  $e\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h$   $p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

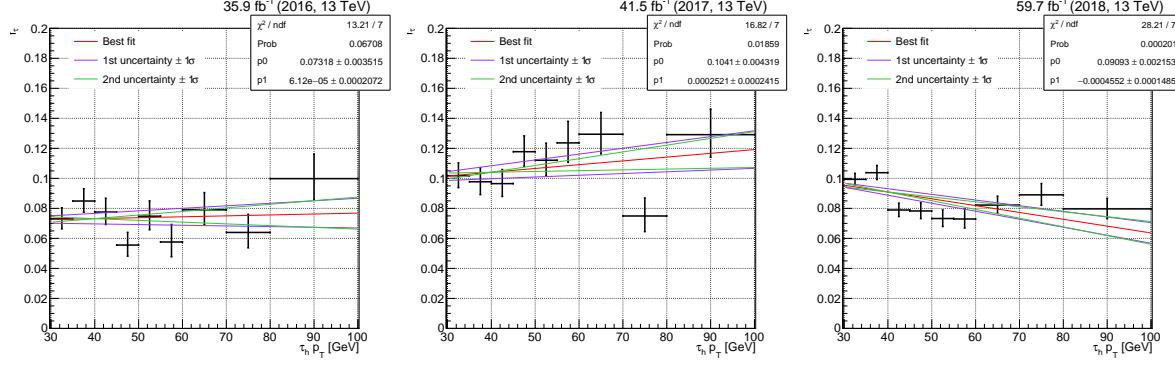


Figure B.14: Fake factors determined in the  $t\bar{t}$  determination region in data in the  $\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

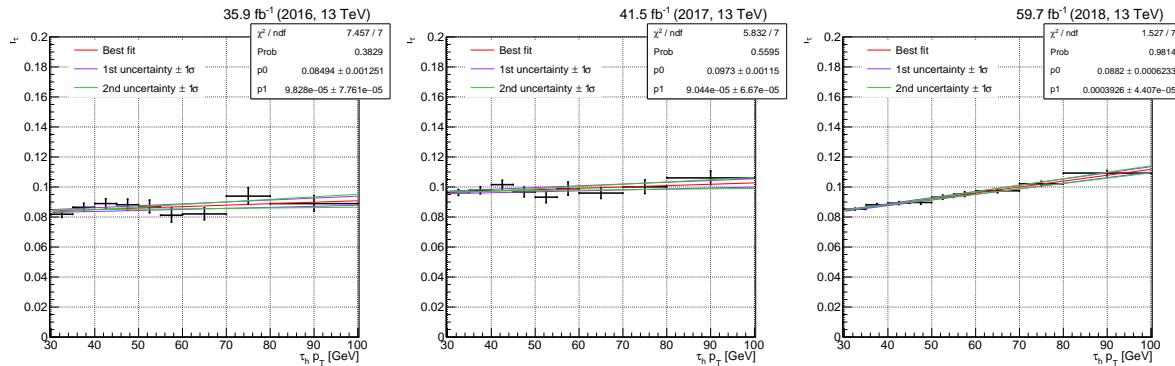


Figure B.15: Fake factors determined in the  $t\bar{t}$  simulation in the  $\tau_h$  final state in 2016 (left), 2017 (center), and 2018 (right). They are fitted with linear functions as a function of the  $\tau_h p_T$ . The green and purple lines indicate the shape systematics obtained by uncorrelating the uncertainties in the two fit parameters returned by the fit.

## Appendix C

# Systematic Uncertainties

Below are the rest of the channels and years from the systematic uncertainty discussion similar to mmmmt 2017 result shown in the main part of the paper 7.9.

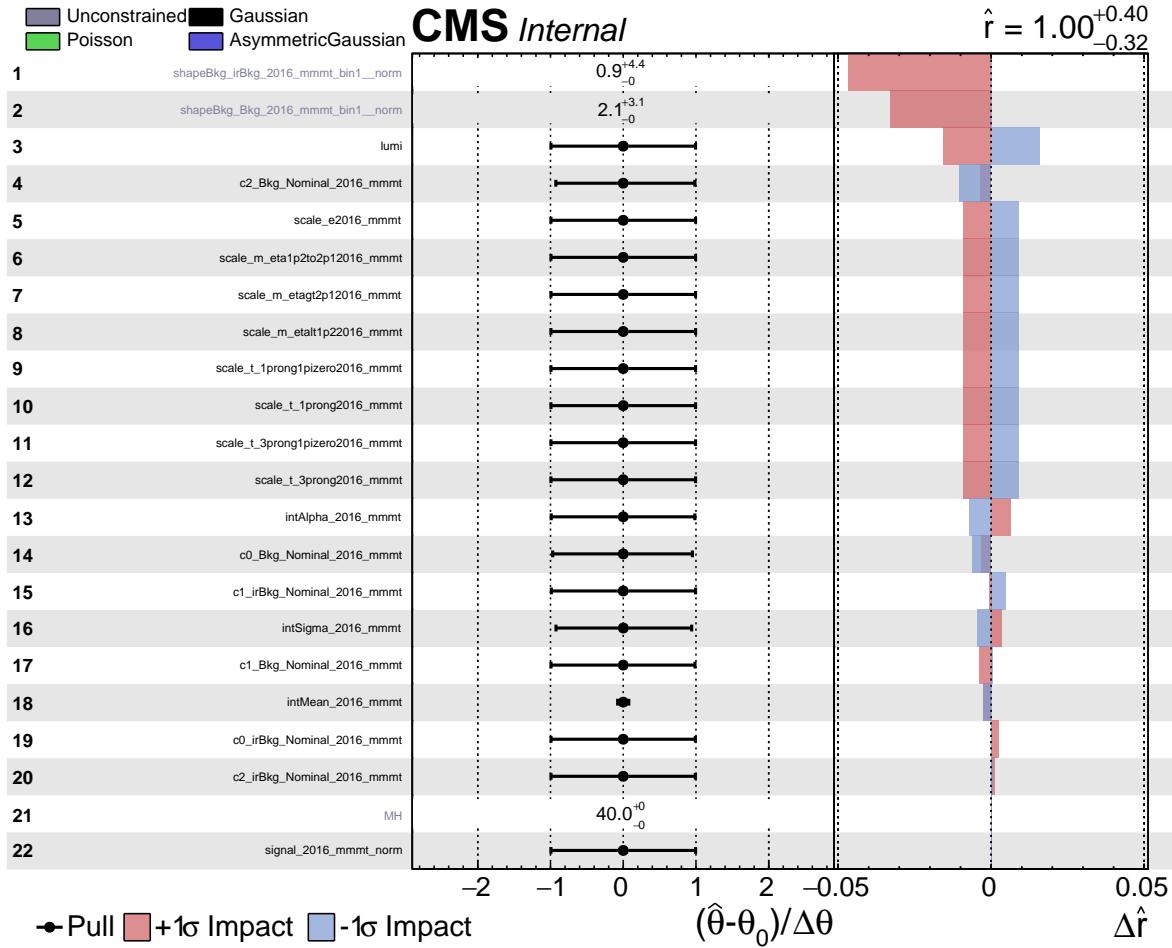
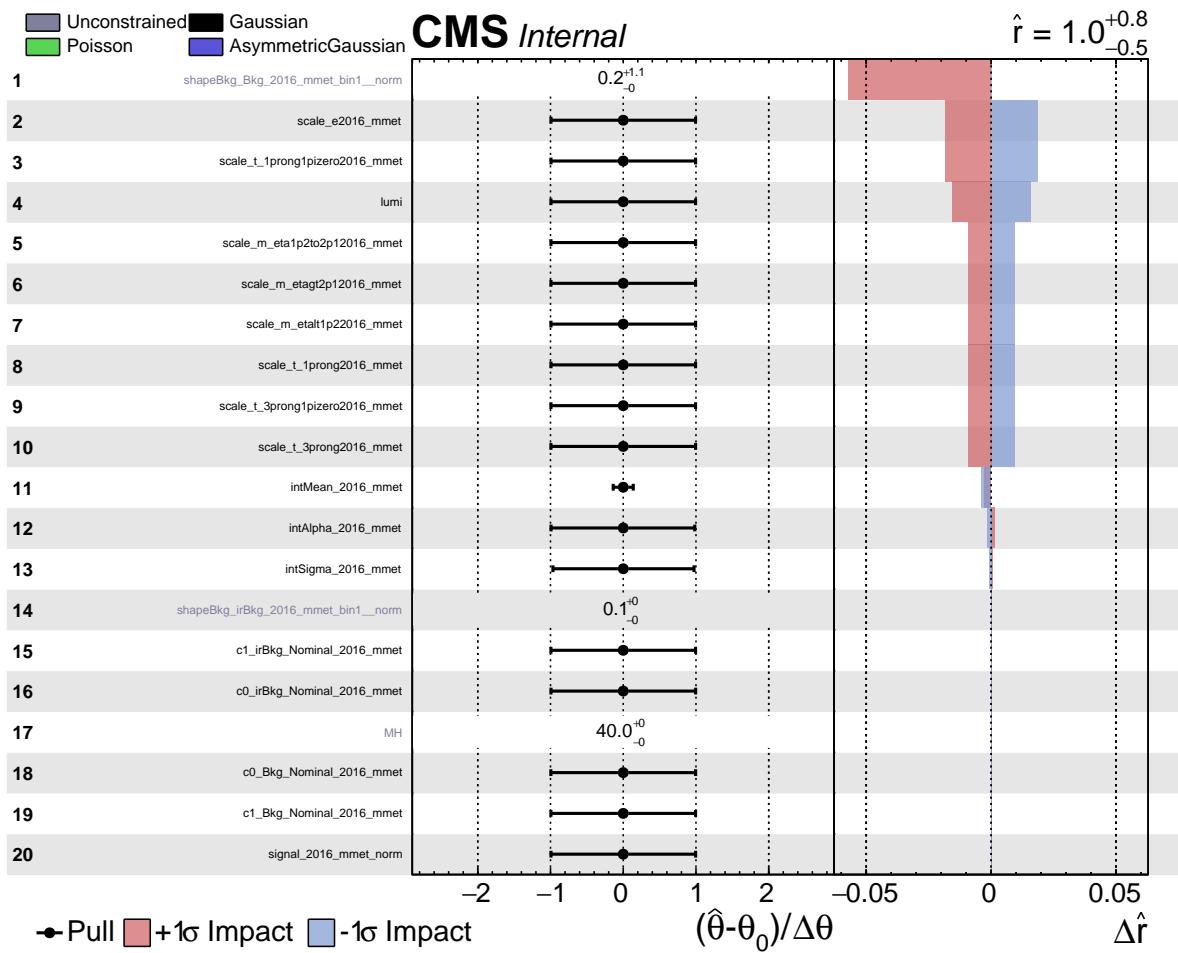


Figure C.1: Expected systematic impacts for the fit model  $\mu\mu\mu\tau$

Figure C.2: Expected systematic impacts for the fit model  $\mu\mu e\tau$

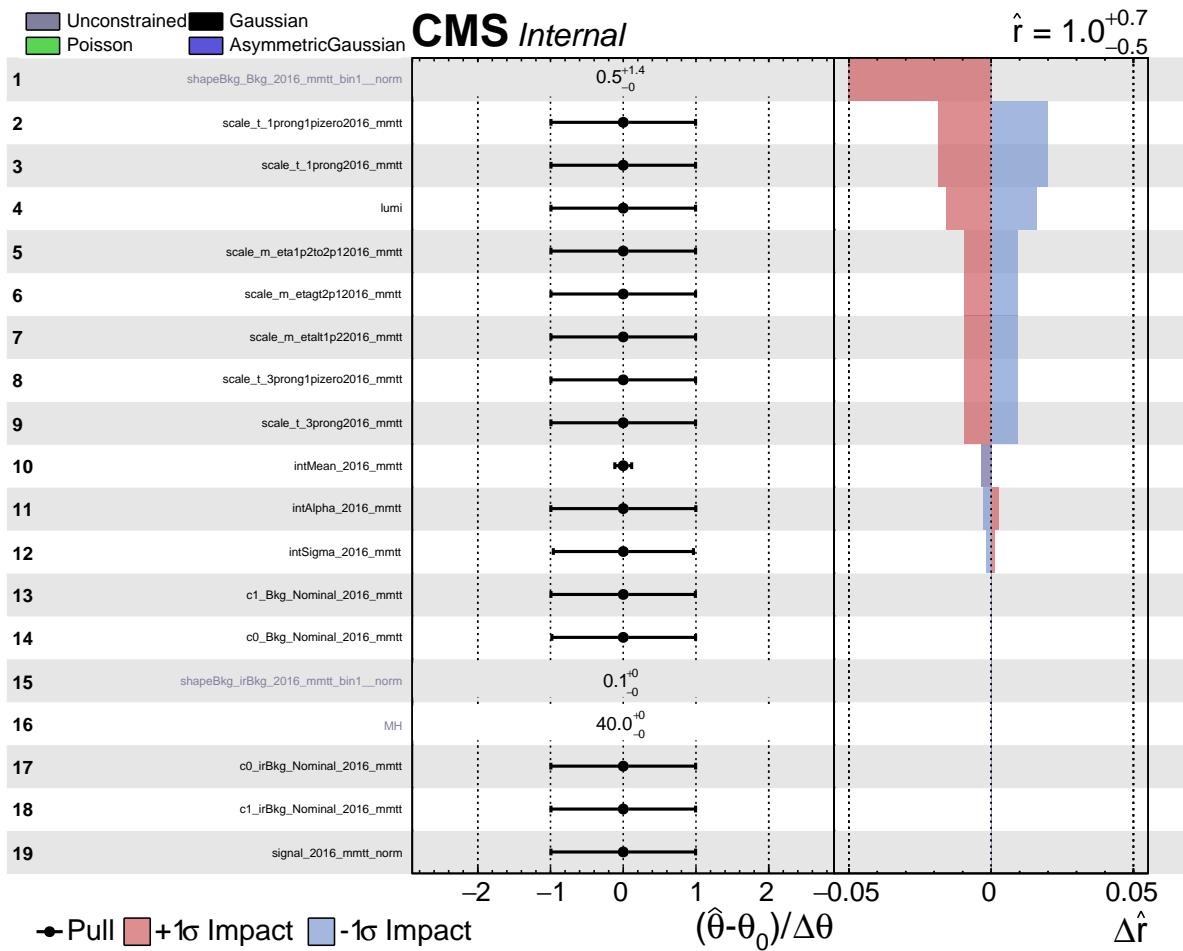


Figure C.3: Expected systematic impacts for the fit model for 2016  $\mu\mu\tau\tau$

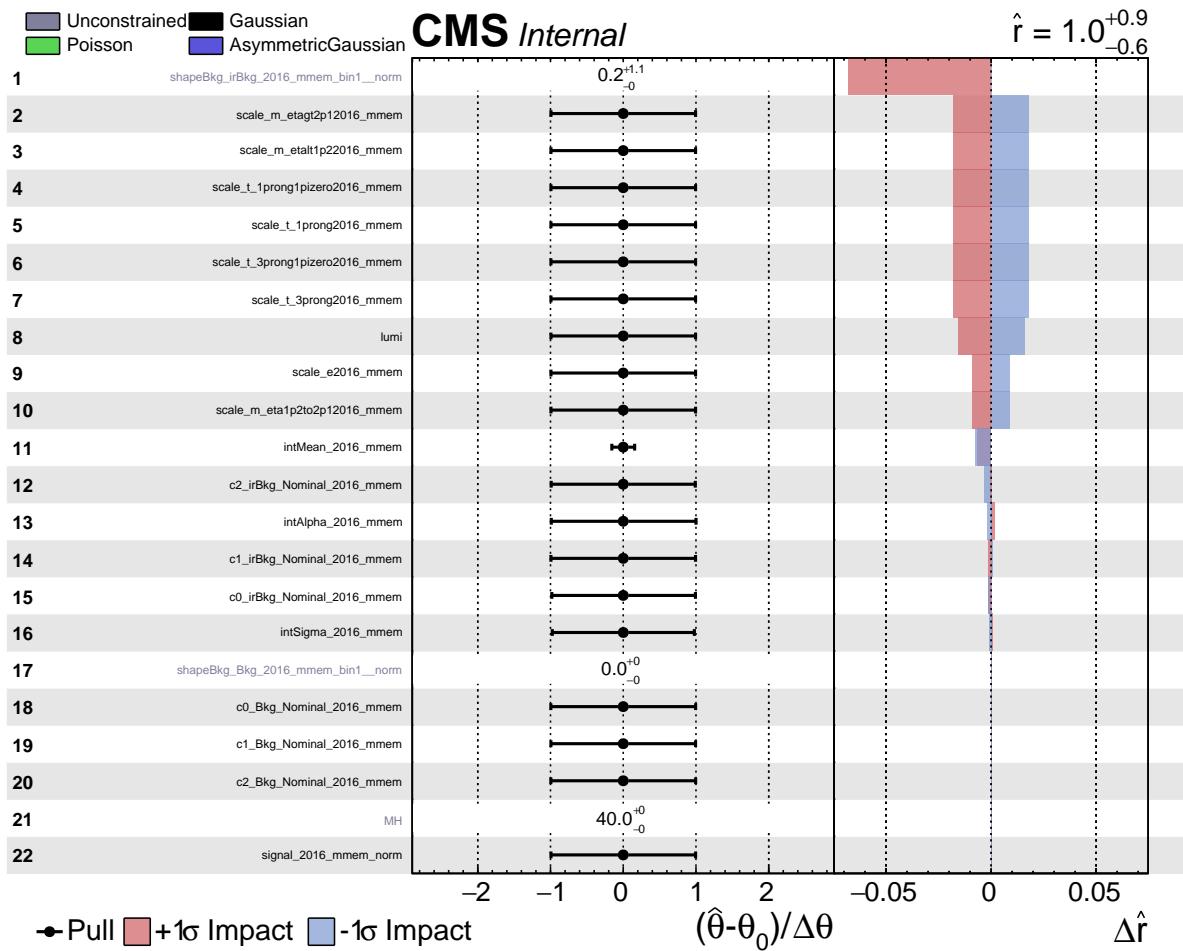


Figure C.4: Expected systematic impacts for the fit model for 2016  $\mu\mu e\mu$

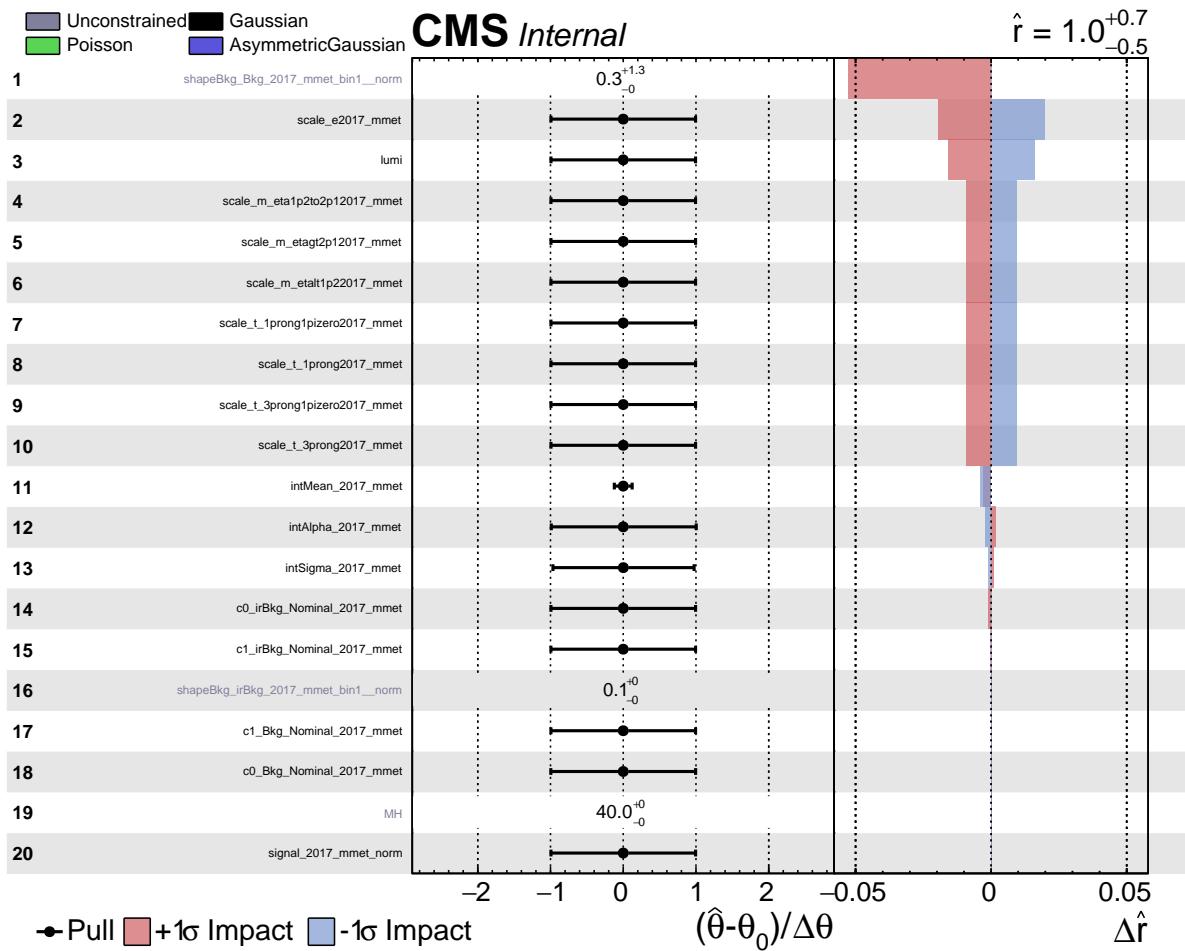


Figure C.5: Expected systematic impacts for the fit model  $\mu\mu e\tau$

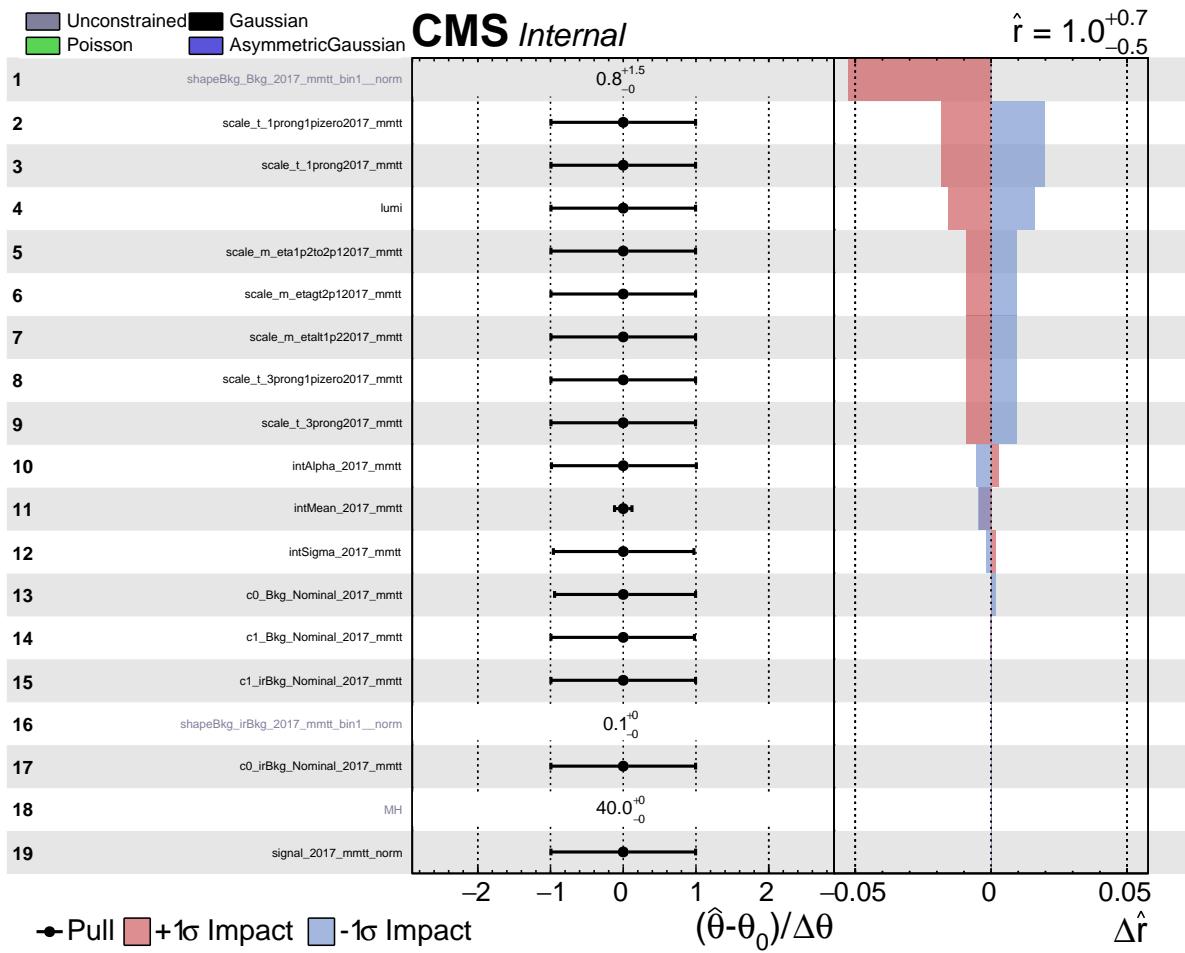


Figure C.6: Expected systematic impacts for the fit model for 2017  $\mu\mu\tau\tau$

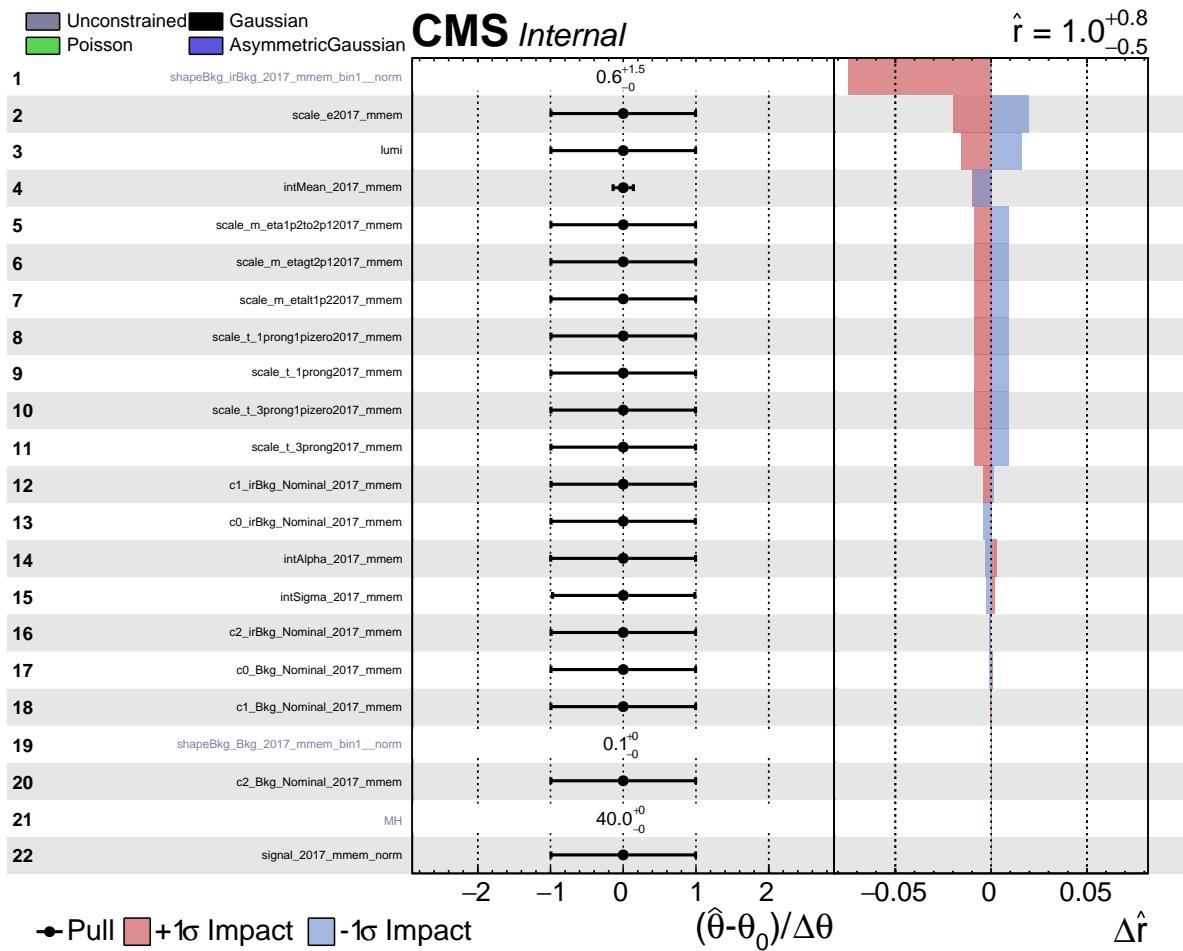


Figure C.7: Expected systematic impacts for the fit model for 2017  $\mu\mu e\mu$

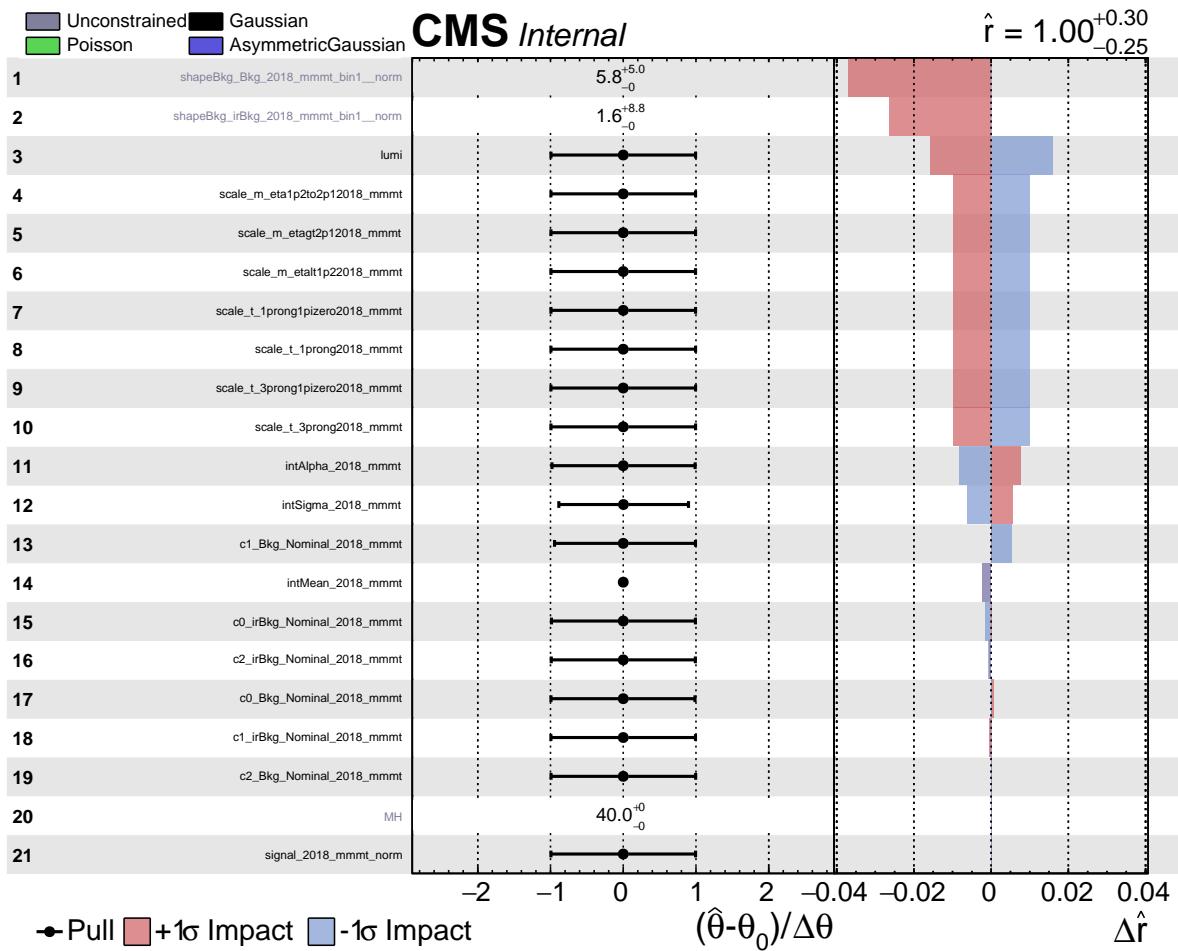


Figure C.8: Expected systematic impacts for the fit model  $\mu\mu\mu\tau$

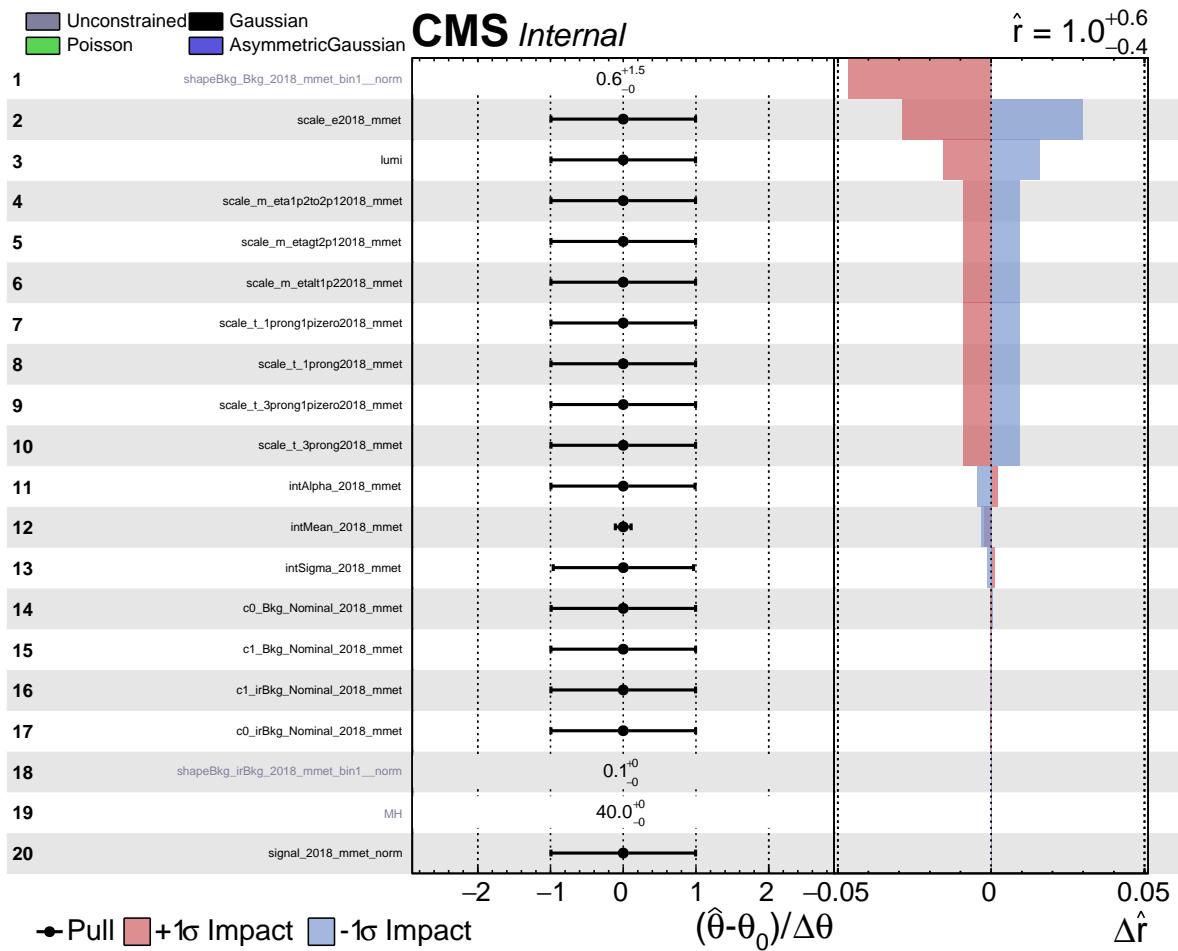


Figure C.9: Expected systematic impacts for the fit model  $\mu\mu e\tau$

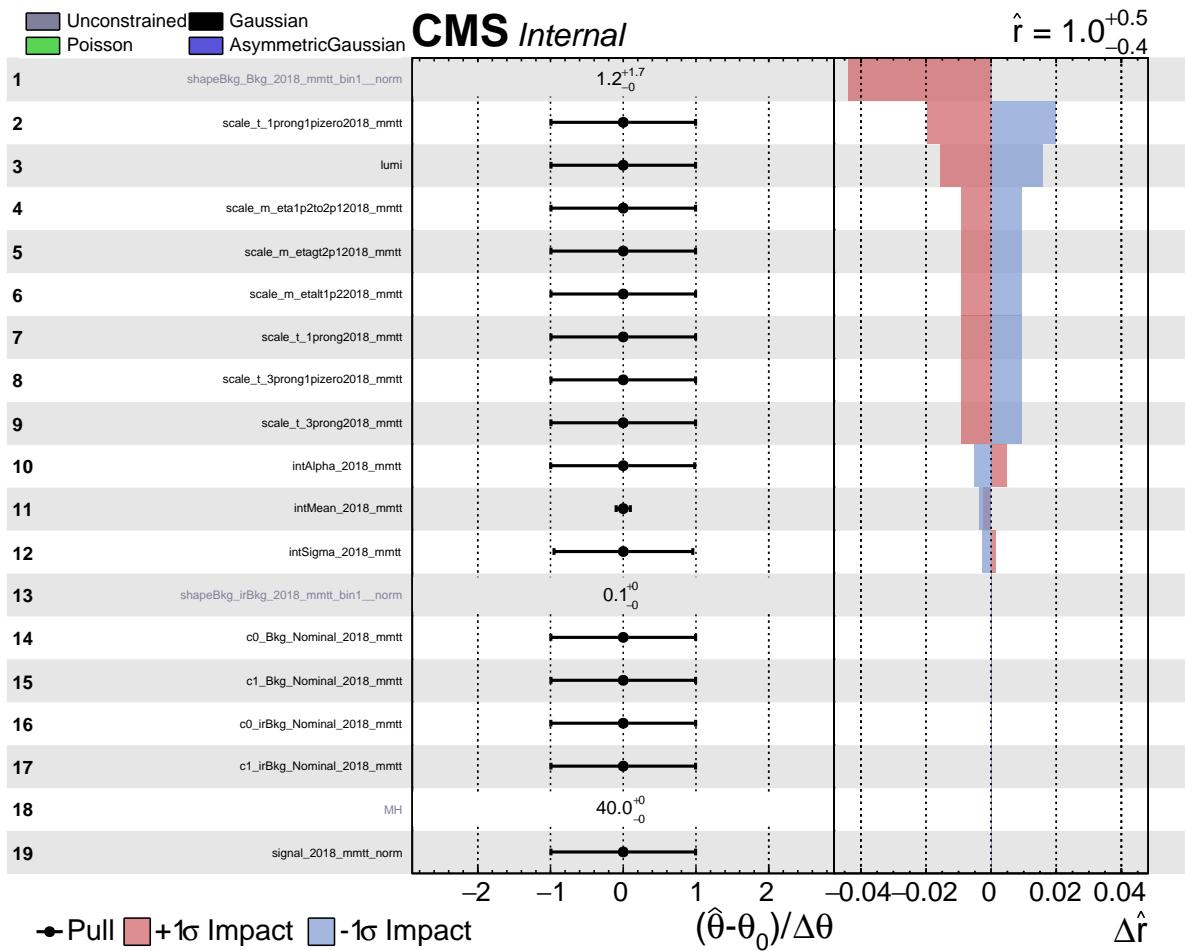


Figure C.10: Expected systematic impacts for the fit model for 2018  $\mu\mu\tau\tau$

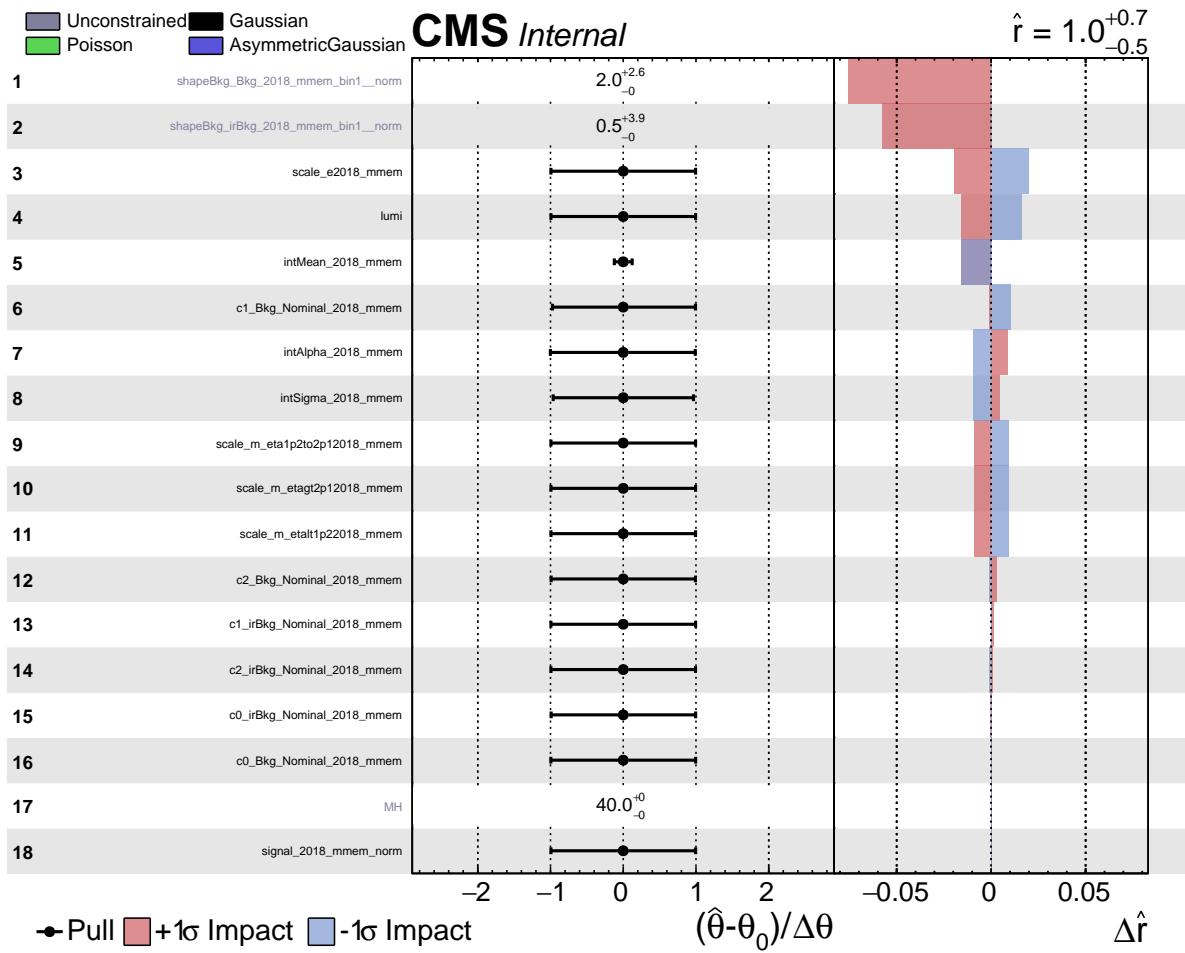


Figure C.11: Expected systematic impacts for the fit model for 2018  $\mu\mu e\mu$

## **Appendix D**

## **Fit Models**

This section contains the remaining parametric fit models for the rest of the years 2017, 2018 and the channels referenced originally in chapter 7.

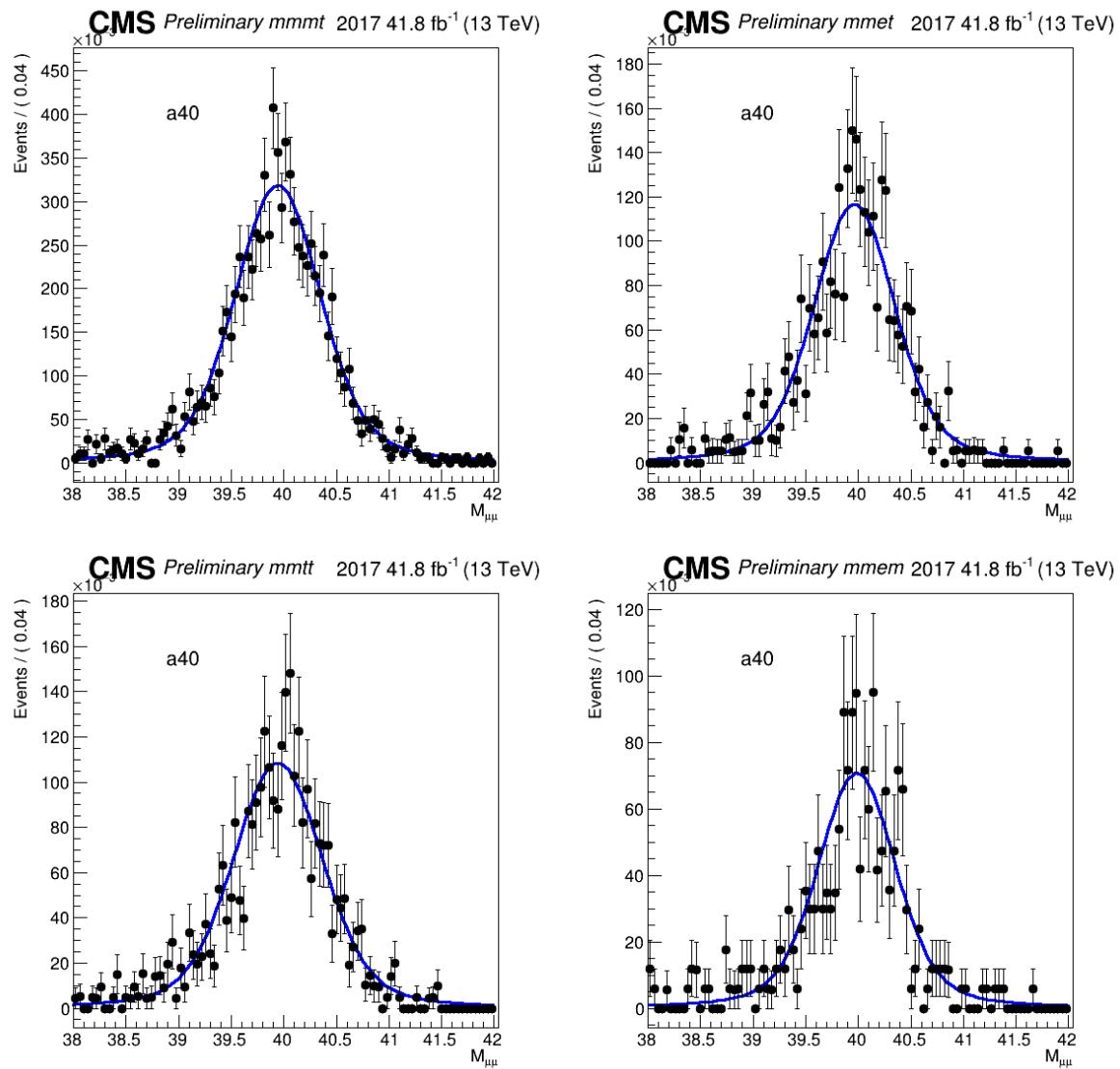


Figure D.1: 2017 Signal fit using a Voigtian function

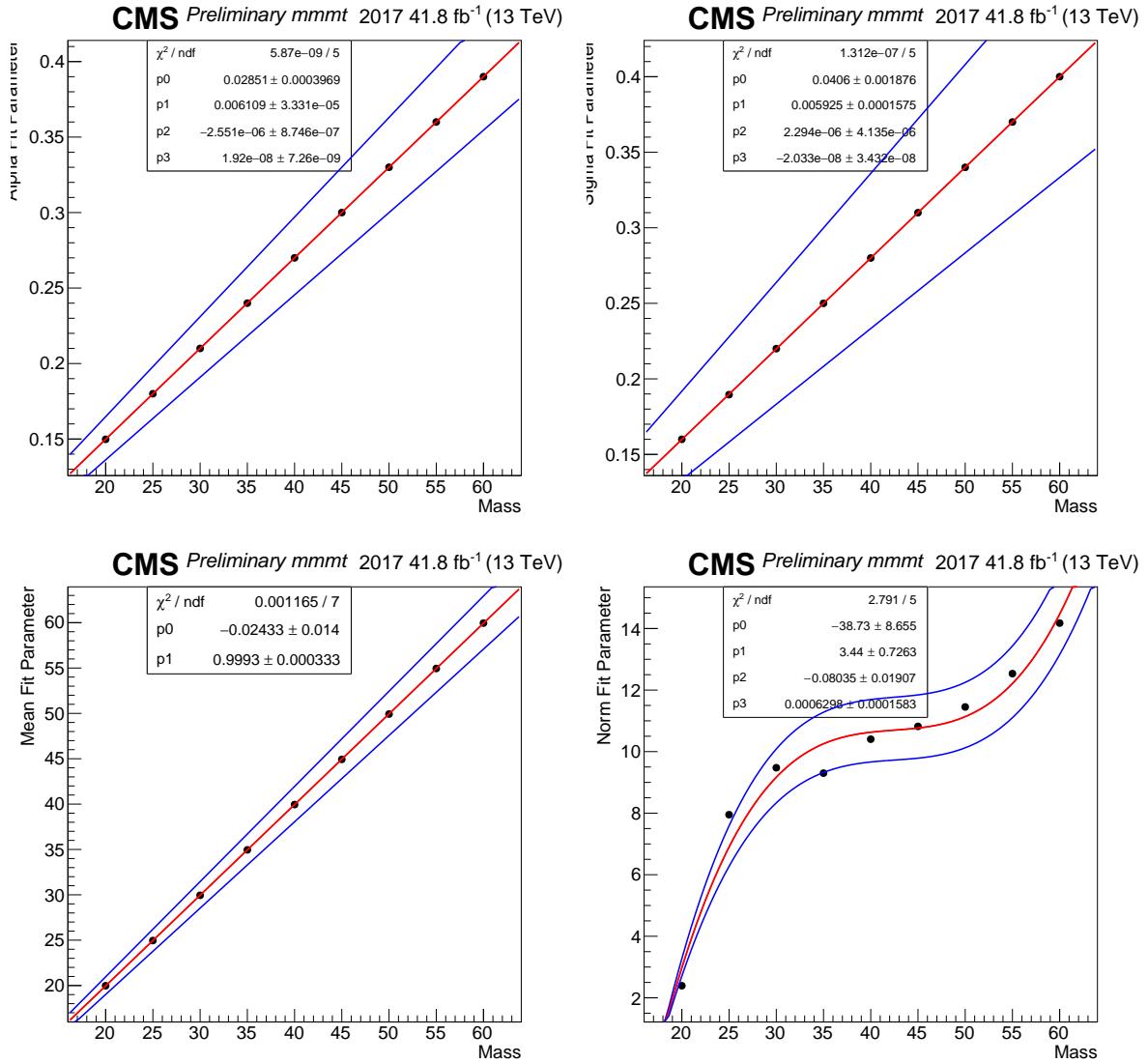


Figure D.2: Spline functions for 2017 mmmt a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

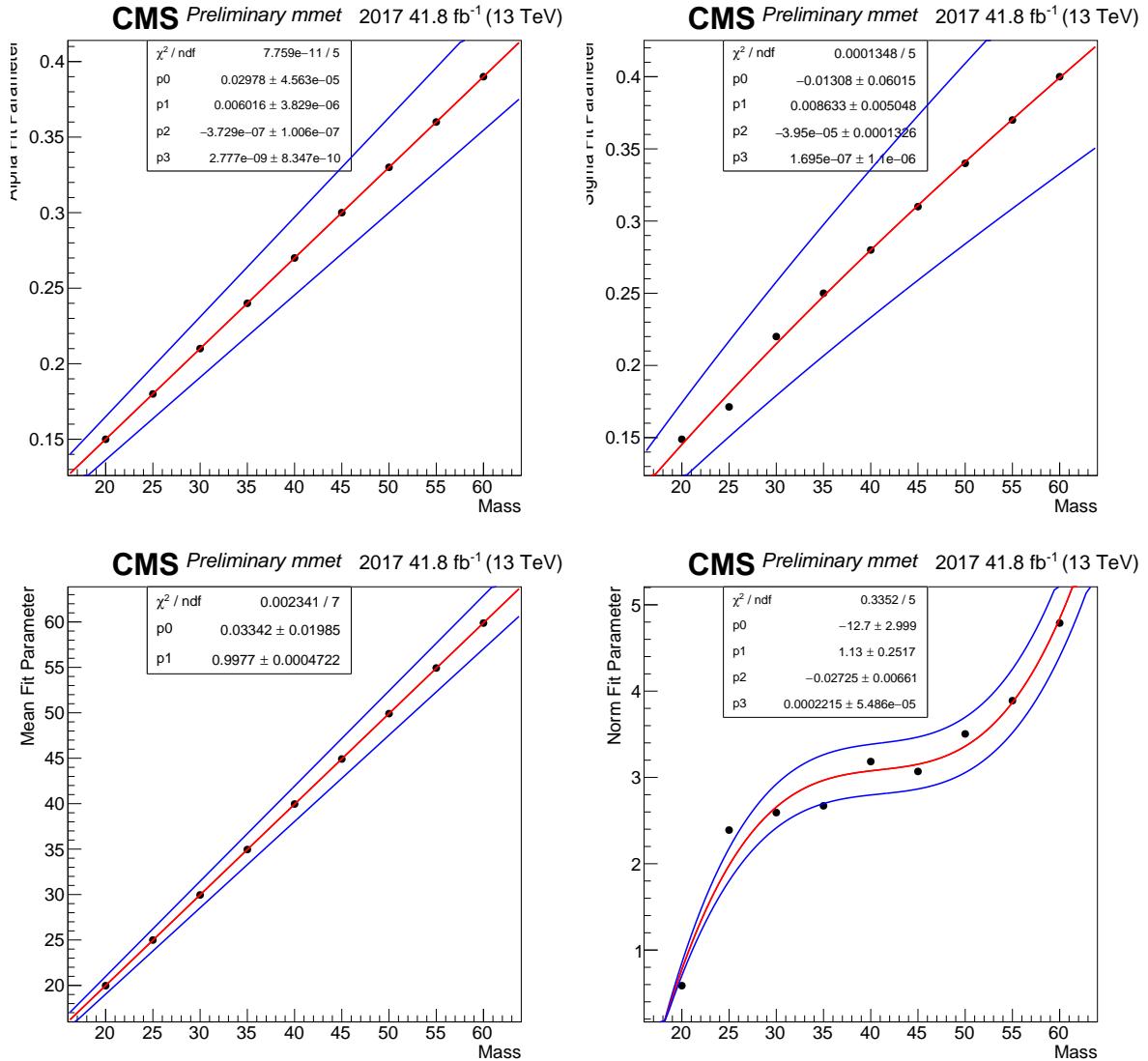


Figure D.3: Spline functions for 2017 mmet a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

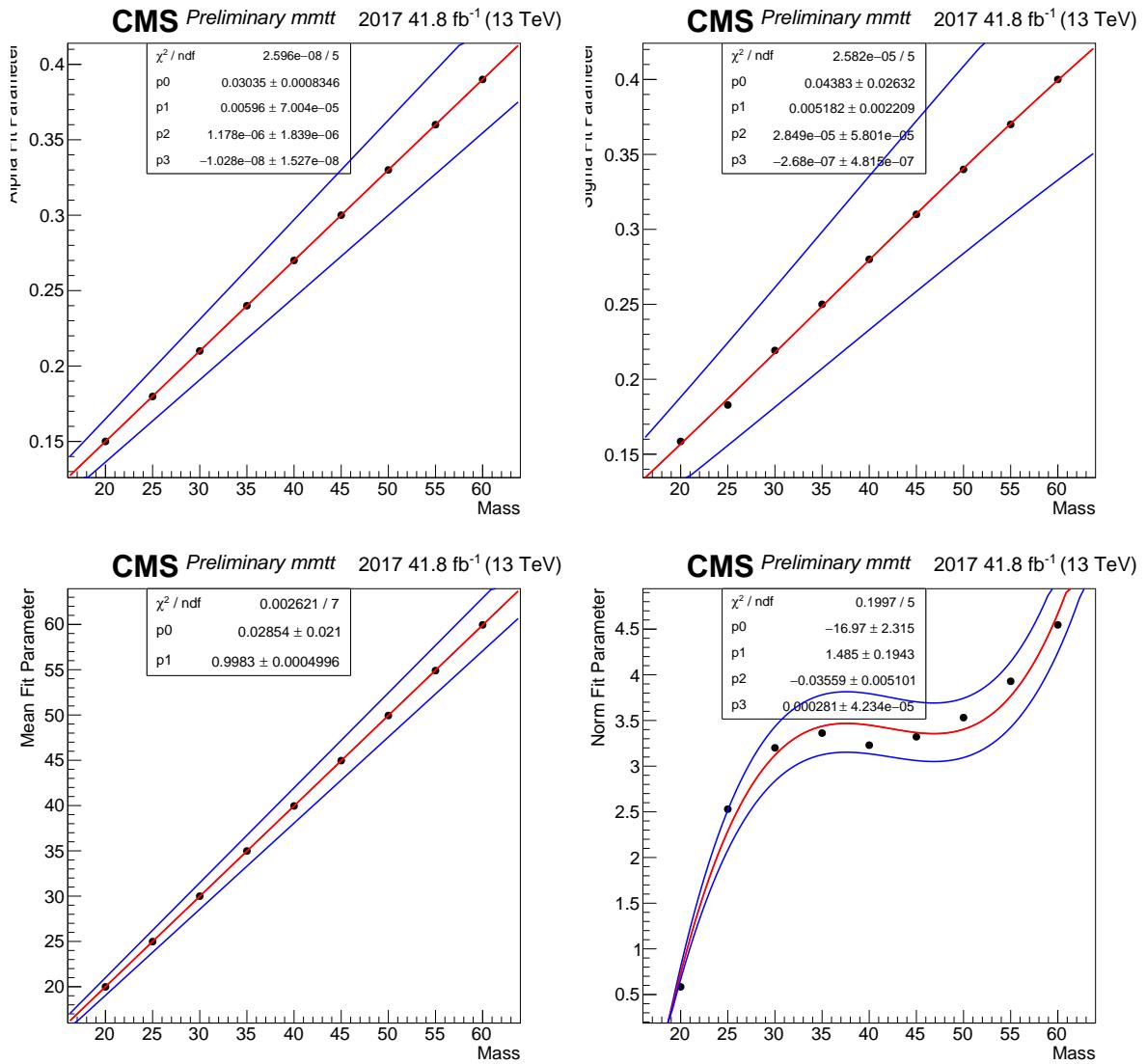


Figure D.4: Spline functions for 2017 mm tt a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

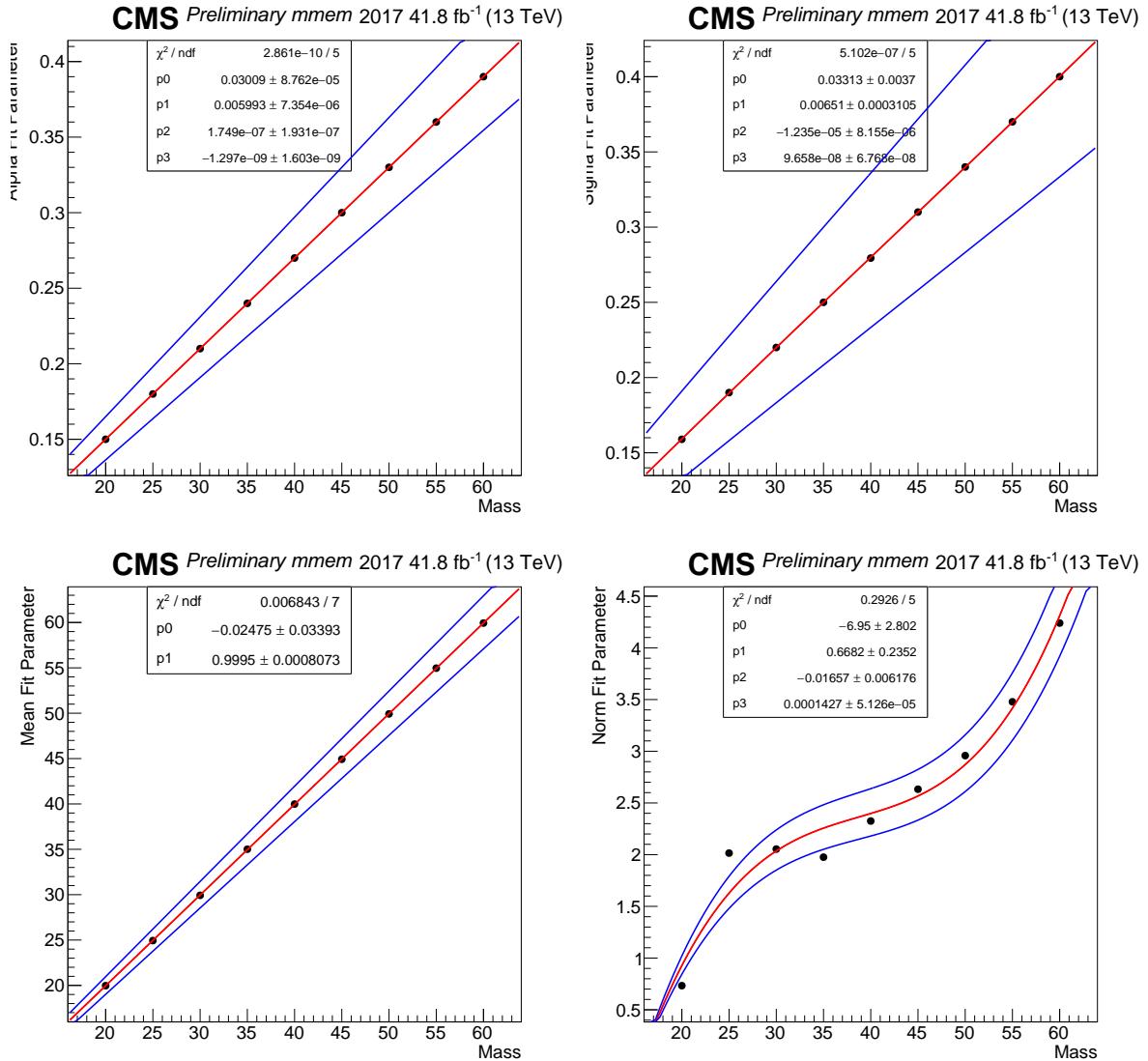


Figure D.5: Spline functions for 2017 mmem a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

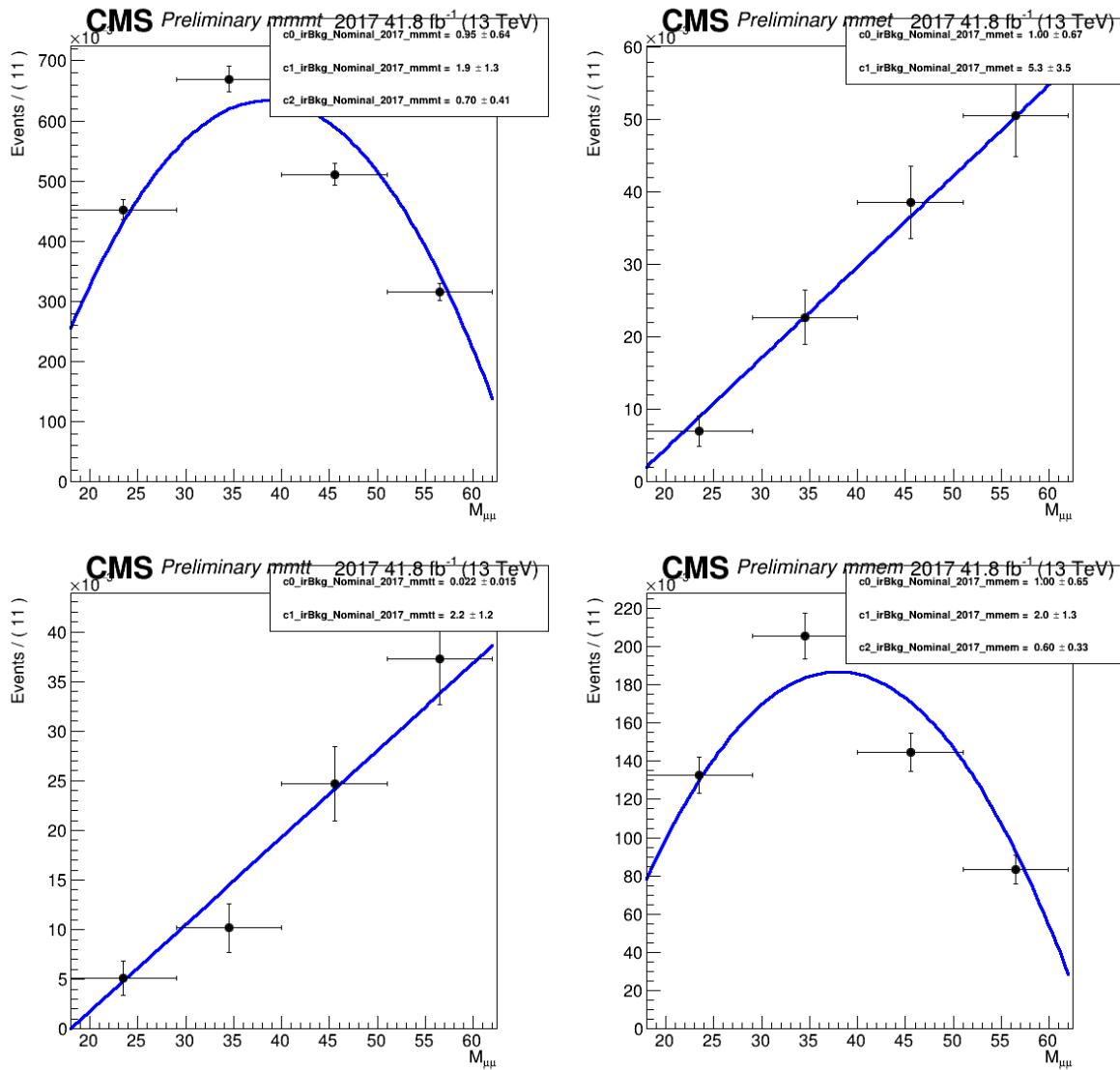


Figure D.6: 2017 irreducible background fit using Bernstein polynomials

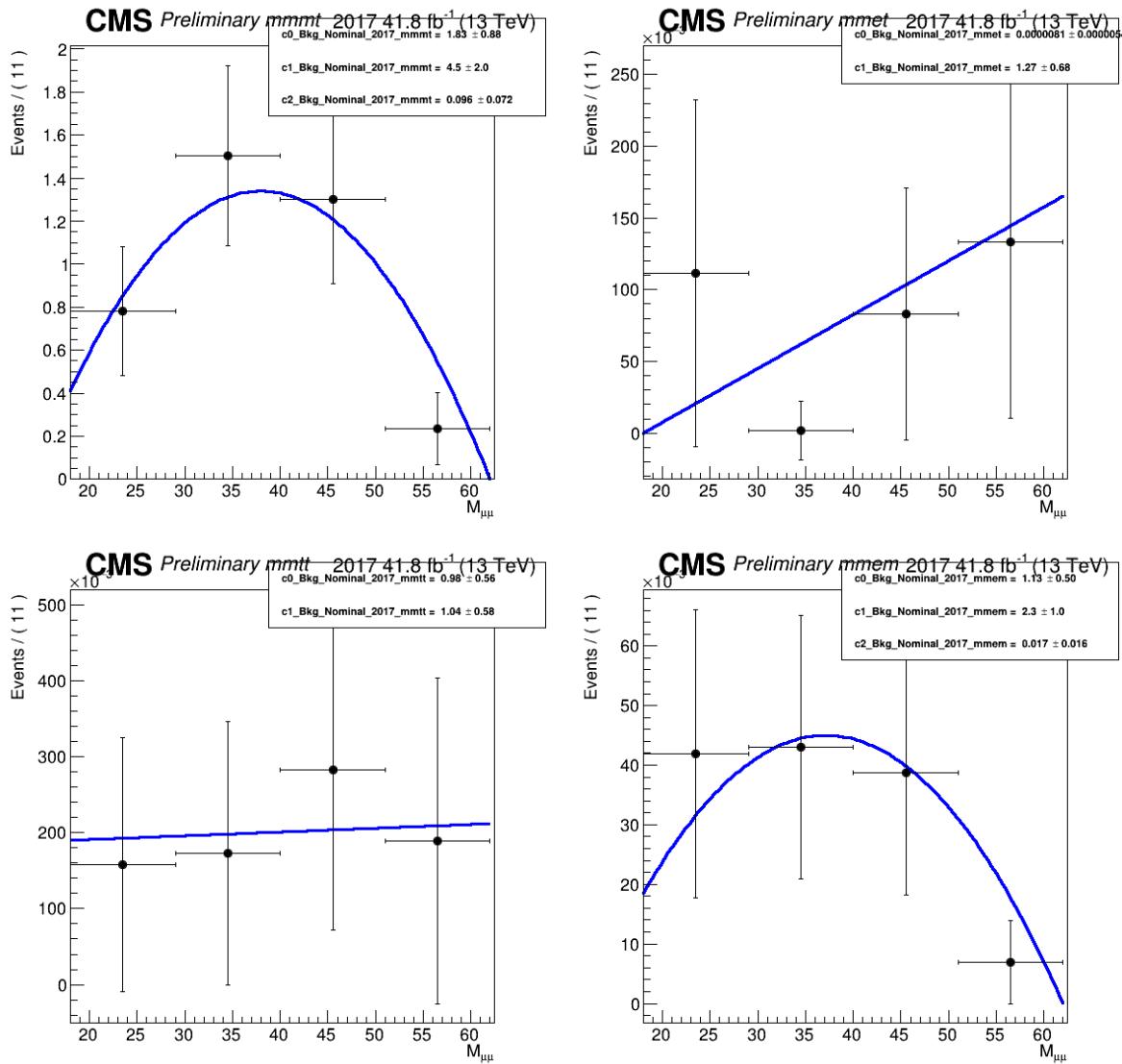


Figure D.7: 2017 reducible background fit using Bernstein polynomials

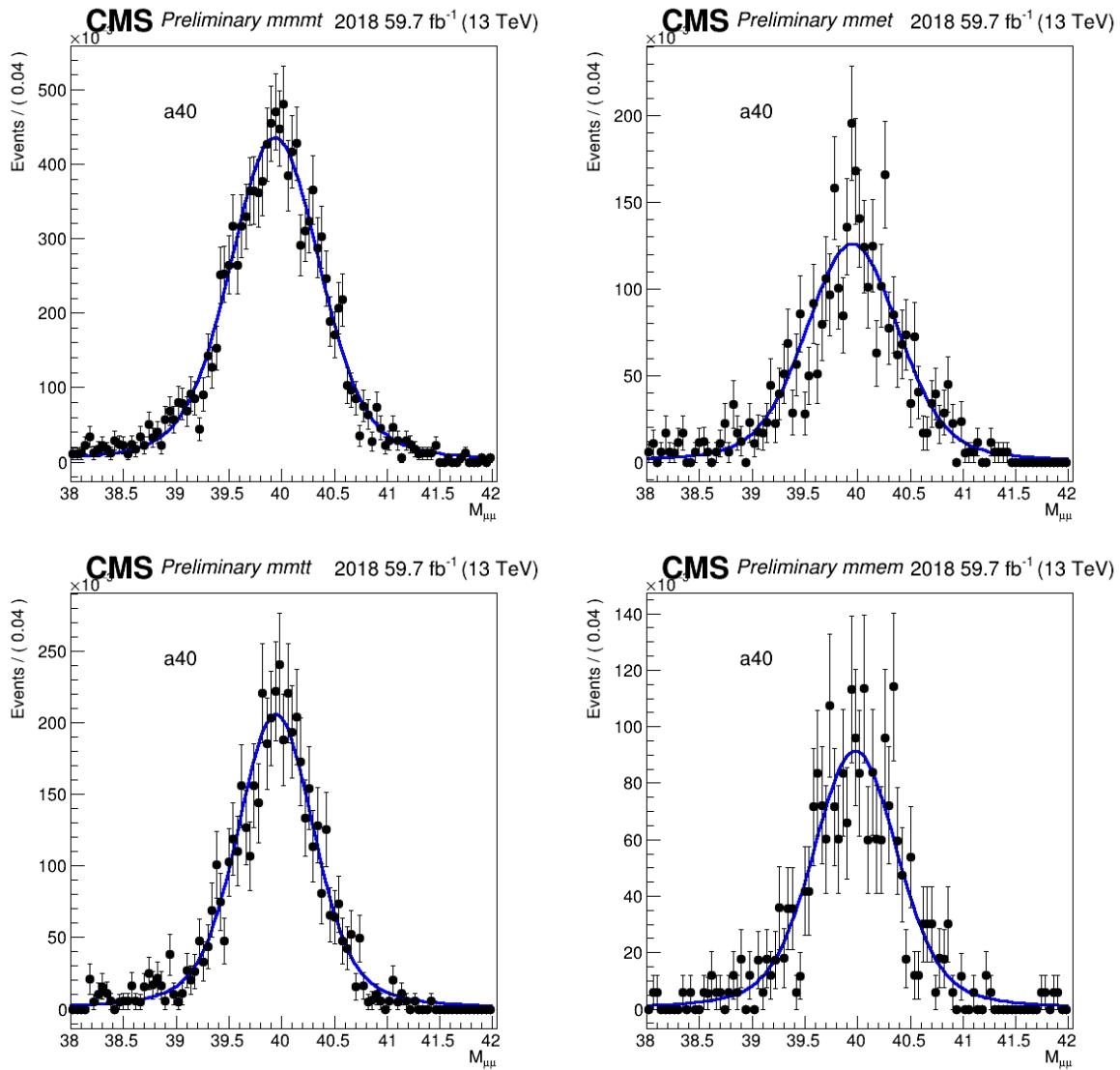


Figure D.8: 2018 Signal fit using a Voigtian function

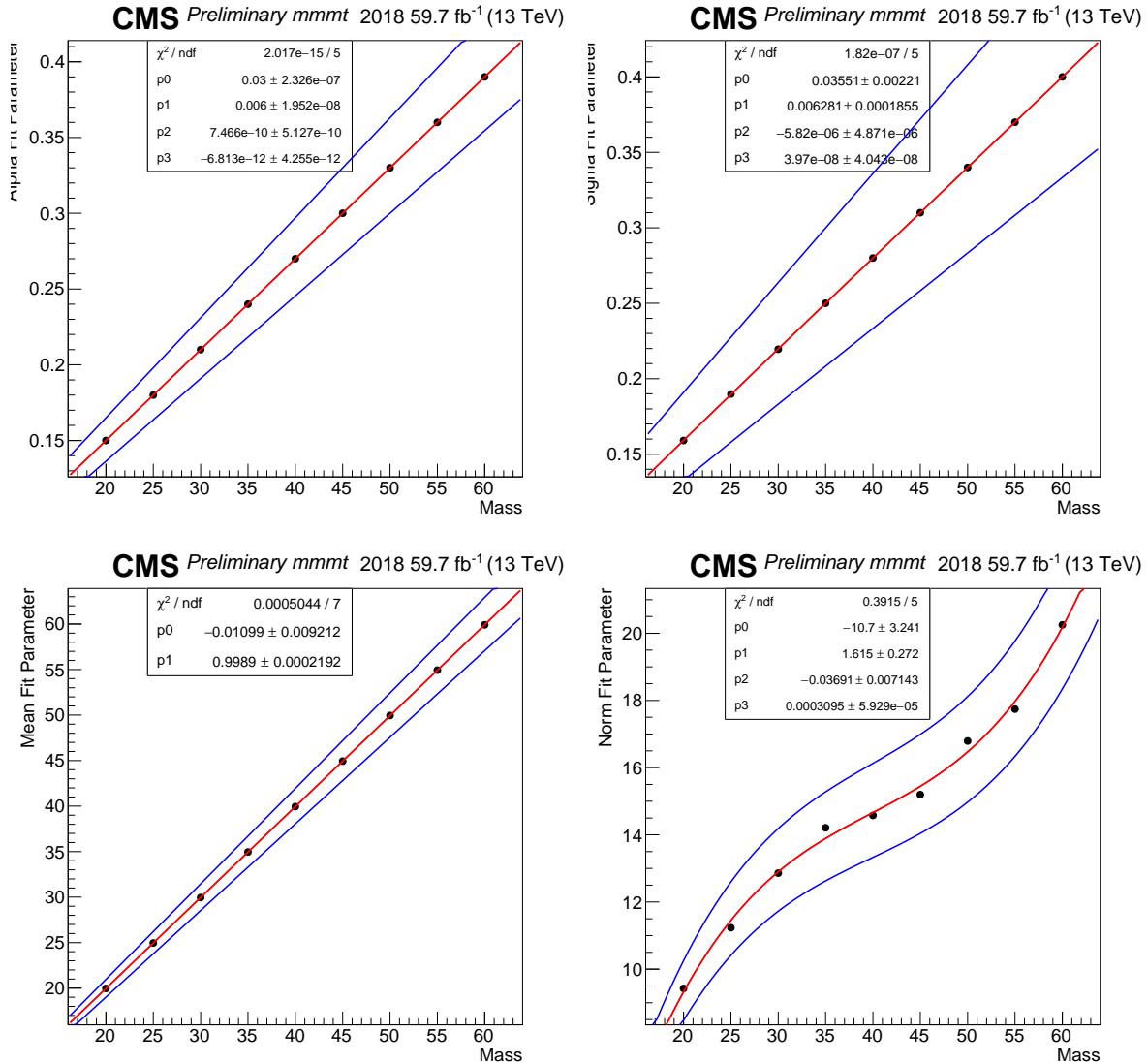


Figure D.9: Spline functions for 2018 mmmt a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

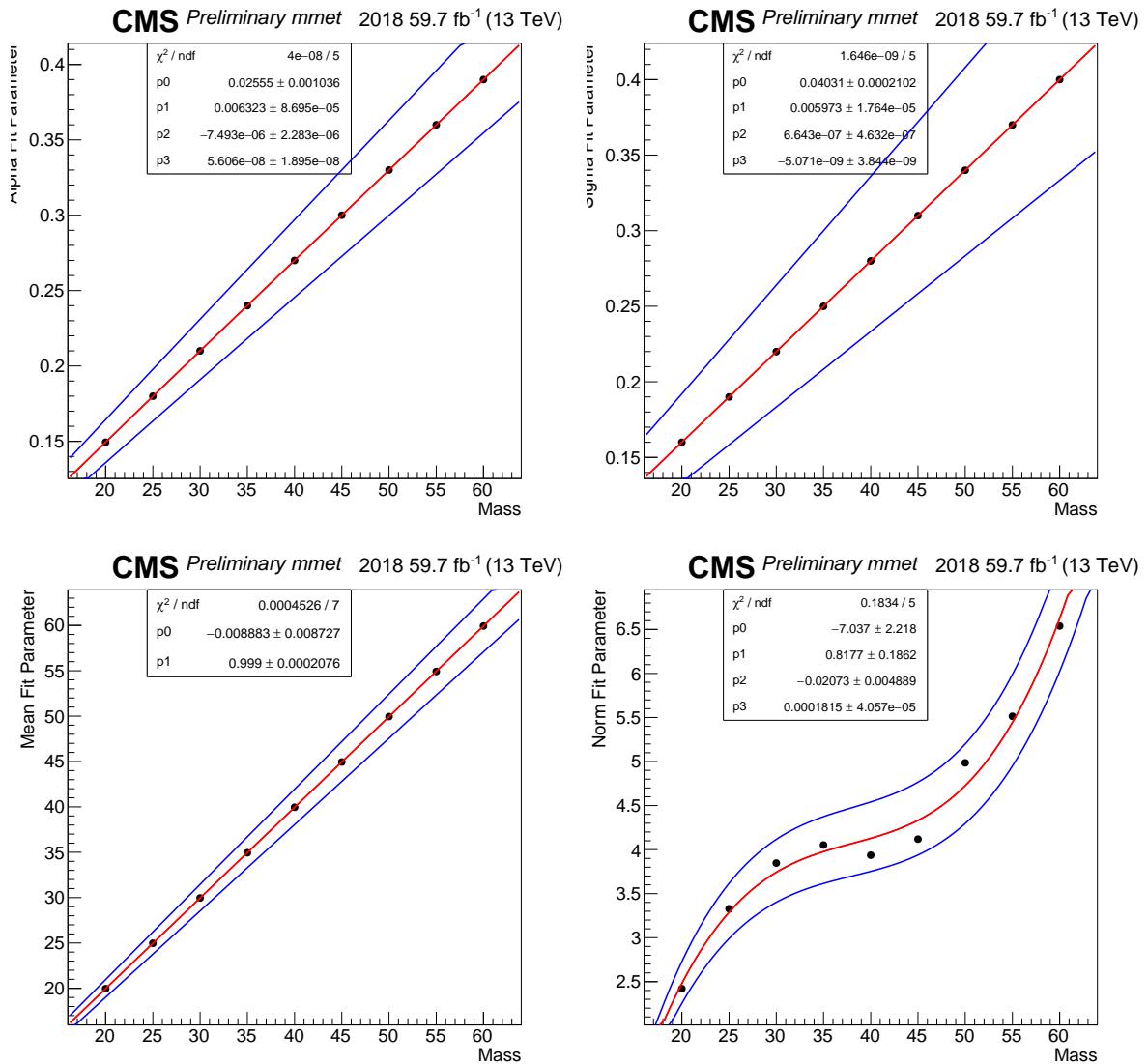


Figure D.10: Spline functions for 2018 mmet a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

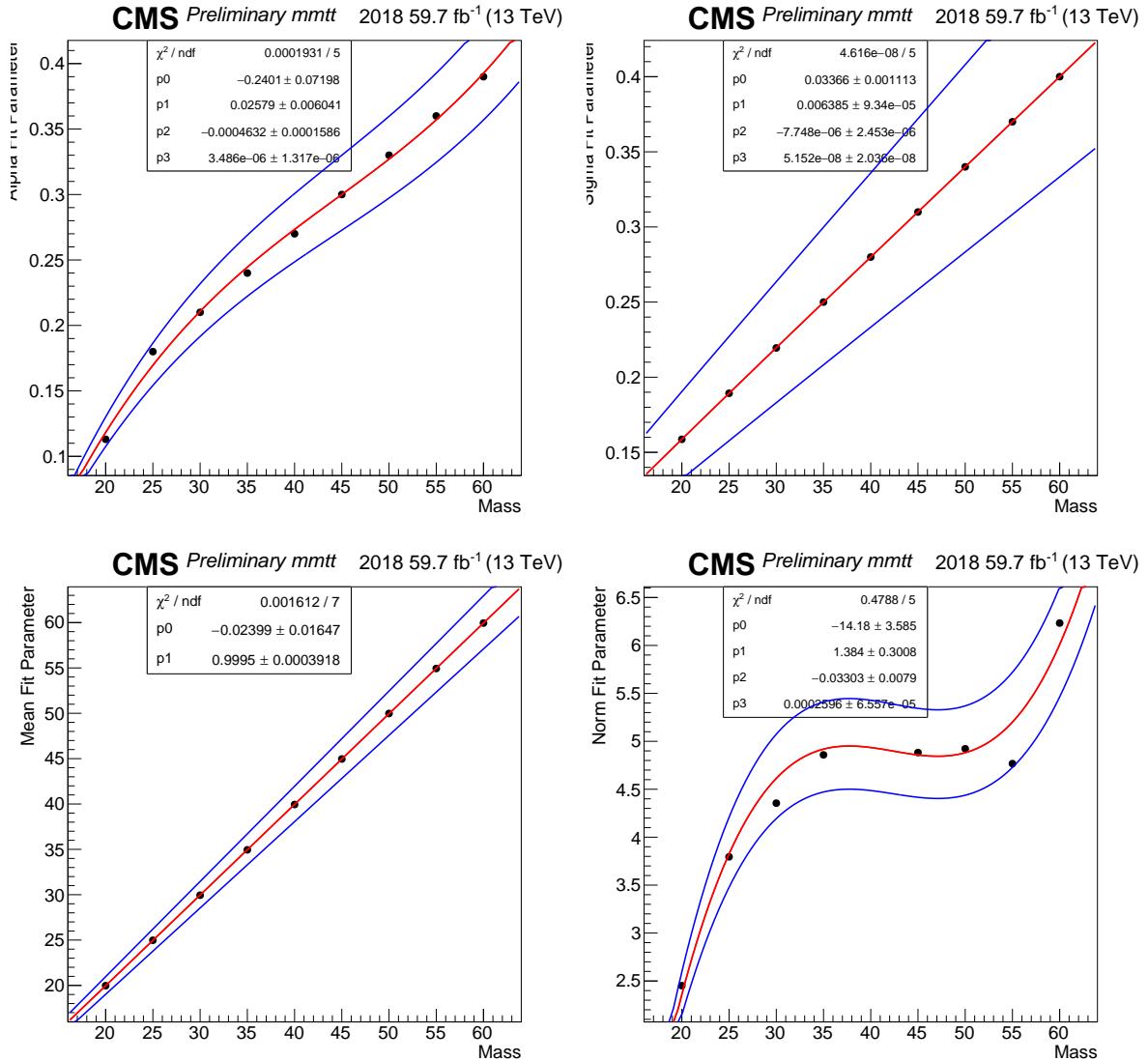


Figure D.11: Spline functions for 2018 mm $t\bar{t}$  a 3rd order polynomial is used for for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

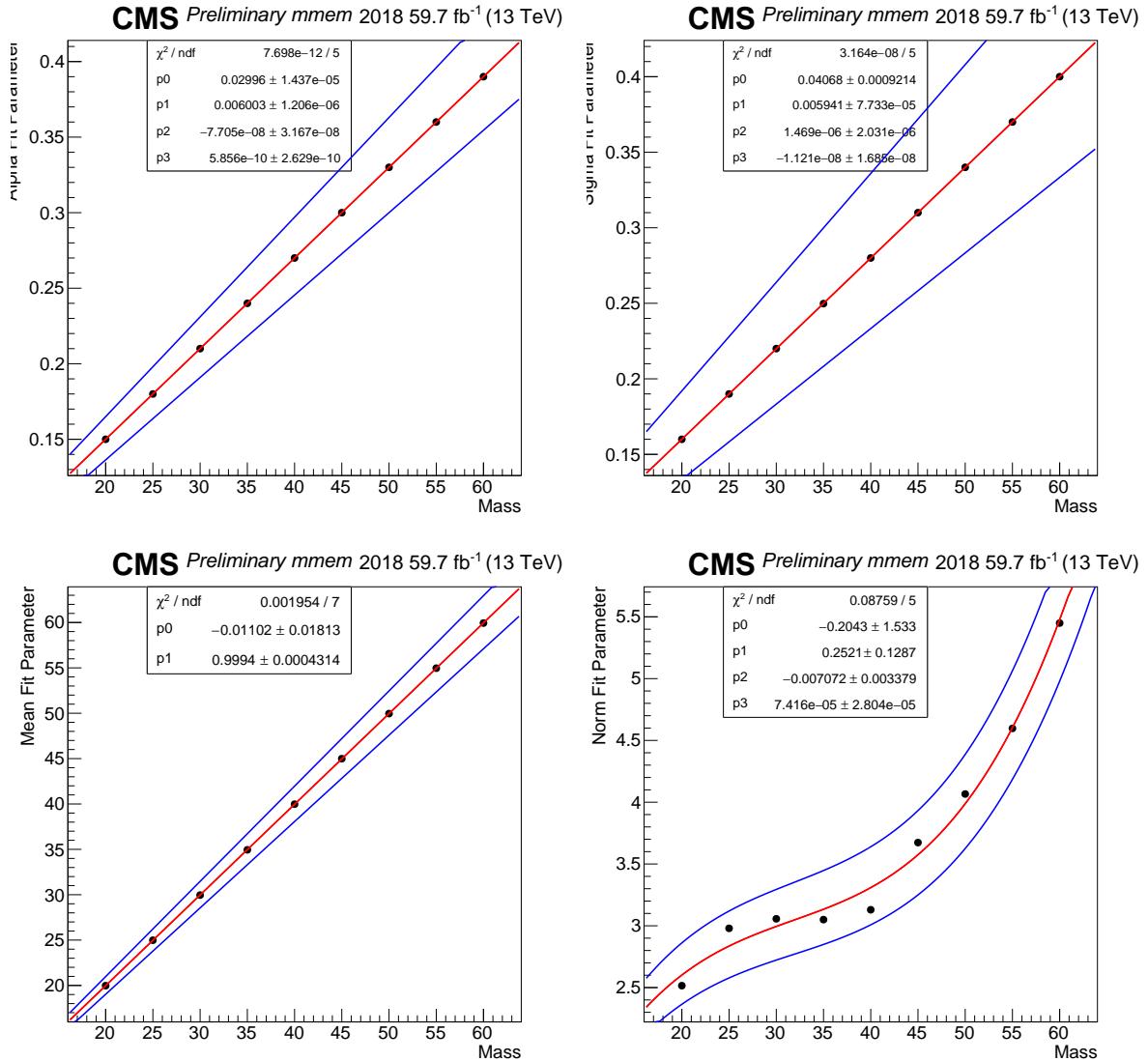


Figure D.12: Spline functions for 2018 mmem a 3rd order polynomial is used for Alpha, Sigma, and Normalization, a 1st order polynomial is used for the Mean

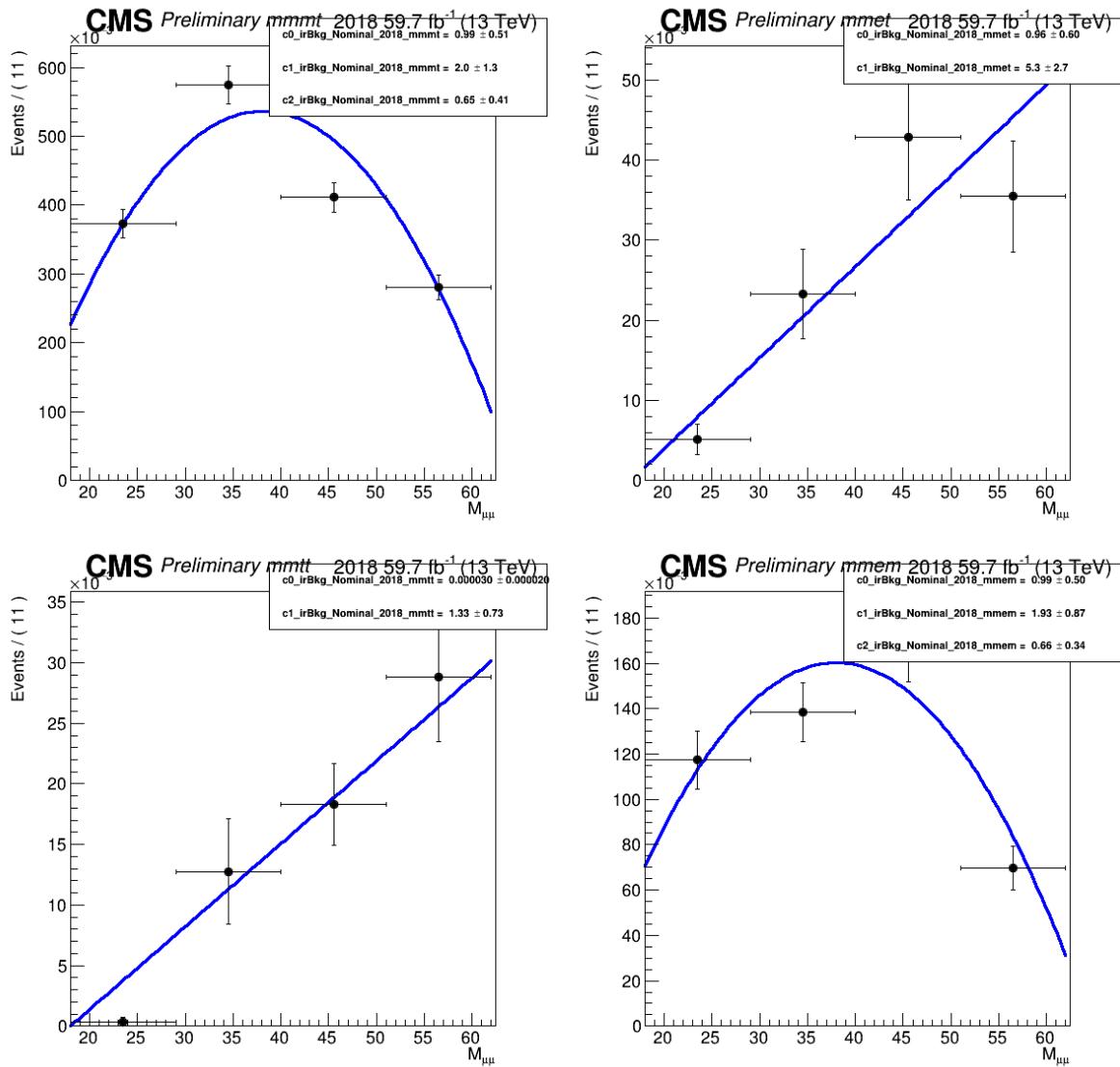


Figure D.13: 2018 irreducible background fit using Bernstein polynomials

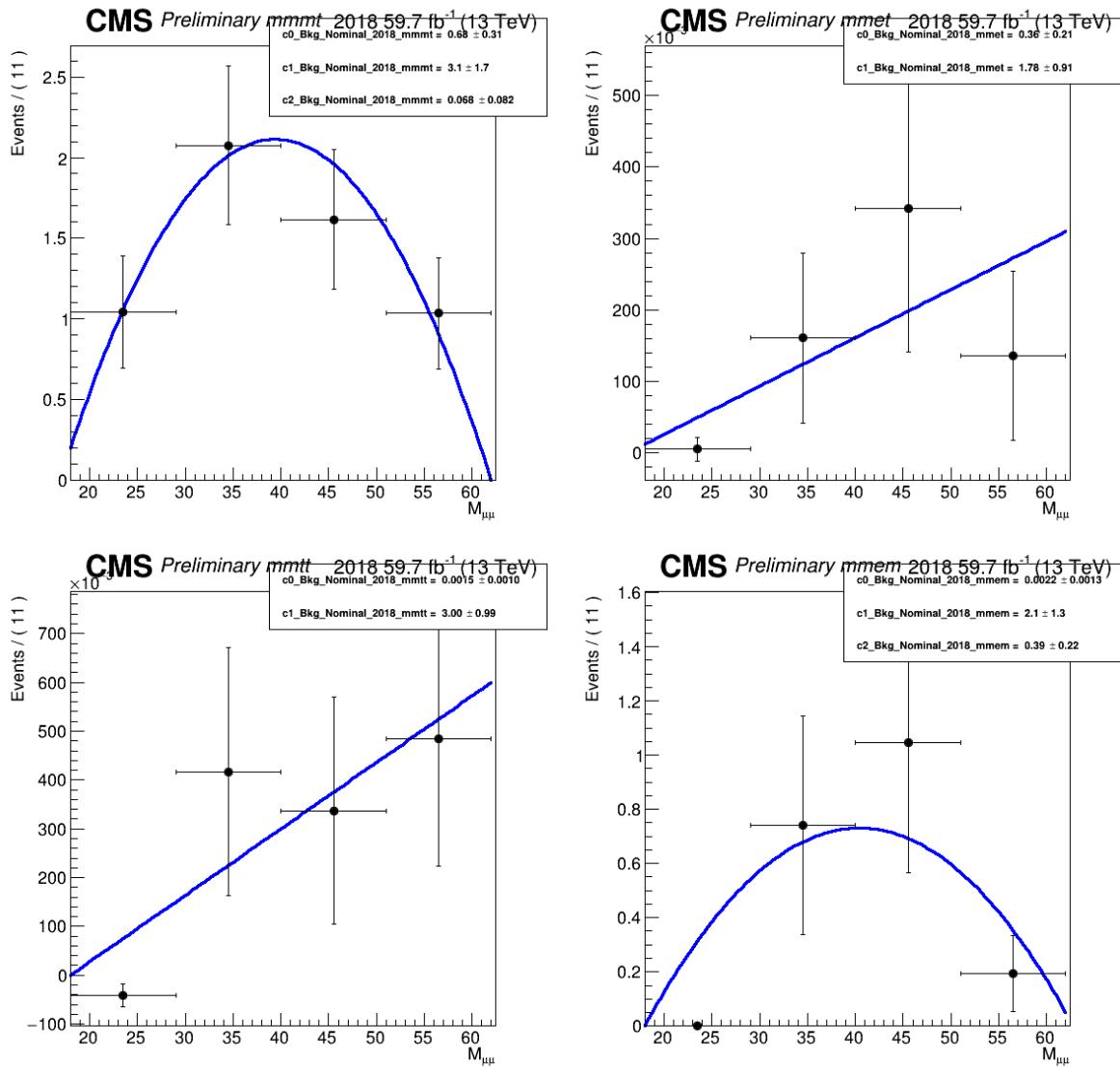


Figure D.14: 2018 reducible background fit using Bernstein polynomials

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