## lagrange interpolation formula

lagrange.m

```
______
% AUTHOR ..... [Lishan Huang]
% UPDATED .... [Jan 23]
% Evaluate the Lagrange interpolation formula
%
% INPUT
% tau .... The vector of interpolation nodes (length n)
% rho .... The vector of values at the interpolation nodes (length n)
% x .... A vector of values to evaluate the interpolating polynomial
at (length 1 to many (probably not n!))
% OUTPUT
% T :
______
function F = lagrange(tau, rho, x)
%initialize F=0
t=tau;
p=rho;
F=0;
%create a for loop
   for k=1:length(t)
      %make L=1 before each loop where 1 means Lk in the function
      L=1;
      for i=1:length(t)
          if i~=k
             L=L.*(x-t(i))./(t(k)-t(i));
          end
      end
      F=F+p(k).*L;
   end
end
```

## The first form of the barycentric formula

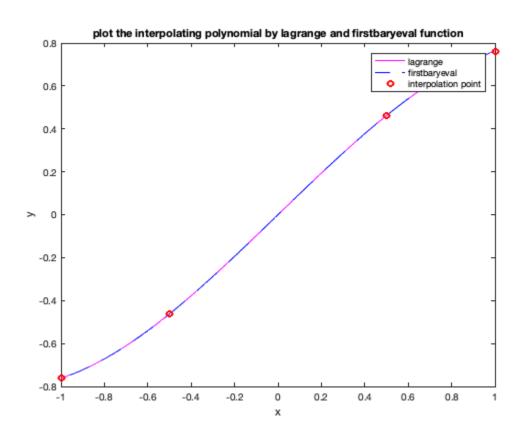
firstbaryeval.m

```
______
% AUTHOR ..... [Lishan Huanq]
% UPDATED .... [Jan 23]
% Evaluate the first form of the barycentric formula
% INPUT
% tau .... The vector of interpolation nodes (length n)
% rho .... The vector of values at the interpolation nodes (length n)
     .... A vector of values to evaluate the interpolating polynomial
at (length 1 to many (probably not n!))
% OUTPUT
% T:
______
function T = firstbaryeval(tau, rho, x)
%initialize t p T and a
   t=tau;
   p=rho;
   T=0;
   a=1;
   %calculate w(x) and store in a
      for k=1:length(t)
          a=a.*(x-t(k));
       end
   %create for loop to add up the function
       for k=1:length(t)
          b=1;
          %for loop for b(k)
          for j=1:length(t)
             if j~=k
                b=b.*((t(k)-t(j))).^{-1};
             end
          end
          T=T+b.*p(k)./(x-t(k));
       end
   T=T.*a;
end
```

## **Script**

```
%The following is a code that use lagrange and firstbaryeval function
to
%plot the interpolating polynomial
%
```

```
%define tau and rho
tau=[-1, -1/2, 1/2, 1];
rho=[-0.7616, -0.4621, 0.4621, 0.7616];
%create 100 equal point between -1 and 1
x=linspace(-1,1,100);
%use lagrange interpolation formula to evalue x
y=lagrange(tau,rho,x);
%use the first form of the barycentric formula to evalue x
z=firstbaryeval(tau,rho,x);
%plot the x y z
plot(x,y,'m',x,z,'--b')
%keep in the same graph
hold on
%plot tau rho
plot(tau,rho,'or')
xlabel('x')
ylabel('y')
title('plot the interpolating polynomial by lagrange and firstbaryeval
 function')
legend('lagrange','firstbaryeval','interpolation point')
```



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