The Macroeconomic Effects of Fiscal Adjusments in The UK

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0.1 Abstract

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1 Introduction

- motivate
- research gap / contribution
- summarise/ outline structure

This paper proceeds as follows, Section 2 provides a review of the related literature, focusing on the costs of high indebtedness and evidence on the effects of fiscal consolidation. We also provide a synthesis of the methods used to estimate fiscal multipliers, highlighting the use of Structural Vector Autoregressions (SVARs). This provides us with sufficient context and foundations to proceed with section 3 where we introduce the data and reduced form model. Here the Vector Error Correction Model (VECM) representation is considered as a generalisation of the VAR model which can yield efficiency gains when properly specified. We considered the merits of this representation and perform pre-testing of the specification. Following this, in Section 4 we introduce the identifying assumptions to allow us to recover the structural shocks. With our model now defined, Section 5 presents the results of this paper, focusing on the Impulse Response Function (IRF) and Forecast Error Variance Decomposition (FEVD). Overall, the IRFs of interest are statistically and practically significant; in Section 6 we consider robustness checks such as parameter stability and a lower lag length to see whether the results are sensitive to the specification. Finding that the result of low fiscal multipliers in the UK are robust to the specification, Section 7 proceeds with a discussion of policy implications. In Section 8 we then contextualize the results of this study and scope for future research, so that the results can be appropriately appreciated. Section 9 concludes.

2 Literature Review

2.1 Costs of high indebtedness

Warmedinger, Checherita-Westphal, and De Cos (2015) emphasise the importance of public debt sustainability for ensuring macroeconomic stability. Recent economic crises have been met with government intervention, leading to further strains on public finances. For instance, Sutherland, Hoeller, and Merola (2012) draw attention to the fiscal challenges facing countries following the Global Financial Crisis (GFC). They also note that gross government debt has exceeded 100% of GDP for the OECD as an aggregate. These concerns have been exacerbated following the Covid pandemic where governments implemented fiscal measures to mitigate the economic costs of the pandemic (IMF, 2023).

Makin and Layton (2021) highlight that governments must employ fiscal responsibility to protect their economies from the risks that high indebtedness exposes them to. There are several mechanisms through which these risks may

be presented. High indebtedness reduces the ability of countries to effectively respond counter cyclically to economic shocks. Additionally, when the interest rate exceeds the growth rate, the economy is unable to sustain the cost of growth. While Blanchard (2019) suggests that the low interest environments relative to growth seen recently have been persistent historically (which would suggest that debt could be self-stabilising due to economic growth outpacing the cost of debt), he also argues that there would still be a welfare cost in such a scenario. This is because Blanchard argues that capital accumulation reduces in response to high indebtedness. This aligns with the analysis of Alesina and Ardagna (1998) that "Wealth rises when future tax burdens decline": economic agents anticipate greater tax burdens due to the excessive levels of public indebtedness, and consequently confidence worsens leading to lower consumption and investment.

Kumar and Woo (2015) provide further evidence of the cost of public indebtedness, finding that greater indebtedness is associated with lower economic growth. They find noticeable non-linearities in this result, with the most severe effect occurring when public indebtedness exceeds 90% of GDP. Ilzetzki, Mendoza, and Vegh (2013) suggest that shocks to government speding can have strong negative effects on output at debt levels of as little as 60% of GDP. Recalling that public indebtedness has exceeded 100% in the OECD overall (Sutherland, Hoeller, and Merola ,2012), these results will be of particular interest for advanced economies. This highlights the importance of fiscal consolidation to ensure the long-term resilience of the economy. The IMF (2024) argue that economies should rebuild their fiscal buffers to reduce debt vulnerabilities, proposing that fiscal adjustments would need to be in the region of 4% of GDP. Sutherland, Hoeller, and Merola (2012) have argued for more aggressive adjustments, exceeding 5% of GDP in order to bring debt down to 50% of GDP. This figure would require the UK to halve its current debt levels (ONS, 2025). Thus, achieving this objective would require significant fiscal adjustments. The next subsection synthesises the literature on fiscal consolidation and its effects.

2.2 Fiscal Consolidaton

While the importance of fiscal consolidation has been highlighted, it is crucial that these measures are not at the expense of the broader economy. By investigating forecast errors for a sample of European countries, Blanchard and Leigh (2013) find that larger anticipated fiscal consolidation was associated with lower growth. This result was interpreted as due to the fiscal multipliers being greater than anticipated by forecasters. Consequently, fiscal tightening would have further dampened demand, meaning that improvements to government finances through fiscal consolidation would be offset by reduced growth. Gechert, Horn, and Paetz (2017) adopt a similar methodology, finding that austerity measures in the Euro Area deepened the GFC, with large persistence in their results. This suggests that, even in the long run, poorly implemented fiscal adjustments

could be counterproductive. Fatas and Summers (2018) extend this research, investigating the long-term effects that fiscal adjustments have had on GDP. Their analysis suggests that fiscal consolidations have failed to lower the debt-to-GDP ratio due to a hysteresis effect of contractionary fiscal policy. This research underscores the need to effectively quantify fiscal multipliers, allowing policymakers to better understand the potential trade-offs between various economic objectives.

Despite this, the literature has struggled to gain consensus on the size, and even the sign of fiscal multipliers (Caldara and Kamps, 2008). Similarly, Ramey (2016) notes that there has been conflicting evidence in the literature as to which fiscal policy has the greater multiplier, noting that the lack of precision of estimates have made it difficult to make meaningful comparisons. The next subsection focuses on the methodologies used to estimate fiscal multipliers. Before proceeding, we discuss further evidence in the literature of heterogeneity in fiscal multipliers.

Canzoneri et al (2016) suggest that fiscal multipliers can vary throughout the business cycle, with greater effects being observed during recessions. Auerbach and Goronichenko (2012) also provide evidence of the greater effectiveness of fiscal policy during recessions. Furthermore, they note that there can be heterogeneity of multipliers within specific fiscal instruments, noting that military spending had the greatest multipliers. Adding to the literature on state dependent multipliers, Ghassibe and Zanetti (2022) note that the cause of a recession determines the extent of fiscal multipliers. While they report government spending to have larger multipliers during demand-driven recessions, they note that these can be ineffective when the recession is driven by supply side factors. On the other hand, they note that policies such as reductions in income taxes can be effective during supply-driven downturns, as they can help to boost aggregate supply.

Ilzetzki, Mendoza, and Vegh (2013) suggest that the heterogeneity in the estimates reported in the literature can be attributed to differences in structural characteristics of the economy considered. Key characteristics that the authors emphasise include: the level of development, public indebtedness, and openness to trade.

Alesina, Favero, and Giavazzi (2015) compare multipliers due to spending and tax adjustments. They find that tax-based adjustments have more severe effects than those based on adjustments to expenditure. They attribute this result to business confidence. They argue that sentiment recovers quickly in response to government spending cuts, however increasing revenue does not address the root of the problem and thus confidence struggles to recover. Similarly, they attribute confidence to their finding that adjustments as less effective when subject to reversals: this creates noise when future adjustments are made, agents are unable to ascertain the reliability of announcements, and consequently their effectiveness decreases. This reinforces the importance of research to better understand the fiscal multiplier for different policy instruments, particularly as

this may vary across countries and over time.

While Baldacci, Gupta, and Granados (2012) find that successful debt consolidations are most likely when based on cuts to current expenditures, they note that raising tax revenue is also needed when the scale of fiscal consolidation needed is large. They use duration analysis to support their analysis, investigating hpw

2.3 Synthesis of Methodology

DSGE

Christiano, Eichenbaum, and Rebelo (2011) investigate the size of the output multiplier for government spending using a Dynamic Stochastic General Equilibrium (DSGE) model. Through this model, they show that the multiplier for government spending can be greater than 1 when the zero bound binds.

Barnichon, Derbotoli, and Matthes (2022) find asymmetric effects of shocks to government spending: while they suggest the contractionary multiplier can exceed 1 during recessions, they find the expansionary multiplier to always be less than 1. The authors employ the Functional Approximations of Impulse Responses methodology (Barnichon and Matthes, 2018)

Woodford (2011) also use a DSGE model, finding that wage rigidities and stiky prices allow for larger multipliers than anticipated in a neoclassical model. They also find that the multiplier can exceed 1 wjem the zero bound binds, attributing this to the ability of government spending to fill the output gap when interest rates cannot be lowered.

Zubairy (2014) estimate a DSGE model, finding a crowding in effect of government spending, peaking at impact.

Capek and Cuasera (2020) simulated 20 million fiscal multipliers, highlighting how methodological choices contribute to the heterogeneity in estimates of fiscal multipliers prevalent in the literature. Consequently, they advocate for explicitly outlining modelling choices and assumptions. Similarly, Gechert (2017) provides a synthesis of the methodologies used to estimate fiscal multipliers, highlighting competing definitions for the fiscal multiplier and possible issues in its estimation. Among these issues, Gechert (2017) highlights potential omitted variable bias in the VAR model. When such variables are excluded from the VAR model, Structural VAR (SVAR) tools such as IRFs may lose their interpretation due to contamination with the unobeserved effect.

Structural Vector Autoregressions (SVARs) have been prominent in the literature to estimate fiscal multipliers. Various approaches to identification have been used, with XXX (YYYY) noting that after accounting for the empirical specification, the competing identifying approaches have little effect on the

estimated multipliers. Blanchard and Perotti (2002) pioneered this strand of the research, leveraging methodologies previously popularised by the monetary economics. To identify their SVAR, Blanchard and Perotti leverage instituional information. They provide a definition for the fiscal variables and highlight that government expenditure is predetermined within a quarter. Recursive measures to identification have been employed by Fatas and Mihov (YYYY) and Fernandex (2008). Fernandez argues that Uhlig and Mountford (200Y) apply restrictions on the signs of the impulse response functions. Caldara and Kamps (2008) reviews the literature on SVAR identification. Caldara and Kamps (2017) introduce a new approach for identification.

Kim et al (2021) extend the recursively identified SVAR, finding evidence of cointegrating relationships ¹. Consequently, they estimate the reduced form by a Vector Error Correction Model (VECM), attempting to take advantage of the information on the model's long run dynamics contained within the cointegrating relationships.

Auerbach and Gorodnichenko (2012) explore state-dependent fiscal multipliers using regime-switching models. They find evidence of substantial differences in multipliers between recessionary and expansionary periods.

Add DSGE lit for context

3 Econometric Methodology

Despite the literature highlighting possible importance of state dependence, we focus on a linear VAR model. Reason is that little research has been performed on mulitpliers for the UK, scope is to ...

This research employs a structural vector autoregressive (SVAR) approach to estimating fiscal multipliers. In this section we outline the empirical methodology, as well as the data. We use quarterly data from 1987:1 to 2023:3, modelling this using a six-dimensional VAR at with a lag length of 4. This lag order follows Blanchard and Perroti (2002), and suggests that past values of the endogenous variables continue to have an effect for up to a year. While statistical procedures were not used to determine this lag order, it has an econometric rationale: Kilian and Lutkepohl (2016) note that due to poor finite sample properties of lag selection techniques, it may be appropriate to impose a fixed lag length. Particularly when concerned with impulse response analysis, the risks of underestimating the lag length exceed those of using a larger order which may better reflect the dynamics of the data at the cost of inefficient estimates. Given these

¹The authors rely on Johansen's cointegration tests although do not appear to consider finite sample bias in the test, which we highlight later in this paper. Nevertheless, given the use of monthly data, their sample size is greater than this paper's leading to a lower finite sample scaling factor. Their tests for cointegrating ranks appear to remain valid after applying the finite sample correction.

considerations, and the degrees of freedom restrictions imposed by the sample size, the lag order of 4 was determined.

Regarding the endogenous variables included in the VAR model, Blanchard and Perotti (2002) investigate the effects of fiscal shocks using a three-dimensional VAR model consisting of GDP, government expenditure, and government revenue. While such a model could be used to estimate the effects of fiscal shocks, Gechert (2017) highlights the potential issues of omitted variable bias. Therefore, we augment the model to include also a short term interest rate, the GDP deflator rate, and and exchange rate index (ERI). These variables are included to account for the effects of monetary policy, price levels, and interactions with the rest of the world respectively. Consequently, the impulse response functions reported later are better interpreted as the response of GDP to the fiscal variables, ceteris paribus.

The fiscal variables are sourced from the ONS and defined following the European System of Accounts (ESA, 2010). The data is available at the central, local, and general levels, the ESA defines general government as encompassing both central and local levels. Therefore the general level is used for this analysis so that the multipliers represent the full effects of fiscal policy. In further detail, government expenditure is defined as the outflows associated with government activities, including consumption, investment, and transfers. The inflows to the government, government revenue, consists of receipts net of transfer and interest payments. These definitions follow those used elsewhere in the literature, minimising the effect of methodological differences on this paper's results (Gechert, 2017). We use variables in real terms, while data for GDP was sourced from the ONS already in real terms, the ONS (2023) report that the data used for public sector finances are not adjusted for inflation. Therefore, we process the fiscal variables into real terms, scaling by the deflator rate. ² Following Capek and Cuaresma (2020), who highlight that data for estimating fiscal multipliers is typically seasonally adjusted, we applied the X-13 ARIMA-SEATS method to our variables. Gross Domestic Product (GDP) was an exception, as it was sourced after seasonal adjustment. This process reduces noise in the data, leading to more meaningful results. Consistent with Fernández (2006), all variables are log-transformed prior to estimation, except for the short-term interest rate, which enters the model in levels. This will facilitate an intuitive interpretation of results in percentage terms. Given that this analysis uses data from 1987, SONIA (which was introduced in 1997) could not be used as the short term interest rate, instead we use the 3 month interbank rates sourced from the Federal Reserve Bank of St Louis. We use the Sterling ERI from the Bank of England, this index is weighted by trade patterns (Lynch and Whitaker, 2005), thus allowing the ERI to effectively capture the effects of the UK's interactions with other economies.

²Given that the GDP data is in terms of current prices, we also divide by the deflator rate in Q4 2024 (the final quarter in our data). This allows for more intuitive comparisons of the data.

The data series across the sample period are plotted in the data appendix. A key feature of these series is the apparent presence of a deterministic linear trend driving the series upwards (with the exception of the exchange rate and mean short run rate). This suggests that the VAR system may be trend stationary, thus we include a linear deterministic trend in our specification. This will mitigate spurious correlation in the model due to exogenous trending factors.

3.0.1 Model

3.1 **VECM**

The reduced-form VAR model can be written as:

$$X_{t} = \mu + A_{1}X_{t-1} + \dots + A_{p}X_{t-p} + \epsilon_{t}$$
 (1)

where:

$$X_t = \begin{pmatrix} G_t \\ R_t \\ GDP_t \\ ERI_t \\ \tau_t \\ P_t \end{pmatrix}$$

Here the vector X_t defines the endogenous variables, as previously mentioned, we have assumed a lag order (p) of 4. The term μ in equation 1 captures the deterministic component of the model. Given the trending behavior between the fiscal variables, the deflator rate, and GDP: we use a linear deterministic trend for this.

Kilian and Lutkepohl (2016) show that the VAR model can be reparameterised as a Vector Error Correction Model (VECM) by subtracting the lagged variables and rearranging terms:

$$\Delta X_t = \Pi X_{t-1} + \sum_{i=1}^{k-1} \Gamma_i \Delta X_{t-i} + \mu + \varepsilon_t \tag{2}$$

When correctly specified, this representation can yield efficiency gains: including the error correction term may allow the model to capture important dynamics in the long run relationships between variables (Martin, Hurn, and Harris; 2013). We therefore perform tests for cointegration to determine the appropriate specification before estimating the model.

Given the small sample sizes associated with macroeconomic time series, various Monte Carlo simulations have been performed to assess the finite sample properties of cointegration tests. Hubrich, Lutkepohl, and Saikkonen (2001) find

that the Likelihood Ratio type tests are among the best performing, with other classes of tests having worse power or size. Therefore we focus on this class of cointegration tests. Madadala and Kim (1998) provide a review of studies investigating Johansen's cointegration tests, highlighting that: sample sizes upwards of 100 may be needed to appeal to asymptotic results, tests can be misleading when too few variables are included, and insufficient lag lengths can lead to size distortions. Fortunately, these considerations do not appear to be a concern for this research. As previously discussed, due to concerns with underestimating the lag order when evaluating IRFs, we assume a lag order of 4, which we believe to be at least equal to the true lag parameter. ³ Additionally, we have added additional control variables to the VAR model to mitigate omitted variable bias (Gechert, 2017) which should alleviate the concern raised by Madadala and Kim. Nevertheless, Madadala and Kim highlight further complications of the test. We therefore consider this in detail before testing for cointegration.

Lutkepohl, Saikkonen, and Trenkler (2001) find that in small samples, while trace tests had size distortions, they had power advantages relative to the maximum eigenvalue test. This suggests that there may be merit in considering both tests. Cheung and Lai (1993), using a Monte Carlo simulation, find that there is finite sample bias in Johansen's cointegration tests, with both the maximimum eigenvalue and trace tests finding cointegration at a rate greater than implied by asymptotic theory. They therefore apply a scaling factor to the asymptotic critical values given by

$$SF = \frac{T}{T - kp} \tag{3}$$

where T is the number of observations, k the number of variables in the system, and p the lag order. Gonzalo and Lee (1998) provide further evidence of bias in Johansen's cointegration tests, identifying cases where the test detects spurious cointegration. In light of this, we ensure the asymptotic results reported as standard are scaled to account for the finite sample bias in the test.

Aside from the type of cointegration test, Hubrich, Lutkepohl, and Saikkonen (1998) highlight that improperly specified deterministic terms invalidate cointegration testing, leading to reduced power. Given that we have suggested the model to follow a deterministic linear trend, we ensure this is captured in our test. Martin, Hurn, and Harris (2013) highlight that a constant deterministic component in cointegration implies a linear trend in the VAR. We therefore include a constant term in cointegration when reporting the following Johansen's tests for cointegration.

Watson (2000): specification of deterministic components affects the power of tests

³While not relied on for determining the lag order, lag order selection procedures including the Akaike Information Criteria suggest that a lag as low as 2 may be appropriate for the levels VAR. Due to the considerations mentioned, we decide to use a fixed lag order of 4. The sensitivity of the final results to the lag order is considered as a robustness check.

We begin by performing Johansen's maximum eigenvalue test for cointegration, which compares the null hypothesis of rank r, to the alternative of rank r+1. Accounting for the finite sample bias in the test, we find insufficient evidence to reject the null hypothesis of no cointegrating relations at the 5% significance level. Consequently, the VECM reduces to a VAR in the differences of variables (Kilian and Lutkepohl, 2016). Per the previous review of cointegration tests, we also perform Johansen's trace test. This test has as the alternative hypothesis that the rank is greater than assumed under the null hypothesis. Again, we reject the null hypothesis of no cointegration after accounting for the test's finite sample bias.

Kilian and Lutkepohl (2016) highlight the asymmetric consequences of imposing a unit root. When the underlying data generating process possesses a unit root, the reduced form model can benefit from increased efficiency in estimation by imposing a unit root. Failing to impose a unit root in such a case would only reduce the precision of the Least Squares estimates. In contrast, when the underlying process does not follow a unit root, incorrectly imposing one would result in over-differencing - yielding an inconsistent estimator. Nevertheless the tests conducted provide little evidence of cointegrating relations, and thus the VAR in differences is viewed as the appropriate specification. As well as the statistical merits of this specification, it yields an intuitive interpretation. As the alternative specification was a VECM with rank 1, we considered the 1st eigenvector for the cointegration relations, and concluded that this did not provide meaningful information on the long run equilibrium behaviour of the system. ⁴ Therefore, we proceed in this analysis with the VAR in differences representation of the model, given the differencing, the lag order reduces to 3.

For robustness we also perform Phillips-Ouliaris' (1990) residual based test for cointegration. Using this test we again fail to reject the null hypothesis of no cointegration, suggesting that a VECM is not an appropriate representation for our data.

Add code results to appendix?

NB on unit root tests: failing to reject H0 does not mean we accept H0!!!! (Lutkepohl)

 $^{^4}$ The reported cointegrating relation was $log_expenditure = -0.14 \cdot mean_SR_Rate + 1.6 \cdot log_GDP + 3.9 \cdot log_ERI - 3 \cdot log_revenue + 9 \cdot log_deflator + \epsilon_t$ where ϵ_t is I(0). Inflation and the short term rate both represent costs for government spending, so these would be expected to have negative signs. While this was true for the mean short term rate, the cointegrating relation suggested that a shock to the long run equilibrium of the deflator rate led to a large positive increase to expenditure. This is not expected, while it could be argued that the government spending is relatively inelastic, meaning that the government absorbs increased costs rather than reduce spending, the magnitude of the reported effect is difficult to reconcile and the inconsistency in the signs of the 2 variables questions the appropriateness of this cointegrating relation. Additionally, the cointegrating relation suggests that an increase in government spending from the long run equilibrium is associated with a 3 times greater increase in government revenue (all else equal).

3.2 Identification

Thus far we have only defined the reduced form VAR. The residuals in this model are not meaningful as they are linearly dependent, instead, the interest of this research lies in the structural model. The structural shocks are mutually uncorrelated and have clear interpretations (Kilian and Lutkepohl, 2016). These shocks will allow us to construct FEVDs and IRFs to report the findings of this paper.

The structural model can be written as

$$\beta_0 X_t = \mu + \beta_1 X_{t-1} + \dots + \beta_p X_{t-p} + u_t \tag{4}$$

Here u_t denotes the structural errors. We also observe that equation 1 for the reduced form model can be rewritten as:

$$X_t = \mu + B_0^{-1} B_1 X_{t-1} + \dots + B_0^{-1} B_p X_{t-p} + \epsilon_t \tag{1a} \label{eq:1a}$$

The term B_0^{-1} is referred to as the structural impact multiplier matrix. Comparing equations 1a and 4, it is clear that knowledge of the structural impact multiplier matrix or its inverse would allow us to move between the structural and reduced form representations, thus recovering the structural shocks. More explicitly, we can write the structural shocks as functions of the reduced form residuals:

$$\epsilon_t = Bu_t \tag{5}$$

As outlined in the literature review, there have been numerous approaches to identifying the structural parameters. This study uses recursive sign restrictions, leveraging the Cholesky decomposition. To recover the structural shocks using this approach, we assume B to be a lower triangular matrix and that the structural shocks have unitary variance 5 . This corresponds to a causal ordering of the transmission of shocks: the first variable is considered the most exogenous, affecting all others. In contrast, the variable ordered last is considered the most endogenous, being contemporaneously effected by shocks to all other variables, whilst having no instantaneous effect itself on the other variables. Having defined this recursive ordering, given that the matrix B is assumed to be lower triangular, we can estimate it using the Cholesky decomposition of the covariance matrix of the reduced-form residuals (Σ_{ϵ}):

$$\Sigma_{\epsilon} = E[\epsilon_t \epsilon_t'] = BB' \tag{6}$$

 $^{^5}$ The assumption of unitary variance for the structural shocks is not restrictive as it can be imposed by rescaling the variables. This assumption, however means that the reduced form covariance matrix reduces to equation 6.

Therefore we have that $B = Chol(\Sigma_{\epsilon})$

This paper uses the following recursive ordering:

$$(G, R, GDP, ERI, T, P) (7)$$

With the variables corresponding to government expenditure, the short term interest rate, GDP, the Exchange Rate Index, net taxes, and the GDP deflator respectively.

The matrix B has the form:

$$B = \begin{pmatrix} b_{11} & 0 & 0 & 0 & 0 & 0 \\ b_{21} & b_{22} & 0 & 0 & 0 & 0 \\ b_{31} & b_{32} & b_{33} & 0 & 0 & 0 \\ b_{41} & b_{42} & b_{43} & b_{44} & 0 & 0 \\ b_{51} & b_{52} & b_{53} & b_{54} & b_{55} & 0 \\ b_{61} & b_{62} & b_{63} & b_{64} & b_{65} & b_{65} \end{pmatrix}$$
(8)

Thus, the structural shocks u_t can be recovered as:

$$u_t = B^{-1}\epsilon_t \tag{5a}$$

Killian and Lutkepohl (2017) highlight that identification of the structural parameters is not a purely statistical concern, the restrictions must also be economically meaningful for the resulting structural parameters to be identified. Therefore we proceed with an exposition of the economic assumptions implicit in our identifying restrictions imposed by the matrix B. The following is comparable to Fernandez's (2006) identifying assumptions.

Blanchard and Perotti (2002) argue that the use of quarterly data allows government spending to be treated as predetermined with respect to the rest of the variables within the quarter. This is motivated by implementation lags for changes to government spending and consequently this is ordered first. Given physical constraints, the interest rate is assumed not to react contemporaneously to price, net taxes, output, or the exchange rate. Thus the short term rate is considered the next most exogenous variable. However monetary policy shocks are assumed to affect output, net taxes, prices, and the exchange rate contemporaneously. Fernandez (2006) justifies this assumption by noting that interest movements are anticipated and thus they can be transmitted to real variables relatively quickly. Shocks to the exchange rate are assumed to affect net taxes contemporaneously as households adjust to changes in the cost of imports. Investment plans take time to adjust, as does consumption due to internal habit which leads to highly persistent levels of consumption. Consequently, we do not expect shocks to net taxes to affect activity. However, shocks to economic activity is expected to affect contemporaneous tax receipts to the government as households respond to prevailing economic conditions. Despite the aforementioned internal habit, this behaviour is expected as households attempt to smooth fluctuations in their consumption path, consequently they may adjust their behaviours towards consumption and saving, which is expected to have tax implications. Due to price stickiness, prices do not react contemporaneously to shocks to GDP.

4 Results

Given that we have performed cointegration tests, it would suggest that the appropriate model has been chosen, and thus we would expect the stability of the VAR model. This is supported by inspecting the eigenvalues of the VAR model, the greatest of which is 0.78 suggesting that we do not have issues of explosive roots. We therefore proceed by presenting the results of the SVAR analysis, focusing on Forecast Error Variance Decompositions (FEVDs) and Impulse Response Functions (IRFs)

4.1 IRFs

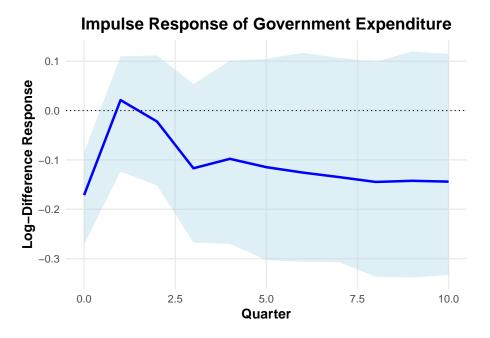


Figure 1: Impulse Response Function of GDP Following a Shock to Expenditure

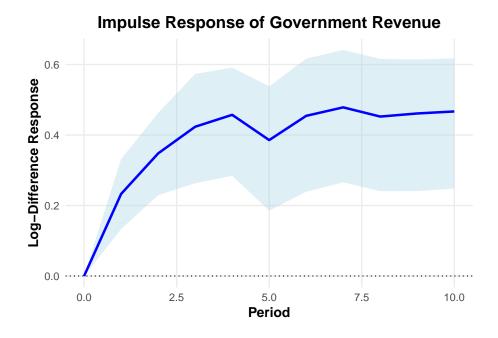


Figure 2: Impulse Response Function of GDP Following a Shock to Revenue

There are multiple definitions for fiscal multipliers in the literature, this paper follow's Ramey (2019), defining them as "the ratio of the change in output to the change in the [fiscal variable] that caused it". This allows us to interpret our IRF results as fiscal multipliers. Clearly this definition is not complete as IRFs are dynamic functions, their value may change depending on the period considered. This paper pays special attention to 2 horizons, the instantaneous multiplier, and the multiplier after 10 quarters. While the dynamics of the fiscal multipliers could be expected to last beyond 10 quarters, we expect the majority of the response of output to a transitory shock to the fiscal variables to be captured within this horizon. Furthermore, extrapolating to further horizons would reduce the confidence with which we could report our results. Therefore we report the cumulative structural impulse response functions up to a horizon of 10 quarters including bands for the 68% confidence intervals. Kilian and Lutkepohl (2016) highlight that given the short sample sizes VAR models are typically estimated on, this level is more appropriate than the typical 5\% significance level. Furthermore, given the low sample size we do not appeal to asymptotic results, instead we report a bootstrap confidence interval. Using a 68% confidence interval therefore requires fewer iterations to accurate estimate this interval. The IRF function from the VARS library in R implements Efron's (1992) percentile interval. It should be highlighted that unlike standard confidence intervals constructed using standard errors, Efron's percentile interval are often asymmetric about the point estimate (Efron, 1981).

Here we focus on the response of GDP to the fiscal variables, the appendix includes comprehensive details of the IRFs for each of the variables. Figure 1 summarises the results for a shock to government expenditure. Given the model specification, the results will be interpreted in terms of percentage growth. We find a point estimate of -0.17, suggesting that a standard deviation shock to the percentage growth of expenditure is associated with a reduction in GDP growth of (-22% of a standard deviation?). The confidence interval for this IRF is - (-0.29, -0.08). As 0 is not contained in this interval, it suggests that there is a statistically significant crowding out effect of government expenditure. Nevertheless, tracing the IRF out over time, by the next quarter the cumulative response is positive, stabilising at a value of -0.14 by the 10th quarter. However, the percentile intervals for these later IRFs contain 0 and thus these results are not statistically significant.

Considering now the response of GDP to a shock to government revenues, we find no effect in the quarter of the shock. There is a temporary negative effect in the following quarter, however this is reversed as we report a positive cumulative IRF by the second quarter. Similar to the response to government expenditure, following the 2nd quarter no further effects are detected. Again, our percentile intervals include 0, and thus the multiplier for government revenue is not statistically significant. Interestingly, the reported point estimates for government spending and revenue have similar magnitudes, despite much of the literature reporting differences.

4.2 FEVDs

Given that we have used a VAR in differences, with a logarithmic functional form for the variables initially in levels, we can interpret the FEVD as illustrating how each shock contributes to volatility in the growth in each variable. Considering GDP, we find that 97% of variability in GDP growth is explained by itself a quarter after a shock. By 10 quarters, this percentage reduces to 76%. While a reduction, this still highlights a notable degree of persistence in GDP. In fact, the fiscal variables explain only 12% of the Mean Squared Prediction Error in GDP growth. This supports the IRF results, which finds negligible impact of fiscal policy on GDP.

cf IRFs, large persistence in GDP growth consistent with the low multipliers observed, after 10 periods, the fiscal variables combinned explain only c 20% of variability in GDP ...

4.3 Counterfactual

5 Robustness

5.1 Chow test for Structural Breaks

Lutkepohl and Kilian (2016) highlight paramater instability as a major concern for SVAR analysis. Following the Global Financial Crisis (GFC) there were major changes to government finances (source?), which may have lead to changes in the structural parameters. This can also be seen in the plots in the data appendix, where the trends appear to change in 2008. We thus consider as a test for robustness whether the parameters have remained stable across the period, using 2008 as a potential breakpoint.

Using an asymptotic likelihood based Chow test we find significant evidence to reject the null hypothesis of no parameter instability. Nevertheless, Lutkepohl and Candelon (2000) highlight that when the sample size is low relative to the nuber of parameters, the Chow test may have distorted size. Given that we are considering a 6-dimensional VAR in this analysis, with a sample period of less than 40 yeas at a quarterly frequency, this issue is likely present in this analysis. Therefore we also consider a bootstrap version of the Chow statistic the authors show to have more desirable finite sample properties.

Following Lutkepohl and Candelon (2000), we implement our recursive residual-based boostrap for the Chow test as follows:

- 1. Estimate the restricted VAR model (pooling both periods around the GFC)
- 2. Obtain the demeaned residuals from the restricted model.
- 3. Generate bootstrap residuals by randomly drawing from the centered residuals with replacement.
- 4. For each iteration, estimate the restricted and unrestricted models (where we allow the parameters to vary across the samples).
- 5. Compute the Chow statistic (Here we use the same likelihood based Chow test as with our asymptotic testing).

Through this process we can derive the empirical distribution of the bootstrap time series. Chow statistic under the null hypothesis of parameter stability. We then compute the pseudo p-value as the percentage of times the bootstrap statistic exceeds the test statistic. Using 100 replications, we find a p-value of 0, this can be further seen in figure 3 where the test statistic exceeds even the greatest boostrap statistic by a factor of 2. This supports the previous asymptotic test of parameter instability. We therefore estimate the SVAR on

Bootstrap Chow Test (Recursive)

Breakpoint: 2008 | p-value: 0

400

400

100

Bootstrap Iteration

Figure 3: Bootstrap Chow Test Results

the post-GFC sample to determine whether there are differences in the estimated fiscal multipliers in the most recent period.

5.1.1 Post GFC Shocks

Figures 3 and 4 compare the IRFs under the restricted model and unrestricted model (post GFC). Only the point estimates are reported, given the reduced sample size while keeping the number of model parameters fixed, we expect greater uncertainty in the IRF estimates, reflected in the confidence intervals. Consequently, we do not expect any of the previously insignificant results to change. 6

We see little difference in IRFs between the restricted and unrestricted models. While for revenue there is a noticeable discrepancy between the models after a year, with a factor of over 3, by 10 quarters this gap has closed. Additionally, the instantaneous response is essentially the same.

For expenditure, the post GFC IRF follows a similar path to the total period,

⁶Along with the IRFs for all of the variables, the confidence intervals for the post GFC specification can be seen in the appendix. It should be noted that the confidence intervals under this specification show noticeable asymmetry. Efron (1981) highlights that this is expected in small samples. This thus supports the use of the restricted model in order to obtain more meaningful estimates which we can test for significance.

IRF: Revenue Response to Expenditure Shock

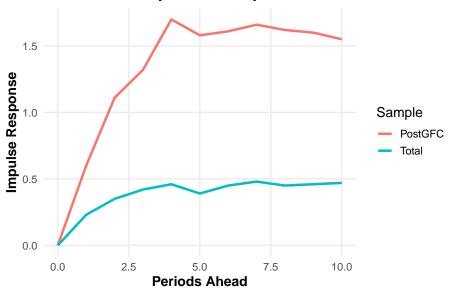


Figure 4: GDP Responses to Government Revenue Compared

IRF: Expenditure Response to Revenue Shock

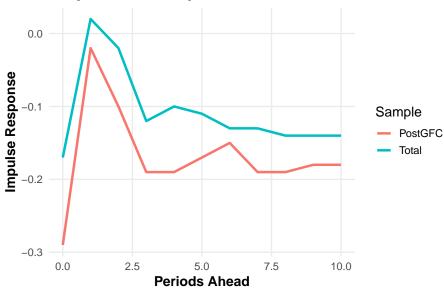


Figure 5: GDP Responses to Government Compared

despite overall reporting lower point estimates by approximately 0.5. Nevertheless, the results for the restricted model are contained within the confidence intervals for both expenditure and revenue. Thus this does not negate this paper's results.

5.2 Lag length

When defining the empirical specification, we highlighted that the lag order was chosen a priori, and that information criteria suggested a lower order lag was compatible with the data. Therefore, here we estimate the model on a single lag (consistent with 2 lags in the levels VAR). Given the evidence of parameter instability, this is reported for both the full sample and the post GFC data. Figures 5 and 6 report the IRFs for government expenditure and revenue respectively across all of the specifications used for robustness testing.

IRF: Revenue Response to Revenue Shock 1.5 Impulse Response Sample 1.0 PostGFC PostGFC_1_lag Total Total_1_lag 0.5 0.0 2.5 5.0 7.5 10.0 **Periods Ahead**

Figure 6: GDP Responses to Government Revenue Compared 2

consider reduced lag length (improved efficiency/ parsimony)

6 Discussion/ Policy Implications

This analysis has found fiscal multipliers that are practically and statistically insignificant

0.0 Impulse Response Sample -0.1 PostGFC PostGFC_1_lag Total -0.2 Total_1_lag -0.30.0 2.5 5.0 7.5 10.0 **Periods Ahead**

RF: Expenditure Response to Expenditure Shock

Figure 7: GDP Responses to Government Compared 2

suggests that there is scope to reduce the government deficit through more aggressive fiscal consolidation measures and thus mitigate against the growing costs of the large deficit.

Results for revenue, baseline model suggests that positive shocks to government revenue growth lead to increased GDP growth. This result is also statistically significant. We note, however, that this result is not robust to our specification checks. Nevertheless, we discuss the implications of such a finding if true.

This result is counter intuitive: the primary components of the government revenue variable used by this analysis are taxes, which would be expected to decrease output. Nevertheless, we consider some explanations.

This analysis has considered the government's revenue as opposed to the tax rate, it is possible that the results of a positive multiplier for government revenue are showing the effects of the Laffer curve: by reducing tax rates economic activity is encouraged in turn leading to greater tax receipts.

Alternatively, this paper has used a linear VAR model, meaning that results are symmetric. Consequently, the baseline result of the output multiplier for government revenue suggests that a negative shock to government revenue leads to a reduction in output. This could be the case due to the decreased competitiveness of UK tax rates, meaning that FDI is discouraged ...

This also highlights limitations of previous SVAR analyses of fiscal multipliers.

B+P, ... use data net taxes which the government does not have full control over. Instead the government controls tax rates and tax legislation. While these would be expected to be positively correlated with government revenue this is not necessarily the case.

cf with research and theory

Lucas critique/ extrapolating.

6.1 Limitations

- potential heterogeneity within expedniture/ revenue
- debt sustainability (effects of policy on inflation and interest rate, changing real cost)

7 Conclusion

This paper has employed a SVAR analysis of fiscal multipliers using a 6-dimensional VAR with quarterly data. We use recursive short run restrictions leveraging economic theory to determine the transmission of shocks across the VAR model thus identifying the structural parameters. We find a negligible and insignificant multiplier effect of government expenditure. For government revenue we report a positive multiplier with a 68% bootstrap confidence interval excluding 0. We perform tests for misspecification to assess the robustness of these results. Across these specifications we find similar, negligible results for the multiplier of government spending. We show, however, that the IRF for government revenue varies across these alternative specifications. We discuss the policy implications of these results. The low reported multipliers for government expenditure suggest scope for the UK government to reduce its spending to improve its fiscal position, without counterproductive effects through a hysterisis effect.

Summary of methodology, this research's results, contributions, and future implications.

8 Bibliography

Alesina, A. and Ardagna, S., 1998. Tales of fiscal adjustment. Economic policy, 13(27), pp.488-545.

Cheung, Y.W. and Lai, K.S., 1993. FINITE-SAMPLE SIZES OF JOHANSEN'S LIKELIHOOD RATIC) TESTS FOR. Oxford Bulletin of Economics and statistics, 55(3), p.1025.

Efron, B., 1981. Nonparametric standard errors and confidence intervals. canadian Journal of Statistics, 9(2), pp.139-158.

Efron, B., 1992. Bootstrap methods: another look at the jackknife. In Breakthroughs in statistics: Methodology and distribution (pp. 569-593). New York, NY: Springer New York.

Efron, B. and Tibshirani, R., 1986. Bootstrap methods for standard errors, confidence intervals, and other measures of statistical accuracy. Statistical science, pp.54-75.

Lüutkepohl and Candelon (2000) https://www.econstor.eu/bitstream/10419/62173/1/723877181.pdf

Lüutkepohl, H., Saikkonen, P. and Trenkler, C., 2001. Maximum eigenvalue versus trace tests for the cointegrating rank of a VAR process. The Econometrics Journal, 4(2), pp.287-310.

Lynch, B. and Whitaker, S., 2004. The new sterling ERI. Bank of England Quarterly Bulletin, Winter. Maddala, G.S. and Kim, I.M., 1998. Unit roots, cointegration, and structural change.

Martin, V., Hurn, S. and Harris, D., 2013. Econometric modelling with time series: specification, estimation and testing. Cambridge University Press.

European system of accounts - ESA 2010 (2013). Available at: https://ec.europa.eu/eurostat/documents/3859598/5925693/KS-02-13-269-EN. PDF.pdf/44cd9d01-bc64-40e5-bd40-d17df0c69334?t=1414781932000 (Accessed: 11 August 2025).

Office for National Statistics (2023) Public sector finances QMI, Public sector finances QMI - Office for National Statistics. Available at: https://www.ons.gov.uk/economy/governmentpublicsectorandtaxes/publicsectorfinance/methodologies/publicsectorfinancesandgovernmentdeficitanddebtunderthemaastrichttreatyqmi (Accessed: 12 August 2025).

UK government debt and deficit: December 2023 (2024) UK government debt and deficit - Office for National Statistics. Available at: https://www.ons.gov.uk/economy/governmentpublicsectorandtaxes/publicspending/bulletins/ukgovernmentdebtanddeficitforeurostatmaast/december2023 (Accessed: 11 August 2025).

9 Data Appendix

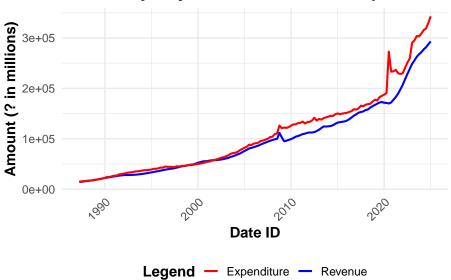
9.1 Data Sources

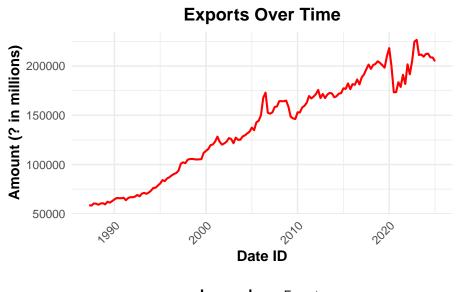
• Fiscal Variables (not seasonally adjusted): https://www.ons.gov.uk/economy/governmentpublicsectorandtaxes/ publicspending/datasets/esatable25quarterlynonfinancialaccountsofgeneralgovernment

- UK ERI (XUQAB82): https://www.bankofengland.co.uk/boeapps/database/fromshowcolumns.asp?Travel=NIxIRxSUx&FromSeries=
 1&ToSeries=50&DAT=RNG&FD=1&FM=Jan&FY=1987&TD=
 12&TM=Aug&TY=2025&FNY=&CSVF=TT&html.x=160&html.y=
 25&C=IIY&Filter=N
- LFS (Pop aged 16-64): https://www.ons.gov.uk/employmentandlabourmarket/peopleinwork/employmentandemployeetypes/timeseries/lf2o/lms
- GDP (SA) and defaltor rate: https://www.ons.gov.uk/economy/grossdomesticproductgdp/datasets/ secondestimateofgdp/current https://www.ons.gov.uk/economy/ grossdomesticproductgdp/bulletins/quarterlynationalaccounts/latest# data-on-gdp-quarterly-national-accounts
- interest rate (SR. This is dates of changes to the policy rate. Have interpolated to get quarterly data): https://www.bankofengland.co.uk/monetary-policy/the-interest-rate-bank-rate
- 3 month interest rate: https://fred.stlouisfed.org/series/IR3TIB01GBM156N

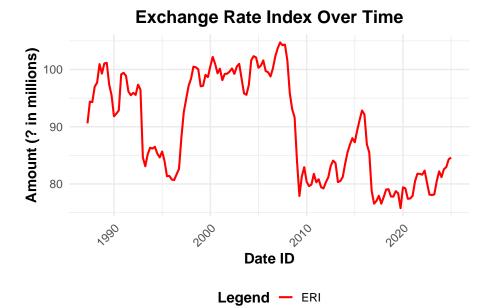
9.2 Data Plots

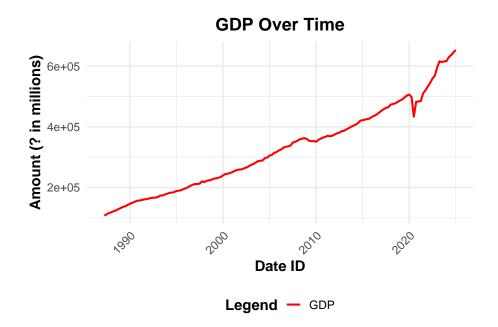
Seasonally Adjusted Revenue and Expenditure

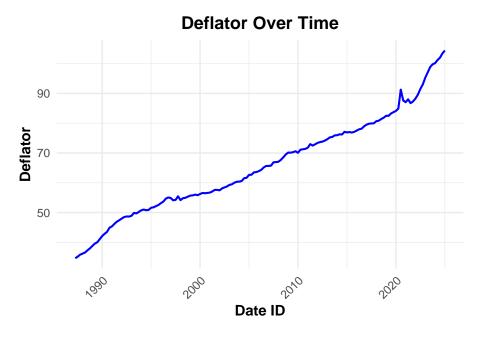


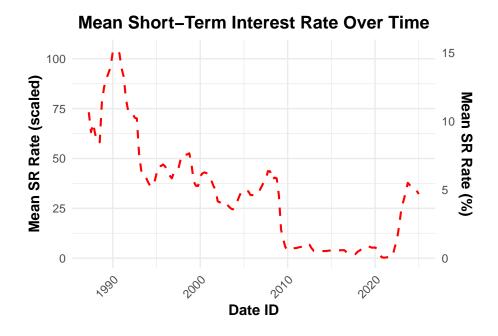












10 Technical Appendix

10.1 VECM Code/ Results

```
##
## #######################
## # Johansen-Procedure #
## #####################
##
## Test type: maximal eigenvalue statistic (lambda max) , with linear trend
##
## Eigenvalues (lambda):
## [1] 0.223775041 0.148961017 0.132547213 0.101343573 0.047927870 0.006444002
##
## Values of teststatistic and critical values of test:
##
             test 10pct 5pct 1pct
##
## r <= 5 |
            0.96 6.50 8.18 11.65
            7.27 12.91 14.90 19.19
## r <= 3 | 15.81 18.90 21.07 25.75
## r <= 2 | 21.04 24.78 27.14 32.14
## r <= 1 | 23.87 30.84 33.32 38.78
## r = 0 | 37.49 | 36.25 | 39.43 | 44.59
```

```
##
## Eigenvectors, normalised to first column:
## (These are the cointegration relations)
##
##
                     log_expenditure.14 mean_SR_Rate.14 log_GDP.14 log_ERI.14
## log_expenditure.14
                              1.0000000
                                             1.000000
                                                        1.0000000 1.00000000
## mean_SR_Rate.14
                              0.1399019
                                             -0.086652 -0.1342240 0.01130355
## log_GDP.14
                                             14.252968 -21.6508463
                             -1.6372129
                                                                    1.58886736
## log_ERI.14
                             -3.9104441
                                             -4.452473
                                                         1.2428321 0.24705510
## log_revenue.14
                              3.0289815
                                             -6.569448 11.2728422 -2.02020864
## log_deflator.14
                             -8.9568521
                                             -9.501705 -0.4121129 0.36227536
##
                     log_revenue.14 log_deflator.14
## log_expenditure.14
                         1.00000000
                                        1.00000000
## mean SR Rate.14
                         0.00444857
                                        0.06014314
## log_GDP.14
                         0.80885702
                                       -5.24585863
## log_ERI.14
                         0.52891404
                                        1.96572040
## log_revenue.14
                        -0.44725310
                                        2.65492223
## log_deflator.14
                        -3.14947822
                                        1.13681500
##
## Weights W:
## (This is the loading matrix)
##
##
                    log_expenditure.14 mean_SR_Rate.14
                                                        log_GDP.14
                                                                     log_ERI.14
## log_expenditure.d
                          0.0047967452 -0.0054772892 -0.028089191 -0.073475961
## mean_SR_Rate.d
                         -0.1772598340
                                         ## log GDP.d
                         0.0073306038
                                        -0.0024839456 0.015066099 0.006043253
## log_ERI.d
                          0.0029490912
                                         ## log_revenue.d
                         -0.0009800666
                                        -0.0008773181 0.002743109 0.039358013
                                         0.0006335918 -0.005195139 -0.013813306
## log_deflator.d
                          0.0110157092
##
                    log_revenue.14 log_deflator.14
## log_expenditure.d
                       0.018733098
                                    -0.0024684460
## mean_SR_Rate.d
                                    -0.0379795002
                       0.229845055
## log GDP.d
                      -0.001697832
                                    -0.0006081400
## log_ERI.d
                      -0.046115309
                                    -0.0018023379
## log_revenue.d
                       0.010392965
                                     -0.0022157030
## log_deflator.d
                       0.006882167
                                    -0.0004199145
##
## ######################
## # Johansen-Procedure #
## #####################
##
## Test type: trace statistic , with linear trend
##
## Eigenvalues (lambda):
## [1] 0.223775041 0.148961017 0.132547213 0.101343573 0.047927870 0.006444002
```

```
##
## Values of teststatistic and critical values of test:
##
##
              test 10pct 5pct
                                  1pct
## r <= 5 |
              0.96 6.50 8.18
                                 11.65
## r <= 4 |
              8.23 15.66 17.95
                                 23.52
## r <= 3 |
             24.04 28.71 31.52
                                 37.22
## r <= 2 |
             45.08 45.23 48.28
                                 55.43
             68.96 66.49 70.60
  r <= 1 |
                                78.87
## r = 0 | 106.45 85.18 90.39 104.20
## Eigenvectors, normalised to first column:
  (These are the cointegration relations)
##
##
##
                      log_expenditure.14 mean_SR_Rate.14
                                                            log_GDP.14
                                                                        log_ERI.14
## log_expenditure.14
                                1.0000000
                                                 1.000000
                                                             1.0000000
                                                                        1.00000000
                                                 -0.086652
## mean_SR_Rate.14
                                0.1399019
                                                            -0.1342240
                                                                        0.01130355
## log_GDP.14
                               -1.6372129
                                                 14.252968 -21.6508463
                                                                        1.58886736
## log_ERI.14
                               -3.9104441
                                                 -4.452473
                                                             1.2428321
                                                                        0.24705510
## log_revenue.14
                                3.0289815
                                                 -6.569448
                                                            11.2728422
                                                                       -2.02020864
## log_deflator.14
                                                -9.501705
                                                            -0.4121129
                                                                        0.36227536
                               -8.9568521
##
                       log_revenue.14 log_deflator.14
## log_expenditure.14
                           1.0000000
                                           1.00000000
## mean_SR_Rate.14
                           0.00444857
                                           0.06014314
## log_GDP.14
                           0.80885702
                                          -5.24585863
## log ERI.14
                           0.52891404
                                           1.96572040
## log_revenue.14
                                           2.65492223
                          -0.44725310
## log_deflator.14
                          -3.14947822
                                           1.13681500
##
## Weights W:
  (This is the loading matrix)
##
##
                     log expenditure.14 mean SR Rate.14
                                                            log GDP.14
                                                                         log ERI.14
## log_expenditure.d
                            0.0047967452
                                           -0.0054772892 -0.028089191 -0.073475961
## mean_SR_Rate.d
                           -0.1772598340
                                            0.2416398994
                                                           0.147719794 -0.828265541
## log_GDP.d
                            0.0073306038
                                           -0.0024839456
                                                           0.015066099
                                                                       0.006043253
## log_ERI.d
                            0.0029490912
                                            0.0057350350
                                                           0.003703400 -0.009018534
## log_revenue.d
                           -0.0009800666
                                                           0.002743109 0.039358013
                                           -0.0008773181
## log_deflator.d
                                            0.0006335918 -0.005195139 -0.013813306
                            0.0110157092
##
                     log_revenue.14 log_deflator.14
## log_expenditure.d
                         0.018733098
                                       -0.0024684460
## mean_SR_Rate.d
                         0.229845055
                                       -0.0379795002
## log GDP.d
                                       -0.0006081400
                        -0.001697832
## log ERI.d
                        -0.046115309
                                       -0.0018023379
## log revenue.d
                         0.010392965
                                       -0.0022157030
## log_deflator.d
                                       -0.0004199145
                         0.006882167
```

```
##
## Coefficient matrix of lagged endogenous variables:
##
## A1:
##
                  log_expenditure.l1 mean_SR_Rate.l1 log_GDP.l1
                                                                  log_ERI.11
## log_expenditure
                          0.38531282
                                        0.012214223 -0.07485611 -0.350217642
## mean_SR_Rate
                         -3.64648776
                                        1.346457575 0.01023456
                                                                 3.474450122
## log_GDP
                                        0.19150858
## log ERI
                         -0.12406325
                                        0.001947887 -0.04507162 1.341595487
## log_revenue
                         -0.10912814
                                        0.006487342 0.11099434 0.001508656
## log_deflator
                         -0.04193098
                                        0.002100529 0.02058047 -0.123903384
##
                  log_revenue.l1 log_deflator.l1
                      0.08207905
                                      1.1988937
## log_expenditure
## mean SR Rate
                      5.34472966
                                     14.9963202
## log_GDP
                      0.19525698
                                      -0.4453185
## log_ERI
                     -0.12246357
                                      0.2567574
## log_revenue
                      1.20162769
                                      0.3667373
## log_deflator
                      0.12128938
                                       0.8406520
##
##
## A2:
                  log_expenditure.12 mean_SR_Rate.12 log_GDP.12 log_ERI.12
##
                          0.62548072
                                      -0.0135873461   0.4563158   0.58722001
## log_expenditure
## mean_SR_Rate
                          3.72623492
                                       -0.2168886410
                                                     3.0867714 -5.46064222
## log_GDP
                         -0.05273096
                                      ## log ERI
                          0.17043336
                                       ## log_revenue
                          0.13234130
                                       -0.0102628952 0.1936387 -0.02455291
## log deflator
                          0.09711999
                                       -0.0006806192 0.1359922 0.16612697
##
                  log_revenue.12 log_deflator.12
                     -0.47636697
                                   -0.905649582
## log_expenditure
## mean SR Rate
                     -9.47275266
                                   -13.079216483
## log_GDP
                     -0.05544829
                                     0.009371408
## log ERI
                     -0.16299038
                                   -0.198278817
## log_revenue
                     -0.42153848
                                   -0.096434762
## log_deflator
                     -0.23169156
                                   -0.089113371
##
##
## A3:
                  log_expenditure.13 mean_SR_Rate.13
                                                      log_GDP.13 log_ERI.13
##
## log_expenditure
                          0.10946997
                                       0.0003953033 -0.057742250 -0.4036346
## mean_SR_Rate
                         -2.39938366
                                       -0.3025523636 -8.964458413
                                                                 4.6440206
## log_GDP
                         -0.14536990
                                       -0.0017108435 0.005044322
                                                                 0.3237275
## log ERI
                         -0.10948543
                                       0.0027312059 -0.510150013
                                                                 0.1055626
## log_revenue
                         -0.07400225
                                       0.0017995895 -0.315784173 0.2119920
## log deflator
                         -0.04670461
                                      -0.0005731131 -0.127689963 -0.1028479
##
                  log_revenue.13 log_deflator.13
```

```
## log_expenditure
                      0.38609811
                                     -0.2269351
## mean_SR_Rate
                                     -4.0719559
                     12.52562982
## log_GDP
                     -0.00957344
                                      0.2346258
## log_ERI
                      0.69670727
                                     -0.1485099
## log_revenue
                      0.34260426
                                     -0.2252602
## log_deflator
                                      0.2094009
                      0.21272266
##
##
## A4:
##
                  log_expenditure.14 mean_SR_Rate.14 log_GDP.14 log_ERI.14
                                       0.0016488938 -0.33157074 0.14787487
## log_expenditure
                        -0.115466769
## mean_SR_Rate
                         2.142376671
                                       0.1481844448 6.15766450 -1.96466378
## log_GDP
                         0.013922881
                                       0.0041647824 -0.02538161 -0.20776510
## log ERI
                         0.066064424
                                       ## log_revenue
                         0.049809023
                                       0.0006943216 -0.04691777 0.01754804
## log_deflator
                         0.002531306
##
                  log_revenue.14 log_deflator.14
## log_expenditure
                      0.02271906
                                     -0.10927276
## mean_SR_Rate
                     -8.93452357
                                     3.74254231
## log_GDP
                     -0.10803099
                                     0.13566214
## log_ERI
                     -0.40232057
                                     0.06361669
## log_revenue
                     -0.12566207
                                     -0.03626412
                     -0.06895411
                                    -0.05960561
## log_deflator
##
##
## Coefficient matrix of deterministic regressor(s).
##
##
                      constant
## log_expenditure 0.001270622
## mean_SR_Rate
                   0.468880597
## log_GDP
                  -0.020712010
## log_ERI
                  -0.010088857
## log_revenue
                   0.014421514
## log_deflator
                  -0.033904832
## [1] "varest"
## [1] "vec2var"
```

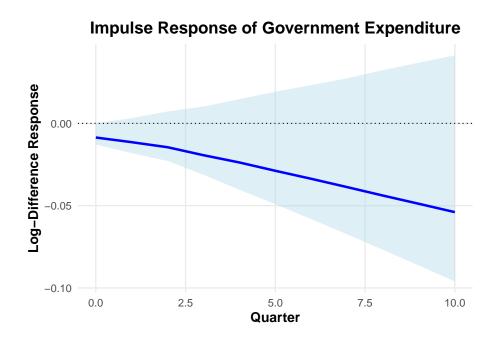


Figure 8: Impulse Response Function of GDP Following a Shock to Expenditure

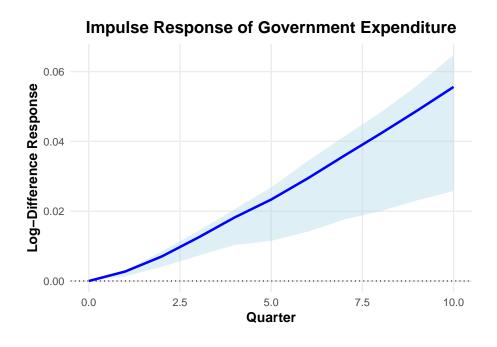
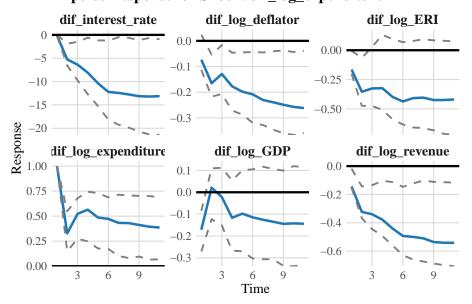


Figure 9: Impulse Response Function of GDP Following a Shock to Expenditure

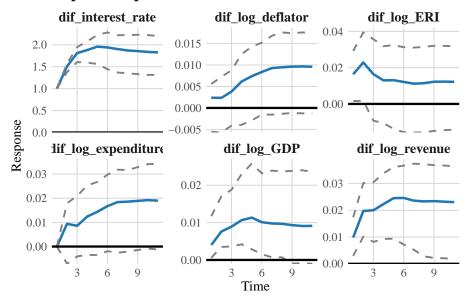
10.2 IRFs

10.2.1 Total Period:

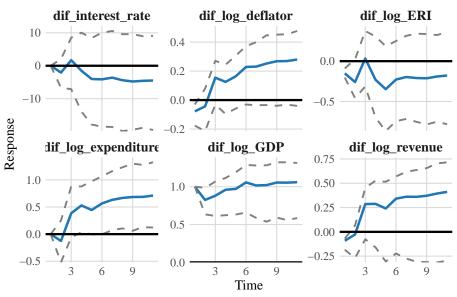
Impulse Response for Shock: dif_log_expenditure



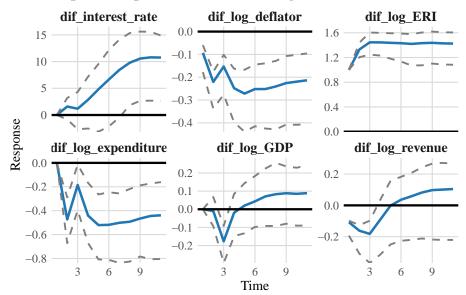
Impulse Response for Shock: dif_interest_rate



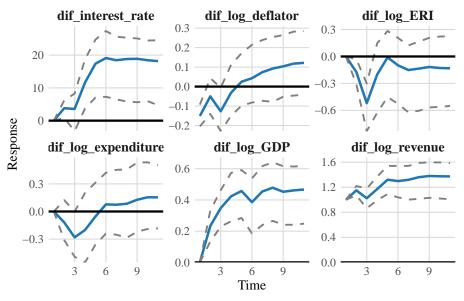
Impulse Response for Shock: dif_log_GDP



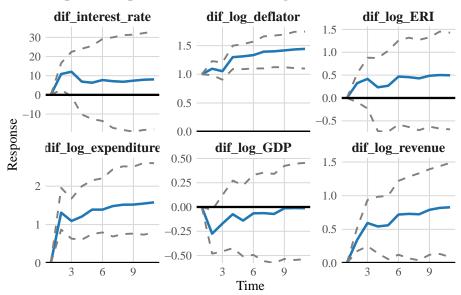
Impulse Response for Shock: dif_log_ERI

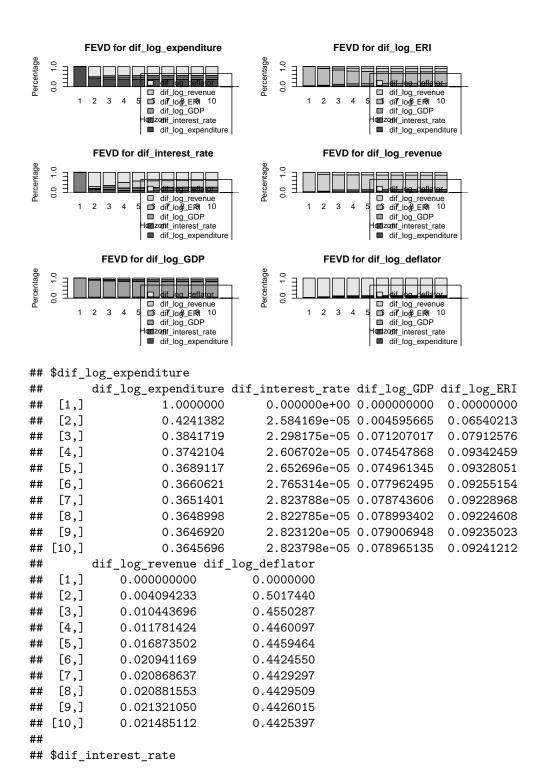


Impulse Response for Shock: dif_log_revenue



Impulse Response for Shock: dif_log_deflator





```
##
         dif_log_expenditure dif_interest_rate dif_log_GDP dif_log_ERI
##
    [1,]
                   0.01295712
                                     0.987042881
                                                   0.00000000
                                                                0.0000000
    [2,]
##
                   0.15872242
                                     0.007513009
                                                   0.02557416
                                                                 0.01508075
##
    [3,]
                   0.15053892
                                     0.007314123
                                                   0.09982501
                                                                 0.01460092
##
    [4,]
                   0.10522773
                                     0.004626601
                                                   0.09790205
                                                                 0.01883297
    [5,]
##
                   0.10537625
                                     0.003986212
                                                   0.10252806
                                                                0.02741493
##
    [6,]
                   0.11156512
                                     0.003855266
                                                   0.09916550
                                                                 0.03609087
    [7,]
##
                   0.11035403
                                     0.003812776
                                                   0.09873004
                                                                 0.04455193
##
    [8,]
                   0.10980644
                                     0.003786408
                                                   0.09965953
                                                                 0.04925528
##
    [9,]
                                                   0.09973430
                   0.10981910
                                     0.003774134
                                                                 0.05079058
                   0.10967549
                                     0.003769568
##
   [10,]
                                                   0.09969765
                                                                0.05085878
##
         dif_log_revenue dif_log_deflator
##
    [1,]
               0.0000000
                                  0.0000000
    [2,]
##
               0.08614565
                                  0.7069640
##
    [3,]
               0.07846588
                                  0.6492552
##
    [4,]
               0.27339378
                                  0.5000169
##
    [5,]
               0.33083548
                                  0.4298591
##
    [6,]
               0.32821044
                                  0.4211128
    [7,]
##
               0.32550775
                                  0.4170435
##
    [8,]
               0.32340336
                                  0.4140890
##
    [9,]
                                  0.4135668
               0.32231504
##
   [10,]
               0.32233895
                                  0.4136596
##
##
   $dif_log_GDP
##
         dif_log_expenditure dif_interest_rate dif_log_GDP dif_log_ERI
##
    [1,]
                   0.02852921
                                    1.562689e-05
                                                     0.9714552 0.000000e+00
    [2,]
##
                   0.05416376
                                    2.371797e-05
                                                     0.8399106 7.968721e-05
    [3,]
##
                   0.05323634
                                    2.396890e-05
                                                     0.8051225 2.172946e-02
##
    [4,]
                                                     0.7765984 3.948014e-02
                   0.05774933
                                    2.523407e-05
##
    [5,]
                   0.05770263
                                    2.543993e-05
                                                     0.7724078 4.037279e-02
##
    [6,]
                   0.05711499
                                    2.616704e-05
                                                     0.7670845 4.021572e-02
##
    [7,]
                                    2.611784e-05
                                                     0.7642307 4.054378e-02
                   0.05690188
##
    [8,]
                   0.05692589
                                    2.610692e-05
                                                     0.7637394 4.062629e-02
##
    [9,]
                   0.05677358
                                    2.609505e-05
                                                     0.7615980 4.048919e-02
##
   [10,]
                   0.05677328
                                    2.613248e-05
                                                     0.7615425 4.049423e-02
##
         dif_log_revenue dif_log_deflator
##
    [1,]
               0.0000000
                                 0.0000000
    [2,]
##
               0.04418904
                                 0.06163317
    [3,]
##
               0.05251867
                                 0.06736908
##
    [4,]
               0.05463680
                                 0.07151010
    [5,]
##
               0.05518527
                                 0.07430606
##
    [6,]
               0.05818579
                                 0.07737286
    [7,]
##
               0.06132794
                                 0.07696955
##
    [8,]
               0.06170792
                                 0.07697436
    [9,]
##
               0.06196214
                                 0.07915095
## [10,]
                                 0.07914995
               0.06201387
```

```
##
   $dif_log_ERI
##
##
         dif_log_expenditure dif_interest_rate dif_log_GDP dif_log_ERI
##
    [1,]
                   0.02563265
                                     0.0002551649
                                                    0.02177229
                                                                  0.9523399
##
    [2,]
                   0.04697018
                                     0.0002311286
                                                    0.02559357
                                                                  0.8260205
    [3,]
##
                   0.04066813
                                     0.0002240027
                                                    0.07598216
                                                                  0.7147571
##
    [4,]
                   0.03597799
                                     0.0002048213
                                                    0.10631817
                                                                  0.6322854
##
    [5,]
                                                                  0.6127912
                   0.03789535
                                     0.0001985038
                                                    0.11049552
    [6,]
                                     0.0001922970
##
                   0.03741253
                                                    0.11429108
                                                                  0.5921642
##
    [7,]
                   0.03774452
                                     0.0001922896
                                                                  0.5907098
                                                    0.11451739
                   0.03772802
                                     0.0001921941
##
    [8,]
                                                    0.11452376
                                                                  0.5903929
    [9,]
##
                   0.03787352
                                     0.0001921419
                                                    0.11428433
                                                                  0.5891487
##
   [10,]
                   0.03785549
                                     0.0001920510
                                                    0.11447713
                                                                  0.5889067
##
         dif log revenue dif log deflator
##
    [1,]
               0.0000000
                                 0.00000000
    [2,]
##
               0.02234413
                                 0.07884052
##
    [3,]
               0.09556630
                                 0.07280233
##
    [4,]
               0.14185143
                                 0.08336220
    [5,]
##
               0.15722504
                                 0.08139436
##
    [6,]
               0.15602029
                                 0.09991962
##
    [7,]
               0.15709038
                                 0.09974566
##
    [8,]
               0.15712932
                                 0.10003382
    [9,]
##
               0.15696131
                                 0.10154003
   [10,]
##
               0.15695269
                                 0.10161593
##
##
   $dif log revenue
##
         dif_log_expenditure dif_interest_rate dif_log_GDP dif_log_ERI
                                     9.285997e-05 0.008055805
##
    [1,]
                   0.01979456
                                                                 0.01118480
##
    [2,]
                   0.04329383
                                     1.593855e-04 0.010257487
                                                                 0.01191389
##
    [3,]
                   0.03801398
                                     1.392641e-04 0.079022747
                                                                 0.01070097
##
    [4,]
                   0.03812603
                                     1.396687e-04 0.077158228
                                                                 0.01615676
##
    [5,]
                                     1.394889e-04 0.076766605
                                                                 0.02128555
                   0.03987554
##
    [6,]
                   0.04059445
                                     1.357819e-04 0.081490009
                                                                 0.02164912
##
    [7,]
                   0.04058601
                                     1.363316e-04 0.081681777
                                                                 0.02195467
##
    [8,]
                   0.04059161
                                     1.361590e-04 0.081549546
                                                                 0.02229012
##
    [9,]
                                     1.356432e-04 0.081317960
                                                                 0.02236574
                   0.04087831
##
   [10,]
                   0.04085937
                                     1.355464e-04 0.081583277
                                                                 0.02235295
##
         dif_log_revenue dif_log_deflator
##
    [1,]
                0.9608720
                                 0.0000000
    [2,]
##
                0.8374775
                                 0.09689795
    [3,]
##
                0.7428712
                                 0.12925184
##
    [4,]
                0.7404136
                                 0.12800572
    [5,]
##
                0.7369278
                                 0.12500497
##
    [6,]
                0.7176326
                                 0.13849805
##
    [7,]
                0.7172106
                                 0.13843061
##
    [8,]
                                 0.13822949
                0.7172031
```

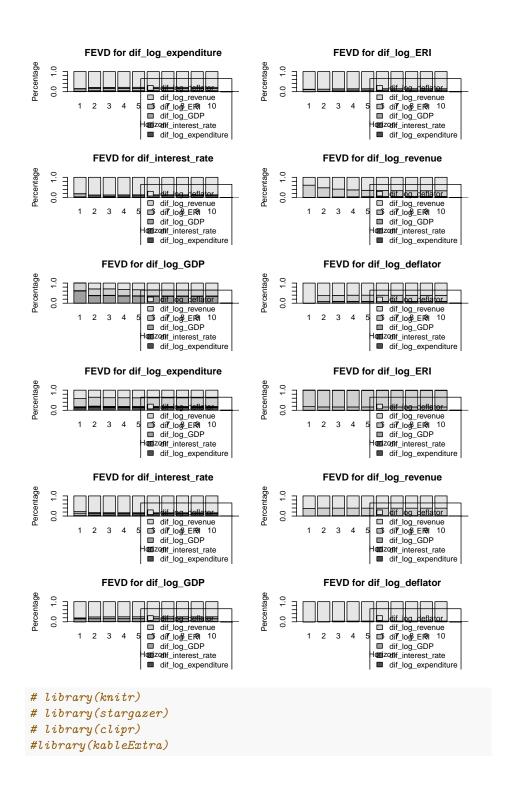
```
[9,]
                0.7146949
                                 0.14060742
                                 0.14100862
## [10,]
                0.7140602
##
##
   $dif_log_deflator
##
         dif_log_expenditure dif_interest_rate dif_log_GDP dif_log_ERI
                                    5.403780e-06 0.005798764 0.008315223
##
    [1,]
                  0.005163587
    [2,]
                  0.012646828
                                    5.179099e-06 0.006636881 0.022927088
##
##
    [3,]
                  0.013183628
                                    6.791875e-06 0.040770104 0.025870212
    [4,]
                  0.014197034
                                    1.087107e-05 0.038747609 0.031562725
##
##
    [5,]
                  0.014479879
                                    1.203351e-05 0.039773178 0.031865042
                                    1.278930e-05 0.042946264 0.032047003
##
    [6,]
                  0.014502968
    [7,]
                                    1.339571e-05 0.042776901 0.031916408
##
                  0.014834188
##
    [8,]
                  0.014886849
                                    1.341089e-05 0.043101214 0.031992357
##
    [9,]
                                    1.342022e-05 0.043267094 0.032146164
                  0.014950009
## [10,]
                  0.014999050
                                    1.341522e-05 0.043247547 0.032161896
##
         dif_log_revenue dif_log_deflator
                                  0.9588518
##
    [1,]
              0.02186523
    [2,]
##
              0.03029032
                                  0.9274937
    [3,]
##
              0.03404133
                                  0.8861279
##
    [4,]
              0.03925235
                                  0.8762294
##
    [5,]
              0.04162234
                                  0.8722475
##
    [6,]
              0.04170878
                                  0.8687822
    [7,]
##
              0.04231152
                                  0.8681476
##
    [8,]
              0.04255619
                                  0.8674500
##
    [9,]
              0.04262875
                                  0.8669946
## [10,]
              0.04276215
                                  0.8668159
```

10.3 FEVDs post GFC:

Table 1: Mean Values of Differenced Variables

Variable	Mean
dif_log_expenditure	0.02082
$dif_interest_rate$	-0.03960
$\operatorname{dif} = \log = \operatorname{ERI}$	-0.00045
$\operatorname{dif}_{\log}\operatorname{GDP}$	0.01196
dif_log_revenue	0.02009
$\operatorname{dif}_{\log_{\operatorname{deflator}}}$	0.00730

```
## [1] 0.6603505 0.6285920 0.3660225 0.2515222 0.2224670 0.2224670
## [1] 0.6765157 0.3713074 0.3394222 0.3394222 0.1048281 0.1048281
```



```
library(ggplot2)
library(knitr)
library(ivreg)
library(ggdag)
library(data.table)
library(dplyr)
library(tidyr)
library(stargazer)
library(clipr)
library(tibble)
library(lubridate)
library(boot)
library(seasonal)
lapply(c("ggplot2", "dplyr", "data.table", "lubridate", "janitor", "broom", "tibble", "tidy:
       require, character.only = TRUE)
# knitr::opts_chunk$set(echo = FALSE)
knitr::opts_chunk$set(echo = FALSE, warning = FALSE, message = FALSE)
df <- fread("D:/Samid work/University/KCL - Econ and Policy/Dissertation/Data/GDP Real.csv"</pre>
# Filter the data frame to exclude rows where the column 'title' matches any of the specifi
filtered_df <- df %>%
  # Keep only the quarterly data
 filter(nchar(CDID) == 7 & substr(CDID, 6, 6) == "Q") %>%
  # Select relevant columns and rename them
 dplyr::select(CDID, Deflator = L8GG, GDP = CAGQ) %>%
  # dplyr::select(CDID, Deflator = L8GG, GDP = ABMI) %>%
  # Create new columns and convert types
 mutate(
    Year = as.numeric(substr(CDID, 1, 4)),
    Quarter = substr(CDID, 6, 7),
    Q = as.numeric(substr(CDID, 7, 7)),
   Deflator = as.numeric(Deflator),
    GDP = as.numeric(GDP)
 ) %>%
```

```
# Filter by year (can modify for testing)
  filter(Year >= 1987)
# fiscal_raw <- fread("D:/Samid work/University/KCL - Econ and Policy/Dissertation/Data/Fis
fiscal_raw <- fread("D:/Samid work/University/KCL - Econ and Policy/Dissertation/Data/Fiscal
fiscal_proc <- fiscal_raw %>%
  dplyr::select(Date_ID = Identifier, Revenue = Revenue, Expenditure = Expenditure) %>%
 mutate(Year = as.numeric(gsub("\\D", "", Date_ID)),
        Period = gsub("\\d{4}", "", Date_ID)) %>%
 mutate(
   Q = case_when(
     Period == "Jan to Mar " ~ 1,
     Period == "Apr to Jun " ~ 2,
     Period == "Jul to Sep " ~ 3,
     Period == "Oct to Dec " ~ 4
     ),
    Unique_Period = Year +(Q/4)
  # Convert to numeric and multiply by 1 million so values as these will later be made into
  mutate(Revenue = as.numeric(gsub(",", "", Revenue) ),
         Expenditure = as.numeric(gsub(",", "", Expenditure )))
# fiscal_proc <- fiscal_raw %>%
    dplyr::select(Date_ID = Transaction, Revenue = OTR, Expenditure = OTE) %>%
   subset(Date_ID != "Dataset identifier code" & Date_ID != "Identifier") %>%
   mutate(Year = as.numeric(gsub("\D", "", Date_ID)),
           Period = gsub("\d{4}", "", Date_ID))  %>%
#
#
   mutate(
     Q = case when(
#
       Period == "Jan to Mar " ~ 1,
       Period == "Apr to Jun " ~ 2,
#
#
       Period == "Jul to Sep " ~ 3,
       Period == "Oct to Dec " ~ 4
      Unique\_Period = Year + (Q/4)
#
   # Convert to numeric and multiply by 1 million so values as these will later be made in
   mutate(Revenue = as.numeric(gsub(",", "", Revenue) ),
#
           Expenditure = as.numeric(qsub(",", "", Expenditure )))
```

```
# join GDP deflator and GDP data
population <- fread("D:/Samid work/University/KCL - Econ and Policy/Dissertation/Data/Population - Fread("D:/Samid work/University/KCL - Econ and Policy/Dissertation/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/Data/Population/D
                                                     skip = 4,
                                                    header = TRUE) %>%
     subset(`Country Name` == "United Kingdom") %>%
    t() %>%
     as.data.frame() %>%
    rownames_to_column(var = "Year") %>%
    rename(Population = V1 ) %>%
    filter(grepl("^\\d{4}$", Year)) %>%
    mutate(Year = as.numeric(Year),
                       Population = as.numeric(Population))
Interest_SR <- fread("D:/Samid work/University/KCL - Econ and Policy/Dissertation/Data/3 mon</pre>
    mutate(Date = dmy(Date),
                       month = month(Date),
                       Year = year(Date),
                        Q = case_when(
                             month %in% 1:3 ~ 1,
                             month %in% 4:6 ~ 2,
                             month %in% 7:9 ~ 3,
                             month %in% 10:12 ~ 4
                       )) %>%
     group_by(Year, Q) %>%
     summarize(mean_SR_Rate = mean(Rate, na.rm = TRUE))
SONIA <- fread("D:/Samid work/University/KCL - Econ and Policy/Dissertation/Data/Bank of Eng
     mutate(Date = dmy(Date),
                       month = month(Date),
                       Year = year(Date),
                       Q = case_when(
                             month %in% 1:3 ~ 1,
                             month %in% 4:6 ~ 2,
                             month %in% 7:9 ~ 3,
                             month %in% 10:12 ~ 4
                       )) %>%
     group_by(Year, Q) %>%
     summarize(mean_SONIA = mean(SONIA, na.rm = TRUE))
Policy_Rate <- fread("D:/Samid work/University/KCL - Econ and Policy/Dissertation/Data/Policy</pre>
    mutate(Date = parse_date_time(`Date Changed`, orders = "dmy"),
```

Q = quarter(Date),

```
Year = year(Date)) %>%
  group_by(Year, Q) %>%
  summarise(mean_SR_Rate = mean(Rate, na.rm = TRUE), .groups = "drop") %%
  complete(Year = full_seq(Year, 1), Q = 1:4) %>% # Ensure all Year-Quarter combinations
  arrange(Year, Q) %>%
  fill(mean_SR_Rate, .direction = "down") # Fill missing rates by propagating the previous
Exports <- fread("D:/Samid work/University/KCL - Econ and Policy/Dissertation/Data/Exports.o
  mutate(Date = dmy(Month),
         month = month(Month),
         Year = year(dmy(Month)),
         Q = case_when(
           month %in% 1:3 ~ 1,
           month %in% 4:6 ~ 2,
           month %in% 7:9 ~ 3,
           month %in% 10:12 ~ 4
         )) %>%
  group_by(Year, Q) %>%
  summarize(Exports = sum(Exports, na.rm = TRUE))
ERI <- fread("D:/Samid work/University/KCL - Econ and Policy/Dissertation/Data/Boe ERI.csv")
  mutate(
         month = month(Date),
         Year = year(dmy(Date)),
         Q = case_when(
           month %in% 1:3 ~ 1,
           month %in% 4:6 ~ 2,
           month %in% 7:9 ~ 3,
           month %in% 10:12 ~ 4
         )) %>%
  rename(ERI = Value)
data <- fiscal_proc %>%
  left_join(filtered_df, by = c("Q" = "Q", "Year" = "Year")) %>%
  left_join(Interest_SR, by = c("Q" = "Q", "Year" = "Year")) %>%
 left_join(Exports, by = c("Q" = "Q", "Year" = "Year")) %>%
  left_join(population, by = c("Year" = "Year")) %>%
  left_join(ERI, by = c("Q" = "Q", "Year" = "Year")) %>%
# Convert variables to per capita, note revenue, expenditure, and GDP are in oldsymbol{	extit{f}} million so n
  mutate(RevenuePerCapita = (Revenue *10^6) /Population,
         ExpenditurePerCapita = (Expenditure *10^6) /Population,
         GDPPerCapita = (GDP *10^6) /Population) %>%
  # Create scaling factor to convert from nominal to current prices
  mutate(real_sf = Deflator /104.4151) %>% # Divide by current deflator rate (104.8583) as
```

```
# Create real fiscal variables
  mutate(Revenue_real = Revenue * real_sf,
         Expenditure_real = Expenditure * real_sf) %>%
  # Seasonal Adjustment of data using X-13ARIMA-SEATS
   mutate(Revenue_SA = final(seas(ts(Revenue_real, start = min(Year), frequency = 4))),
         Expenditure_SA = final(seas(ts(Expenditure_real, start = min(Year), frequency = 4)
         GDP_SA = final(seas(ts(GDP, start = min(Year), frequency = 4)))) %>%
 # convert back to numeric
    mutate(
    Revenue_SA = as.numeric(Revenue_SA),
    Expenditure_SA = as.numeric(Expenditure_SA),
    GDP_SA = as.numeric(GDP_SA)
 ) %>%
# Convert variables (except interest rate) to logs
  # Note multiplying by 10 6 for variables that are defined in £millions
 mutate(log_revenue = log(Revenue_SA *10^6),
         log_expenditure = log(Expenditure_SA *10^6),
         log_{GDP} = log(GDP_{SA} *10^6),
         log_deflator = log(Deflator),
         log_ERI = log(ERI),
         log_exports = log(Exports *10^6)) %>%
 mutate(
    dif_log_revenue = log_revenue - lag(log_revenue),
    dif_log_expenditure = log_expenditure - lag(log_expenditure),
    dif_log_GDP = log_GDP - lag(log_GDP),
    dif_log_deflator = log_deflator - lag(log_deflator),
   dif_log_ERI = log_ERI - lag(log_ERI),
   dif_interest_rate = mean_SR_Rate - lag(mean_SR_Rate),
    dif_log_exports = log_exports - lag(log_exports)
 )
model_data2 <- data %>%
  dplyr::select(Year, CDID, log_expenditure, mean_SR_Rate, log_GDP, log_ERI, log_revenue,
# model_data2 <- data %>%
    dplyr::select(Year, CDID, log_expenditure, mean_SR_Rate, log_GDP, log_exports, log_rever
# model_data <- data %>%
    dplyr::select(Year, CDID, dif_log_expenditure, dif_interest_rate, dif_log_exports, dif_
```

```
model_data <- data %>%
dplyr::select(Year, CDID, dif_log_expenditure, dif_interest_rate, dif_log_GDP, dif_log_ERI,
# Adding Exports
# Load required packages
# library(dplyr)
# library(purrr)
# library(tseries)
# Select relevant variables (excluding Year and CDID)
# vars_to_test <- model_data2 %>%
    dplyr::select(-Year, -CDID)
# # Apply ADF test to each variable
\# \ adf\_results <- \ map(vars\_to\_test, \ {\it ``adf.test(.x)})
# # Extract p-values and test statistics
# adf_summary <- map_df(adf_results, function(res) {</pre>
  tibble(
     statistic = res$statistic,
#
     p\_value = res p.value
# }, .id = "variable")
# # View results
# print(adf_summary)
# # Apply KPSS test and extract results
# kpss_summary <- map_df(names(vars_to_test), function(var_name) {</pre>
   series <- vars_to_test[[var_name]]</pre>
   test <- ur.kpss(series, type = "mu")</pre>
#
  tibble(
#
     variable = var_name,
     statistic = test@teststat,
    critical_10pct = test@cval["10pct"],
    critical_5pct = test@cval["5pct"],
     critical_1pct = test@cval["1pct"],
      stationary_5pct = test@teststat < test@cval["5pct"]</pre>
```

```
# })
# # View results
# print(kpss_summary)
clean_data <- na.omit(model_data)</pre>
clean_data2 <- na.omit(model_data2)</pre>
tmp <- clean_data[,-c(1,2)]</pre>
OptimalLag <- VARselect(clean_data[,-c(1,2)], lag.max = 5, type = "const")
OptimalLag2 <- VARselect(clean_data2[,-c(1,2)], lag.max = 5, type = "const")</pre>
# OptimalLag2$selection
# OptimalLag$criteria
# OptimalLag$selection
# OptimalLag$criteria
# OptimalLag2$criteria
# library(vars)
reduced_VAR <- VAR(clean_data[,-c(1,2)], p = 3, type = "const")</pre>
\# reduced_VAR2 \leftarrow VAR(clean_data2[,-c(1,2)], p = 4, type = "both")
\# reduced_VAR \leftarrow VAR(clean_data[, -1], p = 4)
# roots(reduced VAR)
# roots(reduced_VAR2)
# summary(reduced_VAR)
# Summary reports the roots of the polynomial.
# Define the 5 dimensional lower triangular matrix, A
# Recover structural VAR using Cholesky decomposition
# Recursive ordering
#
                   NA, 1, 0, 0, 0,
#
                   NA, NA, 1, 0, 0,
#
                   NA, NA, NA, 1, 0,
```

```
NA, NA, NA, NA, 1),
#
                  nrow = 5, byrow = TRUE)
# Variables are already ordered per the recursive identification strategy. Thus create a los
k <- ncol(clean_data[,-c(1,2)])</pre>
Amat <- diag(1, k)
Amat[lower.tri(Amat)] <- NA</pre>
# print(Amat)
svar_model <- SVAR(reduced_VAR, Amat = Amat, estmethod = "direct")</pre>
# svar_model2 <- SVAR(reduced_VAR2, Amat = Amat, estmethod = "direct")
# ?SVAR()
structural_shocks <- residuals(svar_model)</pre>
# svar_model
irf_result <- irf(svar_model, n.ahead = 10, ci = 0.68, boot = 5000, cumulative = TRUE) # F</pre>
\# irf_result2 \leftarrow irf(svar_model2, n.ahead = 10, ci = 0.68, boot = 5000, cumulative = FALSE)
\# irf_result \leftarrow irf(svar_model, n.ahead = 10, ci = 0.68, boot = 5000, cumulative = TRUE) \#
# plot(irf_result)
# Visualize IRFs
FEVD_result <- fevd(svar_model, n.ahead = 10) # Forecast horizons</pre>
# FEVD_result2 <- fevd(svar_model2, n.ahead = 10) # Forecast horizons
# plot(FEVD_result)
# plot(FEVD_result2)
# Post Covid:
# Extract IRFs
exp_irf <- round(irf_result$irf$dif_log_expenditure[, 3],2)</pre>
rev_irf <- round(irf_result$irf$dif_log_revenue[, 3],2)</pre>
```

```
exp_irf_df <- as.data.frame(</pre>
 cbind(
    seq(0,10),
    irf_result$irf$dif_log_expenditure[, 3],
    irf_result$Lower$dif_log_expenditure[, 3],
    irf_result$Upper$dif_log_expenditure[, 3]
 )
)
colnames(exp_irf_df) <- c("Quarter", "Expenditure", "LB", "UB")</pre>
rev irf df <- as.data.frame(</pre>
  cbind(
    seq(0,10),
    irf_result$irf$dif_log_revenue[, 3],
    irf_result$Lower$dif_log_revenue[, 3],
    irf_result$Upper$dif_log_revenue[, 3]
)
colnames(rev_irf_df) <- c("Quarter", "Revenue", "LB", "UB")</pre>
# Define a custom theme for consistency
custom_theme <- theme_minimal(base_size = 14) +</pre>
 theme(
    plot.title = element_text(hjust = 0.5, face = "bold"),
    axis.title = element_text(face = "bold"),
    panel.grid.minor = element_blank()
 )
# Plot for Expenditure IRF
ggplot(exp_irf_df, aes(x = Quarter)) +
 geom_ribbon(aes(ymin = LB, ymax = UB), fill = "lightblue", alpha = 0.4) +
 geom_line(aes(y = Expenditure), color = "blue", size = 1.2) +
  geom_hline(yintercept = 0, linetype = "dotted", color = "black") +
 labs(
```

```
title = "Impulse Response of Government Expenditure",
   x = "Quarter",
   y = "Log-Difference Response"
 ) +
  custom_theme
# Plot for Revenue IRF
ggplot(rev_irf_df, aes(x = Quarter)) +
  geom_ribbon(aes(ymin = LB, ymax = UB), fill = "lightblue", alpha = 0.4) +
  geom_line(aes(y = Revenue), color = "blue", size = 1.2) +
  geom_hline(yintercept = 0, linetype = "dotted", color = "black") +
   title = "Impulse Response of Government Revenue",
   x = "Period",
   y = "Log-Difference Response"
 ) +
  custom_theme
# structural_shocks <- residuals(svar_model)</pre>
# irf_result <- irf(svar_model, n.ahead = 10) # Forecast horizons
# plot(irf_result) # Visualize IRFs
# normality.test(reduced_VAR)
serial_test <- serial.test(reduced_VAR, lags.pt = 16, type = "PT.asymptotic")</pre>
# serial_test # Don't reject HO of no autocorrelation
normality_test <- normality.test(reduced_VAR)</pre>
# normality_test
hetero_test <- arch.test(reduced_VAR, lags.multi = 5)</pre>
# hetero_test
# --- Step 1: Define Restricted Model ---
\# reduced_VAR \leftarrow VAR(clean_data[,-c(1,2)], p = 3, type = "const")
# --- Step 1: Define Parameters ---
break_year <- 2008</pre>
```

```
p \leftarrow 1
Rep <- 100
T_break <- which((clean_data$Year == break_year))[1] # First observation of break year</pre>
# --- Step 2: Estimate VAR & Prepare Data ---
Y <- clean_data[, -c(1, 2)] # Drop Year + Quarter columns
var_orig <- VAR(Y, p = p, type = "const")</pre>
resids <- residuals(var_orig)</pre>
centered_resids <- scale(resids, scale = FALSE) # Centered residuals</pre>
Y_vals <- as.matrix(Y)</pre>
presample <- Y_vals[1:p, ]</pre>
coef_matrix <- Bcoef(var_orig)</pre>
A <- as.matrix(coef_matrix[, -ncol(coef_matrix)])
c <- coef_matrix[, ncol(coef_matrix)]</pre>
# --- Step 3: Define Chow Function (Lambda_BP) ---
chow_stat <- function(Y, T_break, p) {</pre>
  tryCatch({
    T_full <- nrow(Y)</pre>
    # Restricted model: full sample
    model_restricted <- VAR(Y, p = p, type = "const")</pre>
    SSR_restricted <- sum(residuals(model_restricted)^2)</pre>
    # Unrestricted model: separate pre and post samples
    Y_pre <- Y[1:T_break, ]</pre>
    Y_post <- Y[(T_break + 1):T_full, ]</pre>
    model_pre <- VAR(Y_pre, p = p, type = "const")</pre>
    model_post <- VAR(Y_post, p = p, type = "const")</pre>
    SSR_unrestricted <- sum(residuals(model_pre)^2) + sum(residuals(model_post)^2)
    SSR 1 <- sum(residuals(model pre)^2)</pre>
    SSR_tot <- sum(residuals(model_restricted)^2)</pre>
    # Extract log-likelihoods
    ll_restricted <- logLik(model_restricted)</pre>
    ll_unrestricted <- logLik(model_pre) + logLik(model_post)</pre>
    # Count number of coefficients per equation (excluding stats like SE, t)
    k <- nrow(coef(reduced_VAR)[[1]])</pre>
```

```
n_eq <- length(coef(reduced_VAR)) # Number of equations</pre>
    # Degrees of freedom = number of extra parameters in unrestricted models
    df_chow <<- k * n_eq</pre>
    # Compute LR test statistic
    lambda_BP <- -2 * (as.numeric(ll_restricted) - as.numeric(ll_unrestricted))</pre>
   return(lambda_BP)
 }, error = function(e) {
    message("Chow statistic failed: ", e$message)
    return(NA)
 })
# --- Step 4: Bootstrap Simulation ---
set.seed(1234)
boot_stats <- numeric(Rep)</pre>
for (r in 1:Rep) {
  # FIX: Sample from available residuals only
 u_star <- centered_resids[sample(1:nrow(centered_resids), size = nrow(Y_vals), replace = "</pre>
 Y_boot <- matrix(NA, nrow = nrow(Y_vals), ncol = ncol(Y_vals),
                    dimnames = list(NULL, colnames(Y_vals)))
 Y_boot[1:p, ] <- presample</pre>
 for (t in (p + 1):nrow(Y_vals)) {
    Y_{lags} \leftarrow as.vector(t(Y_{boot}[(t - p):(t - 1), ]))
    Y_boot[t, ] <- c + A %*% Y_lags + u_star[t, ]</pre>
 boot_stats[r] <- if (anyNA(Y_boot)) NA else chow_stat(Y_boot, T_break, p)
  # if (r \%\% 50 == 0) cat("Completed iteration", r, "\n")
}
boot_stats <- na.omit(boot_stats)</pre>
# --- Step 5: Actual Statistic & p-value ---
actual_stat <- chow_stat(Y_vals, T_break, p)</pre>
p_value_asymptotic <- 1 - pchisq(actual_stat, df_chow)</pre>
p_val <- mean(boot_stats > actual_stat)
# --- Step 6: Plot Results ---
if (length(boot_stats) > 0) {
```

```
boot_df <- data.frame(</pre>
    Iteration = 1:length(boot_stats),
    Chow_Statistic = boot_stats
 )
 chow_plot <<- ggplot(boot_df, aes(x = Iteration, y = Chow_Statistic)) +</pre>
    geom_line(color = "dodgerblue", alpha = 0.7) +
    geom_hline(yintercept = actual_stat, color = "red", linetype = "dashed", linewidth = 1)
    geom_point(aes(x = 0, y = actual_stat), color = "red", size = 3) +
    labs(
      title = "Bootstrap Chow Test (Recursive)",
      subtitle = paste("Breakpoint:", break_year, "| p-value:", round(p_val, 4)),
      x = "Bootstrap Iteration",
      y = "Chow Test Statistic"
    ) +
   theme_minimal()
} else {
 warning("No valid bootstrap statistics available to plot.")
# print(actual_stat)
# print(p_val)
# print(p_value_asymptotic)
chow_plot+
  custom_theme
T_break <- which((clean_data$Year == break_year))[1] # First observation of break year
Y_post_GFC <- Y[(T_break + 1):nrow(Y), ]</pre>
# reduced VAR \leftarrow VAR(clean data[,-c(1,2)], p = 3, type = "const")
reduced_VAR_post_GFC <- VAR(Y_post_GFC, p = 3, type = "const")</pre>
svar_model_post_gfc <- SVAR(reduced_VAR_post_GFC, Amat = Amat, estmethod = "direct")</pre>
irf_result_post_gfc <- irf(svar_model_post_gfc, n.ahead = 10, ci = 0.68, boot = 5000, cumula
exp_irf_post_GFC <- round(irf_result_post_gfc\space\sirf\space\dif_log_expenditure[, 3],2)</pre>
rev_irf_post_GFC <- round(irf_result_post_gfc$irf$dif_log_revenue[, 3],2)</pre>
```

```
# Combine into one table
# Combine IRFs into one table
irf_combined <- cbind(</pre>
 Period = 0:(length(exp_irf) - 1),
 Total_Expenditure = exp_irf,
 Total_Revenue = rev_irf,
 PostGFC_Expenditure = exp_irf_post_GFC,
 PostGFC_Revenue = rev_irf_post_GFC
)
# Prepare data for Revenue plot
df rev <- data.frame(</pre>
 Period = 0:(length(rev_irf) - 1),
 Total = rev_irf,
 PostGFC = rev_irf_post_GFC
 pivot_longer(cols = -Period, names_to = "Sample", values_to = "IRF")
# Prepare data for Expenditure plot
df_exp <- data.frame(</pre>
 Period = 0:(length(exp_irf) - 1),
 Total = exp_irf,
 PostGFC = exp_irf_post_GFC
) %>%
 pivot_longer(cols = -Period, names_to = "Sample", values_to = "IRF")
# Plot Revenue IRFs
ggplot(df_rev, aes(x = Period, y = IRF, color = Sample)) +
  geom_line(size = 1.2) +
 labs(
   title = "IRF: Revenue Response to Expenditure Shock",
   x = "Periods Ahead",
   y = "Impulse Response"
 ) +
  theme_minimal(base_size = 14) +
 theme(plot.title = element_text(face = "bold", hjust = 0.5)) +
  custom_theme
# Plot Expenditure IRFs
ggplot(df_exp, aes(x = Period, y = IRF, color = Sample)) +
  geom_line(size = 1.2) +
 labs(
   title = "IRF: Expenditure Response to Revenue Shock",
   x = "Periods Ahead",
```

```
y = "Impulse Response"
 ) +
 theme_minimal(base_size = 14) +
 theme(plot.title = element_text(face = "bold", hjust = 0.5)) +
  custom_theme
\# T_break \leftarrow which((clean_data\$Year == break_year))[1] \# First observation of break year
# Y_post_GFC <- Y[(T_break + 1):nrow(Y), ]
\# reduced_VAR \leftarrow VAR(clean_data[,-c(1,2)], p = 3, type = "const")
reduced_VAR_1_lag <- VAR(clean_data[,-c(1,2)], p = 1, type = "const")</pre>
svar_model_1_lag <- SVAR(reduced_VAR_1_lag, Amat = Amat, estmethod = "direct")</pre>
irf_result_1_lag <- irf(svar_model_1_lag, n.ahead = 10, ci = 0.68, boot = 5000, cumulative =
exp_irf_1_lag <- round(irf_result_1_lag\sirf\start dif_log_expenditure[, 3],2)
rev_irf_1_lag <- round(irf_result_1_lag$irf$dif_log_revenue[, 3],2)</pre>
reduced_VAR_post_GFC_1_lag <- VAR(Y_post_GFC, p = 1, type = "const")</pre>
svar_model_post_gfc_1_lag <- SVAR(reduced_VAR_post_GFC_1_lag, Amat = Amat, estmethod = "dire")</pre>
irf_result_post_gfc_1_lag <- irf(svar_model_post_gfc_1_lag, n.ahead = 10, ci = 0.68, boot =
exp_irf_post_GFC_1_lag <- round(irf_result_post_gfc_1_lag$irf$dif_log_expenditure[, 3],2)</pre>
rev_irf_post_GFC_1_lag <- round(irf_result_post_gfc_1_lag$irf$dif_log_revenue[, 3],2)</pre>
# Combine into one table
# Combine IRFs into one table
# irf_combined <- cbind(</pre>
  Period = 0: (length(exp_irf) - 1),
   Total_Expenditure = exp_irf,
   Total_Revenue = rev_irf,
  PostGFC_Expenditure = exp_irf_post_GFC,
  PostGFC_Revenue = rev_irf_post_GFC,
  PostGFC_Expenditure_1_lag = exp_irf_post_GFC_1_lag,
```

```
PostGFC_Revenue_1_lag = rev_irf_post_GFC_1_lag
# )
# Prepare data for Revenue plot
df_rev_all <- data.frame(</pre>
 Period = 0:(length(rev_irf) - 1),
 Total = rev_irf,
 PostGFC = rev_irf_post_GFC,
 PostGFC_1_lag = rev_irf_post_GFC_1_lag,
 Total_1_lag = rev_irf_1_lag
) %>%
 pivot_longer(cols = -Period, names_to = "Sample", values_to = "IRF")
# Prepare data for Expenditure plot
df_exp_all <- data.frame(</pre>
 Period = 0:(length(exp_irf) - 1),
 Total = exp_irf,
 PostGFC = exp_irf_post_GFC,
 PostGFC_1_lag = exp_irf_post_GFC_1_lag,
 Total_1_lag = exp_irf_1_lag
) %>%
 pivot_longer(cols = -Period, names_to = "Sample", values_to = "IRF")
# Plot Revenue IRFs
ggplot(df_rev_all, aes(x = Period, y = IRF, color = Sample)) +
 geom_line(size = 1.2) +
 labs(
   title = "IRF: Revenue Response to Revenue Shock",
   x = "Periods Ahead",
   y = "Impulse Response"
 theme_minimal(base_size = 14) +
 theme(plot.title = element_text(face = "bold", hjust = 0.5)) +
  custom_theme
# Plot Expenditure IRFs
ggplot(df_exp_all, aes(x = Period, y = IRF, color = Sample)) +
  geom_line(size = 1.2) +
```

```
labs(
   title = "IRF: Expenditure Response to Expenditure Shock",
   x = "Periods Ahead",
   y = "Impulse Response"
 ) +
  theme_minimal(base_size = 14) +
  theme(plot.title = element_text(face = "bold", hjust = 0.5)) +
  custom_theme
ggplot(data, aes(x = Unique_Period)) +
  geom_line(aes(y = Revenue_SA, color = "Revenue"), size = 1) +
  geom_line(aes(y = Expenditure_SA, color = "Expenditure"), size = 1) +
 labs(
   x = "Date ID",
   y = "Amount (? in millions)",
   title = "Seasonally Adjusted Revenue and Expenditure",
   color = "Legend"
  ) +
  scale_color_manual(values = c("Revenue" = "blue", "Expenditure" = "red")) +
  theme_minimal(base_size = 15) +
  theme(
   axis.text.x = element_text(angle = 45, hjust = 1),
   plot.title = element_text(hjust = 0.5, face = "bold"),
   axis.title.x = element_text(face = "bold"),
    axis.title.y = element_text(face = "bold"),
   legend.position = "bottom",
   legend.title = element_text(face = "bold")
 )
ggplot(data, aes(x = Unique_Period)) +
  geom_line(aes(y = Exports, color = "Exports"), size = 1) +
 labs(
   x = "Date ID",
   y = "Amount (? in millions)",
   title = "Exports Over Time",
   color = "Legend"
  scale_color_manual(values = c("Exports" = "red")) +
  theme_minimal(base_size = 15) +
    axis.text.x = element_text(angle = 45, hjust = 1),
   plot.title = element_text(hjust = 0.5, face = "bold"),
    axis.title.x = element_text(face = "bold"),
```

```
axis.title.y = element_text(face = "bold"),
    legend.position = "bottom",
    legend.title = element_text(face = "bold")
ggplot(data, aes(x = Unique_Period)) +
  geom_line(aes(y = ERI, color = "ERI"), size = 1) +
  labs(
   x = "Date ID",
   y = "Amount (? in millions)",
   title = "Exchange Rate Index Over Time",
    color = "Legend"
 ) +
  scale_color_manual(values = c("ERI" = "red")) +
  theme minimal(base size = 15) +
  theme(
    axis.text.x = element_text(angle = 45, hjust = 1),
   plot.title = element_text(hjust = 0.5, face = "bold"),
   axis.title.x = element_text(face = "bold"),
   axis.title.y = element_text(face = "bold"),
   legend.position = "bottom",
   legend.title = element_text(face = "bold")
ggplot(data, aes(x = Unique_Period)) +
  geom_line(aes(y = GDP, color = "GDP"), size = 1) +
 labs(
    x = "Date ID",
   y = "Amount (? in millions)",
   title = "GDP Over Time",
    color = "Legend"
  ) +
  scale_color_manual(values = c("GDP" = "red")) +
  theme_minimal(base_size = 15) +
  theme(
    axis.text.x = element_text(angle = 45, hjust = 1),
   plot.title = element_text(hjust = 0.5, face = "bold"),
   axis.title.x = element_text(face = "bold"),
    axis.title.y = element_text(face = "bold"),
   legend.position = "bottom",
    legend.title = element_text(face = "bold")
```

```
ggplot(data, aes(x = Unique_Period)) +
  geom_line(aes(y = Deflator), color = "blue", size = 1) +
 labs(
   x = "Date ID",
   y = "Deflator",
   title = "Deflator Over Time"
 theme_minimal(base_size = 15) +
 theme(
   axis.text.x = element_text(angle = 45, hjust = 1),
   plot.title = element_text(hjust = 0.5, face = "bold"),
   axis.title.x = element_text(face = "bold"),
   axis.title.y = element_text(face = "bold")
 )
# Define scaling factor
scale_factor2 <- max(data$Deflator, na.rm = TRUE) / max(data$mean_SR_Rate, na.rm = TRUE)</pre>
ggplot(data, aes(x = Unique_Period)) +
  geom_line(aes(y = mean_SR_Rate * scale_factor2), color = "red", size = 1, linetype = "das]
  scale_y_continuous(
   name = "Mean SR Rate (scaled)",
   sec.axis = sec_axis(~ . / scale_factor2, name = "Mean SR Rate (%)")
 ) +
 labs(
   x = "Date ID",
   title = "Mean Short-Term Interest Rate Over Time"
 theme_minimal(base_size = 15) +
 theme(
   axis.text.x = element_text(angle = 45, hjust = 1),
   plot.title = element_text(hjust = 0.5, face = "bold"),
   axis.title.x = element_text(face = "bold"),
   axis.title.y = element_text(face = "bold")
 )
# library(urca)
# urca::cajolst()
# vec2var
# Perform cointegration testing on the (log) levels variables
```

```
ca.jo_result_max_eig <- ca.jo(clean_data2[,-c(1,2)], type = "eigen", ecdet = "none", K =4)</pre>
ca.jo_result_trace <- ca.jo(clean_data2[,-c(1,2)], type = "trace", ecdet = "none", K =4)</pre>
ca.po_result <- ca.po(clean_data2[,-c(1,2)], demean = "const", type = "Pz")</pre>
\# ca.lut_result <- cajolst(clean_data2[,-c(1,2)], trend = TRUE, K = 2, season = NULL)
summary(ca.jo_result_max_eig)
summary(ca.jo_result_trace)
# summary(ca.po_result)
# summary(ca.lut_result)
# ca.jo()
\# scaling\_factor \leftarrow T/(T-N*k)
scaling_factor <- length(clean_data2$Year)/(length(clean_data2$Year)-6*4)
# Max Eigenvalue test HO r=0:
# test statistic: 41.78
# Asymptotic Critical value (5% sig level): 39.43
\# scaling_factor = 1.1875
# Finite sample critical value = 90.39 * scaling_factor = 46.82312
# After applying the scaling factor we no longer reject the null of no cointegration. We not
# Trace test HO r=0:
# test statistic: 115.81
# Asymptotic Critical value (5% sig level): 90.39
\# scaling factor = 1.1875
# Finite sample critical value = 90.39 * scaling_factor = 107.3381
# After applying the scaling factor, we no longer have sufficient evidence to reject the nu
vecm <- vec2var(ca.jo_result_max_eig, r = 1) # r = cointegration rank</pre>
# SVECM <- SVAR(vecm, Amat = Amat, estmethod = "direct")
\# irf_result_SVECM \leftarrow irf(SVECM, n.ahead = 10, ci = 0.68, boot = 5000, cumulative = TRUE)
LR_mat <- matrix(nrow = k, ncol=k)</pre>
```

```
svecm <- SVEC(ca.jo_result_max_eig, SR =Amat, LR =LR_mat)</pre>
irf_temp <- irf(svecm, n.ahead = 10, ci = 0.68, boot = 5000, cumulative = TRUE)</pre>
# plot(irf_temp)
# plotres(ca.jo_result)
\# vecm \leftarrow cajorls(ca.jo_result, r = 1)
johansen_test <- cajorls(ca.jo_result_max_eig, r = 1)</pre>
# johansen_test
vec2var_model <- vec2var(ca.jo_result_max_eig, r = 1)</pre>
vec2var_model
class(reduced_VAR)
class(vec2var_model)
# svar_model <- SVAR(vec2var_model, estmethod = "direct", Amat = Amat)
# irf_result <- irf(svar_model, n.ahead = 10, boot = TRUE, ci = 0.68)</pre>
# plot(irf_result)
# arch.test(reduced_VAR)
# serial.test(reduced_VAR)
# normality.test(reduced_VAR)
# Extract IRFs
exp_irf_vecm <- round(irf_temp$irf$log_expenditure[, 3],2)</pre>
rev_irf_vecm <- round(irf_temp$irf$log_revenue[, 3],2)</pre>
```

```
exp_irf_df_vecm <- as.data.frame(</pre>
 cbind(
    seq(0,10),
    irf_temp$irf$log_expenditure[, 3],
    irf_temp$Lower$log_expenditure[, 3],
    irf_temp$Upper$log_expenditure[, 3]
 )
)
colnames(exp_irf_df_vecm) <- c("Quarter", "Expenditure", "LB", "UB")</pre>
rev_irf_df_vecm <- as.data.frame(</pre>
 cbind(
    seq(0,10),
    irf_temp$irf$log_revenue[, 3],
    irf_temp$Lower$log_revenue[, 3],
    irf_temp$Upper$log_revenue[, 3]
 )
)
colnames(rev_irf_df_vecm) <- c("Quarter", "Revenue", "LB", "UB")</pre>
# Define a custom theme for consistency
# custom_theme <- theme_minimal(base_size = 14) +</pre>
#
      plot.title = element_text(hjust = 0.5, face = "bold"),
     axis.title = element_text(face = "bold"),
      panel.grid.minor = element_blank()
#
# Plot for Expenditure IRF
ggplot(exp_irf_df_vecm, aes(x = Quarter)) +
  geom_ribbon(aes(ymin = LB, ymax = UB), fill = "lightblue", alpha = 0.4) +
 geom_line(aes(y = Expenditure), color = "blue", size = 1.2) +
 geom_hline(yintercept = 0, linetype = "dotted", color = "black") +
 labs(
    title = "Impulse Response of Government Expenditure",
```

```
x = "Quarter",
   y = "Log-Difference Response"
 ) +
  custom_theme
# Plot for Expenditure IRF
ggplot(rev_irf_df_vecm, aes(x = Quarter)) +
  geom_ribbon(aes(ymin = LB, ymax = UB), fill = "lightblue", alpha = 0.4) +
  geom_line(aes(y = Revenue), color = "blue", size = 1.2) +
  geom_hline(yintercept = 0, linetype = "dotted", color = "black") +
 labs(
    title = "Impulse Response of Government Expenditure",
    x = "Quarter",
    y = "Log-Difference Response"
 ) +
  custom_theme
plot_irf_with_ci <- function(IRF_name) {</pre>
  # Extract response and confidence intervals
  irf_data <- as.data.frame(IRF_name$irf)</pre>
  irf_lower <- as.data.frame(IRF_name$Lower)</pre>
  irf_upper <- as.data.frame(IRF_name$Upper)</pre>
  # Create time index
  irf_data$Time <- seq_len(nrow(irf_data))</pre>
  irf_lower$Time <- irf_data$Time</pre>
  irf_upper$Time <- irf_data$Time</pre>
  # Reshape to long format
  irf_long <- pivot_longer(irf_data, cols = -Time, names_to = "Variable", values_to = "IRJ</pre>
  lower_long <- pivot_longer(irf_lower, cols = -Time, names_to = "Variable", values_to = "L</pre>
 upper_long <- pivot_longer(irf_upper, cols = -Time, names_to = "Variable", values_to = "U
  # Merge and label
  irf_combined <- irf_long %>%
    left_join(lower_long, by = c("Time", "Variable")) %>%
    left_join(upper_long, by = c("Time", "Variable")) %>%
    mutate(
      Shock = sub("\\..*", "", Variable),
      Affected_Var = sub(".*\\.", "", Variable)
```

```
# Plot IRFs by shock
  shock_names <- unique(irf_combined$Shock)</pre>
  for (shock in shock_names) {
    p <- irf_combined %>%
      filter(Shock == shock) %>%
      ggplot(aes(x = Time, y = IRF)) +
      geom_line(size = 1.2, color = "#1f77b4") +
      geom_line(aes(y = Lower), linetype = "dashed", color = "#7f7f7f", size = 0.9) +
      geom_line(aes(y = Upper), linetype = "dashed", color = "#7f7f7f", size = 0.9) +
      geom_hline(yintercept = 0, color = "black", size = 1.1) +
      facet_wrap(~ Affected_Var, scales = "free_y") +
      theme_minimal(base_family = "serif") +
      theme(
        plot.title = element_text(size = 16, face = "bold"),
        axis.title.x = element_text(size = 14),
        axis.title.y = element_text(size = 14),
        axis.text = element_text(size = 12),
        panel.grid.major = element_line(color = "gray85"),
        panel.grid.minor = element_blank(),
        strip.text = element_text(size = 14, face = "bold")
      ) +
      labs(
        title = paste("Impulse Response for Shock:", shock),
        x = "Time",
        y = "Response"
      scale_y_continuous(expand = expansion(mult = c(0, 0.05)))
    print(p)
  }
}
plot_irf_with_ci(irf_result)
# plot_irf_with_ci(irf_result2)
plot(FEVD_result)
FEVD_result
library(knitr)
```

```
# Create named vector of means
means <- c(
 mean(model_data$dif_log_expenditure, na.rm = TRUE),
 mean(model_data$dif_interest_rate, na.rm = TRUE),
 mean(model_data$dif_log_ERI, na.rm = TRUE),
 mean(model_data$dif_log_GDP, na.rm = TRUE),
 mean(model_data$dif_log_revenue, na.rm = TRUE),
 mean(model_data$dif_log_deflator, na.rm = TRUE)
)
# Variable names
variables <- c(</pre>
  "dif_log_expenditure",
  "dif_interest_rate",
  "dif_log_ERI",
  "dif_log_GDP",
  "dif_log_revenue",
  "dif log deflator"
)
# Assemble and display
mean_table <- data.frame(Variable = variables, Mean = round(means, 5))</pre>
kable(mean_table, align = "lr", caption = "Mean Values of Differenced Variables")
run_var_analysis <- function(model_data_type) {</pre>
  # Extract suffix from input name
  input_name <- deparse(substitute(model_data_type))</pre>
  suffix <- sub("^[^_]+_", "", input_name)</pre>
  suffix <- ifelse(nchar(suffix) == 0, "data", suffix)</pre>
  # Split data into pre- and post-2008 samples
  clean_data_a <- model_data_type %>%
    filter(Year < 2008 & complete.cases(.))</pre>
  clean_data_b <- model_data_type %>%
    filter(!is.na(Year) & Year >= 2008)
  assign(paste0("clean_data_a_", suffix), clean_data_a, envir = .GlobalEnv)
  assign(paste0("clean_data_b_", suffix), clean_data_b, envir = .GlobalEnv)
  # Choose VAR specification
    var_a \leftarrow VAR(clean_data_a[,-c(1,2)], p = 1, type = "const")
    var_b \leftarrow VAR(clean_data_b[,-c(1,2)], p = 1, type = "const")
```

```
assign(paste0("reduced_VAR_a_", suffix), var_a, envir = .GlobalEnv)
  assign(paste0("reduced_VAR_b_", suffix), var_b, envir = .GlobalEnv)
  # Check stability
 print(roots(var_a))
 print(roots(var_b))
  # Recursive identification matrix
 k <- ncol(clean_data_a[,-c(1,2)])
  Amat <- diag(1, k)
  Amat[upper.tri(Amat)] <- NA</pre>
  # SVAR estimation
  svar_a <- SVAR(var_a, Amat = Amat, estmethod = "direct")</pre>
  svar_b <- SVAR(var_b, Amat = Amat, estmethod = "direct")</pre>
  assign(paste0("svar_model_a_", suffix), svar_a, envir = .GlobalEnv)
  assign(paste0("svar_model_b_", suffix), svar_b, envir = .GlobalEnv)
  # TRFs
  irf_a <- irf(svar_a, n.ahead = 10, ci = 0.68, boot = 5000, cumulative = TRUE)
  irf_b <- irf(svar_b, n.ahead = 10, ci = 0.68, boot = 5000, cumulative = TRUE)</pre>
  assign(paste0("irf_result_a_", suffix), irf_a, envir = .GlobalEnv)
  assign(paste0("irf_result_b_", suffix), irf_b, envir = .GlobalEnv)
  # FEVDs
 fevd_a <- fevd(svar_a, n.ahead = 10)</pre>
  fevd_b <- fevd(svar_b, n.ahead = 10)</pre>
  assign(paste0("FEVD_result_a_", suffix), fevd_a, envir = .GlobalEnv)
  assign(paste0("FEVD_result_b_", suffix), fevd_b, envir = .GlobalEnv)
  # Plot FEVDs
 plot(fevd_a)
 plot(fevd_b)
run_var_analysis(model_data)
# run_var_analysis(model_data2)
# run the chow test
```

```
# plot_irf_with_ci(irf_result2_data)
```

Apply processing and plotting functions