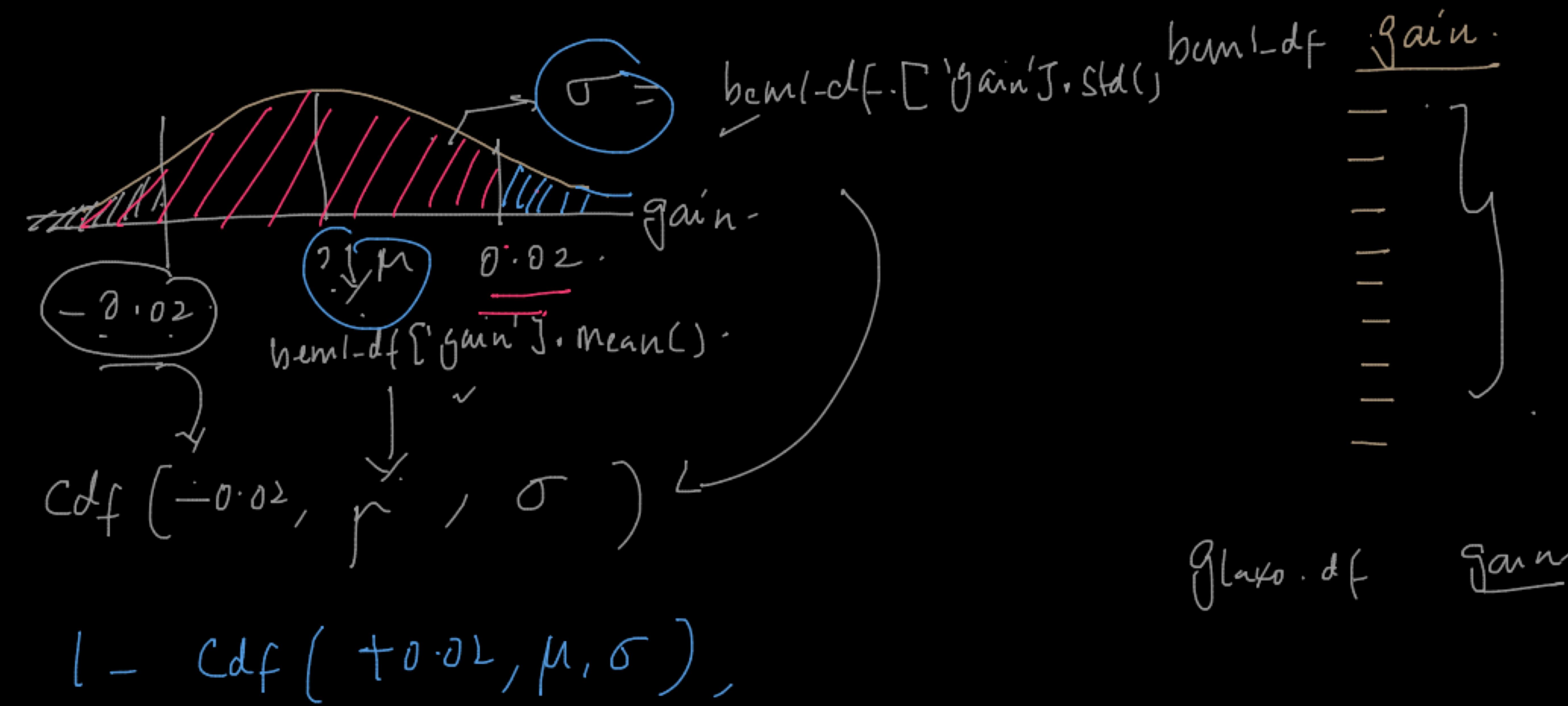


$$Z_{680} = \frac{680 - 711}{29} = -1.06$$

Python \Rightarrow `cdf(680, 711, 29)`
 $= P(X \leq 680)$

$P(X > 720) = 1 - cdf(720, 711, 29)$



Moments

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$x_1 \rightarrow (x_1 - \bar{x})$$

$$x_2 \rightarrow (x_2 - \bar{x})^2$$

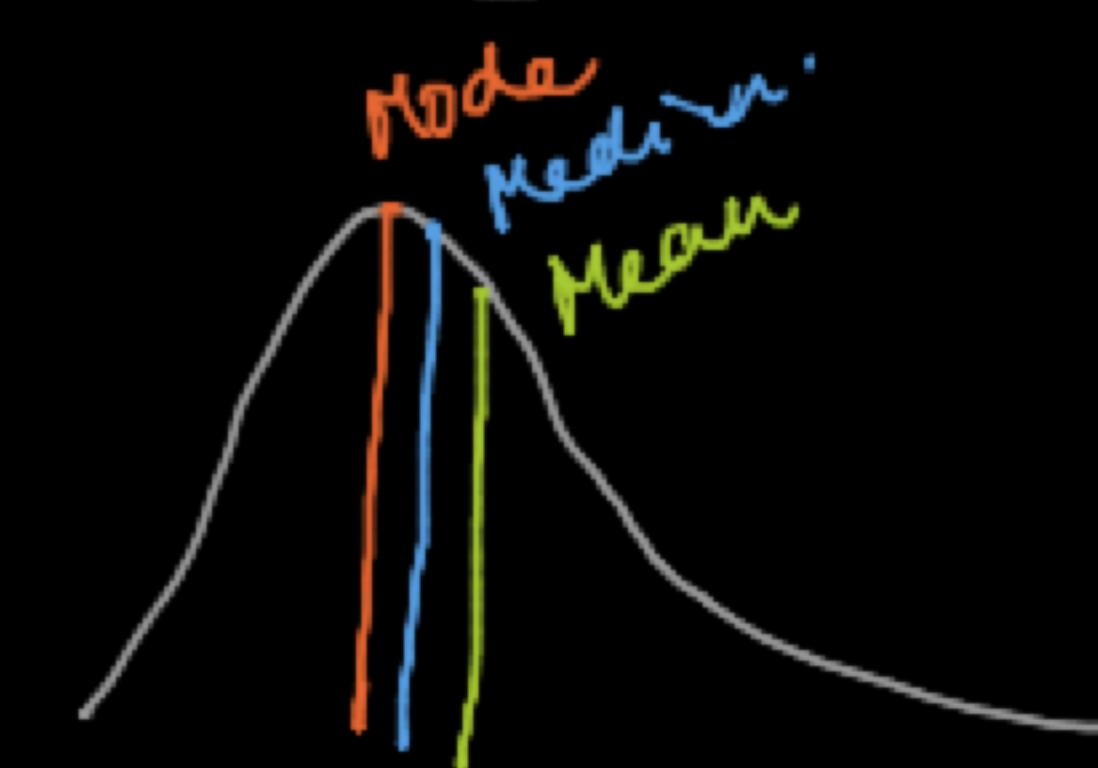
$$\sigma^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$

$$\sigma = \sqrt{\sigma^2}$$

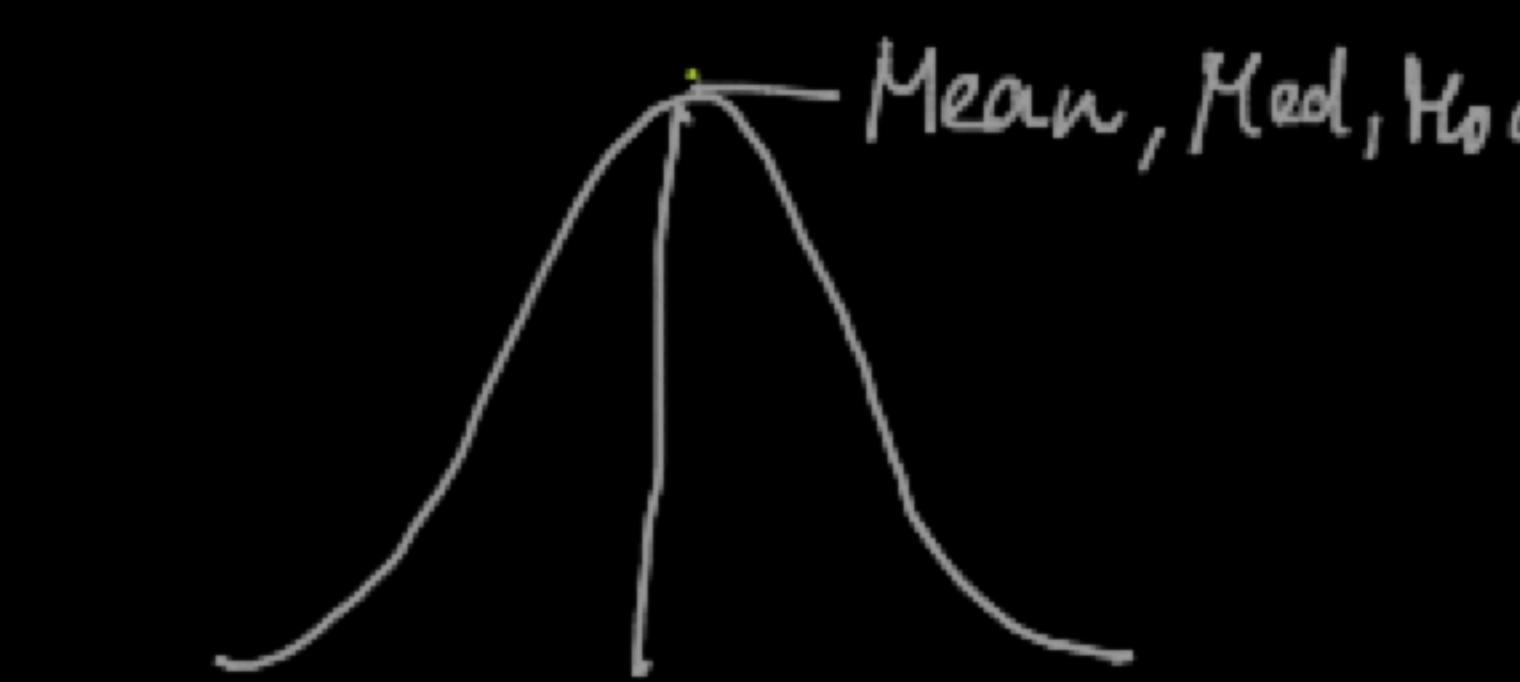
2. Second moment -

— Variance

3. Third moment — Skewness -



Right Skew

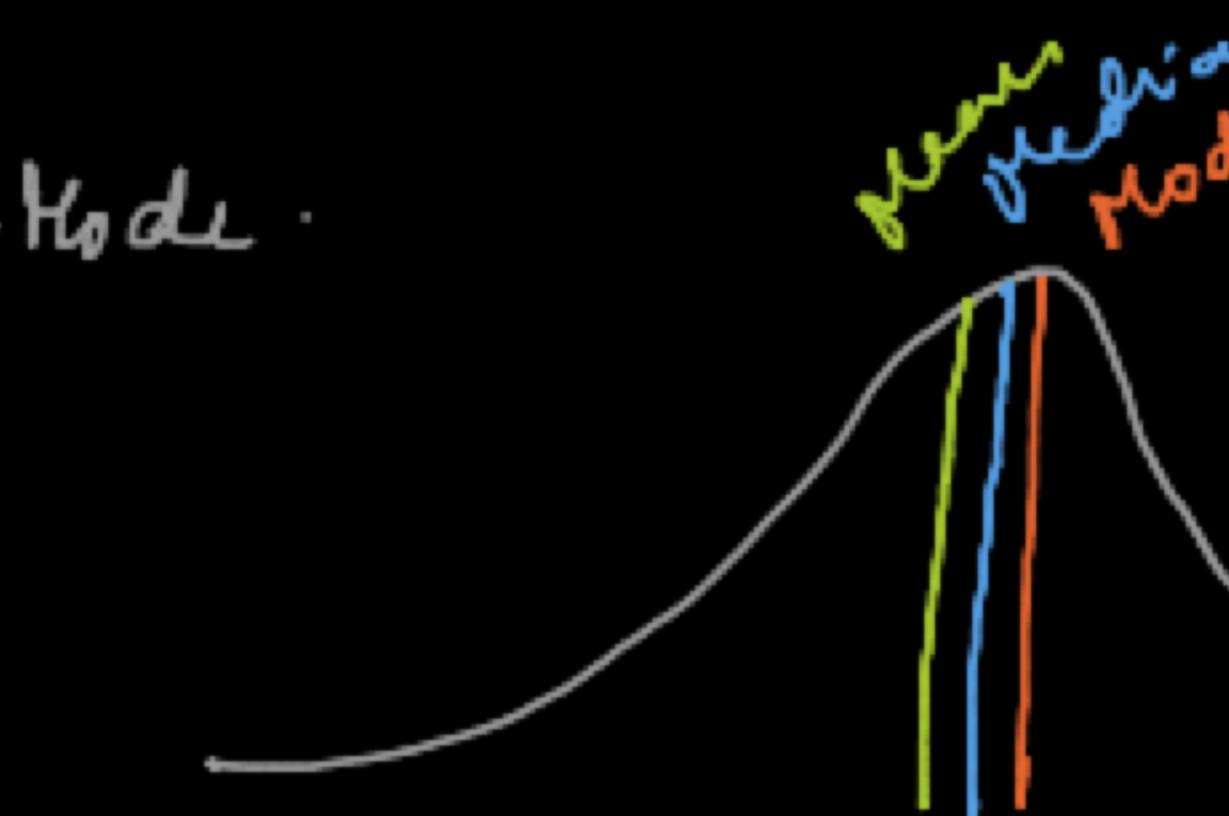
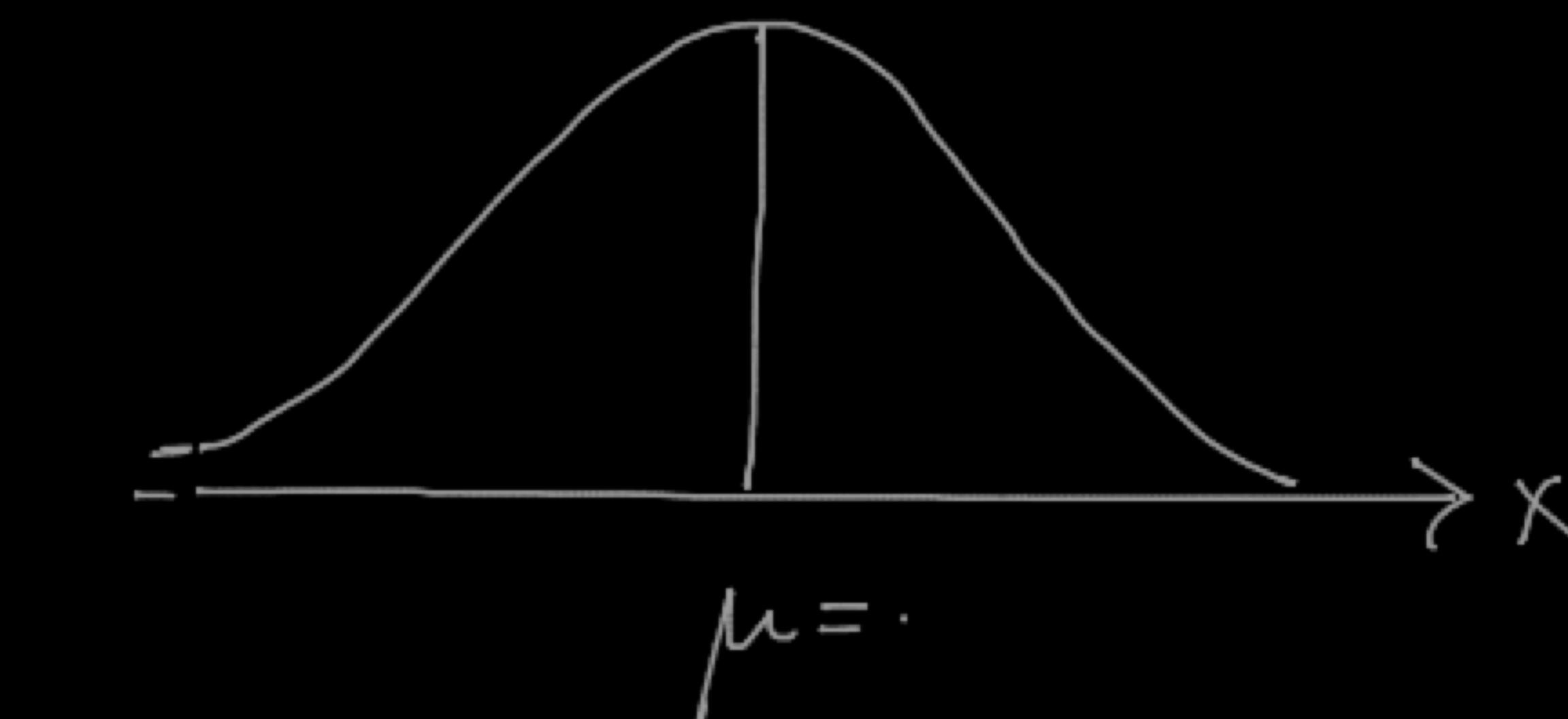


Moments

→ Define the shape of a distribution -
— Four moments of ND

→ Mean Value

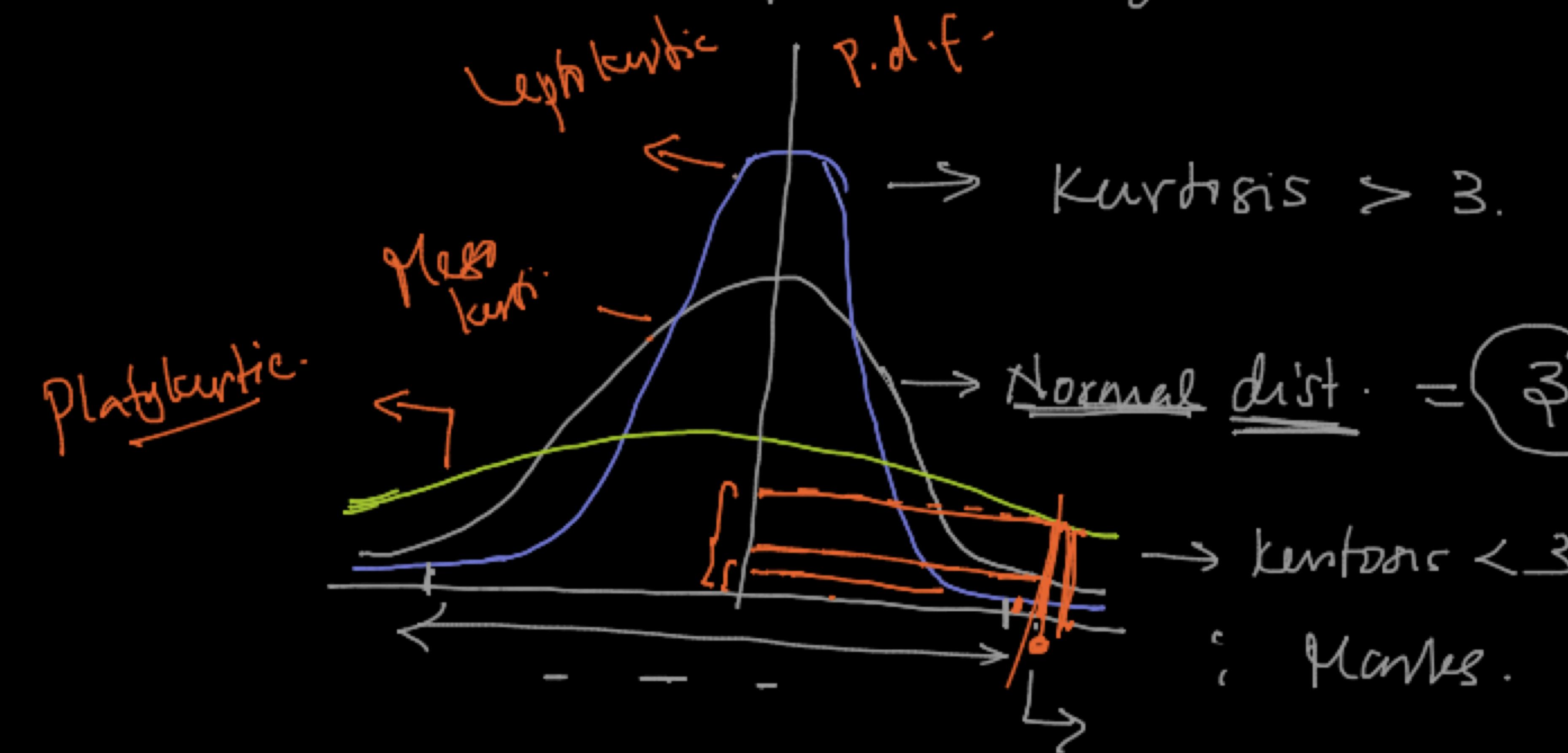
→ Central Value



Left Skew

→ Moments

4. Kurtosis \rightarrow Peakedness of the dist.



Excess kurtosis

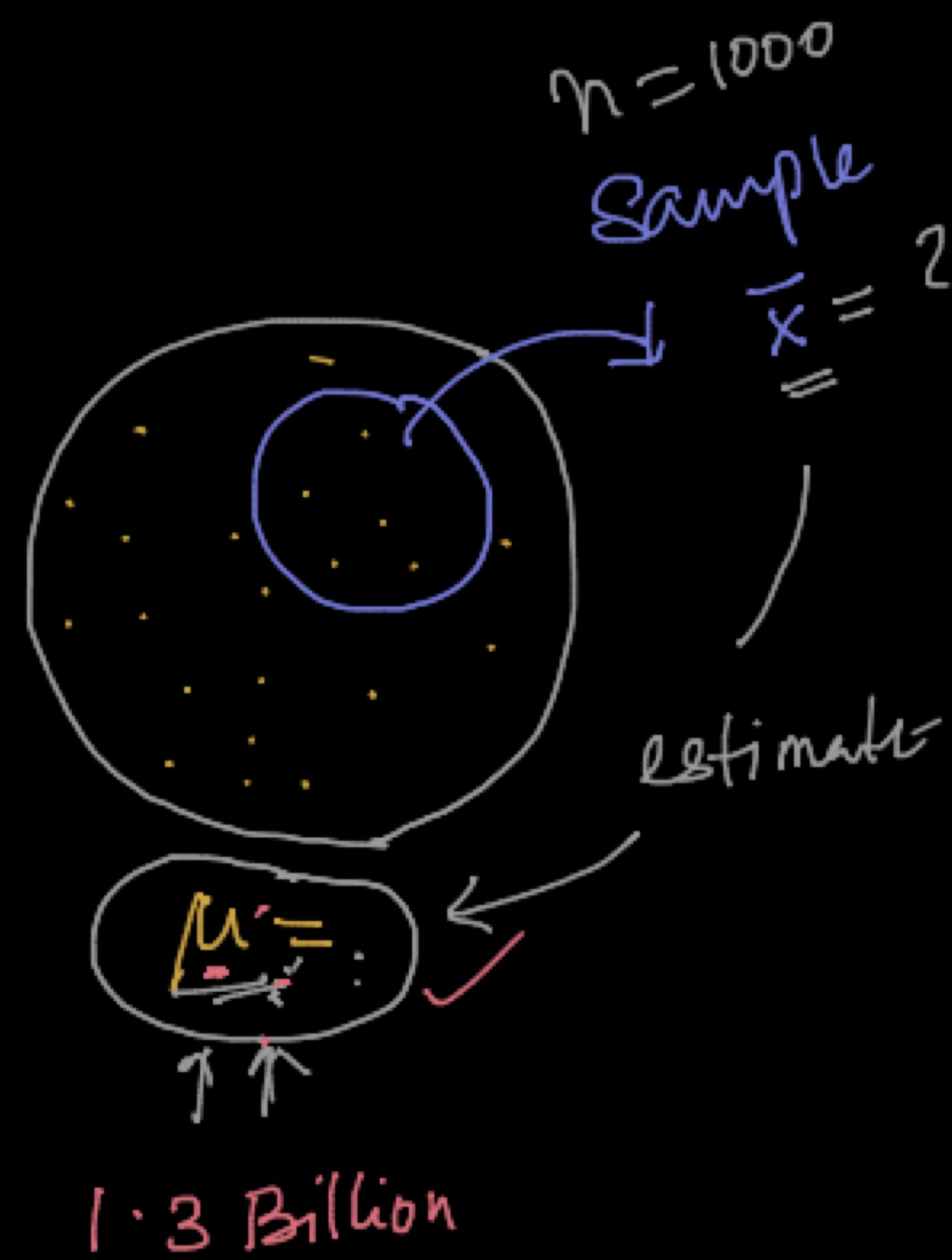
$$\Rightarrow (\text{kurtosis} - 3)$$

+ve; -ve -

$$= 0$$

Tail \rightarrow prob. of finding
extreme value.

(|)



$$\mu_{\bar{x}} = \mu_{\text{pop}}$$

$$\sigma_{\bar{x}} = \sigma_{\text{pop}} / \sqrt{n}$$

$n \rightarrow \text{Sample Size}$

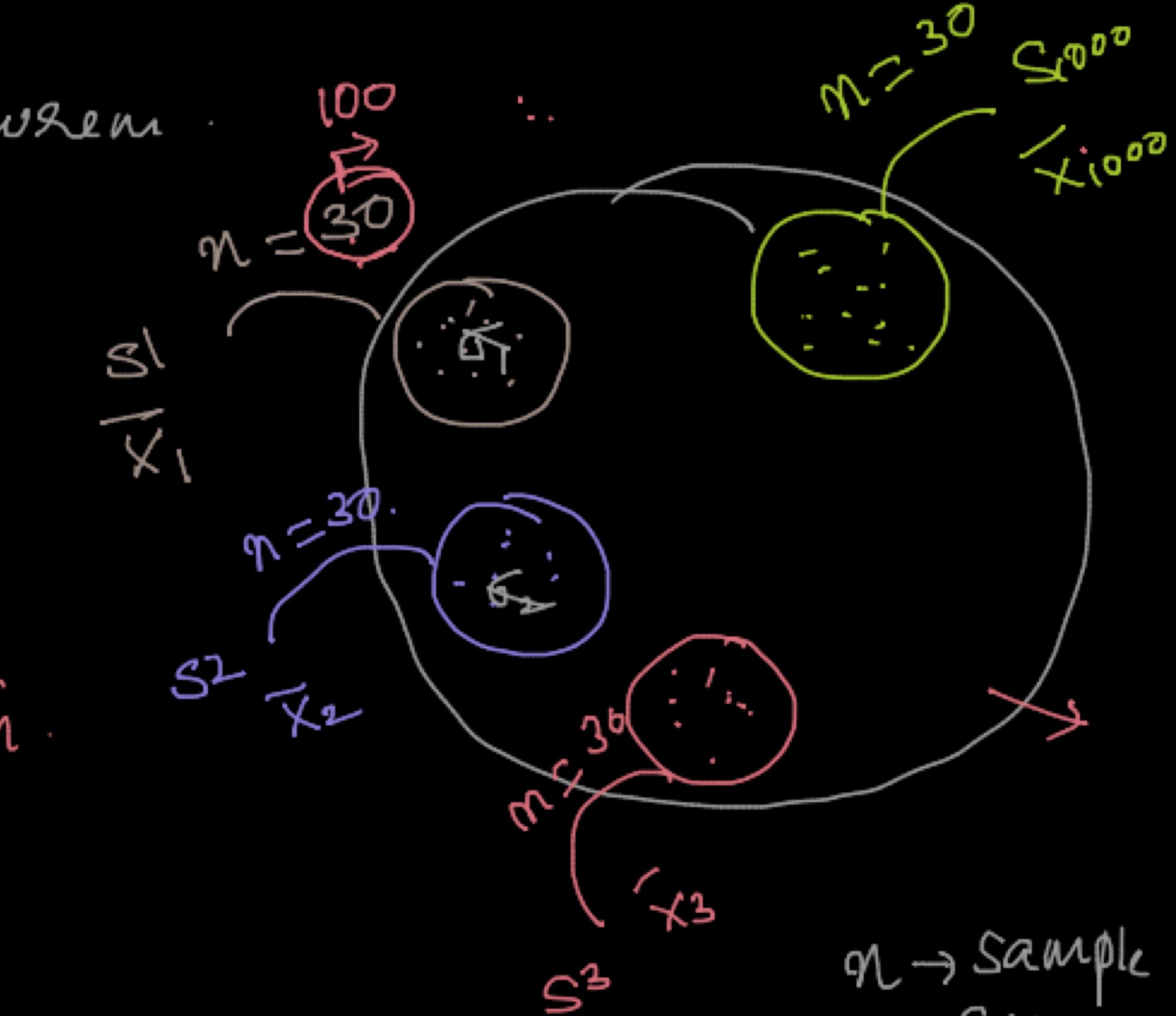
Central Limit Theorem

Sample Means ✓

$$\begin{aligned} \bar{x}_1 &= 1200 \\ \bar{x}_2 &= 1350 \\ \bar{x}_3 &= 1500 \\ &\vdots \\ \bar{x}_{1000} &= 2200 \end{aligned}$$

Sampling distribution of Sample Means

$$\sigma_{\bar{x}} = \sigma_{\text{pop}} / \sqrt{n}$$

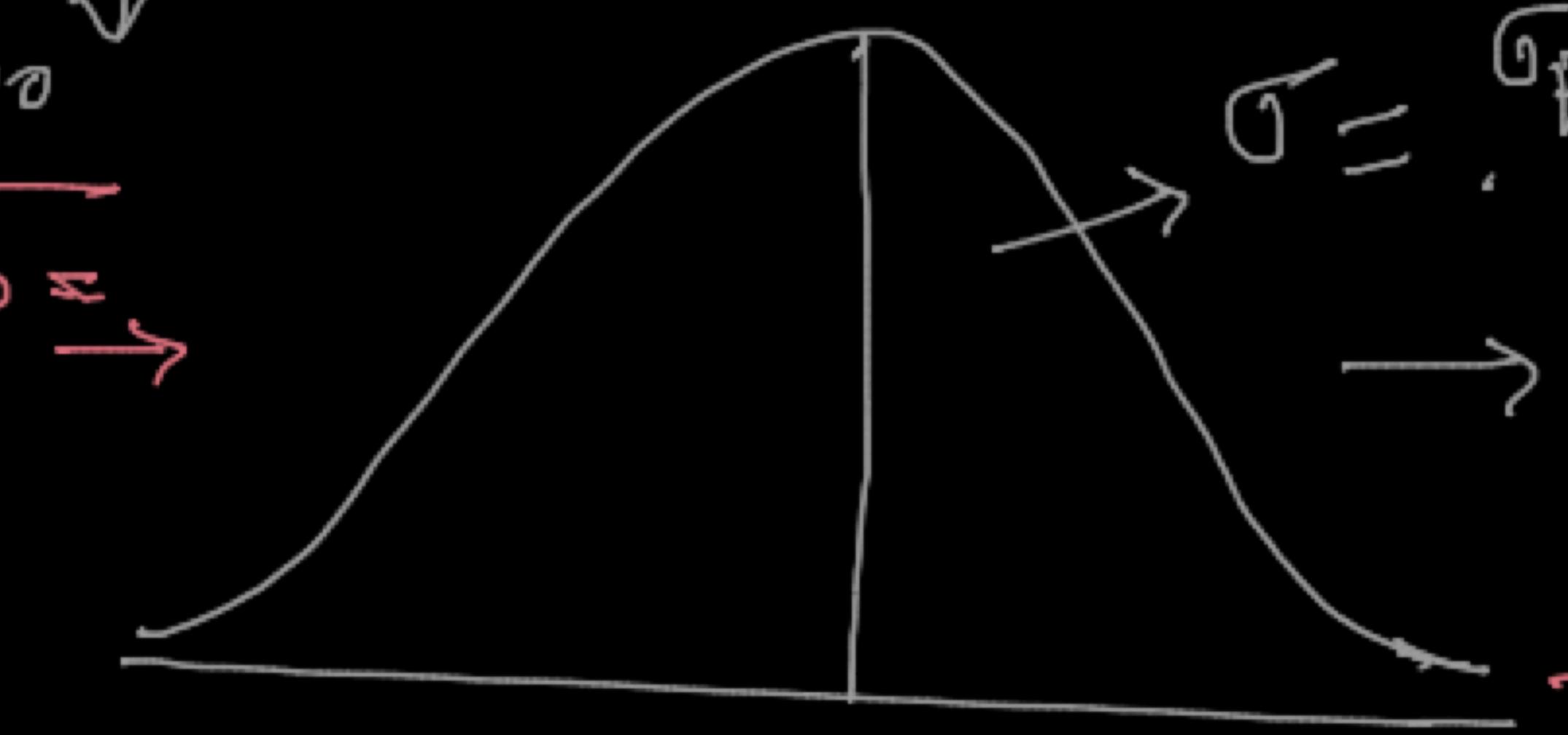


$n \rightarrow \text{Sample Size}$

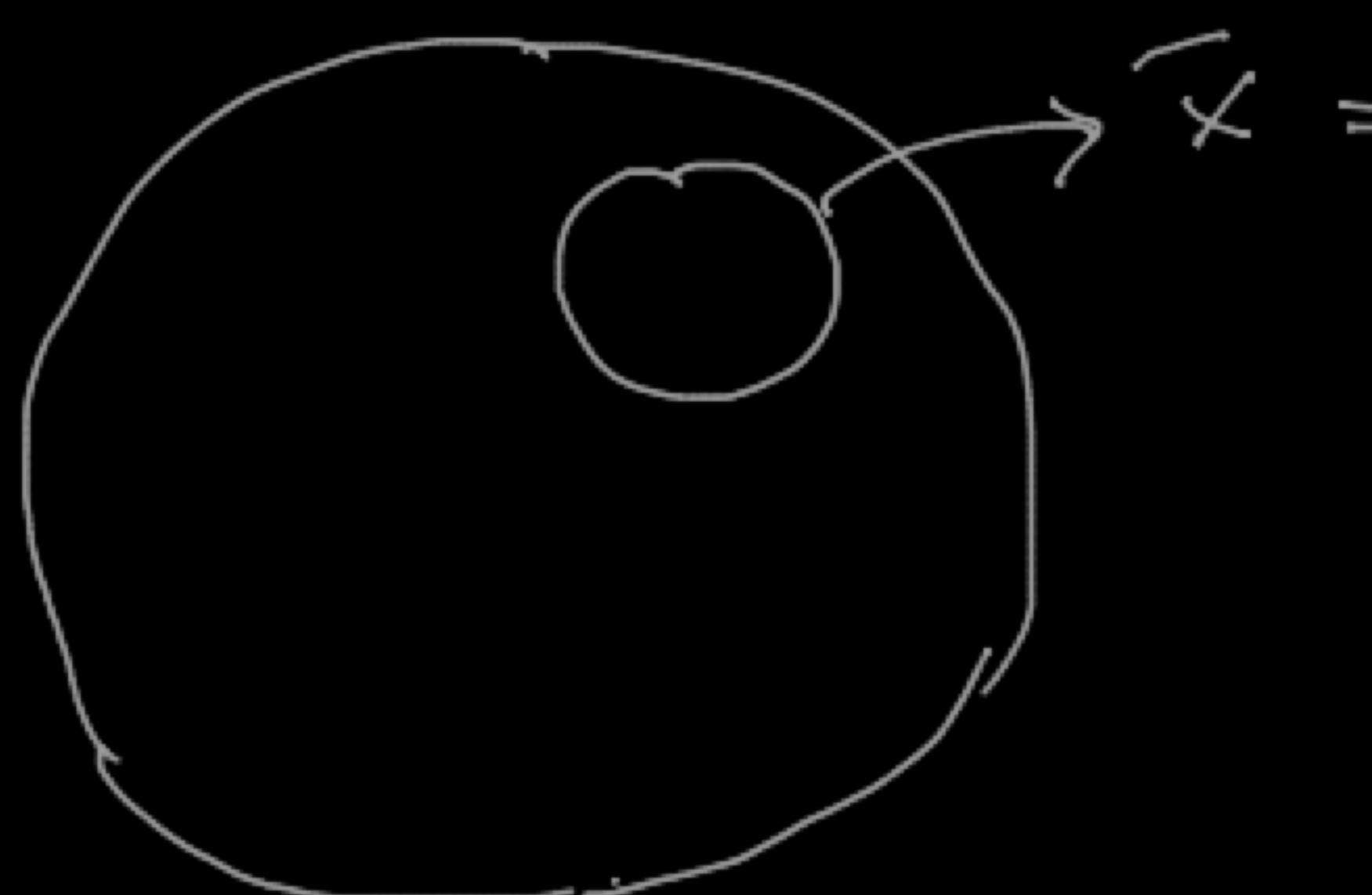
$$\sigma_{\bar{x}} = \sigma_{\text{pop}} / \sqrt{n}$$

Always Normally distributed

Distr of \bar{x} Sample



$$\frac{30,000}{100,000} \checkmark$$



Point Estimate -

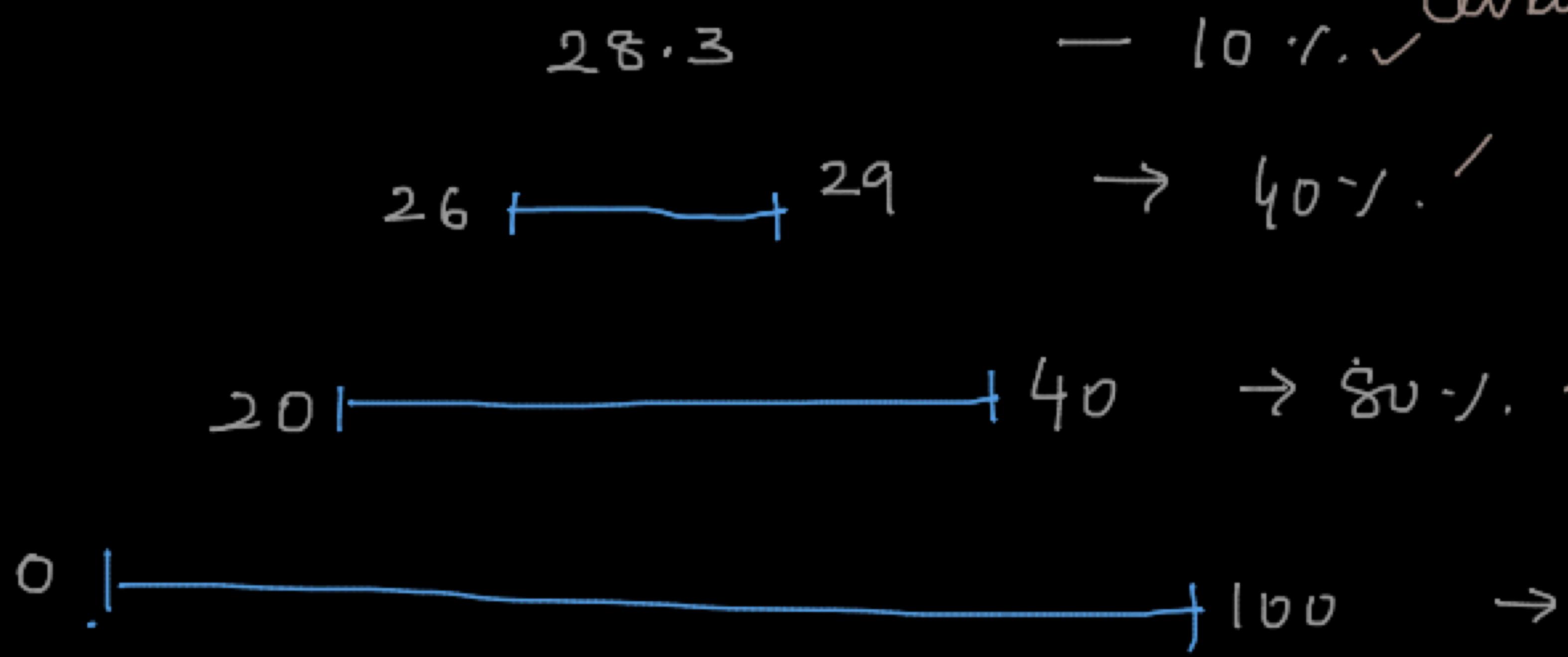
$$\text{Avg. Income} = \bar{x}$$

$$\text{Avg. Income} = \bar{x} \pm \Delta \rightarrow ?$$

Confidence Level

↳ Range Estimate -

$$\begin{aligned} 90\% &\rightarrow C(0.90) \\ 95\% &\rightarrow C(0.95) \\ 98\% &\rightarrow C(0.98) \end{aligned}$$



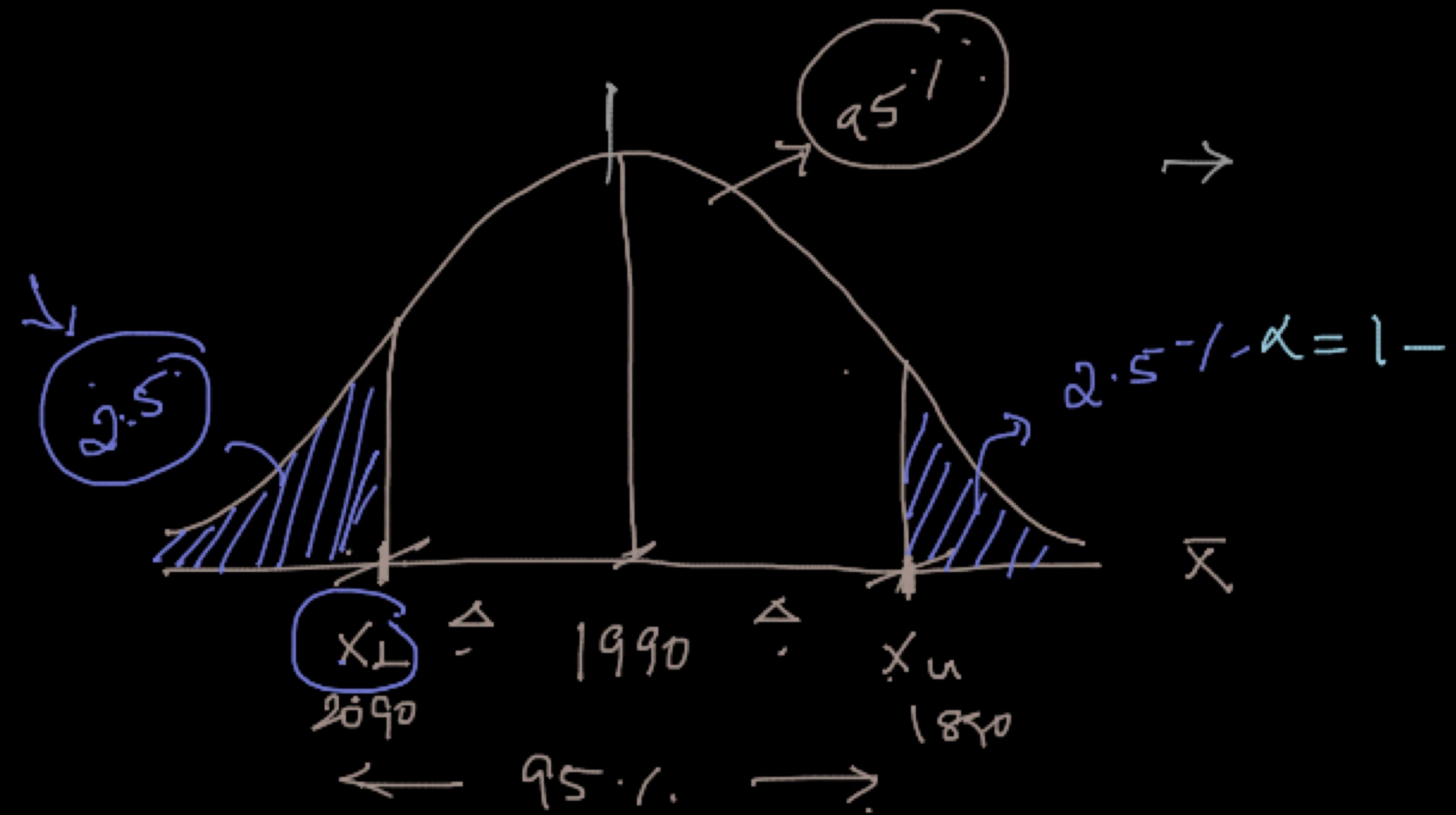
$\alpha \rightarrow \text{Significance}$

$$\alpha = 1 - C$$

$$\alpha = 1 - 0.95$$

$$= 0.05$$

$$\Delta = Z_{\alpha/2} \cdot \frac{\sigma_{\text{pop}}}{\sqrt{n}}$$



$\bar{x} \pm \Delta$,
 \rightarrow Confidence level = 95%
 $C = 0.95$ $\alpha = 0.05$
 $\alpha/2 = 0.025$

$\bar{x} + \Delta$, $\bar{x} - \Delta$

$(1990 + 100, 1990 - 100)$
 $(1990, 1890)$

Range Estimate = $\bar{x} \pm \Delta$. || Standardise

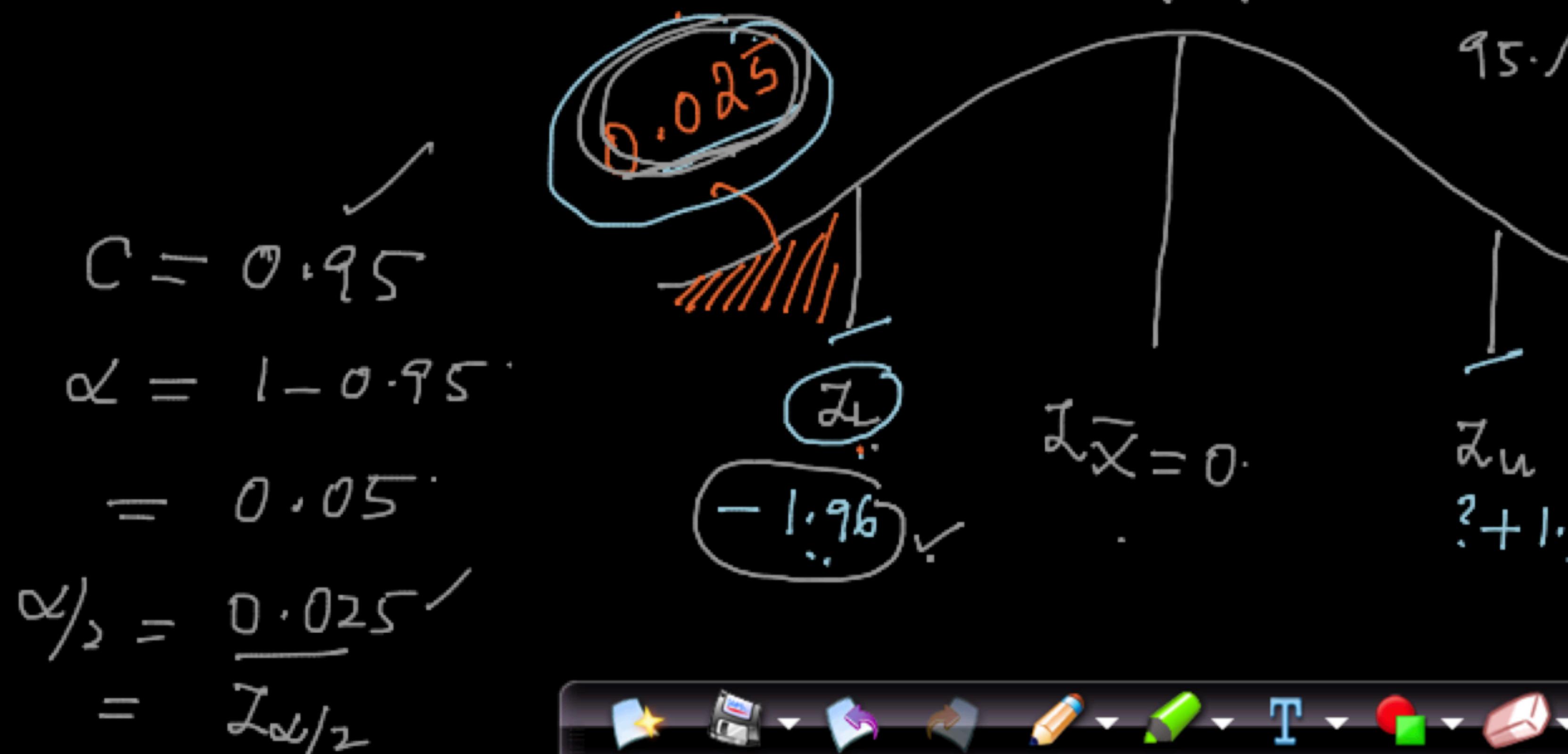
$$= \left[1990 \pm 1.96 \cdot \frac{2500}{\sqrt{140}} \right] \rightarrow \left[1576, 2404 \right]$$

$$\Delta = \left(Z_{\alpha/2} \right) \frac{\sigma_{pop}}{\sqrt{n}}$$

$$\Delta = \pm 1.96 \cdot \frac{\sigma_{pop}}{\sqrt{n}}$$

$$= \pm 1.96 \cdot \frac{2500}{\sqrt{140}}$$

$$= \pm 414.$$



$$C = 0.95$$

$$\alpha = 1 - 0.95$$

$$= 0.05$$

$$\alpha/2 = 0.025$$

$$= Z_{\alpha/2}$$