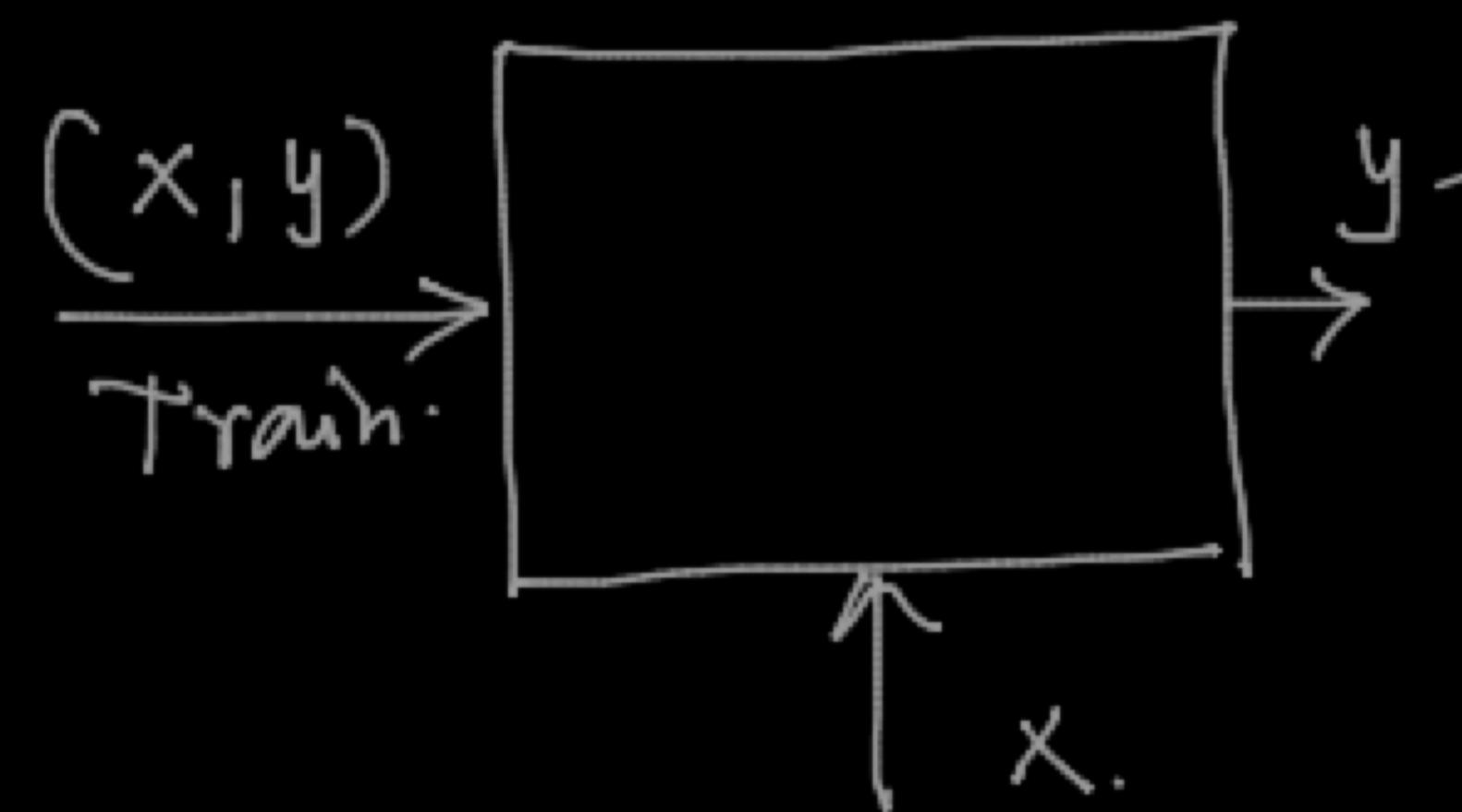




## Model Validation Techniques

	$x$			$y$
1	$x_1$	$x_2$	$x_3$	$\dots$
2	✓	✓	✓	$x_{100}$
3	-	-	-	-
4	-	-	-	-
5	-	-	-	-
:	-	-	-	-
$n=1000$	-	-	-	-



# Create the model

model = LinearRegression()

# Train the model

model.fit(x, y)

— Estimate the model parameters ( $\beta$ 's)

# Predict the outcomes

model.predict(x)

$\hookrightarrow \hat{y}$

✓ MSE

✓ RMSE =  $\sqrt{\text{MSE}}$

How well the model performs on  
‘UNSEEN DATA’.



Validate the Model -

```
Xtrain, Ytrain, Xtest, Ytest = train-test-split(X, y, 0.20)
# Create the Model
final-model = LinearRegression() ✓
↳ python code
```

so,  $\begin{bmatrix} i \\ 1 \\ 2 \\ 3 \\ \vdots \\ n=1000 \end{bmatrix}$

$X_{\text{train}}$ :  $\begin{bmatrix} x_1 & x_2 & x_3 & \dots & x_{\text{all}} \end{bmatrix}$

$y$ :  $\begin{bmatrix} y \\ y_{\text{train}} \\ \vdots \\ y_{\text{train}} \end{bmatrix}$

$\hat{y}$ :  $\begin{bmatrix} \hat{y} \\ \hat{y}_{\text{train}} \\ \vdots \\ \hat{y}_{\text{train}} \end{bmatrix}$

$y - \hat{y}$ :  $\begin{bmatrix} \text{Training Error} \\ \text{Training Error} \\ \vdots \\ \text{Training Error} \end{bmatrix}$

# Train the model

```
final-model.fit(X-train, Y-train)
```

# Predict for training data (Seen data)

```
final-model.predict(X-train) → Ytrain
```

# Predict for unseen data

```
final-model.predict(X-test) ↳  $\hat{Y}_{\text{test}}$ 
```

Training Error ↓ ✓  
Testing Error ↓

Training Error ↓ }  
Testing Error ↑ } → overfitting

Training Error ↑ } underfitting  
Testing Error ↑ }

## Errors $\rightarrow$ Regression

### Ideal

- Low Training Error
- Low Testing Error

### Overfitting

- $\rightarrow$  Low training Error
- $\rightarrow$  High testing Error

### Underfitting

- High Training Error
- High Testing Error

## Accuracy $\rightarrow$ Classification

High training Acc

High testing Acc.

High training Acc

$\rightarrow$  Low testing Acc

Low training Acc

Low testing Acc

$$\text{df} = \left[ \begin{array}{c|ccc} & \xleftarrow{\quad} & \xrightarrow{\quad} & \\ & H_p & Vol & Wt \\ \hline \begin{bmatrix} 80/1 \\ \vdots \\ 20/1 \end{bmatrix} & \times & \begin{bmatrix} \end{bmatrix} & \begin{bmatrix} Mpg \\ \vdots \\ \end{bmatrix} \end{array} \right]$$

$$\text{df} [Mpg] = y$$

Metric -  
Regressions → Errors -

MSE, RMSE, MAE

Classification → Accuracy -

✓ ✓  
80 - 20

75 - 25

66 - 33%  
 $x_{\text{train}}, y_{\text{train}}, x_{\text{test}}, y_{\text{test}}$  ↑ train-test-split ( $\frac{x, y}{=}$ , 20%)

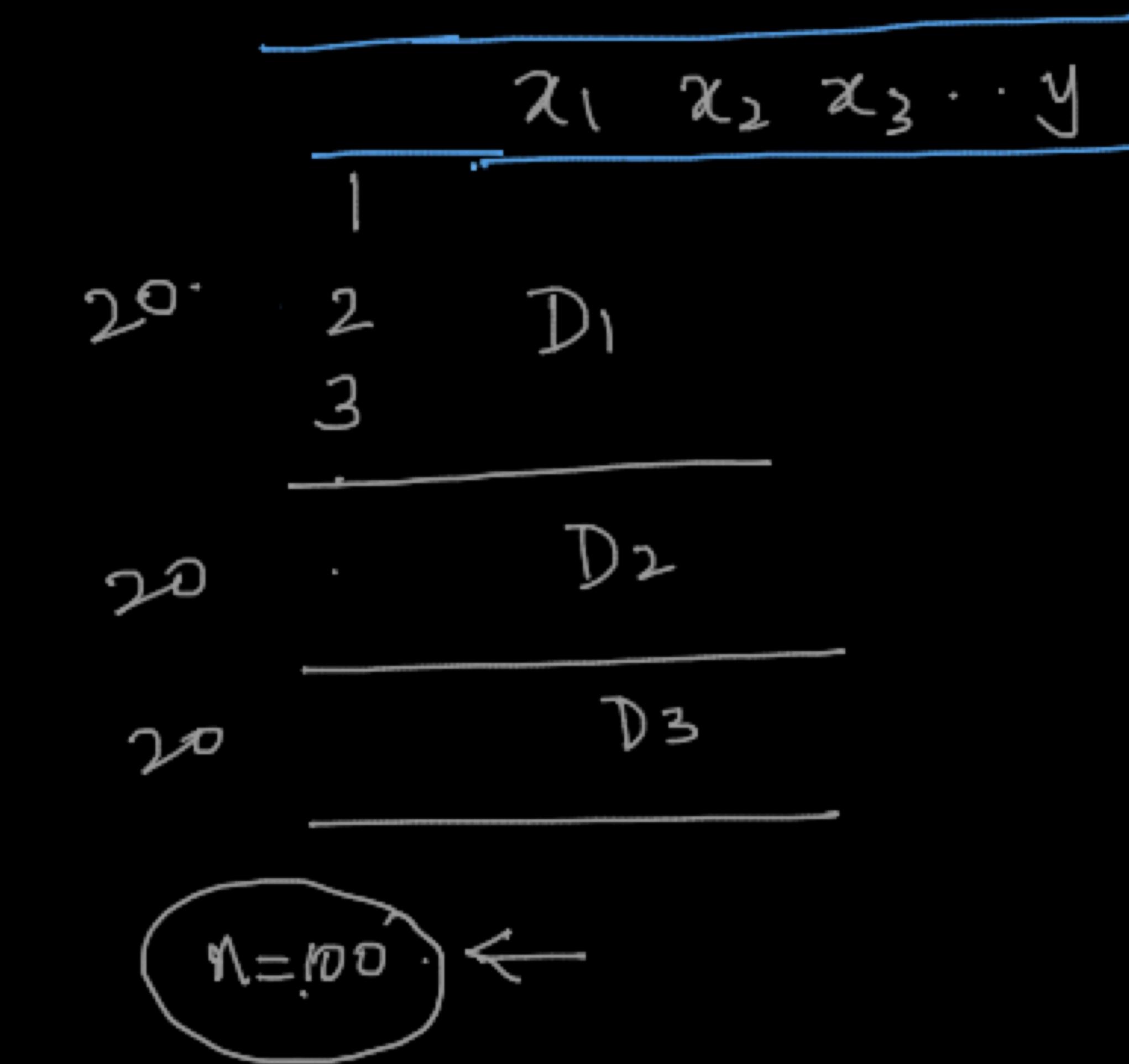
↳ % of testing data

Sqft Bed Price -  
 1 (1000 1 53)  
 2 (1500 2 65) → testing  
 3 (1800 3 73)  
 4 (1400 2 55)

5 (1700 1 67)

	$y$	$\hat{y}$
-	Yes	Yes ✓
-	Yes	No ✗
→	No	No ✓
→	No	Yes ✗
		—

$x_{\text{test}} 1500 \quad 2 \quad 65 \quad y_{\text{test}}$   
 $1400 \quad 2 \quad 55$



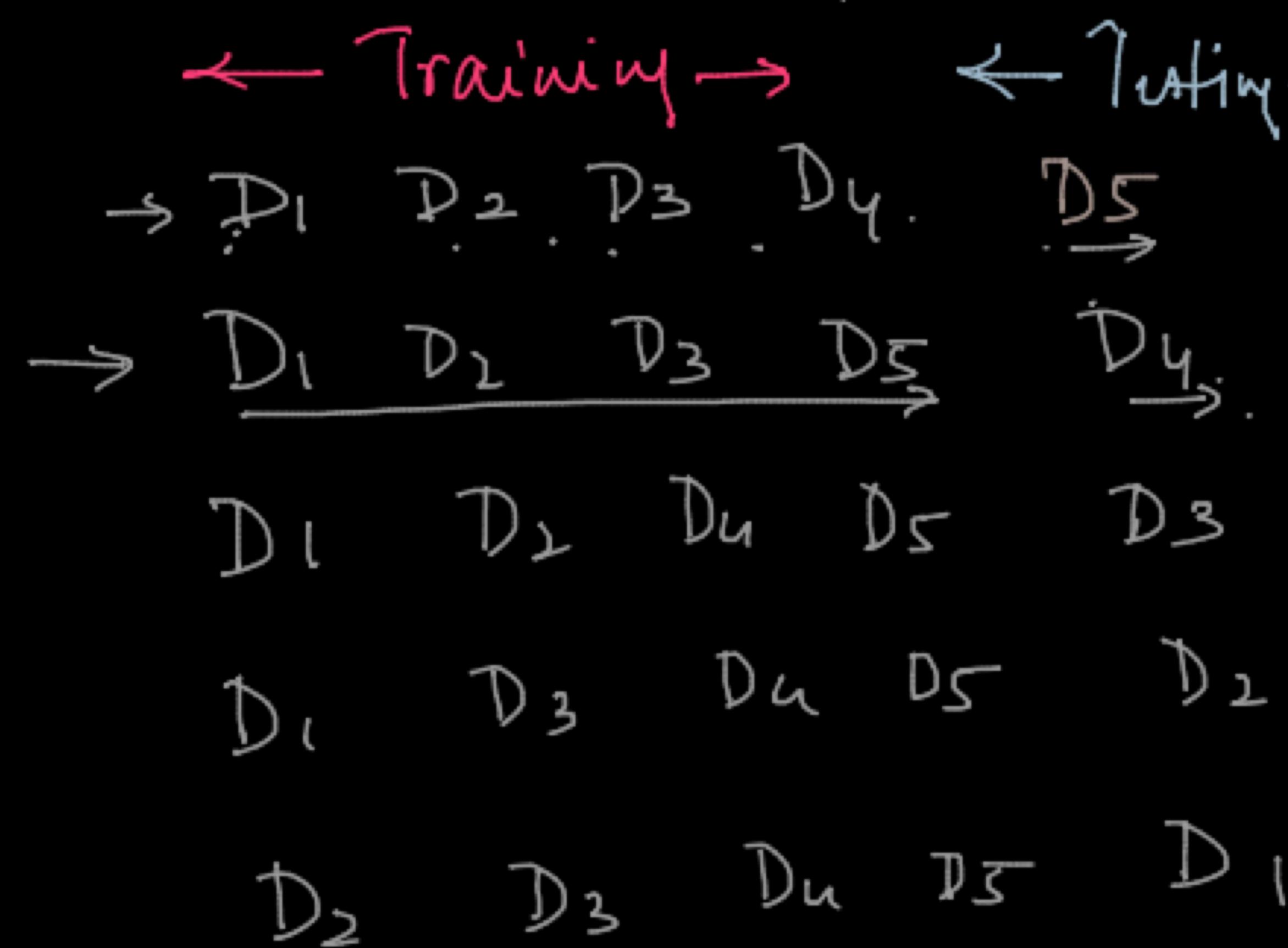
K-Fold Validation

$k$  - Hyperparameter

$\rightarrow k = 5$ ; 20%  $\rightarrow$  testing.

$$n = 100; k = 5;$$

$$D_1 = 20$$



10.20 AM

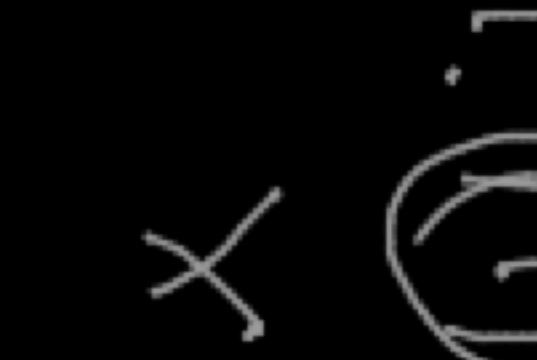
Loop

— Leave one out Validation

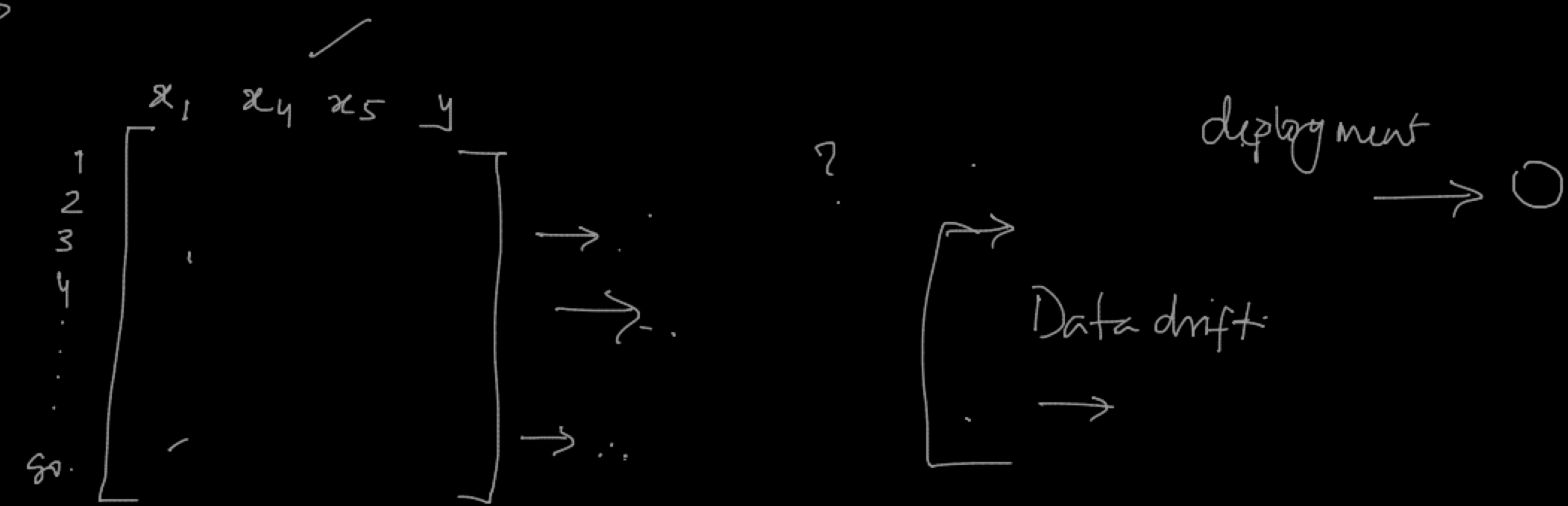
	$x_1$	$x_2$	$x_3$	$y$	Training	Testing
1					1 to 9	10
2					1 - 8, 10	$\rightarrow$ 9 <sup>th</sup>
3					1 - 7, 9-10	8 <sup>th</sup>
4					1 - 6, 8-10	7 <sup>th</sup>
5						
6						
7						
8						
$\rightarrow$	1 - - - -	$y - \hat{y}$	$= E_1$			
-	10	( - - - )	$\hat{y} \rightarrow$ Err			

feature Engineering

$x_1 \cancel{x_2} x_3 y$

X 

—  
—  
—



20%      80%       $\rightarrow$  y

10%      90%       $\rightarrow$  surf

50 48, 3

100.      50% —  $\rightarrow$  ( = )  $\rightarrow$  underflow

50% —