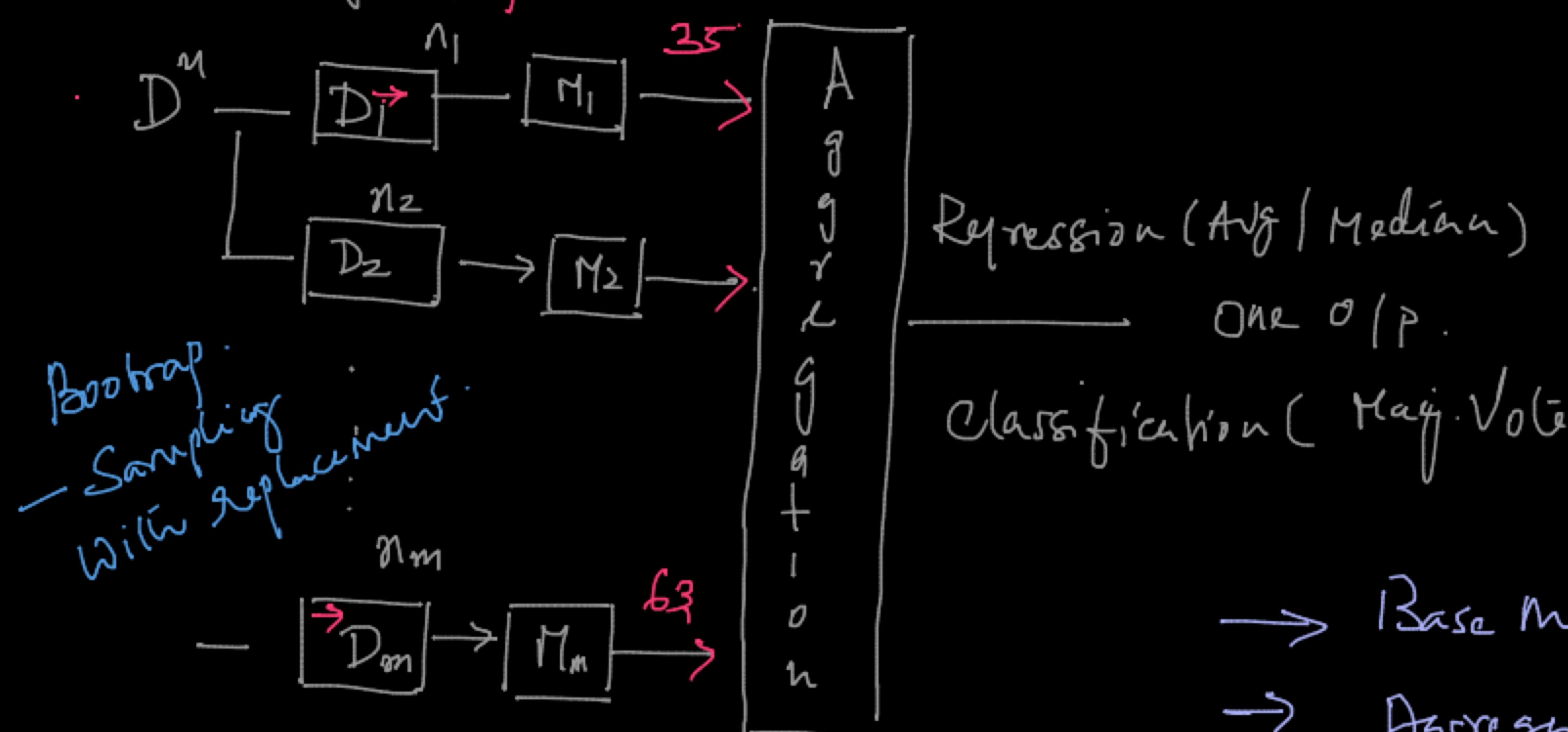


Ensemble Models

1. Bagging \rightarrow Bootstrapped Aggregation
2. Boosting
3. Stacking

D_{bo}'s

Bagging



Random Forest

- All base models are D_1 's
- Feature Sampling + Row Sampling

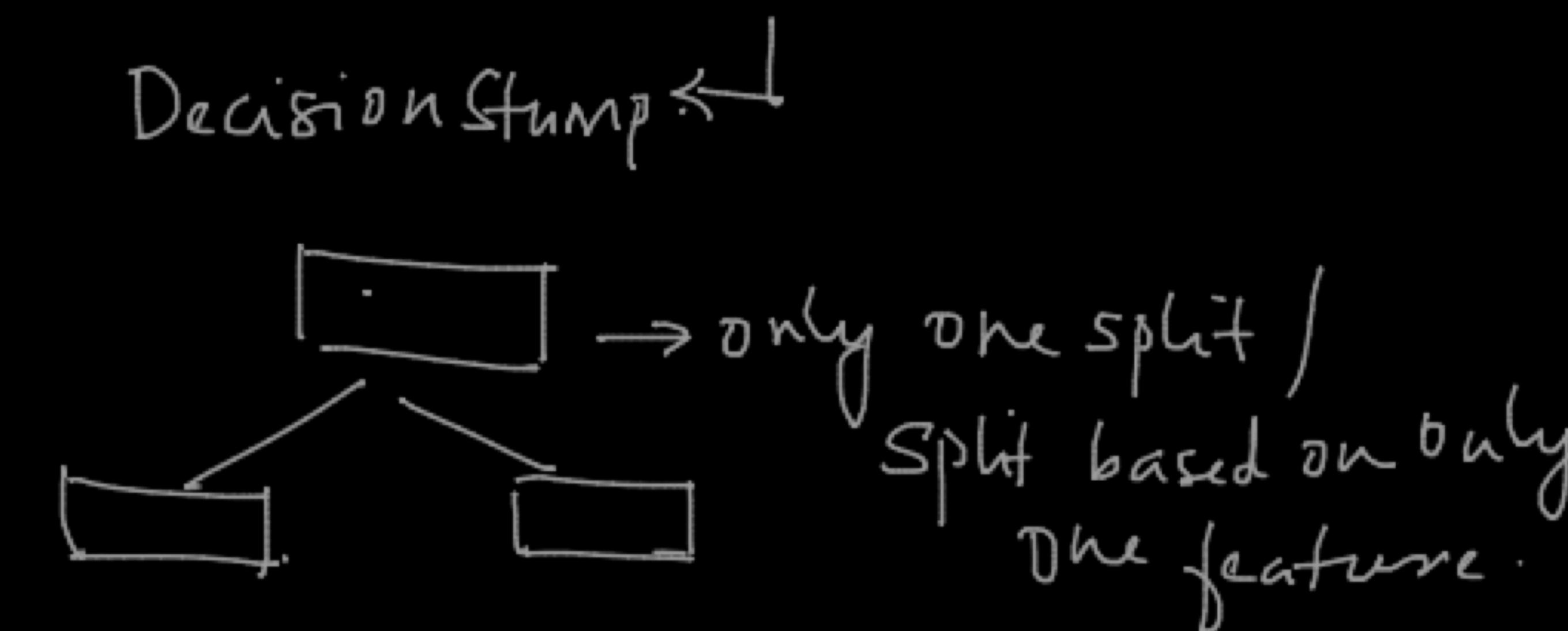
Regression (Avg / Median)
Classification (Majority Vote).

- \rightarrow Base models low bias / high variance
- \rightarrow Aggregation reduces variance

→ parallelizable

Boosting

- Sequential Model / Additive Model.
- Make a rough prediction of y .
- Subsequent models will work to reduce the errors from prev. models.
- Base models: High Bias / Low Variance.



ADABoost.

- Classification.
- Wrongly classified records are given high-weightage.
- Individual models are also given weightage based on their performance.

Gradient Descent
— minimize the 'loss function'
(Errors / Residual)

$$\hat{y} = \beta_0 + \beta_1 x$$

$$\text{residual} = y - \hat{y}$$

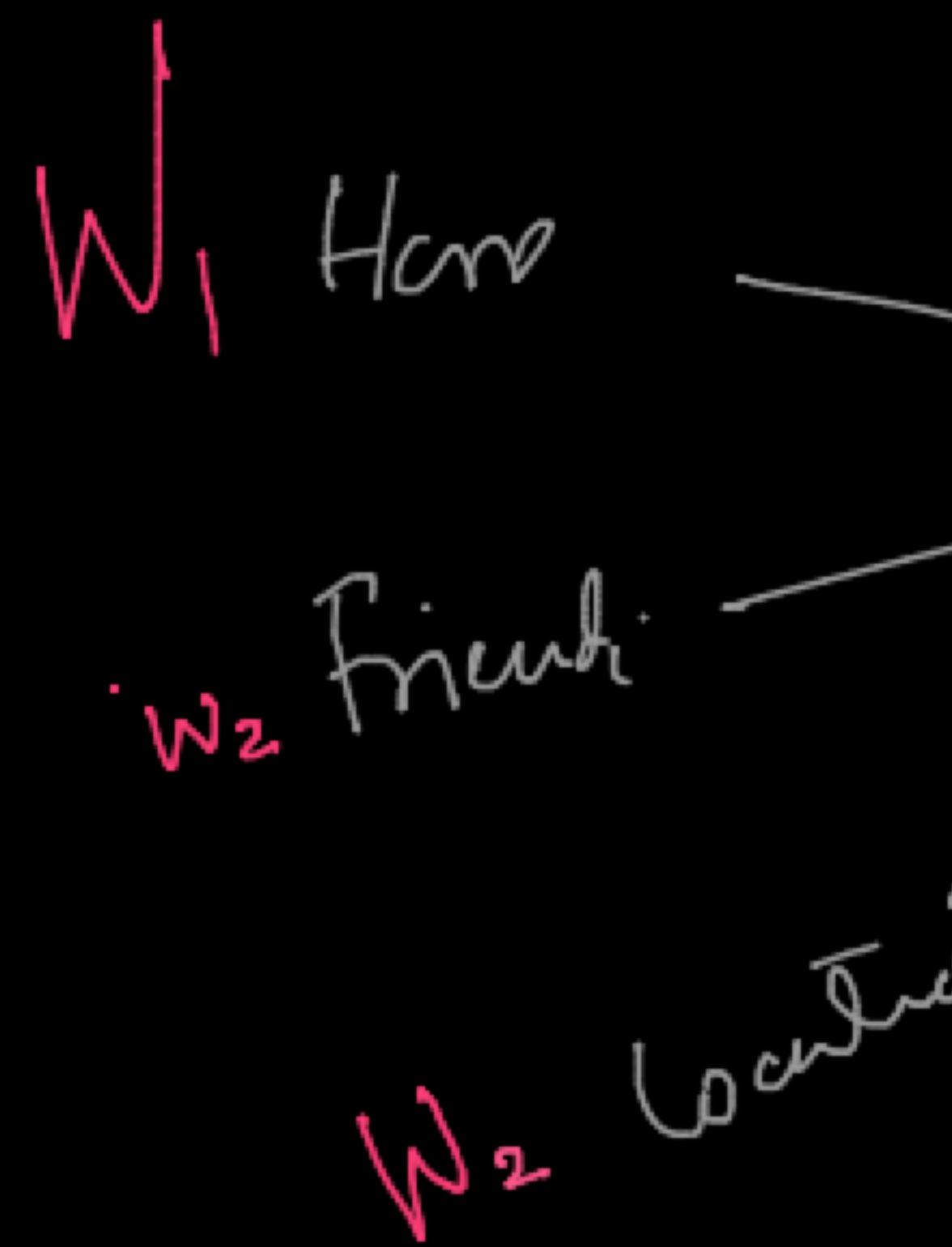
OLS.

→ line of best fit → loss fn. $\Rightarrow (y - \hat{y})^2$ → Minimum Error.
 → (β_0, β_1) → minimum squared loss. in the model.

$$SSE_{(L)} = \left[y - (\beta_0 + \beta_1 x) \right]^2$$

Find β_0, β_1 which will minimize the loss fn.

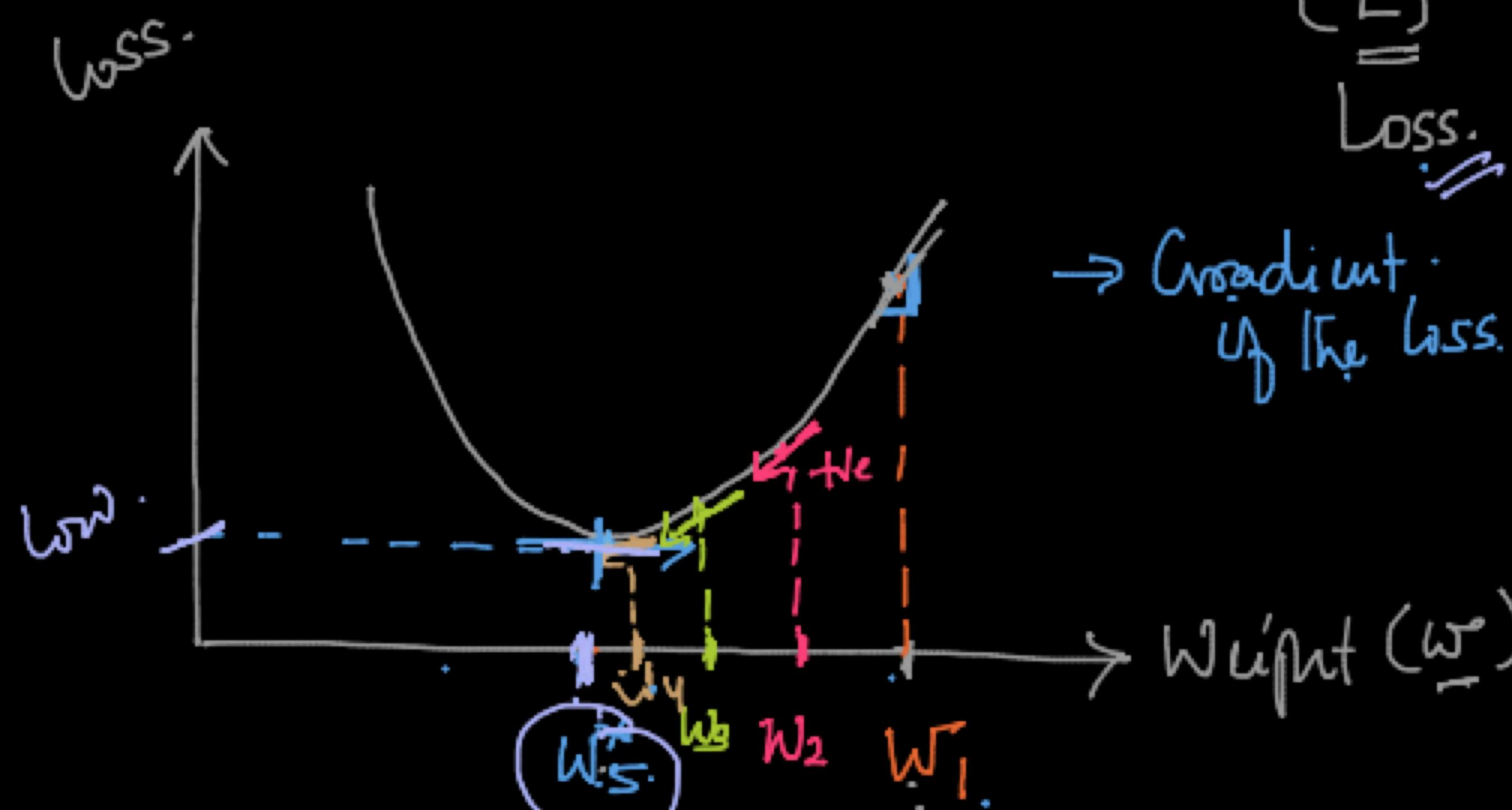
B's → Weights.



$$y = w_1 x_1 + w_2 x_2 + \dots + b.$$

↳ Weightage given to feature x_i ,
→ w_i

$$y = w x + b$$



$$w_6 = w_5 - \left(\frac{\partial L}{\partial w} \right)_{w_5} = 0.$$

$$w_6 = w_5$$

$$(dy/dx) \rightarrow \text{gradient}$$



$$w_3 = w_2 + - \left(\frac{\partial L}{\partial w} \right)_{w_2}$$

$$\leftarrow \Delta w$$

$$w_4 = w_3 - \left(\frac{\partial L}{\partial w} \right)_{w_3}$$

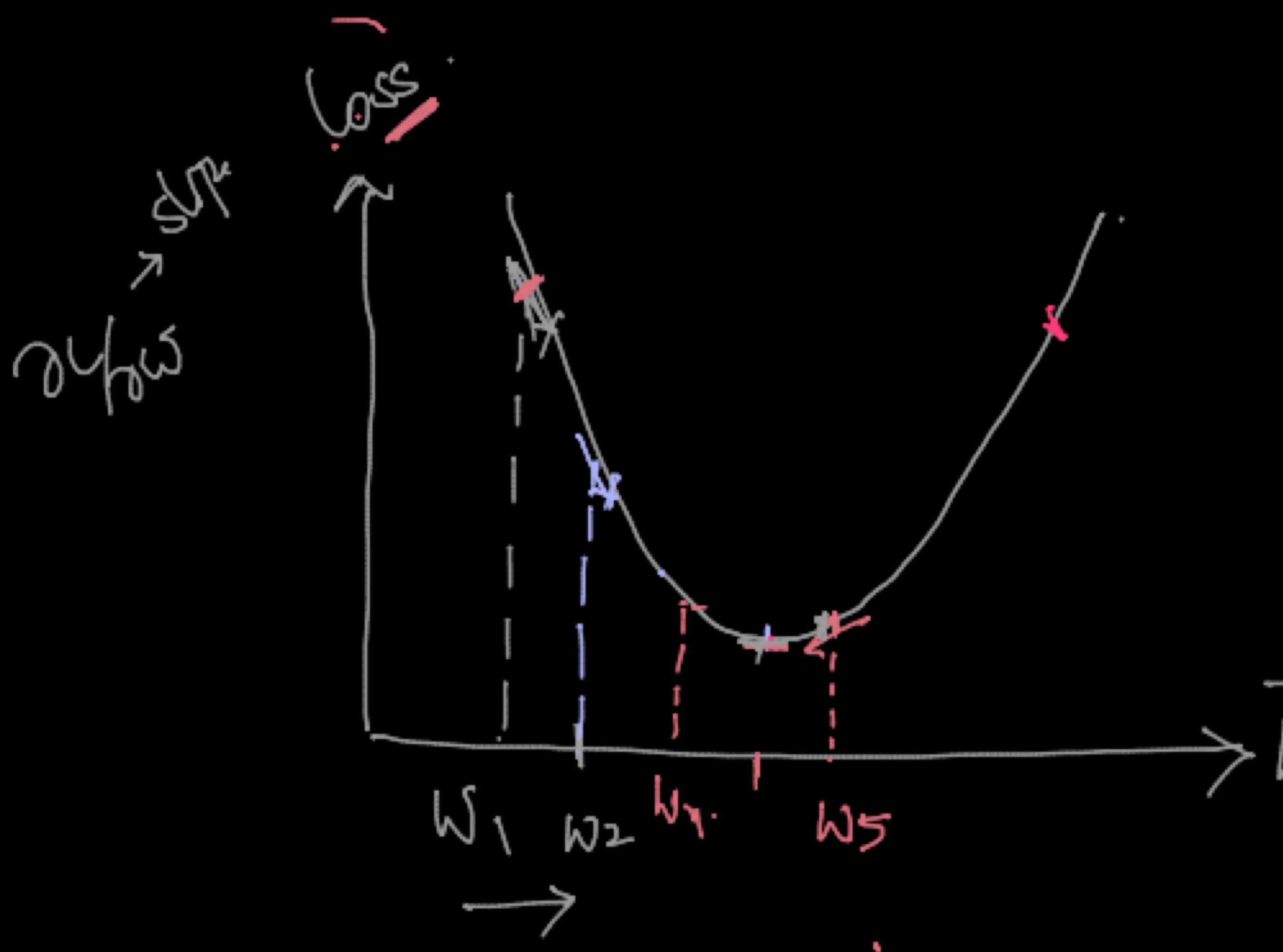
$$= w_3 - \Delta w$$

$\left(\frac{\partial L}{\partial w} \right)_{w_1} \rightarrow$ Gradient of the loss fn wrt. the weight at $w = w_1$

update the weight → +ve.

$$w_2 = w_1 + \left(- \frac{\partial L}{\partial w} \right)_{w_1}$$

$$w_2 = w_1 - \Delta w$$

Neural \rightarrow

$$w_2 = w_1 + \left[-\frac{\partial L}{\partial w} \right]_{w_1} - (\text{v.L}) \xleftarrow{\Delta w \rightarrow}$$

$$\rightarrow \beta_0 | \beta_1$$

$$w_2 = w_1 + \Delta w$$

lossfn \Rightarrow (Hinge Loss)statsmodels.api.fr \rightarrow Ols

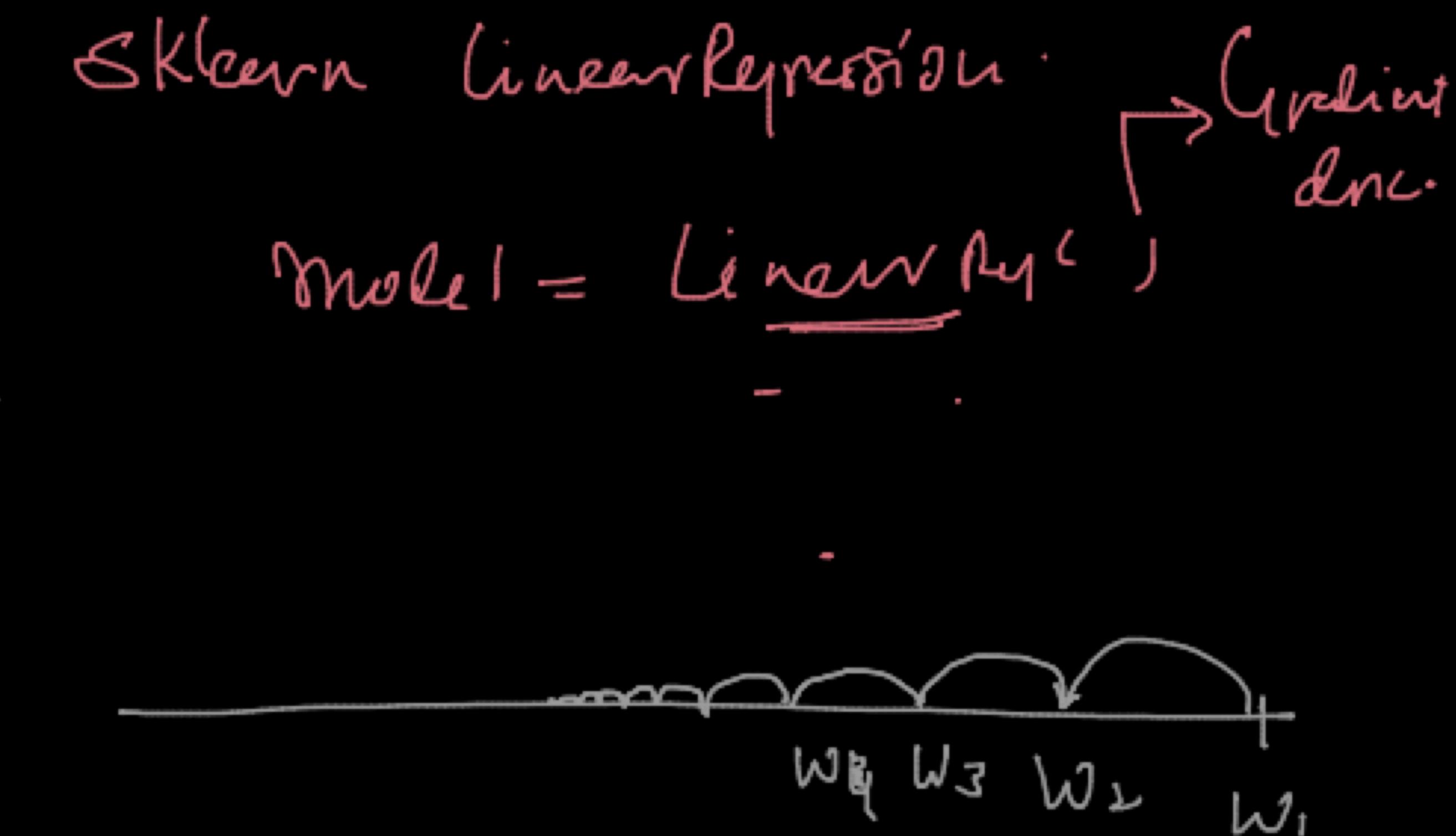
- Step 1: Randomly choose w_1
- Step 2: Find the gradient of the loss fn at that w .
- Step 3: Update the Weights.
- Repeat until Convergence

$$w_{\text{new}} = w_{\text{old}} + \left[-\frac{\partial L}{\partial w} \right]_{w_{\text{old}}} \xleftarrow{\Delta w \rightarrow}$$

$$\text{Convergence} \Rightarrow \boxed{\Delta w = 0 \pm \epsilon_w}$$

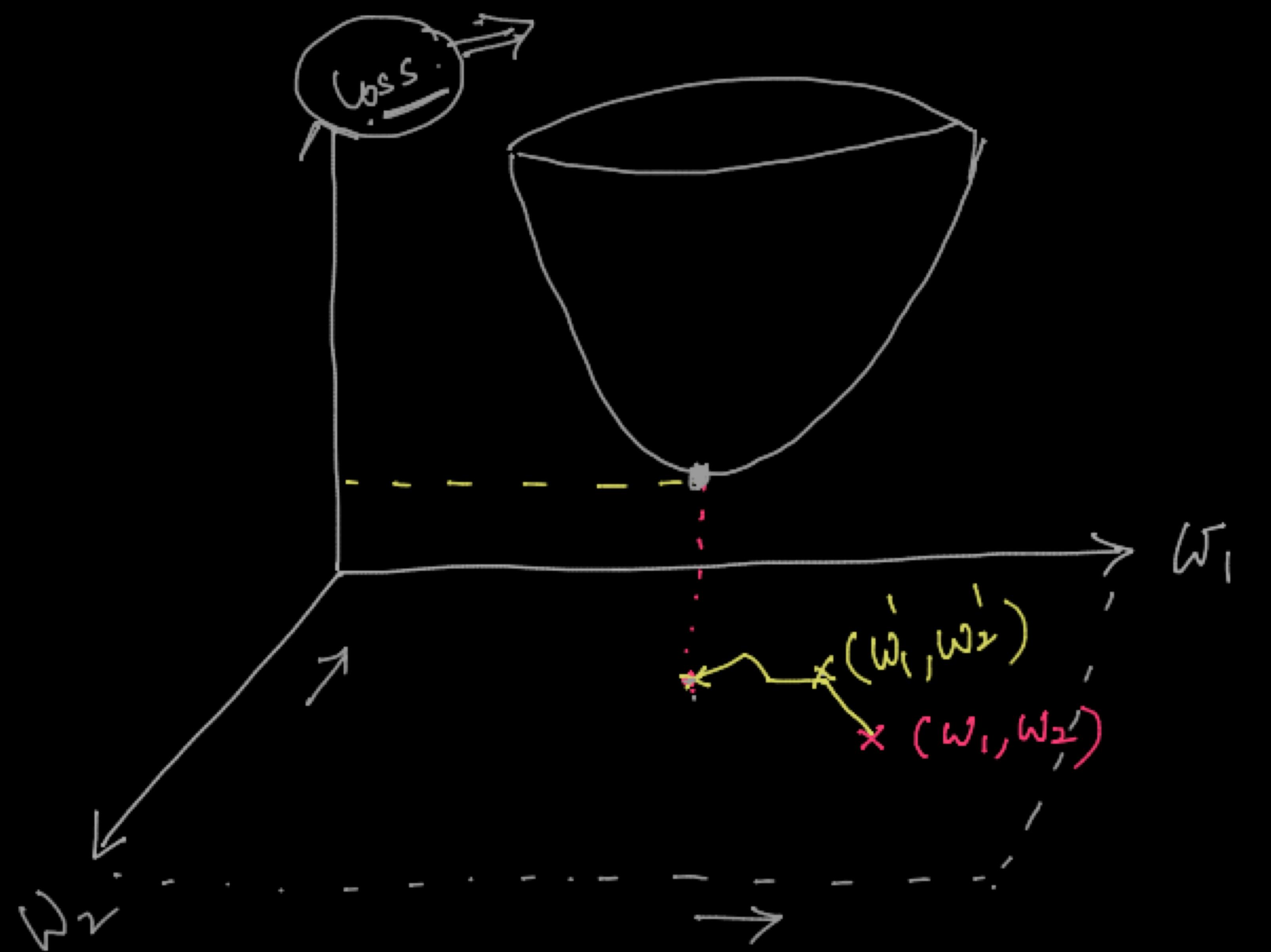
x | y

max-iterations = 400



Gradient desc.

Model = Linear Reg



$x_1 \ x_2 \ x_3 \ \dots \ x_d.$

$w_1, w_2 \rightarrow$ Randomly choose

Update the weights simultaneously

$$w_1' = w_1 + [-\frac{\partial L}{\partial w_1}]_{w_1} \rightarrow x_1 \ x_2 \ y.$$

$$w_2' = w_2 + [-\frac{\partial L}{\partial w_2}]_{w_2}$$

$$(w_1', w_2', w_3', \dots, w_n')$$

\times

$$(w_1, w_2, w_3, \dots, w_n)$$

$\xrightarrow{x_0=1}$

$$y = \beta_0 x_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3.$$

$$y = \overbrace{w_1 x_1}^1 + \overbrace{w_2 x_2}^1 + \overbrace{w_3 x_3}^1 + \dots + \overbrace{w_d x_d}^1.$$

Any \rightarrow SVM \rightarrow
 \rightarrow Logist.
linearly
Decision.

Logloss.

Minimize / maximize
obj. fn
— find the model params
which will give you
minimum.

w's \rightarrow "Hinge loss" ✓
 \hookrightarrow Gradient.

