

## Descriptive Statistics .

### 1. Measures of Frequency

- Counts, percentage , proportions

### 2. Measures of Central tendency

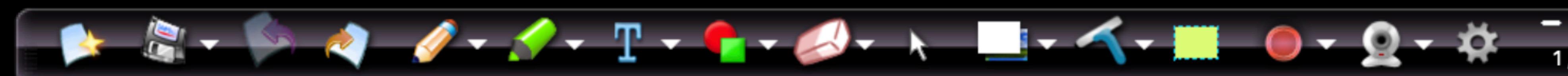
- Mean, Median, Mode

### 3. Measures of dispersion

- Variance, Standard deviation, range

### 4. Measures of position

- Percentile, Quartiles, deciles, - -



Random Variable.

— Probability distributions.

Probability = Chance of an event occurring -

= 0 to 1 (0 - 100%).

= -ve probabilities not possible -

$$P(H) = \frac{1}{2} = \frac{\text{# No. of Fav. outcomes}}{\text{Total No. of possible outcomes}} \rightarrow \text{Sample Space}$$

↳ Experiment

$$P(X=1) = \frac{1}{6}$$

Tossing a coin =  $\{H, T\}$  → discrete Random Variable

Rolling dice =  $\{1, 2, 3, 4, 5, 6\}$  → Sample Space contains only finite no. of options.

$$\text{Prob}(1) \Rightarrow \frac{1}{6}$$

Continuous Random Variable  $\leftarrow$

$\rightarrow [150, 151, 152, 153]$  ]  
120  
190 .

$X \rightarrow$  Random Variable used to hold the height of student

[150, 150.01, 150.001, 153.5, ...]  $\hookrightarrow \infty$

$$P(\underbrace{X = 153.5}) = \frac{1}{\# \text{ total no. of possible outcomes}} = \frac{1}{\infty} = 0$$

(153 <  $x < 154$ )  $\rightarrow$  Finite Value

$X \rightarrow$  can take a set of possible values

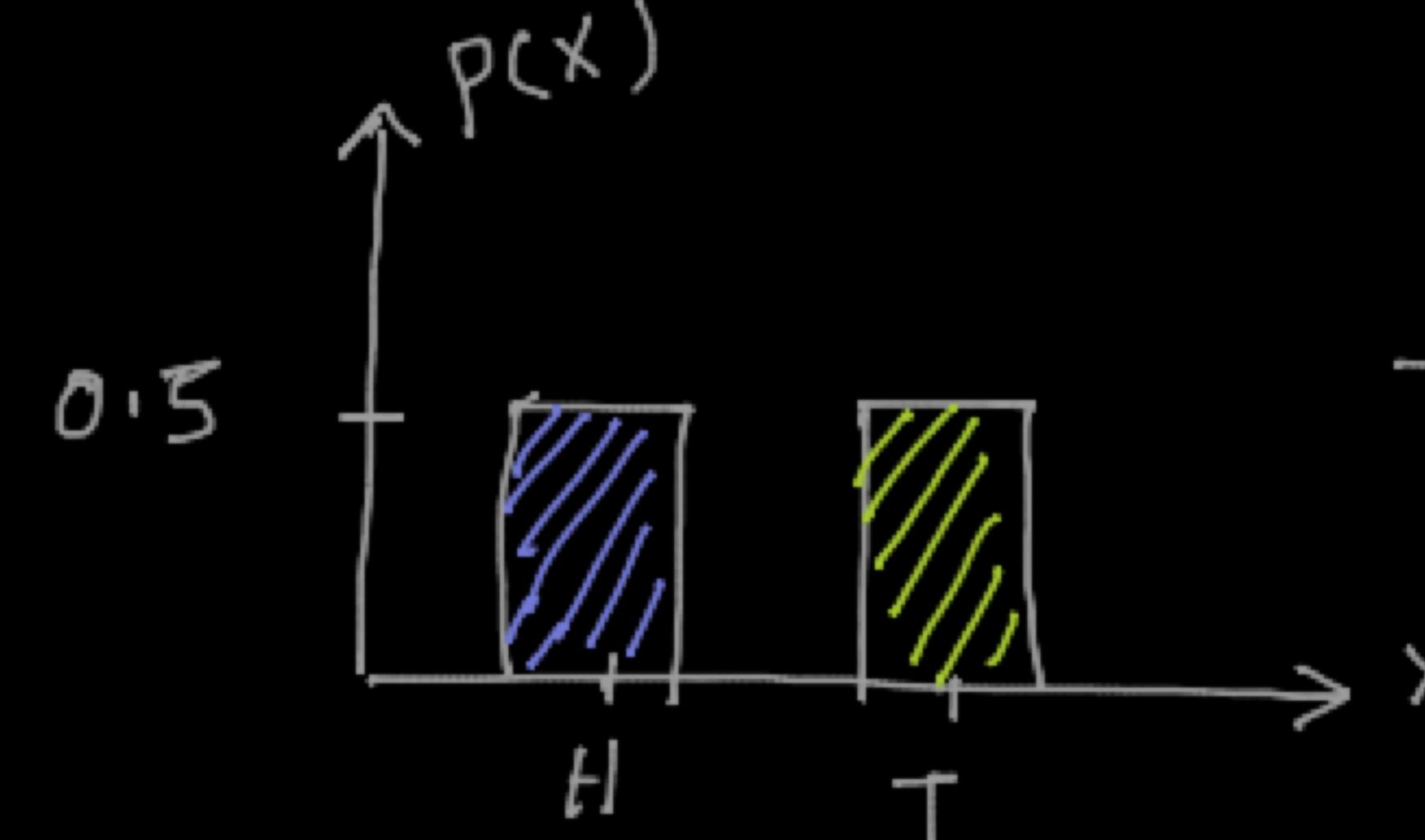
$\rightarrow$  probability distribution of  $X$ .

Discrete  
Random  
Variable

$$X = [H, T]$$

$\uparrow \uparrow$

$$P(X=H) = 0.5 ; P(X=T) = 0.5$$



$\rightarrow$  uniform distribution

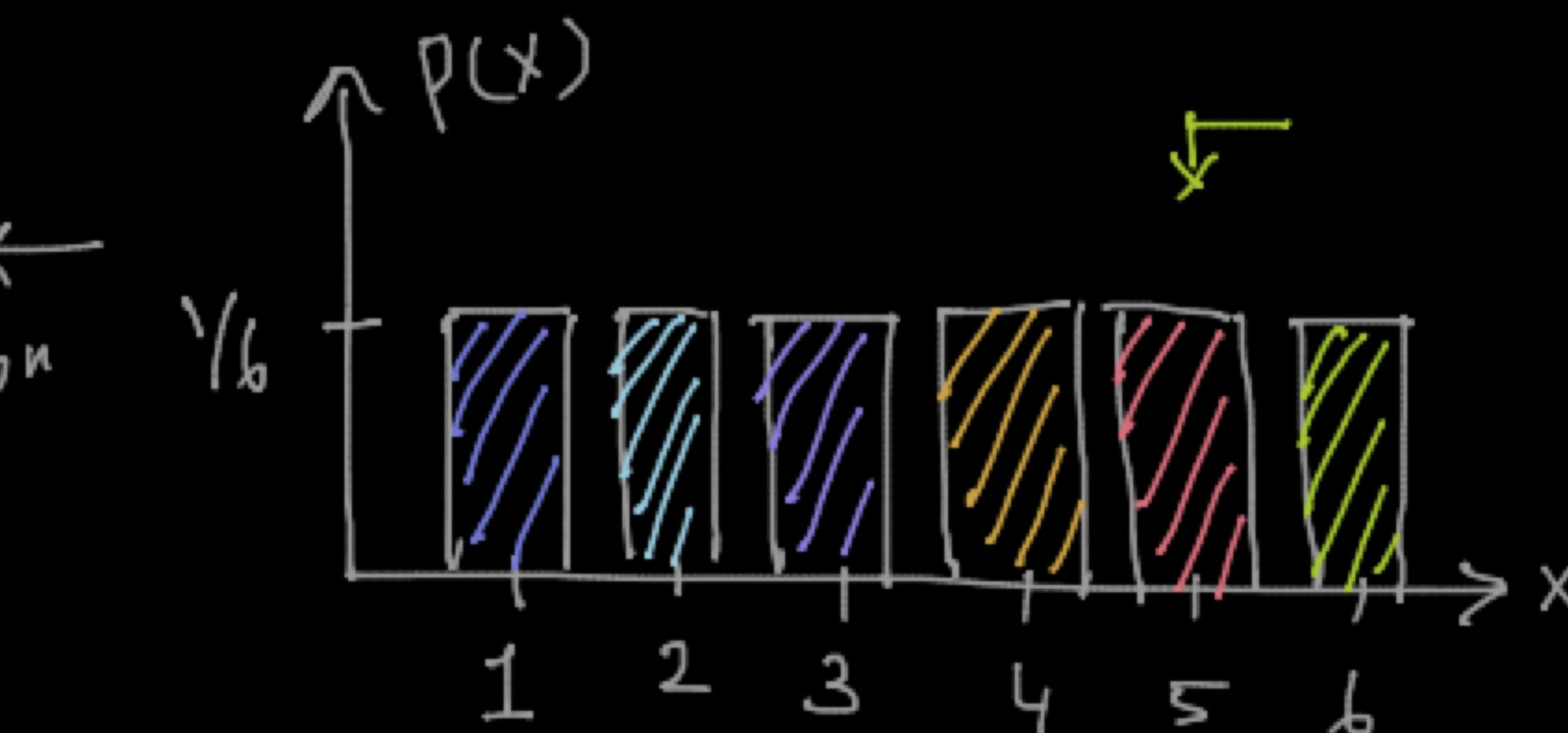
$\hookrightarrow$  Bernoulli distribution

Continuous  
Random Variable

$$X = [1, 2, 3, 4, 5, 6]$$

$$P(X=1) = \frac{1}{6} ; P(X=3) = \frac{1}{6}$$

$$P(X=2) = \frac{1}{6} ; P(X=4) = \frac{1}{6}$$



## uniform distribution

- Every possible outcome has equal Prob. of occurring .

## Bernoulli distribution

- repeat an exp. only ONCE
- There should be only 2 possible outcomes .

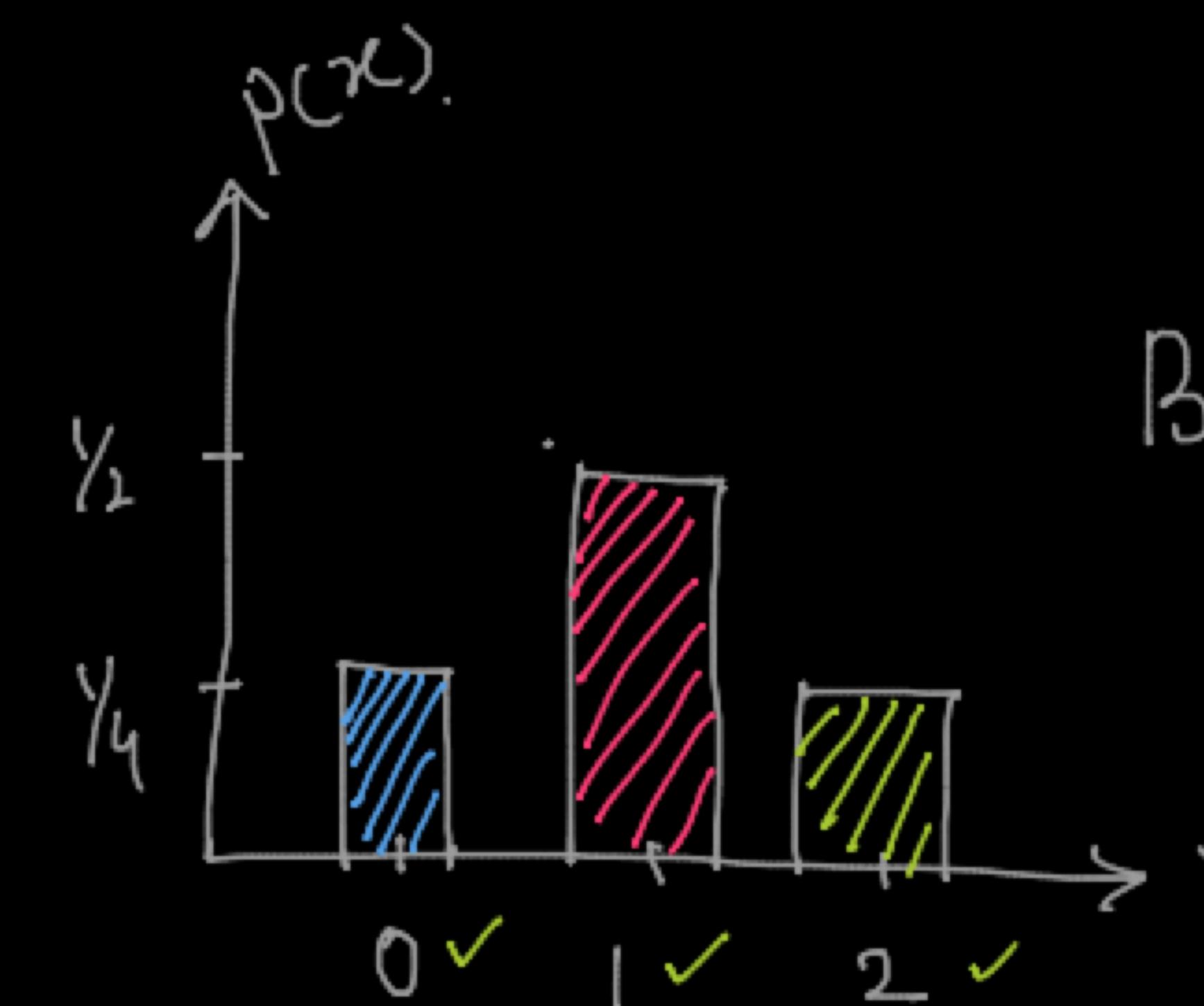
## Binomial distribution

- Toss a coin twice ; thrice, - - -



$$x=0; \quad x=1, \quad x=2, \quad x=3$$

$\left\{ \begin{array}{l} H \quad H \Rightarrow \frac{1}{4} \\ H \quad T \quad \} \frac{2}{4} \\ T \quad H \quad \} \frac{2}{4} \\ \rightarrow \underline{T} \quad \underline{T} \quad \frac{1}{4} \end{array} \right.$



Binomial distribution

Prob. dist.  $\rightarrow$

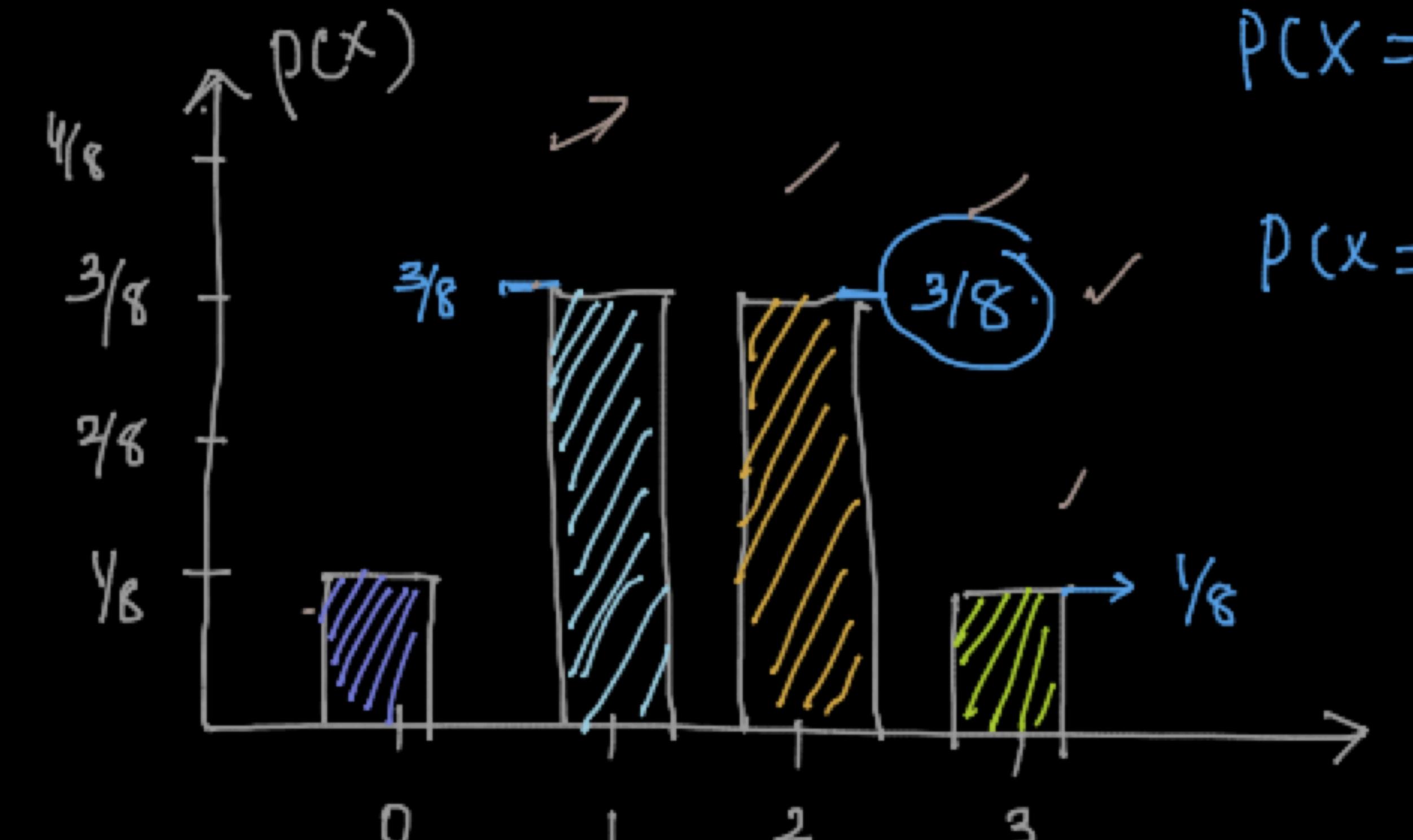
$$= \frac{n!}{(n-x)! x!} p^x q^{n-x}$$

50 times, 33 Heads

$\begin{matrix} & & \\ \cancel{H} & H & H & \checkmark \\ \checkmark & \cancel{H} & H & T \\ \checkmark & H & T & H \\ H & T & T & \checkmark \\ \checkmark & T & H & H \\ T & H & T & \checkmark \\ T & T & H & \checkmark \\ T & T & T & \checkmark \end{matrix}$

$P(x=0) \quad P(x=1) \quad P(x=2) \quad P(x=3)$   $\rightarrow$  No. of success

$\rightarrow$  Prob. of success (0.5)  $\rightarrow$  Prob. of fail (0.5)



$P(x=2) \rightarrow 3$  times

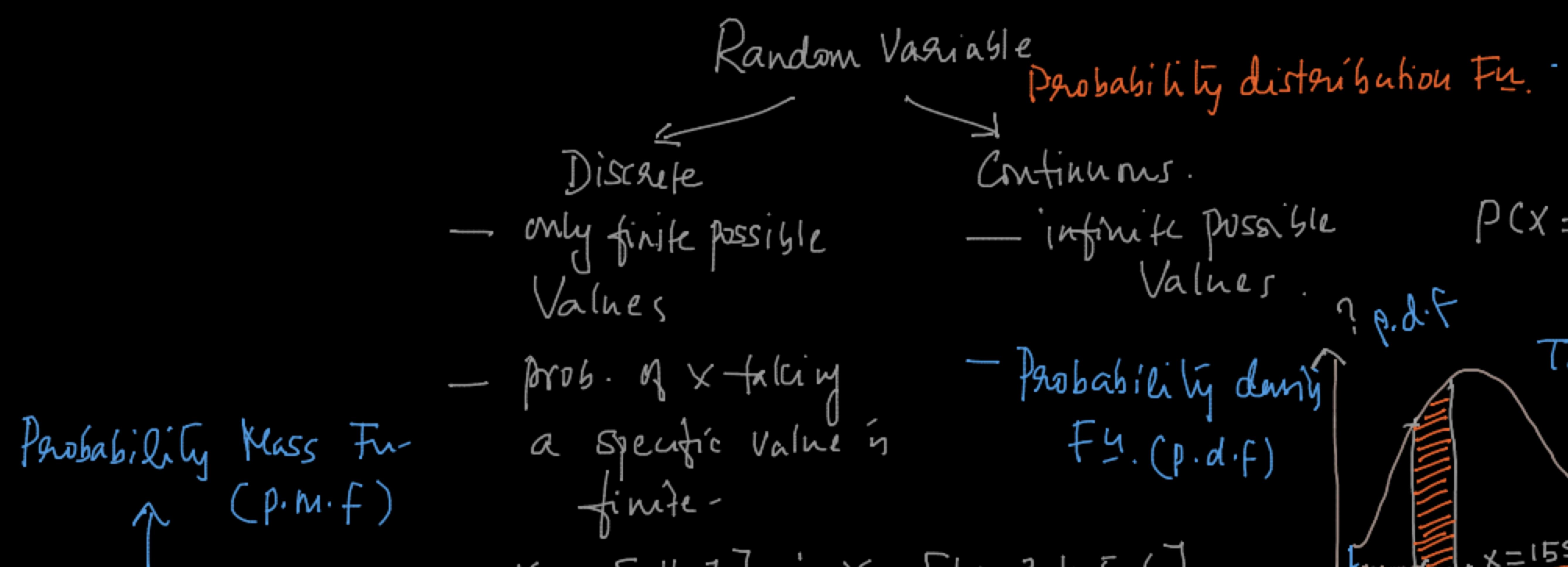
$$n=3, \quad x=2$$

$$P(x=2) = \frac{3!}{(3-2)! 2!} (0.5)^2 (0.5)^{3-2}$$

$$= \frac{3!}{1! 2!} \times (0.5)^2 \times 0.5$$

$$= \frac{3 \times 2 \times 1}{3 \times 2 \times 1} \times (0.25)^2 \times 0.5$$

$$= 3/8$$

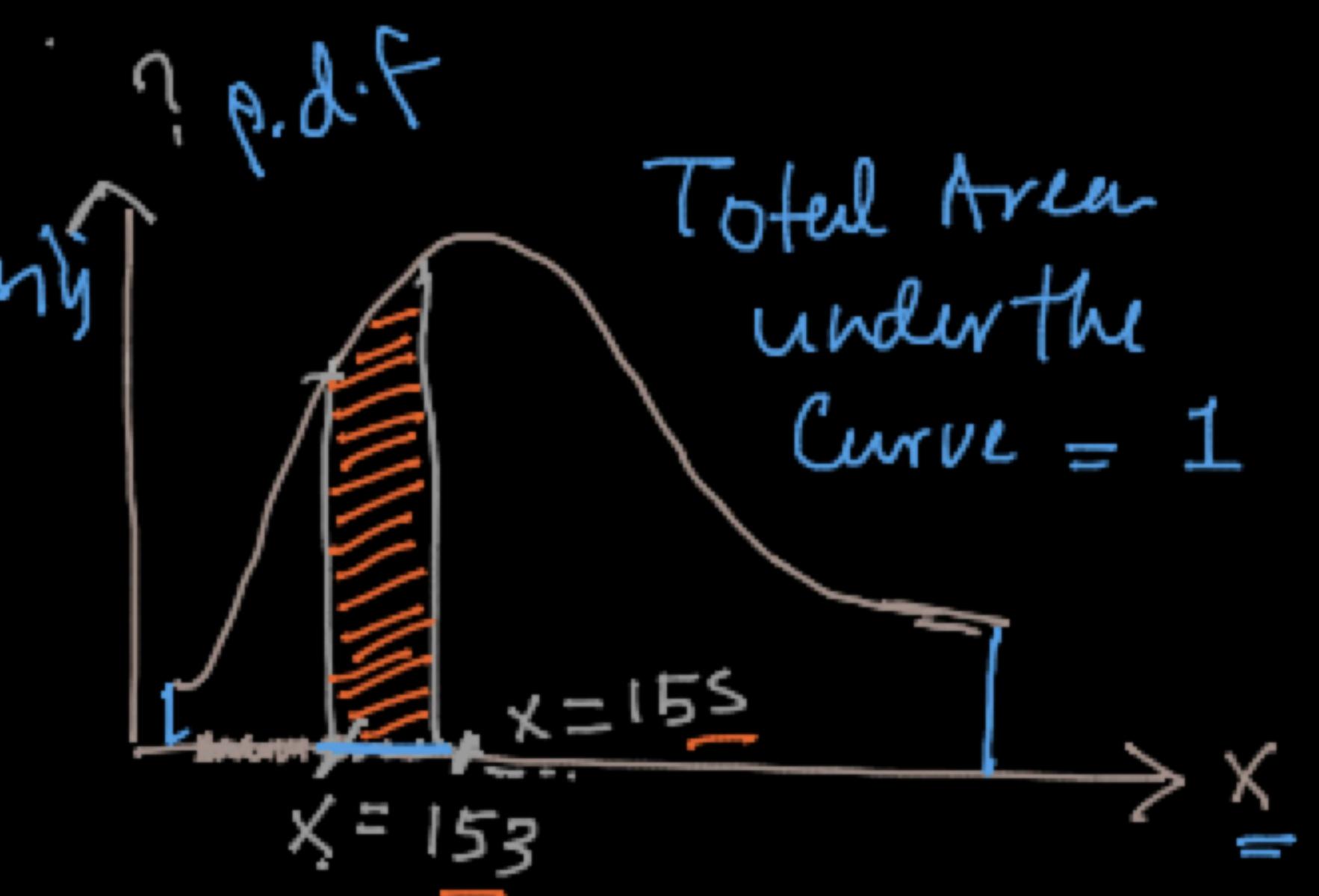
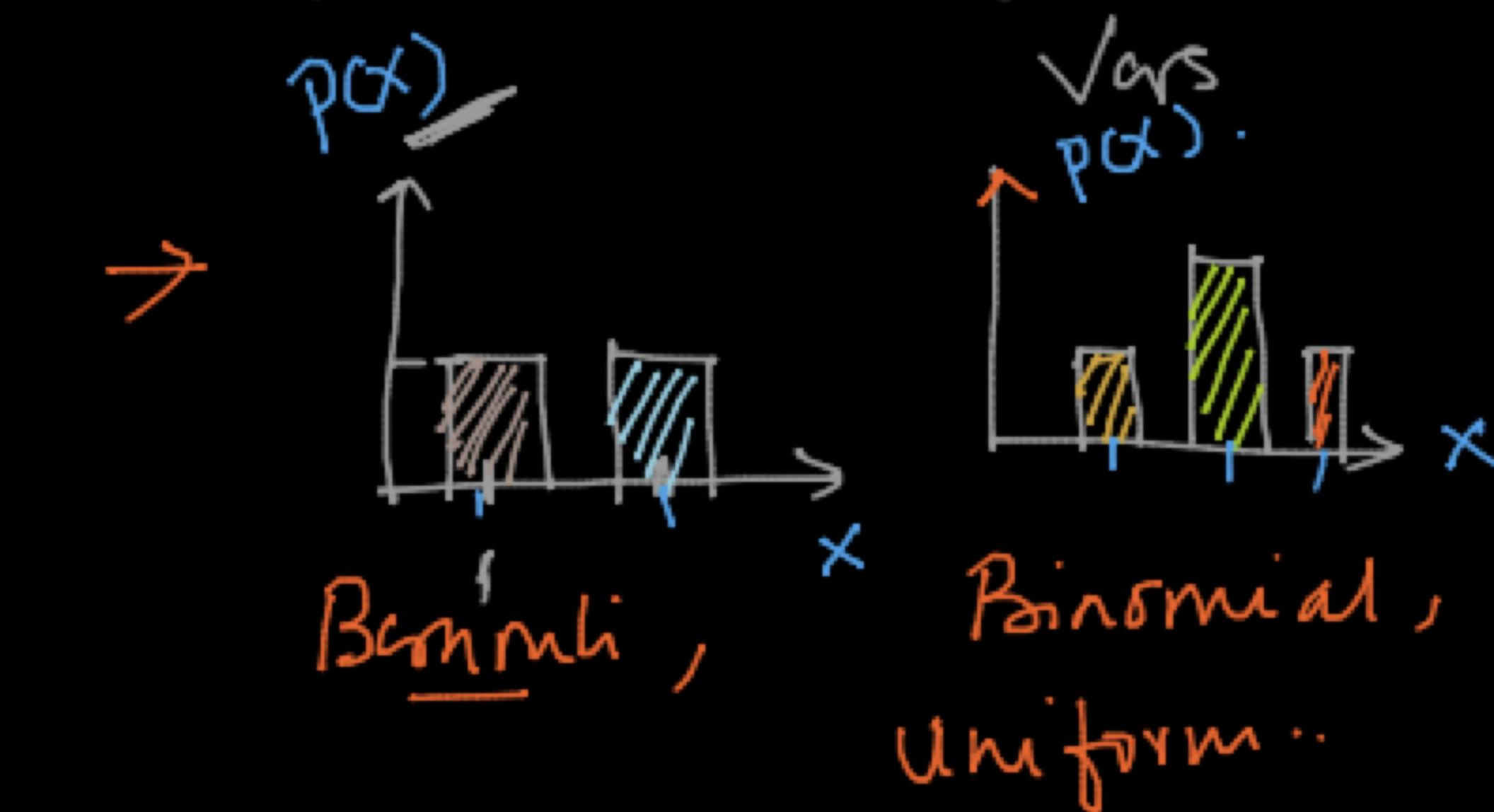


Probability Mass F.d.F  
↑ (P.M.F)

$$P(X) = \frac{n!}{(n-x)!x!} \cdot p^x \cdot q^{(n-x)}$$

$$P(X=1) = \frac{1}{2} \quad P(X=2) = \frac{1}{6}$$

— Prob. dist. of discrete random



— Normal dist.

— SND (Z-dist)

— Student's (t-dist.)

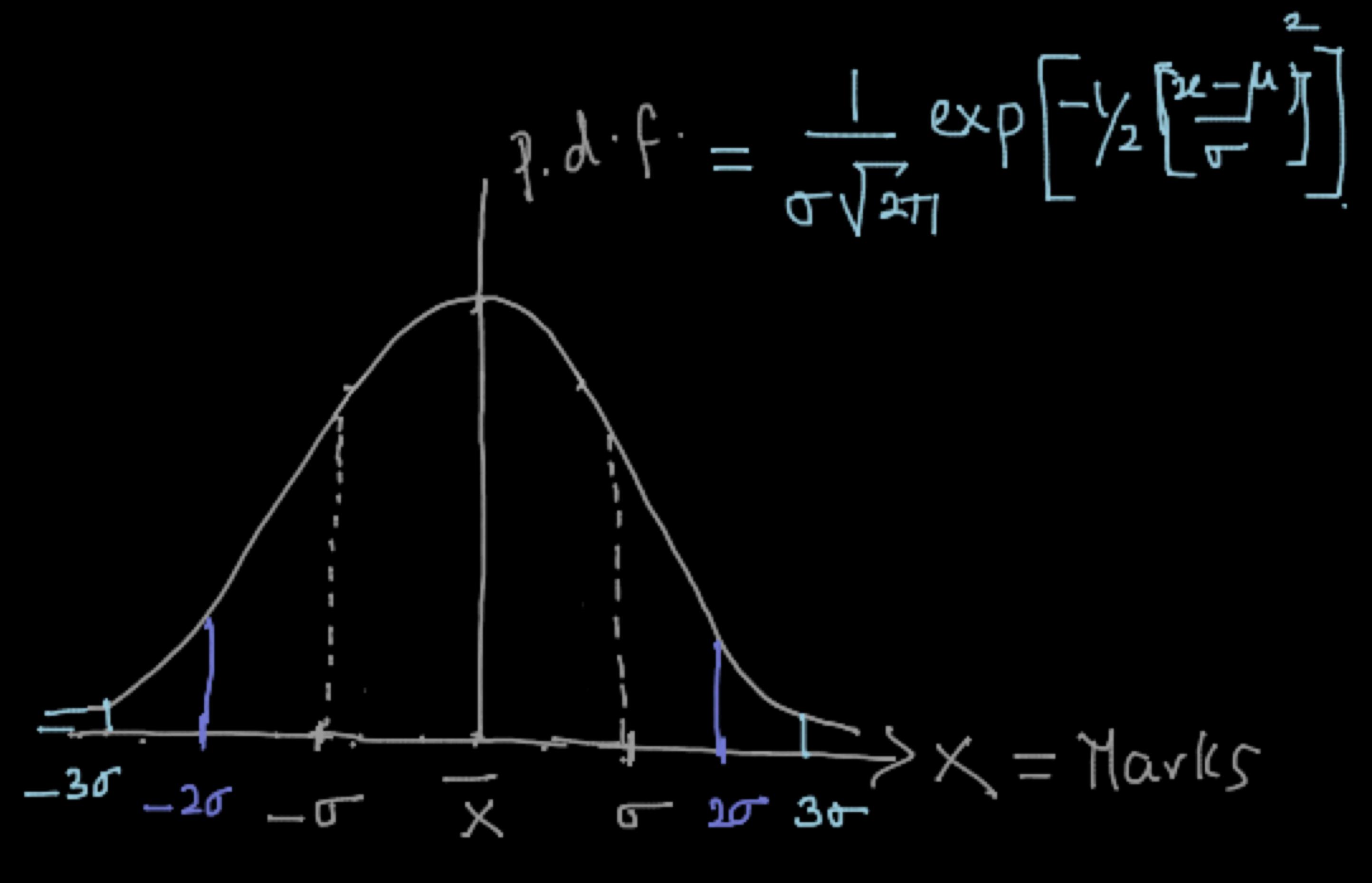
$$P(153 < X < 155)$$

$$\Rightarrow \int_{x=153}^{x=155} p.d.f.$$

$$P(X=1)$$

# 1. Normal Distribution

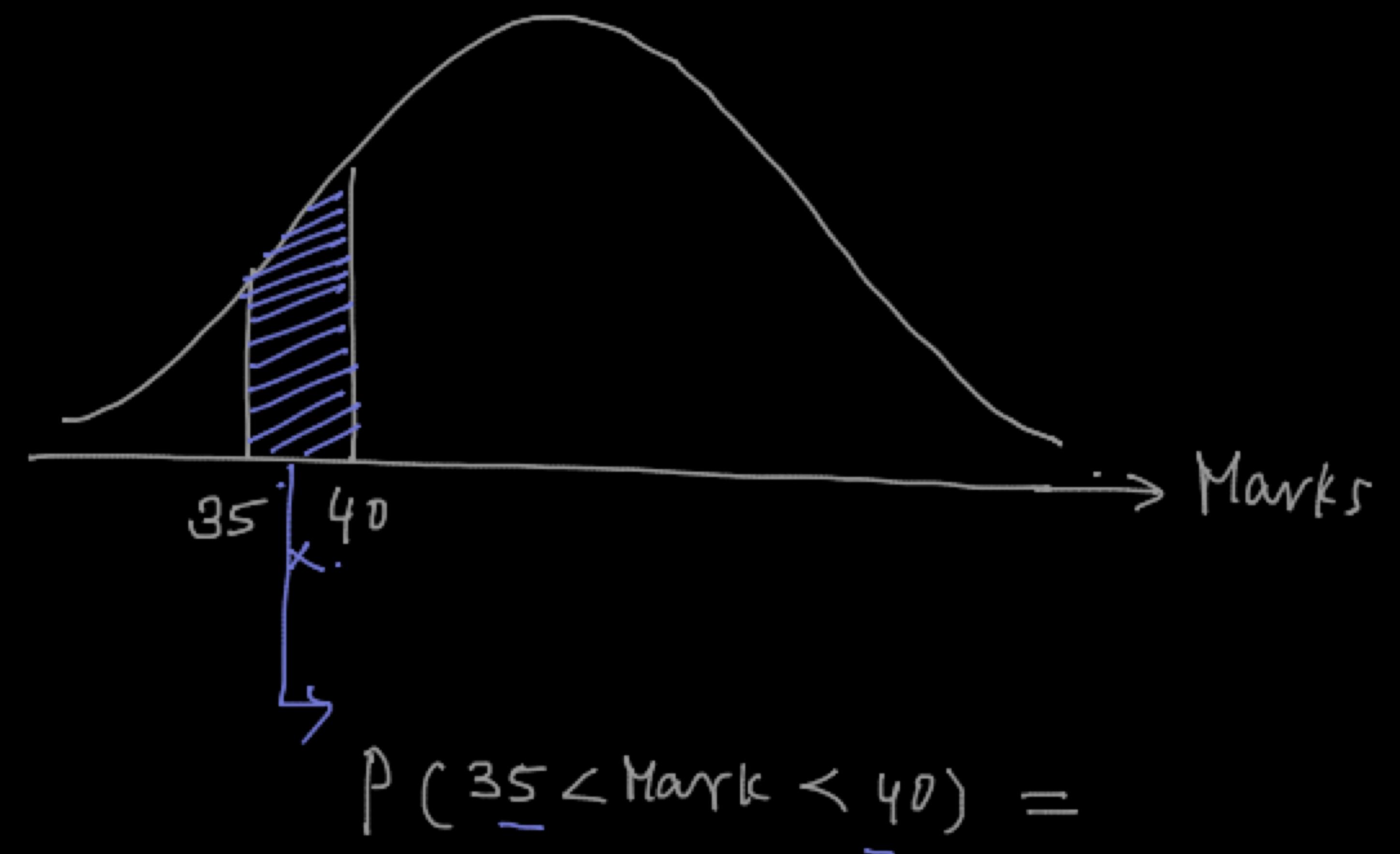
- Bell shaped
  - Symmetric
  - Mean/Median/Mode
  - Empirical Rule.



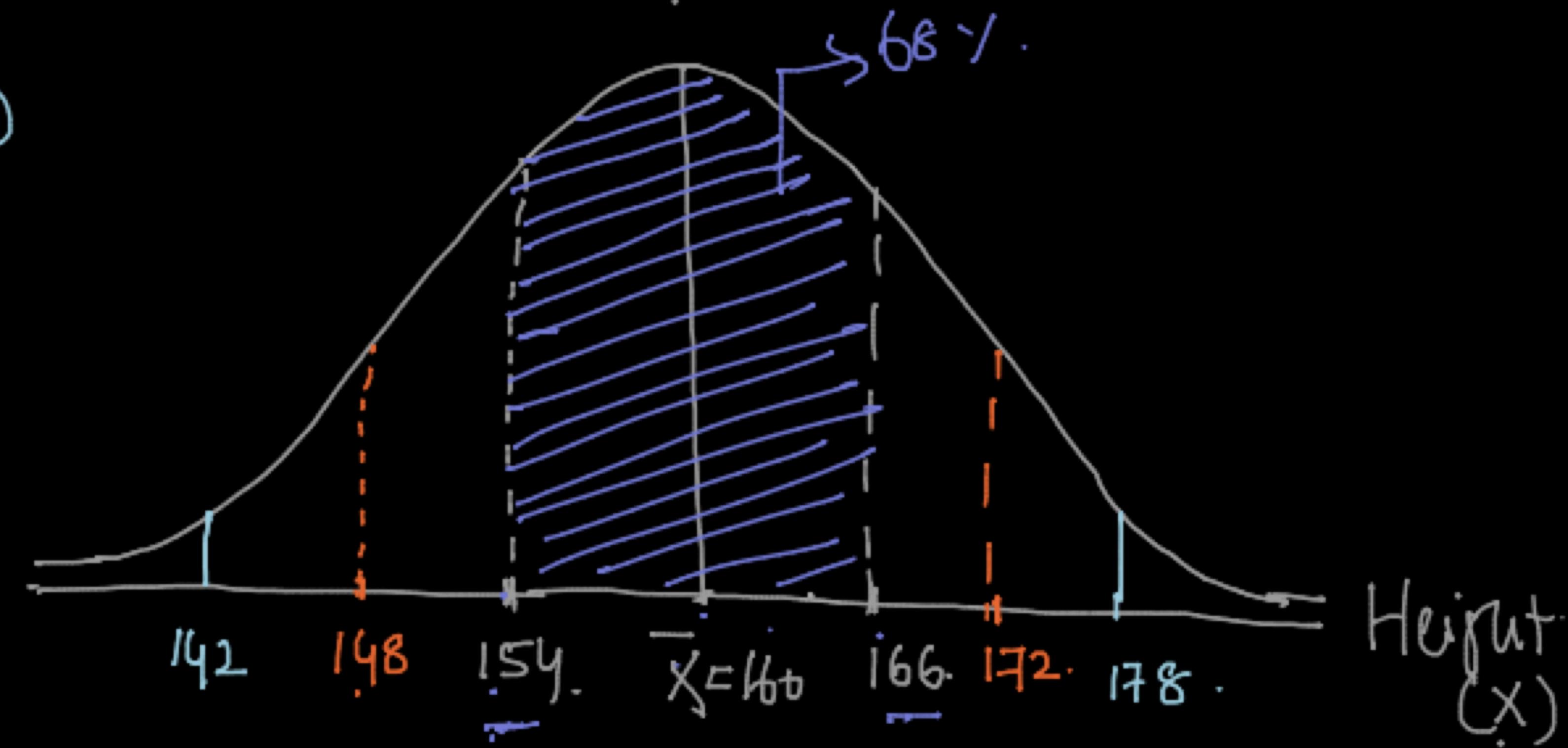
The figure consists of three vertically stacked normal distribution curves, each centered at 100. The top curve is labeled σ = 10, the middle curve σ = 5, and the bottom curve σ = 3. Each curve is divided into three standard deviation intervals: the innermost interval is shaded dark blue, the middle interval is light blue, and the outermost interval is white. The x-axis is marked with values 68, 50, 34, 100, and 136.

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

# Blackboard



Height  $\sim N(\mu, \sigma)$   
 $\sim N(160, 6)$



$$\leftarrow P(148 < H < 172) \rightarrow 95\%$$
$$\leftarrow 99.7\% \rightarrow$$

Heights  
(X)

$$\bar{X} = 160, \sigma = 6 \text{ cms.}$$

$$n = 100 \rightarrow 68\%$$

$$\bar{X} \pm 2\sigma \Rightarrow 160 \pm 12$$

$$\bar{X} \pm 3\sigma \Rightarrow 160 \pm 18$$

Weights  
 $(\underline{x}) \rightarrow N.D$

$\times \text{UN}(\mu, \sigma)$ .

68% =  $x \pm \sigma$

95% =  $x \pm 2\sigma$

99.7% =  $x \pm 3\sigma$

45

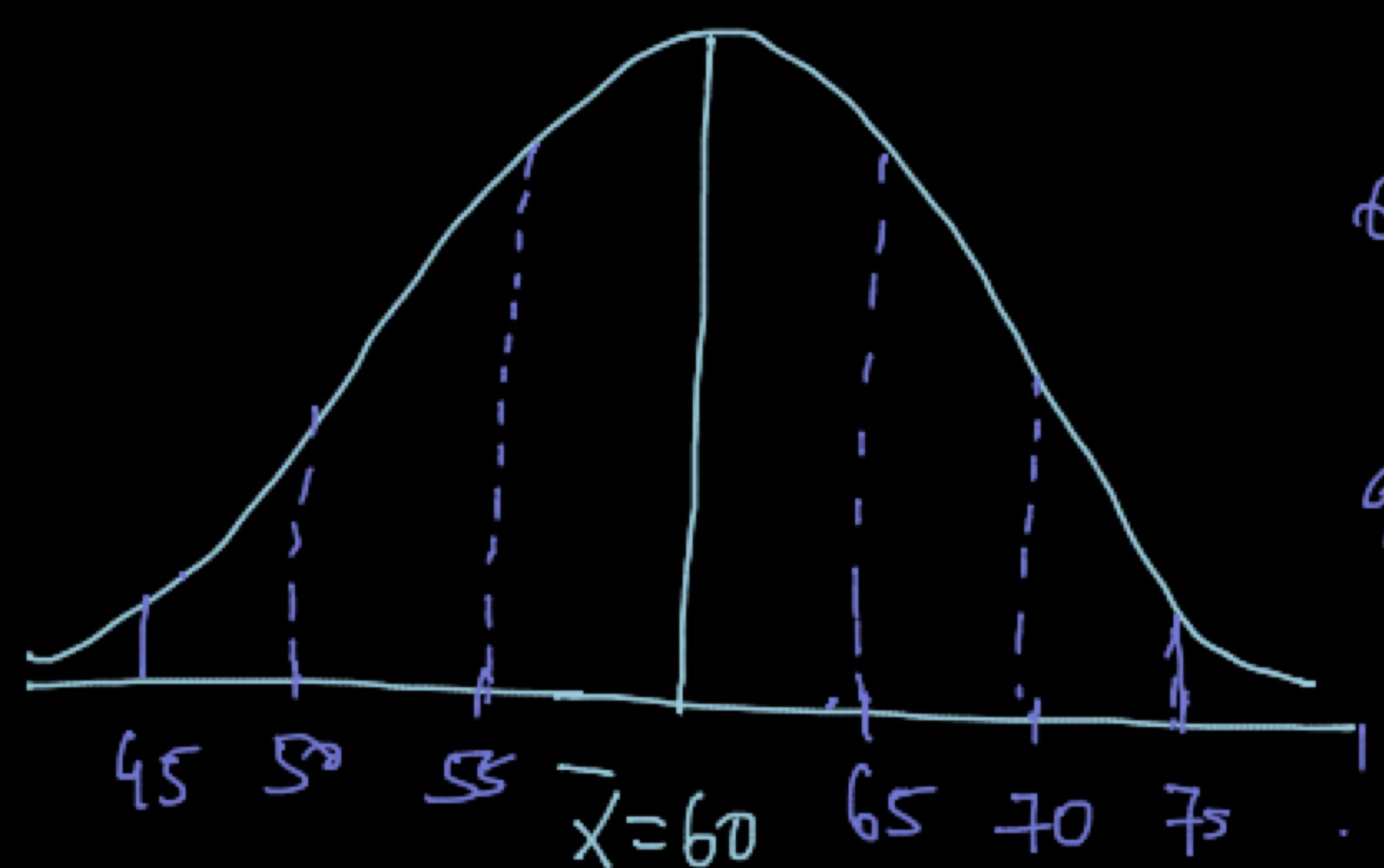
63

47

55

:

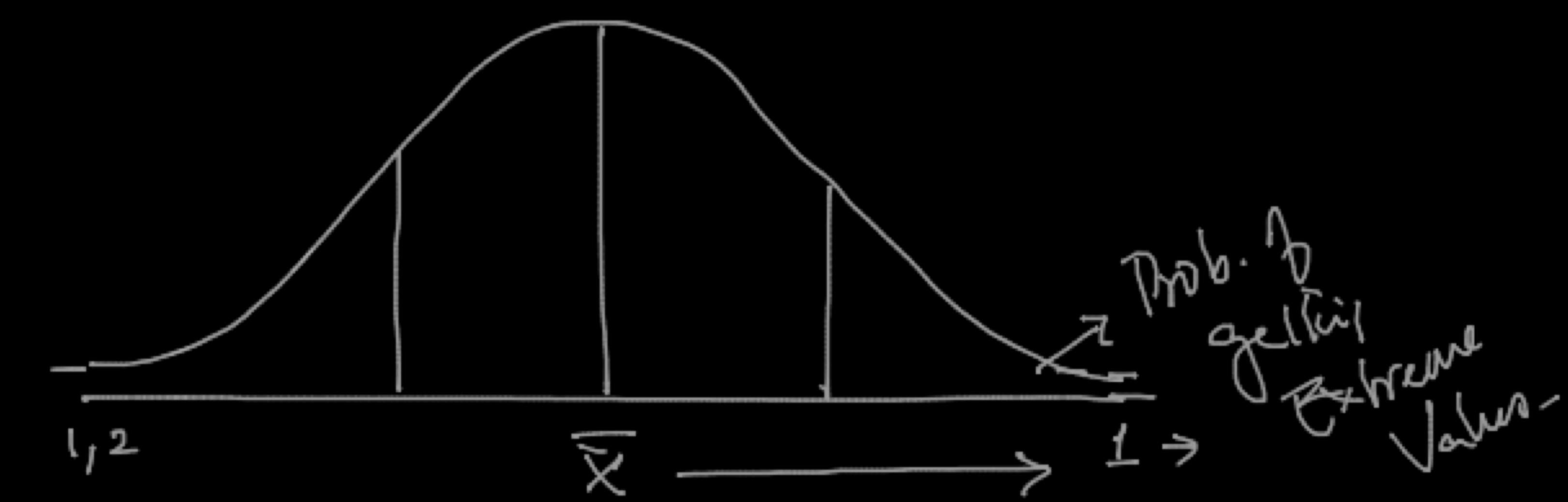
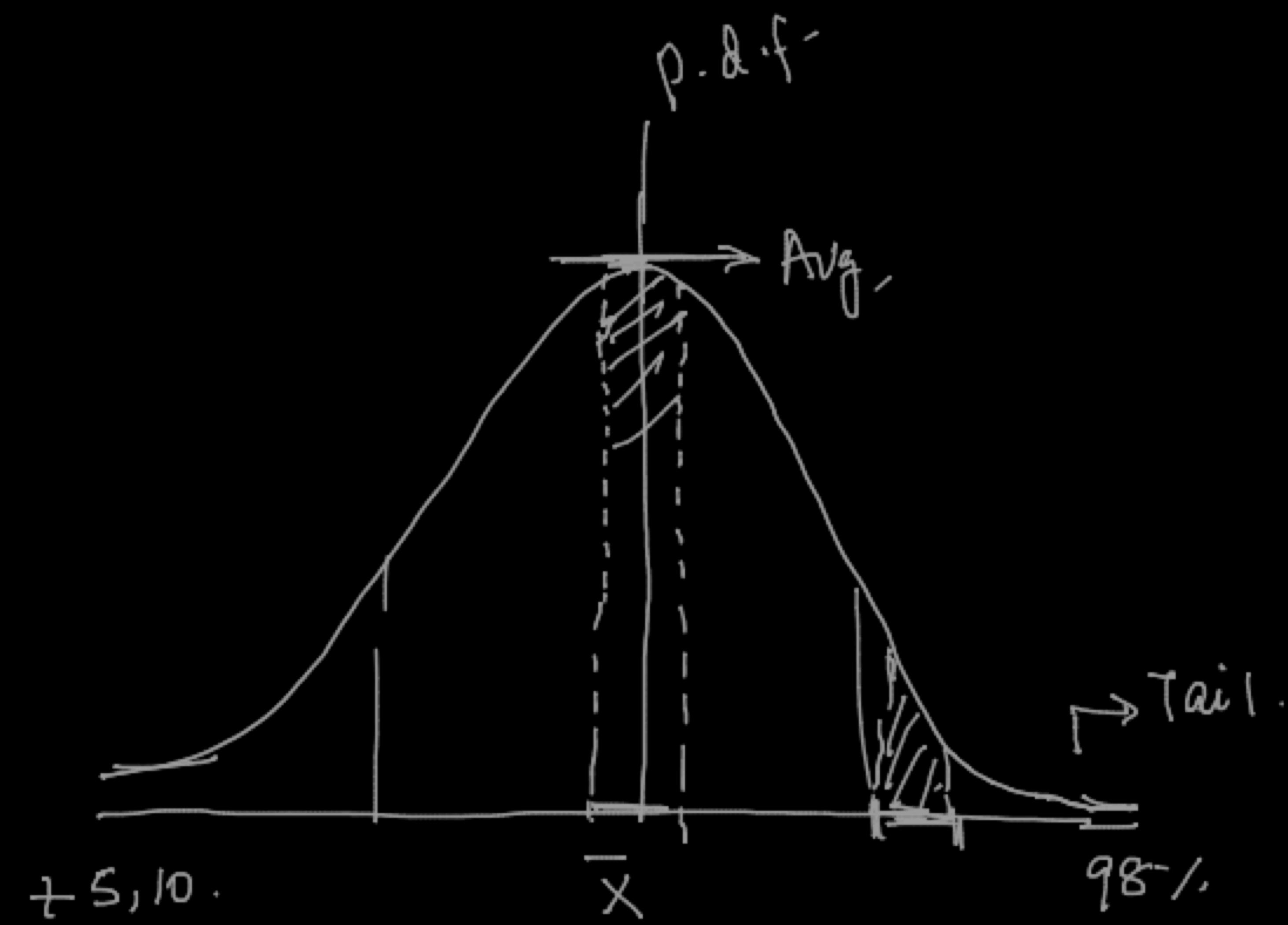
$$\bar{x} = 60 \text{ kg} \quad \sigma = 5 \text{ kg}$$



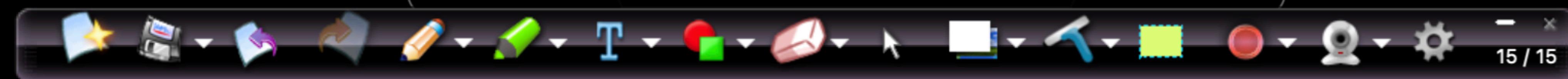
$\leftarrow 68\% \rightarrow$

$\leftarrow 95\% \rightarrow$

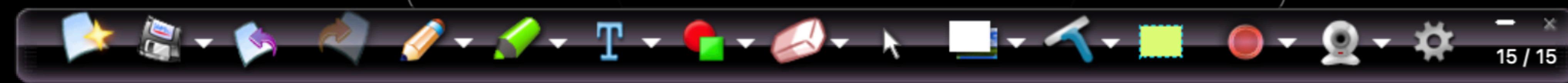
$\leftarrow 99.7 \rightarrow$



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Population

No. of datapoints

N

Sample

n

Mean

$\mu$

$\bar{x}$

Variance

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2$$

$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

Std. Deviation

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2}$$

$$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$



$N = 1.3 \text{ Billion}$

$$\mu = \$2000$$

$$\bar{x} = 3$$

$$\begin{aligned} x_1 &= 3 \\ x_2 &= 3 \\ \boxed{x_3 = 3} \end{aligned}$$

$n = 1000$

$$\bar{x} =$$

$$s =$$

Underestimates

$$\text{Variance} = \frac{1}{n-1} \sum_{i=1}^n (\underline{x}_i - \bar{x})^2$$

$\hookrightarrow (x_1 - \bar{x})^2 + (x_2 - \bar{x})^2$

$\hookrightarrow \text{Degree of Freedom}$

$\checkmark$  — No. of data points free to vary.

$$\boxed{\text{Total} = 100} \quad \text{Constraint: } \bar{x} = ?$$

$$\left. \begin{array}{l} p_1 \rightarrow \\ p_2 \rightarrow \\ p_3 \rightarrow \\ \vdots \\ p_9 \rightarrow \\ \rightarrow p_{10} \rightarrow \end{array} \right\} \Rightarrow 93$$

$$p_1 + p_2 + p_3 + \dots + p_{10} \Rightarrow \sum_{i=1}^{10} p_i$$