

Chapter - 05* Binary Parallel Adder / Ripple Carry Adder :

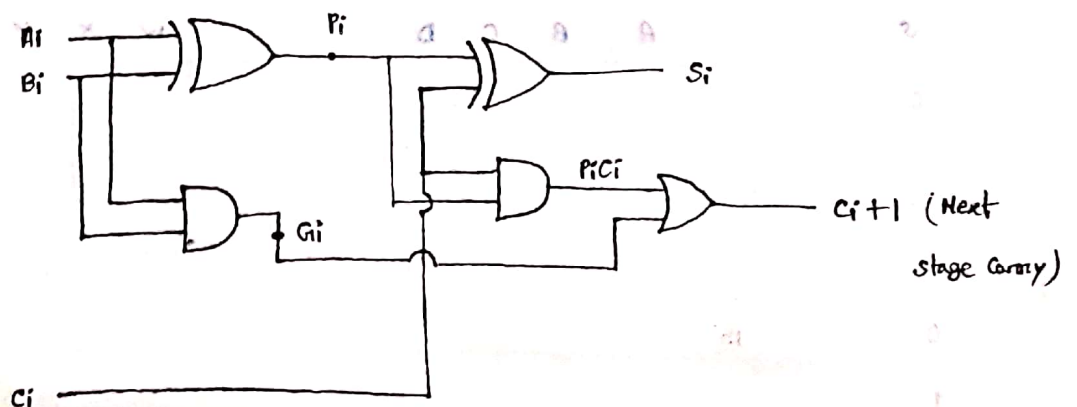
A_3	A_2	A_1
B_3	B_2	B_1

* Carry Look-ahead adder :

$$S = \overbrace{A \oplus B \oplus C_{in}}^{\text{carry propagate}}$$

$$C_{out} = \underbrace{AB \oplus C_{in}(A \oplus B)}_{\text{Carry generate}}$$

From truth table of 1 bit
Full Adder



here, $P_i = A_i \oplus B_i$

$$G_i = A_i B_i$$

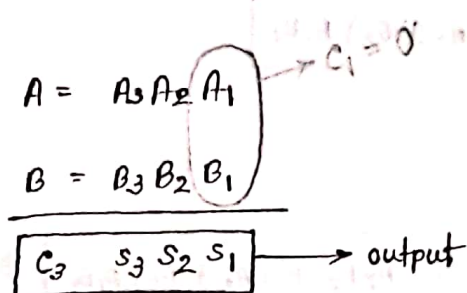
$$S_i = P_i \oplus C_i$$

$$C_{i+1} = G_i + P_i C_i$$

→ G_i is called a carry generate and it produces an output carry.

→ P_i is called a carry propagation which propagates the carry from previous stage.

For 3 bit Binary :



Simplification :

1st bit : $P_1 = A_1 \oplus B_1$

$i = 1$ $G_1 = A_1 B_1$

$$C_1 = 0$$

$$S_1 = P_1 \oplus C_1 = A_1 \oplus B_1$$

2nd bit :

$$P_2 = A_2 \oplus B_2$$

$$G_2 = A_2 B_2$$

$$C_2 = G_1 + P_1 C_1$$

$$= A_1 B_1 + (A_1 \oplus B_1) \cdot 0$$

$$= A_1 B_1$$

$$S_2 = P_2 \oplus C_2$$

$$= (A_2 \oplus B_2) \oplus A_1 B_1$$

3rd bit:

$$P_3 = A_3 \oplus B_3$$

$$G_3 = A_3 B_3$$

$$C_3 = G_2 + P_2 C_2$$

$$= A_2 B_2 + (A_2 \oplus B_2) A_1 B_1$$

$$S_3 = P_3 \oplus C_3$$

$$= (A_3 \oplus B_3) \oplus A_2 B_2 + (A_2 \oplus B_2) A_1 B_1$$

4th bit

(7.5)

Quiz # 1:

$$F = A \oplus B$$

$$F = \bar{A}B + A\bar{B}$$

Apply duality principle

$$F = (\bar{A} + B) \cdot (A + \bar{B}) = \bar{A}\bar{B} + AB = \overline{A \oplus B} \rightarrow \text{which is complement of } A \oplus B$$

* BCD Adder:

$$A = A_3 \quad A_2 \quad A_1 \quad A_0 \quad \rightarrow 15$$

$$B = B_3 \quad B_2 \quad B_1 \quad B_0 \quad \rightarrow 15$$

$$\begin{array}{ccccc} C_3 & S_3 & S_2 & S_1 & S_0 \\ 1 & 1 & 1 & 1 & 0 \end{array}$$

$$\begin{array}{r} A = 0 - 9 \\ B = 0 - 9 \\ \hline 18 \\ \text{Cin} = 1 \quad = 19 \end{array} \quad \left. \begin{array}{c} 0 \\ 1 \\ 1 \\ 19 \end{array} \right\} \text{sum} \Rightarrow \begin{array}{l} 10 \rightarrow 16 \\ 11 \rightarrow 17 \\ 12 \rightarrow 18 \\ 19 \rightarrow 25 \end{array}$$

Sum

C	S ₄	S ₃	S ₂	S ₁	
0	1	0	1	0	10
0	1	0	1	1	11
0	1	1	0	0	12
0	1	1	0	1	13
0	1	1	1	0	14
0	1	1	1	1	15
1	0	0	0	0	16
1	0	0	0	1	17
1	0	0	1	0	18
1	0	0	1	1	19

Uncorrected sum:

	$\overline{S_2} \overline{S_1}$	$\overline{S_2} S_1$	$S_2 \overline{S_1}$	$S_2 S_1$
$\overline{S_4} \overline{S_3}$				
$\overline{S_4} S_3$				
$S_4 \overline{S_3}$	1	1	1	1
$S_4 S_3$			1	1

BCD Adder :

\Rightarrow Each input digit does not exceed 9

\Rightarrow the output digit $9+9+1 = 19$ and does not exceed 19.

⇒ Take input bits to the 4 bit adder

⇒ check if result > 9

⇒ if it is not then return as it is

⇒ if it is, add 6 to it and return.

$$F = s_4 s_3 + s_2 s_4$$

$$= s_1(s_3 + s_2)$$

To add 6, equation is,

$$F' = c + F$$

$$= C + s_1 (s_3 + s_2)$$

৭ এর জন্য

C	S ₄	S ₃	S ₂	S ₁
	1	0	0	1

$$F = s_1(s_3 + s_2) + c$$

$$= 1 \quad 0 \quad 0 \quad 0 = 0$$

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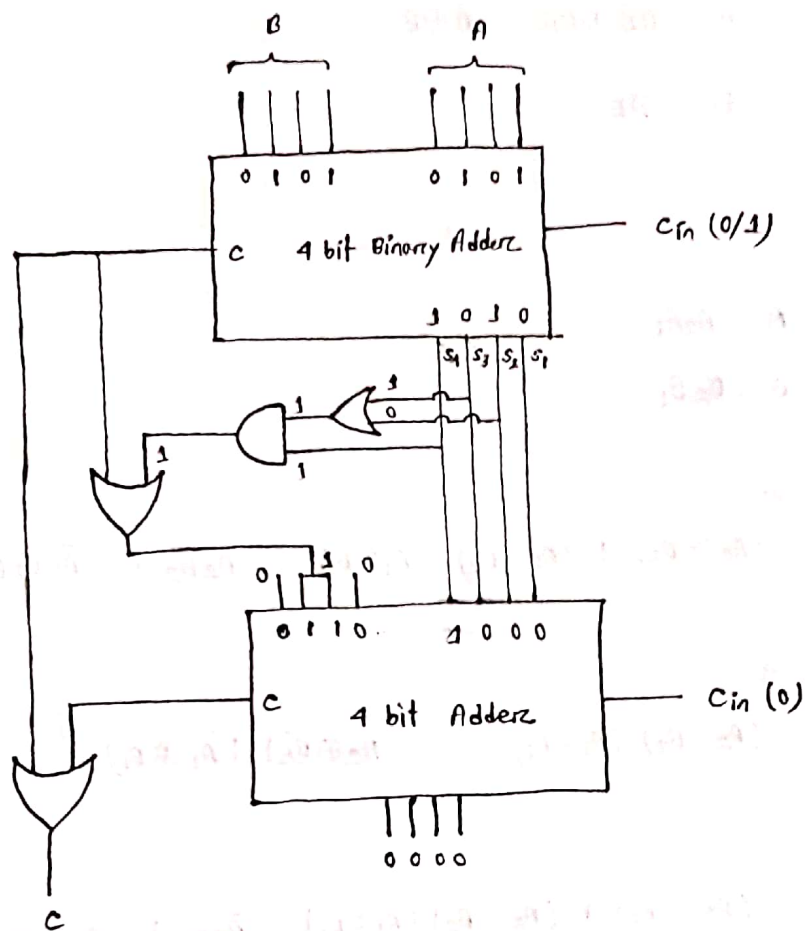
$$\begin{array}{cccc} s_4 & s_3 & s_2 & s_1 \\ 1 & 0 & 1 & 0 \end{array}$$

$$F = s_1(s_3 + s_2) + C$$

$$= 101$$

$$= 1$$

Block Diagram :



* Magnitude Comparator :

Truth Table for 1 bit Comparator

A	B	$F_1 (A > B)$	$F_2 (A = B)$	$F_3 (A < B)$
0	0	0	1	0
0	1	0	0	1
1	0	1	0	0
1	1	0	1	0

$$A > B, \quad F_1 = A\bar{B}$$

$$A = B, \quad F_2 = \bar{A}\bar{B} + AB = \overline{A \oplus B}$$

$$A < B, \quad F_3 = \bar{A}B$$

Für 2 bit:

$$A = A_2 A_1$$

$$B = B_2 B_1$$

$$A > B \Rightarrow$$

$$(A_2 > B_2) + (A_2 = B_2) \cdot (A_1 > B_1) = A_2 \bar{B}_2 + (\bar{A}_2 \oplus \bar{B}_2) A_1 \bar{B}_1$$

$$A = B \Rightarrow$$

$$(A_2 = B_2) (A_1 = B_1) = (\bar{A}_2 \oplus \bar{B}_2) (\bar{A}_1 \oplus \bar{B}_1)$$

$$A < B \Rightarrow$$

$$(A_2 < B_2) + (A_2 = B_2) (A_1 < B_1) = \bar{A}_2 B_2 + (\bar{A}_2 \oplus \bar{B}_2) \bar{A}_1 B_1$$

Für 3 bit:

$$A = A_3 A_2 A_1$$

$$B = B_3 B_2 B_1$$

$$A > B \Rightarrow$$

$$(A_3 > B_3) + (A_3 = B_3) (A_2 > B_2) + (A_3 = B_3) (A_2 = B_2) (A_1 > B_1)$$

$$A = B \Rightarrow$$

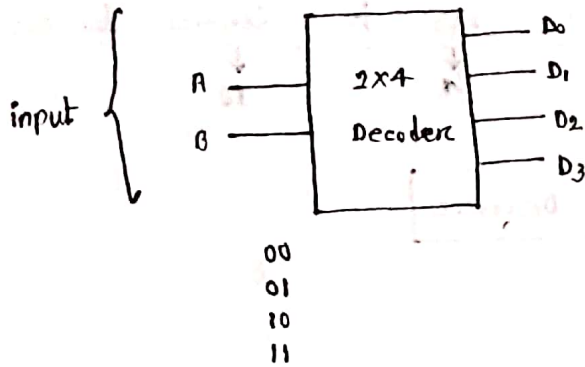
$$(A_3 = B_3) (A_2 = B_2) (A_1 = B_1)$$

$$A < B \Rightarrow$$

$$(A_3 < B_3) + (A_3 = B_3) (A_2 < B_2) + (A_3 = B_3) (A_2 = B_2)$$

* Decoder :

2 to 4 line Decoder (2x4 Decoder) :



Truth Table :

Input		Output			
A	B	D ₀	D ₁	D ₂	D ₃
0	0	1	0	0	0
0	1	0	1	0	0
1	0	0	0	1	0
1	1	0	0	0	1

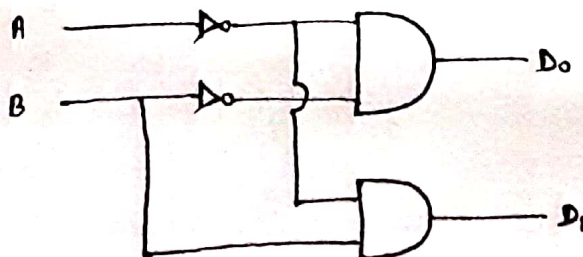
0 এর জন্য D₀ (৩ 1)

1 এর জন্য D₁ (৩ 1)

2 এর জন্য D₂ (৩ 1)

3 এর জন্য D₃ (৩ 1)

Logic Diagram :



ii) 3 to 8 line Diagram (3x8 Decoder)

iii) 4 to 16 line Diagram (4x16 Decoder)

* Draw logic Diagram of a BCD to - decimal decoder :

4 to 10 line Decoder

Truth Table :

Input				Output									
A	B	C	D	D ₀	D ₁	D ₂	D ₃	D ₄	D ₅	D ₆	D ₇	D ₈	D ₉

Expression :

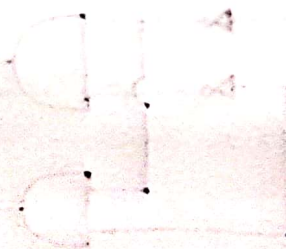
$$D_0 = \bar{A}\bar{B}\bar{C}\bar{D}$$

$$D_1 = \bar{A}\bar{B}\bar{C}D$$

$$D_2 = \bar{A}\bar{B}C\bar{D}$$

⋮

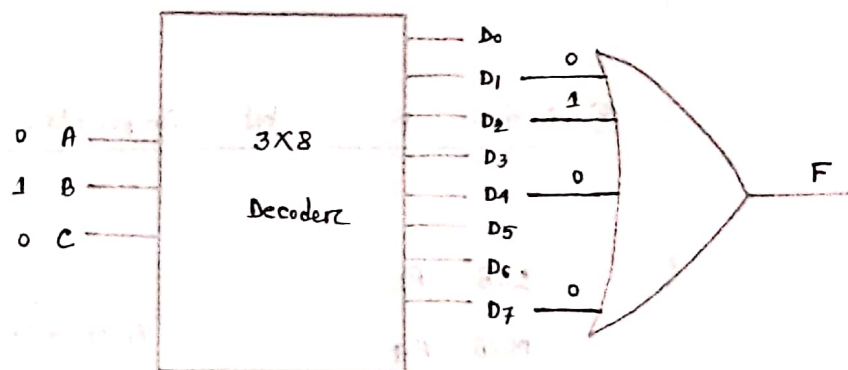
$$D_9 = A\bar{B}\bar{C}\bar{D}$$



* Decoder: $F(A, B, C) = \sum (1, 2, 4, 7)$
 \downarrow
 output 1

Truth Table:

A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1



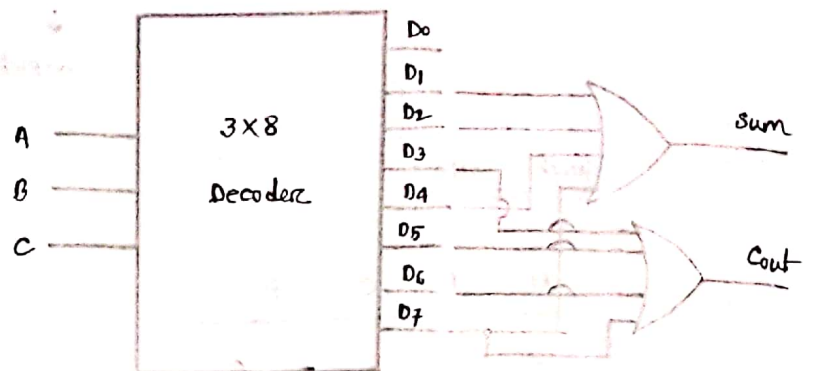
* Design a 1 bit full adder using a decoder and orz gates.

Truth Table:

Input			Output	
Cin	A	B	Carry	Sum
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

$$\text{Sum} = \sum (1, 2, 4, 7)$$

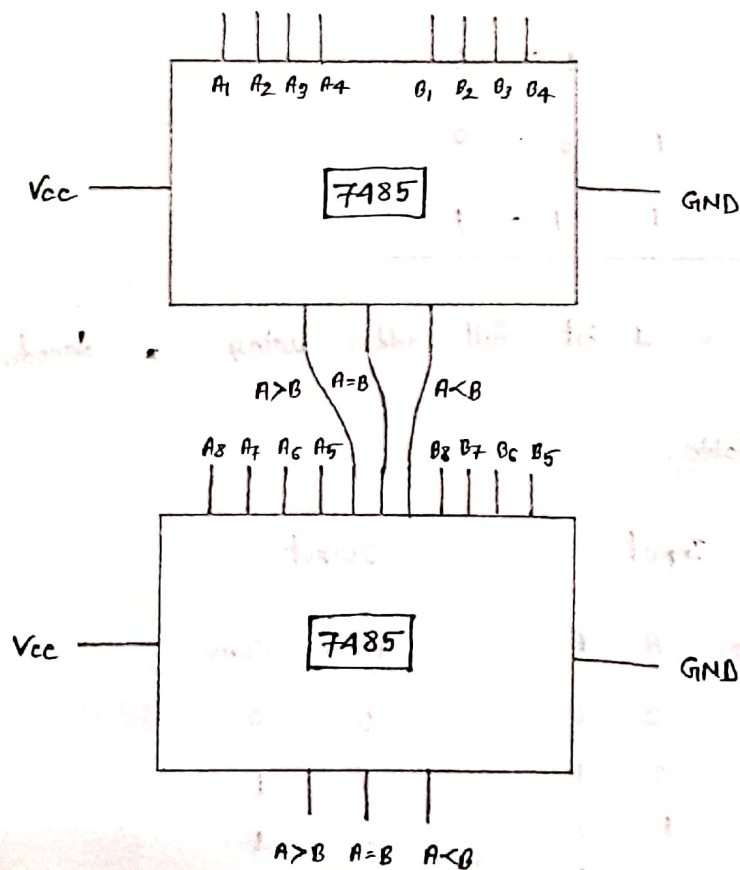
$$\text{Carry} = \sum (3, 5, 6, 7)$$



* Design a 8 bit Comparator ckt using 7485:

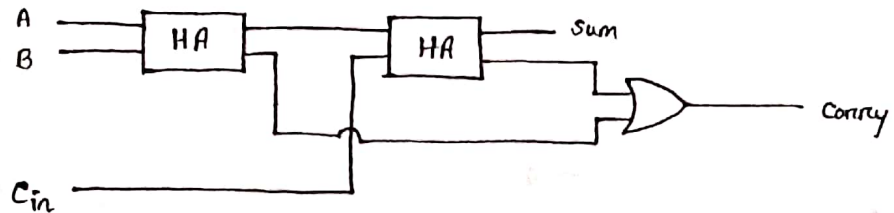
$$\text{LSB} = A_1$$

$$\text{MSB} = A_4$$



H.W. →
Subtractor

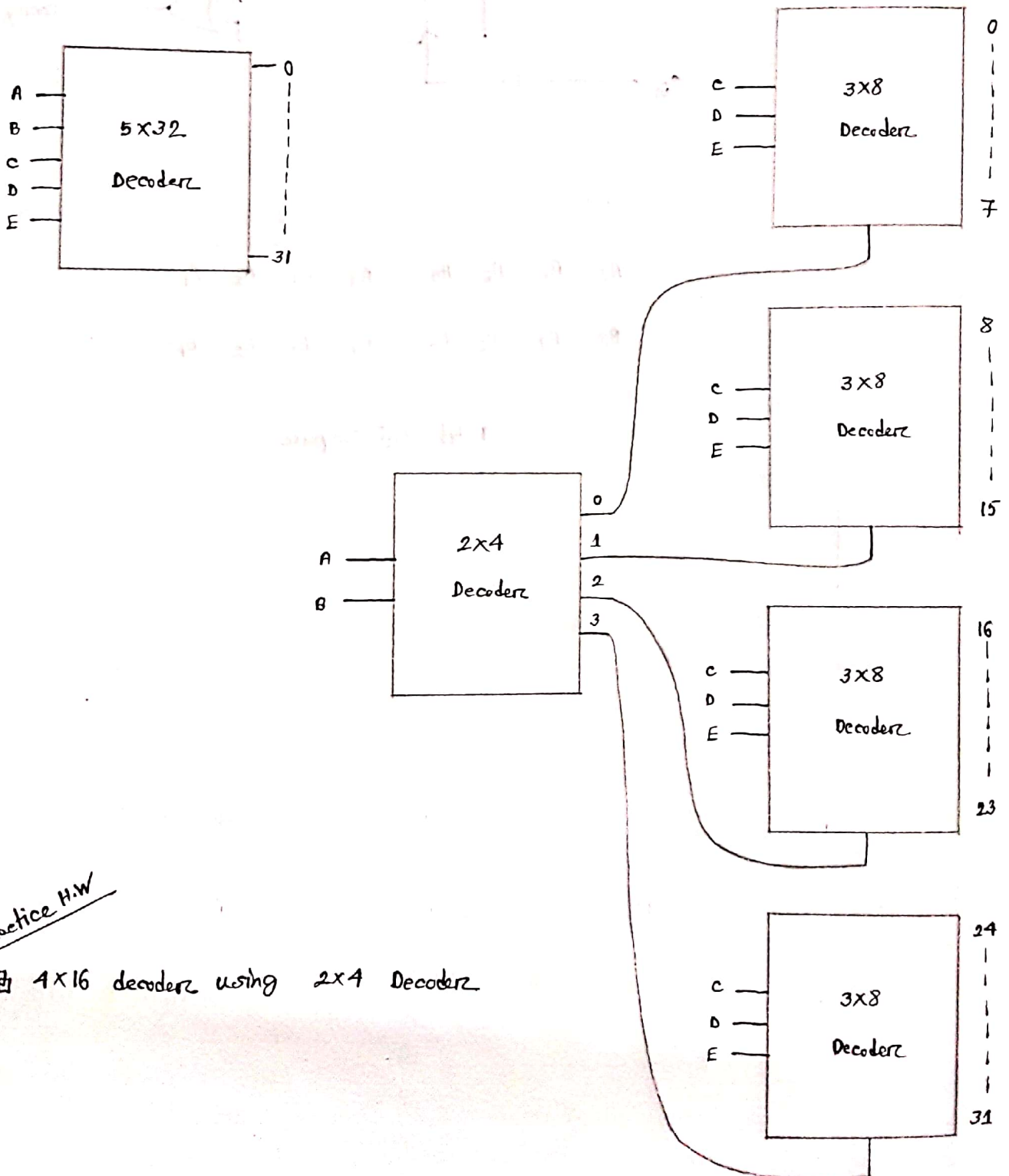
⊛ A full adder using two half adders and other basic gates.



A ₈	A ₇	A ₆	A ₅	A ₄	A ₃	A ₂	A ₁
B ₈	B ₇	B ₆	B ₅	B ₄	B ₃	B ₂	B ₁

1 bit binary compare

* Construct a 5×32 decoder with four 3×8 decoders and a 2×4 decoder.

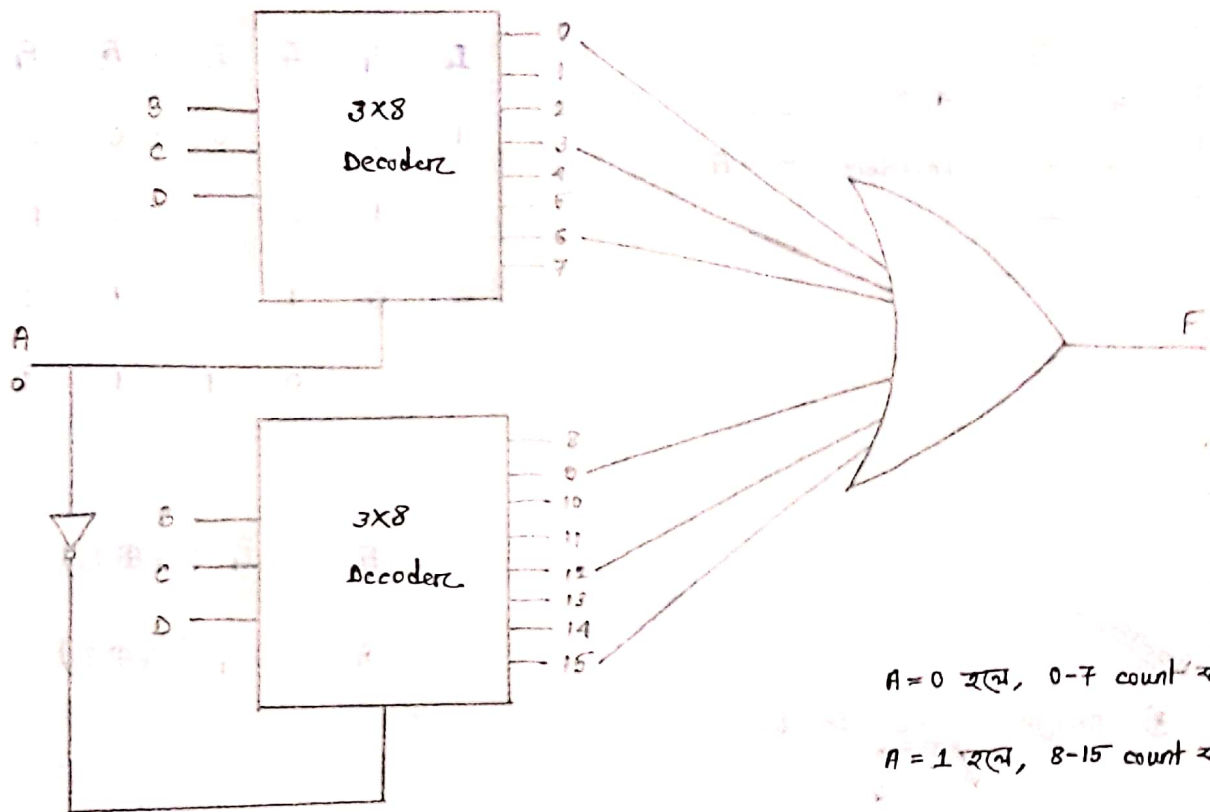


Practice H.W

□ 4×16 decoder using 2×4 Decoder

* Implement the following function using 3x8 decoder

$$F = \sum (0, 3, 6, 9, 12, 15)$$



A = 0 হলে, 0-7 count করবে

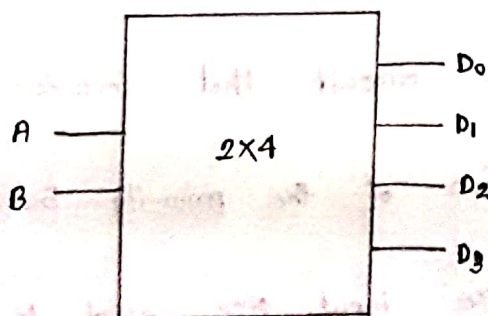
A = 1 হলে, 8-15 count করবে

4 bit এর জন্য, 1st ও 0 দিমে 0-7

নিখা যায় & 1st ও 1 দিমে 8-15

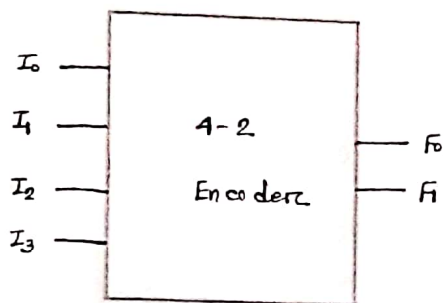
Decoder :

Truth Table :



A	B	D ₀	D ₁	D ₂	D ₃
0	0	1	0	0	0
0	1	0	1	0	0
1	0	0	0	1	0
1	1	0	0	0	1

Encoder :



Truth Table:

I_0	I_1	I_2	I_3	F_0	F_1
1	0	0	0	0	0
0	1	0	0	0	1
0	0	1	0	1	0
0	0	0	1	1	1

$$F_0 = \bar{I}_0 \bar{I}_1 (I_2 \oplus I_3)$$

$$F_1 = \bar{I}_0 \bar{I}_1 (I_2 \oplus I_3)$$

Practice

* Design 8x3 Encoder

↓ ↓
Octal to Binary

* Priority Encoder :

— A priority is an encoder circuit that includes the priority function. The operation of the priority Encoder is such that if two or more inputs are equal to 1 at the same time, the input having the highest priority will take precedence.

Quiz + Final
→ 2/2/22

$$3 > 2 > 1 > 0$$

I_3	I_2	I_1	I_0	F_0	F_1
0	0	0	1	0	0
0	0	1	x	0	1
0	1	x	x	1	0
1	x	x	x	1	1

$$2 > 3 > 1 > 0$$

I_2	I_3	I_1	I_0	F_0	F_1
0	0	0	1	0	0
0	0	1	x	0	1
0	1	x	x	1	0
1	x	x	x	1	1

$$F_0 = \overline{I_2} I_3 + I_2$$