

CSE 4125: Distributed Database Systems

Chapter – 2: Part C

Review of Databases and Computer
Networks

Symmetric?

$$\begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix} = \begin{pmatrix} 3 & 5 \\ 3 & 5 \end{pmatrix}$$

while

$$\begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix} \cdot \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} = \begin{pmatrix} 3 & 3 \\ 5 & 5 \end{pmatrix}.$$

Which Relational Algebra is symmetric?

- Selection
- Projection
- Union
- Difference
- Cartesian product
- Join
- Natural Join
- Semi join
- Natural Semi Join

Prove that, semi – join is not symmetric.

The Relational Model

- ✓ **Grade:** Number of columns
- ✓ **Cardinality:** Number of rows

Unary: Selection

Example: $SL_{A=a} R$

Selection operation affect Row

R		
A	B	C
a	1	a
b	1	b
a	1	d
b	2	f

S		
A	B	C
a	1	a
a	3	f

T		
B	C	D
1	a	1
3	b	1
3	c	2
1	d	4
2	a	3

Result		
A	B	C
a	1	a
a	1	d

$G(\text{Result}) = G(R)$

Unary: Projection

Example: $PJ_{A,B} R$

R		
A	B	C
a	1	a
b	1	b
a	1	d
b	2	f

S		
A	B	C
a	1	a
a	3	f

T		
B	C	D
1	a	1
3	b	1
3	c	2
1	d	4
2	a	3

Result	
A	B
a	1
b	1
b	2

$G(\text{Result}) \leq G(R)$

Binary: Union

Example: $R \cup S$

In case of $R \cup T$, the order of R & the order of T does not match. So we can't perform \cup operation.

R		
A	B	C
a	1	a
b	1	b
a	1	d
b	2	f

char, number, char

S		
A	B	C
a	1	a
a	3	f

T		
B	C	D
1	a	1
3	b	1
3	c	2
1	d	4
2	a	3

number, char, number

Result		
A	B	C
a	1	a
b	1	b
a	1	d
b	2	f
a	3	f

$G(\text{Result}) = G(R) = G(S)$

Binary: Difference

Example: $R \bowtie S$

R		
A	B	C
a	1	a
b	1	b
a	1	d
b	2	f

S		
A	B	C
a	1	a
a	3	f

T		
B	C	D
1	a	1
3	b	1
3	c	2
1	d	4
2	a	3

Result		
A	B	C
b	1	b
a	1	d
b	2	f

$$G(\text{Result}) = G(R) = G(S)$$

Binary: Cartesian Product

Example: $R \bowtie S$

$$G(\text{Result}) = G(R) + G(S)$$

R		
A	B	C
a	1	a
b	1	b
a	1	d
b	2	f

S		
A	B	C
a	1	a
a	3	f

T		
B	C	D
1	a	1
3	b	1
3	c	2
1	d	4
2	a	3

Result					
R.A	R.B	R.C	S.A	S.B	S.C
a	1	a	a	1	a
b	1	b	a	1	a
a	1	d	a	1	a
b	2	f	a	1	a
a	1	a	a	3	f
b	1	b	a	3	f
a	1	d	a	3	f
b	2	f	a	3	f

Binary: Join

Example: $R \bowtie_{R.C=T.C} T$

$$G(\text{Result}) = G(R) + G(S)$$

R		
A	B	C
a	1	a
b	1	b
a	1	d
b	2	f

S		
A	B	C
a	1	a
a	3	f

T		
B	C	D
1	a	1
3	b	1
3	c	2
1	d	4
2	a	3

Result					
A	R.B	R.C	T.B	T.C	D
a	1	a	1	a	1
a	1	a	2	a	3
b	1	b	3	b	1
a	1	d	1	d	4

Binary: Natural Join

Example: $R \bowtie T$

R		
A	B	C
a	1	a
b	1	b
a	1	d
b	2	f

S		
A	B	C
a	1	a
a	3	f

T		
B	C	D
1	a	1
3	b	1
3	c	2
1	d	4
2	a	3

Result			
A	B	C	D
a	1	a	1
a	1	d	4

$$G(\text{Result}) = G(R) + G(S) - \text{No of common column}$$

$$G(\text{Result}) < G(R) + G(S)$$

Binary: Semi-join

Example: $R \text{ SJ}_{R.C=T.C} T$

R		
A	B	C
a	1	a
b	1	b
a	1	d
b	2	f

S		
A	B	C
a	1	a
a	3	f

T		
B	C	D
1	a	1
3	b	1
3	c	2
1	d	4
2	a	3

Result		
A	B	C
a	1	a
b	1	b
a	1	d

$G(\text{Result}) = G(R)$

Binary: Natural Semi-join

Example: $R \bowtie S \bowtie T$

R		
A	B	C
a	1	a
b	1	b
a	1	d
b	2	f

S		
A	B	C
a	1	a
a	3	f

T		
B	C	D
1	a	1
3	b	1
3	c	2
1	d	4
2	a	3

Result		
A	B	C
a	1	a
a	1	d

$$G(\text{Result}) = G(R)$$

- Join is Cartesian Product of two relations followed by a selection operation.
- Semi-join is Join between two relations followed by a projection operation.

Sample Questions

- a) If R and S are the input relations, and T is the output relation, for which relational algebraic operation(s) the following statements are true?
- i. $\text{grade}(R) = \text{grade}(S) = \text{grade}(T)$ $R \cup S$
 - ii. $\text{grade}(R) + \text{grade}(S) = \text{grade}(T)$ $R \Join S, R \bowtie S$
- b) Give examples of protocol and session from the context of DDB.