

**Ahsanullah University of Science and Technology    Date: 07/09/2020**  
**Department of Arts and Sciences**  
**Programme: B.Sc. in Computer Science and Engineering**  
**Quiz#2   Year: 2019   Semester: Fall**  
**Course Name: Mathematics III, Course Code: Math 2101**

**Time: 75 min**

**Marks:30**

Answer all the questions

1. Evaluate  $\int_0^{\infty} t e^{-3t} \cos t \, dt$  [6]

2. Write down the function defined by  $f(t) = \begin{cases} 2 & \text{when } t < 1 \\ 3t & \text{when } 1 \leq t < 2 \\ e^{2t} & \text{when } t \geq 2 \end{cases}$  into its corresponding unit step function and hence find out its the Laplace transform. [8]

3. Using Laplace transform solve the initial value problem  $y'' + 4y = f(t)$ ,  $y(0) = y'(0) = 0$  where  $f(t) = \begin{cases} 0 & \text{for } t < 3 \\ t & \text{for } t \geq 3. \end{cases}$  [8]

4. Find a)  $L^{-1} \left\{ \frac{1}{s(s-4)^2} \right\}$  ; b)  $L^{-1} \left\{ \frac{1}{(s+1)\sqrt{s^2+a^2}} \right\}$ . [8]

Marks will be deducted for late submission.

**Exam Time: 60 min**

**For Scan and uploading Time :15 min. (max)**

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