

Representation of Numbers and Characters

The background of the slide is a deep blue gradient. On the right side, there are dynamic, flowing, wavy lines that create a sense of movement. These lines transition into a grid-like pattern of lighter blue and white, which appears to be a stylized representation of data or a digital space. The overall aesthetic is modern and technological.

Outline

- Number systems
- Conversion between number systems
- Addition and subtraction
- Integer representation in computer
- Character representation

Number Systems

- Decimal Number System

- There are ten basic symbols(digits): 0, 1, 2, 3, 4, 5, 6, 7, 8, 9.
- The base ten is represented in decimal as 10.
- $3932 = 3 \times 10^3 + 9 \times 10^2 + 3 \times 10^1 + 2 \times 10^0$.

- Binary Number System

- There are two digits: 0 and 1.
- The base 2 is represented in binary as 10.
- $11010 = 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$.

- Hexadecimal Number System

- There are sixteen digits: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F.
- The base is sixteen is represented in hex by 10.
- $1A = 1 \times 16^1 + 10 \times 16^0$.

Converting Binary and Hex to Decimal

- Hex Number, 8A2Dh = $8 \times 16^3 + A \times 16^2 + 2 \times 16^1 + D \times 16^0$
= $8 \times 16^3 + 10 \times 16^2 + 2 \times 16^1 + 13 \times 16^0$
= 35373d
- Binary Number, 1101b = $1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0$
= 13d

Converting Decimal to Binary and Hex

- Decimal Number, 11172d

$$\begin{aligned}11172 &= 698 \times 16 + 4 \\698 &= 43 \times 16 + 10(A) \\43 &= 2 \times 16 + 11(B) \\2 &= 0 \times 16 + 2 \\&= 2BA4h\end{aligned}$$

- Decimal Number, 95d

$$\begin{aligned}95 &= 47 \times 2 + 1 \\47 &= 23 \times 2 + 1 \\23 &= 11 \times 2 + 1 \\11 &= 5 \times 2 + 1 \\5 &= 2 \times 2 + 1 \\2 &= 1 \times 2 + 0 \\1 &= 0 \times 2 + 1 \\&= 1011111b\end{aligned}$$

Conversion Between Hex and Binary

- Hex Number, 2B3Ch = 0010101100111100b

2	B	3	C
0010	1011	0011	1100

- Binary Number, 1110101010b = 3AAh

0011	1010	1010
3	A	A

Addition

- Hex Addition

5	B	3	9	h
7	A	F	4	h
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D	6	2	D	h

- Binary Addition

1	0	0	1	0	1	1	1	1	b
			1	1	0	1	1	0	b
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1	0	1	1	0	0	1	0	1	b

Subtraction

- Hex Subtraction

D	2	6	F	h
B	A	9	4	h
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1	7	D	B	h

- Binary Subtraction

1	0	0	1	b
0	1	1	1	b
<hr/>				
0	0	1	0	b

One's Complement Representation

- Representation of 5 and one's complement of 5

0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1
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1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	0

- If we add 5 and its one's complement we will get 1111111111111111.

Two's Complement Representation

- Representation of 5 and two's complement of 5

$$\begin{array}{cccccccccccccccc} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 1 & 0 \\ & & & & & & & & & & & & & & & 1 \\ \hline 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 1 & 1 \end{array}$$

- If we add 5 and its two's complement we will get 10000000000000000.
- So the two's complement of a number represents its negative form.
- Two's complement of two's complement of 5 is 5.

Integer Representations

- Unsigned Integers

- Represents a magnitude so it is never negative.
- Largest unsigned integer stored in a byte is $11111111b = FFh = 255d$.
- Biggest unsigned integer stored in a word is $1111111111111111b = FFFFh = 65535d$.
- If least significant bit is 0 then number is even otherwise number is odd.
- Example: Addresses of memory locations, ASCII character codes.

- Signed Integers

- It can either be positive or negative.
- Most significant bit is reserved for sign: 0 for positive and 1 for negative.
- Negative integers are stored in a computer as two's complement.

Decimal Interpretations

- Unsigned Decimal Interpretation
 - Binary to decimal conversion.
- Signed Decimal Interpretation
 - If MSB is 0 then signed decimal is same as unsigned decimal.
 - If MSB is 1 take two's complement and convert it to decimal.

Decimal Interpretation

- Most significant bit of a positive signed integer is 0. So the leading hex digit of a positive signed integer is 0-7h. Integers beginning with 8-Fh have 1 in their sign bit so they are negative.
- For a word largest positive signed integer is 7FFFh=32767 and smallest negative signed integer is 8000h=-32768.
- For a byte largest positive signed integer is 7Fh=127 and smallest negative signed integer is 80h= -128.
- For 0000h-7FFFh and 00h-7Fh, signed decimal=unsigned decimal.
- For 8000h-FFFFh, signed decimal =unsigned decimal-65536.
- For 80h-FFh, signed decimal =unsigned decimal-256.

Character Representation

- ASCII Code
 - Most popular encoding scheme for characters.
 - Uses seven bits to code each character so there are total of 128 ASCII codes.
 - Only 95 ASCII codes from 32-126 are considered to be printable.
 - Others are used for communication control purposes.
- Keyboard
 - Identifies a key by generating an ASCII code when the key is pressed.
 - For IBM-PC each key is assigned an unique number called scan code.