

### 3.3. A\* Search: Minimization of the total estimated solution cost

#### a) Distinctive features

1) Widely known form of best-first search

2) Evaluation function,

$$f(n) = g(n) + h(n), \text{ where}$$

$g(n)$  – an actual path cost from initial node to node  $n$ ,

$h(n)$  – estimated cost of the cheapest path from  $n$  to the goal,

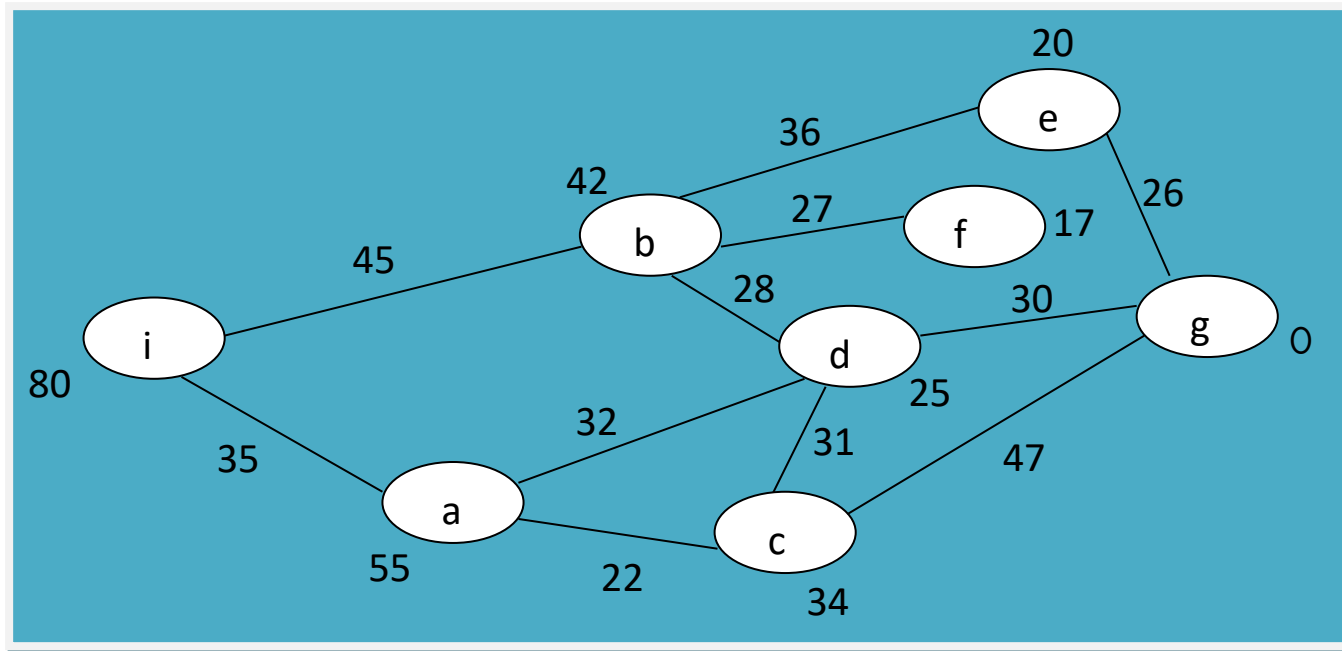
$f(n)$  – estimated cost of the cheapest solution through node  $n$ .

3) Generates all neighbors (may be repeatedly), and puts in PQ

4) Suboptimal solutions are avoided.

## b) Execution of the algorithm

- ❖ The same problem instance is taken:



i – Initial state/node

g – Goal state/node

- ❖ Execution shown in the tree of visited nodes and their children:

.....

### c) Important decisions about A\* search:

1. A\* in tree search is optimal if  $h(n)$  is admissible.
2. A\* in general graph search is optimal if  $h(n)$  is consistent.
3. If  $h(n)$  is consistent, then the values of  $f(n)$  along any path are non decreasing.
4. A\* expands all nodes with  $f(n) < C^*$ , where  $C^*$  is the cost of the optimal solution.
5. A\* is complete, assuming that there are only finite number of nodes with cost less than or equal to  $C^*$ .
6. A\* is said to be optimally efficient, that is, no other optimal algorithm is guaranteed to expand fewer nodes than A\* does.

#### d) Problems:

1. Number of expanded nodes for most problems grows exponentially.
2. Admissible and consistent heuristics are very hard to find.

#### Remedies:

- a) Various memory bounded search techniques (drop worst nodes when memory is full, ...) are used.
- b. Variants of  $A^*$  do not insist on optimal solution, but find good solution (suboptimal) even with heuristics not strictly admissible.