



# Pre-Algebra

*Student Workbook*

$$a + b = c$$

# Adding Whole Numbers

**EXAMPLE**

Combine like places when adding.

$$\begin{array}{r} 1 \\ 47 \\ + 28 \\ \hline 5 \end{array}$$

Add the ones. Regroup.

$$\begin{array}{r} 1 \\ 17a \\ + 39a \\ \hline 6a \end{array}$$

Add the ones. Regroup.

$$\begin{array}{r} 1 \\ 47 \\ + 28 \\ \hline 75 \end{array}$$

Add the tens.

Check.  $28 + 47 = 75$ 

$$\begin{array}{r} 1 \\ 17a \\ + 39a \\ \hline 56a \end{array}$$

Add the tens.

Check.  $39a + 17a = 56a$ **Directions** Write each problem in vertical form. Then solve it by adding.

1.  $32 + 28$

tens	ones

2.  $23 + 49$

tens	ones

3.  $297a + 39a$

hundreds	tens	ones	letters

4.  $1,238x + 246x + 99x$

thousands	hundreds	tens	ones	letters

5.  $943b + 644b + 86b$

thousands	hundreds	tens	ones	letters

**Directions** Add the following addends. Show how to check each problem.**Check**

6. 
$$\begin{array}{r} 44 \\ + 17 \\ \hline \end{array}$$

7. 
$$\begin{array}{r} 91 \\ + 89 \\ \hline \end{array}$$

8. 
$$\begin{array}{r} 77x \\ + 139x \\ \hline \end{array}$$

9. 
$$\begin{array}{r} 311 \\ + 109 \\ \hline \end{array}$$

**Check**

10. 
$$\begin{array}{r} 38b \\ 467b \\ + 877b \\ \hline \end{array}$$

11. 
$$\begin{array}{r} 312a \\ 29a \\ + 443a \\ \hline \end{array}$$

12. 
$$\begin{array}{r} 808 \\ 913 \\ + 97 \\ \hline \end{array}$$

**Check**

13. 
$$\begin{array}{r} 1,412y \\ 391y \\ + 2,744y \\ \hline \end{array}$$

14. 
$$\begin{array}{r} 27 \\ 4,281 \\ + 916 \\ \hline \end{array}$$

15. 
$$\begin{array}{r} 2,491z \\ 3,647z \\ + 244z \\ \hline \end{array}$$

# Subtracting Whole Numbers

**EXAMPLE**

Sometimes when subtracting, you will need to rename.

To check a subtraction problem, use addition.

		Rename	Check
14	$17x$	$\overset{2}{\cancel{3}} \overset{14}{\cancel{4}}$	18
$\underline{- 8}$	$\underline{- 12x}$	$\underline{- 1 \ 6}$	$\underline{+ 16}$
6	$5x$	1 8	34

**Directions** Write each problem in vertical form. Then subtract.

1.  $27 - 14$

5.  $45c - 39c$

9.  $750b - 243b$

2.  $56 - 22$

6.  $63 - 27$

10.  $912c - 728c$

3.  $84 - 31$

7.  $144 - 28$

11.  $1,874y - 678y$

4.  $77y - 42y$

8.  $233 - 118$

12.  $3,135a - 2,679a$

**Directions** Subtract. Then show how to check each problem.

**Check**

13.  $\begin{array}{r} 37 \\ - 16 \\ \hline \end{array}$

**Check**

16.  $\begin{array}{r} 325c \\ - 66c \\ \hline \end{array}$

**Check**

19.  $\begin{array}{r} 3,131z \\ - 1,967z \\ \hline \end{array}$

14.  $\begin{array}{r} 142x \\ - 87x \\ \hline \end{array}$

17.  $\begin{array}{r} 291y \\ - 36y \\ \hline \end{array}$

20.  $\begin{array}{r} 5,416a \\ - 879a \\ \hline \end{array}$

15.  $\begin{array}{r} 421 \\ - 277 \\ \hline \end{array}$

18.  $\begin{array}{r} 1,044b \\ - 426b \\ \hline \end{array}$

# Estimating Sums and Differences

**EXAMPLE**

Use an estimate to check whether a sum or a difference makes sense.  
To estimate, look at the numeral next to the greatest place value.

Round up if the numeral is 5 or more.	↓	
	59 ———>	60
	↓	
	263 ———>	300
	↓	
	+ 1,720 ———>	+ 2,000
		2,360 estimate
Round down if the numeral is less than 5.	↓	
	1,065 ———>	1,000
	↓	
	- 237 ———>	- 200
		800 estimate

**Directions** Round each number to the greatest place value.

- |                |                |                 |
|----------------|----------------|-----------------|
| 1. 67 _____    | 6. 362 _____   | 11. 8,125 _____ |
| 2. 136 _____   | 7. 5,187 _____ | 12. 654 _____   |
| 3. 241 _____   | 8. 488 _____   | 13. 5,871 _____ |
| 4. 1,047 _____ | 9. 237 _____   | 14. 453 _____   |
| 5. 2,668 _____ | 10. 551 _____  | 15. 9,412 _____ |

**Directions** Estimate each sum. Use rounding. Then find the exact sum.

- |                            |                              |                              |
|----------------------------|------------------------------|------------------------------|
| 16. $64 + 87 =$<br>_____   | 18. $714 + 892 =$<br>_____   | 20. $3,821 + 451 =$<br>_____ |
| 17. $252 + 524 =$<br>_____ | 19. $1,561 + 243 =$<br>_____ |                              |

**Directions** Estimate each difference. Use rounding. Then find the exact difference.

- |                            |                            |                              |
|----------------------------|----------------------------|------------------------------|
| 21. $65 - 42 =$<br>_____   | 23. $852 - 361 =$<br>_____ | 25. $1,961 - 457 =$<br>_____ |
| 22. $431 - 297 =$<br>_____ | 24. $631 - 288 =$<br>_____ |                              |

# Multiplying Whole Numbers

**EXAMPLE**

Sometimes when multiplying, you will need to rename.  
When a letter is part of the answer, remember to include it in the answer.

$$\begin{array}{r} 2 \\ 27a \\ \times 64 \\ \hline 108 \end{array}$$

Multiply ones.  
Rename.

$$\begin{array}{r} 4 \\ 27a \\ \times 64 \\ \hline 108 \end{array}$$

Multiply tens.  
Rename.

$$\begin{array}{r} 27a \\ \times 64 \\ \hline 108 \\ 1,620 \\ \hline 1,728a \end{array}$$

Add.

**Directions** Multiply the following problems.

1.  $4 \times 8 =$  \_\_\_\_\_

3.  $9 \cdot 9 =$  \_\_\_\_\_

5.  $(4)(3b) =$  \_\_\_\_\_

2.  $(7)(9) =$  \_\_\_\_\_

4.  $5a \cdot 6 =$  \_\_\_\_\_

6.  $10y \times 4 =$  \_\_\_\_\_

**Directions** Multiply. Remember to rename.

7.  $\begin{array}{r} 16 \\ \times 24 \\ \hline \end{array}$

9.  $\begin{array}{r} 35x \\ \times 17 \\ \hline \end{array}$

11.  $\begin{array}{r} 87z \\ \times 9 \\ \hline \end{array}$

8.  $\begin{array}{r} 34 \\ \times 23 \\ \hline \end{array}$

10.  $\begin{array}{r} 91 \\ \times 8x \\ \hline \end{array}$

12.  $\begin{array}{r} 19c \\ \times 8 \\ \hline \end{array}$

**Directions** Write each problem in vertical form. Then multiply.

13.  $28 \times 76y$

14.  $19 \times 32z$

15.  $81b \times 22$

# Dividing Whole Numbers

**EXAMPLE**

When dividing, place the numbers correctly in each step.

To check an answer, use multiplication and add the remainder.

**Check**

$$\begin{array}{r} 59 \text{ r}1 \\ 8 \overline{)473} \\ \underline{40} \phantom{0} \\ 73 \\ \underline{72} \\ 1 \end{array}$$

$$8 \times 59 + 1 = 473$$

**Directions** Divide these problems.

1.  $45 \div 9 =$  \_\_\_\_\_

5.  $36 \div 6 =$  \_\_\_\_\_

9.  $10 \div 5 =$  \_\_\_\_\_

2.  $16 \div 2 =$  \_\_\_\_\_

6.  $9 \div 3 =$  \_\_\_\_\_

10.  $33 \div 11 =$  \_\_\_\_\_

3.  $27 \div 3 =$  \_\_\_\_\_

7.  $18 \div 2 =$  \_\_\_\_\_

11.  $48 \div 12 =$  \_\_\_\_\_

4.  $14 \div 2 =$  \_\_\_\_\_

8.  $72a \div 9 =$  \_\_\_\_\_

12.  $54y \div 6 =$  \_\_\_\_\_

**Directions** Divide these problems.

13.  $7 \overline{)434}$

16.  $8 \overline{)272x}$

19.  $9 \overline{)463}$

14.  $4 \overline{)296}$

17.  $3 \overline{)402a}$

20.  $2 \overline{)365}$

15.  $5 \overline{)625}$

18.  $6 \overline{)528b}$

21.  $8 \overline{)682}$

**Directions** Divide. Check your work.

**Check**

22.  $18 \overline{)4,482}$

24.  $61 \overline{)8,419}$

**Check**

23.  $27 \overline{)2,457x}$

25.  $43 \overline{)5,762a}$

# Basic Operations

**EXAMPLE**

There are four basic operations.

addition  $32 + 9 = 41$

multiplication  $8 \times 7 = 56$

subtraction  $44 - 20 = 24$

division  $36 \div 4 = 9$

**Directions** Solve each problem.

1. 
$$\begin{array}{r} 112a \\ + 9a \\ \hline \end{array}$$

6. 
$$\begin{array}{r} 99 \\ - 47 \\ \hline \end{array}$$

11.  $24 \overline{)192a}$

2.  $75 \overline{)750}$

7.  $74 \overline{)2,368b}$

12.  $48 \overline{)96x}$

3.  $16 \overline{)224x}$

8. 
$$\begin{array}{r} 639 \\ + 124 \\ \hline \end{array}$$

13. 
$$\begin{array}{r} 92x \\ + 12x \\ \hline \end{array}$$

4. 
$$\begin{array}{r} 15 \\ \times 15 \\ \hline \end{array}$$

9. 
$$\begin{array}{r} 34a \\ \times 22 \\ \hline \end{array}$$

14. 
$$\begin{array}{r} 1,432b \\ + 3,698b \\ \hline \end{array}$$

5. 
$$\begin{array}{r} 77a \\ - 76a \\ \hline \end{array}$$

10.  $36 \overline{)936}$

15. 
$$\begin{array}{r} 198 \\ - 163 \\ \hline \end{array}$$

**Directions** Use a calculator to solve each problem.

16.  $112,342 - 9,479 =$

\_\_\_\_\_

18.  $206 \cdot 432 =$

\_\_\_\_\_

20.  $114,204 \div 62 =$

\_\_\_\_\_

17.  $6,048 \div 72 =$

\_\_\_\_\_

19.  $1,210 + 6,352 + 4,418 =$

\_\_\_\_\_

# Estimating Products and Quotients

**EXAMPLE**

To estimate a product, round to the greatest place value. Round up if 5 or more. Round down if less than 5.

$$23 \times 67 =$$

estimate  $20 \times 70 = 1,400$

To estimate a quotient, use two numbers that form a basic division fact.

$$1,721 \div 61 =$$

$17 \div 6$  is not a basic fact.  
 $18 \div 6$  is a basic fact.  
 estimate  $1,800 \div 60 = 300$

**Directions** Round. Estimate. Then find the exact product.

Problem	Rounded	Estimate	Exact Product
1. $63 \times 24$	_____	_____	_____
2. $85 \times 36$	_____	_____	_____
3. $17 \times 42$	_____	_____	_____
4. $44 \times 75$	_____	_____	_____
5. $59 \times 14$	_____	_____	_____
6. $32 \times 55$	_____	_____	_____
7. $73 \times 64$	_____	_____	_____
8. $27 \times 83$	_____	_____	_____

**Directions** Round. Estimate. Then find the exact quotient.

Problem	Rounded	Estimate	Exact Quotient
9. $534 \div 6$	_____	_____	_____
10. $736 \div 8$	_____	_____	_____
11. $1,380 \div 23$	_____	_____	_____
12. $2,862 \div 54$	_____	_____	_____
13. $6,290 \div 74$	_____	_____	_____
14. $4,758 \div 78$	_____	_____	_____
15. $11,613 \div 49$	_____	_____	_____



# Arithmetic and Algebra

**EXAMPLE**
**Four Basic Operations**

 addition  $21 + 7 = 28$ 

 subtraction  $16 - 4 = 12$ 

 multiplication  $8 \times 3 = 24$ 

 division  $18 \div 9 = 2$ 
**True, False, and Open Statements**

 True  $31 + 4 = 35$ 

 False  $27 - 4 = 12$ 

 Open  $45 + n = 51$ 

**Directions** Write the operation or operations used in each expression.

- |                       |                             |
|-----------------------|-----------------------------|
| 1. $6 + n$ _____      | 6. $16 \cdot 18$ _____      |
| 2. $48 \div b$ _____  | 7. $3 \overline{)27}$ _____ |
| 3. $3x$ _____         | 8. $3x - 15$ _____          |
| 4. $27 - y$ _____     | 9. $74 + 6n$ _____          |
| 5. $54n \div 9$ _____ | 10. $6x + 17 - 8$ _____     |

**Directions** Write *true* if the statement is true or *false* if it is false. Write *open* if the statement is neither true nor false.

- |                             |                             |
|-----------------------------|-----------------------------|
| 11. $13 + 8 = 21$ _____     | 21. $6n = 36$ _____         |
| 12. $48 - 12 = 36$ _____    | 22. $12 \cdot 3 = 30$ _____ |
| 13. $6 \times 9 = 48$ _____ | 23. $n + 18 = 25$ _____     |
| 14. $42 \div 7 = 7$ _____   | 24. $64 - 23 = 41$ _____    |
| 15. $83 + n = 92$ _____     | 25. $12n = 144$ _____       |
| 16. $5 \cdot 4 = 20$ _____  | 26. $66 \div 11 = 6$ _____  |
| 17. $21 \div 7 = 3$ _____   | 27. $16 - 6 = 20$ _____     |
| 18. $16 - b = 12$ _____     | 28. $75 + 15 = 90$ _____    |
| 19. $15 \div 4 = 5$ _____   | 29. $n \div 8 = 2$ _____    |
| 20. $126 + 10 = 116$ _____  | 30. $6 \times 7 = 42$ _____ |

# Representing Numbers Using Letters

**EXAMPLE**

Numerical Expressions (only numbers are used)

$42 - 12$

$3 \times 3$

Algebraic Expressions (numbers and letters are used)

$2x + 6$

$7a \div 3$

Variables (letters)  $n$  in  $7n + 4$ 

Operations (addition, subtraction, multiplication, division)

$6x + 4$

(multiplication and addition)

$(18 \div 3) - 8$

(division and subtraction)

**Directions** Write *numerical* or *algebraic* for each expression.

1.  $6x + 3$  \_\_\_\_\_

6.  $n + 19$  \_\_\_\_\_

2.  $24 - 16$  \_\_\_\_\_

7.  $64 \div 8 - 7$  \_\_\_\_\_

3.  $55 \div 11$  \_\_\_\_\_

8.  $63 \times 8$  \_\_\_\_\_

4.  $9x + 17$  \_\_\_\_\_

9.  $8b + 7b$  \_\_\_\_\_

5.  $128 + 76$  \_\_\_\_\_

10.  $17c \div 3$  \_\_\_\_\_

**Directions** Identify the variable in each expression.

11.  $6x + 17$  \_\_\_\_\_

16.  $x - 83$  \_\_\_\_\_

12.  $8 \div 2b$  \_\_\_\_\_

17.  $4 + y$  \_\_\_\_\_

13.  $16y - 8$  \_\_\_\_\_

18.  $3m \div 5$  \_\_\_\_\_

14.  $k + 12$  \_\_\_\_\_

19.  $4x + 12$  \_\_\_\_\_

15.  $d \div 4$  \_\_\_\_\_

20.  $5d$  \_\_\_\_\_

**Directions** List the operation or operations used in each expression.

21.  $8y - 16$  \_\_\_\_\_

22.  $16 \times 32$  \_\_\_\_\_

23.  $32 + 6b$  \_\_\_\_\_

24.  $9 \cdot 17$  \_\_\_\_\_

25.  $(16 \div 8) - y$  \_\_\_\_\_

# Replacing Variables

**EXAMPLE**

This is how to evaluate whether an open statement is true or false.

**Step 1** Substitute a number for the variable.

$$6 + x = 11 \quad \text{when } x = 5$$

$$6 + 5 = \square$$

$$8 - a = 6 \quad \text{when } a = 3$$

$$8 - 3 = \square$$

**Step 2** Perform the operation.

$$6 + 5 = 11 \quad \text{is a true statement}$$

$$8 - 3 = 6 \quad \text{is a false statement}$$

**Directions** Read each statement. Substitute each given number for  $n$ .

Write whether the statement is *true* or *false* for the value of  $n$ .

**Statement:**  $6n = 30$

1.  $n = 3$  \_\_\_\_\_

2.  $n = 6$  \_\_\_\_\_

3.  $n = 5$  \_\_\_\_\_

**Statement:**  $12 - n = 7$

4.  $n = 10$  \_\_\_\_\_

5.  $n = 5$  \_\_\_\_\_

6.  $n = 7$  \_\_\_\_\_

**Statement:**  $21 + n = 28$

7.  $n = 4$  \_\_\_\_\_

8.  $n = 16$  \_\_\_\_\_

9.  $n = 7$  \_\_\_\_\_

**Statement:**  $36 \div n = 4$

10.  $n = 9$  \_\_\_\_\_

11.  $n = 6$  \_\_\_\_\_

12.  $n = 5$  \_\_\_\_\_

**Directions** Evaluate each expression.

13.  $m + 17$  when  $m$  is 15 \_\_\_\_\_

14.  $3x - 6$  when  $x$  is 3 \_\_\_\_\_

15.  $18 \div g$  when  $g$  is 6 \_\_\_\_\_

16.  $21 + 2c$  when  $c$  is 5 \_\_\_\_\_

17.  $48 - g$  when  $g$  is 17 \_\_\_\_\_

18.  $n \div 4$  when  $n$  is 24 \_\_\_\_\_

19.  $8x$  when  $x$  is 8 \_\_\_\_\_

20.  $27 - 3y$  when  $y$  is 3 \_\_\_\_\_

# Place Value

**EXAMPLE**

165.8742

The digit 1 is in the hundreds place.

The digit 6 is in the tens place.

The digit 5 is in the ones place.

The digit 8 is in the tenths place.

The digit 7 is in the hundredths place.

The digit 4 is in the thousandths place.

The digit 2 is in the ten-thousandths place.

The value of the digit 6 is 60. The value of the digit 7 is 0.07.

0.7 = seven tenths    0.42 = forty-two hundredths

**Directions** Write each number in words.

1. 0.3 \_\_\_\_\_
2. 0.81 \_\_\_\_\_
3. 0.12 \_\_\_\_\_
4. 0.077 \_\_\_\_\_
5. 0.325 \_\_\_\_\_

**Directions** Write the number expressed by each phrase.

6. forty-two one-hundredths

\_\_\_\_\_

7. seven tenths

\_\_\_\_\_

8. two one-hundredths

\_\_\_\_\_

9. thirty-three one-thousandths

\_\_\_\_\_

10. twenty-five one-hundredths

\_\_\_\_\_

# Comparing and Rounding Decimals

**EXAMPLE**

Round 4.26 to the nearest tenth: 4.3

Round 8.241 to the nearest hundredth: 8.24

Round 2.7835 to the nearest thousandth: 2.784

Compare 6.8621 and 6.86.

Add two zeros to 6.86: 6.8600

 $6.8621 > 6.8600$        $6.8621 > 6.86$ **Directions** Round each decimal to the nearest tenth.

1. 46.87 \_\_\_\_\_

4. 2.098 \_\_\_\_\_

2. 108.21 \_\_\_\_\_

5. 39.03 \_\_\_\_\_

3. 16.967 \_\_\_\_\_

**Directions** Round each decimal to the nearest hundredth.

6. 199.987 \_\_\_\_\_

9. 77.8061 \_\_\_\_\_

7. 20.062 \_\_\_\_\_

10. 10.7777 \_\_\_\_\_

8. 5.9927 \_\_\_\_\_

**Directions** Round each decimal to the nearest thousandth.

11. 13.4259 \_\_\_\_\_

14. 12.6669 \_\_\_\_\_

12. 0.0571 \_\_\_\_\_

15. 251.7032 \_\_\_\_\_

13. 399.1129 \_\_\_\_\_

**Directions** Compare each pair of decimals. Write  $<$  or  $>$ .16. 17.092 ☐ 17.09 \_\_\_\_\_21. 25.77 ☐ 25.771 \_\_\_\_\_17. 2.3 ☐ 2.31 \_\_\_\_\_22. 0.8871 ☐ 0.88711 \_\_\_\_\_18. 937.328 ☐ 937.32 \_\_\_\_\_23. 33.99 ☐ 33.909 \_\_\_\_\_19. 14.8276 ☐ 14.82 \_\_\_\_\_24. 406.22 ☐ 406.222 \_\_\_\_\_20. 8.901 ☐ 8.9017 \_\_\_\_\_25. 7.63954 ☐ 7.639549 \_\_\_\_\_

# Adding and Subtracting Decimals

**EXAMPLE**

To find the perimeter of a triangle, use the formula  $P = a + b + c$  where  $a$ ,  $b$ , and  $c$  are the lengths of the sides of the triangle.

Triangle A:  $a = 4.23$  cm  $b = 13.1$  cm  $c = 10.012$  cm

To add or subtract decimals, add zeros where necessary and line up the decimal points.

$$\begin{array}{r} 4.230 \\ 13.100 \\ + 10.012 \\ \hline 27.342 \text{ cm} \end{array}$$

**Directions** The numbers below show the length of each side of a triangle. Find the perimeter of each triangle.

- |                                       |  |
|---------------------------------------|--|
| 1. 3.42 cm, 8.19 cm, 4.5 cm _____     | 6. 13.459 cm, 17.847 cm, 19.003 cm _____ |
| 2. 0.663 cm, 1.12 cm, 0.997 cm _____  | 7. 29.317 cm, 33.822 cm, 21.1 cm _____   |
| 3. 18.02 cm, 16.477 cm, 13.9 cm _____ | 8. 0.168 cm, 3.04 cm, 2.3 cm _____       |
| 4. 1.7 cm, 2.34 cm, 2.11 cm _____     | 9. 7.65 cm, 6.011 cm, 9.7 cm _____       |
| 5. 8.176 cm, 12.5 cm, 10.015 cm _____ |  |

**Directions** Add or subtract the dollar amounts.

- |                                |                               |
|--------------------------------|-------------------------------|
| 10. $\$39.75 - \$18.98$ _____  | 14. $\$1.45 - \$0.76$ _____   |
| 11. $\$0.84 - \$0.67$ _____    | 15. $\$991.81 - \$4.92$ _____ |
| 12. $\$494.16 + \$78.87$ _____ | 16. $\$323.13 + \$9.99$ _____ |
| 13. $\$100.00 - \$16.29$ _____ | 17. $\$17.32 - \$0.54$ _____  |

**Directions** Solve the problems.

18. Jon and Brooke each planted a bean seed. Jon's plant grew to 9.967 cm. Brooke's plant grew to 13.14 cm. How much taller was Brooke's plant than Jon's? \_\_\_\_\_
19. Alana earned \$9.75 selling vegetables from her garden in June, \$62 in July, and \$109.25 in August. What were Alana's total earnings from her garden for the three months? \_\_\_\_\_
20. Julio rode his bicycle 32.097 miles on Saturday and 9.84 miles on Sunday. How many more miles did he ride on Saturday than on Sunday? \_\_\_\_\_

# Multiplying Decimals by Powers of 10

**EXAMPLE**

$$10^2 = 100 \quad 10^3 = 1,000 \quad 10^4 = 10,000$$

$$8.52 \times 100 = 852$$

Move the decimal point two places to the right.

$$5.37 \times 10^3 = 5,370$$

Move the decimal point three places to the right.

**Directions** Rewrite each operation by replacing the power of 10 with its equivalent number. Then multiply.

$$45.6 \times 10^3$$

$$45.6 \times 1,000$$

$$45,600$$

$$2.345 \times 10^1$$

1. \_\_\_\_\_

2. \_\_\_\_\_

$$17.425 \times 10^2$$

3. \_\_\_\_\_

4. \_\_\_\_\_

$$8.7 \times 10^4$$

5. \_\_\_\_\_

6. \_\_\_\_\_

$$0.0651 \times 10^5$$

7. \_\_\_\_\_

8. \_\_\_\_\_

$$643 \times 10^2$$

9. \_\_\_\_\_

10. \_\_\_\_\_

**Directions** Rewrite each operation by writing the multiple of 10 as a power of 10. Then multiply.

$$12.8 \times 100$$

$$12.8 \times 10^2$$

$$1,280$$

$$0.53219 \times 1,000$$

11. \_\_\_\_\_

12. \_\_\_\_\_

$$44.22 \times 10$$

13. \_\_\_\_\_

14. \_\_\_\_\_

$$1.359 \times 10,000$$

15. \_\_\_\_\_

16. \_\_\_\_\_

$$39.71 \times 100,000$$

17. \_\_\_\_\_

18. \_\_\_\_\_

$$0.07125 \times 100$$

19. \_\_\_\_\_

20. \_\_\_\_\_

# Multiplying Decimals

**EXAMPLE**

To find the circumference of a circle, use the formula  $C = \pi d$ .

$C$  = circumference       $\pi$  = pi (about 3.14)       $d$  = diameter

Find the circumference of a circle with a diameter of 4.3 cm.

$$C = \pi \times 4.3$$

$$C = 3.14 \times 4.3$$

$$\begin{array}{r} 3.14 \\ \times 4.3 \\ \hline 942 \\ 1256 \\ \hline 13.502 \end{array}$$

$$C = 13.502 \text{ cm}$$

**Directions** Find the circumference of each circle with the diameter shown.

You may use your calculator.

1.  $d = 7.2 \text{ cm}$  \_\_\_\_\_

2.  $d = 2.9 \text{ inches}$  \_\_\_\_\_

3.  $d = 14 \text{ cm}$  \_\_\_\_\_

4.  $d = 18.12 \text{ cm}$  \_\_\_\_\_

5.  $d = 5.67 \text{ inches}$  \_\_\_\_\_

6.  $d = 0.53 \text{ inches}$  \_\_\_\_\_

7.  $d = 64.3 \text{ cm}$  \_\_\_\_\_

8.  $d = 29.1 \text{ inches}$  \_\_\_\_\_

9.  $d = 13.37 \text{ cm}$  \_\_\_\_\_

10.  $d = 3.693 \text{ cm}$  \_\_\_\_\_

**Directions** Multiply.

11.  $4.36 \times 7$  \_\_\_\_\_

12.  $9.11 \times 4$  \_\_\_\_\_

13.  $5.46 \times 3$  \_\_\_\_\_

14.  $12.07 \times 3.2$  \_\_\_\_\_

15.  $2.8 \times 7.1$  \_\_\_\_\_

16.  $8.13 \times 23.22$  \_\_\_\_\_

17.  $90.17 \times 3.21$  \_\_\_\_\_

18.  $4.305 \times 0.216$  \_\_\_\_\_

19.  $77.12 \times 9.332$  \_\_\_\_\_

20.  $81.51 \times 3.67$  \_\_\_\_\_



# Dividing Decimals by Powers of 10

**EXAMPLE**

$$2.6 \div 100 = 0.026$$

Move the decimal point two places to the left.

$$643.50 \div 1,000 = 0.6435$$

Move the decimal point three places to the left.

**Directions** Complete the chart by dividing each number by the power of 10 shown.

	$10^1$	$10^2$	$10^3$	$10^4$
824.2	82.42	1.	0.8242	2.
61.49	3.	4.	5.	6.
0.267	7.	8.	9.	10.
3.195	11.	12.	13.	14.
0.53	15.	16.	17.	18.
184.75	19.	20.	21.	22.
7.08	23.	24.	25.	26.
14.85	27.	28.	29.	30.

# Dividing Decimals

**EXAMPLE**

$$\begin{array}{r} 3.68 \\ 5 \overline{)18.40} \\ \underline{-15} \phantom{00} \\ 34 \phantom{00} \\ \underline{-30} \phantom{00} \\ 40 \phantom{00} \\ \underline{-40} \phantom{00} \\ 0 \end{array}$$

$$1.5 \overline{)9.75}$$

$$\begin{array}{r} 6.5 \\ 15 \overline{)97.5} \\ \underline{-90} \phantom{00} \\ 75 \phantom{00} \\ \underline{-75} \phantom{00} \\ 0 \end{array}$$

**Directions** Divide.

1.  $18.76 \div 4$  \_\_\_\_\_

6.  $59.90 \div 5$  \_\_\_\_\_

2.  $78.84 \div 8$  \_\_\_\_\_

7.  $121.28 \div 32$  \_\_\_\_\_

3.  $48.96 \div 3$  \_\_\_\_\_

8.  $223.14 \div 6$  \_\_\_\_\_

4.  $18.84 \div 12$  \_\_\_\_\_

9.  $154.62 \div 9$  \_\_\_\_\_

5.  $28.71 \div 9$  \_\_\_\_\_

10.  $119.32 \div 4$  \_\_\_\_\_

**Directions** Divide. Round your answer to the nearest hundredth.  
You may use your calculator.

11.  $58.86 \div 0.6$  \_\_\_\_\_

16.  $728.52 \div 1.2$  \_\_\_\_\_

12.  $4.851 \div 0.3$  \_\_\_\_\_

17.  $34.84 \div 0.04$  \_\_\_\_\_

13.  $137.28 \div 5.2$  \_\_\_\_\_

18.  $0.8665 \div 0.05$  \_\_\_\_\_

14.  $35.87 \div 1.74$  \_\_\_\_\_

19.  $75.12 \div 0.823$  \_\_\_\_\_

15.  $155.52 \div 8.1$  \_\_\_\_\_

20.  $385.14 \div 2.1$  \_\_\_\_\_

## Using Decimals

1. Luis brought 12 pounds of aluminum cans to the recycling center. He received \$3.36. How much does the recycling center pay for each pound of aluminum? \_\_\_\_\_
2. The average temperature in Key West, Florida, is  $77.7^{\circ}\text{F}$ . The average temperature in International Falls, Minnesota, is  $36.4^{\circ}\text{F}$ . On average, how much warmer is it in Key West than in International Falls? \_\_\_\_\_
3. A small swimming pool holds 5,263 gallons of water. A bathtub holds 55.4 gallons of water. How many times would you have to fill the bathtub to use the amount of water it takes to fill the pool? \_\_\_\_\_
4. Sam earned \$5.75 for mowing the lawn, \$14.50 for delivering newspapers, and \$12.00 for washing windows last week. How much did he earn? \_\_\_\_\_
5. The George Washington Bridge is 1,066.8 m long. The Golden Gate Bridge is 213.4 m longer than the George Washington Bridge. How long is the Golden Gate Bridge? \_\_\_\_\_
6. Gina rode 496.24 miles on a bicycle trip. The trip took 9 days. What was the average number of miles Gina rode each day? Round your answer to the nearest tenth. \_\_\_\_\_
7. A recipe for fruit salad calls for 1.5 pounds of apples, 2 pounds of oranges, and 1.25 pounds of grapes. At the market, apples cost \$0.69 per pound, oranges cost \$0.79 per pound, and grapes cost \$0.86 per pound. How much will it cost to make the fruit salad? \_\_\_\_\_
8. Jim's grandparents sent him \$35.00 for his birthday. He bought a CD for \$12.99 and put \$15.00 in his savings account. How much did Jim have left? \_\_\_\_\_
9. Kay purchased 16 tomato plants for \$0.48 each. How much did she spend? \_\_\_\_\_
10. A camper hiked 41.7 kilometers on the first day, 21.2 kilometers on the second day, and 37.4 kilometers on the third day. How many more kilometers did the camper hike on the first two days than on the third day? \_\_\_\_\_

# Decimals and Fractions

**EXAMPLE**

Write 0.25 as a fraction. 5 is in the hundredths place. The denominator is 100.

$$\frac{25}{100} = \frac{1}{4}$$

Write  $\frac{29}{100}$  as a decimal.

0.29

Write  $\frac{30}{50}$  as a decimal.

$$\frac{30}{50} = \frac{30 \times 2}{50 \times 2} = \frac{60}{100}$$

$$\frac{60}{100} = 0.60$$

**Directions** Write the denominator that would be used to change each decimal to a fraction.

1. 0.7 \_\_\_\_\_

4. 0.1 \_\_\_\_\_

2. 0.21 \_\_\_\_\_

5. 0.119 \_\_\_\_\_

3. 0.03 \_\_\_\_\_

**Directions** Write each decimal as a fraction. Simplify.

6. 0.34 \_\_\_\_\_

11. 0.13 \_\_\_\_\_

7. 0.24 \_\_\_\_\_

12. 3.08 \_\_\_\_\_

8. 0.45 \_\_\_\_\_

13. 0.006 \_\_\_\_\_

9. 0.010 \_\_\_\_\_

14. 0.36 \_\_\_\_\_

10. 0.2 \_\_\_\_\_

15. 7.8 \_\_\_\_\_

**Directions** Write each fraction as a decimal.

16.  $\frac{8}{25}$  \_\_\_\_\_

21.  $3\frac{18}{25}$  \_\_\_\_\_

17.  $\frac{3}{20}$  \_\_\_\_\_

22.  $\frac{3}{8}$  \_\_\_\_\_

18.  $1\frac{7}{50}$  \_\_\_\_\_

23.  $7\frac{1}{5}$  \_\_\_\_\_

19.  $\frac{29}{40}$  \_\_\_\_\_

24.  $\frac{61}{100}$  \_\_\_\_\_

20.  $\frac{13}{20}$  \_\_\_\_\_

25.  $\frac{16}{25}$  \_\_\_\_\_

# Repeating Decimals

**EXAMPLE**

To change degrees Fahrenheit to degrees Celsius, use the formula  $C = \frac{5}{9}(F - 32)$ .

45 degrees F = how many degrees Celsius?

$$C = \frac{5}{9}(45 - 32)$$

$$C = \frac{5}{9}(13)$$

$$C = \frac{65}{9}$$

$C = 7.2222$  To write a repeating decimal, write a bar over the repeating digits.

$$7.\overline{2}$$

You may round off a temperature to the nearest degree:  $7^{\circ}\text{C}$

**Directions** Find the Celsius temperature for each Fahrenheit temperature.  
Round each answer to the nearest whole degree.

1.  $F = 24^{\circ}$  \_\_\_\_\_

2.  $F = 109^{\circ}$  \_\_\_\_\_

3.  $F = 84^{\circ}$  \_\_\_\_\_

4.  $F = 68^{\circ}$  \_\_\_\_\_

5.  $F = 32^{\circ}$  \_\_\_\_\_

6.  $F = 76^{\circ}$  \_\_\_\_\_

7.  $F = 42^{\circ}$  \_\_\_\_\_

8.  $F = 164^{\circ}$  \_\_\_\_\_

9.  $F = 52^{\circ}$  \_\_\_\_\_

10.  $F = 90^{\circ}$  \_\_\_\_\_

**Directions** Write each fraction as a repeating decimal.

11.  $\frac{2}{9}$  \_\_\_\_\_

12.  $\frac{8}{15}$  \_\_\_\_\_

13.  $\frac{5}{9}$  \_\_\_\_\_

14.  $\frac{1}{6}$  \_\_\_\_\_

15.  $\frac{4}{15}$  \_\_\_\_\_

16.  $\frac{7}{9}$  \_\_\_\_\_

17.  $\frac{3}{11}$  \_\_\_\_\_

18.  $\frac{7}{12}$  \_\_\_\_\_

19.  $\frac{13}{18}$  \_\_\_\_\_

20.  $\frac{2}{11}$  \_\_\_\_\_

## Renaming Percents to Decimals

**EXAMPLE**

$$5\% = 0.05$$

$$8\frac{1}{2}\% = .085$$

What is the interest for one year on a principal of \$600 at a rate of 7%?

$$I = p \times r \times t$$

$$I = 600 \times 0.07 \times 1$$

$$I = \$42.00$$

**Directions** Change each percent to a decimal.

1. 18% \_\_\_\_\_

2. 94% \_\_\_\_\_

3. 0.3% \_\_\_\_\_

4.  $2\frac{3}{4}\%$  \_\_\_\_\_

5. 29% \_\_\_\_\_

6. 300% \_\_\_\_\_

7. 48% \_\_\_\_\_

8. 1.2% \_\_\_\_\_

9. 81% \_\_\_\_\_

10. 2% \_\_\_\_\_

**Directions** Find the interest each principal will earn. If necessary, round each answer to the nearest cent.

11. Principal: \$18,500

Rate: 9.75%

Time: 9 months

\_\_\_\_\_

14. Principal: \$6,400

Rate: 5%

Time: 2 years

\_\_\_\_\_

12. Principal: \$750

Rate: 6.75%

Time: 6 months

\_\_\_\_\_

15. Principal: \$11,650

Rate: 7%

Time: 3 months

\_\_\_\_\_

13. Principal: \$1,200

Rate: 5.75%

Time: 1 year

\_\_\_\_\_

## Evaluating Expressions with Decimals

**EXAMPLE**Evaluate  $6.21n$  when  $n = 3.2$ 

$$6.21 \times 3.2 = 19.872$$

**Directions** Evaluate each expression.

1.  $p - 8.02$  when  $p = 62.35$  \_\_\_\_\_
2.  $n + 14.375$  when  $n = 0.027$  \_\_\_\_\_
3.  $s \div 0.125$  when  $s = 3$  \_\_\_\_\_
4.  $73.21a$  when  $a = 1.19$  \_\_\_\_\_
5.  $9p + 16n$  when  $p = 7.26$  and  $n = 0.24$  \_\_\_\_\_

**Directions** Solve each problem.

6. Lucia has  $n$  dollars. Kelly has \$12.81 more than Lucia. Write an algebraic expression for how much money Kelly has. Then evaluate the expression when  $n = \$37.65$ .  
\_\_\_\_\_  
\_\_\_\_\_
7. Fox Hills has  $l$  number of lots with 4.2 acres in each lot. Forest Point has  $m$  number of lots with 5.6 acres in each lot. Write an algebraic expression showing how many acres are in Fox Hills and Forest Point combined. Then evaluate the expression when  $l = 13$  and  $m = 8$ .  
\_\_\_\_\_  
\_\_\_\_\_
8. Anthony has  $p$  dollars in his bank account. He spends \$42.95 on a sweater. Write an algebraic expression for how much Anthony will have left in the bank after he buys the sweater. Then evaluate the expression when  $p = \$116.80$ .  
\_\_\_\_\_  
\_\_\_\_\_
9. Jim has  $n$  number of employees. His payroll totals \$4,503.04 per week. Write an algebraic expression for how much each employee is paid per week if all employees receive equal pay. Then evaluate the expression when  $n = 8$ .  
\_\_\_\_\_  
\_\_\_\_\_
10. Martina sold  $l$  number of paintings. Each painting cost \$125.75. Write an algebraic expression for the total amount Martina made on her paintings. Then evaluate the expression when  $l = 18$ .  
\_\_\_\_\_  
\_\_\_\_\_

## Divisibility Rules

**EXAMPLE**

A number that can be divided by a whole number with no remainder is said to be divisible.

The symbol  $|$  means divides.

$2|10$  is a true statement because 10 is divisible by 2 and there is no remainder.

$$10 \div 2 = 5 \text{ (no remainder)}$$

$2|17$  is a false statement because 17 is not divisible by 2 without leaving a remainder.

$$17 \div 2 = 8 \text{ r}1$$

**Directions** Write *true* if the statement is true and *false* if the statement is false. Write a division equation to prove your answer.

- |             |       |       |
|-------------|-------|-------|
| 1. $5 15$   | _____ | _____ |
| 2. $4 36$   | _____ | _____ |
| 3. $6 39$   | _____ | _____ |
| 4. $8 40$   | _____ | _____ |
| 5. $9 82$   | _____ | _____ |
| 6. $6 46$   | _____ | _____ |
| 7. $3 90$   | _____ | _____ |
| 8. $5 85$   | _____ | _____ |
| 9. $4 128$  | _____ | _____ |
| 10. $8 374$ | _____ | _____ |
| 11. $2 577$ | _____ | _____ |
| 12. $4 634$ | _____ | _____ |
| 13. $9 567$ | _____ | _____ |
| 14. $7 473$ | _____ | _____ |
| 15. $8 688$ | _____ | _____ |



# Prime and Composite Numbers

**EXAMPLE**

A prime number has two factors: 1 and itself

5 is a prime number. Its factors are 5 and 1.  $5 \times 1 = 5$

A composite number has factors other than 1 and itself.

14 is a composite number. Its two factors are 7 and 2.  $7 \times 2 = 14$

**Directions** Write the numbers in each pair in the correct column to show which number is a prime number and which number is a composite number.

	Prime	Composite
1. 3, 6		
2. 8, 17		
3. 27, 31		
4. 5, 12		
5. 13, 16		
6. 43, 50		
7. 20, 41		
8. 83, 106		
9. 125, 149		
10. 97, 221		

	Prime	Composite
11. 7, 12		
12. 20, 37		
13. 38, 41		
14. 81, 89		
15. 67, 121		
16. 72, 79		
17. 177, 691		
18. 197, 221		
19. 109, 301		
20. 108, 239		

**Directions** Circle two factors for each composite number.

21. 18    2    5    8    9
22. 21    3    5    7    8
23. 15    3    4    5    6
24. 24    4    5    6    9
25. 32    3    4    6    8

26. 35    4    5    6    7
27. 48    5    6    8    9
28. 45    2    4    5    9
29. 12    3    4    5    7
30. 30    4    5    6    8

# Greatest Common Divisor

**EXAMPLE**

To find the greatest common divisor (GCD) of two numbers, list all the factors.  
The greatest common factor is the greatest common divisor.

(14, 21)	14:	1	2	7	14
	21:	1	3	7	21

7 is the greatest common divisor (GCD) of 14 and 21.

**Directions** Write the factors for each number. Then write the greatest common divisor (GCD).

	Factors	GCD
1. (9, 24)	9: _____ 24: _____	_____
2. (14, 28)	14: _____ 28: _____	_____
3. (8, 16)	8: _____ 16: _____	_____
4. (11, 77)	11: _____ 77: _____	_____
5. (4, 20)	4: _____ 20: _____	_____
6. (3x, 21)	3x: _____ 21: _____	_____
7. (8, 48y)	8: _____ 48y: _____	_____
8. (12x, 60x)	12x: _____ 60x: _____	_____
9. (7a, 42a)	7a: _____ 42a: _____	_____
10. (6c, 54c)	6c: _____ 54c: _____	_____

# Factoring

**EXAMPLE**

Factor  $6x + 8$ .

**Step 1** Find the greatest common divisor.

$$\begin{array}{rclclcl} 6x: & 1 & \textcircled{2} & 3 & 6 & x \\ 8: & 1 & \textcircled{2} & 4 & 8 & \end{array}$$

**Step 2** Write the GCD outside parentheses.  $2( \quad )$

**Step 3** Use the distributive property in reverse.  $2(3x + 4)$

**Step 4** Check using the distributive property.

$$2(3x + 4) = (2 \cdot 3x) + (2 \cdot 4) = 6x + 8$$

**Directions** Circle the GCD for each expression.

1.  $3x + 9$       1      3      9

6.  $30y + 36z$       3      5      6

2.  $12y + 18$       2      3      6

7.  $9d + 54e$       3      6      9

3.  $32b + 8$       4      8      16

8.  $3c + 7y$       1      3      7

4.  $44a + 4$       2      4      11

9.  $25d + 100c$       4      5      25

5.  $10z + 50b$       2      5      10

10.  $18x + 33y$       3      6      11

**Directions** Use the distributive property to factor each expression.

11.  $18x + 12$       \_\_\_\_\_

16.  $54b + 9w$       \_\_\_\_\_

12.  $6y + 8$       \_\_\_\_\_

17.  $20m + 15k$       \_\_\_\_\_

13.  $3c + 9$       \_\_\_\_\_

18.  $12n + 4p$       \_\_\_\_\_

14.  $6a + 15$       \_\_\_\_\_

19.  $9q + 81c$       \_\_\_\_\_

15.  $2h + 11$       \_\_\_\_\_

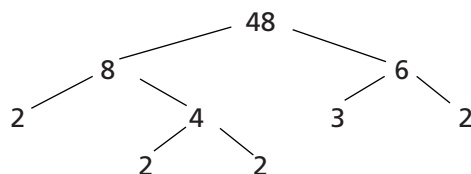
20.  $ab + bc$       \_\_\_\_\_

# Least Common Multiple

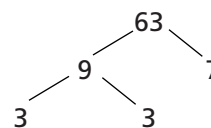
## EXAMPLE

Find the least common multiple (LCM) of 48 and 63.

**Step 1** Write the prime factorization of each number.



$2 \cdot 2 \cdot 2 \cdot 2 \cdot 3$  or  $2^4 \cdot 3$   
(prime factorization)



$3 \cdot 3 \cdot 7$  or  $3^2 \cdot 7$   
(prime factorization)

**Step 2** Identify the greatest power of each prime factor.

The greatest power of the prime factor 2 is  $2^4$ .

The greatest power of the prime factor 3 is  $3^2$ .

The greatest power of the prime factor 7 is 7.

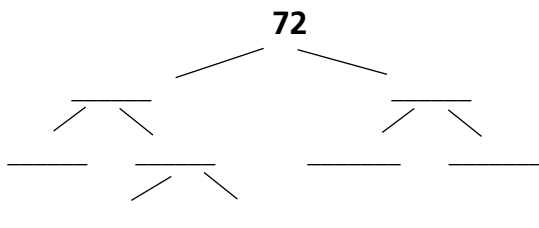
**Step 3** Find the product.

$$2^4 \cdot 3^2 \cdot 7 = 16 \cdot 9 \cdot 7 = 1,008$$

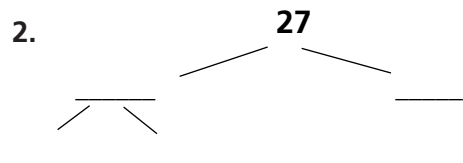
The LCM of 48 and 63 is 1,008.

**Directions** Complete each factor tree.

1.



2.



**Directions** Write the prime factorization for each factor tree above.

3. \_\_\_\_\_

4. \_\_\_\_\_

**Directions** Find each least common multiple (LCM).

5. LCM (4, 12) \_\_\_\_\_

9. LCM (10, 28) \_\_\_\_\_

6. LCM (5, 18) \_\_\_\_\_

10. LCM (21, 24) \_\_\_\_\_

7. LCM (30, 60) \_\_\_\_\_

8. LCM (16, 35) \_\_\_\_\_

# Scientific Notation

## EXAMPLE

To write large numbers using scientific notation, move the decimal to make a number between 1 and 10.

Count the number of places the decimal was moved.

$$65,000,000 = 6.5 \times 10^7$$

7 654 321 (number of places from the decimal point = 7)

$$0.658 = 6.58 \times 10^{-1} \text{ (number of places from the decimal point = 1)}$$

If the decimal is moved to the left, the exponent is positive. ( $10^7$ )

If the decimal is moved to the right, the exponent is negative. ( $10^{-1}$ )

**Directions** To write the number in scientific notation: Write how many places each decimal must be moved. Write *left* or *right* to tell in which direction to move the decimal point.

Number	Places Moved	Direction	Scientific Notation
1. 325,000	_____	_____	_____
2. 27,800	_____	_____	_____
3. 105,000,000	_____	_____	_____
4. 0.653	_____	_____	_____
5. 0.0325	_____	_____	_____
6. 0.0000817	_____	_____	_____
7. 681,000,000,000	_____	_____	_____
8. 0.000000783	_____	_____	_____
9. 0.00001818	_____	_____	_____
10. 86,000,000,000	_____	_____	_____

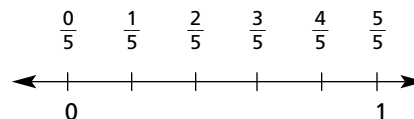
**Directions** Write the number that each example of scientific notation stands for.

- |                        |       |                           |       |
|------------------------|-------|---------------------------|-------|
| 11. $6.2 \times 10^2$  | _____ | 14. $7.15 \times 10^{-1}$ | _____ |
| 12. $8.7 \times 10^4$  | _____ | 15. $3.84 \times 10^{-2}$ | _____ |
| 13. $3.87 \times 10^8$ | _____ |                           |       |

# Proper Fractions

**EXAMPLE**

Which proper fractions are named by this number line?

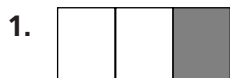


**Step 1** Count the total number of marks between 0 and 1, including the mark at 1. This will tell you the denominator.

**Step 2** Counting each mark away from 0 will tell you the numerator.

The following are proper fractions:  $\frac{0}{5}$   $\frac{1}{5}$   $\frac{2}{5}$   $\frac{3}{5}$   $\frac{4}{5}$ .

**Directions** Write the proper fraction that represents the shaded part of each whole or set.

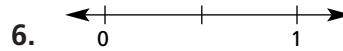
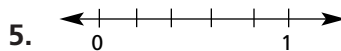
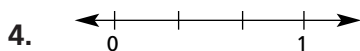


\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

**Directions** Which proper fractions are named by these number lines?



\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

**Directions** Write a proper fraction to answer each question.

7. Julie has 15 new pencils. Eleven of them are primary colors. What part of the total number of pencils are primary colors? \_\_\_\_\_
8. Ed took a survey of students in his math class. Fifteen out of a total of twenty-one students have pets. What part of the total number of students have pets? \_\_\_\_\_
9. Twenty-three students in Mrs. Edwards' music class were also taking Spanish. Mrs. Edwards has a total of 27 students. What part of the total class was taking Spanish? \_\_\_\_\_
10. Isaac checked out eight books from the library. He read only three of them before he had to return them. What part of the whole number of books did he read? \_\_\_\_\_

# Improper Fractions and Mixed Numbers

**EXAMPLE**Express  $\frac{11}{3}$  as a mixed number.

$$\frac{11}{3} = 11 \div 3 = 3 \overline{)11}$$
$$\begin{array}{r} 3 \overline{)11} \\ \underline{-9} \phantom{0} \\ 2 \phantom{0} \end{array}$$

Write the remainder as a fraction:  $\frac{11}{3} = 3\frac{2}{3}$ **Directions** Express each improper fraction as a mixed or whole number.

1.  $\frac{8}{3}$  \_\_\_\_\_

2.  $\frac{9}{5}$  \_\_\_\_\_

3.  $\frac{10}{2}$  \_\_\_\_\_

4.  $\frac{21}{6}$  \_\_\_\_\_

5.  $\frac{11}{8}$  \_\_\_\_\_

6.  $\frac{25}{8}$  \_\_\_\_\_

7.  $\frac{32}{5}$  \_\_\_\_\_

8.  $\frac{12}{11}$  \_\_\_\_\_

9.  $\frac{36}{6}$  \_\_\_\_\_

10.  $\frac{32}{10}$  \_\_\_\_\_

11.  $\frac{15}{4}$  \_\_\_\_\_

12.  $\frac{7}{7}$  \_\_\_\_\_

13.  $\frac{9}{2}$  \_\_\_\_\_

14.  $\frac{26}{19}$  \_\_\_\_\_

15.  $\frac{8}{7}$  \_\_\_\_\_

**Directions** Express each number as an improper fraction.

16.  $4\frac{2}{3}$  \_\_\_\_\_

17.  $2\frac{5}{8}$  \_\_\_\_\_

18.  $5\frac{1}{3}$  \_\_\_\_\_

19.  $1\frac{9}{11}$  \_\_\_\_\_

20.  $4\frac{2}{7}$  \_\_\_\_\_

21.  $68\frac{1}{3}$  \_\_\_\_\_

22.  $12\frac{1}{2}$  \_\_\_\_\_

23.  $7\frac{7}{8}$  \_\_\_\_\_

24.  $12\frac{3}{4}$  \_\_\_\_\_

25.  $7\frac{1}{2}$  \_\_\_\_\_

26.  $9\frac{3}{4}$  \_\_\_\_\_

27.  $33\frac{1}{2}$  \_\_\_\_\_

28.  $14\frac{1}{5}$  \_\_\_\_\_

29.  $9\frac{9}{10}$  \_\_\_\_\_

30.  $18\frac{4}{5}$  \_\_\_\_\_

# Equivalent Fractions

**EXAMPLE**

Write an equivalent fraction for  $\frac{2}{5}$ .

Multiply the numerator and the denominator of  $\frac{2}{5}$  by 3.

$$\frac{2}{5} \cdot \frac{3}{3} = \frac{6}{15}$$

**Directions** Write two equivalent fractions for each fraction.

1.  $\frac{2}{3}$  \_\_\_\_\_

5.  $\frac{2}{5}$  \_\_\_\_\_

9.  $\frac{1}{2}$  \_\_\_\_\_

2.  $\frac{3}{4}$  \_\_\_\_\_

6.  $\frac{7}{10}$  \_\_\_\_\_

10.  $\frac{3}{10}$  \_\_\_\_\_

3.  $\frac{5}{6}$  \_\_\_\_\_

7.  $\frac{2}{7}$  \_\_\_\_\_

4.  $\frac{1}{16}$  \_\_\_\_\_

8.  $\frac{5}{9}$  \_\_\_\_\_

**EXAMPLE**

Use a calculator to decide if  $\frac{3}{8}$  and  $\frac{9}{24}$  are equal.

For  $\frac{3}{8}$ : Press 3  $\div$  8  $=$ . The display reads 0.375.

For  $\frac{9}{24}$ : Press 9  $\div$  24  $=$ . The display reads 0.375.

Since the answers are the same, the fractions are equal.

If the answers are not the same, the fractions are not equivalent.

**Directions** Use your calculator to decide if the two fractions are equivalent.

Write *yes* or *no*.

11.  $\frac{1}{2}$  and  $\frac{15}{30}$  \_\_\_\_\_

19.  $\frac{7}{8}$  and  $\frac{28}{32}$  \_\_\_\_\_

12.  $\frac{16}{35}$  and  $\frac{8}{17}$  \_\_\_\_\_

20.  $\frac{15}{30}$  and  $\frac{5}{10}$  \_\_\_\_\_

13.  $\frac{11}{12}$  and  $\frac{33}{40}$  \_\_\_\_\_

21.  $\frac{9}{15}$  and  $\frac{6}{8}$  \_\_\_\_\_

14.  $\frac{4}{20}$  and  $\frac{1}{4}$  \_\_\_\_\_

22.  $\frac{3}{21}$  and  $\frac{2}{14}$  \_\_\_\_\_

15.  $\frac{6}{7}$  and  $\frac{30}{35}$  \_\_\_\_\_

23.  $\frac{20}{30}$  and  $\frac{4}{6}$  \_\_\_\_\_

16.  $\frac{20}{55}$  and  $\frac{2}{5}$  \_\_\_\_\_

24.  $\frac{6}{12}$  and  $\frac{9}{20}$  \_\_\_\_\_

17.  $\frac{4}{5}$  and  $\frac{8}{10}$  \_\_\_\_\_

25.  $\frac{5}{8}$  and  $\frac{15}{16}$  \_\_\_\_\_

18.  $\frac{3}{4}$  and  $\frac{2}{3}$  \_\_\_\_\_



## Simplest Form

**EXAMPLE**

Find GCD (10, 15).

List all of the factors of each number and circle the common factors.

10:    1    2    5    1015:    1    3    5    15Choose the *greatest* common factor.    GCD (10, 15) = 5**Directions** Find the greatest common divisor (GCD) of each pair of numbers.

- |                  |                   |                  |
|------------------|-------------------|------------------|
| 1. (8, 24) _____ | 3. (14, 16) _____ | 5. (8, 10) _____ |
| 2. (5, 10) _____ | 4. (9, 12) _____  |                  |

**Directions** Express each fraction in simplest form.

- |                           |                            |                            |
|---------------------------|----------------------------|----------------------------|
| 6. $\frac{10}{15}$ _____  | 12. $\frac{8}{20}$ _____   | 18. $\frac{27}{54}$ _____  |
| 7. $\frac{16}{24}$ _____  | 13. $\frac{6}{9}$ _____    | 19. $\frac{16}{48}$ _____  |
| 8. $\frac{78}{90}$ _____  | 14. $\frac{18}{20}$ _____  | 20. $\frac{81}{108}$ _____ |
| 9. $\frac{10}{50}$ _____  | 15. $\frac{48}{60}$ _____  | 21. $\frac{60}{90}$ _____  |
| 10. $\frac{55}{66}$ _____ | 16. $\frac{20}{80}$ _____  | 22. $\frac{30}{65}$ _____  |
| 11. $\frac{12}{15}$ _____ | 17. $\frac{63}{108}$ _____ |                            |

**Directions** Solve the problems.

23. Shelly said she has  $\frac{6}{8}$  of all the 1998 NFL collectors' cards. Mark said he has  $\frac{9}{12}$  of them. Do they have the same number of cards? Explain.
- \_\_\_\_\_
24. Ashley said  $\frac{3}{4}$  of her stuffed animals have button eyes. Pam said Ashley has 15 stuffed animals. Is it possible that Pam is correct? Explain.
- \_\_\_\_\_
25. Vince said his survey showed  $\frac{2}{3}$  of his math class liked rap music. There are 24 students in the class. Is it possible that Vince's survey is correct? Explain.
- \_\_\_\_\_

# Comparing and Ordering Fractions

**EXAMPLE**

Compare the fractions. Write  $>$  or  $<$ .

$$\frac{4}{5} \text{ — } \frac{3}{4}$$

**Step 1** Write equivalent fractions using the LCM.

$$\frac{4}{5} = \frac{16}{20}$$

$$\frac{3}{4} = \frac{12}{20}$$

**Step 2** Compare  $\frac{16}{20}$  and  $\frac{12}{20}$ .  $\frac{16}{20}$  is greater than  $\frac{12}{20}$ .  $\frac{4}{5} > \frac{3}{4}$

**Directions** Compare the fractions. Write  $>$  or  $<$ .

1.  $\frac{5}{8}$  —  $\frac{1}{2}$

4.  $\frac{4}{7}$  —  $\frac{2}{5}$

7.  $\frac{2}{3}$  —  $\frac{5}{12}$

10.  $4\frac{1}{2}$  —  $5\frac{2}{3}$

2.  $\frac{8}{9}$  —  $\frac{2}{3}$

5.  $\frac{1}{5}$  —  $\frac{1}{3}$

8.  $\frac{3}{16}$  —  $\frac{1}{4}$

11.  $6\frac{2}{5}$  —  $6\frac{3}{10}$

3.  $\frac{3}{4}$  —  $\frac{4}{5}$

6.  $\frac{6}{15}$  —  $\frac{9}{15}$

9.  $\frac{7}{8}$  —  $\frac{3}{4}$

**EXAMPLE**

Order  $\frac{2}{3}$ ,  $\frac{1}{2}$ , and  $\frac{3}{4}$  from least to greatest.

**Step 1** Write equivalent fractions using the LCM.

$$\frac{2}{3} = \frac{8}{12}$$

$$\frac{1}{2} = \frac{6}{12}$$

$$\frac{3}{4} = \frac{9}{12}$$

**Step 2** Compare  $\frac{8}{12}$ ,  $\frac{6}{12}$ , and  $\frac{9}{12}$ .  $\frac{6}{12} < \frac{8}{12} < \frac{9}{12}$

Therefore, the order from least to greatest is  $\frac{1}{2}$ ,  $\frac{2}{3}$ ,  $\frac{3}{4}$ .

**Directions** Order from least to greatest.

12.  $\frac{2}{3}$ ,  $\frac{3}{8}$ ,  $\frac{1}{2}$  \_\_\_\_\_

17.  $\frac{7}{10}$ ,  $\frac{3}{5}$ ,  $\frac{17}{20}$  \_\_\_\_\_

13.  $\frac{1}{2}$ ,  $\frac{1}{3}$ ,  $\frac{1}{4}$  \_\_\_\_\_

18.  $\frac{5}{16}$ ,  $\frac{9}{32}$ ,  $\frac{1}{4}$  \_\_\_\_\_

14.  $\frac{3}{4}$ ,  $\frac{3}{5}$ ,  $\frac{2}{3}$  \_\_\_\_\_

19.  $\frac{3}{35}$ ,  $\frac{3}{7}$ ,  $\frac{3}{5}$  \_\_\_\_\_

15.  $\frac{7}{8}$ ,  $\frac{1}{2}$ ,  $\frac{3}{4}$  \_\_\_\_\_

20.  $\frac{3}{8}$ ,  $\frac{5}{16}$ ,  $\frac{1}{2}$  \_\_\_\_\_

16.  $\frac{3}{16}$ ,  $\frac{7}{8}$ ,  $\frac{2}{3}$  \_\_\_\_\_

# Fractions—Like Denominators

**EXAMPLE**Find  $(1\frac{2}{3} + 2\frac{2}{3}) - 3\frac{1}{3}$ **Step 1** Perform the computation inside the ( ) first.

$$(1\frac{2}{3} + 2\frac{2}{3}) - 3\frac{1}{3} =$$

$$4\frac{1}{3} - 3\frac{1}{3} =$$

**Step 2** Perform the remaining computation.

$$4\frac{1}{3} - 3\frac{1}{3} = 1$$

**Directions** Add or subtract. If necessary, perform the computation inside the ( ) first. Write your answer in simplest form.

1.  $\frac{3}{5} - \frac{2}{5}$  \_\_\_\_\_

2.  $\frac{5}{6} + \frac{5}{6}$  \_\_\_\_\_

3.  $\frac{9}{10} - \frac{7}{10}$  \_\_\_\_\_

4.  $2\frac{15}{16} - 1\frac{7}{16}$  \_\_\_\_\_

5.  $11\frac{11}{12} - 5\frac{9}{12}$  \_\_\_\_\_

6.  $4\frac{3}{4} - 2\frac{1}{4}$  \_\_\_\_\_

7.  $6\frac{7}{15} + 8\frac{14}{15}$  \_\_\_\_\_

8.  $\frac{5x}{8} - \frac{3x}{8}$  \_\_\_\_\_

9.  $\frac{9x}{10} - \frac{6x}{10}$  \_\_\_\_\_

10.  $\frac{6}{y} + \frac{7}{y}$  \_\_\_\_\_

11.  $\frac{4}{y} + \frac{x}{y}$  \_\_\_\_\_

12.  $\frac{3x}{4} - \frac{x}{4}$  \_\_\_\_\_

13.  $\frac{y}{16} + \frac{9y}{16}$  \_\_\_\_\_

14.  $\frac{3y}{12} + \frac{5}{12}$  \_\_\_\_\_

15.  $\frac{4x}{9} + \frac{10x}{9}$  \_\_\_\_\_

16.  $(\frac{9}{10} + \frac{3}{10}) - \frac{4}{10}$  \_\_\_\_\_

17.  $\frac{3}{8} + (\frac{7}{8} - \frac{4}{8})$  \_\_\_\_\_

18.  $\frac{7}{16} - (\frac{1}{16} + \frac{3}{16})$  \_\_\_\_\_

19.  $(\frac{8}{11} - \frac{5}{11}) + \frac{6}{11}$  \_\_\_\_\_

20.  $\frac{11}{12} + (\frac{6}{12} - \frac{1}{12})$  \_\_\_\_\_

21.  $\frac{4}{6} - (\frac{4}{6} - \frac{2}{6})$  \_\_\_\_\_

22.  $\frac{3}{25} + (\frac{24}{25} - \frac{16}{25})$  \_\_\_\_\_

23.  $(\frac{3x}{8} + \frac{9x}{8}) - \frac{5x}{8}$  \_\_\_\_\_

24.  $\frac{2x}{3} + (\frac{2x}{3} - \frac{x}{3})$  \_\_\_\_\_

25.  $\frac{3y}{12} + (\frac{9y}{12} - \frac{5y}{12})$  \_\_\_\_\_

# Fractions—Unlike Denominators

**EXAMPLE**Add  $6\frac{2}{3} + 3\frac{1}{2}$ .**Step 1** Find the LCM of the denominators.

LCM (2, 3) = 6

**Step 2** Write an equivalent mixed number for each fraction using the LCM.

$$\frac{2}{3} \cdot \frac{2}{2} = \frac{4}{6}$$

$$6\frac{2}{3} = 6\frac{4}{6}$$

$$\frac{1}{2} \cdot \frac{3}{3} = \frac{3}{6}$$

$$3\frac{1}{2} = 3\frac{3}{6}$$

**Step 3** Add.  $6\frac{4}{6} + 3\frac{3}{6} = 9\frac{7}{6}$ **Step 4** Simplify.  $9\frac{7}{6} = 10\frac{1}{6}$ **Directions** Add or subtract. Write your answer in simplest form.

1.  $\frac{2}{3} + \frac{5}{6}$  \_\_\_\_\_

6.  $\frac{19}{20} - \frac{3}{4}$  \_\_\_\_\_

2.  $\frac{7}{8} - \frac{7}{16}$  \_\_\_\_\_

7.  $\frac{5}{8} + \frac{5}{6}$  \_\_\_\_\_

3.  $\frac{3}{4} + \frac{2}{3}$  \_\_\_\_\_

8.  $\frac{4}{5} - \frac{2}{3}$  \_\_\_\_\_

4.  $\frac{9}{10} - \frac{3}{4}$  \_\_\_\_\_

9.  $\frac{15}{16} + \frac{1}{2}$  \_\_\_\_\_

5.  $\frac{3}{5} - \frac{7}{45}$  \_\_\_\_\_

10.  $\frac{11}{12} + \frac{3}{4}$  \_\_\_\_\_

**Directions** Add or subtract. Write your answer in simplest form.

11.  $\frac{4x}{7} - \frac{x}{3}$  \_\_\_\_\_

14.  $\frac{1}{2y} + \frac{5}{16y}$  \_\_\_\_\_

12.  $\frac{1}{x} + \frac{4}{y}$  \_\_\_\_\_

15.  $\frac{3x}{4} - \frac{2x}{3}$  \_\_\_\_\_

13.  $\frac{5x}{12} + \frac{7x}{8}$  \_\_\_\_\_

**Directions** Add or subtract. Write your answer in simplest form.

16.  $5\frac{7}{8} + 6\frac{3}{5}$  \_\_\_\_\_

21.  $16\frac{5}{16} - 10\frac{7}{32}$  \_\_\_\_\_

17.  $2\frac{3}{7} - 1\frac{1}{3}$  \_\_\_\_\_

22.  $5\frac{5}{8} - 4\frac{2}{5}$  \_\_\_\_\_

18.  $8\frac{9}{10} + 6\frac{1}{5}$  \_\_\_\_\_

23.  $42\frac{5}{6} + 22\frac{7}{12}$  \_\_\_\_\_

19.  $10\frac{3}{5} - 2\frac{3}{10}$  \_\_\_\_\_

24.  $6\frac{3}{4}x + 2\frac{5}{8}x$  \_\_\_\_\_

20.  $2\frac{7}{12} + 13\frac{3}{4}$  \_\_\_\_\_

25.  $3\frac{4}{5}x - 2\frac{3}{10}x$  \_\_\_\_\_

# Subtracting Fractions with Regrouping

**EXAMPLE**

Solve  $4\frac{3}{8} - 2\frac{2}{3}$ .

**Step 1** Find the LCM of the denominators.

$$\text{LCM}(8, 3) = 24$$

**Step 2** Write equivalent mixed numbers for  $4\frac{3}{8}$  and  $2\frac{2}{3}$  using the LCM (24) as denominators.

$$4\frac{3}{8} = 4\frac{9}{24}$$

$$2\frac{2}{3} = 2\frac{16}{24}$$

**Step 3** Since  $\frac{16}{24}$  cannot be subtracted from  $\frac{9}{24}$ , it must be renamed.

$$4\frac{9}{24} = 3\frac{33}{24} \quad (\text{Think: } 4\frac{9}{24} = 3\frac{9}{24} + \frac{24}{24} = 3\frac{33}{24})$$

**Step 4** Subtract.

$$\begin{array}{r} 3\frac{33}{24} \\ - 2\frac{16}{24} \\ \hline 1\frac{17}{24} \end{array}$$

**Directions** Subtract. Write your answer in simplest form.

1.  $2\frac{1}{3} - 1\frac{5}{8}$  \_\_\_\_\_

5.  $16\frac{1}{8} - 8\frac{3}{8}$  \_\_\_\_\_

9.  $8\frac{3}{8} - 5\frac{3}{4}$  \_\_\_\_\_

2.  $6\frac{3}{4} - 2\frac{1}{2}$  \_\_\_\_\_

6.  $9\frac{3}{7} - 4\frac{6}{7}$  \_\_\_\_\_

10.  $4\frac{1}{3} - 1\frac{5}{6}$  \_\_\_\_\_

3.  $4\frac{3}{10} - 3\frac{13}{15}$  \_\_\_\_\_

7.  $21\frac{9}{15} - 6\frac{14}{15}$  \_\_\_\_\_

11.  $12\frac{15}{16} - 4\frac{3}{4}$  \_\_\_\_\_

4.  $6\frac{7}{10} - 4\frac{9}{10}$  \_\_\_\_\_

8.  $15\frac{3}{10} - 8\frac{1}{2}$  \_\_\_\_\_

12.  $32\frac{4}{9} - 17\frac{13}{18}$  \_\_\_\_\_

**Directions** Add or subtract.

13. Kerim jogged  $3\frac{3}{4}$  miles on Thursday. On Friday, he jogged  $\frac{2}{3}$  of a mile farther. How far did he jog on Friday? \_\_\_\_\_

14. Lejla caught a bass that was  $1\frac{7}{8}$  pounds and a trout that was  $3\frac{5}{8}$  pounds. How much heavier was the trout? \_\_\_\_\_

15. Mike studied  $3\frac{1}{3}$  hours after school on Tuesday. On Wednesday, he studied  $1\frac{3}{4}$  hours. How much longer did he study on Tuesday? \_\_\_\_\_

# Multiplying Fractions and Mixed Numbers

**EXAMPLE**Multiply  $1\frac{2}{3} \cdot 2\frac{1}{2}$ .**Step 1** Change the mixed numbers to improper fractions.

$$1\frac{2}{3} = \frac{5}{3} \qquad 2\frac{1}{2} = \frac{5}{2}$$

**Step 2** Multiply the numerators and denominators.

$$\frac{5}{3} \cdot \frac{5}{2} = \frac{5 \cdot 5}{3 \cdot 2} = \frac{25}{6}$$

**Step 3** Simplify.  $\frac{25}{6} = 4\frac{1}{6}$ **Directions** Multiply. Write your answer in simplest form.

1.  $\frac{1}{5} \cdot \frac{5}{6}$  \_\_\_\_\_

4.  $\frac{5}{9} \cdot \frac{9}{10}$  \_\_\_\_\_

7.  $\frac{2}{9} \cdot \frac{3}{4}$  \_\_\_\_\_

2.  $\frac{3}{4} \cdot \frac{4}{5}$  \_\_\_\_\_

5.  $\frac{6}{7} \cdot \frac{1}{2}$  \_\_\_\_\_

8.  $\frac{19}{20}y \cdot \frac{5}{6}x$  \_\_\_\_\_

3.  $\frac{3}{8} \cdot \frac{2}{3}$  \_\_\_\_\_

6.  $\frac{3}{7} \cdot \frac{7}{12}$  \_\_\_\_\_

9.  $\frac{4}{5} \cdot \frac{5}{8}y$  \_\_\_\_\_

**Directions** Multiply. Write your answer in simplest form.

10.  $2\frac{3}{8} \cdot 1\frac{5}{19}$  \_\_\_\_\_

13.  $4\frac{1}{2} \cdot 2\frac{1}{9}$  \_\_\_\_\_

16.  $2\frac{5}{6} \cdot 3\frac{4}{17}a$  \_\_\_\_\_

11.  $1\frac{3}{4} \cdot 1\frac{6}{7}$  \_\_\_\_\_

14.  $5\frac{1}{3} \cdot 2\frac{2}{5}$  \_\_\_\_\_

17.  $4\frac{4}{5}y \cdot 2\frac{7}{12}$  \_\_\_\_\_

12.  $3\frac{1}{5} \cdot 1\frac{3}{16}$  \_\_\_\_\_

15.  $3\frac{3}{4} \cdot 1\frac{3}{10}$  \_\_\_\_\_

18.  $1\frac{2}{3}x \cdot 2\frac{7}{8}$  \_\_\_\_\_

**Directions** Multiply to solve each problem. Write your answer in simplest form.

19. Four-fifths of Mrs. Martinez's class likes the color purple, while  $\frac{7}{8}$  of Mr. Burns's class likes the color. What fraction of both classes like purple?

\_\_\_\_\_

20. Bobbie made a cake, which needed  $4\frac{1}{3}$  cups of flour. Each cup weighs  $8\frac{3}{4}$  ounces. How many ounces of flour did she use?

\_\_\_\_\_

## Dividing Fractions and Mixed Numbers

**EXAMPLE**Divide  $1\frac{1}{3} \div 2\frac{1}{3}$ .**Step 1** Change each mixed number into an improper fraction.

$$1\frac{1}{3} = \frac{4}{3} \qquad 2\frac{1}{3} = \frac{7}{3}$$

**Step 2** Multiply the dividend by the reciprocal of the divisor.

$$\frac{4}{3} \div \frac{7}{3} \text{ becomes } \frac{4}{3} \cdot \frac{3}{7}.$$

$$\frac{4}{3} \cdot \frac{3}{7} = \frac{12}{21}$$

**Step 3** If possible, simplify.  $\frac{12}{21} = \frac{4}{7}$ **Directions** Divide. Write your answer in simplest form.

1.  $\frac{5}{8} \div \frac{5}{6}$  \_\_\_\_\_

4.  $\frac{3}{8} \div \frac{3}{5}$  \_\_\_\_\_

7.  $\frac{1}{3} \div \frac{3}{7}$  \_\_\_\_\_

2.  $\frac{1}{5} \div \frac{3}{4}$  \_\_\_\_\_

5.  $\frac{7}{8} \div \frac{1}{2}$  \_\_\_\_\_

8.  $\frac{6}{11n} \div \frac{4}{11}$  \_\_\_\_\_

3.  $\frac{7}{10} \div \frac{14}{15}$  \_\_\_\_\_

6.  $\frac{9}{10} \div \frac{3}{8}$  \_\_\_\_\_

9.  $\frac{15}{16} \div \frac{5}{8y}$  \_\_\_\_\_

**Directions** Divide. Write your answer in simplest form.

10.  $2\frac{2}{5} \div 1\frac{3}{5}$  \_\_\_\_\_

13.  $3\frac{1}{3} \div 1\frac{1}{3}$  \_\_\_\_\_

16.  $2\frac{2}{3} \div 5\frac{1}{3}$  \_\_\_\_\_

11.  $6\frac{5}{8} \div 2\frac{1}{2}$  \_\_\_\_\_

14.  $1\frac{3}{4} \div 2\frac{1}{2}$  \_\_\_\_\_

17.  $1\frac{2}{7} \div 3\frac{6}{7}j$  \_\_\_\_\_

12.  $1\frac{2}{3} \div 1\frac{1}{4}$  \_\_\_\_\_

15.  $4\frac{3}{8} \div 3\frac{1}{2}$  \_\_\_\_\_

18.  $5\frac{3}{8}w \div 1\frac{19}{24}$  \_\_\_\_\_

**Directions** Solve each problem. If necessary, reduce to simplest form.

19. Kelvin has a log that is  $15\frac{1}{3}$  feet long. He must cut it into pieces that each measure  $\frac{1}{2}$  foot. How many pieces can he cut?

\_\_\_\_\_

20. Melissa walked  $12\frac{2}{3}$  miles in  $2\frac{2}{3}$  hours. How many miles per hour did she walk?

\_\_\_\_\_

# Using Fractions

**Directions** Complete the chart.

1. Sara surveyed 30 of her classmates for a civics project. In the group,  $\frac{1}{2}$  said they watched TV for 2 hours every day.  $\frac{1}{3}$  said they watched for 1 hour.  $\frac{1}{15}$  said they watched for less than  $\frac{1}{2}$  hour each day. The rest of the group said they did not watch television on a daily basis.

30 Classmates	How Many?
$\frac{1}{2}$ watch television 2 hours	_____
$\frac{1}{3}$ watch television 1 hour	_____
$\frac{1}{15}$ watch television $<\frac{1}{2}$ hour	_____
_____ do not watch daily	_____

**Directions** Solve each problem.

2. Mike can walk a mile in  $\frac{2}{3}$  of an hour. Dennis can walk a mile in  $\frac{5}{8}$  of an hour. Who walks a mile faster? \_\_\_\_\_
3. On Wednesday, Elaine told Sam she finished  $\frac{7}{8}$  of her science project. Sam said he finished  $\frac{15}{16}$ . Who has finished more of the project? \_\_\_\_\_
4. Kendra lives  $\frac{6}{7}$  of a mile from the mall. Ali lives  $\frac{5}{9}$  of a mile from the mall. Who lives closer to the mall? \_\_\_\_\_
5. To go to the video store, Jennifer walks  $2\frac{5}{8}$  blocks north and  $4\frac{1}{2}$  blocks east. How many blocks does she walk to the video store? \_\_\_\_\_
6. To build a birdhouse, Pat needs  $16\frac{5}{8}$  inches of pine and  $9\frac{2}{3}$  inches of cedar. How many more inches of pine does she need? \_\_\_\_\_
7. Darlene walked for  $2\frac{3}{8}$  hours at  $3\frac{2}{3}$  miles per hour. How many miles did she walk? \_\_\_\_\_
8. Grass seed costs \$3.50 ( $3\frac{1}{2}$ ) a pound. Frank needs  $2\frac{1}{2}$  pounds of grass seed. How much will the grass seed cost? \_\_\_\_\_
9. Jack and Bill disagreed over their homework. Jack said  $10\frac{1}{3} \cdot 4\frac{7}{8} = 50\frac{3}{8}$ . Is he correct? \_\_\_\_\_
10. At lunch, Ti's restaurant sells 150 sandwiches.  $\frac{3}{5}$  of the sandwiches are beef,  $\frac{3}{10}$  are chicken, and  $\frac{1}{25}$  are cheese. The rest of the sandwiches are ham. How many ham sandwiches are sold? \_\_\_\_\_



# The Order of Operations

**EXAMPLE**

$$5(3 + 2) - 8 \div 4$$

**Step 1** Do the operation inside the parentheses.

$$5(5) - 8 \div 4$$

**Step 2** Multiply and divide from left to right.

$$25 - 2$$

**Step 3** Subtract.

$$25 - 2 = 23$$

**Directions** Simplify each expression using the order of operations.

- |                                      |  |
|--------------------------------------|--|
| 1. $16 - 5 \cdot 3$ _____            | 11. $9(1 + 4) - 3 \cdot 8$ _____       |
| 2. $9 + 11 \cdot 2$ _____            | 12. $35 \div (5 \cdot 7) + 1$ _____    |
| 3. $4(6 - 3)$ _____                  | 13. $25(8 \div 2) - 10(22 - 19)$ _____ |
| 4. $8(42 \div 7)$ _____              | 14. $15 \div 3 \div 5 + 6$ _____       |
| 5. $3 + 5(20 - 18)$ _____            | 15. $8 + 28 \div 7$ _____              |
| 6. $(4 \cdot 2) \div 2 + 10$ _____   | 16. $9 - 12 \div 4 + 2$ _____          |
| 7. $25 - 4(10 - 4)$ _____            | 17. $6 \cdot 2 + 25 \div 5$ _____      |
| 8. $3 + 4 \cdot 5 - 12 \div 4$ _____ | 18. $8(6 - 3) - 4 \div 2$ _____        |
| 9. $7 \cdot 6 + 20 \div 10$ _____    | 19. $16 \div (2 \cdot 2) - 3$ _____    |
| 10. $20 - 10 \div 2 \cdot 3$ _____   | 20. $20(20 \div 4) + 3 - 2$ _____      |

**Directions** Use a calculator to simplify each expression.

- |  |   |
|--|---|
| 21. $100 - 8 \cdot 7 + 23$ _____               | 26. $42 \div 7 + 6(154 \div 11)$ _____    |
| 22. $7(625 \div 25) - 4 \cdot 5 \cdot 5$ _____ | 27. $97 - 128 \div 4 \cdot 3$ _____       |
| 23. $32 \div 4(62 - 60)$ _____                 | 28. $(18 + 6) \div 4 \cdot 10$ _____      |
| 24. $16 + 5 \cdot 7 - 81 \div 9 + 30$ _____    | 29. $19 - 3 \cdot 2 \cdot 8 \div 6$ _____ |
| 25. $20 + 12(169 \div 13) \div 6$ _____        | 30. $45 + 10(32 - 32) + 40$ _____         |

# Evaluating Algebraic Expressions

**EXAMPLE**

Evaluate  $5y + 2$ , when  $y = 1, 2, 3$ .

When  $y = 1$ :

$$5(1) + 2 =$$

$$5 + 2 = 7$$

When  $y = 2$ :

$$5(2) + 2 =$$

$$10 + 2 = 12$$

When  $y = 3$ :

$$5(3) + 2 =$$

$$15 + 2 = 17$$

**Directions** Evaluate each expression for  $n = 6$ .

1.  $n + 4$  \_\_\_\_\_

2.  $n - 3$  \_\_\_\_\_

3.  $42 - 3n$  \_\_\_\_\_

4.  $5n + 2$  \_\_\_\_\_

5.  $14 + \frac{n}{3}$  \_\_\_\_\_

6.  $\frac{n}{2} - 1$  \_\_\_\_\_

7.  $4n - 13$  \_\_\_\_\_

8.  $2 + \frac{n}{4}$  \_\_\_\_\_

9.  $\frac{5}{2n} + \frac{3}{3n}$  \_\_\_\_\_

10.  $3n - 2n$  \_\_\_\_\_

**Directions** Evaluate each expression for  $y = 7$ .

11.  $y + 3$  \_\_\_\_\_

12.  $2y - 10$  \_\_\_\_\_

13.  $21 - 3y$  \_\_\_\_\_

14.  $6y + 1$  \_\_\_\_\_

15.  $12 + \frac{y}{7}$  \_\_\_\_\_

16.  $\frac{y}{3} - 1$  \_\_\_\_\_

17.  $4y - 16$  \_\_\_\_\_

18.  $6 + \frac{1}{y}$  \_\_\_\_\_

19.  $\frac{2}{3y} + \frac{2y}{3}$  \_\_\_\_\_

20.  $4y + 2y$  \_\_\_\_\_

**Directions** Evaluate each expression for  $z = 10$ .

21.  $4z - 12$  \_\_\_\_\_

22.  $z + 8$  \_\_\_\_\_

23.  $52 - 5z$  \_\_\_\_\_

24.  $3z + 4$  \_\_\_\_\_

25.  $11 + \frac{z}{2}$  \_\_\_\_\_

26.  $\frac{z}{3} - 1$  \_\_\_\_\_

27.  $5z - 3z$  \_\_\_\_\_

28.  $1 + \frac{1}{z}$  \_\_\_\_\_

29.  $3\frac{z}{5} + \frac{5}{z}$  \_\_\_\_\_

30.  $z + 2z$  \_\_\_\_\_

# Equations—Solution by Substitution

**EXAMPLE**

Substitute numbers into  $2x + 3 = 13$  to find the root of the equation.

Substitute 0 for the variable.

$$2(0) + 3 = 13$$

$3 = 13$  is false.

When  $x = 5$ ,  $2x + 3 = 13$  is true.

Therefore,  $x = 5$  is true.

**Directions** Substitute numbers into each equation to find the root of the equation.

1.  $6x + 1 = 19$  \_\_\_\_\_

2.  $12x - 4 = 44$  \_\_\_\_\_

3.  $28 - 2x = 14$  \_\_\_\_\_

4.  $\frac{1}{2}x + 2 = 7$  \_\_\_\_\_

5.  $3 + 4x = 3$  \_\_\_\_\_

6.  $9 \cdot x = 27$  \_\_\_\_\_

7.  $6 + 4x = 26$  \_\_\_\_\_

8.  $15 - 6x = 3$  \_\_\_\_\_

9.  $7x - 14 = 14$  \_\_\_\_\_

10.  $x \cdot 5 = 35$  \_\_\_\_\_

11.  $2 + 3x = 8$  \_\_\_\_\_

12.  $x + x = 10$  \_\_\_\_\_

13.  $4x - 4 = 20$  \_\_\_\_\_

14.  $60 - 2x = 40$  \_\_\_\_\_

15.  $\frac{5}{8}x + \frac{3}{8} = 1$  \_\_\_\_\_

16.  $2x + 13 = 25$  \_\_\_\_\_

17.  $10 - 3x = 1$  \_\_\_\_\_

18.  $23 - 4x = 15$  \_\_\_\_\_

19.  $20x - 15 = 65$  \_\_\_\_\_

20.  $\frac{1}{2}x + 3 = 7$  \_\_\_\_\_

21.  $5 + 3x = 26$  \_\_\_\_\_

22.  $8 \cdot x = 72$  \_\_\_\_\_

23.  $2 + 6x = 62$  \_\_\_\_\_

24.  $x \cdot 4 = 8$  \_\_\_\_\_

25.  $x - 3 = 1$  \_\_\_\_\_

# Solving Addition Equations

**EXAMPLE**Solve  $5 + x = 16$  for  $x$ .**Step 1** Subtract 5 from each side.

$$5 + x - 5 = 16 - 5$$

**Step 2** Perform the operations.

$$x = 11$$

**Step 3** Check by substitution.

$$5 + 11 = 16 \text{ is true.}$$

**Directions** Solve for each variable. Write your answer in simplest form.  
Check each solution.

1.  $a + 11 = 17$  \_\_\_\_\_

2.  $x + 16 = 38$  \_\_\_\_\_

3.  $42 + y = 72$  \_\_\_\_\_

4.  $29 + b = 46$  \_\_\_\_\_

5.  $x + 19 = 37$  \_\_\_\_\_

6.  $n + 16 = 32$  \_\_\_\_\_

7.  $x + 9 = 29$  \_\_\_\_\_

8.  $19 + m = 30$  \_\_\_\_\_

9.  $67 + x = 72$  \_\_\_\_\_

10.  $v + 15 = 28$  \_\_\_\_\_

11.  $c + 7 = 28$  \_\_\_\_\_

12.  $36 + e = 59$  \_\_\_\_\_

13.  $w + \frac{5}{8} = 1$  \_\_\_\_\_

14.  $\frac{1}{2} + b = \frac{11}{16}$  \_\_\_\_\_

15.  $\frac{1}{3} + f = \frac{5}{6}$  \_\_\_\_\_

16.  $x + \frac{3}{4} = \frac{7}{8}$  \_\_\_\_\_

17.  $\frac{4}{5} + t = 1\frac{2}{5}$  \_\_\_\_\_

18.  $c + \frac{1}{5} = \frac{13}{15}$  \_\_\_\_\_

19.  $j + \frac{1}{5} = 1$  \_\_\_\_\_

20.  $\frac{1}{2} = \frac{1}{3} + g$  \_\_\_\_\_

21.  $\frac{7}{8} = \frac{5}{8} + p$  \_\_\_\_\_

22.  $1\frac{3}{8} = y + \frac{5}{8}$  \_\_\_\_\_

23.  $1\frac{2}{15} = \frac{4}{5} + d$  \_\_\_\_\_

24.  $\frac{1}{2} = s + \frac{1}{4}$  \_\_\_\_\_

25.  $\frac{5}{6} = h + \frac{1}{6}$  \_\_\_\_\_

## Solving Subtraction Equations

**EXAMPLE**Solve  $x - \frac{1}{2} = \frac{3}{4}$  for  $x$ .**Step 1** Isolate the variable  $x$  by adding the inverse.

$$x - \frac{1}{2} + \frac{1}{2} = \frac{3}{4} + \frac{1}{2}$$

**Step 2** Perform each operation.

$$x - \frac{1}{2} + \frac{1}{2} = \frac{3}{4} + \frac{2}{4}$$

$$x = \frac{5}{4}$$

**Step 3** Simplify if necessary.

$$x = 1\frac{1}{4}$$

**Directions** Solve for each variable. Write your answer in simplest form.

1.  $x - 13 = 25$  \_\_\_\_\_

2.  $y - 7 = 8$  \_\_\_\_\_

3.  $a - 19 = 23$  \_\_\_\_\_

4.  $d - 9 = 2$  \_\_\_\_\_

5.  $e - 17 = 33$  \_\_\_\_\_

6.  $s - 25 = 42$  \_\_\_\_\_

7.  $t - 18 = 20$  \_\_\_\_\_

8.  $n - 23 = 49$  \_\_\_\_\_

9.  $f - 16 = 39$  \_\_\_\_\_

10.  $g - \frac{1}{4} = \frac{1}{4}$  \_\_\_\_\_

11.  $v - \frac{3}{8} = \frac{1}{4}$  \_\_\_\_\_

12.  $c - \frac{1}{6} = \frac{1}{2}$  \_\_\_\_\_

13.  $z - \frac{3}{16} = \frac{9}{16}$  \_\_\_\_\_

14.  $n - \frac{1}{2} = \frac{3}{8}$  \_\_\_\_\_

15.  $h - \frac{5}{8} = \frac{5}{8}$  \_\_\_\_\_

16.  $x - \frac{1}{2} = \frac{7}{16}$  \_\_\_\_\_

17.  $j - \frac{3}{10} = \frac{3}{5}$  \_\_\_\_\_

18.  $x - \frac{1}{10} = \frac{3}{10}$  \_\_\_\_\_

**Directions** Use addition or subtraction to solve these problems.

19. The United States and Canada produced 16 million ounces of gold. Canada alone produced 5 million ounces of gold. How much gold did the U.S. produce?

\_\_\_\_\_

20. Mexico and Congo produced 578 thousand ounces of gold. Congo produced 257 thousand ounces of gold. How much gold did Mexico produce?

\_\_\_\_\_

# Complex Fractions

**EXAMPLE**

Simplify  $\frac{\frac{2}{3}}{\frac{2}{5}}$ .

**Step 1** Rewrite the complex fraction horizontally  $\frac{\frac{2}{3}}{\frac{2}{5}} = \frac{2}{3} \div \frac{2}{5}$

**Step 2** To divide, multiply the dividend by the reciprocal of the divisor.

$$\frac{2}{3} \div \frac{2}{5} = \frac{2}{3} \cdot \frac{5}{2} = \frac{10}{6} \quad \text{or} \quad \frac{\frac{2}{3} \cdot \frac{5}{2}}{\frac{2}{5} \cdot \frac{5}{2}} = \frac{\frac{2}{3} \cdot \frac{5}{2}}{1} = \frac{2}{3} \cdot \frac{5}{2} = \frac{10}{6}$$

**Step 3** Simplify.

$$\frac{10}{6} = 1\frac{4}{6} = 1\frac{2}{3}$$

**Directions** Simplify each complex fraction.

1.  $\frac{\frac{2}{3}}{\frac{1}{3}}$  \_\_\_\_\_

10.  $\frac{\frac{3}{4}}{6}$  \_\_\_\_\_

19.  $\frac{4}{\frac{2}{3}}$  \_\_\_\_\_

2.  $\frac{\frac{5}{8}}{\frac{3}{4}}$  \_\_\_\_\_

11.  $\frac{7}{\frac{3}{8}}$  \_\_\_\_\_

20.  $\frac{\frac{7}{9}}{3}$  \_\_\_\_\_

3.  $\frac{\frac{1}{5}}{\frac{3}{8}}$  \_\_\_\_\_

12.  $\frac{\frac{5}{9}}{\frac{2}{3}}$  \_\_\_\_\_

21.  $\frac{\frac{1}{4}}{\frac{3}{4}}$  \_\_\_\_\_

4.  $\frac{\frac{15}{16}}{\frac{1}{8}}$  \_\_\_\_\_

13.  $\frac{1}{\frac{3}{10}}$  \_\_\_\_\_

22.  $\frac{16}{\frac{5}{8}}$  \_\_\_\_\_

5.  $\frac{6}{\frac{2}{3}}$  \_\_\_\_\_

14.  $\frac{\frac{3}{5}}{\frac{9}{10}}$  \_\_\_\_\_

23.  $\frac{\frac{4}{5}}{\frac{5}{14}}$  \_\_\_\_\_

6.  $\frac{\frac{4}{5}}{\frac{4}{9}}$  \_\_\_\_\_

15.  $\frac{\frac{1}{2}}{\frac{7}{8}}$  \_\_\_\_\_

24.  $\frac{\frac{1}{2}}{6}$  \_\_\_\_\_

7.  $\frac{\frac{6}{7}}{\frac{5}{7}}$  \_\_\_\_\_

16.  $\frac{\frac{5}{6}}{\frac{2}{3}}$  \_\_\_\_\_

25.  $\frac{5}{\frac{1}{3}}$  \_\_\_\_\_

8.  $\frac{\frac{3}{8}}{\frac{3}{4}}$  \_\_\_\_\_

17.  $\frac{8}{\frac{4}{11}}$  \_\_\_\_\_

9.  $\frac{\frac{7}{9}}{\frac{7}{8}}$  \_\_\_\_\_

18.  $\frac{\frac{2}{5}}{\frac{7}{10}}$  \_\_\_\_\_

## Simplifying by Addition

**EXAMPLE**Simplify  $\frac{3x}{8} + \frac{5x}{12}$ .**Step 1** Find the LCM of the denominators.

$$\text{LCM} = 24$$

**Step 2** Write equivalent fractions.

$$\frac{3x \cdot 3}{8 \cdot 3} + \frac{5x \cdot 2}{12 \cdot 2} = \frac{9x}{24} + \frac{10x}{24}$$

**Step 3** Add the equivalent fractions.

$$\frac{9x}{24} + \frac{10x}{24} = \frac{19x}{24}$$

**Step 4** Simplify if possible.  $\frac{19x}{24}$  is in simplest form.**Directions** Simplify. Write your answer in simplest form.

1.  $\frac{1}{5x} + \frac{2}{5x}$  \_\_\_\_\_

6.  $\frac{3}{8j} + \frac{2}{8j}$  \_\_\_\_\_

11.  $\frac{4g}{5} + \frac{1g}{5}$  \_\_\_\_\_

2.  $\frac{2c}{4} + \frac{1c}{4}$  \_\_\_\_\_

7.  $\frac{3w}{10} + \frac{2w}{10}$  \_\_\_\_\_

12.  $\frac{1}{4b} + \frac{1}{4b}$  \_\_\_\_\_

3.  $\frac{5}{8y} + \frac{2}{8y}$  \_\_\_\_\_

8.  $\frac{3}{4x} + \frac{3}{4x}$  \_\_\_\_\_

13.  $\frac{3}{10q} + \frac{9}{10q}$  \_\_\_\_\_

4.  $\frac{4b}{7} + \frac{6b}{7}$  \_\_\_\_\_

9.  $\frac{13d}{16} + \frac{3d}{16}$  \_\_\_\_\_

14.  $\frac{5x}{8} + \frac{7x}{8}$  \_\_\_\_\_

5.  $\frac{3z}{5} + \frac{4z}{5}$  \_\_\_\_\_

10.  $\frac{5}{9y} + \frac{2}{9y}$  \_\_\_\_\_

15.  $\frac{2}{11p} + \frac{5}{11p}$  \_\_\_\_\_

**Directions** Simplify by collecting like terms. Write your answer in simplest form.

16.  $\frac{2}{5c} + \frac{1}{3c}$  \_\_\_\_\_

20.  $\frac{3}{5r} + \frac{1}{6r}$  \_\_\_\_\_

24.  $\frac{2n}{9} + \frac{1n}{3}$  \_\_\_\_\_

17.  $\frac{5b}{8} + \frac{3b}{16}$  \_\_\_\_\_

21.  $\frac{2e}{7} + \frac{5e}{14}$  \_\_\_\_\_

25.  $\frac{1}{5v} + \frac{3}{4v}$  \_\_\_\_\_

18.  $\frac{1y}{4} + \frac{2y}{3}$  \_\_\_\_\_

22.  $\frac{5}{12k} + \frac{3}{4k}$  \_\_\_\_\_

19.  $\frac{2}{3j} + \frac{11}{12j}$  \_\_\_\_\_

23.  $\frac{7}{9m} + \frac{2}{3m}$  \_\_\_\_\_

## Simplifying by Subtraction

**EXAMPLE**Simplify  $\frac{b}{2} - \frac{b}{5}$ .**Step 1** Find the LCM of the denominators. LCM = 10**Step 2** Write equivalent fractions.  $\frac{b \cdot 5}{2 \cdot 5} - \frac{b \cdot 2}{5 \cdot 2} = \frac{5b}{10} - \frac{2b}{10}$ **Step 3** Subtract the equivalent fractions.  $\frac{5b}{10} - \frac{2b}{10} = \frac{3b}{10}$ **Step 4** Simplify if possible.  $\frac{3b}{10}$  is in simplest form.**Directions** Simplify. Write your answer in simplest form.

1.  $\frac{5c}{8} - \frac{3c}{8}$  \_\_\_\_\_

4.  $\frac{15}{16e} - \frac{7}{16e}$  \_\_\_\_\_

7.  $\frac{5}{6s} - \frac{1}{6s}$  \_\_\_\_\_

2.  $\frac{3}{4d} - \frac{1}{4d}$  \_\_\_\_\_

5.  $\frac{11}{14h} - \frac{5}{14h}$  \_\_\_\_\_

8.  $\frac{7b}{9} - \frac{4b}{9}$  \_\_\_\_\_

3.  $\frac{3w}{5} - \frac{2w}{5}$  \_\_\_\_\_

6.  $\frac{9g}{10} - \frac{3g}{10}$  \_\_\_\_\_

9.  $\frac{2}{3q} - \frac{1}{3q}$  \_\_\_\_\_

**Directions** Simplify by collecting like terms. Write your answer in simplest form.

10.  $\frac{9}{10a} - \frac{1}{2a}$  \_\_\_\_\_

13.  $\frac{2}{3r} - \frac{5}{8r}$  \_\_\_\_\_

16.  $\frac{5}{9k} - \frac{1}{3k}$  \_\_\_\_\_

11.  $\frac{8c}{9} - \frac{2c}{3}$  \_\_\_\_\_

14.  $\frac{4x}{5} - \frac{5x}{8}$  \_\_\_\_\_

17.  $\frac{11y}{16} - \frac{1y}{2}$  \_\_\_\_\_

12.  $\frac{5p}{16} - \frac{1p}{4}$  \_\_\_\_\_

15.  $\frac{3s}{4} - \frac{7s}{16}$  \_\_\_\_\_

**Directions** Solve these problems.

18. Ed spends
- $\frac{3}{8}$
- of his study time on history. How much of his study time does he have left?
- 
- \_\_\_\_\_

20. Jenny's survey showed that
- $\frac{11}{16}$
- of her class picked blue as their favorite color. What part of her class picked a different color?
- 
- \_\_\_\_\_

19. Juan has
- $\frac{7}{8}$
- yards of string. He used
- $\frac{2}{3}$
- yards of string. How much does he have left?
- 
- \_\_\_\_\_



# Multiplying Rational Expressions

**EXAMPLE**

Multiply  $\frac{5}{8} \cdot \frac{2}{5}$ .

**Step 1** Multiply the numerators and the denominators.

$$\frac{5}{8} \cdot \frac{2}{5} = \frac{5 \cdot 2}{8 \cdot 5} = \frac{10}{40}$$

**Step 2** If possible, simplify the fraction.

$$\frac{10}{40} = \frac{1}{4}$$

**Directions** Multiply. Write your answer in simplest form.

1.  $\frac{3}{4} \cdot \frac{4}{5}$  \_\_\_\_\_

9.  $\frac{5}{12} \cdot \frac{24}{25}$  \_\_\_\_\_

17.  $\frac{7}{15m} \cdot \frac{5}{7}$  \_\_\_\_\_

2.  $\frac{5}{8} \cdot \frac{8}{9}$  \_\_\_\_\_

10.  $\frac{1}{9} \cdot \frac{2}{3}$  \_\_\_\_\_

18.  $\frac{9}{10n} \cdot \frac{2n}{3}$  \_\_\_\_\_

3.  $\frac{14}{15} \cdot \frac{5}{7}$  \_\_\_\_\_

11.  $\frac{5}{16} \cdot \frac{8}{9}$  \_\_\_\_\_

19.  $\frac{9x}{13} \cdot \frac{13}{27}$  \_\_\_\_\_

4.  $\frac{9}{10} \cdot \frac{5}{6}$  \_\_\_\_\_

12.  $\frac{1}{2s} \cdot \frac{1}{6}$  \_\_\_\_\_

20.  $\frac{5}{6a} \cdot \frac{1a}{2}$  \_\_\_\_\_

5.  $\frac{6}{7} \cdot \frac{14}{15}$  \_\_\_\_\_

13.  $\frac{4v}{7} \cdot \frac{7}{16v}$  \_\_\_\_\_

21.  $\frac{4b}{15} \cdot \frac{5}{6}$  \_\_\_\_\_

6.  $\frac{1}{5} \cdot \frac{8}{9}$  \_\_\_\_\_

14.  $\frac{7}{8} \cdot \frac{16g}{17}$  \_\_\_\_\_

22.  $\frac{8v}{9} \cdot \frac{1}{2v}$  \_\_\_\_\_

7.  $\frac{2}{3} \cdot \frac{3}{4}$  \_\_\_\_\_

15.  $\frac{3}{8c} \cdot \frac{7c}{21}$  \_\_\_\_\_

8.  $\frac{8}{11} \cdot \frac{11}{12}$  \_\_\_\_\_

16.  $\frac{4}{5} \cdot \frac{10}{11d}$  \_\_\_\_\_

**Directions** Solve each problem. Write your answer in simplest form.

23. Glenn has  $\frac{2}{5}$  of a granola bar. If he eats  $\frac{7}{8}$  of it, how much of the granola bar is left?

\_\_\_\_\_

24. Amanda pours  $\frac{2}{9}$  of a bag of pretzels into a dish. She eats  $\frac{1}{2}$  of the pretzels in the dish. How much of the bag did she eat?

\_\_\_\_\_

25. The Jordan River is  $\frac{1}{3}$  the length of the Tisza River. The Tisza River is 600 miles long. How long is the Jordan River?

\_\_\_\_\_

# Ratios

**EXAMPLE**

A ratio is a comparison of two quantities using fractions.

Here are some ways to write a ratio:  $\frac{3}{8}$     3 to 8    3:8

Express a ratio in simplest form.

$$\frac{10}{24} = \frac{10 \div 2}{24 \div 2} = \frac{5}{12} \quad 5 \text{ to } 12 \quad \text{or} \quad 5:12$$

**Directions** Complete the chart to show how to write each ratio two other ways.

1. $\frac{8}{13}$		
2.	4 to 11	
3.		5:17
4.	16 to 9	
5. $\frac{12}{7}$		
6.		21:14
7. $\frac{11}{15}$		
8.	27 to 41	
9.		37:19
10.	53 to 61	

**Directions** Write *OK* if each ratio is a fraction expressed in its simplest form. If the fraction is *not* expressed in its simplest form, write the simplest form.

11.  $\frac{5}{15}$  \_\_\_\_\_

16.  $\frac{14}{56}$  \_\_\_\_\_

12.  $\frac{2}{5}$  \_\_\_\_\_

17.  $\frac{32}{57}$  \_\_\_\_\_

13.  $\frac{6}{8}$  \_\_\_\_\_

18.  $\frac{9}{24}$  \_\_\_\_\_

14.  $\frac{3}{24}$  \_\_\_\_\_

19.  $\frac{7}{15}$  \_\_\_\_\_

15.  $\frac{17}{25}$  \_\_\_\_\_

20.  $\frac{32}{9}$  \_\_\_\_\_

# Proportions

**EXAMPLE**

A proportion is an equation made up of two equal ratios:  $\frac{a}{b} = \frac{c}{d}$

A proportion is a true proportion if this equation is true:  $ad = bc$ .

The terms  $ad$  and  $bc$  are called cross products and can be used to solve for a missing variable.

$$\frac{16}{24} = \frac{2}{n} \quad (16)(n) = (24)(2) \quad 16(n) = 48 \quad n = 3$$

**Directions** Write *yes* or *no* to show whether each proportion is a true proportion.

1.  $\frac{6}{13} = \frac{18}{39}$  \_\_\_\_\_ 3.  $\frac{9}{12} = \frac{3}{5}$  \_\_\_\_\_ 5.  $\frac{10}{16} = \frac{5}{8}$  \_\_\_\_\_

2.  $\frac{2}{7} = \frac{4}{13}$  \_\_\_\_\_ 4.  $\frac{4}{16} = \frac{1}{4}$  \_\_\_\_\_ 6.  $\frac{5}{8} = \frac{40}{64}$  \_\_\_\_\_

**Directions** Write the proportions as an equation of cross products.

7.  $\frac{2}{3} = \frac{6}{x}$  \_\_\_\_\_ 10.  $\frac{x}{12} = \frac{30}{72}$  \_\_\_\_\_

8.  $\frac{1}{9} = \frac{b}{81}$  \_\_\_\_\_ 11.  $\frac{42}{48} = \frac{t}{8}$  \_\_\_\_\_

9.  $\frac{6}{c} = \frac{36}{42}$  \_\_\_\_\_ 12.  $\frac{3}{8} = \frac{30}{w}$  \_\_\_\_\_

**Directions** Solve for the variable in each proportion.

13.  $\frac{2}{5} = \frac{x}{20}$  \_\_\_\_\_

17.  $\frac{4}{15} = \frac{d}{75}$  \_\_\_\_\_

14.  $\frac{3}{8} = \frac{c}{24}$  \_\_\_\_\_

18.  $\frac{3}{4} = \frac{6}{y}$  \_\_\_\_\_

15.  $\frac{5}{w} = \frac{1}{5}$  \_\_\_\_\_

19.  $\frac{3}{1} = \frac{x}{4}$  \_\_\_\_\_

16.  $\frac{6}{9} = \frac{12}{a}$  \_\_\_\_\_

20.  $\frac{c}{3} = \frac{28}{21}$  \_\_\_\_\_

# Ratios and Proportions

**EXAMPLE**

A table can be helpful in solving proportion problems.

A record store sold 1 tape for every 5 CDs. If 60 CDs were sold, how many tapes were sold?

<b>Number of Tapes</b>	1	$x$
<b>Number of CDs</b>	5	60

Write an equation and solve it.

$$\frac{1}{5} = \frac{x}{60} \quad (1)(60) = (5)(x) \quad 60 = 5x \quad x = 12$$

**Directions** Fill in each chart. Solve the problem.

1. Three cans of peas cost \$1.80. How much do 9 cans cost? \_\_\_\_\_

<b>Number of Cans</b>		
<b>Cost</b>		

2. A soccer player averaged 1 goal for every 18 tries. If the player made 6 goals, how many tries were made? \_\_\_\_\_

<b>Goals</b>		
<b>Tries</b>		

3. A bag of pecans has 2 broken pecans for each 84 nuts. How many broken pecans were found in a sack of 504 nuts? \_\_\_\_\_

<b>Number of Broken Pecans</b>		
<b>Total Nuts</b>		

4. In a class, two out of every nine students were left-handed. How many left-handers would be found in a group of 63 students? \_\_\_\_\_

<b>Left-handers</b>		
<b>Total Students</b>		

5. If 20 pounds of bird seed cost \$4.40, how much would 3 pounds cost? \_\_\_\_\_

<b>Number of Pounds</b>		
<b>Cost</b>		

# Percents and Fractions

**EXAMPLE**

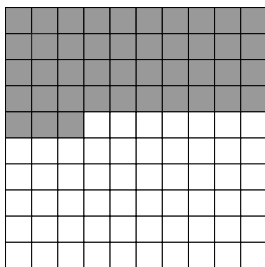
A percent is a ratio based on the number 100.

29 percent means 29 parts of a 100.

It can be written  $\frac{29}{100}$  or 29%.

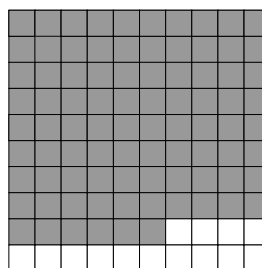
**Directions** Write a fraction to show the percent of each shaded square.

1.



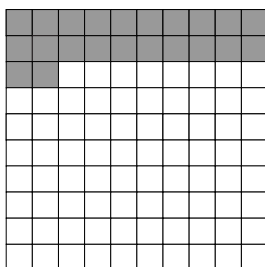
\_\_\_\_\_

2.



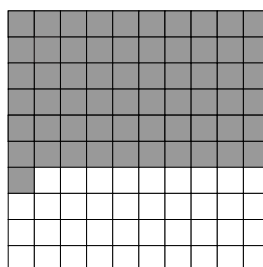
\_\_\_\_\_

3.



\_\_\_\_\_

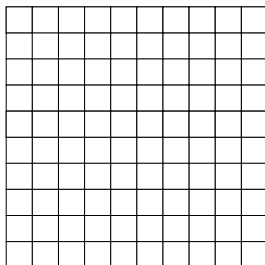
4.



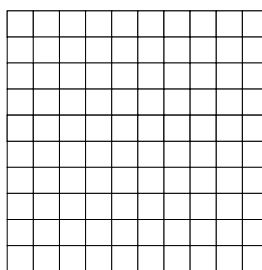
\_\_\_\_\_

**Directions** Shade in the following percents.

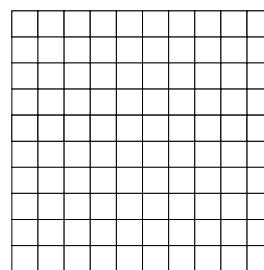
5. 8%



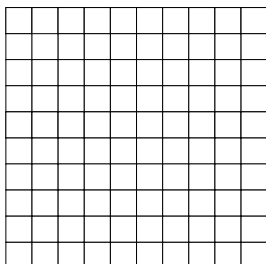
6. 25%



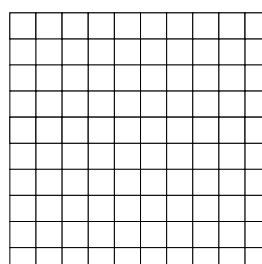
7. 87%



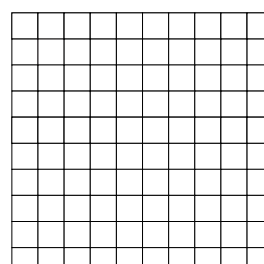
8. 43%



9. 92%



10. 12%



# Percents and Decimals

**EXAMPLE**

Change a decimal to a percent.      0.35 to 35%      0.07 to 7%

Change a percent to a decimal.      46% to  $\frac{46}{100}$  to 0.46

Change a fraction to a percent.       $\frac{46}{100}$  to 46%

Change a fraction with a denominator that is not 100.

$$\frac{3}{4} \text{ to } 3 \div 4 \text{ to } 0.75 \text{ to } 75\%$$

**Directions** Complete the chart by filling in the missing numbers.

Decimal	Percent	Fraction
1.	63%	
2.		$\frac{2}{5}$
3. 0.10		
4.	25%	
5.		$\frac{51}{100}$
6. 0.41		
7.	55%	
8. 0.67		
9.		$\frac{9}{25}$
10.		$\frac{17}{20}$
11. 0.50		
12.	93%	
13.		$\frac{21}{50}$
14.		$\frac{7}{20}$
15.	88%	

## More Percents and Decimals

**Directions** Change each fraction to a percent.

1.  $\frac{1}{10}$  \_\_\_\_\_

2.  $\frac{4}{5}$  \_\_\_\_\_

3.  $\frac{1}{2}$  \_\_\_\_\_

4.  $\frac{7}{8}$  \_\_\_\_\_

5.  $\frac{1}{5}$  \_\_\_\_\_

6.  $\frac{3}{5}$  \_\_\_\_\_

7.  $\frac{1}{4}$  \_\_\_\_\_

8.  $\frac{17}{25}$  \_\_\_\_\_

9.  $\frac{3}{8}$  \_\_\_\_\_

10.  $\frac{7}{16}$  \_\_\_\_\_

**Directions** Change each percent above to a decimal.

11. \_\_\_\_\_

12. \_\_\_\_\_

13. \_\_\_\_\_

14. \_\_\_\_\_

15. \_\_\_\_\_

16. \_\_\_\_\_

17. \_\_\_\_\_

18. \_\_\_\_\_

19. \_\_\_\_\_

20. \_\_\_\_\_

**Directions** Read each problem and write a percent *and* a decimal for the fraction used in the problem. Then solve the problem.

21. One-third of a school's students went to the football game. There are 270 students in the school. How many students attended the game? \_\_\_\_\_

22. Two-fifths of a school's 640 students eat a school lunch each day. How many students eat school lunches each day? \_\_\_\_\_

23. Of the 200 trees in the park, five-eighths are by the lake. How many trees are by the lake? \_\_\_\_\_

24. Three-tenths of the birds in the zoo live in the rainforest. The zoo has 470 birds. How many of the zoo's birds live in the rainforest? \_\_\_\_\_

25. Nine hundred people visit the elephants every day. That is three-fourths of the visitors to the zoo. How many people visit the zoo each day? \_\_\_\_\_

## Finding the Percent of a Number

**EXAMPLE**

Here are some ways to find the percent of a number:

20% of 400

Use a proportion.  $\frac{20}{100} = \frac{x}{400}$  to  $(20)(400) = (100)(x)$  to  $8,000 = 100x$  to  $x = 80$

Use the 1% solution.  $100\% = 400$  to  $\frac{100\%}{100} = \frac{400}{100}$

1% of 400 is 4.

$1\% \cdot 20 = 4 \cdot 20$  20% = 80

Use an equation.  $(20\%)(400) = (.20)(400) = 80$

**Directions** Find the percent. Fill in the missing number to complete each equation. Then solve it.

1. 75% of 16       $(75\%)(\quad) = (\quad)(16) =$  \_\_\_\_\_

2. 30% of 30       $(\quad)(30) = (0.30)(\quad) =$  \_\_\_\_\_

3. 26% of 55       $(26\%)(\quad) = (\quad)(55) =$  \_\_\_\_\_

4. 93% of 70       $(\quad)(70) = (0.93)(\quad) =$  \_\_\_\_\_

5. 77% of 42       $(77\%)(\quad) = (\quad)(42) =$  \_\_\_\_\_

**Directions** Find the percent of each number.

6. 20% of 40      \_\_\_\_\_

11. 12% of 53      \_\_\_\_\_

7. 25% of 120      \_\_\_\_\_

12. 78% of 36      \_\_\_\_\_

8. 35% of 70      \_\_\_\_\_

13. 90% of 56      \_\_\_\_\_

9. 60% of 80      \_\_\_\_\_

14. 80% of 223      \_\_\_\_\_

10. 81% of 25      \_\_\_\_\_

15. 45% of 390      \_\_\_\_\_



## Finding the Percent

**EXAMPLE**

What percent of 800 is 200?

Here are some ways to find out.

Use a ratio.  $\frac{200}{800} = \frac{x}{100}$  to  $(200)(100) = (800)(x)$  to  $20,000 = 800x$  to  $x = 25\%$

Use the 1% solution.  $100\% = 800$  to  $\frac{100\%}{100} = \frac{800}{100}$

$1\% = 8$   $\frac{200}{8} = 25\%$

Use an equation.  $(x)(800) = 200$  to  $800x = 200$  to  $x = \frac{2}{8} = \frac{1}{4} = 25\%$

**Directions** Find the missing percent.

1. 15 is \_\_\_\_\_% of 20.

4. 300 is \_\_\_\_\_% of 120.

2. 64 is \_\_\_\_\_% of 320.

5. 44 is \_\_\_\_\_% of 11.

3. 48 is \_\_\_\_\_% of 96.

6. 900 is \_\_\_\_\_% of 45.

**Directions** Find the given percentage of each number.

18% of

26% of

73% of

21    7. \_\_\_\_\_

8. \_\_\_\_\_

9. \_\_\_\_\_

73    10. \_\_\_\_\_

11. \_\_\_\_\_

12. \_\_\_\_\_

65    13. \_\_\_\_\_

14. \_\_\_\_\_

15. \_\_\_\_\_

56    16. \_\_\_\_\_

17. \_\_\_\_\_

18. \_\_\_\_\_

82    19. \_\_\_\_\_

20. \_\_\_\_\_

21. \_\_\_\_\_

37    22. \_\_\_\_\_

23. \_\_\_\_\_

24. \_\_\_\_\_

28    25. \_\_\_\_\_

26. \_\_\_\_\_

27. \_\_\_\_\_

45    28. \_\_\_\_\_

29. \_\_\_\_\_

30. \_\_\_\_\_

# Percent of Increase and Decrease

**EXAMPLE**

A plant grew from 6 inches to 24 inches. By what percent did it increase?

To find an increase: Subtract.  $24 - 6 = 18$

Write and solve an equation. 18 inches is what percent of 6 inches?

$$\frac{\text{amount of increase}}{\text{original amount}} = \frac{18}{6} = x \quad x = 3 = 300\%$$

There were 200 towels on a roll. Now there are 184 sheets.  
What was the percent of decrease?

To find the decrease: Subtract.  $200 - 184 = 16$

Write a proportion and solve.

$$\frac{\text{amount of decrease}}{\text{total}} = \frac{x}{100} \quad \frac{16}{200} = \frac{x}{100} \quad (16)(100) = (200)(x) \quad 1,600 = 200x \quad x = 8\%$$

**Directions** Solve each increase or decrease problem.

From	Amount of Increase	Percent of Increase
1. 120 to 200	_____	_____
2. 85 to 105	_____	_____
3. 60 to 72	_____	_____
4. 123 to 265	_____	_____
5. 212 to 316	_____	_____
6. 87 to 93	_____	_____
7. 212 to 444	_____	_____
From	Amount of Decrease	Percent of Decrease
8. 210 to 156	_____	_____
9. 84 to 64	_____	_____
10. 168 to 46	_____	_____
11. 454 to 360	_____	_____
12. 15 to 3	_____	_____
13. 344 to 268	_____	_____
14. 92 to 76	_____	_____
15. 212 to 146	_____	_____

# Formulas and Percents

**EXAMPLE**

The formula for compound interest involves percents.

$$A = P(1 + i)^n$$

$A$  = amount of money

$$A = \$200(1 + 0.04)^2$$

$P$  = principal or original deposit

$$A = \$200(1.04)^2$$

$i$  = interest rate per period (shown as a decimal)

$$A = \$200(1.0816)$$

$n$  = number of compounding periods

$$A = \$216.32$$

**Directions** Write each percentage rate as a decimal.

1.  $3\frac{3}{4}$  \_\_\_\_\_

4.  $1\frac{1}{4}$  \_\_\_\_\_

7.  $5\frac{1}{2}$  \_\_\_\_\_

2.  $4\frac{1}{4}$  \_\_\_\_\_

5.  $3\frac{1}{3}$  \_\_\_\_\_

8.  $4\frac{1}{4}$  \_\_\_\_\_

3.  $2\frac{1}{2}$  \_\_\_\_\_

6.  $2\frac{3}{4}$  \_\_\_\_\_

9.  $8\frac{3}{4}$  \_\_\_\_\_

**Directions** Solve each problem. Round to the fourth digit.

10.  $(1.04)^3$  \_\_\_\_\_

13.  $(1.0375)^2$  \_\_\_\_\_

11.  $(1.034)^2$  \_\_\_\_\_

14.  $(1.0875)^3$  \_\_\_\_\_

12.  $(1.0425)^2$  \_\_\_\_\_

15.  $(1.025)^2$  \_\_\_\_\_

**Directions** Solve each problem.

A bank advertised an interest rate on a savings account of  $3\frac{1}{2}\%$  annually. How much did each person have at the end of two years?

Original Deposit

Amount After Two Years

16. \$250

\_\_\_\_\_

17. \$1,800

\_\_\_\_\_

18. \$735

\_\_\_\_\_

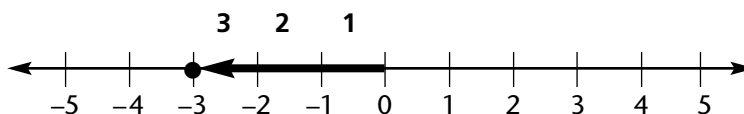
19. \$2,145

\_\_\_\_\_

20. \$8,620

\_\_\_\_\_

# The Real Number Line and Integers

**EXAMPLE** $|-3| = 3$       $-3$  is 3 units from 0.The absolute value of  $|-3|$  is 3.**Directions** Find the absolute value.

- |                 |                  |                  |
|-----------------|------------------|------------------|
| 1. $ -6 $ _____ | 5. $ 11 $ _____  | 9. $ -92 $ _____ |
| 2. $ 4 $ _____  | 6. $ -72 $ _____ | 10. $ 16 $ _____ |
| 3. $ -8 $ _____ | 7. $ -31 $ _____ |                  |
| 4. $ 0 $ _____  | 8. $ 25 $ _____  |                  |

**Directions** Name the opposite of each integer.

- |                 |                 |                 |
|-----------------|-----------------|-----------------|
| 11. $-6$ _____  | 15. $11$ _____  | 19. $-42$ _____ |
| 12. $-9$ _____  | 16. $-52$ _____ | 20. $38$ _____  |
| 13. $15$ _____  | 17. $84$ _____  |                 |
| 14. $-24$ _____ | 18. $-5$ _____  |                 |

**Directions** Write an integer that describes each situation.

21. The Chicago Bulls make a three-point shot in basketball. \_\_\_\_\_
22. The Green Bay Packers lose ten yards in a football game. \_\_\_\_\_
23. The stock of Company XYZ falls eight dollars in value. \_\_\_\_\_
24. School Inc., gains five dollars on the stock market. \_\_\_\_\_
25. Eighty dollars is taken out of a paycheck for taxes. \_\_\_\_\_
26. Pay fifty-five dollars for electric. \_\_\_\_\_
27. Win three hundred dollars in a raffle. \_\_\_\_\_
28. The temperature falls to twenty degrees below zero. \_\_\_\_\_
29. In five minutes, the test begins. \_\_\_\_\_
30. The test began four minutes ago. \_\_\_\_\_

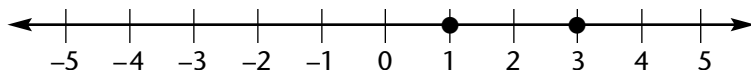
## Comparing Integers—Greater Than

**EXAMPLE**

Compare  $|-3|$  and 1.

$|-3|$  is 3 units from zero, so  $|-3| = 3$ .

1 is 1 unit from zero.



3 is farther to the right than 1, so  $|-3| > 1$ .

**Directions** Compare each pair. Use  $>$  or  $=$ .

1.  $7 \square 6$  \_\_\_\_\_

2.  $11 \square 9$  \_\_\_\_\_

3.  $4 \square 3$  \_\_\_\_\_

4.  $-2 \square -3$  \_\_\_\_\_

5.  $-8 \square -10$  \_\_\_\_\_

6.  $4 \square -5$  \_\_\_\_\_

7.  $3 \square |3|$  \_\_\_\_\_

8.  $7 \square -1$  \_\_\_\_\_

9.  $10 \square 8$  \_\_\_\_\_

10.  $2 \square -3$  \_\_\_\_\_

11.  $-4 \square -5$  \_\_\_\_\_

12.  $|-8| \square 6$  \_\_\_\_\_

13.  $8 \square 6$  \_\_\_\_\_

14.  $-1 \square -5$  \_\_\_\_\_

15.  $3 \square -3$  \_\_\_\_\_

16.  $7 \square |-7|$  \_\_\_\_\_

17.  $-1 \square -4$  \_\_\_\_\_

18.  $2 \square -1$  \_\_\_\_\_

19.  $5 \square 2$  \_\_\_\_\_

20.  $|-6| \square -6$  \_\_\_\_\_

21.  $10 \square -3$  \_\_\_\_\_

22.  $|-6| \square |6|$  \_\_\_\_\_

23.  $8 \square 5$  \_\_\_\_\_

24.  $-8 \square -9$  \_\_\_\_\_

25.  $6 \square |-6|$  \_\_\_\_\_

26.  $-2 \square -2$  \_\_\_\_\_

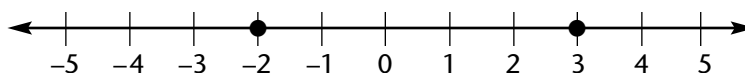
27.  $-3 \square -6$  \_\_\_\_\_

28.  $|-1| \square -3$  \_\_\_\_\_

29.  $|-9| \square 9$  \_\_\_\_\_

30.  $|-10| \square |-9|$  \_\_\_\_\_

# Comparing Integers—Less Than

**EXAMPLE**Compare  $-2$  and  $3$ . $-2$  is to the left of  $3$  on the number line.Therefore,  $-2 < 3$ .**Directions** Compare each pair. Use  $<$  or  $=$ .

- |                            |                              |                             |
|----------------------------|------------------------------|-----------------------------|
| 1. $-5 \square 1$ _____    | 10. $1 \square 8$ _____      | 19. $2 \square 6$ _____     |
| 2. $4 \square 8$ _____     | 11. $5 \square 6$ _____      | 20. $0 \square 4$ _____     |
| 3. $-9 \square  -2 $ _____ | 12. $2 \square 8$ _____      | 21. $-1 \square 10$ _____   |
| 4. $3 \square  -3 $ _____  | 13. $-6 \square 4$ _____     | 22. $-9 \square 3$ _____    |
| 5. $ -8  \square 9$ _____  | 14. $-12 \square  2 $ _____  | 23. $4 \square 6$ _____     |
| 6. $6 \square 6$ _____     | 15. $9 \square 10$ _____     | 24. $ 5  \square  5 $ _____ |
| 7. $-10 \square 3$ _____   | 16. $11 \square 12$ _____    | 25. $ -2  \square 2$ _____  |
| 8. $-2 \square -1$ _____   | 17. $ 8  \square  -9 $ _____ |                             |
| 9. $3 \square 7$ _____     | 18. $6 \square 7$ _____      |                             |

**Directions** Solve these problems.

- |  |  |
|--|--|
| <p>26. Tuesday's temperature was <math>-3^{\circ}\text{F}</math>. On Wednesday the temperature was <math>-7^{\circ}\text{F}</math>. Which day was warmer?</p> <p>_____</p>             | <p>29. On Friday the temperature was <math>32^{\circ}\text{F}</math>. Saturday's temperature was <math>14^{\circ}\text{F}</math>. Which day was colder?</p> <p>_____</p> |
| <p>27. Draw a number line to show that <math> -2 </math> is less than <math> -5 </math>.</p> <p>_____</p>  | <p>30. Jamie claims <math>-6, -2, 0</math>, and <math>5</math> are in order from least to greatest. Is she correct?</p> <p>_____</p>                                     |
| <p>28. Jimmy listed his last five golf scores for the first hole as <math>0, -1, 3, 1</math>, and <math>-2</math>. List these scores in order from least to greatest.</p> <p>_____</p> |  |

## Even and Odd Integers

**EXAMPLE**

Find the product of  $27 \cdot 42$ . Tell whether it is even or odd.

$27 \cdot 42 = 1,134$ . This product is even, because odd  $\cdot$  even = even.

**Directions** Find each sum or difference. Tell whether it is *even* or *odd*.

1.  $614 - 551$  \_\_\_\_\_

2.  $251 - 138$  \_\_\_\_\_

3.  $58 + 56$  \_\_\_\_\_

4.  $678 - 438$  \_\_\_\_\_

5.  $1,235 + 15$  \_\_\_\_\_

6.  $89 + 381$  \_\_\_\_\_

7.  $216 + 429$  \_\_\_\_\_

8.  $368 - 122$  \_\_\_\_\_

9.  $128 + 147$  \_\_\_\_\_

10.  $791 - 543$  \_\_\_\_\_

11.  $360 + 369$  \_\_\_\_\_

12.  $192 + 189$  \_\_\_\_\_

13.  $372 - 276$  \_\_\_\_\_

14.  $2,541 + 591$  \_\_\_\_\_

15.  $168 - 55$  \_\_\_\_\_

**Directions** Find each product. Tell whether it is *even* or *odd*.

16.  $15 \cdot 52$  \_\_\_\_\_

17.  $21 \cdot 23$  \_\_\_\_\_

18.  $52 \cdot 36$  \_\_\_\_\_

19.  $64 \cdot 82$  \_\_\_\_\_

20.  $32 \cdot 48$  \_\_\_\_\_

21.  $9 \cdot 12$  \_\_\_\_\_

22.  $61 \cdot 53$  \_\_\_\_\_

23.  $72 \cdot 24$  \_\_\_\_\_

24.  $84 \cdot 30$  \_\_\_\_\_

25.  $60 \cdot 23$  \_\_\_\_\_

26.  $19 \cdot 17$  \_\_\_\_\_

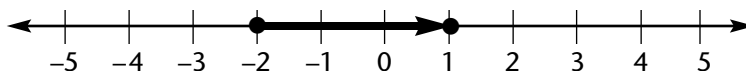
27.  $13 \cdot 64$  \_\_\_\_\_

28.  $25 \cdot 59$  \_\_\_\_\_

29.  $71 \cdot 17$  \_\_\_\_\_

30.  $69 \cdot 24$  \_\_\_\_\_

# Adding Positive Integers

**EXAMPLE**Find the sum of  $-2$  and  $3$ .Begin at  $-2$ . Then move to the right 3 units.  $-2 + 3 = 1$ **Directions** Find each sum.

- |             |       |              |       |
|-------------|-------|--------------|-------|
| 1. $-5 + 5$ | _____ | 11. $-3 + 1$ | _____ |
| 2. $4 + 7$  | _____ | 12. $5 + 6$  | _____ |
| 3. $-2 + 3$ | _____ | 13. $-2 + 8$ | _____ |
| 4. $-9 + 9$ | _____ | 14. $9 + 8$  | _____ |
| 5. $4 + 5$  | _____ | 15. $-5 + 7$ | _____ |
| 6. $3 + 4$  | _____ | 16. $5 + 3$  | _____ |
| 7. $-8 + 2$ | _____ | 17. $7 + 2$  | _____ |
| 8. $1 + 9$  | _____ | 18. $-9 + 7$ | _____ |
| 9. $-6 + 7$ | _____ | 19. $-1 + 8$ | _____ |
| 10. $7 + 8$ | _____ | 20. $9 + 3$  | _____ |

**Directions** Find each sum using a calculator.

- |                  |       |                  |       |
|------------------|-------|------------------|-------|
| 21. $-251 + 787$ | _____ | 26. $-789 + 575$ | _____ |
| 22. $456 + 651$  | _____ | 27. $-123 + 261$ | _____ |
| 23. $-621 + 524$ | _____ | 28. $469 + 431$  | _____ |
| 24. $876 + 957$  | _____ | 29. $-921 + 951$ | _____ |
| 25. $426 + 436$  | _____ | 30. $-435 + 342$ | _____ |

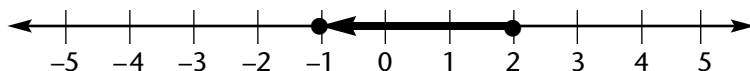


## Adding Negative Integers

**EXAMPLE**Find the sum of  $2 + (-3)$ .

Begin at 2. Then move to the left 3 units.

$2 + (-3) = -1$

**Directions** Find each sum.

- |                      |                       |                        |
|----------------------|-----------------------|------------------------|
| 1. $-5 + (-9)$ _____ | 6. $-2 + (-11)$ _____ | 11. $7 + (-3)$ _____   |
| 2. $10 + (-7)$ _____ | 7. $-3 + (-4)$ _____  | 12. $5 + (-8)$ _____   |
| 3. $9 + (-6)$ _____  | 8. $8 + (-5)$ _____   | 13. $-1 + (-4)$ _____  |
| 4. $-8 + (-3)$ _____ | 9. $-7 + (-7)$ _____  | 14. $-4 + (-12)$ _____ |
| 5. $1 + (-1)$ _____  | 10. $6 + (-2)$ _____  |                        |

**Directions** Find each sum using a calculator.

- |                           |                           |                           |
|---------------------------|---------------------------|---------------------------|
| 15. $-512 + (-613)$ _____ | 20. $712 + (-152)$ _____  | 25. $183 + (-161)$ _____  |
| 16. $452 + (-512)$ _____  | 21. $921 + (-671)$ _____  | 26. $-821 + (-687)$ _____ |
| 17. $329 + (-144)$ _____  | 22. $-159 + (-257)$ _____ | 27. $500 + (-425)$ _____  |
| 18. $-482 + (-169)$ _____ | 23. $-215 + (-812)$ _____ | 28. $-263 + (-691)$ _____ |
| 19. $519 + (-321)$ _____  | 24. $-812 + (-234)$ _____ |                           |

**Directions** Solve each problem by adding integers.

29. The Brazil Basin in the Atlantic Ocean is 20,076 feet deep, which is 2,195 feet deeper than the Eurasia Basin in the Arctic Ocean. How deep is the Eurasia Basin? \_\_\_\_\_

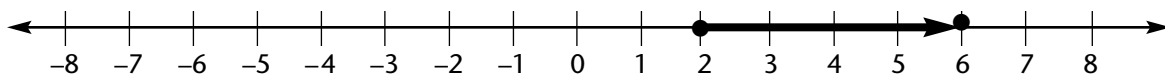
30. The Mariana Trench in the Pacific Ocean is 7,864 feet deeper than the Yap Trench. The Yap Trench is 27,976 feet deep. How deep is the Mariana Trench? \_\_\_\_\_

# Subtracting Positive and Negative Integers

**EXAMPLE**

Find the difference of  $2 - (-4)$ .

Begin at 2. Then move to the right 4 units.  $2 - (-4) = 6$



Notice that  $2 - (-4) = 6$  and  $2 + 4 = 6$ , because subtracting  $-4$  is the same as adding 4.

**Directions** Find the sum of the new expression. (Hint: First rewrite each subtraction expression as an addition expression.)

- |                       |                       |                       |
|-----------------------|-----------------------|-----------------------|
| 1. $-6 - 7$ _____     | 11. $-4 - 8$ _____    | 21. $7 - 8$ _____     |
| 2. $5 - (-8)$ _____   | 12. $3 - 3$ _____     | 22. $-2 - (-4)$ _____ |
| 3. $-8 - 9$ _____     | 13. $-8 - (-8)$ _____ | 23. $4 - 5$ _____     |
| 4. $7 - (-2)$ _____   | 14. $-9 - 5$ _____    | 24. $11 - (-7)$ _____ |
| 5. $-3 - 1$ _____     | 15. $7 - 3$ _____     | 25. $-10 - 5$ _____   |
| 6. $-2 - 9$ _____     | 16. $6 - (-9)$ _____  | 26. $-9 - (-4)$ _____ |
| 7. $1 - (-6)$ _____   | 17. $-10 - 2$ _____   | 27. $5 - 3$ _____     |
| 8. $0 - 4$ _____      | 18. $6 - (-4)$ _____  | 28. $-6 - (-8)$ _____ |
| 9. $-9 - 8$ _____     | 19. $12 - (-8)$ _____ |                       |
| 10. $5 - (-11)$ _____ | 20. $-8 - (-1)$ _____ |                       |

**Directions** Use integers to solve these problems.

29. The Nadelhorn, a mountain in Switzerland, is 14,196 feet.  
The Nadelhorn is 6,124 feet lower than Mt. McKinley in Alaska.  
How tall is Mt. McKinley? \_\_\_\_\_

30. Pikes Peak, Colorado, is 14,110 feet high. Mt. Kilimanjaro, Tanzania,  
is 5,230 feet higher. How tall is Mt. Kilimanjaro? \_\_\_\_\_

## Using Positive and Negative Integers

**Directions** Use the chart to find the difference in height between these points.

1. Mount Kenya and Turfan Depression

\_\_\_\_\_

2. Turfan Depression and Death Valley

\_\_\_\_\_

3. Annapurna I and Danakil Depression

\_\_\_\_\_

4. Mont Blanc and Mount McKinley

\_\_\_\_\_

5. Death Valley and Mont Blanc

\_\_\_\_\_

Highest and Lowest Points in the World	
Annapurna I, Nepal	26,504 ft
Mount McKinley, U.S.	20,320 ft
Mount Kenya, Kenya	17,058 ft
Mont Blanc, France/Italy	15,771 ft
Death Valley, U.S.	-282 ft
Danakil Depression, Ethiopia	-383 ft
Turfan Depression, China	-505 ft
Dead Sea, Israel/Jordan	-1,312 ft

**Directions** Look at the chart. How many degrees separate the record high and low temperatures at these locations?

6. Seville and Roger's Pass

\_\_\_\_\_

7. Ifrane and Northice

\_\_\_\_\_

8. Vostok and El Azizia

\_\_\_\_\_

9. Rivadavia and Death Valley

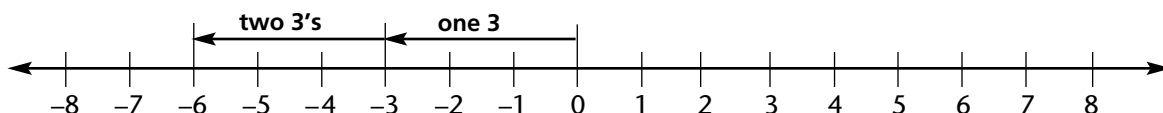
\_\_\_\_\_

10. Ifrane and El Azizia

\_\_\_\_\_

Highest and Lowest Temperatures in the World	
El Azizia, Libya	136°
Death Valley, U.S.	134°
Seville, Spain	122°
Rivadavia, Argentina	120°
Ifrane, Morocco	-11°
Roger's Pass, U.S.	-70°
Northice, Greenland	-87°
Vostok, Antarctica	-129°

# Multiplying by Positive Integers

**EXAMPLE**Find the product  $(-2)(+3)$ .Begin at 0. Then count by 3's to the left. You will reach -6.  $(-2)(+3) = -6$ **Directions** Find each product.

- |                    |                     |                     |
|--------------------|---------------------|---------------------|
| 1. $(-5)(8)$ _____ | 8. $(-4)(8)$ _____  | 15. $(-5)(7)$ _____ |
| 2. $(8)(6)$ _____  | 9. $(6)(8)$ _____   | 16. $(2)(5)$ _____  |
| 3. $(-6)(7)$ _____ | 10. $(-2)(9)$ _____ | 17. $(-3)(7)$ _____ |
| 4. $(3)(2)$ _____  | 11. $(5)(4)$ _____  | 18. $(7)(6)$ _____  |
| 5. $(2)(3)$ _____  | 12. $(-1)(5)$ _____ | 19. $(-4)(9)$ _____ |
| 6. $(-7)(1)$ _____ | 13. $(-9)(2)$ _____ | 20. $(1)(6)$ _____  |
| 7. $(9)(9)$ _____  | 14. $(3)(1)$ _____  |                     |

**Directions** Tell whether each product is *positive* or *negative*.

- |                        |                        |
|------------------------|------------------------|
| 21. $(-334)(89)$ _____ | 26. $(675)(57)$ _____  |
| 22. $(-53)(34)$ _____  | 27. $(-522)(43)$ _____ |
| 23. $(76)(43)$ _____   | 28. $(500)(69)$ _____  |
| 24. $(39)(643)$ _____  | 29. $(-124)(65)$ _____ |
| 25. $(-78)(28)$ _____  | 30. $(43)(56)$ _____   |

# Multiplying by Negative Integers

**EXAMPLE**

Find the product  $(-2)(-4)$ .

The product of  $(-2)(-4)$  is  $+8$ .

When you multiply a negative number and a negative number, the product is positive.

**Directions** Tell whether each product is *positive* or *negative*.

- |                          |                          |
|--------------------------|--------------------------|
| 1. $(-52)(-45)$ _____    | 15. $(-68)(-123)$ _____  |
| 2. $(56)(-432)$ _____    | 16. $(583)(-44)$ _____   |
| 3. $(34)(-33)$ _____     | 17. $(-346)(-721)$ _____ |
| 4. $(-864)(-42)$ _____   | 18. $(57)(-33)$ _____    |
| 5. $(456)(-129)$ _____   | 19. $(-233)(-661)$ _____ |
| 6. $(-843)(-93)$ _____   | 20. $(-672)(-423)$ _____ |
| 7. $(-123)(-96)$ _____   | 21. $(278)(-467)$ _____  |
| 8. $(462)(-34)$ _____    | 22. $(-652)(-597)$ _____ |
| 9. $(532)(-405)$ _____   | 23. $(55)(-622)$ _____   |
| 10. $(-831)(-100)$ _____ | 24. $(-18)(-577)$ _____  |
| 11. $(800)(-52)$ _____   | 25. $(457)(-24)$ _____   |
| 12. $(-23)(-115)$ _____  | 26. $(-33)(-744)$ _____  |
| 13. $(76)(-341)$ _____   | 27. $(934)(-35)$ _____   |
| 14. $(-43)(-733)$ _____  | 28. $(43)(-34)$ _____    |

**Directions** Solve each problem.

29. The temperature fell  $4^{\circ}\text{F}$  each day for six days. What was the total change in temperature? \_\_\_\_\_
30. When initially started, a commercial freezer will cool at a rate of  $-20^{\circ}\text{F}$  an hour. How much colder will the freezer be in two hours? \_\_\_\_\_

## Dividing Positive and Negative Integers

**EXAMPLE**

Find the quotient of  $-36 \div -4$ .

The quotient of  $-36 \div -4$  is 9.

When you divide a negative number by a negative number, the quotient is positive.

**Directions** Find each quotient.

- |                            |                               |                             |
|----------------------------|-------------------------------|-----------------------------|
| 1. $16 \div 4$ _____       | 8. $80 \div (-10)$ _____      | 15. $(-28) \div 7$ _____    |
| 2. $(-25) \div (-5)$ _____ | 9. $(-14) \div 7$ _____       | 16. $15 \div (-5)$ _____    |
| 3. $42 \div (-6)$ _____    | 10. $32 \div 8$ _____         | 17. $63 \div 9$ _____       |
| 4. $(-30) \div 6$ _____    | 11. $(-100) \div (-25)$ _____ | 18. $(-36) \div (-6)$ _____ |
| 5. $81 \div (-9)$ _____    | 12. $51 \div 3$ _____         | 19. $100 \div 10$ _____     |
| 6. $(-20) \div 5$ _____    | 13. $(-24) \div (-6)$ _____   | 20. $(-35) \div (-7)$ _____ |
| 7. $(-18) \div 6$ _____    | 14. $64 \div (-8)$ _____      |                             |

**Directions** Tell whether each quotient is *positive*, *negative*, or *zero*.

- |                              |                                  |
|------------------------------|----------------------------------|
| 21. $453 \div (-84)$ _____   | 26. $5,532 \div 124$ _____       |
| 22. $0 \div 515$ _____       | 27. $(-5,089) \div (-301)$ _____ |
| 23. $1,256 \div (-68)$ _____ | 28. $(-854) \div 52$ _____       |
| 24. $(-541) \div 268$ _____  |                                  |
| 25. $4,587 \div (-67)$ _____ |                                  |

**Directions** Solve each problem.

29. A school has 704 desks. Each classroom has 32 desks.  
How many classrooms are in the school? \_\_\_\_\_
30. The principal of a school bought 1,000 new desks.  
There are 25 desks in each classroom. How many  
classrooms are in the school? \_\_\_\_\_

# Exponents

**EXAMPLE**

You can use the symbol  $5^3$  to show  $5 \cdot 5 \cdot 5$ .

$5^3$  5 is the base. 3 is the exponent.  $5^3$  is read "five to the third power" or "five cubed."

When you write a negative number with an exponent, place the negative number in parentheses, and then write the exponent.

$(-6)^2$   $(-6)$  is the base. 2 is the exponent.  $(-6)^2$  is read "negative six to the second power."

$m^4$   $m$  is the base. 4 is the exponent.  $m^4$  is read " $m$  to the fourth power."

**Directions** Write an expression for each phrase.

- |   |  |
|---|--|
| 1. ten to the second power _____            | 6. two to the seventh power _____        |
| 2. four to the tenth power _____            | 7. $a$ to the fourth power _____         |
| 3. negative six to the third power _____    | 8. negative ten to the fifth power _____ |
| 4. eight to the fourth power _____          | 9. negative $b$ to the tenth power _____ |
| 5. negative three to the second power _____ | 10. nine to the ninth power _____        |

**Directions** Name the exponent in each of the following.

- |                     |                  |                 |
|---------------------|------------------|-----------------|
| 11. $(-10)^8$ _____ | 13. $5^n$ _____  | 15. $7^3$ _____ |
| 12. $2^9$ _____     | 14. $12^1$ _____ |                 |

**Directions** Name the base in each of the following.

- |                     |                       |                    |
|---------------------|-----------------------|--------------------|
| 16. $5^2$ _____     | 18. $2^4$ _____       | 20. $(-n)^4$ _____ |
| 17. $15^{10}$ _____ | 19. $(-5)^{11}$ _____ |                    |

**Directions** Rewrite each of the following using exponents.

- |  |  |
|--|--|
| 21. $(-7) \cdot (-7) \cdot (-7) \cdot (-7) \cdot (-7)$ _____ | 24. $(-c) \cdot (-c) \cdot (-c)$ _____ |
| 22. $4 \cdot 4$ _____  | 25. $12 \cdot 12 \cdot 12$ _____       |
| 23. $8 \cdot 8 \cdot 8 \cdot 8$ _____                        |  |

# Multiplying with Exponents

**EXAMPLE**

If two terms with exponents have the same base, you can multiply the terms by adding exponents.

$$4^2 \cdot 4^3$$

The base of both terms is 4.

$$4^2 \cdot 4^3 = (4 \cdot 4) \cdot (4 \cdot 4 \cdot 4) \\ = 4 \cdot 4 \cdot 4 \cdot 4 \cdot 4$$

$$4^2 \cdot 4^3 = 4^5$$

$$b^2 \cdot b^2$$

The base of both terms is  $b$ .

$$b^2 \cdot b^2 = (b \cdot b) \cdot (b \cdot b) \\ b^2 \cdot b^2 = b^4$$

$$3^n \cdot 3^n$$

The base of both terms is 3.

$$3^n \cdot 3^n = 3^{n+n} \\ 3^n \cdot 3^n = 3^{2n}$$

**Directions** Simplify each expression.

1.  $7^4 \cdot 7^2$  \_\_\_\_\_

2.  $6^2 \cdot 6$  \_\_\_\_\_

3.  $(-m)^2 \cdot (-m)^8$  \_\_\_\_\_

4.  $2^4 \cdot 2^3$  \_\_\_\_\_

5.  $n^3 \cdot n$  \_\_\_\_\_

6.  $14^4 \cdot 14^7$  \_\_\_\_\_

7.  $a^5 \cdot a^2$  \_\_\_\_\_

8.  $(-10)^2 \cdot (-10)^3$  \_\_\_\_\_

9.  $3^{2y} \cdot 3^y$  \_\_\_\_\_

10.  $6^5 \cdot 6^5$  \_\_\_\_\_

11.  $2^3p \cdot 2^3p$  \_\_\_\_\_

12.  $15^5 \cdot 15^6$  \_\_\_\_\_

13.  $3^3 \cdot 3^4$  \_\_\_\_\_

14.  $b^3 \cdot b^3$  \_\_\_\_\_

15.  $(-n)^2 \cdot (-n)^2$  \_\_\_\_\_

**Directions** Tell whether each statement is *true* or *false*. If a statement is false, tell why.

16.  $(-8)^8 \cdot (-8)^8 = (-8)^{16}$  \_\_\_\_\_

17.  $5^3 \cdot 5^4 = 5^{12}$  \_\_\_\_\_

18.  $6^{4n} \cdot 6^{3n} = 6^{7n}$  \_\_\_\_\_

19.  $b^7 \cdot b^2 = b^5$  \_\_\_\_\_

20.  $25^5 \cdot 25 = 25^6$  \_\_\_\_\_

21.  $3^4 \cdot 3^2 = 3^8$  \_\_\_\_\_

22.  $2^6 \cdot 2^6 = 2^{12}$  \_\_\_\_\_

23.  $2^n \cdot 2^{3n} = 2^{4n}$  \_\_\_\_\_

24.  $7^7 \cdot 7^4 = 7^{11}$  \_\_\_\_\_

25.  $b^2 \cdot b^{10} = b^{12}$  \_\_\_\_\_



# Dividing with Exponents

**EXAMPLE**

If two terms with exponents have the same base, you can divide the terms by subtracting exponents.

$$8^6 \div 8^3 = \frac{8^6}{8^3}$$

The base of both terms is 8.

$$= \frac{(8 \cdot 8 \cdot 8 \cdot 8 \cdot 8 \cdot 8)}{(8 \cdot 8 \cdot 8)}$$

$$= (8 \cdot 8 \cdot 8)$$

$$8^6 \div 8^3 = 8^{6-3} = 8^3$$

$$a^4 \div a^2 = \frac{a^4}{a^2}$$

$$= \frac{(a \cdot a \cdot a \cdot a)}{(a \cdot a)}$$

$$a^4 \div a^2 = a^{4-2} = a^2$$

$$6^{2n} \div 6^n = \frac{6^{2n}}{6^n}$$

$$= \frac{(6^n \cdot 6^n)}{(6^n)}$$

$$6^{2n} \div 6^n = 6^{2n-n} = 6^n$$

**Directions** Simplify each expression.

1.  $7^{6n} \div 7^{3n}$  \_\_\_\_\_

2.  $8^8 \div 8^2$  \_\_\_\_\_

3.  $m^4 \div m^4$  \_\_\_\_\_

4.  $22^8 \div 22^4$  \_\_\_\_\_

5.  $k^2 \div k$  \_\_\_\_\_

6.  $10^9 \div 10^7$  \_\_\_\_\_

7.  $(-y)^6 \div (-y)^3$  \_\_\_\_\_

8.  $11^{10} \div 11^{10}$  \_\_\_\_\_

9.  $7^{14} \div 7^7$  \_\_\_\_\_

10.  $10^3 \div 10$  \_\_\_\_\_

11.  $(-6)^{6n} \div (-6)^{2n}$  \_\_\_\_\_

12.  $2^5 \div 2^5$  \_\_\_\_\_

13.  $30^4 \div 30^3$  \_\_\_\_\_

14.  $d^5 \div d^2$  \_\_\_\_\_

15.  $17^8 \div 17^2$  \_\_\_\_\_

**Directions** Tell whether each statement is *true* or *false*. If a statement is false, tell why.

16.  $4^4 \div 4^4 = 4$  \_\_\_\_\_

17.  $12^3 \div 12 = 12^2$  \_\_\_\_\_

18.  $3^{8n} \div 3^{6n} = 3^{2n}$  \_\_\_\_\_

19.  $9^7 \div 9^2 = 9^5$  \_\_\_\_\_

20.  $1^5 \div 1^2 = 1^3$  \_\_\_\_\_

21.  $16^4 \div 16^2 = 16^6$  \_\_\_\_\_

22.  $4^6 \div 4^4 = 4^2$  \_\_\_\_\_

23.  $10^{10} \div 10^3 = 10^7$  \_\_\_\_\_

24.  $(-j)^7 \div (-j)^2 = (-j)^9$  \_\_\_\_\_

25.  $5^{12} \div 5^2 = 5^{10}$  \_\_\_\_\_

# Squares

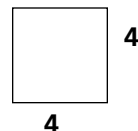
**EXAMPLE**

Write an expression for the area of a square.

Area of a square = length • width =  $4 \cdot 4 = 4^2$

or Area of a square = side squared, or  $s^2 = 4 \cdot 4 = 4^2$

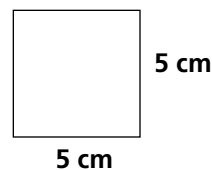
That is why  $4^2$  can be read as "4 squared."



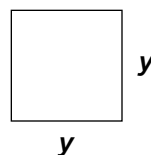
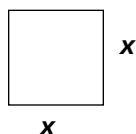
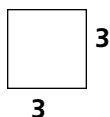
Find the area of a square in square units by multiplying.

Area of a square =  $s^2 = 5^2$

$= 5^2 = 5 \cdot 5 = 25$  sq cm



**Directions** Write an expression for the area of each square.



1. \_\_\_\_\_

2. \_\_\_\_\_

3. \_\_\_\_\_

**Directions** Multiply to find the area of each square. Use the formula Area =  $s^2$ .

4. Square with sides 7 centimeters long \_\_\_\_\_

5. Square with sides 2 centimeters long \_\_\_\_\_

6. Square with sides 6 centimeters long \_\_\_\_\_

**Directions** Write an expression to describe the problem. Then solve the problem.

7. Alicia has a board game that is 18 inches wide and 18 inches long.

What is the area of the board game? \_\_\_\_\_

8. Harris is cultivating a garden that is 20 feet long and 20 feet wide.

What is the area of his garden? \_\_\_\_\_

9. The floor plan for the game room in the new recreation center is 40

feet by 40 feet. What is the floor area in the game room? \_\_\_\_\_

10. Iris bought a new square tablecloth for the kitchen table. The cloth is 5

feet by 5 feet. What is its area? \_\_\_\_\_

# Cubes

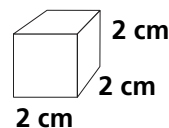
**EXAMPLE**

Write an expression for the volume of a cube.

Volume = length • width • height =  $2 \cdot 2 \cdot 2 = 2^3$

or Volume = side cubed, or  $s^3 = 2 \cdot 2 \cdot 2 = 2^3$

That is why  $2^3$  can be read as “two cubed.”

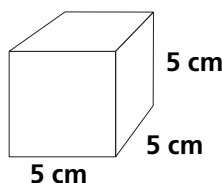


Find the volume of the cube in cubic units by multiplying.

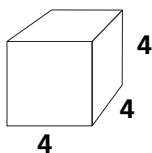
Volume =  $s^3$

Volume =  $5^3$

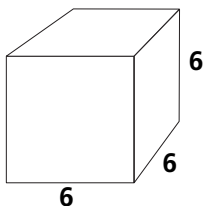
=  $5 \cdot 5 \cdot 5 = 125$  cubic cm



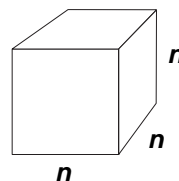
**Directions** Write an expression for the volume of each cube.



1. \_\_\_\_\_



2. \_\_\_\_\_



3. \_\_\_\_\_

**Directions** Multiply to find the volume of each cube. Use the formula Volume =  $s^3$ .

4. Cube with sides 7 centimeters long \_\_\_\_\_

5. Cube with sides 1 centimeter long \_\_\_\_\_

**Directions** Use a calculator to find the volume of each cube. Use the formula Volume =  $s^3$ .

6. Cube with sides 9 centimeters long \_\_\_\_\_

7. Cube with sides 13 centimeters long \_\_\_\_\_

8. Cube with sides 35 centimeters long \_\_\_\_\_

**Directions** Use the formula for volume to solve each problem.

9. Ana Maria keeps her hats and scarves in a decorated box with sides 8 inches long. What is the volume of the box? \_\_\_\_\_

10. Victor's computer monitor came in a packing box with sides 3 feet long. What is the volume of the packing box? \_\_\_\_\_

# Square Roots

**EXAMPLE**

Find the length of the side of a square.

Area = 16	4
	4

Recall that the formula for area is  $A = s^2$ . For this square,  $A = s^2 = 4^2 = 16$ .

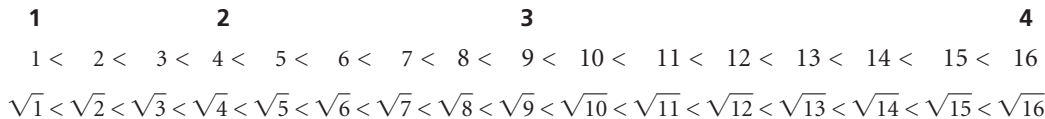
To find the length of a side of the square, you must find the square root.

$$s = \sqrt{A} = \sqrt{16} = 4$$

**EXAMPLE**

Find the square root of 5.

You can use a number line to estimate the square roots of numbers that are not perfect squares.

From the number line, you can see that  $\sqrt{5}$  is between 2 and 3.

$$2 < \sqrt{5} < 3$$

To find the accurate decimal square root, use a calculator.

Round the decimal to the nearest hundredth.  $\sqrt{5} = 2.24$ 

**Directions** Use the number line to make each statement true. Then use a calculator to find a decimal value of each square root. Round the decimal to the nearest hundredth.

1.  $\square < \sqrt{15} < \square$  \_\_\_\_\_

5.  $\square < \sqrt{3} < \square$  \_\_\_\_\_

2.  $\square < \sqrt{12} < \square$  \_\_\_\_\_

6.  $\square < \sqrt{7} < \square$  \_\_\_\_\_

3.  $\square < \sqrt{8} < \square$  \_\_\_\_\_

7.  $\square < \sqrt{14} < \square$  \_\_\_\_\_

4.  $\square < \sqrt{11} < \square$  \_\_\_\_\_

8.  $\square < \sqrt{6} < \square$  \_\_\_\_\_

**Directions** Find the length of a side of the square. You may use your calculator. Round to the nearest hundredth if necessary.

9. 

Area = 25
-----------

 \_\_\_\_\_

10. 

Area = 39
-----------

 \_\_\_\_\_

# Irrational Numbers and Square Roots

## EXAMPLE

The square roots of some numbers are whole numbers. Whole numbers are rational numbers. For example,  $\sqrt{25} = 5$ , which is a whole number and is a rational number.

The square roots of some numbers are not whole numbers. They are irrational numbers. For example,  $\sqrt{3} = 1.73$ , which is not a whole number and is an irrational number.

You can use a graph to find the approximate value of an irrational number.

Find the value of  $\sqrt{50}$  on the graph below.

**Step 1** Estimate the value of  $\sqrt{50}$ . 50 is between the perfect squares 49 and 64, so  $\sqrt{50}$  is between 7 and 8.

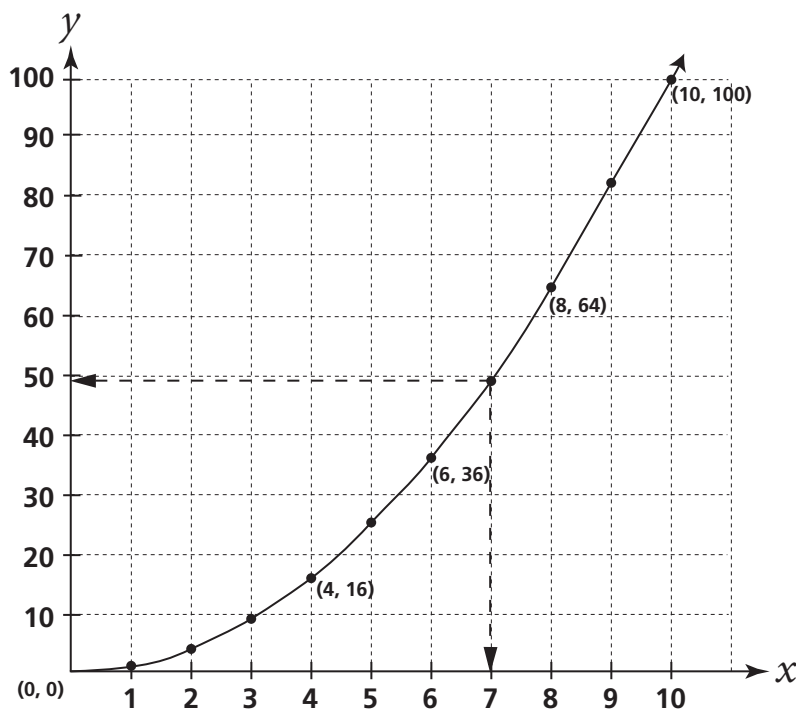
**Step 2** Find 50 on the left-hand scale and draw a straight line to the graph.

**Step 3** Draw a straight line from the point of the graph to the bottom axis. That line will cross the axis at about  $\sqrt{50}$ . The value is about 7.1.

**Step 4** Compare your estimated value to the calculator value, which is 7.07. So 7.1 for the graph is close to the calculator value of 7.07 rounded to the nearest hundredth.

**Directions** Use the graph to estimate these values.

1.  $\sqrt{95}$  \_\_\_\_\_
2.  $\sqrt{90}$  \_\_\_\_\_
3.  $\sqrt{85}$  \_\_\_\_\_
4.  $\sqrt{80}$  \_\_\_\_\_
5.  $\sqrt{75}$  \_\_\_\_\_
6.  $\sqrt{70}$  \_\_\_\_\_
7.  $\sqrt{65}$  \_\_\_\_\_
8.  $\sqrt{60}$  \_\_\_\_\_
9.  $\sqrt{45}$  \_\_\_\_\_
10.  $\sqrt{40}$  \_\_\_\_\_
11.  $\sqrt{35}$  \_\_\_\_\_
12.  $\sqrt{30}$  \_\_\_\_\_
13.  $\sqrt{25}$  \_\_\_\_\_
14.  $\sqrt{20}$  \_\_\_\_\_
15.  $\sqrt{15}$  \_\_\_\_\_



# Pythagorean Theorem

**EXAMPLE**

In any right triangle, sides  $a$  and  $b$  are the sides of the triangle that form the right angle. Side  $c$  is the hypotenuse, or longest side, of a right triangle. If you know the length of two sides of a right triangle, you can use the Pythagorean theorem to find the length of the third side.

The Pythagorean theorem is this formula:  $a^2 + b^2 = c^2$ .

Use the Pythagorean theorem to find the hypotenuse of this right triangle.

**Step 1** Substitute the values in the equation. Then square the values.

$$c^2 = a^2 + b^2$$

$$c^2 = 6^2 + 8^2$$

$$c^2 = 36 + 64$$

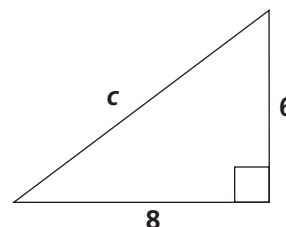
**Step 2** Take the square root of each side of the equation.

$$\sqrt{c^2} = \sqrt{36 + 64}$$

$$c = \sqrt{100}$$

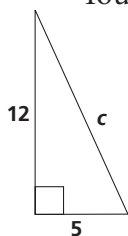
$$c = 10$$

The hypotenuse is 10 units long.



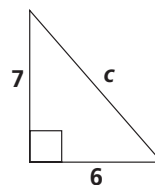
**Directions** Use the Pythagorean theorem to find the length of the side not given. You may use a calculator. If necessary, round to the nearest tenth.

1.



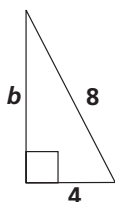
\_\_\_\_\_

2.



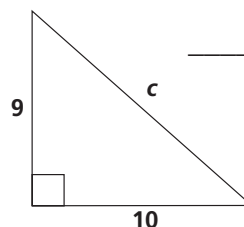
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3.



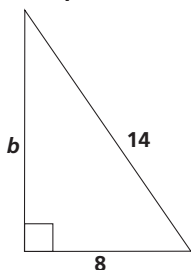
\_\_\_\_\_

4.



\_\_\_\_\_

5.



\_\_\_\_\_

## More About Triangles

**EXAMPLE**

Is this scalene triangle a right triangle?

**Step 1** Write the Pythagorean formula.

$$a^2 + b^2 = c^2$$

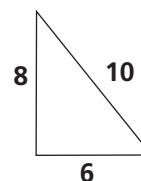
**Step 2** Substitute the triangle's values for  $a$ ,  $b$ , and  $c$ .

$$a^2 + b^2 = c^2$$

$$6^2 + 8^2 = 10^2$$

$$36 + 64 = 100$$

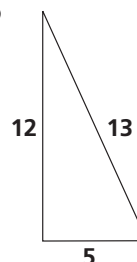
The equation is true, so this scalene triangle is also a right triangle.



**Directions** Answer the question. Then use the Pythagorean theorem to determine whether the triangle is also a right triangle.

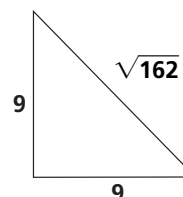
1. Is this triangle a scalene triangle, an isosceles triangle, or an equilateral triangle?

\_\_\_\_\_ Is it a right triangle? \_\_\_\_\_



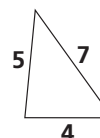
2. Is this triangle a scalene triangle, an isosceles triangle, or an equilateral triangle?

\_\_\_\_\_ Is it a right triangle? \_\_\_\_\_



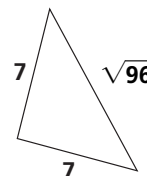
3. Is this triangle a scalene triangle, an isosceles triangle, or an equilateral triangle?

\_\_\_\_\_ Is it a right triangle? \_\_\_\_\_



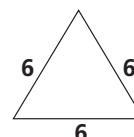
4. Is this triangle a scalene triangle, an isosceles triangle, or an equilateral triangle?

\_\_\_\_\_ Is it a right triangle? \_\_\_\_\_



5. Is this triangle a scalene triangle, an isosceles triangle, or an equilateral triangle?

\_\_\_\_\_ Is it a right triangle? \_\_\_\_\_

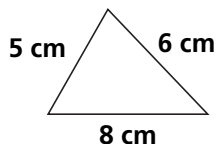
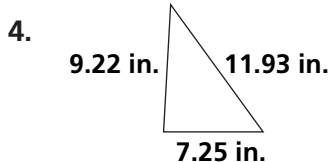
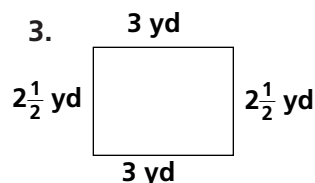
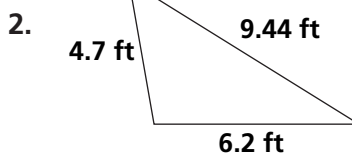
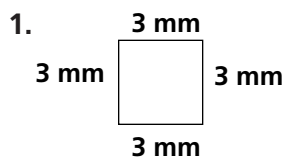


# Perimeters of Polygons

**EXAMPLE**

Find the perimeter of this figure.

$$\text{Perimeter} = 5 + 6 + 8 = 19 \text{ cm}$$

**Directions** Find the perimeter of each figure.**Directions** Solve each problem to find the perimeter.

- The sides of a quadrilateral measure  $6\frac{7}{8}$  ft,  $4\frac{1}{2}$  ft,  $3\frac{1}{8}$  ft, and  $7\frac{1}{2}$  ft. What is the perimeter? \_\_\_\_\_
- Two sides of an isosceles triangle measure 6.42 m each. The remaining side measures 9.73 m. What is the perimeter of the triangle? \_\_\_\_\_
- Each side of an equilateral triangle measures 48 yards. What is the perimeter? \_\_\_\_\_
- A scalene triangle has sides measuring 532.6 ft, 429.3 ft, and 830.6 ft. What is the perimeter? \_\_\_\_\_

**Directions** Solve each problem.

- Hector made a dog kennel in his backyard. He used a total of 28 feet of fencing, including the gate. If two sides of the kennel are ten feet each, what are the lengths of the other two sides? \_\_\_\_\_
- Maya has 13.75 inches of gold string, which she wants to glue around a picture frame in the shape of an equilateral triangle. Each side of the triangle is 4.25 inches. Does she have enough string? \_\_\_\_\_

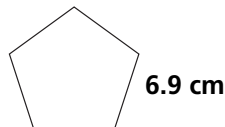


## Perimeters of Regular Polygons

**EXAMPLE**

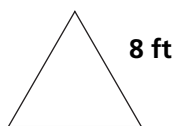
Each side of a regular pentagon measures 6.9 cm. Find the perimeter.

$$P = 5(6.9) = 34.5 \text{ cm}$$



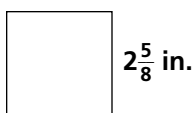
**Directions** Find the perimeter of each regular polygon.

1.



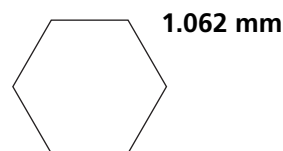
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2.



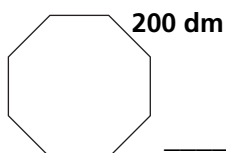
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3.



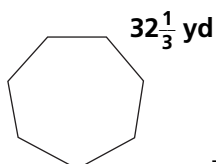
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4.



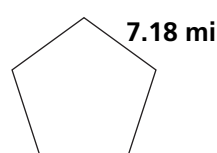
\_\_\_\_\_

5.



\_\_\_\_\_

6.



\_\_\_\_\_

**Directions** Find the number of sides that each shape has.

7. Each side of a regular polygon measures 3.67 m. The perimeter of the polygon is 47.71 m. How many sides does this regular polygon have?

\_\_\_\_\_

8. The perimeter of a regular polygon is 1,071 cm. Each side of the polygon measures 63 cm. How many sides does this regular polygon have?

\_\_\_\_\_

9. The sum of all sides of a regular polygon is 253 ft. Each side measures 11 ft. How many sides does this regular polygon have?

\_\_\_\_\_

10. The perimeter of a regular polygon is 13.125 ft. Each side measures 1.875 ft. How many sides does this regular polygon have?

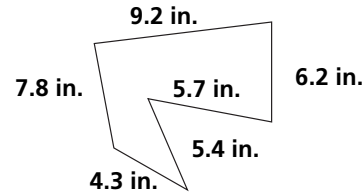
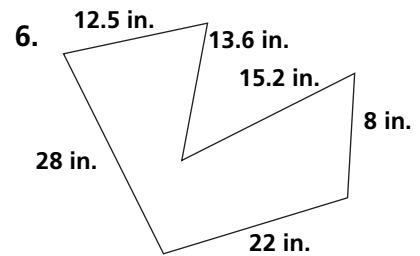
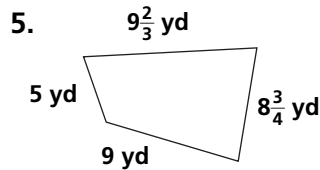
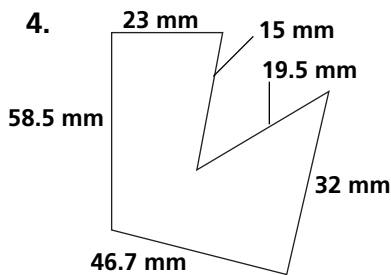
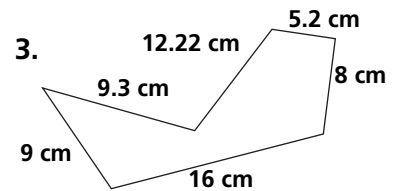
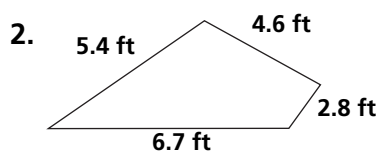
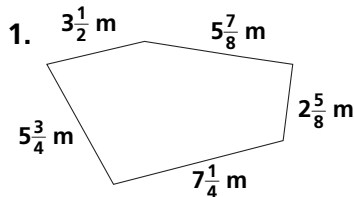
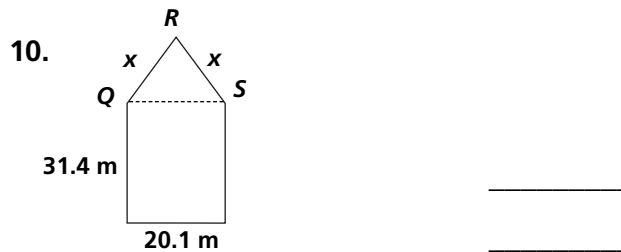
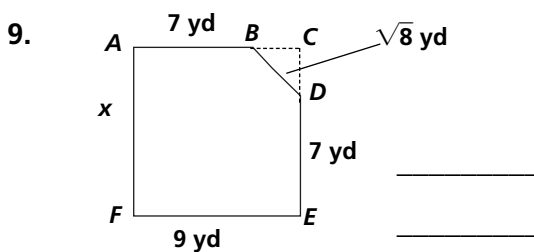
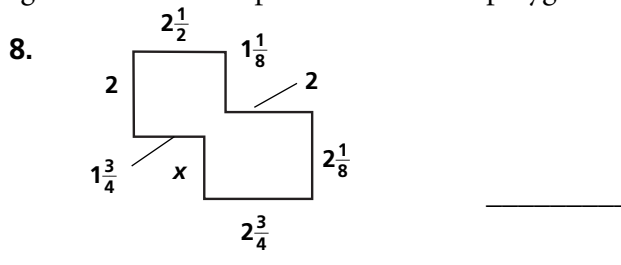
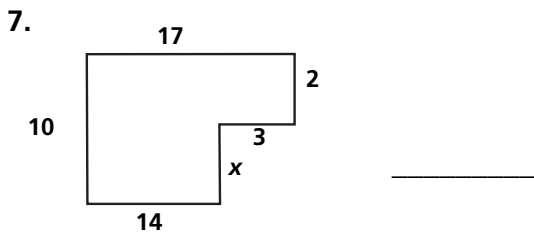
\_\_\_\_\_

# Perimeters of Irregular Polygons

**EXAMPLE**

Find the perimeter of this polygon.

$$P = 6.2 + 5.7 + 5.4 + 4.3 + 7.8 + 9.2 = 38.6 \text{ in.}$$

**Directions** Find the perimeter of each polygon.**Directions** Find the measure of each missing  $x$ . Then find the perimeter of each polygon.

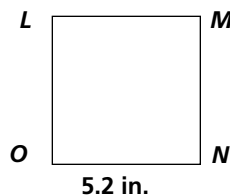
ACEF is a square.

Triangle QRS is an equilateral triangle.

# Areas of Rectangles and Squares

**EXAMPLE**Find the area of square  $LMNO$ .Substitute 5.2 into the formula  $A = s^2$ .

$$A = (5.2)^2 = 27.04 \text{ in.}^2$$

**Directions** Find the area of each rectangle.

1. Rectangle with  $l = 8$  ft and  $w = 6$  ft \_\_\_\_\_
2. Rectangle with  $l = 13$  m and  $w = 4$  m \_\_\_\_\_
3. Rectangle with  $l = 15.5$  cm and  $w = 8$  cm \_\_\_\_\_
4. Rectangle with  $l = 4\frac{1}{2}$  yd and  $w = 6\frac{1}{4}$  yd \_\_\_\_\_

**Directions** Find the area of each square.

5. Square with  $s = 10$  mm \_\_\_\_\_
6. Square with  $s = 21$  ft \_\_\_\_\_
7. Square with  $s = 4.2$  cm \_\_\_\_\_
8. Square with  $s = 5\frac{1}{2}$  m \_\_\_\_\_

**Directions** Use the formula  $A = s^2$  and a calculator to find the area of each square.

9.  $s = 23$  m \_\_\_\_\_
10.  $s = 6.7$  ft \_\_\_\_\_
11.  $s = 8.5$  cm \_\_\_\_\_
12.  $s = 42$  in. \_\_\_\_\_
13.  $s = 1.42$  mi \_\_\_\_\_

**Directions** Solve each problem.

14. Allen is painting a family room. Two walls are 8 ft high and 15 ft long. The other two walls are 8 ft high and 9 ft long. Allen has one gallon of paint, which will cover  $400 \text{ ft}^2$  of walls. Will he have enough paint? Explain.  
\_\_\_\_\_
15. Consuela cuts lawns as a part-time job. The last lawn she cut was rectangular and totaled  $1,365 \text{ yd}^2$ . One side of the lawn was 35 yards long. What was the length of the other side?  
\_\_\_\_\_

## Areas of Triangles

**EXAMPLE**

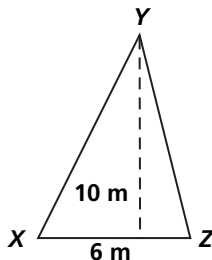
Find the area of triangle XYZ.

Use the formula  $A = \frac{1}{2}bh$ .

$$A = \frac{1}{2}(6)(10)$$

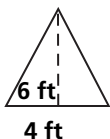
$$A = \frac{1}{2}(60)$$

$$A = 30 \text{ m}^2$$



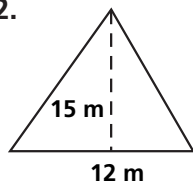
**Directions** Find the area of each figure.

1.



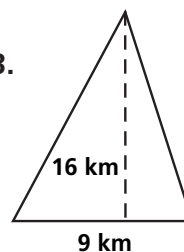
\_\_\_\_\_

2.



\_\_\_\_\_

3.



\_\_\_\_\_

**Directions** Find the base or height of each triangle.

4. The area of a triangle is  $12 \text{ ft}^2$  and the base is 4 ft. What is the height? \_\_\_\_\_
5. The area of a triangle is  $32 \text{ in.}^2$  and the height is 8 in. What is the base? \_\_\_\_\_
6. The area of a triangle is  $15 \text{ m}^2$  and the base is 10 m. What is the height? \_\_\_\_\_
7. The area of a triangle is  $36 \text{ yd}^2$  and the height is 9 yd. What is the base? \_\_\_\_\_
8. The area of a triangle is  $36 \text{ km}^2$  and the height is 12 km. What is the base? \_\_\_\_\_

**Directions** Solve these problems.

9. Howard is constructing a triangular garden edge out of brick. The base of the garden is 15 ft. The area is  $165 \text{ ft}^2$ . What is the height of the triangle?  
\_\_\_\_\_
10. Jana is making curtains in the shape of triangles. She needs to make two triangle curtains for one window. The triangles have a base of 2 ft and a height of 4 ft. What is the total area of the triangle curtains for one window?  
\_\_\_\_\_

# Areas of Trapezoids and Parallelograms

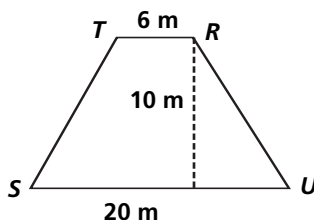
**EXAMPLE**

Find the area of trapezoid  $STRU$ .

$$A = \frac{b_1 + b_2}{2} h$$

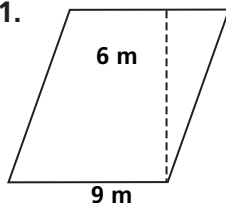
$$A = \frac{6 + 20}{2}(10) = \frac{26}{2}(10)$$

$$A = (13)(10) = 130 \text{ m}^2$$



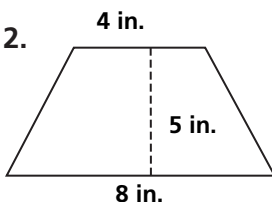
**Directions** Find the area of each quadrilateral.

1.



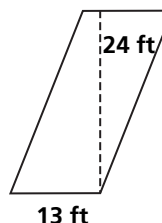
\_\_\_\_\_

2.



\_\_\_\_\_

3.



\_\_\_\_\_

**Directions** Find the base or height of each quadrilateral.

4. A parallelogram has a height of 9 cm and an area of  $108 \text{ cm}^2$ .

What is the length of its base? \_\_\_\_\_

5. A trapezoid has one base 6 ft long and another base 8 ft long. Its area is  $240 \text{ ft}^2$ .

What is its height? \_\_\_\_\_

6. If a parallelogram has a base of 11 m and an area of  $176 \text{ m}^2$ , what is its height?

\_\_\_\_\_

7. A parallelogram has a height of 12 in. and an area of  $168 \text{ in.}^2$ .

What is the length of its base? \_\_\_\_\_

8. The bases of a trapezoid equal 16 km and its area is  $32 \text{ km}^2$ . What is its height? \_\_\_\_\_

9. If a parallelogram has a base of 13 mm and an area of  $78 \text{ mm}^2$ ,

what is its height? \_\_\_\_\_

10. The bases of a trapezoid equal 17 yd and its area is  $68 \text{ yd}^2$ . What is its height? \_\_\_\_\_

# Areas of Irregular Polygons

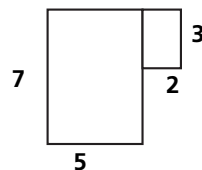
**EXAMPLE**

Find the area of this polygon.

Divide the polygon into smaller regions to calculate the areas.

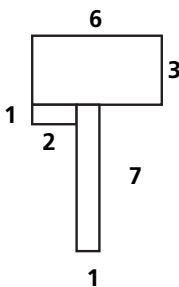
$$A = (5 \cdot 7) + (2 \cdot 3)$$

$$A = 35 + 6 = 41 \text{ units}^2$$



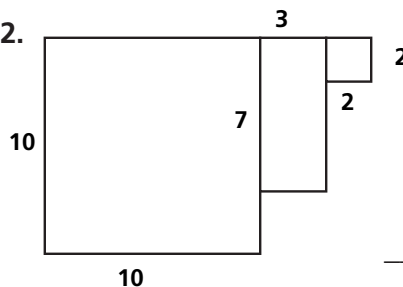
**Directions** Find the area of each polygon.

1.



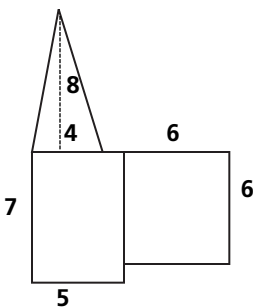
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2.



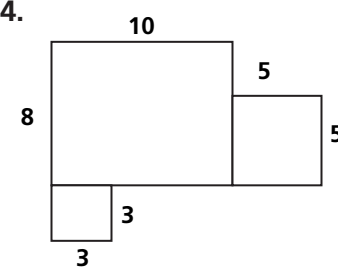
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3.



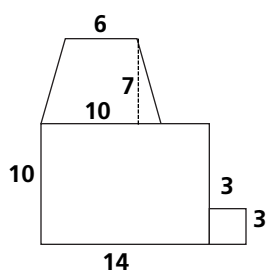
\_\_\_\_\_

4.



\_\_\_\_\_

5.



\_\_\_\_\_

## Working with Areas of Shapes

**Directions** Find the area of each rectangle or square.

1. Rectangle with  $l = 9$  in. and  $w = 3.85$  in. \_\_\_\_\_
2. Rectangle with  $l = 3\frac{1}{3}$  mi and  $w = 7\frac{1}{2}$  mi \_\_\_\_\_
3. Square with  $s = 16.3$  yd \_\_\_\_\_
4. Square with  $s = 3\frac{1}{4}$  ft \_\_\_\_\_
5. Square with  $s = 12.33$  mi \_\_\_\_\_

**Directions** Use the area to find the base or height of each triangle, trapezoid, or parallelogram.

6. The area of a triangle is  $14 \text{ ft}^2$  and the base is 7 ft. What is the height? \_\_\_\_\_
7. The area of a triangle is  $15 \text{ mm}^2$  and the height is 5 mm. What is the base? \_\_\_\_\_
8. The area of a triangle is  $9 \text{ cm}^2$  and the base is 3 cm. What is the height? \_\_\_\_\_
9. The area of a triangle is  $50 \text{ in.}^2$  and the base is 10 in. What is the height? \_\_\_\_\_
10. The area of a triangle is  $80 \text{ m}^2$  and the height is 8 m. What is the base? \_\_\_\_\_
11. The area of a triangle is  $40.5 \text{ ft}^2$  and the base is 9 ft. What is the height? \_\_\_\_\_
12. The area of a triangle is  $17.5 \text{ dm}^2$  and the height is 7 dm. What is the base? \_\_\_\_\_
13. A trapezoid has one base 23 in. long and another base 27 in. long. Its area is  $400 \text{ in.}^2$ .  
What is its height? \_\_\_\_\_
14. The bases of a trapezoid equal 68 mm and its area is  $1,768 \text{ mm}^2$ .  
What is its height? \_\_\_\_\_
15. A parallelogram has a height of 23 mi and an area of  $667 \text{ mi}^2$ .  
What is the length of its base? \_\_\_\_\_

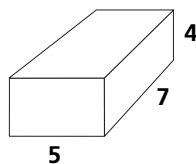
# Volume

**EXAMPLE**

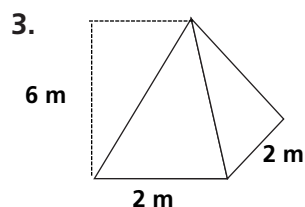
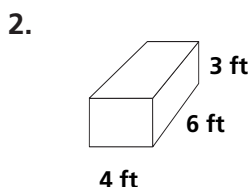
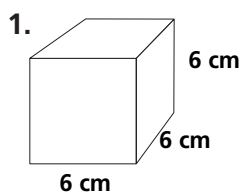
Find the volume of this rectangular prism.

$$V = lwh$$

$$V = (7)(5)(4) = 140 \text{ in.}^3$$



**Directions** Find the volume of each figure.



**Directions** Use the formula  $V = e^3$  and a calculator to find the volume of each cube.

4.  $e = 23 \text{ mm}$  \_\_\_\_\_

10.  $e = 68 \text{ dm}$  \_\_\_\_\_

5.  $e = 1.8 \text{ in.}$  \_\_\_\_\_

11.  $e = 43 \text{ m}$  \_\_\_\_\_

6.  $e = 126 \text{ ft}$  \_\_\_\_\_

12.  $e = 19.2 \text{ in.}$  \_\_\_\_\_

7.  $e = 0.9 \text{ mi}$  \_\_\_\_\_

13.  $e = 202 \text{ ft}$  \_\_\_\_\_

8.  $e = 50 \text{ cm}$  \_\_\_\_\_

9.  $e = 1.02 \text{ km}$  \_\_\_\_\_

**Directions** Solve each problem.

14. Marcus is shipping books to his brother in New York. The box is 10 inches by 10 inches and 6 inches deep. Each book is 5 inches by 5 inches and 2 inches thick. How many books can Marcus ship in one package? \_\_\_\_\_

15. Lisa's suitcase is 18 inches wide, 32 inches high, and 36 inches long. What is the volume of the suitcase? \_\_\_\_\_



## Circumferences and Areas of Circles

**EXAMPLE**

Find the circumference and area of a circle with a radius of 5 feet.

To find the circumference, use the formula  $C = \pi d$ .

First, calculate the diameter.

$$2 \cdot 5 = 10 \text{ feet}$$

$$C = (3.14)(10) = 31.4 \text{ feet}$$

To find the area, use the formula  $A = \pi r^2$ .

$$A = (3.14)(5^2) = 78.5 \text{ feet}^2$$

**Directions** Find the circumference of a circle with the given radius or diameter. Use the formula  $C = \pi d$ . Use 3.14 for  $\pi$ .

1. radius = 4 in. \_\_\_\_\_

4. diameter = 10 mm \_\_\_\_\_

2. diameter = 6 ft \_\_\_\_\_

5. radius = 7 km \_\_\_\_\_

3. radius = 2 m \_\_\_\_\_

**Directions** Find the area of a circle with the given radius or diameter. Use the formula  $A = \pi r^2$ . Use 3.14 for  $\pi$ .

6. radius = 3 yd \_\_\_\_\_

11. radius = 6 km \_\_\_\_\_

7. diameter = 10 cm \_\_\_\_\_

12. radius = 5 mi \_\_\_\_\_

8. radius = 7 ft \_\_\_\_\_

13. diameter = 6 in. \_\_\_\_\_

9. diameter = 4 m \_\_\_\_\_

14. radius = 8 ft \_\_\_\_\_

10. diameter = 14 in. \_\_\_\_\_

15. radius = 10 m \_\_\_\_\_

**Directions** Use a calculator and the formula  $A = \pi r^2$  to find the areas of circles with the following measures. Use 3.14 for  $\pi$ .

16. diameter = 1.25 yd \_\_\_\_\_

19. diameter = 9.5 m \_\_\_\_\_

17. radius = 215 mi \_\_\_\_\_

20. radius = 1.8 km \_\_\_\_\_

18. radius = 6.7 ft \_\_\_\_\_

## Volumes of Cylinders and Spheres

**EXAMPLE**

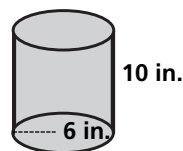
Find the volume of this cylinder.

Use the formula  $V = \pi r^2 h$ .

$$V = (3.14)(6)^2(10)$$

$$V = (3.14)(36)(10)$$

$$V = 1,130.4 \text{ in.}^3$$



**Directions** Find the volume of a cylinder with the given height and radius or diameter. Use the formula  $V = \pi r^2 h$ . Use 3.14 for  $\pi$ .

- |   |   |
|---|---|
| 1. diameter = 6 in.; height = 5 in. _____ | 6. diameter = 4 cm; height = 4 cm _____   |
| 2. radius = 4 ft; height = 7 ft _____     | 7. radius = 9 m; height = 13 m _____      |
| 3. diameter = 10 mm; height = 8 mm _____  | 8. radius = 1 ft; height = 6 ft _____     |
| 4. radius = 3 cm; height = 2 cm _____     | 9. radius = 7 cm; height = 14 cm _____    |
| 5. diameter = 2 yd; height = 6 yd _____   | 10. diameter = 6 yd; height = 50 yd _____ |

**Directions** Find the volume of a sphere with the given radius or diameter. Use the formula  $V = \frac{4}{3}\pi r^3$ . Use 3.14 for  $\pi$ .

- |                            |                             |
|----------------------------|-----------------------------|
| 11. radius = 3 cm _____    | 15. diameter = 30 cm _____  |
| 12. radius = 6 ft _____    | 16. radius = 12 ft _____    |
| 13. diameter = 48 mm _____ | 17. diameter = 21 m _____   |
| 14. radius = 9 yd _____    | 18. diameter = 15 in. _____ |

**Directions** Solve each problem.

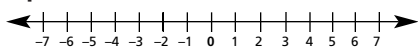
19. George filled a plastic bag with water until it had a diameter of 9 inches. What was the volume of the bag? \_\_\_\_\_
20. Lin has two boxes to choose from to mail a package to her sister in Florida. One is a rectangular box measuring 12 inches long, 9 inches high, and 10 inches wide. The other is a cylinder with a diameter of 10 inches and a height of 14 inches. She wants the larger box. Which one should she pick? Explain.
- \_\_\_\_\_

# Graphing Equalities

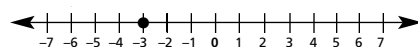
**EXAMPLE**

Graph the solution  $x = -3$  on a number line.

**Step 1** Draw a number line.



**Step 2** Make a shaded circle on the number line at  $-3$ .



**Directions** Graph each solution on a number line.

1.  $t = 5$

5.  $y = -3$

9.  $s = -\frac{1}{3}$

2.  $a = 3$

6.  $q = -10$

10.  $m = 2$

3.  $d = -5$

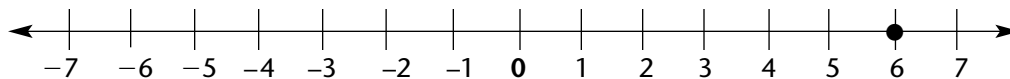
7.  $j = 6$

4.  $x = 0$

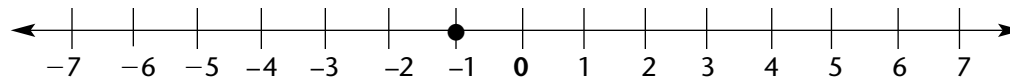
8.  $z = -2$

**Directions** Write a solution for each equality. Use  $x$  as the variable in each of the solutions.

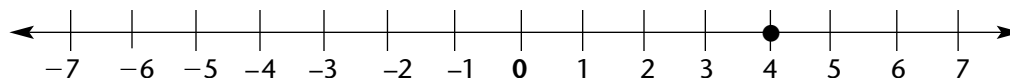
11. \_\_\_\_\_



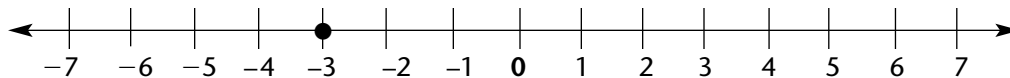
12. \_\_\_\_\_



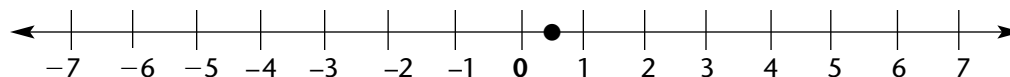
13. \_\_\_\_\_



14. \_\_\_\_\_



15. \_\_\_\_\_

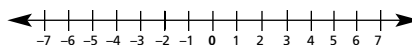


# Graphing Inequalities

**EXAMPLE**

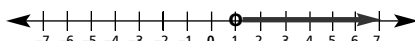
Graph the solution  $y > 1$  on a number line.

**Step 1** Draw a number line.



**Step 2** Note that  $y > 1$  means the solution is greater than 1.

**Step 3** Make an open circle on 1 with a line extending right and an arrow pointing right.



**Directions** Graph each solution on a number line.

1.  $y > 8$

5.  $a \geq 6$

9.  $l \neq 8$

2.  $x < 4$

6.  $w < -5$

10.  $k \geq -3$

3.  $t \leq -2$

7.  $h > -9$

4.  $s > 0$

8.  $j \leq 12$

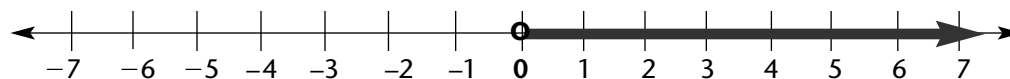
**Directions** Write a solution for each inequality. Use  $x$  as the variable in each of the solutions.



11. \_\_\_\_\_



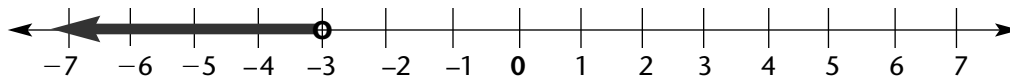
12. \_\_\_\_\_



13. \_\_\_\_\_



14. \_\_\_\_\_



15. \_\_\_\_\_

# Graphing Solutions of Equalities

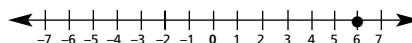
**EXAMPLE**

Solve  $c + 4 = 10$  for  $c$ . Then graph the solution.

**Step 1** Solve for  $c$  by subtracting 4 from each side of the equality.

$$c + 4 - 4 = 10 - 4 \quad c = 10 - 4 \quad c = 6$$

**Step 2** Graph the solution on a number line.



**Step 3** Check your work by substitution.

$$c + 4 = 10 \quad 6 + 4 = 10 \quad \text{True}$$

**Directions** Solve each equality for the variable. Then graph and check each solution.

- |                 |       |                   |       |
|-----------------|-------|-------------------|-------|
| 1. $x + 3 = 7$  | _____ | 10. $p - 3 = -5$  | _____ |
| 2. $5 + c = 4$  | _____ | 11. $y + 5 = -3$  | _____ |
| 3. $h - 3 = 0$  | _____ | 12. $t - 7 = -6$  | _____ |
| 4. $m + 6 = -3$ | _____ | 13. $a + 9 = 9$   | _____ |
| 5. $4 + j = -1$ | _____ | 14. $e - 8 = 5$   | _____ |
| 6. $s - 2 = 4$  | _____ | 15. $l - 2 = 3$   | _____ |
| 7. $g + 7 = 3$  | _____ | 16. $b + 10 = -5$ | _____ |
| 8. $7 + v = 9$  | _____ | 17. $-5 + n = -3$ | _____ |
| 9. $d - 1 = 7$  | _____ | 18. $z - 3 = 4$   | _____ |

**Directions** Write and solve an equality for each problem. Use  $x$  as the variable in the equality. Graph your solution on a number line.

19. Calvin sprinted 300 meters more today than yesterday. He sprinted 900 meters today. How many meters did he sprint yesterday? \_\_\_\_\_
20. Maria jumped 3 inches farther in the long jump Thursday than Friday. She jumped 6 feet 8 inches on Friday. How far did she jump on Thursday? \_\_\_\_\_

# Graphing Solutions of Inequalities

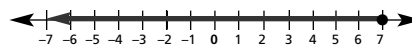
**EXAMPLE**

Solve  $m + 3 \leq 10$  for  $m$ . Then graph the solution.

**Step 1** Solve for  $m$  by subtracting 3 from each side of the inequality.

$$m + 3 - 3 \leq 10 - 3 \quad m \leq 7$$

**Step 2** Graph the solution on a number line.



**Step 3** Check your work by substitution.

$$7 + 3 \leq 10 \quad 10 \leq 10 \quad \text{True}$$

**Directions** Solve each equality or inequality for the variable. Then graph and check each solution.

- |                           |                           |
|---------------------------|---------------------------|
| 1. $x + 4 \leq 6$ _____   | 13. $s - 9 > -6$ _____    |
| 2. $p - 3 < 8$ _____      | 14. $g + 7 \geq 9$ _____  |
| 3. $2 + d > -2$ _____     | 15. $n - 8 \leq -5$ _____ |
| 4. $t - 2 > -4$ _____     | 16. $m - 2 \geq 8$ _____  |
| 5. $r - 6 \geq -1$ _____  | 17. $k + 8 < 7$ _____     |
| 6. $e + 3 < -4$ _____     | 18. $p - 6 > 5$ _____     |
| 7. $w - 5 \leq 6$ _____   | 19. $w + 2 \leq -1$ _____ |
| 8. $q + 5 \leq 2$ _____   | 20. $4 + u > 8$ _____     |
| 9. $a - 7 < 2$ _____      | 21. $d - 7 < -5$ _____    |
| 10. $b - 1 > -3$ _____    | 22. $i - 4 \geq 1$ _____  |
| 11. $x + 4 < -6$ _____    | 23. $-1 + z \geq 0$ _____ |
| 12. $2 + f \geq -4$ _____ |                           |

**Directions** Write and solve an inequality for each problem. Use  $x$  as the variable in the inequality. Graph your solution on a number line.

- |  |   |
|--|---|
| <p>24. The results of a survey taken at Washington High School showed that 6 or fewer of every 10 people said rock music was their favorite type of music. How many people did not choose rock music?</p> <p>_____</p> | <p>25. The number of students attending a home basketball game at Washington High School is always at least 25 more than the number of rows in the bleachers. There are 10 rows of bleachers. How many people attend each home game?</p> <p>_____</p> |
|--|---|

# The Coordinate System—Locating Points

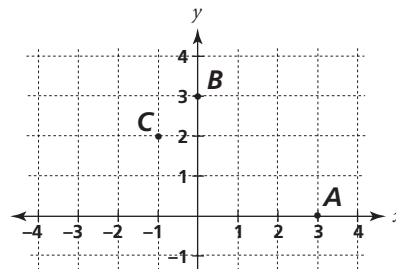
**EXAMPLE**

Locate points  $A$ ,  $B$ , and  $C$ . Remember to always read the  $x$ -axis first, then the  $y$ -axis.

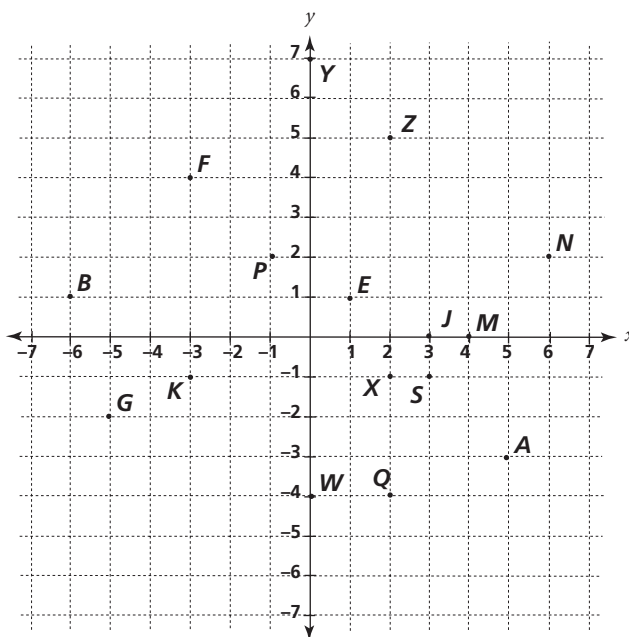
The ordered pair for Point  $A$  is  $(3, 0)$ .

The ordered pair for Point  $B$  is  $(0, 3)$ .

The ordered pair for Point  $C$  is  $(-1, 2)$ .



**Directions** Write the ordered pair that describes the location of each point.



- |                    |                     |                     |
|--------------------|---------------------|---------------------|
| 1. Point $E$ _____ | 6. Point $Q$ _____  | 11. Point $M$ _____ |
| 2. Point $J$ _____ | 7. Point $Y$ _____  | 12. Point $X$ _____ |
| 3. Point $K$ _____ | 8. Point $B$ _____  | 13. Point $A$ _____ |
| 4. Point $N$ _____ | 9. Point $F$ _____  | 14. Point $G$ _____ |
| 5. Point $P$ _____ | 10. Point $W$ _____ | 15. Point $Z$ _____ |

**Directions** Identify the quadrant in which each of these points is located.

- |                     |                     |                     |
|---------------------|---------------------|---------------------|
| 16. Point $N$ _____ | 18. Point $B$ _____ | 20. Point $Z$ _____ |
| 17. Point $A$ _____ | 19. Point $G$ _____ |                     |

# The Coordinate System—Plotting Points

**EXAMPLE**

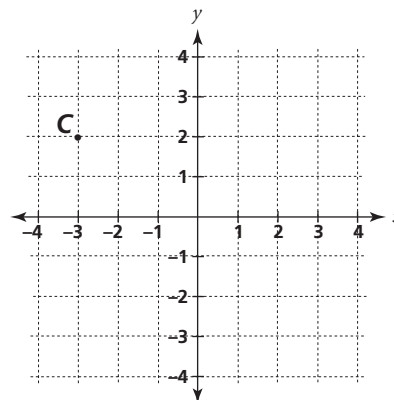
Plot a point at  $(-3, 2)$ . Label the point C.

**Step 1** Construct a coordinate system large enough to include the ordered pair  $(-3, 2)$ .

**Step 2** To plot  $(-3, 2)$ , begin at the origin  $(0,0)$ . Move 3 units *left* on the  $x$ -axis.

**Step 3** Move 2 units up.

**Step 4** Make a shaded circle at  $(-3, 2)$ .



**Directions** On a sheet of graph paper, draw a coordinate system. Then use it to plot and label each point shown in problems 1–20.

- |                       |                        |                        |
|-----------------------|------------------------|------------------------|
| 1. Point X $(5, 6)$   | 8. Point D $(3, -4)$   | 15. Point B $(-1, 5)$  |
| 2. Point Q $(2, -5)$  | 9. Point C $(-5, -4)$  | 16. Point Y $(-7, -8)$ |
| 3. Point A $(-5, 0)$  | 10. Point V $(0, 6)$   | 17. Point H $(-6, -7)$ |
| 4. Point W $(-1, -3)$ | 11. Point F $(-6, -3)$ | 18. Point N $(7, -6)$  |
| 5. Point S $(-2, 5)$  | 12. Point R $(-7, 5)$  | 19. Point J $(4, 4)$   |
| 6. Point Z $(1, 3)$   | 13. Point T $(5, -5)$  | 20. Point M $(2, -6)$  |
| 7. Point E $(-4, 6)$  | 14. Point G $(4, 6)$   |                        |

**Directions** Using the above points, identify the quadrant in which each point is located.

21. Point F \_\_\_\_\_
22. Point N \_\_\_\_\_
23. Point G \_\_\_\_\_
24. Point B \_\_\_\_\_
25. Point Q \_\_\_\_\_



# Determining the Points of a Line

## EXAMPLE

Complete the table of values for the line  $y = x + 3$ .

**Step 1** Substitute  $-2$  for  $x$  and solve for  $y$ .

$$y = x + 3 \quad y = -2 + 3 \quad y = 1$$

**Step 2** Substitute  $3$  for  $y$  and solve for  $x$ .

$$y = x + 3 \quad 3 = x + 3 \quad 3 - 3 = x + 3 - 3 \quad 0 = x$$

**Step 3** Substitute  $4$  for  $x$  and solve for  $y$ .

$$y = x + 3 \quad y = 4 + 3 \quad y = 7$$

**Step 4** Complete the table of values.

$y = x + 3$	
$x$	$y$
$-2$	
	$3$
$4$	

$y = x + 3$	
$x$	$y$
$-2$	$1$
$0$	$3$
$4$	$7$

**Directions** Complete each table of values.

1.

$y = x + 5$	
$x$	$y$
$-3$	
$2$	
$6$	

2.

$y = x - 4$	
$x$	$y$
$-2$	
$-1$	
	$-1$

3.

$y = x + 7$	
$x$	$y$
$-4$	
	$7$
$4$	

4.

$y = x - 3$	
$x$	$y$
	$1$
	$-3$
	$-5$

5.

$y = x + 9$	
$x$	$y$
	$6$
	$9$
$5$	

6.

$y = x + 8$	
$x$	$y$
	$1$
$0$	
	$10$

7.

$y = x - 2$	
$x$	$y$
$-1$	
	$1$
	$4$

8.

$y = x + 6$	
$x$	$y$
$-7$	
	$2$
$-1$	

**Directions** Use a calculator to complete the tables of values.

9.

$y = x + 25.7$	
$x$	$y$
	$18.8$
$-3.4$	
$8.7$	

10.

$y = x - 12.3$	
$x$	$y$
$-7.8$	
	$-8.2$
	$10.9$

# Tables of Values and Coordinate Systems

**Directions** Make a table of values for each linear equation.

1.

$y = x + 1$	
$x$	$y$

2.

$y = x - 5$	
$x$	$y$

3.

$y = x - 7$	
$x$	$y$

4.

$y = x - 1$	
$x$	$y$

5.

$y = x + 2$	
$x$	$y$

6.

$y = x + 4$	
$x$	$y$

**Directions** On a sheet of graph paper, draw a coordinate system with  $x$  values from  $-7$  to  $7$  and  $y$  values from  $-7$  to  $7$ . Suppose that the system stands for a grid to map a lake. Use it to answer these questions.

7. How far away is the sandbar  $(2, 0)$  from the boat  $(2, 6)$ ?

\_\_\_\_\_

8. Willie drives the boat  $(2, 6)$  to the sandbar  $(2, 0)$  and then to the deepest part of the lake  $(-4, 0)$ . How far does he drive the boat?

\_\_\_\_\_

9. Sarah swims from the end of the sandbar  $(-1, 0)$  to the boat dock  $(-1, -7)$ . How far does she swim?

\_\_\_\_\_

10. Zach walks along the sandbar  $(2, 0)$  to the end of the sandbar  $(-1, 0)$  and back again. How far does he walk?

\_\_\_\_\_

# Graphing Lines

**EXAMPLE**

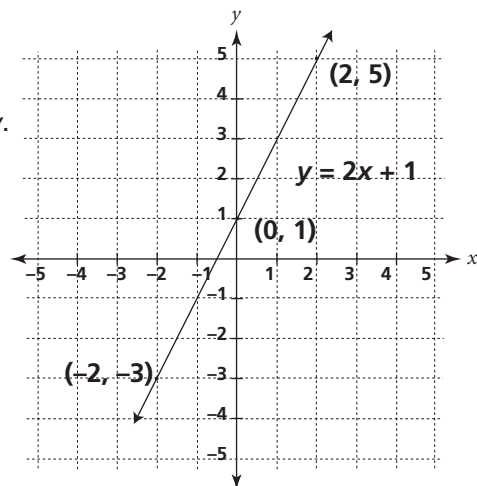
Graph the linear equation  $y = 2x + 1$ .

**Step 1** Make a table of values.

**Step 2** Choose three different values for  $x$  and solve for  $y$ .

**Step 3** Draw a coordinate system and plot the points from the table of values. Connect the points, draw arrows at the ends of the line, and label the line  $y = 2x + 1$ .

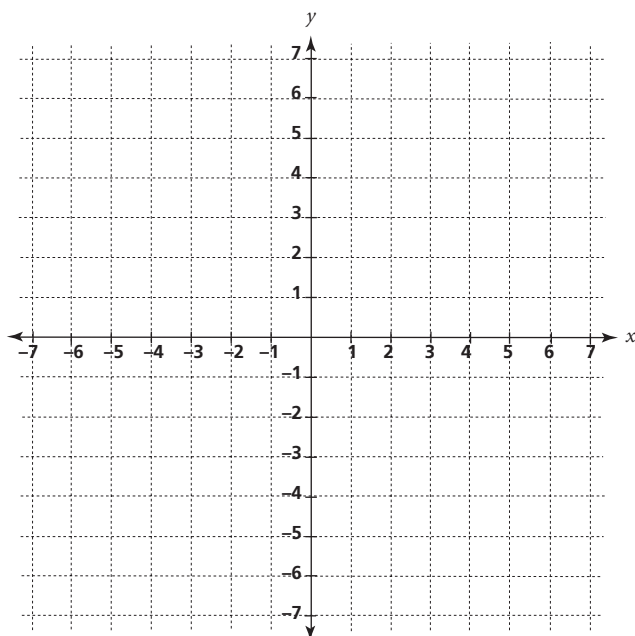
$y = 2x + 1$	
$x$	$y$
-2	-3
0	1
2	5



**Directions** Complete each table of values. Graph the first linear equation here and the others on graph paper.

1.

$y = x + 3$	
$x$	$y$



2.

$y = 2x + 4$	
$x$	$y$

3.

$y = x - 1$	
$x$	$y$

4.

$y = 3x$	
$x$	$y$

5.

$y = -x$	
$x$	$y$

# The Slope of a Line

## EXAMPLE

What is the slope of a roof that is 20 feet long and falls 5 feet in that distance?

**Step 1** Express the slope as the fraction  $\frac{\text{rise}}{\text{run}}$ .

**Step 2**  $\frac{\text{rise}}{\text{run}} = \frac{-5}{+20}$

**Step 3** Simplify if possible.  $\frac{-5}{+20} = \frac{-1}{4}$

A slope of  $\frac{-1}{4}$  means that for every 4 feet of horizontal distance, the roof falls 1 foot.

On a calculator, press  $-5 \div 20$ . The display shows  $-0.25$ .

**Directions** In this chart, *Distance* is a horizontal measure and *Change in Elevation* is a vertical measure. Use a calculator to find each slope.

Distance	Change in Elevation	Slope
1. 8 mi	6 mi	
2. 80 ft	70 ft	
3. 63.2 yd	151.38 yd	
4. 5.2 m	−3.588 m	
5. 4.2 cm	7.686 cm	
6. 5.1 mm	0.102 mm	
7. 9 in.	−117 in.	
8. 8.1 km	18.225 km	
9. 6.6 yd	6.138 yd	
10. 24 mi	144 mi	
11. 15 m	11.55 m	
12. 13 in.	−416 in.	
13. 6.6 cm	29.04 cm	
14. −8.5 km	2.55 km	
15. 3.25 ft	−83.2 ft	

## Formula for the Slope of a Line

**EXAMPLE**

A line passes through points (0, 0) and (2, 4). Find the slope of the line.

**Step 1** Substitute the values for  $(x_1, y_1)$  and  $(x_2, y_2)$  into the formula  $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{4 - 0}{2 - 0} = \frac{4}{2}$ .

Remember that points (0, 0) and (2, 4) are written in the form  $(x_1, y_1)$  and  $(x_2, y_2)$ .

**Step 2** Simplify.  $\frac{4 - 0}{2 - 0} = \frac{4}{2} = 2$

The slope of a line passing through points (0, 0) and (2, 4) is 2.

**Directions** Find the slope of a line that passes through the given points.

- |                              |                                 |
|------------------------------|---------------------------------|
| 1. (0, 2) and (3, 11) _____  | 10. (2, -4) and (6, 3) _____    |
| 2. (4, 12) and (-1, 7) _____ | 11. (-3, -3) and (-8, -4) _____ |
| 3. (8, 4) and (-6, -3) _____ | 12. (6, 2) and (3, 8) _____     |
| 4. (4, 2) and (-8, -1) _____ | 13. (0, 1) and (5, 7) _____     |
| 5. (5, 4) and (7, -2) _____  | 14. (-3, 0) and (1, 8) _____    |
| 6. (-1, 8) and (5, 8) _____  | 15. (1, 1) and (5, 9) _____     |
| 7. (3, 1) and (2, 5) _____   | 16. (5, 3) and (9, 2) _____     |
| 8. (7, 9) and (-5, -1) _____ | 17. (3, -3) and (4, -5) _____   |
| 9. (7, 8) and (0, 3) _____   |                                 |

**Directions** Answer each question.

18. In a soapbox derby, the first part of a hill has a slope of  $\frac{-5}{25}$  and the second part of the hill has a slope of  $\frac{-4}{16}$ . Which part of the hill has the steeper slope? Explain. \_\_\_\_\_
19. A bicycle trail has two slopes. The first slope is  $\frac{-3}{20}$  and the second slope is  $\frac{5}{15}$ . Which is the easier to ride? Explain. \_\_\_\_\_
20. Tae wants to exercise by jogging up a hill. One hill has a slope of  $\frac{3}{20}$ . Another hill has a slope of  $\frac{6}{40}$ . Which hill will be more difficult to jog up? Explain. \_\_\_\_\_

# The Slope-Intercept Form of a Line

## EXAMPLE

Find the slope, x-intercept, and y-intercept of the line  $2y = 6x + 4$ .

**Step 1** Write  $2y = 6x + 4$  in the slope-intercept form by solving for  $y$ .

$$\frac{2y}{2} = \frac{6x}{2} + \frac{4}{2} \quad y = 3x + 2$$

**Step 2** Determine the slope by looking at the form  $y = mx + b$ .

$y = 3x + 2$  The slope is 3, since it corresponds to  $m$ .

**Step 3** Determine the y-intercept by looking at the form  $y = mx + b$ .

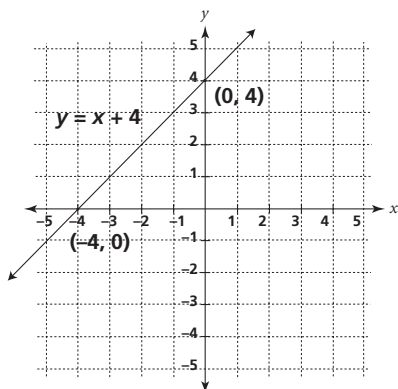
$y = 3x + 2$  The y-intercept is 2, since it corresponds to  $b$ .

**Step 4** Determine the x-intercept by substituting 0 for  $y$  and solving for  $x$ .

$$y = 3x + 2 \quad 0 = 3x + 2 \quad -3x = 2 \quad x = \frac{-2}{3} \quad \text{The x-intercept of the line is } \frac{-2}{3}.$$

**Directions** Identify the slope, x-intercept, and y-intercept of each line.

1.

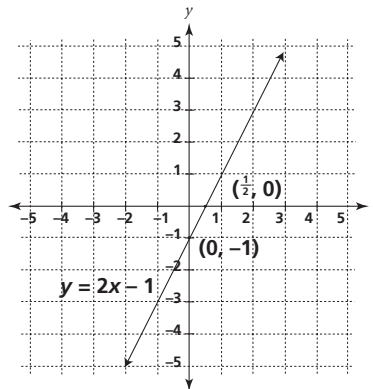


\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

2.



\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

**Directions** Write each of these linear equations in slope-intercept form.

3.  $4y = 8x + 20$  \_\_\_\_\_

6.  $-3y = 6x + 3$  \_\_\_\_\_

4.  $-y = -x + 8$  \_\_\_\_\_

7.  $4y = 4x - 28$  \_\_\_\_\_

5.  $2y = -6x + 6$  \_\_\_\_\_

8.  $-2y = 2x - 1$  \_\_\_\_\_

**Directions** Find the slope, x-intercept, and y-intercept of each line.

9.  $y = x - 5$  \_\_\_\_\_

13.  $y = 4x + 1$  \_\_\_\_\_

10.  $y = 2x + 4$  \_\_\_\_\_

14.  $2y = -2x + 6$  \_\_\_\_\_

11.  $y = -3x - 1$  \_\_\_\_\_

15.  $-3y = 6x - 15$  \_\_\_\_\_

12.  $y = x - 2$  \_\_\_\_\_

# Angles and Angle Measures

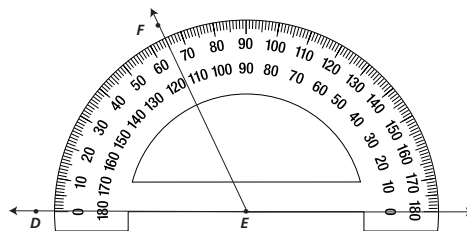
## EXAMPLE

Find the measure of  $\angle DEF$ .

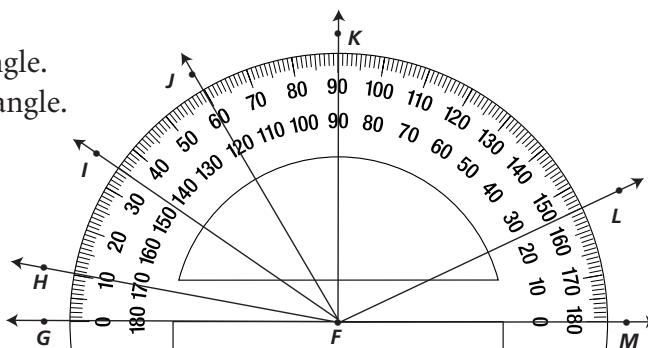
**Step 1** Place the center of the protractor at the vertex of the angle.

**Step 2** Place the  $0^\circ$  line of the protractor along one of the rays in the angle.

**Step 3** Read the measure of the angle, counting up from  $0^\circ$ . The measure of  $\angle DEF = 65^\circ$ .



**Directions** Use the illustration at the right.  
Name the rays that make each angle.  
Then write the measure of each angle.



Angle

Rays

Measure

1.  $\angle GFH$

\_\_\_\_\_

\_\_\_\_\_

2.  $\angle GFI$

\_\_\_\_\_

\_\_\_\_\_

3.  $\angle GFJ$

\_\_\_\_\_

\_\_\_\_\_

4.  $\angle GFK$

\_\_\_\_\_

\_\_\_\_\_

5.  $\angle GFL$

\_\_\_\_\_

\_\_\_\_\_

Angle

Rays

Measure

6.  $\angle LFM$

\_\_\_\_\_

\_\_\_\_\_

7.  $\angle KFM$

\_\_\_\_\_

\_\_\_\_\_

8.  $\angle JFM$

\_\_\_\_\_

\_\_\_\_\_

9.  $\angle IFM$

\_\_\_\_\_

\_\_\_\_\_

10.  $\angle HFM$

\_\_\_\_\_

\_\_\_\_\_

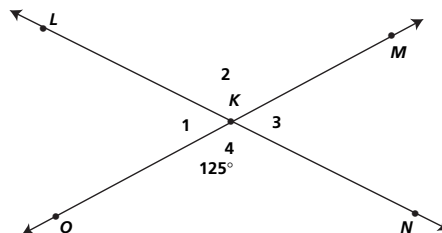
# Identifying and Classifying Angles

## EXAMPLE

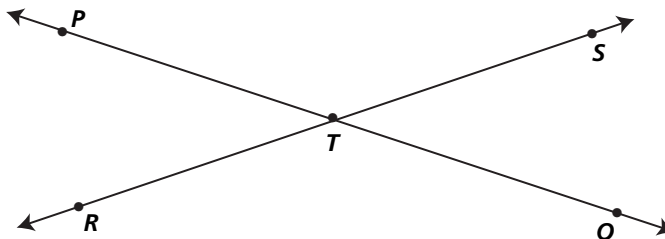
Name two angles adjacent to  $\angle LKO$ .  
Name the angle that is vertical to  $\angle 1$ .

$\angle OKN$  and  $\angle LKM$  are adjacent to  $\angle LKO$  because they have point  $K$  as their vertex and a common side ( $LK$  or  $OK$ ).

$\angle 1$  and  $\angle 3$  are vertical angles, because  $\angle 3$  is opposite  $\angle 1$ .



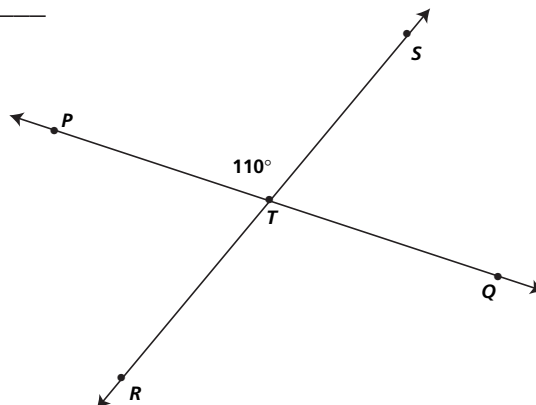
**Directions** Identify these angles.  
Write *adjacent*, *vertical*, *acute*, or *obtuse*. Some angles may have more than one description.



1.  $\angle PTS$  and  $\angle RTQ$  \_\_\_\_\_
2.  $\angle PTS$  and  $\angle STQ$  \_\_\_\_\_
3.  $\angle PTS$  \_\_\_\_\_
4.  $\angle PTR$  \_\_\_\_\_
5.  $\angle RTP$  and  $\angle PTS$  \_\_\_\_\_
6.  $\angle RTP$  and  $\angle STQ$  \_\_\_\_\_
7.  $\angle QTS$  \_\_\_\_\_
8.  $\angle RTQ$  \_\_\_\_\_

**Directions** Find the measures.

9.  $m\angle STQ$  \_\_\_\_\_
10.  $m\angle RTQ$  \_\_\_\_\_





# Complementary and Supplementary Angles

## EXAMPLE

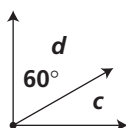
If the sum of the measures of two angles is  $90^\circ$ , the angles are complementary.

Angles  $c$  and  $d$  are complementary. Write an equation to find  $m\angle c$ .

$$m\angle c + 60^\circ = 90^\circ$$

$$m\angle c = 90^\circ - 60^\circ$$

$$m\angle c = 30^\circ$$



**Directions**  $\angle x$  and  $\angle y$  are complementary. Write an equation to find the measure of  $\angle y$ .

- $m\angle x = 50^\circ$  \_\_\_\_\_
- $m\angle x = 20^\circ$  \_\_\_\_\_
- $m\angle x = 45^\circ$  \_\_\_\_\_
- $m\angle x = 30^\circ$  \_\_\_\_\_

## EXAMPLE

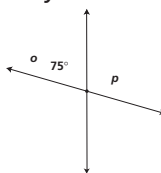
If the sum of the measures of two angles is  $180^\circ$ , the angles are supplementary.

Angles  $o$  and  $p$  are supplementary. Write an equation to find  $m\angle p$ .

$$m\angle p + 75^\circ = 180^\circ$$

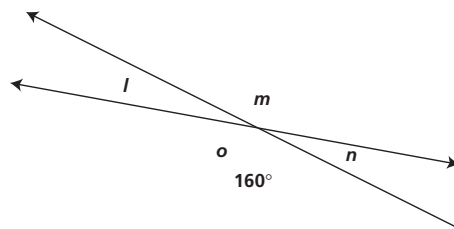
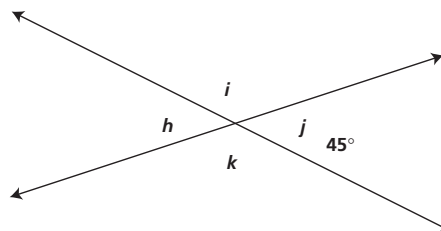
$$m\angle p = 180^\circ - 75^\circ$$

$$m\angle p = 105^\circ$$



**Directions** Find the measures.

- What is the measure of  $\angle h$ ? \_\_\_\_\_
- What is the measure of  $\angle k$ ? \_\_\_\_\_
- What is the measure of  $\angle i$ ? \_\_\_\_\_
- What is the measure of  $\angle m$ ? \_\_\_\_\_
- What is the measure of  $\angle l$ ? \_\_\_\_\_
- What is the measure of  $\angle n$ ? \_\_\_\_\_



# Angle Measure in a Triangle

**EXAMPLE**

Write an equation to find the missing measure.

$$m\angle KLM + 70^\circ = 180^\circ$$

$$m\angle KLM = 180^\circ - 70^\circ$$

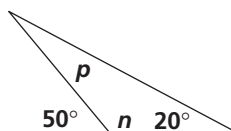
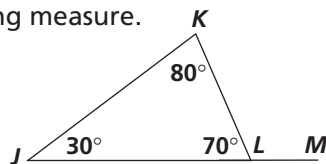
$$m\angle KLM = 110^\circ$$

Find  $m\angle p$ .

$$n = 180^\circ - 50^\circ$$

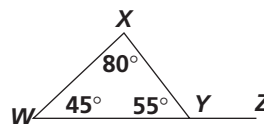
$$n = 130^\circ$$

$$130^\circ + 20^\circ + p = 180^\circ \quad p = 30^\circ$$

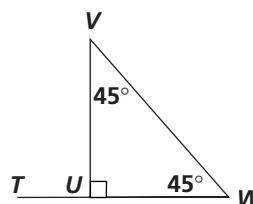


**Directions** Write an equation to find the missing measure.

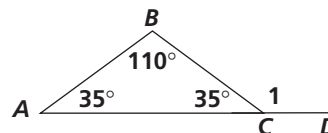
1.  $m\angle XYZ$  \_\_\_\_\_



2.  $m\angle TUV$  \_\_\_\_\_



3.  $m\angle 1$  \_\_\_\_\_



**Directions** Find the measures.

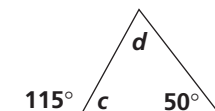
4.  $m\angle a$  \_\_\_\_\_

$m\angle b$  \_\_\_\_\_



5.  $m\angle c$  \_\_\_\_\_

$m\angle d$  \_\_\_\_\_

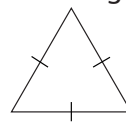


# Naming Triangles

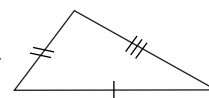
**EXAMPLE**

Tick marks show whether sides have the same or different lengths.

This triangle has 3 sides of the same length.

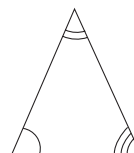


This triangle has sides of 3 different lengths.

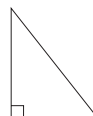


Arcs show whether angles are the same or different.

This triangle has angles with 3 different measures.

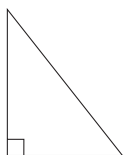


A square is used to show a  $90^\circ$  angle.



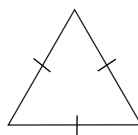
**Directions** Write the name of each triangle. Some triangles may have more than one name.

1.



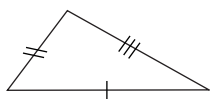
\_\_\_\_\_

2.



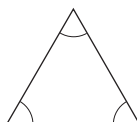
\_\_\_\_\_

3.



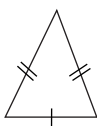
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4.



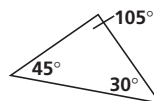
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5.



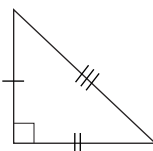
\_\_\_\_\_

6.



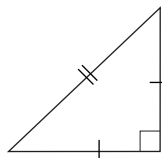
\_\_\_\_\_

7.



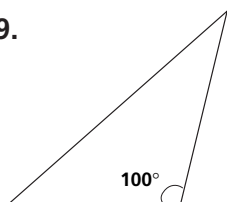
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8.



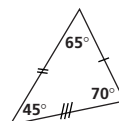
\_\_\_\_\_

9.



\_\_\_\_\_

10.



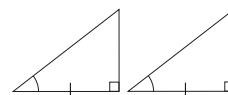
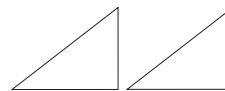
\_\_\_\_\_

# Congruent Triangles

**EXAMPLE**

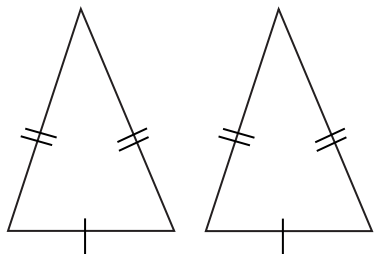
Are these 2 triangles congruent?  
Measure the sides and angles of both triangles.

Label the sides and angles that match. Because the triangles have 2 angles and an included side that are equal, they are congruent. (ASA)

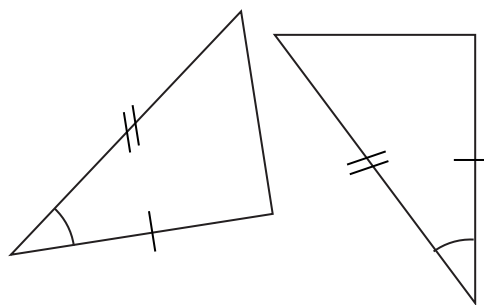


**Directions** Are the triangles in each pair congruent? Tell why or why not.

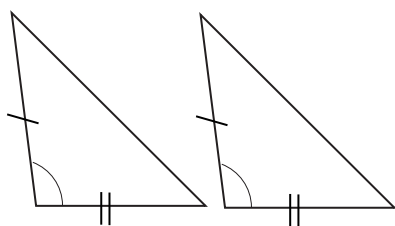
1.



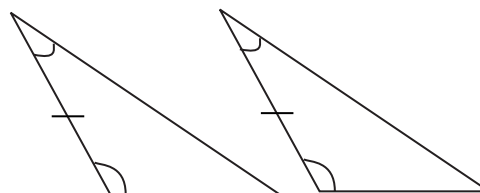
2.



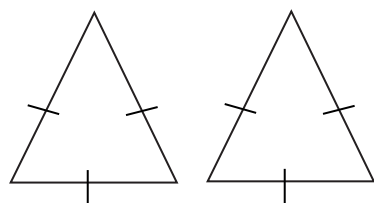
3.



4.



5.



# Similar Triangles

**EXAMPLE**

$\triangle PLM \sim \triangle PNO$ . Study the measurements given. Find  $m\angle N$  and  $m\angle L$ .  
Find the length of  $\overline{PO}$ .

**Step 1** The triangles are similar so the two angles will have the same measurement.

**Step 2**  $m\angle L + 75^\circ + 45^\circ = 180^\circ$

$$m\angle L = 180^\circ - 75^\circ - 45^\circ$$

$$m\angle L = 60^\circ$$

$$m\angle N = 60^\circ$$

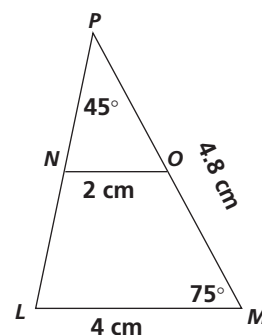
**Step 3** The triangles are similar so the corresponding sides form equal ratios.

**Step 4**  $\frac{LM}{NO} = \frac{PM}{PO}$

$$\frac{4}{2} = \frac{4.8}{PO}$$

$$PO = 4.8\left(\frac{2}{4}\right)$$

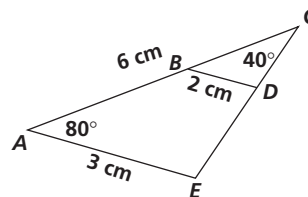
$$PO = 2.4 \text{ cm}$$



**Directions** Study the illustrations. Find the measures.

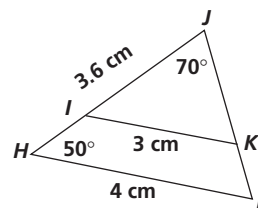
1.  $m\angle D$  \_\_\_\_\_

2.  $m$  of  $\overline{CB}$  \_\_\_\_\_

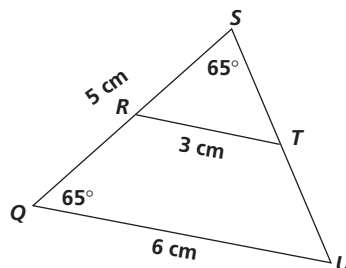


3.  $m\angle K$  \_\_\_\_\_

4.  $m$  of  $\overline{IJ}$  \_\_\_\_\_



5.  $m\angle T$  \_\_\_\_\_



# Parallelograms

**EXAMPLE**

Describe the properties of this quadrilateral. Then name it.

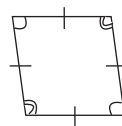
All sides are the same length.

It has 2 pairs of parallel sides.

The opposite sides are the same length.

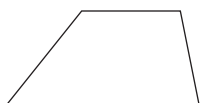
The opposite angles are equal.

It is a rhombus.



**Directions** Name 2 properties of each figure. Then name the figure.

1.



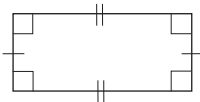
\_\_\_\_\_  
\_\_\_\_\_

2.



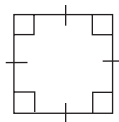
\_\_\_\_\_  
\_\_\_\_\_

3.



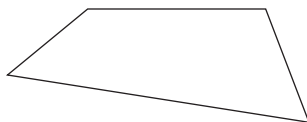
\_\_\_\_\_  
\_\_\_\_\_

4.



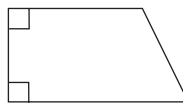
\_\_\_\_\_  
\_\_\_\_\_

5.



\_\_\_\_\_  
\_\_\_\_\_

6.



\_\_\_\_\_  
\_\_\_\_\_

**Directions** Tell whether each statement is *true* or *false*.

7. A rhombus is also a parallelogram. \_\_\_\_\_

8. A parallelogram is also a quadrilateral. \_\_\_\_\_

9. A trapezoid is also a rhombus. \_\_\_\_\_

10. A square is also a rectangle. \_\_\_\_\_

# Quadrilaterals and Diagonals

## EXAMPLE

Use the Pythagorean theorem to find the length of the diagonal.  
Use a scientific calculator and round your answer to the nearest hundredth.

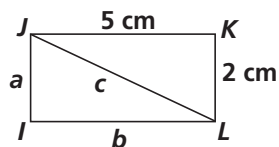
$$a^2 + b^2 = c^2$$

$$2^2 + 5^2 = c^2$$

$$4 + 25 = c^2$$

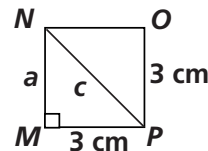
$$\sqrt{29} = c$$

$$5.39 = c$$

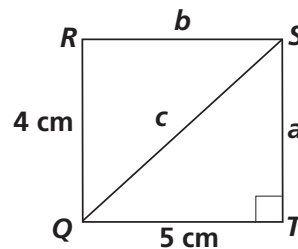


**Directions** Answer the questions about these rectangles. Use a scientific calculator and round your answer to the nearest hundredth.

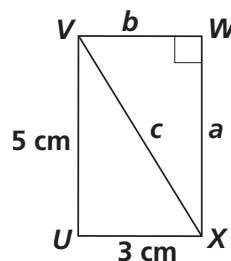
- What is the length of  $MN$ ? \_\_\_\_\_
- Use the Pythagorean theorem to find  $c$ . \_\_\_\_\_
- Is  $\triangle NMP$  congruent to  $\triangle NPO$ ? \_\_\_\_\_



- What is the  $m\angle R$ ? Explain. \_\_\_\_\_  
\_\_\_\_\_
- What is the length of  $ST$ ? \_\_\_\_\_
- Find the length of  $SQ$ . \_\_\_\_\_
- What would be the length of  $RT$ ? \_\_\_\_\_



- What is the length of  $VW$ ? \_\_\_\_\_
- What is  $m\angle VUX$ ? \_\_\_\_\_
- Is  $\triangle VUX$  congruent to  $\triangle VXW$ ? \_\_\_\_\_



# Polygons and Diagonals

## EXAMPLE

Find the sum of the measures of the angles and the measure of each interior and exterior angle.

To find the sum of all the angle measures in a regular hexagon:

$$(6 - 2)180^\circ = a$$

$$(4)180^\circ = a$$

$$720^\circ = a$$

To find the measure of each interior angle:

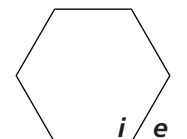
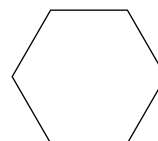
$$\frac{720^\circ}{6} = 120^\circ$$

To find the measure of each exterior angle:

$$120^\circ + e = 180^\circ$$

$$e = 180^\circ - 120^\circ$$

$$e = 60^\circ$$



**Directions** Find the measures of these regular polygons.

1.  $m\angle 6$

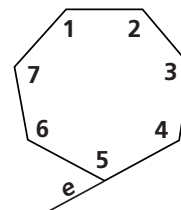
\_\_\_\_\_

2.  $m\angle e$

\_\_\_\_\_

3. The sum of all interior angles

\_\_\_\_\_

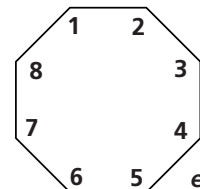


4.  $m\angle 8$

\_\_\_\_\_

5.  $m\angle e$

\_\_\_\_\_



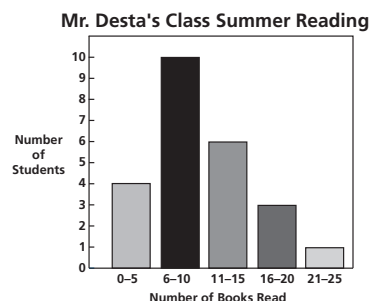


# Bar Graphs

**EXAMPLE**

A bar graph uses rectangular bars to organize and display data. It is made up of these individual parts:

- a title
- a horizontal axis with labels
- a vertical axis with labels
- an interval
- data



**Directions** Suppose you were asked to construct a bar graph that organizes and displays the data shown in this table. The table shows the results of a class election for president.

Election Results	
Candidate A	10 votes
Candidate B	12 votes
Candidate C	4 votes

1. What title would you choose for the bar graph?

\_\_\_\_\_

2. What label would you choose for the horizontal axis?

\_\_\_\_\_

3. What label would you choose for the vertical axis?

\_\_\_\_\_

4. What interval would you use? Explain.

\_\_\_\_\_

5. Use your answers from problems 1–4 to construct a bar graph for the data on your own paper.

# Circle Graphs

**EXAMPLE**

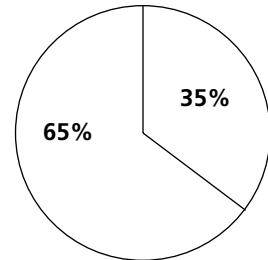
A circle graph uses parts of a circle to organize and display data.

The part of this graph labeled 65% makes up  $234^\circ$  of the graph because  $65\%$  of  $360^\circ = 0.65 \cdot 360^\circ = 234^\circ$ .

The part of this graph labeled 35% makes up  $126^\circ$  of the graph because  $35\%$  of  $360^\circ = 0.35 \cdot 360^\circ = 126^\circ$ .

You can check your work by finding the sum of the parts.

$$234^\circ + 126^\circ = 360^\circ \quad \checkmark$$



**Directions** Study this circle graph. Answer the questions that follow.

1. Name the fraction in simplest form, the decimal, and the number of degrees that represent Part A of the graph.

\_\_\_\_\_

2. Name the fraction in simplest form, the decimal, and the number of degrees that represent Part B of the graph.

\_\_\_\_\_

3. Name the fraction in simplest form, the decimal, and the number of degrees that represent Part C of the graph.

\_\_\_\_\_

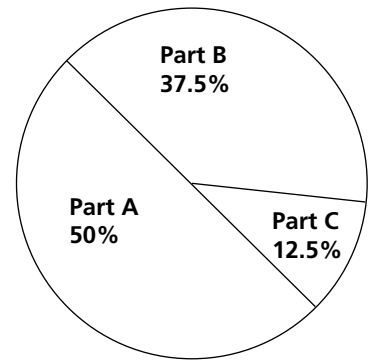
4. Describe how a circle graph can be checked for accuracy.

\_\_\_\_\_

\_\_\_\_\_

5. In the graph, suppose that Part A represents 500 votes. How many votes altogether are represented by the graph?

\_\_\_\_\_



# Frequency Tables

## EXAMPLE

Suppose two 1–6 number cubes are tossed at the same time and the outcomes of the cubes are added to create a sum.

For example, if the outcome on the first cube is 3 and the outcome on the second cube is 4, the sum of the outcomes is  $3 + 4$  or 7.

This frequency table shows the number of different ways various sums can be made by tossing two 1–6 number cubes.

Outcome Sum	Tally	Frequency
2		1
3		2
4		3
5		4
6	+	5
7	+	6
8	+	5
9		4
10		3
11		2
12		1

**Directions** Answer these questions about the frequency table in the example.

- What is the greatest possible sum that can be created by tossing two 1–6 number cubes? Explain how that sum can be created.  
\_\_\_\_\_
- What is the least possible sum that can be created by tossing two 1–6 number cubes? Explain how that sum can be created.  
\_\_\_\_\_
- How many tosses of the number cubes are shown in the data? Tell how you know.  
\_\_\_\_\_
- Based on the data, which sum will occur most often when two 1–6 number cubes are tossed? Which sums will occur least often?  
\_\_\_\_\_
- What interval was used to create this frequency table? Is there a better interval that could have been used? Explain.  
\_\_\_\_\_

# Mean

**EXAMPLE**

Study the data shown in the table. The data show the average amount of precipitation received each month in Miami, Florida.

Month	Precipitation in Inches	Month	Precipitation in Inches
January	2.0	July	5.7
February	2.1	August	7.6
March	2.4	September	7.6
April	2.9	October	5.6
May	6.2	November	2.7
June	9.3	December	1.8

To find the mean of a set of data, find the sum of the data values in the set, then divide by the number of data values.

**Directions** Answer these questions about the data table in the example.

1. What useful information do the labels in the table provide?

\_\_\_\_\_

2. How many data values does the set of data contain? \_\_\_\_\_

3. What is the sum of the data values? \_\_\_\_\_

4. Identify the steps to follow to determine the mean of the set of data.

\_\_\_\_\_

\_\_\_\_\_

5. What is the mean amount of precipitation received each month in Miami, Florida? Round your answer to the nearest hundredth inch.

\_\_\_\_\_

# Median

**EXAMPLE**

Study the data shown in the table.  
The data show the inauguration ages  
of some U.S. presidents.

The median of a set of data is the middle  
value when the set is ordered from greatest  
to least or least to greatest. To find the mean  
of a set of data, order the values in the set  
from greatest to least or least to greatest.  
Cross off the greatest and least values in the set.  
The median is the middle data value, or the  
mean of the two middle values.

President	Inauguration Age (in years)
Washington	57
Jefferson	57
Lincoln	52
Harrison	55
Cleveland	55
McKinley	54
Wilson	56
Hoover	54
L. Johnson	55
Carter	52

**Directions** Answer these questions about the data table in the example.

1. Order the data values from greatest to least or from least to greatest.

---

2. Does the set of data have an even number or an odd number of data values?

---

3. How is finding the median of a data set with an even number of values different from finding the median of a data set with an odd number of values?

---

---

4. What is the median inauguration age of the presidents shown in the table?

---

5. President Bill Clinton was 46 years old at inauguration, and President Truman was 60 years old. Suppose these two presidents were added to the table. Would the median change? If so, to what?

---

# Mode

**EXAMPLE**

Study the data shown in the table.  
The data show elevation in feet  
above sea level of selected U.S. cities.

The mode of a set of data is the value  
or values that occur most often. To  
determine the mode of a set of data,  
count the number of times each value  
appears. The value or values that appear  
most often are the mode.

City	Elevation Above Sea Level (in feet)
San Diego, CA	20
Bellingham, WA	60
Galveston, TX	5
Cambridge, MA	20
Orlando, FL	70
Wilmington, NC	35
New Haven, CT	40
Baltimore, MD	20
Key West, FL	5
Albany, NY	20

**Directions** Answer these questions about the data table in the example.

1. What useful information do the labels in the table provide?

---

2. How many different data values appear in the table? What are those values?

---

3. How could you determine the mode of the data?

---

4. What is the mode of the data?

---

5. Suppose each value in a set of data occurs the same number of times.  
What is the mode of the set of data?

---

## Range

**EXAMPLE**

Study the data shown in the table.  
The data show the lengths in miles  
of selected rivers in North America.

The range of a set of data is the  
difference between the greatest  
and least values.

River	Length (miles)
Missouri	2,315
Kentucky	259
Arkansas	1,459
Milk	625
Porcupine	569
Snake	1,038
Mississippi	2,340
White	722
Yukon	1,979
Pecos	926

**Directions** Answer these questions about the data table in the example.

1. What is the longest river shown in the table? What is its length?

---

2. What is the shortest river shown in the table? What is its length?

---

3. How could you determine the range of the data?

---

4. What is the range of the data?

---

5. In order to find the range of a set of data, is it necessary to order data in a set  
from greatest to least or from least to greatest? Explain.

---

---

## Data and Statistics

**EXAMPLE**

Study the data shown in this table. The data show the locations and heights in feet of famous waterfalls.

Waterfall	Location	Height (in feet)
Panther	Alberta, Canada	600
Multnomah	Oregon, U.S.	620
Augrabies	South Africa	480
Feather	California, U.S.	640
Marina	Guyana	500
Bridalveil	Yosemite National Park, U.S.	620

**Directions** Answer these questions about the data table in the example.

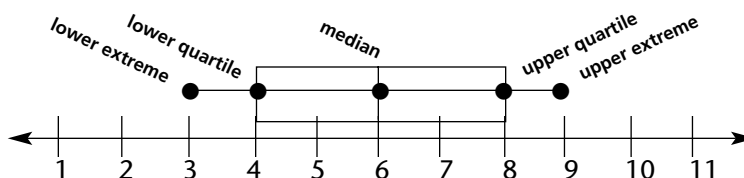
1. What data are represented in the table? \_\_\_\_\_
2. How many data values does the table display? \_\_\_\_\_
3. Suppose you were asked to display the data using a bar graph. What interval would you use? Explain.  
\_\_\_\_\_
4. When should you break the vertical axis of a bar graph? Explain.  
\_\_\_\_\_
5. Would it be easy or difficult to display the waterfall data in a circle graph? Tell why.  
\_\_\_\_\_
6. Is a frequency table the best way to organize and display the data in the table? Tell why or why not.  
\_\_\_\_\_
7. Find the mean of the data. Round your answer to the nearest whole number. \_\_\_\_\_
8. Find the median of the data. \_\_\_\_\_
9. Find the mode of the data. \_\_\_\_\_
10. Find the range of the data. \_\_\_\_\_



## Box-and-Whiskers Plots

**EXAMPLE**

Study the data shown in this box-and-whiskers plot.



To construct a box-and-whiskers plot:

- Find the median of the entire set of data. Label this value *median*.
- Find the median of all values below the median. Label this value *lower quartile*.
- Find the median of all values above the median. Label this value *upper quartile*.
- Find the least value in the set of data. Label this value *lower extreme*.
- Find the greatest value in the set of data. Label this value *upper extreme*.

**Directions** Use the set of data shown below for problems 1–5.

{16 19 11 23 15 18 22 17 10 12 21}

1. Order the data in the set from greatest to least or from least to greatest.

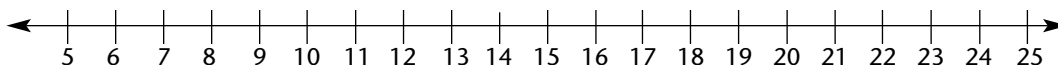
\_\_\_\_\_

2. What is the median of the set of data? \_\_\_\_\_

3. What value represents the lower quartile? \_\_\_\_\_ The upper quartile? \_\_\_\_\_

4. What value represents the lower extreme? \_\_\_\_\_ The upper extreme? \_\_\_\_\_

5. Construct a box-and-whiskers plot of the data using this number line.



# The Probability Fraction

## EXAMPLE

Consider the frequency table that shows the number of different ways various sums can be made by tossing two 1–6 number cubes.

When two 1–6 number cubes are tossed at the same time, 36 different outcomes are possible.

Outcome Sum	Tally	Frequency
2		1
3		2
4		3
5		4
6	+	5
7	+	6
8	+	5
9		4
10		3
11		2
12		1

**Directions** Use the probability fraction  $P = \frac{\text{number of favorable outcomes}}{\text{number of possible outcomes}}$  and the frequency table to find each of the following probabilities. Whenever possible, express your answer in simplest form.

1.  $P(10)$  \_\_\_\_\_

5.  $P(\text{an even sum})$  \_\_\_\_\_

2.  $P(5)$  \_\_\_\_\_

6.  $P(\text{an odd sum})$  \_\_\_\_\_

3.  $P(3)$  \_\_\_\_\_

4.  $P(12)$  \_\_\_\_\_

7. Which outcome shown in the table is most likely? \_\_\_\_\_

8. Which outcomes are least likely? \_\_\_\_\_

9. Which outcome is twice as likely as an outcome of 4? \_\_\_\_\_

Which outcomes are  $\frac{1}{3}$  as likely as an outcome of 7? \_\_\_\_\_

10. Some board games require a player to roll two number cubes. How might knowing the probability of which sums are more likely to occur help you become a better board game player?

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# The Fundamental Principle of Counting

## EXAMPLE

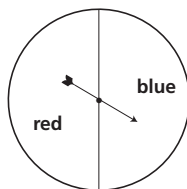
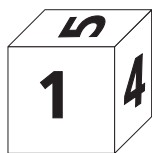
These combinations show all of the different ways the letters *a*, *b*, and *c* can be arranged if the letters cannot be used more than once in any arrangement.

*abc acb bac bca cab cba*

Another way to determine the number of different ways the letters can be arranged is to use the fundamental principle of counting. It states that three letters can be arranged  $3 \cdot 2 \cdot 1$  or 6 different ways.

**Directions** Use the fundamental principle of counting or draw a diagram to determine the number of arrangements in each of the following problems.

- How many different ways can two students seat themselves in two chairs? \_\_\_\_\_
- How many different four-digit whole numbers can be made using the digits 1, 3, 5, and 7 if the digits can appear only once in each number? \_\_\_\_\_
- Angela is choosing a skirt and a blouse to wear from five skirts and four blouses. How many different combinations of one skirt and one blouse does Angela have to choose from? \_\_\_\_\_
- Suppose the 1–6 number cube and the spinner shown below are each used once. How many different outcomes are possible? \_\_\_\_\_



- How many different three-digit numbers are possible when each spinner shown below is spun once? The left spinner will provide the first digit of the number, the center spinner will provide the second digit, and the right spinner will provide the third digit. \_\_\_\_\_

