Bayesian anomaly detection

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Will Handley group meeting

What is anomaly detection useful for?

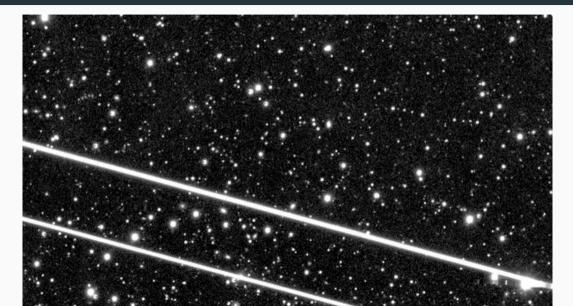
1. Contamination

• Simultaneously detecting and mitigating contaminated data.

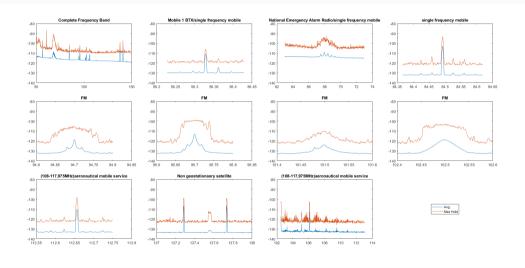
2. Anomalies

 Radio transients, cosmic ray flares, GW signals etc.)

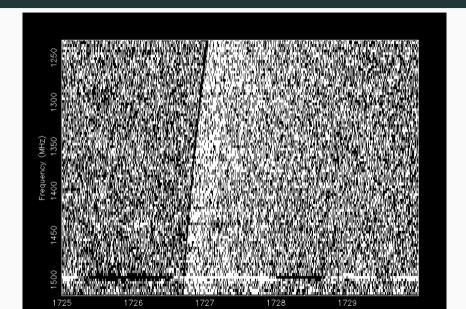
Contaminated data



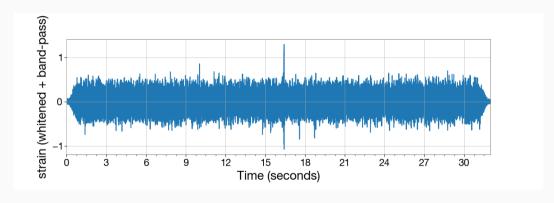
Contaminated data on the REACH site



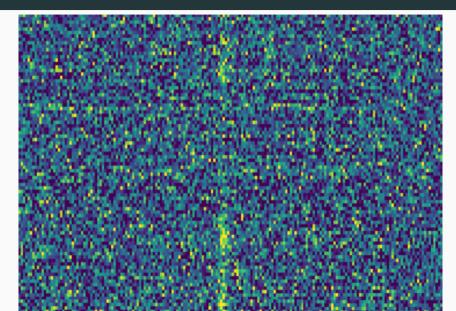
Anomalies - FRB 1



Anomalies (GW150914)



What do(nt) we look for?



7

Defining an anomaly sensitive likelihood

a) Generate new likelihood:

$$P(\mathcal{D}_i|\theta) = \begin{cases} \mathcal{L}_i(\theta) & : \text{ expected} \\ \Delta^{-1}[0 < \mathcal{D}_i < \Delta] & : \text{ anomalous,} \end{cases}$$
 (1)

b) Ascribe Bernoulli prior:

$$P(\varepsilon_i) = p_i^{(1-\varepsilon_i)} (1-p_i)^{\varepsilon_i}. \tag{2}$$

c) Marginalise over epsilon:

$$P(\mathcal{D}|\theta) = \sum_{\varepsilon \in \{0,1\}^N} P(\mathcal{D}, \varepsilon|\theta)$$
(3)

d) Approximate correct mask is most likely

$$P(\mathcal{D}|\theta, \varepsilon_{\max}) \gg \max_{j} P(\mathcal{D}|\theta, \varepsilon^{(j)}),$$
 (4)

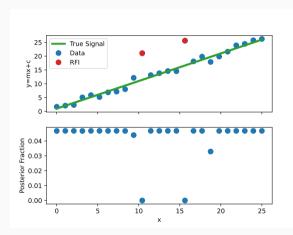
d) Loglikelihood:

$$\log P(\mathcal{D}|\theta) = \sum_{i} [\log \mathcal{L}_{i} + \log(1 - p_{i})] \varepsilon_{i}^{\max} + [\log p_{i} - \log \Delta] (1 - \varepsilon_{i}^{\max})$$
 (5)

Visualising on a simple toy model

Using numerical sampling techniques to make predictions with \mathcal{L} .

 This computes the fraction of posterior believed to 'fit' model given the data.

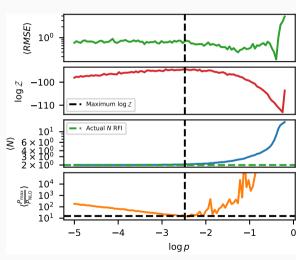


Probability thresholding condition p

$$\log P(\mathcal{D}|\theta) = \sum_{i} [\log \mathcal{L}_{i} + \log(1 - p_{i})] \varepsilon^{\max} + [\log p_{i} - \log \Delta] (1 - \varepsilon_{i}^{\max}), \tag{6}$$

Selection strategy for p.

• 'Select *p* such that the Bayesian evidence is maximised'



Fully automated anomaly detection

- ullet Putting a prior on p, we can fit it dynamically as a free parameter.
- This fully automates the anomaly detection process.

Implement with 2 lines of code

```
41
42 def likelihood(theta):
43
     sig = theta[0]
       logL = -(f_noise - window)**2/sig**2/2 - np.log(2*np.pi*sig**2)/2
44
45
        return logL, []
46
35 def likelihood(theta):
       sig = theta[0]
       logL = -(f_noise - window)**2/sig**2/2 - np.log(2*np.pi*sig**2)/2 + np.log(1-p)
38
       emax = logL > logp - np.log(delta)
39
       logPmax = np.where(emax, logL, logp - np.log(delta)).sum()
40
       return logPmax, []
47
```

Tutorial @ github.com/samleeney

Read the paper!

PHYSICAL REVIEW D 108, 062006 (2023)

Bayesian approach to radio frequency interference mitigation

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(Received 5 May 2023; accepted 29 August 2023; published 29 September 2023)

Interfering signals such as radio frequency interference from ubiquitous satellite constellations are becoming an endemic problem in fields involving physical observations of the electromagnetic spectrum. To address this we propose a novel data cleaning methodology. Contamination is simultaneously flagged and managed at the likelihood level. It is modeled in a Bayesian fashion through a piecewise likelihood that is constrained by a Bernoulli prior distribution. The techniques described in this paper can be implemented with just a few lines of code.

DOI: 10.1103/PhysRevD.108.062006

arxiv: 2211.15448

Time sensitive anomaly detection

Time sensitive likelihood

• Likelihood from before is extended into two dimensions, becoming

$$\log \mathcal{L}\left(heta
ight) = \sum_{ij} \left[\log \mathcal{L}_{ij}\left(heta
ight) + \log \left(1 -
ho_{ij}
ight)
ight] \epsilon_{ij} +$$

$$[\log p_{ij} - \log \Delta] (1 - \epsilon_{ij}) \quad (7)$$

Time sensitive likelihood

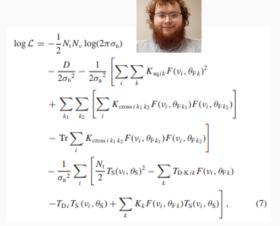
• Computation time of the likelihood grows linearly with the number of time bins used in the data set.

$$\log \mathcal{L}\left(heta
ight) = \sum_{ij} \left[\log \mathcal{L}_{ij}\left(heta
ight) + \log\left(1 - p_{ij}
ight)
ight] \epsilon_{ij} +$$

$$[\log p_{ij} - \log \Delta] (1 - \epsilon_{ij}) \quad (8)$$

Speeding up

- Anstey proposes a solution to this problem in [Anstey et al., 2023].
- Common model per time bin is fit jointly.
- Speeds up fit but not sensitive to transients.

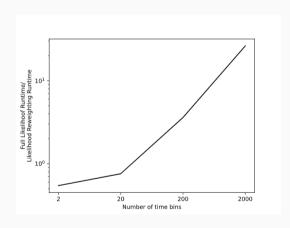


Likelihood reweighting

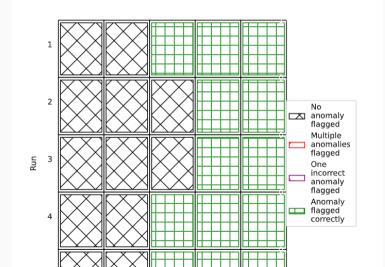
- Introduced in context of gravitational waves
 by [Payne et al., 2019] [Romero-Shaw et al., 2019].
- Bayesian sampling techniques spend lots of time at tails of distribution.
- Reweighting is essentially a course then fine search, using a simple (fast) then complex (slow) likelihood.

How does this help us?

- We can use the fast method for a coarse scan.
- Then the slower method for refined scan.
- Increases speed massively for larger problems.



Testing on a simple toy example



Read the paper!

Enhanced Bayesian RFI Mitigation and Transient Flagging Using Likelihood Reweighting

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ABSTRACT

Contamination by Radio Frequency Interference (RFI) is a ubiquitous challenge for radio astronomy. In particular, transient RFI is difficult to detect and avoid, especially in large data sets with many time bins. In this work, we present a Bayesian methodology for time-dependent, transient anomaly mitigation. In general, the computation time for correcting for transient anomalies in time-separated data sets grows proportionally with the number of time bins. We demonstrate that utilising likelihood reweighting can allow our Bayesian anomaly mitigation method to be performed with a computation time close to independent of the number of time bins. In particular, we identify a factor of 25 improvement in computation time for a test case with 2000 time bins. We also demonstrate how this method enables the flagging this bin because the strength of the stre

Key words: methods: data analysis - radio continuum: transients

arxiv: 2310.02146

Conclusions

- Fast scans of old data hopefully find something new!
- 2 lines of code to implement into existing Bayesian systems
- Colaborate with us!



Scan the QR code for the slides or to

contact mal

References

Anstey, D., de Lera Acedo, E., and Handley, W. (2023).

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Romero-Shaw, I. M., Lasky, P. D., and Thrane, E. (2019).

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