

# Todo list

■ <b>Important:</b> Lay abstract. . . . .	iii
■ <b>Important:</b> Abstract. . . . .	iv
■ <b>Important:</b> Acknowledgements. . . . .	v
■ <b>Important:</b> Replace reading notes. . . . .	xii
■ <b>Important:</b> Declaration of Academic Achievement. . . . .	xiii
■ <i>Easy:</i> Such as this one, but check out Section 2.4 for more options. . . .	3
■ <b>Important:</b> “Important” notes. . . . .	6
■ Generic inlined notes. . . . .	6
■ <i>Later:</i> TODO notes for later! For finishing touches, etc. . . . .	6
■ <i>Easy:</i> Easier notes. . . . .	6
■ <i>Needs time:</i> Tedious notes. . . . .	6
■ <b>Q #1:</b> Questions I might have? . . . . .	6
■ investigate more: Steele 1990? . . . . .	7
■ get original source from Czarnecki and Eisenecker 2000 . . . . .	10
■ clarify what “free-form source code generation” means . . . . .	10
■ Investigate . . . . .	11
■ Investigate? . . . . .	11
■ should I change this if it’s British English? . . . . .	19
■ Add example . . . . .	20
■ Add source(s)? . . . . .	20
■ Investigate . . . . .	22
■ Describe anyway . . . . .	22
■ Investigate . . . . .	26
■ Do this! . . . . .	27
■ Find formal description of unit, integration, and system testing . . . . .	29
■ add source? . . . . .	30
■ Is this sufficient? . . . . .	31
■ add original source: KA85 . . . . .	32
■ Investigate . . . . .	33
■ Should I include the definition of <b>Constraints</b> ? . . . . .	37
■ cite Dr. Smith . . . . .	37
■ add refs to ‘underlying Theory’ comment and ‘not all outputs be IMs’ comment . . . . .	37
■ add constraints . . . . .	37

## THE GENERATION OF TEST CASES IN DRASIL

# THE GENERATION OF TEST CASES IN DRASIL

By SAMUEL CRAWFORD, B.Eng.

A THESIS  
SUBMITTED TO THE DEPARTMENT OF COMPUTING AND SOFTWARE  
AND THE SCHOOL OF GRADUATE STUDIES  
OF MCMASTER UNIVERSITY  
IN PARTIAL FULFILLMENT OF THE REQUIREMENTS  
FOR THE DEGREE OF  
MASTER OF APPLIED SCIENCE

Master of Applied Science (2023)  
(Department of Computing and Software)

McMaster University  
Hamilton, Ontario

TITLE: The Generation of Test Cases in Drasil  
AUTHOR: Samuel Crawford, B.Eng.  
SUPERVISOR: Dr. Carette and Dr. Smith  
PAGES: **xiii, 41**

# Lay Abstract

**Important:** Lay abstract.

# Abstract

**Important:** Abstract.

# Acknowledgements

**Important:** Acknowledgements.

# Contents

<b>Todo list</b>	<b>i</b>
<b>Lay Abstract</b>	<b>iii</b>
<b>Abstract</b>	<b>iv</b>
<b>Acknowledgements</b>	<b>v</b>
<b>Contents</b>	<b>vi</b>
<b>List of Figures</b>	<b>viii</b>
<b>List of Tables</b>	<b>ix</b>
<b>List of Source Codes</b>	<b>x</b>
<b>List of Abbreviations and Symbols</b>	<b>xi</b>
<b>Reading Notes</b>	<b>xii</b>
<b>Declaration of Academic Achievement</b>	<b>xiii</b>
<b>1 Introduction</b>	<b>1</b>
1.1 Template Organization . . . . .	1
1.2 Writing Tips . . . . .	2
1.3 Development Recommendations . . . . .	3
1.4 Troubleshooting . . . . .	4
<b>2 Extras</b>	<b>5</b>
2.1 Writing Directives . . . . .	5
2.2 HREFs . . . . .	5
2.3 Pseudocode Code Snippets . . . . .	6
2.4 TODOs . . . . .	6
<b>3 Notes</b>	<b>7</b>
3.1 A Survey of Metaprogramming Languages . . . . .	7
3.1.1 Definitions . . . . .	7
3.1.2 Metaprogramming Models . . . . .	8



3.1.3	Phase of Evaluation . . . . .	12
3.1.4	Metaprogram Source Location . . . . .	13
3.1.5	Relation to the Object Language . . . . .	14
3.2	Overview of Generative Software Development . . . . .	15
3.2.1	Definitions . . . . .	15
3.3	Structured Program Generation Techniques . . . . .	16
3.3.1	Techniques for Program Generation [4, p. 3-5] . . . . .	17
3.3.2	Kinds of Generator Safety [4, p. 5-8] . . . . .	17
3.3.3	Methods for Guaranteeing Fully Structured Generation [4, p. 8-20] . . . . .	17
3.4	Taxonomy of Fundamental Concepts of Meta-Programming . . . . .	18
3.4.1	Definitions . . . . .	18
3.4.2	Other Notes . . . . .	19
3.5	Roadblocks to Meta-Programming . . . . .	19
3.6	Roadblocks to Testing Scientific Software [5, p. 67] . . . . .	19
3.7	Software Metrics . . . . .	20
3.8	Software Testing . . . . .	20
3.8.1	Definitions . . . . .	20
3.8.2	General Testing Notes . . . . .	21
3.8.3	Static Black-Box (Specification) Testing [7, p. 56-62] . . . . .	22
3.8.4	Dynamic Black-Box (Behavioural) Testing [7, pp. 64-65] . . . . .	22
3.8.5	Static White-Box Testing (Structural Analysis) [7, pp. 91-104] . . . . .	27
3.8.6	Dynamic White-Box (Structural) Testing [7, p. 105-121] . . . . .	29
3.8.7	Regression Testing . . . . .	32
3.8.8	Metamorphic Testing (MT) . . . . .	33
<b>4</b>	<b>Development Process</b>	<b>35</b>
4.1	Improvements to Manual Test Code . . . . .	36
4.1.1	Testing with Mocks . . . . .	36
4.2	The Use of Assertions in Code . . . . .	37
4.3	Generating Requirements . . . . .	37
	<b>Bibliography</b>	<b>39</b>
	<b>Appendix</b>	<b>40</b>

# List of Figures

# List of Tables

1.1	Template Organization . . . . .	1
3.1	Types of Data Flow Coverage . . . . .	32

# List of Source Codes

2.1	Pseudocode: exWD . . . . .	5
2.2	Pseudocode: exPHref . . . . .	6
A.1	Tests for main with an invalid input file . . . . .	40
A.2	Projectile’s choice for constraint violation behaviour in code . . . . .	41
A.3	Projectile’s manually created input verification requirement . . . . .	41
A.4	“MultiDefinitions” (MultiDefn) Definition . . . . .	41
A.5	Pseudocode: Broken QuantityDict Chunk Retriever . . . . .	41

# List of Abbreviations and Symbols

<b>AOP</b>	Aspect-Oriented Programming
<b>AST</b>	Abstract Syntax Tree
<b>CSP</b>	Cross-Stage Persistence
<b>CTMP</b>	Compile-Time MetaProgramming
<b>DSL</b>	Domain-Specific Language
<b>GOOL</b>	Generic Object-Oriented Language
<b>HREF</b>	Hypertext REference
<b>IDE</b>	Integrated Development Environment
<b>MDD</b>	Model-Driven Development
<b>MOP</b>	MetaObject Protocol
<b>MR</b>	Metamorphic Relation
<b>MSL</b>	MultiStage Language
<b>MSP</b>	MultiStage Programming
<b>MT</b>	Metamorphic Testing
<b>PDF</b>	Portable Document Format
<b>PPTMP</b>	PreProcessing-Time MetaProgramming
<b>RTMP</b>	RunTime MetaProgramming
<b>SST</b>	Skeleton Syntax Tree
<b>C-use</b>	Computational Use
<b>DblPend</b>	Double Pendulum
<b>GamePhysics</b>	Game Physics
<b>P-use</b>	Predicate Use
<b>Projectile</b>	Projectile
<b>SglPend</b>	Single Pendulum
<b>SSP</b>	Slope Stability analysis Program
<b>V&amp;V</b>	Verification and Validation

# Reading Notes

Before reading this thesis, I encourage you to read through these notes, keeping them in mind while reading.

- The source code of this thesis is [publicly available](#).
- This thesis template is primarily intended for usage by the computer science community<sup>1</sup>. However, anyone is free to use it.
- I’ve tried my best to make this template conform to the thesis requirements as per [those set forth in 2021 by McMaster University](#). However, you should double-check that your usage of this template is compliant with whatever the “current” rules are.

**Important:** Replace reading notes.

---

<sup>1</sup>Hence why there are some  $\text{\LaTeX}$  macros for “code” snippets.

# Declaration of Academic Achievement

**Important:** Declaration of Academic Achievement.

# Chapter 1

## Introduction

Congratulations! If you're seeing this, it means you've managed to compile the PDF, which also means you can get started on typesetting your thesis<sup>1</sup>.

This template is adapted from my [thesis](#). If you'd like to see an example of this template in practice, please feel free to use my thesis as an example.

### 1.1 Template Organization

I've broken up the template according to my preferred organization: chapters in separate files, various kinds of assets (images, tables, code snippets, macros, etc.) in separate files, etc. The split is approximately according to [Table 1.1](#).

Table 1.1: Template Organization

File/Folder	Intended Usage & Description
<code>thesis.tex</code>	Focal $\text{\LaTeX}$ file that collects everything and is used to build your thesis/report document.
<code>Makefile</code>	A basic <code>Makefile</code> configuration. See <code>make help</code> for a list of helpful commands.
<code>build/</code>	When you build your PDF, this folder is used as the working directory of LuaLaTeX. Using this allows us to quickly get rid of $\text{\LaTeX}$ build files that can cause problems when we re-build documents.
<code>manifest.tex</code>	Basic options that you should certainly configure according to your needs.
<code>chapters.tex</code>	All chapters of your thesis should be included here.

---

<sup>1</sup>Or report or ...



<code>chapters/</code>	Enumeration of the chapters of your thesis. I prefer using a two-digit indexing pattern for the prefix of file names so that I can quickly open up by chapter number using VS Codium.
<code>assets.tex</code>	Enumeration of the various kinds of “assets” in the <code>assets/</code> folder. See the file for examples on how you can write your extra utility macros.
<code>assets/</code>	Enumeration of various kinds of “assets,” with subdirectories for images and figures, tables, and code snippets.
<code>front.tex</code>	All front matter of your thesis should be included here.
<code>front/</code>	Enumeration of the front chapters of your thesis. These chapters should all be numbered using Roman numerals.
<code>back.tex</code>	All back matter of your thesis should be included here.
<code>back/</code>	Enumeration of the back matter content.
<code>acronyms.tex</code>	List of acronyms you intend to use in your thesis. This uses the “acro” $\LaTeX$ package.
<code>macros.tex</code>	Helpful macros!
<code>unicode_chars.tex</code>	At times, you might find issues with unicode characters, especially in verbatim environments, where you might need to manually define them using other font glyphs.
<code>mcmaster_colours.tex</code>	Macros for the McMaster colour palette.
<code>README.md</code>	Read it!
<code>.gitignore</code>	List of files in the working directory that should be ignored by git.
<code>latexmkrc</code>	Used for setting the timezone for latexmk, but can be used for other options.

## 1.2 Writing Tips

When drafting chapters, I:

1. wrote “writing directives” for each chapter to understand what I need to write about (see [Section 2.1](#)),
2. wrote “todo” notes for tedious things that I might want to do later (such as citations, figures, code snippets, etc., see [Section 2.4](#)), and

3. regularly built my thesis using `make debug` to make sure that whatever I wrote didn't break the  $\text{\LaTeX}$  code.

For workflow recommendations, you should speak with your supervisor as they might prefer you work in a specific way with them.

## 1.3 Development Recommendations

Other than the basic tools I used for this template, I enjoyed using the following tools while writing my thesis:

1. **VS Codium**/**VS Code**<sup>2</sup> with the following extensions:
  - (a)  **$\text{\LaTeX}$  Workshop**, for  $\text{\LaTeX}$  syntax highlighting, code formatting (this is highly recommended), and code completion,
  - (b) **LT $\text{\TeX}$  - LanguageTool grammar/spell checking**, for grammar checking using **LanguageTool**, and
  - (c) **Todo Tree**, for quickly listing all of my TODO notes in my IDE (in addition to the list at the top of the PDF).
2. **texcount** (which should come with your  $\text{\LaTeX}$  installation) to quickly check the word count of individual  $\text{\LaTeX}$  files, and
3. **Zotero** for collecting my references and quickly exporting bib entries that I could use.

In particular, when writing, I found it particularly helpful to use VS Code's "Zen Mode" (to see your keybind, press **CTRL+ALT+P** and search for "Zen"), which enters a stripped-down full-screen version of the current working file, keeping your eyes purely focused on the document in front of you. Being comfortable with the keybinds is particularly helpful for working effectively in this setup. For example, I found the following<sup>3</sup> to be helpful: **CTRL+TAB** and **CTRL+SHIFT+TAB** to scroll between open files, **CTRL+P** to quickly open up recent files, **CTRL+ALT+P** to run commands you forgot the keybind for, **CTRL+O** to open up files out of the current working directory.

While writing, I enjoyed:

1. using "TODO" notes

*Easy:* Such as this one, but check out [Section 2.4](#) for more options.

to collect notes that I would want to do later,

2. formatting the  $\text{\LaTeX}$  code to make it easier to read (the  $\text{\LaTeX}$  Workshop plugin has functionality for this),

---

<sup>2</sup>I prefer VS Codium simply because I prefer libre software.

<sup>3</sup>If you're not using Linux, I cannot guarantee that these will be the same for you, so you should use **CTRL+ALT+P** to look for your appropriate bound keybinds.

3. breaking the non-textual content into separate files and “include”-ing them in the  $\text{\LaTeX}$  code so that they didn’t cause large visual interruptions,
4. using git to version control copies of my thesis, chapters, etc.,
5. using [TikZ](#) and [draw.io/diagrams.net](#) to build graphics and diagrams, and
6. building the thesis often using `make debug` to quickly debug issues in the written code.

## 1.4 Troubleshooting

“StackOverflow” is a great area to look for solutions to common  $\text{\LaTeX}$  issues. Otherwise, feel free to use create a ticket or sending an email to me.

# Chapter 2

## Extras

### Writing Directives

- What macros do I want the reader to know about?

### 2.1 Writing Directives

I enjoy writing directives (mostly questions) to navigate what I should be writing about in each chapter. You can do this using:

Source Code 2.1: Pseudocode: exWD

---

```
\begin{writingdirectives}
  \item What macros do I want the reader to know about?
\end{writingdirectives}
```

---

Personally, I put them at the top of chapter files, just after chapter declarations.

### 2.2 HREFs

For PDFs, we have (at least) 2 ways of viewing them: on our computers, and printed out on paper. If you choose to view through your computer, reading links (as they are linked in this example, inlined everywhere with “clickable” links) is fine. However, if you choose to read it on printed paper, you will find trouble clicking on those same links. To mitigate this issue, I built the “porthref” macro (see `macros.tex` for the definition) to build links that appear as clickable text when “compiling for computer-focused reading,” and adds links to footnotes when “compiling for printing-focused reading.” There is an option (`compilingforprinting`) in the `manifest.tex` file that controls whether PDF builds should be done for

computers or for printers. For example, by default, **McMaster** is made with clickable functionality, but if you change the `manifest.tex` option as mentioned, then you will see the link in a footnote (try it out!).

Source Code 2.2: Pseudocode: `exPHref`

---

```
\porthref{McMaster}{https://www.mcmaster.ca/}
```

---

## 2.3 Pseudocode Code Snippets

For pseudocode, you can also use the pseudocode environment, such as that used in [Source Code A.5](#).

## 2.4 TODOs

While writing, I plastered my thesis with notes for future work because, for whatever reason, I just didn't want to, or wasn't able to, do said work at that time. To help me sort out my notes, I used the `todonotes` [package](#) with a few extra macros (defined in `macros.tex`). For example,...

Important notes:

**Important:** “Important” notes.

Generic inlined notes:

**Generic inlined notes.**

Notes for later:

Some “easy” notes:

*Easy:* Easier notes.

Tedious work:

*Needs time:* Tedious notes.

Questions:

*Later:* TODO notes for later! For finishing touches, etc.

**Q #1:** Questions I might have?

# Chapter 3

## Notes

### 3.1 A Survey of Metaprogramming Languages

investigate more:  
Steele 1990?

- Often done with Abstract Syntax Trees (ASTs), although other bases are used:
  - Skeleton Syntax Trees (SSTs), used by Dylan [1, p. 113:6]
- Allows for improvements in:
  - “performance by generating efficient specialized programs based on specifications instead of using generic but inefficient programs” [1, p. 113:2]
  - reasoning about object programs through “analyzing and discovering object-program characteristics that enable applying further optimizations as well as inspecting and validating the behavior of the object program” [1, p. 113:2]
  - code reuse through capturing “code patterns that cannot be abstracted” [1, p. 113:2]

#### 3.1.1 Definitions

“*Metaprogramming* is the process of writing computer programs, called *metaprograms*, that [can] ...generate new programs or modify existing ones” [1, p. 113:1]. “It constitutes a flexible and powerful reuse solution for the ever-growing size and complexity of software systems” [1, p. 113:31].

- Metalanguage: “the language in which the metaprogram is written” [1, p. 113:1]
- Object language: “the language in which the generated or transformed program is written” [1, p. 113:1]
- Homogeneous metaprogramming: when “the object language and the metalanguage are the same” [1, p. 113:1]
- Heterogeneous metaprogramming: when “the object language and the metalanguage are ...different” [1, p. 113:1]

### 3.1.2 Metaprogramming Models

#### Macro Systems [1, p. 113:3-7]

- Map specified input sequences in a source file to corresponding output sequences (“macro expansion”) until no input sequences remain [1, p. 113:3]; this process can be:
  1. procedural (involving algorithms; this is more common [1, p. 113:31]), or
  2. pattern-based (only using pattern matching) [1, p. 113:4]
- Must avoid variable capture (unintended name conflicts) by being “hygienic” [1, p. 113:4]; this may be overridden to allow for “intentional variable capture”, such as Scheme’s *syntax-case* macro [1, p. 113:5]

#### Lexical Macros

- Language agnostic [1, p. 113:3]
- Usually only sufficient for basic metaprogramming since changes to the code without considering its meaning “may cause unintended side effects or name clashes and may introduce difficult-to-solve bugs” [1, p. 113:5]
- Marco was the first safe, language-independent macro system that “enforce[s] specific rules that can be checked by special oracles” for given languages (as long as the languages “produce descriptive error messages”) [1, p. 113:6]

#### Syntactic Macros

- “Aware of the language syntax and semantics” [1, p. 113:3]
- MS<sup>2</sup> “was the first programmable syntactic macro system for syntactically rich languages”, including by using “a type system to ensure that all generated code fragments are syntactically correct” [1, p. 113:5]

#### Reflection Systems [1, p. 113:7-9]

- “Perform computations on [themselves] in the same way as for the target application, enabling one to adjust the system behavior based on the needs of its execution” [1, p. 113:7]
- Means that the system can “observe and possibly modify its structure and behaviour” [2, p. 22]; these processes are called “introspection” and “intercession”, respectively [1, p. 113:7]
  - The representation of a system can either be structural or behavioural (e.g., variable assignment) [1, p. 113:7]

- “Runtime code generation based on source text can be impractical, inefficient, and unsafe, so alternatives have been explored based on ASTs and quasi-quote operators, offering a structured approach that is subject to typing for expressing and combining code at runtime” [1, p. 113:8]
- “Not limited to runtime systems”, as some “compile-time systems ...rely on some form of structural introspection to perform code generation” [1, p. 113:9]

### **MetaObject Protocols (MOPs) [1, p. 113:9-11]**

- “Interfaces to the language enabling one to incrementally transform the original language behavior and implementation” [1, p. 113:9]
- Three different approaches:
  - Metaclass-based Approach: “Classes are considered to be objects of metaclasses, called metaobjects, that are responsible for the overall behavior of the object system” [1, p. 113:9]
  - Metaobject-based Approach: “Classes and metaobjects are distinct” [1, p. 113:9]
  - Message Reification Approach: used with message passing [1, p. 113:9]
- Can either be runtime (more common) or compile-time (e.g., OpenC++); the latter protocols “operate as advanced macro systems that perform code transformation based on metaobjects rather than on text or ASTs” [1, p. 113:11]

**Dynamic Shells** “Pseudo-objects with methods and instance variables that may be attached to other objects” that “offer efficient and type-safe MOP functionality for statically typed languages” [1, p. 113:10].

**Dynamic Extensions** “Offer similar functionality [to dynamic shells] but for classes, allowing a program to replace the methods of a class and its subclasses by the methods of another class at runtime” [1, p. 113:10].

### **Aspect-Oriented Programming (AOP) [1, p. 113:11-13]**

- The use of *aspects*: “modular units ...[that] contain information about the additional behavior, called *advice*, that will be added to the base program by the aspect as well as the program locations, called *join points*, where this extra behavior is to be inserted based on some matching criteria, called *pointcuts*” [1, p. 113:12]
- Weaving: the process of “combining the base program with aspect code ...[to form] the final code” [1, p. 113:12]
- Two variants:



1. Static AOP: when weaving takes place at compile time, usually with “a separate language and a custom compiler, called [an] *aspect weaver*”; results in better performance [1, p. 113:12]
  2. Dynamic AOP: when weaving takes place at runtime by instrumenting “the bytecode ...to be able to weave the aspect code”; provides more flexibility [1, p. 113:12]
- This model originates from reflecting and MOPs (AspectS and AspectL “support AOP by building respectively on the runtime MOPs of Smalltalk and Lisp”) [1, p. 113:12]
  - While “AOP can support metaprogramming by inserting code before, after, or around matched join points, as well as introducing data members and methods through intertype declarations”, it is usually done the other way around, as most AOP frameworks “rely on metaprogramming techniques” [1, p. 113:12]

### Generative Programming [1, p. 113:13-17]

- “A software development paradigm based on modeling software system families such that, given a particular requirements specification, a highly customized and optimized intermediate or end-product can be automatically manufactured on demand from elementary, reusable implementation components by means of configuration knowledge”
- Often done with using ASTs [1, p. 113:31]
- Most “support code templates and quasi-quotes” [1, p. 113:31]
- Related to macro systems, but normal code and metacode are distinct

get original source from Czarnecki and Eisenecker 2000

### Template Systems [1, p. 113:13-14]

- Template code is instantiated with specific parameters to generate ALL code in a target language; “no free-form source code generation is allowed” [1, p. 113:13]
- It is possible, though complex, to express any “to express any generative metaprogram”, as long as “the appropriate metaprogramming logic for type manipulation” is present [1, p. 113:14]

clarify what “free-form source code generation” means

### AST Transformations [1, p. 113:14-15]

- “Offer code templates through quasi-quotation to support AST creation and composition and complement them with AST traversal or transformation features” [1, p. 113:14]

### Compile-Time Reflections [1, p. 113:15-16]

- “Offer compile-time reflection features to enable generating code based on existing code structures” while trying to ensure that “the generator will always produce well-formed code” (this is not always fully possible; for example, Genoupe “cannot guarantee that the generated code is always well typed”) [1, p. 113:15]

### Class Compositions [1, p. 113:16-17]

- Offer “flexibility and expressiveness” through composition approaches [1, p. 113:16]

Investigate

- *Mixins*:
- *Traits*: “support a uniform, expressive, and type-safe way for metaprogramming without resorting to ASTs” and offer “compile-time pattern-based reflection” through parameterization [1, p. 113:16]

Investigate?

- Includes *feature-oriented programming* approaches

### MultiStage Programming (MSP) [1, p. 113:17-20]

- “Makes ...[levels of evaluation] accessible to the programmer through ...*staging annotations*” to “specify the evaluation order of the program computations” and work with these computation stages [1, p. 113:17]
- Related to program generation and procedural macro systems [1, p. 113:17]; macros are often implemented as multistage computations [1, p. 113:18]
- Languages that use MSP are called *MultiStage Languages (MSLs)* or *two-stage languages*, depending on how many stages of evaluation are offered [1, p. 113:17]; MSLs are more common [1, p. 113:31]
  - C++ first instantiates templates, then translates nontemplate code [1, p. 113:19]
  - Template Haskell evaluates “the top-level splices to generate object-level code” at compile time, then executes the object-level code at run-time [1, p. 113:19]
- Often involves *Cross-Stage Persistence (CSP)*, which allows “values ...available in the current stage” to be used in future stages [1, p. 113:17]
  - If this is used, *cross-stage safety* is often also used to prevent “variables bound at some stage ...[from being] used at an earlier stage” [1, p. 113:17]
- Usually homogeneous, but there are exceptions; MetaHaskell, a modular framework [1, p. 113:19] with a type system, allows for “heterogeneous metaprogramming with multiple object languages” [1, p. 113:18]
- “Type safety ...comes at the cost of expressiveness” [1, p. 113:19]

### 3.1.3 Phase of Evaluation

- “In theory, any combination of them [the phases of evaluation] is viable; however, in practice most metalanguages offer only one or two of the options” [1, p. 113:20]
- “The phase of evaluation does not necessarily dictate the adoption of a particular metaprogramming model; however, there is a correlation between the two” [1, p. 113:20]

#### Preprocessing-Time Evaluation [1, p. 113:20-21]

- In PreProcessing-Time MetaProgramming (PPTMP), “metaprograms present in the original source are evaluated during the preprocessing phase and the resulting source file contains only normal program code and no metacode” [1, p. 113:20]
- These systems are called *source-to-source preprocessors* [1, p. 113:20] and are usually examples of generative programming [1, p. 113:21]
  - “All such cases involve syntactic transformations” [1, p. 113:21], usually using ASTs
- “Translation can reuse the language compiler or interpreter without the need for any extensions” [1, p. 113:20]
- Varying levels of complexity (e.g., these systems “may be fully aware of the language syntax and semantics”) [1, p. 113:20]
- Includes all lexical macro systems [1, p. 113:20] and some “static AOP and generative programming systems” [1, p. 113:31]
- Typically doesn’t use reflection (Reflective Java is an exception), MOPs, or dynamic AOP [1, p. 113:21]

#### Compilation-Time Evaluation [1, p. 113:21-23]

- In Compile-Time MetaProgramming (CTMP), “the language compiler is extended to handle metacode translation and execution” [1, p. 113:22]
  - There are many ways of extending the compiler, including “plugins, syntactic additions, procedural or rewrite-based AST transformations, or multistage translation” [1, p. 113:22]
  - Metacode execution can be done by “interpreting the source metacode ...or compiling the source metacode to binary and then executing it” [1, p. 113:22]
- These systems are usually examples of generative programming but can also use macros, MOPs, AOP [1, p. 113:22], and/or reflection [1, p. 113:23]

### **Execution-Time Evaluation [1, p. 113:23-25]**

- RunTime MetaProgramming (RTMP) “involves extending the language execution system and offering runtime libraries to enable dynamic code generation and execution” and is “the only case where it is possible to extend the system based on runtime state and execution” [1, p. 113:23]
- Includes “most reflection systems, MOPs, MSP systems, and dynamic AOP systems” [1, p. 113:31]

### **3.1.4 Metaprogram Source Location**

#### **Embedded in the Subject Program [1, p. 113:25-26]**

- Usually occurs with macros, templates, MSLs, reflection, MOPs, and AOP [1, p. 113:25]

#### **Context Unaware [1, p. 113:25]**

- Occurs when metaprograms only need to know their input parameters to generate ASTs [1, p. 113:25]
- Very common: supported by “most CTMP systems” [1, p. 113:31] and “for most macro systems..., generative programming systems ...and MSLs ...it is the only available option” [1, p. 113:25]

#### **Context Aware [1, p. 113:25-26]**

- “Typically involves providing access to the respective program AST node and allowing it to be traversed” as “an extra ...parameter to the metaprogram” [1, p. 113:25]
- Allows for code transformation “at multiple different locations reachable from the initial context” [1, p. 113:25]
- Very uncommon [1, p. 113:25, 31]

#### **Global [1, p. 113:26]**

- Involves “scenarios that collectively introduce, transform, or remove functionality for the entire program” [1, p. 113:26]
- Usually occurs with reflection, MOPs, and AOP [1, p. 113:26]; offered by “most RTMP systems” [1, p. 113:31]
- Can be used with “any PPTMP or CTMP system that provides access to the full program AST” [1, p. 113:26]
- “Can also be seen as a context-aware case where the context is the entire program” [1, p. 113:26]

**External to the Subject Program [1, p. 113:27]**

- Occurs when metaprograms “are specified as separate transformation programs applied through PPTMP systems or supplied to the compiler together with the target program to be translated as extra parameters” [1, p. 113:27]
- Includes many instances of AOP [1, p. 113:27]

**3.1.5 Relation to the Object Language**

- Each metaprogramming language has two layers:
  1. “The basic object language”
  2. “The metaprogramming elements for implementing the metaprograms” (the *metalayer*) [1, p. 113:27]
- Sometimes the metalayer of a language is added to a language later, independently of the object language [1, p. 113:27]

**Metalanguage Indistinguishable from the Object Language [1, p. 113:28-29]**

- Two categories:
  1. “Object language and metalanguage ...use the same constructs through the same syntax”
  2. “Metalanguage constructs ...[are] modeled using object language syntax and applied through special language or execution system features” [1, p. 113:28]
    - Includes many examples of MOPs and AOP [1, p. 113:28]

**Metalanguage Extends the Object Language [1, p. 113:29]**

- Allows for reuse of “the original language[s] ...well-known features instead of adopting custom programming constructs” [1, p. 113:29]
- “Typically involve new syntax and functionality used to differentiate normal code from metacode” [1, p. 113:29]
- Often used in quasi-quote constructs, two-stage and multistage languages, and MOPs [1, p. 113:29]
- Used with MSLs “as the base languages are extended with staging annotations to deliver MSP functionality” [1, p. 113:31]

### **Metalinguage Different from the Object Language [1, p. 113:29-31]**

- Allows for “the metalinguage syntax and constructs ...[to be] selected to better reflect the metalinguage concepts to ease their use in developing metaprograms and enable them to become more concise and understandable” [1, p. 113:29]
- However, it can lead to “different development practices and disable[s] the potential for design or code reuse between them [the languages]”, as well as requiring users to know how to use both languages [1, p. 113:30]
- Used by some AOP and generative metaprogramming systems [1, p. 113:30]

## **3.2 Overview of Generative Software Development**

“System family engineering seeks to exploit the commonalities among systems from a given problem domain while managing the variabilities among them in a systematic way” [3, p. 326]. “Generative software development is a system-family approach ...that focuses on automating the creation of system-family members ...from a specification written in [a Domain-Specific Language (DSL)]” [3, p. 327]. “DSLs come in a wide variety of forms, ...[including] textual ...[and] diagrammatic” [3, p. 328].

“System family engineering distinguishes between at least two kinds of development processes: *domain engineering* and *application engineering*” [3, p. 328]. “Domain engineering ...is concerned with the development of reusable assets such as components, generators, DSLs, analysis and design models, user documentation, etc.” [3, p. 328-329]. It includes “determining the scope of the family to be built, identifying the common and variable features among the family members”, and “the development of a common architecture for all the members of the system family” [3, p. 329]. Application engineering includes “requirements elicitation, analysis, and specification” and “the manual or automated construction of the system from the reusable assets” [3, p. 329]. The assets from domain engineering are used to build the system development by application engineering, which provides domain engineering which the requirements to analyze for commonalities and create reusable assets for [3, p. 329].

Aspect-Oriented Programming (AOP) “provides more powerful localization and encapsulation mechanisms than traditional component technologies” but there is still the need to “configure aspects and other components to implement abstract features” [3, p. 338]. AOP “cover[s] the solution space and only a part of the configuration knowledge”, although “aspects can also be found in the problem space” [3, p. 338].

### **3.2.1 Definitions**

- Generative domain model: “a mapping between *problem space* and *solution space*” which “takes a specification and returns the corresponding implementation” [3, p. 330]

- Configuration view: “the problem space consists of domain-specific concepts and their features” such as “illegal feature combinations, default settings, and default dependencies” [3, p. 331]. “An application programmer creates a configuration of features by selecting the desired ones, [sic] which then is mapped to a configuration of components” [3, p. 331]
- Transformational view: “a problem space is represented by a ...[DSL], whereas the solution space is represented by an implementation language” [3, p. 331]. “A program in a ...[DSL]” is transformed into “its implementation in the implementation language” [3, p. 331]
- Problem space: “a set of domain-specific abstractions that can be used to specify the desired system-family member” [3, p. 330]
- Solution space: “consists of implementation-oriented abstractions, which can be instantiated to create implementations of the [desired] specifications” [3, p. 330]
- Network of domains: the graph built from “spaces and mappings ...where each implementation of a domain exposes a DSL, which may be implemented by transformations to DSLs exposed by other domain implementations” [3, p. 332-333]
- Feature modeling: “a method and notation to elicit and represent common and variable features of the systems in a system family” [3, p. 333]. Can be used during domain analysis as “the starting point in the development of both system-family architecture and DSLs” [3, p. 334]
- Model-Driven Development (MDD): uses “abstract representation[s] of a system and the portion[s] of the world that interact[] with it” to “captur[e] every important aspect of a software system” [3, p. 336]. Often uses DSLs and sometimes deals with system families, making it related to generative software development [3, p. 336-337]

### 3.3 Structured Program Generation Techniques

- Program transformer: something that “modifies an existing program, instead of generating a new one” (for example, by making a program’s code adhere to style guides); the term “program generator” often includes program transformers [4, p. 1]
- Generators are used “to automate, elevate, modularize or otherwise facilitate program development” [4, p. 2]
- Why is it beneficial “to statically check the generator and be sure that no type error arises during its *run time*” [4, p. 2] instead of just checking the generated program(s)?

- “An error in the generated program can be very hard to debug and may require full understanding of the generator itself” [4, p. 2]
- Errors can occur in the generator from “mismatched assumptions”; for example, “the generator fails to take into account some input case, so that, even though the generator writer has tested the generator under several inputs, other inputs result in badly-formed programs” [4, p. 6]

### 3.3.1 Techniques for Program Generation [4, p. 3-5]

1. Generation as text: “producing character strings containing the text of a program, which is subsequently interpreted or compiled” [4, p. 3]
2. Syntax tree manipulation: building up code using constructors in a syntactically meaningful way that preserves its structure
3. Code templates/quoting: involves “language constructs for generating program fragments in the target language ...as well as for supplying values to fill in holes in the generated syntax tree” [4, p. 4]
4. Macros: “reusable code templates with pre-set rules for parameterizing them” [4, p. 4]
5. Generics: Mechanisms with “the ability to parameterize a code template with different static types” [4, p. 5]
6. Specialized languages: Languages with specific features for program generators, such as AOP and *inter-type declarations* [4, p. 5]

### 3.3.2 Kinds of Generator Safety [4, p. 5-8]

- Lexical and syntactic well-formedness: “any generated/transformed program is guaranteed to pass the lexical analysis and parsing phases of a traditional compiler”; usually done “by encoding the syntax of the object language using the type system of the host language” [4, p. 6]
- Scoping and hygiene: avoiding issues with scope and unintentional variable capture
- Full well-formedness: ensuring that any generated/transformed program is guaranteed to be fully well-formed (e.g., “guaranteed to pass any static check in the target language” [4, p. 8])

### 3.3.3 Methods for Guaranteeing Fully Structured Generation [4, p. 8-20]

1. MultiStage Programming (MSP): “the generator and the generated program ...are type-checked by the same type system[] and some parts of the program



are merely evaluated later (i.e., generated)”; similar to *partial evaluation* [4, p. 9]

2. Class Morphing: similar to MetaObject Protocols (MOPs)?
3. Reflection: (e.g., SafeGen [4, p. 15])
4. The use of “a powerful type system that can simultaneously express conventional type-level properties of a program and the logical structure of a generator under unknown inputs. This typically entails the use of dependent types” (e.g., Ur) [4, p. 16]
5. Macro systems, although “safety guarantees carry the cost of some manual verification effort by the programmer” [4, p. 19]

## 3.4 Taxonomy of Fundamental Concepts of Meta-Programming

### 3.4.1 Definitions

- Program transformation: “the process of changing one form of a program (source code, specification or model) into another, as well as a formal or abstract description of an algorithm that implements this transformation” [2, p. 18]
  - It may or may not preserve the program’s semantics [2, p. 18]
  - In metaprogramming, “the transformation algorithm describes generation of a particular instance depending upon values of the generic parameters” [2, p. 18]
  - Formal program transformation: “A stepwise manipulation, which (1) is defined on a programming language domain, (2) uses a formal model to support the refinement, and (3) simultaneously preserves the semantics” [2, p. 18]
- Code generation: “the process by which a code generator converts a syntactically correct high-level program into a series of lower-level instructions”; the input can take many forms “typically consists of a parse tree, abstract syntax tree or intermediate language code” and “the output ...could be in any language” [2, p. 19]
- Generic component: “a software module ...[that] abstractly and concisely represents a set of closely related (‘look-alike’) software components with slightly different properties” [2, p. 19]
- Generative component: a generic component that has “explicitly added generative technology” [2, p. 24]
- Separation of concerns: “the process of breaking a design problem into distinct tasks that are orthogonal and can be implemented separately” [2, p. 21]

### 3.4.2 Other Notes

- Structural meta-programming concepts “are defined by the designer”, “used during construction of the meta-programming systems and artefacts”, and “depend upon [the] specific ...meta-language” used [2, p. 24]
- Most processes “are used in compile time or run time” except for generalization, which “is used during the creation of the meta-programming artefacts” [2, p. 24-25]

should I change this if it's British English?

## 3.5 Roadblocks to Meta-Programming

- “Generators are often the technique of last resort” [4, p. 2]
- “A major stumbling block to achieving the promised benefits [of meta-programming] is the understanding and learning the meta-programming approach. One reason may be that we do not yet thoroughly understand the fundamental concepts that define meta-programming” [2, p. 26]
- Meta-programming does not provide instant results; instead, the effort and design put in at the beginning of the process later pay off potentially large dividends that are not seen right away; “most ...programmers and designers ...like to reuse the existing software artefacts, but not much is done and [sic] invested into designing for reuse” [2, p. 26] (example, meta-programming was proposed by McIlroy in 1968 but “software factories have not become a reality ...partly due to ...[this] significant initial investment”) [2, p. 27]
- Software development involves “work[ing] with multiple levels of abstraction”, including “the syntax, semantics, abilities and limitations” of given languages, their implementation details, their communication details, and “impeding mismatches” between them [2, p. 27]
- “Modification of the generated code usually removes the program from the scope of the meta-programming system” [2, p. 27]

## 3.6 Roadblocks to Testing Scientific Software [5, p. 67]

- “Correct answers are often unknown”: if the results were already known, there would be no need to develop software to model them [5, p. 67]
- “Practically difficult to validate the computed output”: complex calculations and outputs are difficult to verify [5, p. 67]
- “Inherent uncertainties”: since scientific software models scenarios that occur in a chaotic and imperfect world, not every factor can be accounted for [5, p. 67]

- “Choosing suitable tolerances”: difficult to decide what tolerance(s) to use when dealing with floating-point numbers [5, p. 67]
- “Incompatible testing tools”: while scientific software is often written in languages like FORTRAN, testing tools are often written in languages like Java or C++ [5, p. 67]

Out of this list, only the first two apply. The scenarios modelled by Drasil are idealized and ignore uncertainties like air resistance, wind direction, and gravitational fluctuations. There are not any instances where special consideration for floating-point arithmetic must be taken; the default tolerance used for relevant testing frameworks has been used and is likely sufficient for future testing. On a related note, the scientific software we are trying to test is already generated in languages with widely-used testing frameworks.

Add example

Add source(s)?

## 3.7 Software Metrics

- The following branches of testing started as parts of quality testing:
  - Reliability testing [6, p. 18, ch. 10]
  - Performance testing [6, p. 18, ch. 7]
- Reliability and maintainability can start to be tested even without code by “measur[ing] structural attributes of representations of the software” [6, p. 18]
- The US Software Engineering Institute has a checklist for determining which types of lines of code are included when counting [6, pp. 30-31]
- Measurements should include an entity to be measured, a specific attribute to measure, and the actual measure (i.e., units, starting state, ending state, what to include) [6, p. 36]
  - These attributes must be defined before they can be measured [6, p. 38]

## 3.8 Software Testing

While [7] groups testing into static/dynamic and white-/black-box, [8, p. 398-399] gives a classification “according to the criterion used to measure the adequacy of a set of test cases”: coverage-based, fault-based (includes mutation testing), and error-based (“based on knowledge of the typical errors that people make”).

### 3.8.1 Definitions

- Error: “a human action that produces an incorrect result” [8, p. 399]
- Fault: “the manifestation of an error” in the software itself [8, p. 400]

- Failure: incorrect output or behaviour resulting from encountering a fault; can be defined as not meeting specifications or expectations and “is a relative notion” [8, p. 400]
- Verification: “the process of evaluating a system or component to determine whether the products of a given development phase satisfy the conditions imposed at the start of that phase” [8, p. 400]
- Validation: “the process of evaluating a system or component during or at the end of the development process to determine whether it satisfies specified requirements” [8, p. 400]

### Documentation

- Verification and Validation (V&V) Plan: a document for the “planning of test activities” described by IEEE Standard 1012 [8, p. 411]
- Test Plan: “a document describing the scope, approach, resources, and schedule of intended test activities” in more detail than the V&V Plan [8, p. 412-413]
- Test Design documentation: “specifies ...the details of the test approach and identifies the associated tests” [8, p. 413]
- Test Case documentation: “specifies inputs, predicted outputs and execution conditions for each test item” [8, p. 413]
- Test Procedure documentation: “specifies the sequence of actions for the execution of each test” [8, p. 413]
- Test Report documentation: “provides information on the results of testing tasks”, addressing software verification and validation reporting [8, p. 413]

### 3.8.2 General Testing Notes

- “Proving the correctness of software ...applies only in circumstances where software requirements are stated formally” and assumes “these formal requirements are themselves correct” [8, p. 398]
- If faults exist in programs, they “must be considered faulty, even if we cannot devise test cases that reveal the faults” [8, p. 401]
- Black-box test cases should be created based on the specification *before* creating white-box test cases to avoid being “biased into creating test cases based on how the module works” [7, p. 113]
- Simple, normal test cases (test-to-pass) should always be developed and run before more complicated, unusual test cases (test-to-fail) [7, p. 66]

### Generating Test Cases

- “A **test adequacy criterion** ...specifies requirements for testing ...and can be used ...as a test case generator.... [For example, i]f a 100% statement coverage has not been achieved yet, an additional test case is selected that covers one or more statements yet untested” [8, p. 402]
- “*Test data generators*” are mentioned on [8, p. 410] but not described

### 3.8.3 Static Black-Box (Specification) Testing [7, p. 56-62]

Most of this section is irrelevant to generating test cases, as they require human involvement (e.g., Pretend to Be the Customer [7, p. 57-58], Research Existing Standards and Guidelines [7, p. 58-59]). However, it provides a “Specification Terminology Checklist” [7, p. 61] that includes some keywords that, if found, could trigger an applicable warning to the user (similar to the idea behind the correctness/consistency checks project):

- **Potentially unrealistic:** always, every, all, none, every, certainly, therefore, clearly, obviously, evidently
- **Potentially vague:** some, sometimes, often, usually, ordinarily, customarily, most, mostly, good, high-quality, fast, quickly, cheap, inexpensive, efficient, small, stable
- **Potentially incomplete:** etc., and so forth, and so on, such as, handled, processed, rejected, skipped, eliminated, if ...then ...(without “else” or “otherwise”), to be determined [8, p. 408]

### Coverage-Based Testing of Specification [8, pp. 425-426]

Requirements can be “depicted as a graph, where the nodes denote elementary requirements and the edges denote relations between [them]” from which test cases can be derived [8, p. 425]. However, it can be difficult to assess whether a set of equivalence classes are truly equivalent, since the specific data available in each node is not apparent [8, p. 426].

### 3.8.4 Dynamic Black-Box (Behavioural) Testing [7, pp. 64-65]

This is the process of “entering inputs, receiving outputs, and checking the results” [7, p. 64]. [8] also calls this “functional testing”.

### Requirements

- Requirements documentation (definition of what the software does) [7, p. 64]; relevant information could be:
  - Requirements: Input-Values and Output-Values
  - Input/output data constraints

### **Exploratory Testing [7, p. 65]**

An alternative to dynamic black-box testing when a specification is not available [7, p. 65]. The software is explored to determine its features, and these features are then tested [7, p. 65]. Finding any bugs using this method is a positive thing [7, p. 65], since despite not knowing what the software *should* do, you were able to determine that something is wrong.

This is not applicable to Drasil, because not only does it already generate a specification, making this type of testing unnecessary, there is also a lot of human-based trial and error required for this kind of testing [9].

### **Equivalence Partitioning/Classing [7, p. 67-69]**

The process of dividing the infinite set of test cases into a finite set that is just as effective (i.e., that reveals the same bugs) [7, p. 67].

#### **Requirements**

- Ranges of possible values [7, p. 67]; could be obtained through:
  - Input/output data constraints
  - Case statements

### **Data Testing [7, p. 70-79]**

The process of “checking that information the user inputs [and] results”, both final and intermediate, “are handled correctly” [7, p. 70]. This type of testing can also occur at the white-box level, such as the implementation of boundaries [8, p. 431] or intermediate values within components.

**Boundary Conditions [7, p. 70-74]** “[S]ituations at the edge of the planned operational limits of the software” [7, p. 72]. Often affects types of data (e.g., numeric, speed, character, location, position, size, quantity [7, p. 72]) each with its own set of (e.g., first/last, min/max, start/finish, over/under, empty/full, shortest/longest, slowest/fastest, soonest/latest, largest/smallest, highest/lowest, next-to/farthest-from [7, p. 72-73]). Data at these boundaries should be included in an equivalence partition, but so should data in between them [7, p. 73]. Boundary conditions should be tested using “the valid data just inside the boundary, ...the last possible valid data, and ...the invalid data just outside the boundary” [7, p. 73].

#### **Requirements**

- Ranges of possible values [7, p. 67, 73]; could be obtained through:
  - Case statements
  - Input/output data constraints (e.g., inputs that would lead to a boundary output)

**Buffer Overruns [7, p. 201-205]** *Buffer overruns* are “the number one cause of software security issues” [7, p. 75]. They occur when the size of the destination for some data is smaller than the data itself, causing existing data (including code) to be overwritten and malicious code to potentially be injected [7, p. 202, 204–205]. They often arise from bad programming practices in “languages [sic] such as C and C++, that lack safe string handling functions” [7, p. 201]. Any unsafe versions of these functions that are used should be replaced with the corresponding safe versions [7, p. 203-204].

**Sub-Boundary Conditions [7, p. 75-77]** Boundary conditions “that are internal to the software [but] aren’t necessarily apparent to an end user” [7, p. 75]. These include powers of two [7, p. 75-76] and ASCII and Unicode tables [7, p. 76-77].

While this is of interest to the domain of scientific computing, this is too involved for Drasil right now, and the existing software constraints limit much of the potential errors from over/underflow [9]. Additionally, strings are not really used as inputs to Drasil and only occur in output with predefined values, so testing these values are unlikely to be fruitful.

There also exist sub-boundary conditions that arise from “complex” requirements, where behaviour depends on multiple conditions [8, p. 430]. These “error prone” points around these boundaries should be tested [8, p. 430] as before: “the valid data just inside the boundary, ...the last possible valid data, and ...the invalid data just outside the boundary” [7, p. 73]. In this type of testing, the second type of data is called an “ON point”, the first type is an “OFF point” for the domain on the *other* side of the boundary, and the third type is an “OFF point” for the domain on the *same* side of the boundary [8, p. 430].

## Requirements

- Increased knowledge of data type structures (e.g., monoids, rings, etc. [9]); this would capture these sub-boundaries, as well as other information like relevant tests cases, along with our notion of these data types (**Space**)

**Default, Empty, Blank, Null, Zero, and None [7, p. 77-78]** These should be their own equivalence class, since “the software usually handles them differently” than “the valid cases or ...invalid cases” [7, p. 78].

Since these values may not always be applicable to a given scenario (e.g., a test case for zero doesn’t make sense if there is a constraint that the value in question cannot be zero), the user should likely be able to select categories of tests to generate instead of Drasil just generating all possible test cases based on the inputs [9].

## Requirements

- Knowledge of an “empty” value for each **Space** (stored alongside each type in **Space**?)

- Knowledge of how input data could be omitted from an input (e.g., a missing command line argument, an empty line in a file); could be obtained from:
  - User responsibilities
- Knowledge of how a programming language deals with `Null` values and how these can be passed as arguments

**Invalid, Wrong, Incorrect, and Garbage Data** [7, p. 78-79] This is testing-to-fail [7, p. 77].

**Requirements** This seems to be the most open-ended category of testing.

- Specification of correct inputs that can be ignored; could be obtained through:
  - Input/output data constraints (e.g., inputs that would lead to a violated output constraint)
  - Type information for each input (e.g., passing a string instead of a number)

**State Testing** [7, p. 79-87]

The process of testing “a program’s states and the transitions between them” [7, p. 79].

**Logic Flow Testing** [7, p. 80-84] This is done by creating a state transition diagram that includes:

- Every possible unique state
- The condition(s) that take(s) the program between states
- The condition(s) and output(s) when a state is entered or exited

to map out the logic flow from the user’s perspective [7, p. 81-82]. Next, these states should be partitioned using one (or more) of the following methods:

1. Test each state once
2. Test the most common state transitions
3. Test the least common state transitions
4. Test all error states and error return transitions
5. Test random state transitions [7, p. 82-83]

For all of these tests, the values of the state variables should be verified [7, p. 83].



### Requirements

- Knowledge of the different states of the program [7, p. 82]; could be obtained through:
  - The program’s modules and/or functions
  - The program’s exceptions
- Knowledge about the different state transitions [7, p. 82]; could be obtained through:
  - Testing the state transitions near the beginning of a workflow more?

**Testing States to Fail [7, p. 84-87]** The goal here is to try and put the program in a fail state by doing things that are out of the ordinary. These include:

- Race Conditions and Bad Timing [7, p. 85-86] (Is this relevant to our examples?)
- Repetition Testing: “doing the same operation over and over”, potentially up to “thousands of attempts” [7, p. 86]
- Stress Testing: “running the software under less-than-ideal conditions” [7, p. 86]
- Load testing: running the software with as large of a load as possible (e.g., large inputs, many peripherals) [7, p. 86]

### Requirements

- Repetition Testing: The types of operations that are likely to lead to errors when repeated (e.g., overwriting files?)
- Stress testing: can these be automated with pytest or are they outside our scope?
- Load testing: Knowledge about the types of inputs that could overload the system (e.g., upper bounds on values of certain types)

### Other Black-Box Testing [7, pp. 87-89]

- Act like an inexperienced user (*likely out of scope*)
- Look for bugs where they’ve already been found (*keep track of previous failed test cases? This could pair well with **Metamorphic Testing (MT)**!*)
- Think like a hacker (*likely out of scope*)
- Follow experience (*implicitly be done by using Drasil*)

Investigate

### 3.8.5 Static White-Box Testing (Structural Analysis) [7, pp. 91-104]

There are also some more specific categories of this, such as Scenario-Based Evaluation [8, pp. 417-418], Correctness Proofs [8, pp. 418-419], and Stepwise Abstraction [8, pp. 419-420] that could be investigated further.

Do this!

- “The process of carefully and methodically reviewing the software design, architecture, or code for bugs without executing it” [7, p. 92]
- Less common than black-box testing, but often used for “military, financial, factory automation, or medical software, ...in a highly disciplined development model” or when “testing software for security issues” [7, p. 91]; often avoided because of “the misconception that it’s too time-consuming, too costly, or not productive” [7, p. 92]
- Especially effective early on in the development process [7, p. 92]
- Can “find bugs that would be difficult to uncover or isolate with dynamic black-box testing” and “gives the team’s black-box testers ideas for test cases to apply” [7, p. 92]
- Largely “done by the language compiler” or by separate tools [8, pp. 413-414]

#### Formal Reviews [7, p. 92-95]

- “The process under which static white-box testing is performed” [7, p. 92]; consists of four main parts:
  1. Identify Problems: Find what is wrong or missing
  2. Follow Rules: There should be a structure to the review, such as “the amount of code to be reviewed ..., how much time will be spent ..., what can be commented on, and so on”, to set expectations; “if a process is run in an ad-hoc fashion, bugs will be missed and the participants will likely feel that the effort was a waste of time”
  3. Prepare: Based on the participants’ roles, they should know what they will be contributing during the actual review; “most of the problems found through the review process are found during preparation”
  4. Write a Report: A summary should be created and provided to the rest of the development team so that they know what problems exist, where they are, etc. [7, p. 93]
- Reviews improve communication, learning, and camaraderie, as well as the quality of code *even before the review*: if a developer “knows that his work is being carefully reviewed by his peers, he might make an extra effort to ...make sure that it’s right” [7, p. 93-94]
- Many forms:

- Peer Review: Includes the four main parts of a formal review, but informally and at a smaller scale [7, p. 94]. One variation is to have each person submit “a ‘best’ program and one of lesser quality”, randomly distribute all programs to be assessed by two people in the group, and return all feedback anonymously to its author [8, p. 414]
  - Walkthrough: The author of the code presents it line by line to a small group that “question anything that looks suspicious” [7, p. 95]; this is done by using test data to “walk through” the execution of the program [8, p. 416]
  - Inspection: Someone who is *not* the author of the code presents it to a small group of people each with a different perspective (e.g., user); changes are made based on issues identified, and a reinspection may take place [7, p. 95]
- Could be used to evaluate code written for generation, as well as for the code that is generated

### **Coding Standards and Guidelines [7, p. 96-99]**

- Code may work but still be incorrect if it doesn’t meet certain criteria, since these affect its reliability, readability, maintainability, and/or portability; e.g., the `goto`, `while`, and `if-else` commands in C can cause bugs if used incorrectly [7, p. 96]
- These guidelines can range in strictness and formality, as long as they are agreed upon and followed [7, p. 96]
- This could be checked using linters

### **Generic Code Review Checklist [7, p. 99-103]**

- Data reference errors: “bugs caused by using a variable, constant, ...[etc.] that hasn’t been properly declared or initialized” for its context [7, p. 99]
- Data declaration errors: bugs “caused by improperly declaring or using variables or constants” [7, p. 100]
- Computation errors: “essentially bad math”; e.g., type mismatches, over/underflow, zero division, out of meaningful range [7, p. 101]
- Comparison errors: “very susceptible to boundary condition problems”; e.g., correct inclusion, floating point comparisons [7, p. 101]
- Control flow errors: bugs caused by “loops and other control constructs in the language not behaving as expected” [7, p. 102]
- Subroutine parameter errors: bugs “due to incorrect passing of data to and from software subroutines” [7, p. 102] (could also be called “interface errors” [8, p. 416])

- Input/output errors: e.g., how are errors handled? [7, p. 102-103]
- ASCII character handling, portability, compilation warnings [7, p. 103]

### Requirements

- Data reference errors: know what operations are allowed for each type and check that values are only used for those operations
- Data declaration errors: I think this will mainly be covered by checking for data reference errors and by our generator (e.g., no typos in type names)
- Computation errors: partially tested dynamically by system tests, but could also more formally check for things like type mismatches (does GOOL do this already?) or if divisors can ever be zero
- Comparison errors: I think this would mainly have to be done manually (maybe except for checking for (in)equality between values where it can never occur), but we may be able to generate a summary of all comparisons for manual verification
- Control flow errors: mostly irrelevant since we don't implement loops yet; would this include system tests?
- Subroutine parameter errors: we could check the types of values returned by a subroutine with the expected type (at least for languages like Python)
- Input/output errors: knowledge of (and more formal specification of) requirements would be needed here
- ASCII character handling, portability, compilation warnings: we could automatically check that the compiler (for languages that meaningfully have a compile stage) doesn't output any warnings (e.g., by saving output to a file and checking it is what is expected from a normal compilation); do we have any string inputs?

### 3.8.6 Dynamic White-Box (Structural) Testing [7, p. 105-121]

- “Using information you gain from seeing what the code does and how it works to determine what to test, what not to test, and how to approach the testing” [7, p. 105]
- *Mentions unit, integration, and system testing without formally describing them* [7, p. 109]
- Two approaches for testing incrementally:
  - Bottom-up testing: uses *test drivers*: “tool[s] that generate[] the test environment for a component to be tested” [8, p. 410] by “sending test-case data to the modules under test, read[ing] back the results, and verify[ing] that they're correct” [7, p. 109]

Find formal description of unit, integration, and system testing

- Top-down testing: uses *test stubs*: tools that “simulate[] the function of a component not yet available” [8, p. 410] by providing “fake” values to a given module to be tested [7, p. 110]

### Code Coverage [7, pp. 117-121] or Control-Flow Coverage [8, pp. 421-424]

“[T]est[ing] the program’s states and the program’s flow among them” [7, p. 117]; allows for redundant and/or missing test cases to be identified [7, p. 118]. Coverage-based testing is often based “on the notion of a control graph ...[where] nodes denote actions, ...(directed) edges connect actions with subsequent actions (in time) ...[and a] path is a sequence of nodes connected by edges. The graph may contain cycles ...[which] correspond to loops ...” [8, pp. 420-421]. “A cycle is called *simple* if its inner nodes are distinct and do not include [the node at the beginning/end of the cycle]” [8, p. 421, emphasis added]. If there are multiple actions represented as nodes that occur one after another, they may be collapsed into a single node [8, p. 421].

We discussed that generating infrastructure for reporting coverage may be a worthwhile goal, and that it can be known how to increase certain types of coverage (since we know the structure of the generated code, to some extent, beforehand), but I’m not sure if all of these are feasible/worthwhile to get to 100% (e.g., line coverage).

- Statement/line coverage: “execut[ing] every statement in the program at least once”; doesn’t guarantee full coverage (e.g., all paths might not be taken) [7, p. 119] or correctness [8, p. 421]
- Path coverage: “[a]ttempting to cover all the paths in the software” [7, p. 119]; if done completely, it “is equivalent to exhaustively testing the program” but is generally “not possible” due to the complexity of loops, branches, and potentially unreachable code [8, p. 421]
- Branch coverage: attempting to, “at each branching node in the control graph, ...[choose] all possible branches ...at least once” [8, p. 421]
  - the simplest form of path coverage [7, p. 119]
  - complete branch coverage does not imply complete path coverage or correctness [8, p. 421]
  - Cyclomatic-number criterion: an adequacy criterion that requires that “all linearly-independent paths are covered” [8, p. 423]; results in complete branch coverage
- (Multiple) condition coverage: “takes the extra conditions on the branch statements into account” (e.g., all possible inputs to a Boolean expression) [7, p. 120]; “also known as **extended branch coverage**” [8, p. 422]

add source?

### Data Coverage [7, p. 114-116]

In addition to **Data Flow Coverage** [7, p. 114], [8, pp. 424-425], there are also some minor forms of data coverage:

- Sub-boundaries: mentioned previously in 3.8.4
- Formulas and equations: related to **computation errors**
- Error forcing: setting variables to specific values to see how errors are handled; any error forced must have a chance of occurring in the real world, even if it is unlikely [7, p. 116]

**Data Flow Coverage** [7, p. 114], [8, pp. 424-425] “[T]racking a piece of data completely through the software” (or a part of it), usually using debugger tools to check the values of variables [7, p. 114].

- “A variable is *defined* in a certain statement if it is assigned a (new) value because of the execution of that statement” [8, p. 424]
- “A definition in statement X is *alive* in statement Y if there exists a path from X to Y in which that variable does not get assigned a new value at some intermediate node” [8, p. 424]
- A path from a variable’s definition to a statement where it is still alive is called **definition-clear** (with respect to this variable) [8, p. 424]
- Predicate Use (P-use): e.g., the use of a variable in a conditional [8, p. 424]
- Computational Use (C-use): e.g., the use of a variable in a computation or I/O statement [8, p. 424]

Table 3.1 contains different types of data flow coverage criteria, approximately from weakest to strongest, as well as their requirements; all information is adapted from [8, pp. 424-425].

### Fault Seeding [8, pp. 427-428]

The introduction of faults to estimate the number of undiscovered faults in the system based on the ratio between the number of new faults and the number of introduced faults that were discovered (which will ideally be small) [8, p. 427]. Makes many assumptions, including “that both real and seeded faults have the same distribution” and requires careful consideration as to which faults are introduced and how [8, p. 427].

Is this sufficient?

Table 3.1: Types of Data Flow Coverage

Criteria	Requirements
All-defs coverage	Each definition to be used at least once
All-P-uses coverage	A definition-clear path from each definition to each P-use
All-P-uses/Some-C-uses coverage	Same as All-P-uses coverage, but if a definition is only used in computations, at least one definition-clear path to a C-use must be included
All-C-uses/Some-P-uses coverage	A definition-clear path from each definition to each C-use; if a definition is only used in predicates, at least one definition-clear path to a P-use must be included
All-Uses coverage	A definition-clear path between each variable definition to each of its uses and each of these uses' successors
All-DU-Paths coverage	Same as All-Uses coverage, but each path must be cycle-free or a simple cycle

### Mutation Testing [8, pp. 428-429]

“A (large) number of variants of a program is generated”, each differing from the original “slightly” (e.g., by deleting a statement or replacing an operator with another) [8, p. 428]. These *mutants* are then tested; if set of tests fails to expose a difference in behaviour between the original and many mutants, “then that test set is of low quality” [8, pp. 428-429]. The goal is to maximize the number of mutants identified by a given test set [8, p. 429]. **Strong mutation testing** works at the program level while **weak mutation testing** works at the component level (and “is often easier to establish”) [8, p. 429].

There is an unexpected byproduct of this form of testing. In some cases of one experiment, “the original program failed, while the modified program [mutant] yielded the right result” [8, p. 432]! In addition to revealing shortcomings of a test set, mutation testing can also point the developer(s) in the direction of a better solution!

### 3.8.7 Regression Testing

- Rerunning old tests to test new changes to the system
- Various levels:
  - Retest-all: “all tests are rerun”; “this may consume a lot of time and effort” [8, p. 411] (although hopefully not, since we’ll be automating testing)
  - Selective retest: “only some of the tests are rerun” after being selected by a *regression test selection technique*; “[v]arious strategies have been

proposed for doing so; few of them have been implemented yet” [8, p. 411]

Investigate

- Does not go into much detail

### 3.8.8 Metamorphic Testing (MT)

The use of Metamorphic Relations (MRs) “to determine whether a test case has passed or failed” [5, p. 67]. “A[n] MR specifies how the output of the program is expected to change when a specified change is made to the input” [5, p. 67]; this is commonly done by creating an initial test case, then transforming it into a new one by applying the MR (both the initial and the resultant test cases are executed and should both pass) [5, p. 68]. “MT is one of the most appropriate and cost-effective testing techniques for scientists and engineers” [5, p. 72].

#### Benefits of MT

- Easier for domain experts; not only do they understand the domain (and its relevant MRs) [5, p. 70], they also may not have an understanding of testing principles [5, p. 69]. *This majorly overlaps with Drasil!*
- Easy to implement via scripts [5, p. 69]. *Again, Drasil*
- Helps negate the test oracle [5, p. 69] and output validation [5, p. 70] problems from **Roadblocks to Testing Scientific Software** [5, p. 67] (*i.e., the two that are relevant for Drasil*)
- Can extend a limited number of test cases (e.g., from an experiment that was only able to be conducted a few times) [5, pp. 70-72]
- Domain experts are sometimes unable to identify faults in a program based on its output [5, p. 71]

#### Examples of MT

- The average of a list of numbers should be equal (within floating-point errors) regardless of the list’s order [5, p. 67]
- For matrices, if  $B = B_1 + B_2$ , then  $A \times B = A \times B_1 + A \times B_2$  [5, pp. 68-69]
- Symmetry of trigonometric functions; for example,  $\sin(x) = \sin(-x)$  and  $\sin(x) = \sin(x + 360^\circ)$  [5, p. 70]
- Modifying input parameters to observe expected changes to a model’s output (e.g., testing epidemiological models calibrated with “data from the 1918 Influenza outbreak”); by “making changes to various model parameters ...authors identified an error in the output method of the agent based epidemiological model” [5, p. 70]



- Using machine learning to predict likely MRs to identify faults in mutated versions of a program (about 90% in this case) [5, p. 71]

# Chapter 4

## Development Process

The following is a rough outline of the steps I have gone through this far for this project:

- Start developing system tests (this was pushed for later to focus on unit tests)
- Test inputting default values as `floats` and `ints`
- Check constraints for valid input
- Check constraints for invalid input
- Test the calculations of:
  - `t_flight`
  - `p_land`
  - `d_offset`
  - `s`
- Test the writing of valid output
- Test for projectile going long
- Integrate system tests into existing unit tests
- Test for assumption violation of `g`
  - Code generation could be flawed, so we can't assume assumptions are respected
  - Test cases shouldn't necessarily match what is done by the code; for example, `g = 0` shouldn't really give a `ZeroDivisionError`; it should be a `ValueError`
  - This inspired the potential for [The Use of Assertions in Code](#)
- Test that calculations stop on a constraint violation; this is a requirement should be met by the software (see [Generating Requirements](#))

- Test behaviour with empty input file
- Start creation of test summary (for `InputParameters` module)
  - It was difficult to judge test case coverage/quality from the code itself
  - This is not really a test plan, as it doesn't capture the testing philosophy
  - Rationale for each test explains why it supports coverage and how Drasil derived (would derive) it
- Start researching testing
- Implement generation of `__init__.py` files ([#3516](#))
- Start the [Generating Requirements](#) subproject

## 4.1 Improvements to Manual Test Code

Even though this code will eventually be generated by Drasil, it is important that it is still human-readable, for the benefit of those reading the code later. This is one of the goals of Drasil (see [#3417](#) for an example of a similar issue). As such, the following improvements were discovered and implement in the manually created testing code:

- use `pytest`'s parameterization
- reuse functions/data for consistency
- improve import structure
- use `conftest` for running code before all tests of a module

### 4.1.1 Testing with Mocks

When testing code, it is common to first test lower-level modules, then assume that these modules work when testing higher-level modules. An example would be using an input module to set up test cases for a calculation module after testing the input module. This makes sense when writing test cases manually since it reduces the amount of code that needs to be written and still provides a reasonably high assurance in the software; if there is an issue with the input module that affects the calculation module tests, the issue would be revealed when testing the input module.

However, since these test cases will be generated by Drasil, they can be consistently generated with no additional effort. This means that the testing of each module can be done completely independently, increasing the confidence in the tests.

## 4.2 The Use of Assertions in Code

While assertions are often only used when testing, they can also be used in the code itself to enforce constraints or preconditions; they act like documentation that determines behaviour! For example, they could be used to ensure that assumptions about values (like the value for gravitational acceleration) are respected by the code, which gives a higher degree of confidence in the code.

## 4.3 Generating Requirements

I structured my manually created test cases around Projectile’s functional requirements, as these are the most objective aspects of the generated code to test automatically. One of these requirements was “Verify-Input-Values”, which said “Check the entered input values to ensure that they do not exceed the data constraints. If any of the input values are out of bounds, an error message is displayed and the calculations stop.” This led me to develop a test case to ensure that if an input constraint was violated, the calculations would stop ([Source Code A.1](#)).

However, this test case failed, since the actual implementation of the code did *not* stop upon an input constraint violation. This was because the code choice for what to do on a constraint violation ([Source Code A.2](#)) was “disconnected” from the manually written requirement ([Source Code A.3](#)), as described in [#3523](#).

This problem has been encountered before ([#3259](#)) and presented a good opportunity for generation to encourage reusability and consistency. However, since it makes sense to first verify outputs before actually outputting them and inserting generated requirements among manually created ones seemed challenging, it made sense to first generate an output requirement.

While working on Drasil in the summer of 2019, I implemented the generation of an input requirement across most examples ([#1844](#)). I had also attempted to generate an output requirement, but due to time constraints, this was not feasible. The main issue with this change was the desire to capture the source of each output for traceability; this source was attached to the `InstanceModel` (or rarely, `DataDefinition`) and not the underlying `Quantity` that was used for a program’s outputs. The way I had attempted to do this was to add the reference as a `Sentence` in a tuple.

Taking another look at this four years later allowed us to see that we should be storing the outputs of a program as their underlying models, allowing us to keep the source information with it. While there is some discussion about how this might change in the future, for now, all outputs of a program should be `InstanceModels`. Since this change required adding the Referable constraints to the output field of `SystemInformation`, the outputs of all examples needed to be updated to satisfy this constraint; this meant that generating the output requirement of each example was nearly trivial once the outputs were specified correctly. After modifying `DataDefinitions` in GlassBR that were outputs to be `InstanceModels` ([#3569](#); [#3583](#)), reorganizing the requirements of SWHS ([#3589](#); [#3607](#)), and clarifying the outputs of SWHS ([#3589](#)), `SglPend` ([#3533](#)), `DblPend` ([#3533](#)), `GamePhysics`

Should I include the definition of Constraints?

cite Dr. Smith

add refs to ‘underlying Theory’ comment and ‘not all outputs be IMs’ comment

add constraints

(#3609), and SSP (#3630), the output requirement was ready to be generated.

# Bibliography

- [1] Yannis Lilis and Anthony Savidis. “A Survey of Metaprogramming Languages”. In: *ACM Computing Surveys*. Vol. 52. Association for Computing Machinery, 2019-10, 113:1–40. DOI: <https://doi.org/10.1145/3354584> (cit. on pp. 7–15).
- [2] Vytautas Štuikys and Robertas Damaševičius. “Taxonomy of Fundamental Concepts of Meta-Programming”. In: *Meta-Programming and Model-Driven Meta-Program Development: Principles, Processes and Techniques*. London: Springer London, 2013, pp. 17–29. ISBN: 978-1-4471-4126-6. DOI: [10.1007/978-1-4471-4126-6\\_2](https://doi.org/10.1007/978-1-4471-4126-6_2). URL: [https://doi.org/10.1007/978-1-4471-4126-6\\_2](https://doi.org/10.1007/978-1-4471-4126-6_2) (cit. on pp. 8, 18, 19).
- [3] Krzysztof Czarnecki. “Overview of Generative Software Development”. In: *Unconventional Programming Paradigms*. Ed. by Jean-Pierre Banâtre, Pascal Fradet, Jean-Louis Giavitto, and Olivier Michel. Lecture Notes in Computer Science. Le Mont Saint Michel, France: Springer Berlin, Heidelberg, 2004-09, pp. 326–341. DOI: <https://doi.org/10.1007/11527800> (cit. on pp. 15, 16).
- [4] Yannis Smaragdakis, Aggelos Biboudis, and George Fourtounis. “Structured Program Generation Techniques”. In: *Grand Timely Topics in Software Engineering*. Ed. by Jácome Cunha, João P. Fernandes, Ralf Lämmel, João Saraiva, and Vadim Zaytsev. Cham: Springer International Publishing, 2017, pp. 154–178. ISBN: 978-3-319-60074-1 (cit. on pp. 16–19).
- [5] Upulee Kanewala and Tsong Yueh Chen. “Metamorphic Testing: A Simple Yet Effective Approach for Testing Scientific Software”. In: *Computing in Science & Engineering* 21.1 (2019), pp. 66–72. DOI: [10.1109/MCSE.2018.2875368](https://doi.org/10.1109/MCSE.2018.2875368) (cit. on pp. 19, 20, 33, 34).
- [6] Norman E. Fenton and Shari Lawrence Pfleeger. *Software Metrics: A Rigorous & Practical Approach*. 2nd ed. Boston, MA, USA: PWS Publishing Company, 1997. ISBN: 0-534-95425-1 (cit. on p. 20).
- [7] Ron Patton. *Software Testing*. 2nd ed. Indianapolis, IN, USA: Sams Publishing, 2006. ISBN: 0-672-32798-8 (cit. on pp. 20–31).
- [8] Hans van Vliet. *Software Engineering: Principles and Practice, 2nd Edition*. English. John Wiley & Sons, Ltd., 2000. ISBN: 0-471-97508-7 (cit. on pp. 20–24, 27–33).
- [9] W. Spencer Smith and Jacques Carette. Private Communication. Hamilton, ON, Canada, 2023-07 (cit. on pp. 23, 24).

# Appendix

## Source Code A.1: Tests for main with an invalid input file

---

```
# from
↳ https://stackoverflow.com/questions/54071312/how-to-pass-command-line-arguments
## \brief Tests main with invalid input file
# \par Types of Testing:
# Dynamic Black-Box (Behavioural) Testing
# Boundary Conditions
# Default, Empty, Blank, Null, Zero, and None
# Invalid, Wrong, Incorrect, and Garbage Data
# Logic Flow Testing
@mark.parametrize("filename", invalid_value_input_files)
@mark.xfail
def test_main_invalid(monkeypatch, filename):
    # from
    ↳ https://stackoverflow.com/questions/10840533/most-pythonic-way-to-delete-a-file
    try:
        remove(output_filename)
    except OSError as e: # this would be "except OSError, e:"
        ↳ before Python 2.6
        if e.errno != ENOENT: # no such file or directory
            raise # re-raise exception if a different error
                ↳ occurred

    assert not path.exists(output_filename)

    with monkeypatch.context() as m:
        m.setattr(sys, 'argv', ['Control.py',
            ↳ str(Path("test/test_input") / f"{filename}.txt")])
        Control.main()

    assert not path.exists(output_filename)
```

---

Source Code A.2: Projectile’s choice for constraint violation behaviour in code

---

```
srsConstraints = makeConstraints Warning Warning,
```

---

Source Code A.3: Projectile’s manually created input verification requirement

---

```
verifyParamsDesc = foldlSent [S "Check the entered", plural
  → inValue,
  S "to ensure that they do not exceed the" +:+. namedRef (datCon
    → [] []) (plural datumConstraint),
  S "If any of the", plural inValue, S "are out of bounds" `sC`
  S "an", phrase errMsg, S "is displayed" `S.andThe` plural
    → calculation, S "stop"]
```

---

Source Code A.4: “MultiDefinitions” (MultiDefn) Definition

---

```
-- | 'MultiDefn's are QDefinition factories, used for showing one
  → or more ways
-- we can define a QDefinition.
data MultiDefn e = MultiDefn{
  -- | UID
  _rUId :: UID,
  -- | Underlying quantity it defines.
  _qd :: QuantityDict,
  -- | Explanation of the different ways we can define a quantity.
  _rDesc :: Sentence,
  -- | All possible ways we can define the related quantity.
  _rvs :: NE.NonEmpty (DefiningExpr e)
}
```

---

Source Code A.5: Pseudocode: Broken QuantityDict Chunk Retriever

---

```
retrieveQD :: UID -> ChunkDB -> Maybe QuantityDict
retrieveQD u cdb = do
  (Chunk expectedQd) <- lookup u cdb
  pure expectedQd
```

---