



Operating Systems

Virtual Memory-Page Replacement

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What Happens if There is no Free Frame?

- Used up by process pages
- Also in demand from the kernel, I/O buffers, etc
- How much to allocate to each?



What Happens if There is no Free Frame? (cont.)

- Page replacement – find some page in memory, but not really in use, page it out
 - Algorithm – terminate? swap out? replace the page?
 - Performance – want an algorithm which will result in minimum number of page faults

- Same page may be brought into memory several times

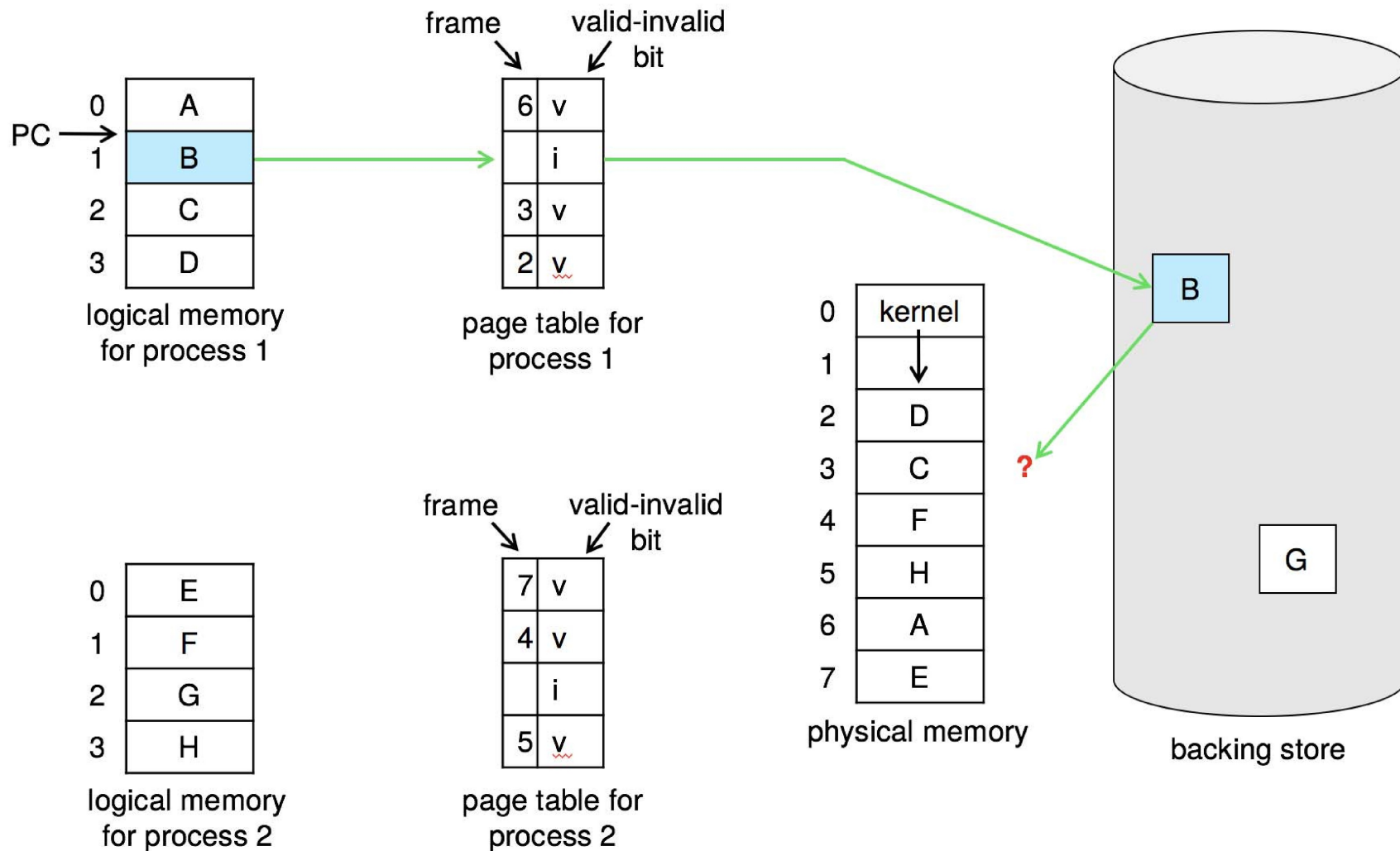


Page Replacement

- Prevent **over-allocation** of memory by modifying page-fault service routine to include page replacement
- Use **modify (dirty) bit** to reduce overhead of page transfers – only modified pages are written to disk.
- Page replacement completes separation between logical memory and physical memory
 - Large virtual memory can be provided on a smaller physical memory.



Need For Page Replacement



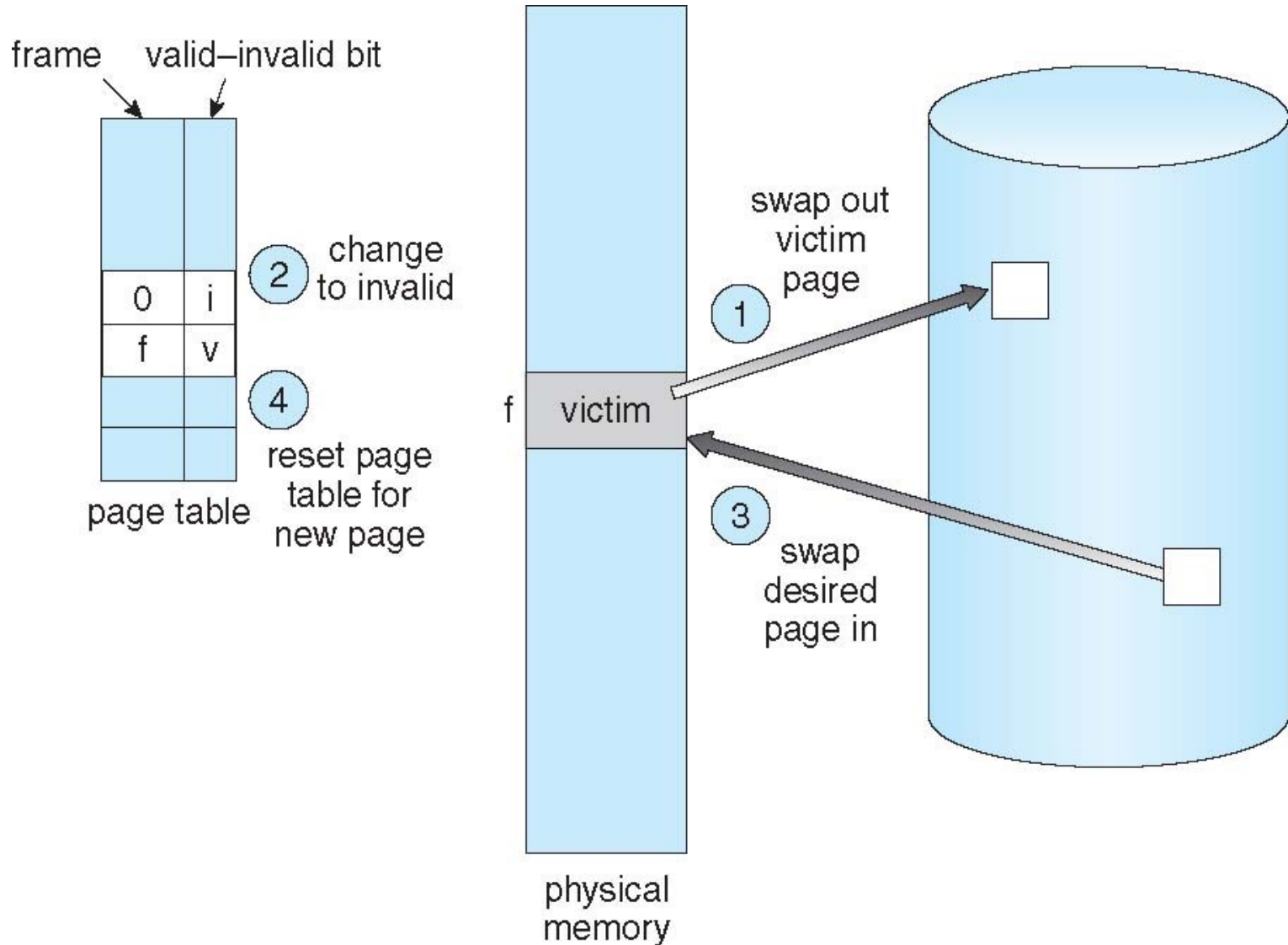
Basic Page Replacement

1. Find the location of the desired page on disk
2. Find a free frame:
 - If there is a free frame, use it
 - If there is no free frame, use a page replacement algorithm to select a *victim frame*
 - Write victim frame to disk if dirty
3. Bring the desired page into the (newly) free frame; update the page and frame tables
4. Continue the process by restarting the instruction that caused the trap

Note now potentially 2 page transfers for page fault – increasing EAT



Page Replacement



Page and Frame Replacement Algorithms

- **Frame-allocation algorithm** determines
 - How many frames to give each process
 - Which frames to replace

- **Page-replacement algorithm**
 - Want lowest page-fault rate on both first access and re-access



Page and Frame Replacement Algorithms

- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string
 - String is just page numbers, not full addresses
 - Repeated access to the same page does not cause a page fault
 - Results depend on ***number of frames available***



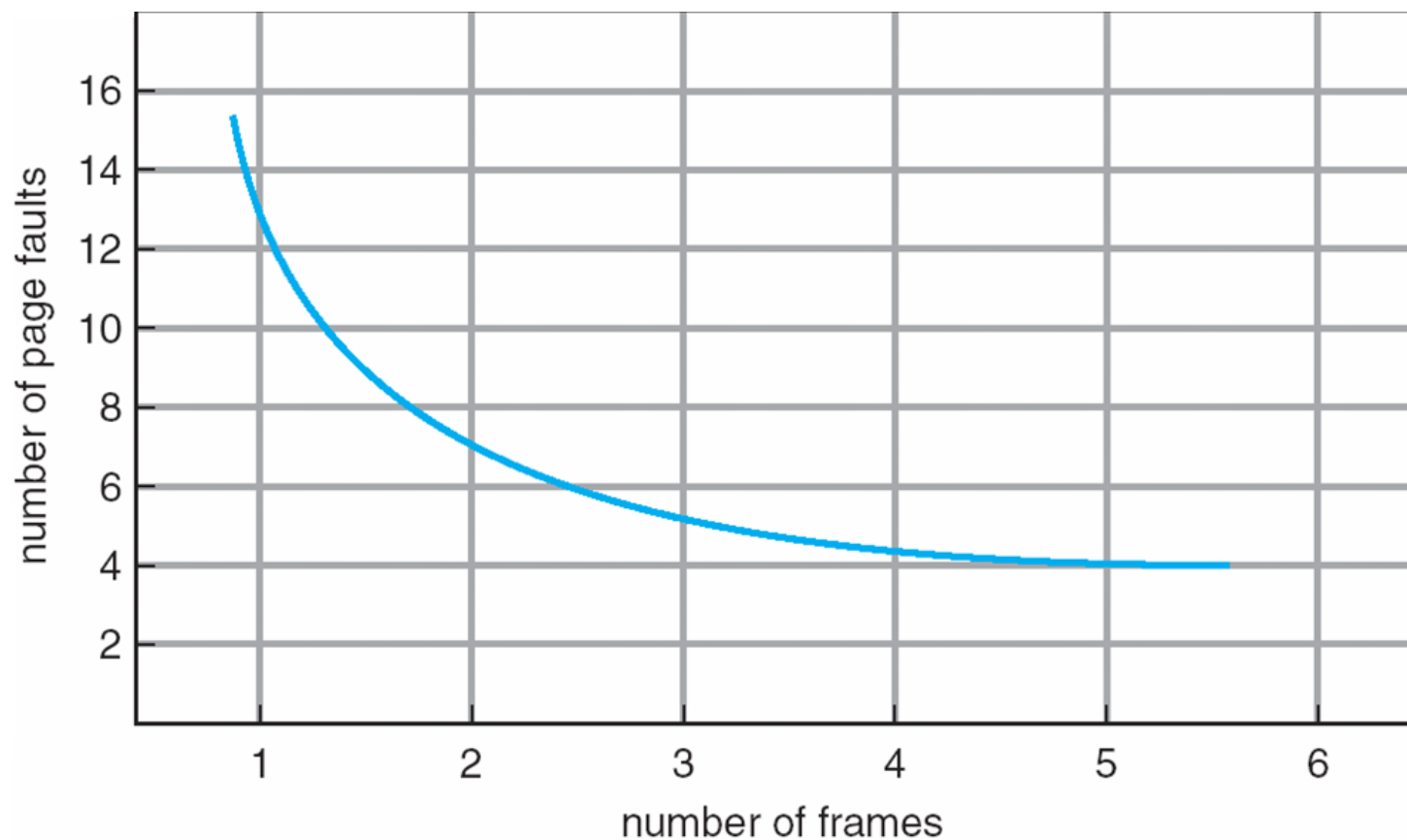
Page and Frame Replacement Algorithms (cont.)

- In all our examples, the **reference string** of referenced page numbers is

7,0,1,2,0,3,0,4,2,3,0,3,0,3,2,1,2,0,1,7,0,1



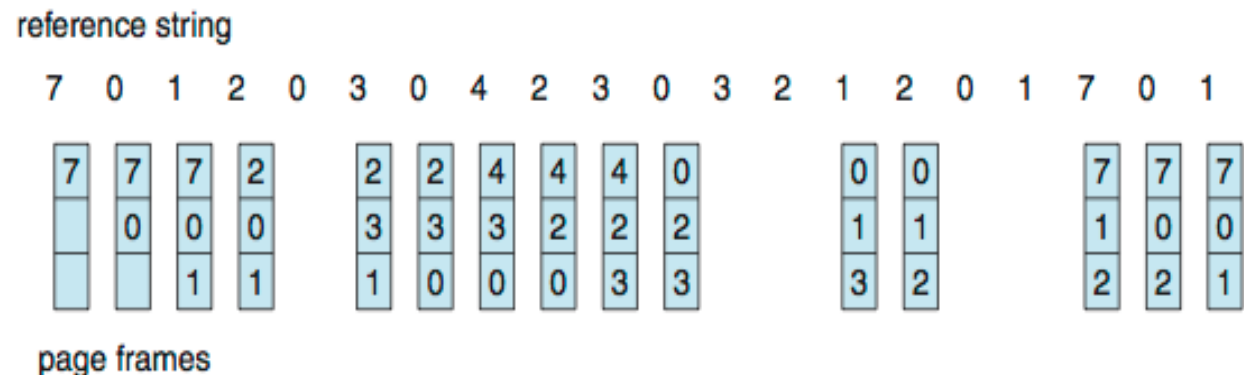
Graph of Page Faults Versus the Number of Frames



First-In-First-Out (FIFO) Algorithm

- Reference string: **7,0,1,2,0,3,0,4,2,3,0,3,0,3,2,1,2,0,1,7,0,1**
- 3 frames (3 pages can be in memory at a time per process)
- How many page faults?

15 page faults

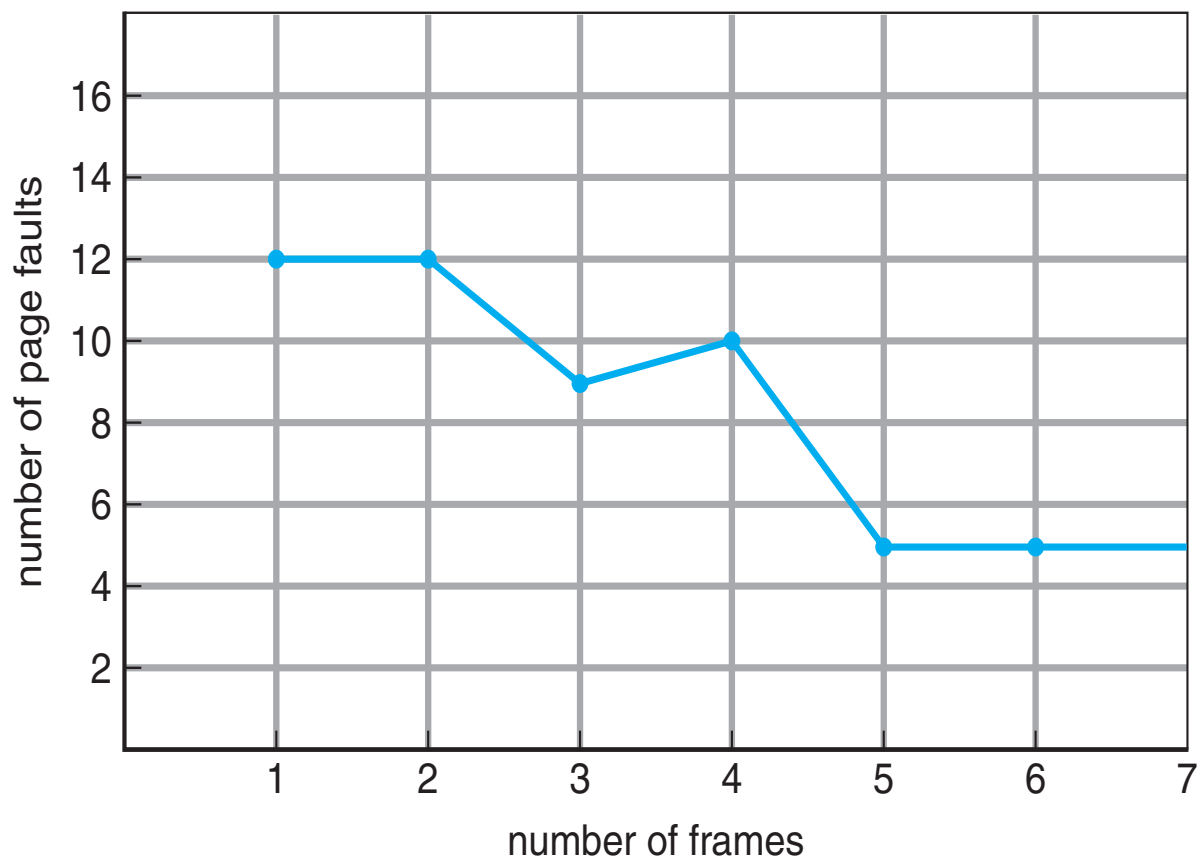


First-In-First-Out (FIFO) Algorithm

- Can vary by reference string: consider 1,2,3,4,1,2,5,1,2,3,4,5
 - Adding more frames can cause more page faults!
 - ▶ **Belady's Anomaly**
 - for some page-replacement algorithms, the page-fault rate may increase as the number of allocated frames increases



FIFO Illustrating Belady's Anomaly



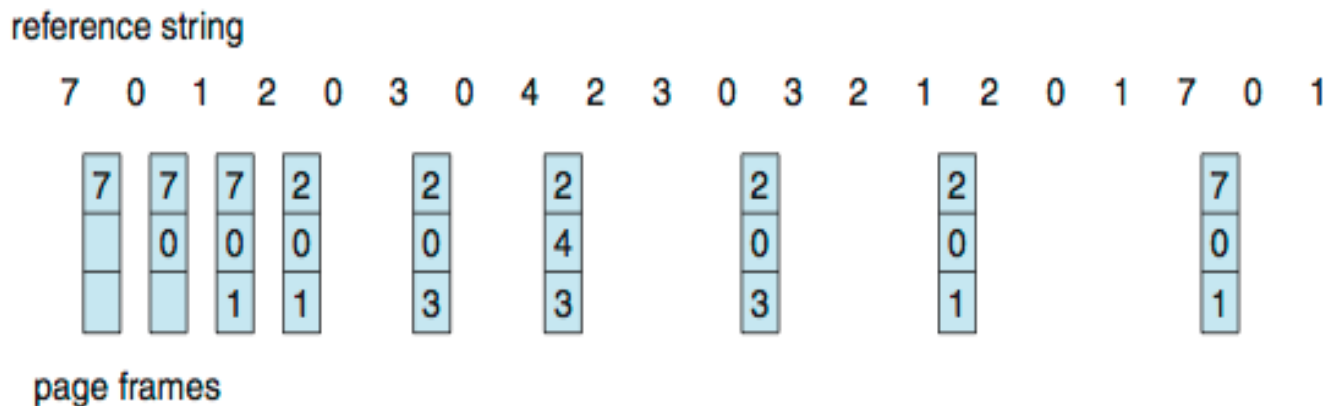
First-In-First-Out (FIFO) Algorithm

- Can vary by reference string: consider 1,2,3,4,1,2,5,1,2,3,4,5
 - Adding more frames can cause more page faults!
 - ▶ **Belady's Anomaly**
 - for some page-replacement algorithms, the page-fault rate may increase as the number of allocated frames increases
- How to track ages of pages?
 - Just use a FIFO queue



Optimal Algorithm

- Replace page that will not be used for longest period of time
 - 9 is optimal for the example



- How do you know this?
 - Can't read the future
- Used for measuring how well your algorithm performs

Least Recently Used (LRU) Algorithm

- Use past knowledge rather than future
- Replace page that has not been used in the most amount of time
- Associate time of last use with each page

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		4	4	4	0		1		1		1
	0	0	0		0		0	0	3	3		3		0		0
		1	1		3		3	2	2	2		2		2		7

page frames

- 12 faults – better than FIFO but worse than OPT
- Generally good algorithm and frequently used
- But how to implement?

LRU Algorithm (cont.)

■ Counter implementation

- Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter
- When a page needs to be changed, look at the counters to find smallest value
 - ▶ Search through table needed



LRU Algorithm (cont.)

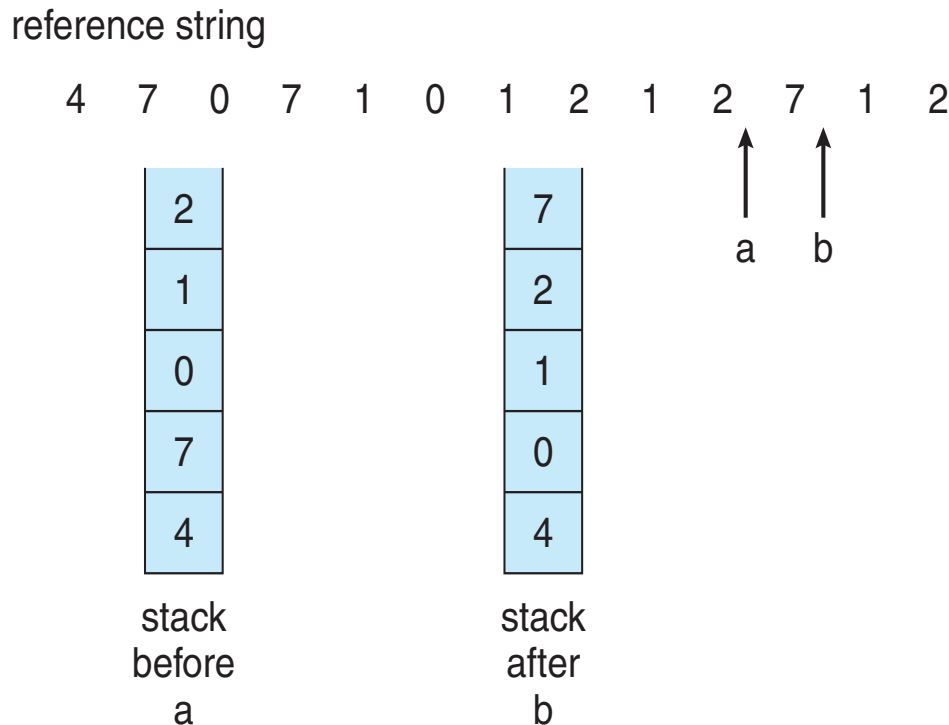
■ Stack implementation

- Keep a stack of page numbers in a double link form:
- Page referenced:
 - ▶ move it to the top
 - ▶ requires 6 pointers to be changed
- But each update more expensive
- No search for replacement



LRU Algorithm (Cont.)

- LRU and OPT are cases of **stack algorithms** that don't have Belady's Anomaly
- Use Of A Stack to Record Most Recent Page References



LRU Approximation Algorithms

- LRU needs special hardware and still slow
- **Reference bit**
 - With each page associate a bit, initially = 0
 - When page is referenced bit set to 1
 - Replace any with reference bit = 0 (if one exists)
 - ▶ We do not know the order, however



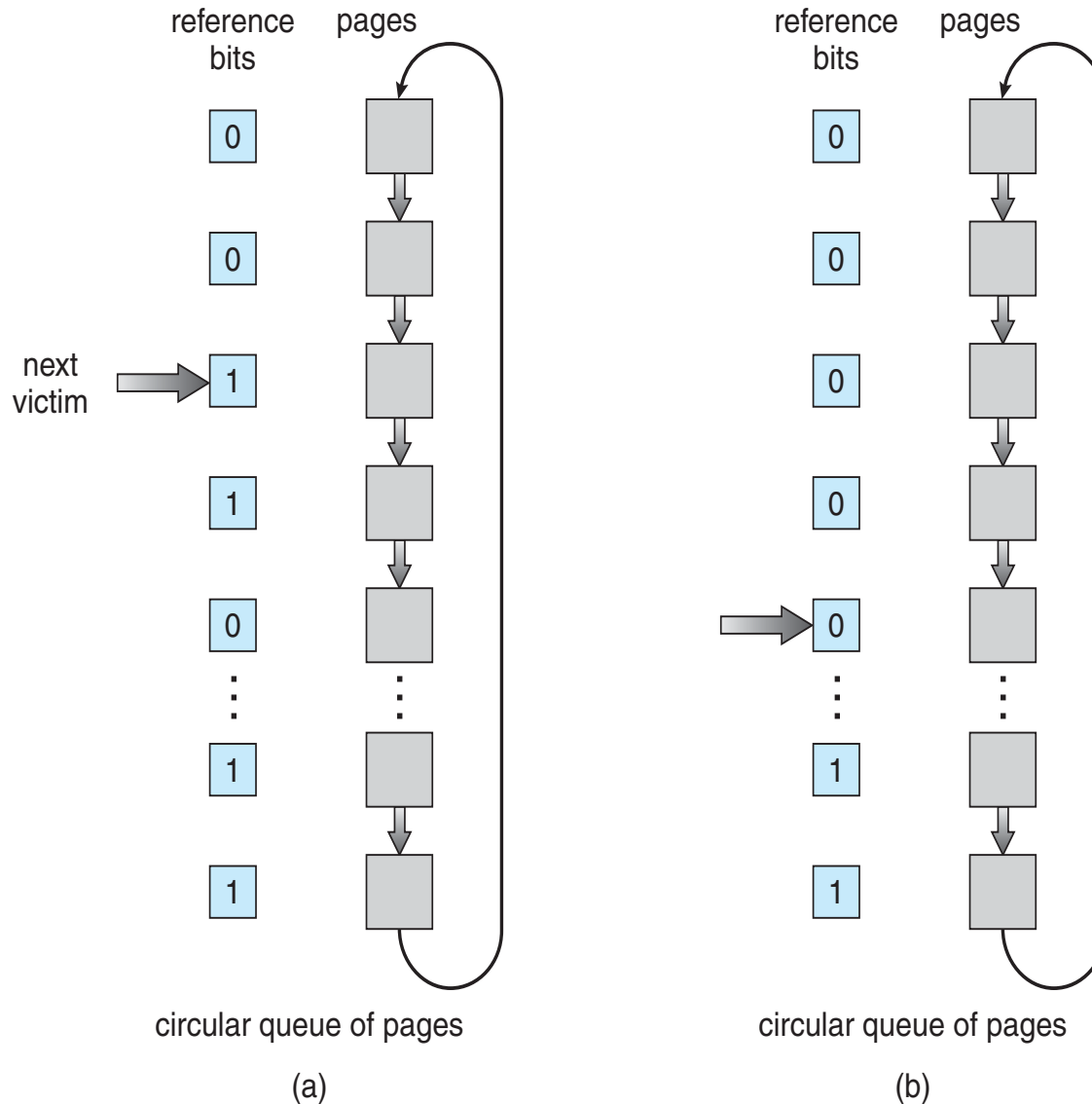
LRU Approximation Algorithms (cont.)

■ Second-chance algorithm

- Generally FIFO, plus hardware-provided reference bit
- **Clock** replacement
- If page to be replaced has
 - ▶ Reference bit = 0 -> replace it
 - ▶ reference bit = 1 then:
 - set reference bit 0, leave page in memory
 - replace next page, subject to same rules



Second-chance Algorithm



Enhanced Second-Chance Algorithm

- Improve algorithm by using reference bit and modify bit (if available)
- Take ordered pair (reference, modify):
 1. (0, 0) neither recently used nor modified – best page to replace
 2. (0, 1) not recently used but modified – not quite as good, must write out before replacement
 3. (1, 0) recently used but clean – probably will be used again soon
 4. (1, 1) recently used and modified – probably will be used again soon and need to write out before replacement



Enhanced Second-Chance Algorithm (cont.)

- When page replacement called for, use the clock scheme but use the four classes.
- Replace page in lowest non-empty class
 - Might need to search circular queue several times
- The major difference between this algorithm and the simpler clock algorithm is that here we give preference to those pages that have been modified to reduce the number of I/Os required.

