# Another approach

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So far, I have not been able to really find a good approach that works consistently. There appears to be some challenges when trying to estimate  $\alpha$  using the pairwise likelihood. Based on some of my previous research, it would appear that the pairwise likelihood does a reasonably good job estimating the bandwidth term  $\rho$ . Brian and I had originally discussed fixing both  $\rho$  and  $\alpha$  in the simulation study, because when they're fixed, we can outperform spatial probit and logit. The purpose of this document is to explore what happens when we search over a grid of  $\rho$  terms and fix rho in the MCMC to arg min $_{\rho}\ell$ .

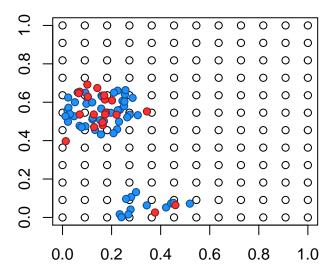
### Setting 1:

 $\alpha = 0.2, \pi = 0.05, \rho = 0.15$ 

#### Dataset 1

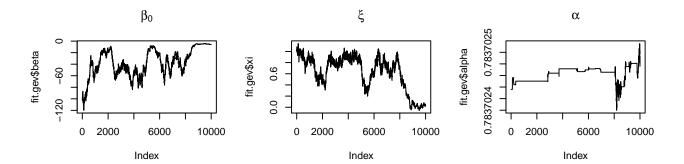
From the pairwise likelihood, we'll be using  $\rho = 0.1429$ . The estimates for the other parameters are  $\hat{\alpha} = 0.746$ ,  $\hat{\xi} = 0.166$ , and  $\hat{\beta}_0 = -3.879$ .

### simulated dataset



### MCMC Results

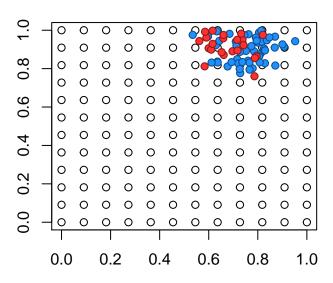
Here are the iteration plots from the two GEV models. The true values are  $\beta_0 = -4.407$ , and  $\xi = 0.25$ .



Dataset 2

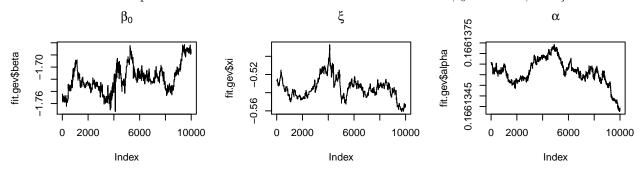
From the pairwise likelihood, we'll be using  $\rho = 0.1429$ . The estimates for the other parameters are  $\hat{\alpha} = 0.167$ ,  $\hat{\xi} = 0.171$ , and  $\hat{\beta}_0 = -3.964$ .

# simulated dataset



### MCMC Results

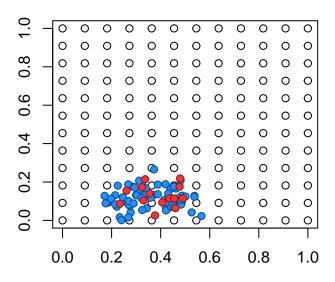
Here are the iteration plots from the two GEV models. The true values are  $\beta_0 = -8.297$ , and  $\xi = 0.25$ .



Dataset 3

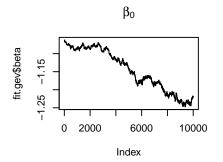
From the pairwise likelihood, we'll be using  $\rho = 0.1429$ . The estimates for the other parameters are  $\hat{\alpha} = 0.233$ ,  $\hat{\xi} = 0.148$ , and  $\hat{\beta}_0 = -3.597$ .

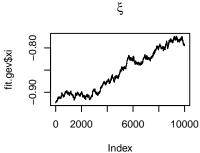
# simulated dataset

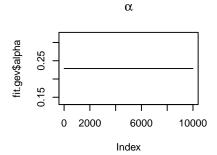


### MCMC Results

Here are the iteration plots from the two GEV models. The true values are  $\beta_0 = -11.026$ , and  $\xi = 0.25$ .







### **Brier Scores**

The brier scores are

Logit 1-1: 0.0296

Probit 1-1: 0.0273

GEV 1-1: 0.0327

The brier scores are

Logit 2-1: 0.0088

Probit 2-1: 0.009

GEV 2-1: 0.0069

The brier scores are

Logit 3-1: 0.0112

Probit 3-1: 0.01

GEV 3-1: 0.0373

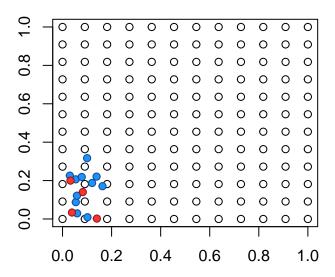
### Setting 2:

$$\alpha = 0.2, \pi = 0.01, \rho = 0.15$$

#### Dataset 1

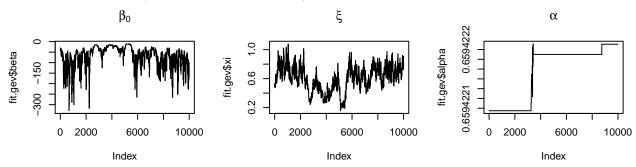
From the pairwise likelihood, we'll be using  $\rho = 0.1429$ . The estimates for the other parameters are  $\hat{\alpha} = 0.849$ ,  $\hat{\xi} = -0.044$ , and  $\hat{\beta}_0 = -4.179$ .

### simulated dataset



#### MCMC Results

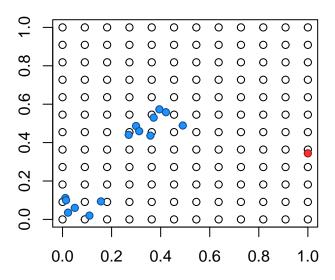
Here are the iteration plots from the two GEV models. The true values are  $\beta_0 = -3.901$ , and  $\xi = 0.25$ . The estimates for the other parameters are  $\hat{\alpha} = 0.849$ ,  $\hat{\xi} = -0.044$ , and  $\hat{\beta}_0 = -4.179$ .



#### Dataset 2

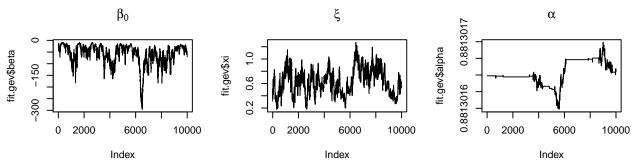
From the pairwise likelihood, we'll be using  $\rho=0.1071$ . The estimates for the other parameters are  $\widehat{\alpha}=0.902$ ,  $\widehat{\xi}=-0.022$ , and  $\widehat{\beta}_0=-4.178$ .

# simulated dataset



### MCMC Results

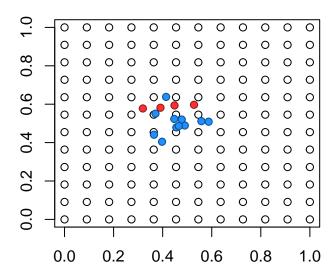
Here are the iteration plots from the two GEV models. The true values are  $\beta_0 = -3.052$ , and  $\xi = 0.25$ .



Dataset 3

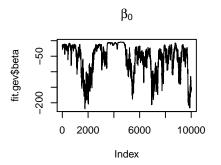
From the pairwise likelihood, we'll be using  $\rho=0.1071$ . The estimates for the other parameters are  $\widehat{\alpha}=0.87$ ,  $\widehat{\xi}=-0.046$ , and  $\widehat{\beta}_0=-4.164$ .

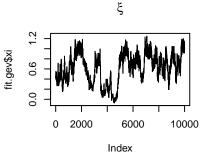
# simulated dataset

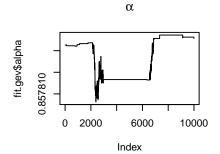


### MCMC Results

Here are the iteration plots from the two GEV models. The true values are  $\beta_0 = -4.297$ , and  $\xi = 0.25$ .







### **Brier Scores**

The brier scores are

Logit 1-2: 10.56

Probit 1-2: 8.61

GEV 1-2: 10.66

The brier scores are

Logit 2-2: 2.75

Probit 2-2: 3.19

GEV 2-2: 2.65

The brier scores are

Logit 3-2: 10.81

Probit 3-2: 10.68

GEV 3-2: 10.61