

# Knot Spacing and Bandwidth Sim

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## Small-scale simulation study on knots and bandwidth

We tried two different true knot spacings in this simulation study. The first spacing sets knots on a  $20 \times 20$  grid in  $[0, 1] \times [0, 1]$ . The second spacing sets knots on a  $10 \times 10$  grid in  $[0, 1] \times [0, 1]$ . We used three different data generation settings.

1.  $\rho = 0.01$  and  $\pi = 0.01$  with  $n_s = 2000$  sites.
2.  $\rho = 0.01$  and  $\pi = 0.05$  with  $n_s = 1000$  sites.
3.  $\rho = 0.02$  and  $\pi = 0.05$  with  $n_s = 1000$  sites.

These all set  $\rho$  to be the knot spacing used in fitting the GEV which is a  $12 \times 12$  grid.

**Setting 1:  $\rho = 0.01$  and  $\pi = 0.01$  with  $n_s = 2000$  sites.**

Table 1: Results (x 100) for Knots:  $20 \times 20$ ,  $\rho = 0.01$ ,  $\pi = 0.01$

	gev	log	pro
<b>1</b>	0.8169	0.7943	0.5434
<b>2</b>	0.3942	0.3978	0.3003
<b>3</b>	0.395	0.4021	0.1733
<b>4</b>	1.572	1.584	1.467
<b>5</b>	0.6053	0.5993	0.5551
<b>6</b>	0.7402	0.5868	0.4869
<b>7</b>	0.7078	0.4031	0.1996
<b>8</b>	0.9244	0.9901	0.4497
<b>9</b>	0.9582	0.99	0.6775
<b>10</b>	0.02199	0.01915	0.2385
<b>Mean</b>	0.7136	0.6767	0.5092

Table 2: Results (x 100) for Knots:  $10 \times 10$ ,  $\rho = 0.01$ ,  $\pi = 0.01$

	gev	log	pro
<b>1</b>	1.04	0.9867	0.9219
<b>2</b>	1.103	1.186	0.9529
<b>3</b>	0.7178	0.7352	0.9585
<b>4</b>	0.2137	0.1602	0.1837
<b>5</b>	0.5744	0.99	0.3817
<b>6</b>	0.8611	0.99	0.81
<b>7</b>	0.9304	0.8974	0.699
<b>8</b>	0.9253	1.186	0.8368
<b>9</b>	0.3633	0.361	0.341
<b>10</b>	1.146	0.4713	0.3015
<b>Mean</b>	0.7876	0.7964	0.6387

**Setting 2:  $\rho = 0.01$  and  $\pi = 0.05$  with  $n_s = 1000$  sites.**

Table 3: Results (x 100) for Knots:  $20 \times 20$ ,  $\rho = 0.01$ ,  $\pi = 0.05$

	gev	log	pro
<b>1</b>	4.11	3.135	3.078

	gev	log	pro
<b>2</b>	5.155	4.788	4.367
<b>3</b>	4.693	4.306	4.361
<b>4</b>	4.482	4.608	4.517
<b>5</b>	3.856	3.857	3.05
<b>6</b>	4.522	4.115	3.464
<b>7</b>	4.421	4.296	4.495
<b>8</b>	6.014	6.404	5.512
<b>9</b>	4.925	4.92	4.717
<b>10</b>	4.1	3.63	3.679
<b>Mean</b>	4.628	4.406	4.124

Table 4: Results (x 100) for Knots: 10 x 10,  $\rho = 0.01$ ,  $\pi = 0.05$

	gev	log	pro
<b>1</b>	2.755	1.857	1.72
<b>2</b>	1.937	1.412	1.499
<b>3</b>	2.432	3.151	1.059
<b>4</b>	2.284	1.354	1.453
<b>5</b>	4.473	3.681	3.076
<b>6</b>	5.104	3.099	3.978
<b>7</b>	1.969	1.504	1.589
<b>8</b>	3.331	1.909	2.023
<b>9</b>	3.072	2.027	1.459
<b>10</b>	2.644	4.571	1.911
<b>Mean</b>	3	2.457	1.977

**Setting 3:**  $\rho = 0.02$  and  $\pi = 0.05$  with  $n_s = 1000$  sites.

Table 5: Results (x 100) for Knots: 20 x 20,  $\rho = 0.02$ ,  $\pi = 0.05$

	gev	log	pro
<b>1</b>	4.305	3.376	2.87
<b>2</b>	4.718	3.846	3.149
<b>3</b>	5.299	4.085	3.873
<b>4</b>	3.494	3.705	3.594
<b>5</b>	2.792	3.502	2.362
<b>6</b>	4.218	3.22	1.843
<b>7</b>	3.71	3.904	4.475
<b>8</b>	5.21	6.035	4.373
<b>9</b>	3.157	3.315	3.176
<b>10</b>	4.028	3.307	3.233
<b>Mean</b>	4.093	3.83	3.295

Table 6: Results (x 100) for Knots: 10 x 10,  $\rho = 0.02$ ,  $\pi = 0.05$

	gev	log	pro
<b>1</b>	2.689	1.768	1.402
<b>2</b>	1.74	1.312	1.533
<b>3</b>	2.454	3.151	1.083
<b>4</b>	2.47	1.738	1.955
<b>5</b>	5.069	3.426	2.772
<b>6</b>	5.193	3.316	3.024
<b>7</b>	2.368	1.874	2.083
<b>8</b>	3.374	1.289	1.203
<b>9</b>	3.059	2.352	1.918
<b>10</b>	2.614	2.021	1.586
<b>Mean</b>	3.103	2.225	1.856

## Next steps

Fit a few datasets with  $\rho$  as a parameter in the MCMC.