

BIRLA INSTITUTE OF TECHNOLOGY & SCIENCE, PILANI (RAJASTHAN)

I Sem/II Sem/Summer Term 2016 - 2017

TEST/Quiz Mid Semester

Sec. No. _____

ID No _____

Name _____

Course No. EEE E111

Course Title Electrical Sciences

Instructor's Name _____

Date 10/10/2017

Day Tuesday

No. of Supplementary copies attached : —

Question No.	Marks obtained	Student's request for rechecking with remarks	Examiner's remarks
1.	20		
2.	20		
3.	25		
4.	15+25		
5.			
6.			
7.			
8.			
Total	105 (in figures)	(in words)	

INSTRUCTIONS TO CANDIDATES

Examiner's Signature _____

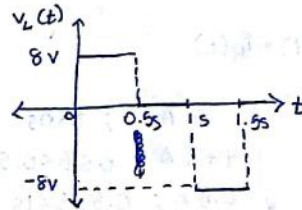
(1) Write clearly and legibly. (2) Enter all the required details on the cover of every answer book. (3) The question number given in the answersheet by the student while answering the question should be the same as in the question paper. (4) Start answering every question from a new page. (5) Write on both sides of the sheet in the answer book. Rough work if any, should be done at the bottom of the page. Finally cross it out and draw a horizontal line to separate it from the rest of the material on the page. (6) Any answer crossed out by the student will not be examined by the examiner. (7) A supplementary answer book should not be asked for until the first answer book is filled up. (8) No sheet should be torn from the answer book. (9) Use of any unfair means will make the candidate liable to disciplinary action. (10) No paper should be brought in the examination hall for scribbling on. (11) A student should not leave the examination hall without handing over the answer book to invigilator on duty.

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$$1. \quad i_L(t) = \begin{cases} 0 \text{ A} ; t < 0 \text{ s} \\ t \text{ A} ; 0 \leq t < 0.5 \text{ s} \\ 0.5 \text{ A} ; 0.5 \leq t < 1 \text{ s} \\ (1.5 - t) \text{ A} ; 1 \leq t < 1.5 \text{ s} \\ 0 \text{ A} ; t \geq 1.5 \text{ s} \end{cases}$$

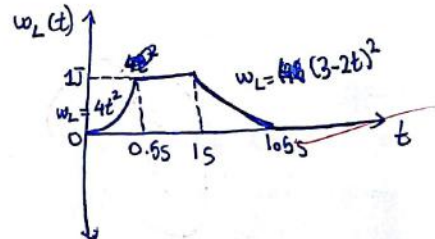
$$(a) \quad v(t) = L \frac{di_L(t)}{dt} \quad [L = 8 \text{ H}]$$

$$= \begin{cases} 0 \text{ V} ; t < 0 \text{ s} \\ 8 \text{ V} ; 0 \leq t < 0.5 \text{ s} \\ 0 \text{ V} ; 0.5 \leq t < 1 \text{ s} \\ -8 \text{ V} ; 1 \leq t < 1.5 \text{ s} \\ 0 \text{ V} ; t \geq 1.5 \text{ s} \end{cases}$$

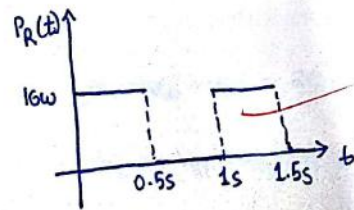


$$(b) \quad w_L(t) = \frac{1}{2} L [i_L(t)]^2$$

$$= \begin{cases} 0 \text{ J} ; t < 0 \text{ s} \\ 4t^2 \text{ J} ; 0 \leq t < 0.5 \text{ s} \\ 1 \text{ J} ; 0.5 \leq t < 1 \text{ s} \\ 4(1.5 - t)^2 \text{ J} ; 1 \leq t < 1.5 \text{ s} \\ 0 \text{ J} ; t \geq 1.5 \text{ s} \end{cases}$$

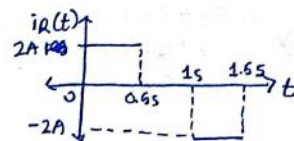


$$(c) \quad P_R(t) = \frac{[v(t)]^2}{R} = \begin{cases} 0 \text{ W} ; t < 0 \text{ s} \\ 16 \text{ W} ; 0 \leq t < 0.5 \text{ s} \\ 0 \text{ W} ; 0.5 \leq t < 1 \text{ s} \\ 16 \text{ W} ; 1 \leq t < 1.5 \text{ s} \\ 0 \text{ W} ; t \geq 1.5 \text{ s} \end{cases}$$



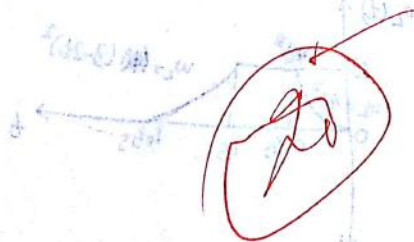
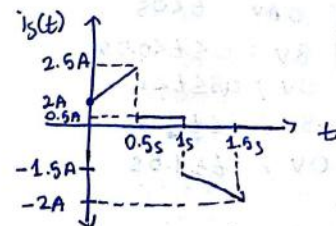
$$(d) i_R(t) = \frac{v_R(t)}{R}$$

$$= \begin{cases} 0A & ; t < 0.5 \\ 2A & ; 0.5 \leq t < 1.5 \\ 0A & ; 1.5 \leq t < 1.65 \\ -2A & ; 1.65 \leq t < 1.8 \\ 0A & ; t \geq 1.8 \end{cases}$$



$$(e) i_s(t) = i_L(t) + i_R(t)$$

$$= \begin{cases} 0A & ; t < 0.5 \\ t+2A & ; 0.5 \leq t < 1.5 \\ 0.5A & ; 1.5 \leq t < 1.65 \\ -(t+0.5)A & ; 1.65 \leq t < 1.8 \\ 0A & ; t \geq 1.8 \end{cases}$$



2.

Considering contribution of 10V source

$$V_{y1} = 0 \text{ V}$$

[in parallel with short circuit]

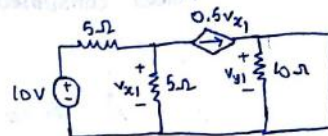
KCL at node V_{x1}

$$\frac{V_{x1} - 10}{5} + \frac{V_{x1}}{5} + \frac{V_{x1}}{2} = 0$$

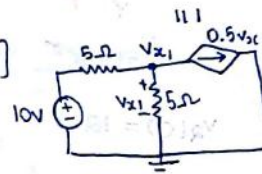
$$\frac{2V_{x1}}{5} + \frac{V_{x1}}{2} = 2$$

$$\frac{9V_{x1}}{10} = 2$$

$$V_{x1} = \frac{20}{9} \text{ V}$$



$$[0.5V_{x1} = \frac{V_{x1}}{2}]$$



Power consumed by
 $R_L = V_{x1} \times$

Considering contribution of 5V source

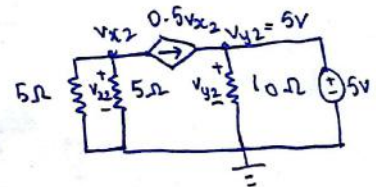
KCL at node V_{x2}

$$\frac{V_{x2}}{5} + \frac{V_{x2}}{5} + 0.5V_{x2} = 0$$

$$V_{x2} = 0 \text{ V}$$

KCL at node V_{y2}

$$V_{y2} = 5 \text{ V}$$



$$V_x = V_{x1} + V_{x2} = \frac{20}{9} \text{ V}$$

$$V_y = V_{y1} + V_{y2} = 5 \text{ V}$$

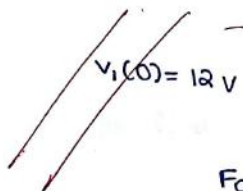
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Power consumed = ~~$v_x v_y$~~ $(v_x - v_y) \times 0.6 v_x$

$$= \left(\frac{20}{9} - 5\right) \times \frac{10}{9}$$

$$= -\frac{250}{81} \text{ W}$$

3.

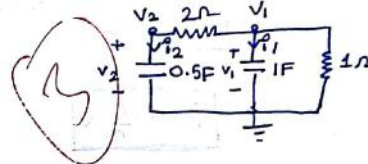


$$v_2(0) = 12 \text{ V}$$

For $t \geq 0$

KCL at v_1

$$\frac{v_1}{1} + i_1 + i_2 = 0 \quad \text{--- (1)}$$



$$i_2 = \frac{v_1 - v_2}{2} = \frac{1}{2} \frac{dv_1 - dv_2}{dt} \quad \text{--- (2)} \quad [i = C \frac{dv}{dt}]$$

$$v_1 = v_2 + \frac{dv_2}{dt} \quad \text{--- (3)}$$

$$i_1 = \frac{dv_1}{dt} \quad \text{--- (4)}$$

In (1),

$$v_1 + \frac{dv_1}{dt} + \frac{v_1 - v_2}{2} = 0 \Rightarrow \frac{3v_1}{2} + \frac{dv_1}{dt} = \frac{v_2}{2}$$

$$\frac{3}{2} [v_2 + \frac{dv_2}{dt}] + \frac{d}{dt} [v_2 + \frac{dv_2}{dt}] = \frac{v_2}{2}$$

$$\frac{dv_1}{dt} + \frac{dv_1}{dt} = v_2 \quad \text{--- (from (3))}$$

$$2 \left[v_2 + \frac{dv_2}{dt} \right] + \frac{d}{dt} \left[v_2 + \frac{dv_2}{dt} \right] = v_2$$

$$\frac{d^2 v_2}{dt^2} + \frac{5}{2} \frac{dv_2}{dt} + v_2 = 0$$

3

$$2\alpha = \frac{5}{2}$$

$$\alpha = \frac{5}{4}$$

$$\omega_n^2 = 1$$

$$\omega_n = 1 \text{ rad/s}$$

$\alpha > \omega_n \Rightarrow$ Overdamped response

$$s_1 = -\alpha - \sqrt{\alpha^2 - \omega_n^2} = -\frac{5}{4} - \sqrt{\frac{25}{16} - 1}$$

$$= -\frac{5}{4} - \frac{3}{4} = -2$$

$$s_2 = -\alpha + \sqrt{\alpha^2 - \omega_n^2} = -\frac{5}{4} + \sqrt{\frac{25}{16} - 1}$$

$$= -\frac{5}{4} + \frac{3}{4} = -\frac{1}{2}$$

$$v_2(t) = A_1 e^{s_1 t} + A_2 e^{s_2 t}$$

$$= A_1 e^{-2t} + A_2 e^{-t/2} \text{ V}$$

$$v_2(0) = 12 \text{ V} \Rightarrow A_1 + A_2 = 12 \text{ --- (1)}$$

$$v_1(t) = v_2 + \frac{dv_2}{dt} = A_1 e^{-2t} + A_2 e^{-t/2} - 2A_1 e^{-2t} - \frac{A_2}{2} e^{-t/2}$$

$$= -A_1 e^{-2t} + \frac{A_2}{2} e^{-t/2}$$

$$v_1(0) = 12 \text{ V} \Rightarrow -A_1 + \frac{A_2}{2} = 12 \text{ --- (2)}$$

$$A_1 = -4 \quad A_2 = 16$$

$$v_2(t) = -4e^{-2t} + 16e^{-t/2} \text{ V}$$

$$v_1(t) = \begin{cases} 12 \text{ V} & ; t < 0 \text{ s} \\ 4e^{-2t} + 8e^{-t/2} \text{ V} & ; t > 0 \text{ s} \end{cases}$$

$$v_2(t) = \begin{cases} 12 \text{ V} & ; t < 0 \text{ s} \\ -4e^{-2t} + 16e^{-t/2} \text{ V} & ; t > 0 \text{ s} \end{cases}$$

$$v_1(t) = 4e^{-2t} + 8e^{-t/2} \text{ V}$$

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4. (A)

$$Z_1 = Z_C \parallel Z_R$$

$$= \frac{R \left(\frac{1}{j\omega C} \right)}{R + \frac{1}{j\omega C}} = \frac{R}{1 + j\omega CR}$$

$$Z_2 = 2R \parallel 2R = \frac{2R \times 2R}{4R} = R$$

By voltage division

$$V_2 = \frac{R}{R + Z_1} \times V_1$$

$$V_2 = \frac{R}{R + \frac{R}{1 + j\omega CR}} \times V_1 = \frac{R}{R + \frac{R}{1 + j\omega CR}} V_1$$

$$= \frac{R(1 + j\omega CR)}{R(2 + j\omega CR)} V_1$$

$$\frac{V_2}{V_1} = \frac{1 + j\omega CR}{2 + j\omega CR}$$

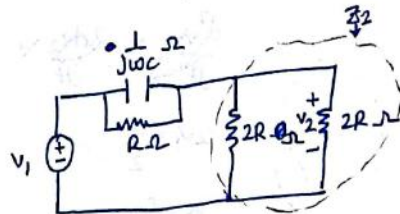
$$H(j\omega) = \left| \frac{V_2}{V_1} \right| = \sqrt{\frac{1 + \omega^2 C^2 R^2}{4 + \omega^2 C^2 R^2}}$$

$$H(\omega) = \frac{1}{2} \quad H(\infty) = 1$$

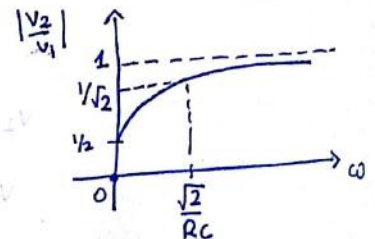
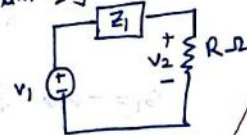
$$H(j\omega_c) = \frac{1}{\sqrt{2}} \times H(\infty) = \frac{1}{\sqrt{2}} = \sqrt{\frac{1 + \omega_c^2 R^2 C^2}{4 + \omega_c^2 R^2 C^2}}$$

$$4 + \omega_c^2 R^2 C^2 = 2 + 2\omega_c^2 R^2 C^2$$

$$2 = \omega_c^2 R^2 C^2 \Rightarrow \omega_c = \frac{\sqrt{2}}{RC} \text{ rad/s}$$



[Voltage across it] will remain V_2



(B)

By current division,

$$i_{AN} = \frac{Z_{CN}}{Z_{CN} + Z_{BN}} i_{AN} = \frac{Z}{Z + Z} i_{AN}$$

$$3 \angle -70^\circ = \frac{i_{AN}}{2}$$

$$i = i_{AN} = 6 \angle -70^\circ \text{ A (rms)}$$

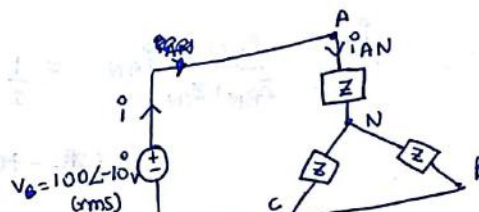
$$\begin{aligned} \theta &= \angle V - \angle i \\ &= (-10^\circ) - (-70^\circ) \\ &= 60^\circ \end{aligned}$$

$$\text{P.F.} = \cos \theta = \cos 60^\circ = 0.5$$

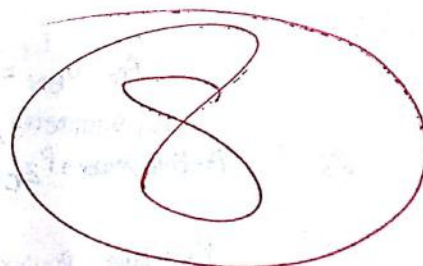
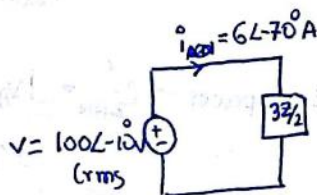
$$\begin{aligned} \text{(b)} \quad Z_{eq} &= Z_{AN} + (Z_{BN} \parallel Z_{CN}) \\ &= Z + \frac{Z \times Z}{Z + Z} = \frac{3Z}{2} \end{aligned}$$

$$\frac{3Z}{2} = \frac{V}{i_{AN}} = \frac{100 \angle -10^\circ}{6 \angle -70^\circ}$$

$$Z = \frac{100}{9} \angle 60^\circ \Omega$$



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(c)
$$i_{CN} = \frac{Z_{BN}}{Z_{BN} + Z_{CN}} i_{AN} = \frac{1}{2} i_{AN}$$

$$= 30 \angle -70^\circ \text{ A (rms)}$$

$$V_{AN} = i_{AN} \times Z$$

$$= 200 \angle -130^\circ \times 6 \angle -70^\circ \times \frac{100}{9} \angle 60^\circ$$

$$= \frac{200}{3} \angle -10^\circ \text{ V (rms)}$$

$$\theta = \angle V_{AN} - \angle i_{AN} = 60^\circ$$

$$V_{BN} = i_{BN} \times Z$$

$$= 30 \angle -70^\circ \times \frac{100}{9} \angle 60^\circ$$

$$= \frac{100}{3} \angle -10^\circ \text{ V (rms)}$$

Active power $\rightarrow P_{Z_{AN}} = |V_{AN}| |i_{AN}| \cos \theta$ $[\theta = 60^\circ]$

$$= \frac{200}{3} \times 6 \times \frac{1}{2}$$

$$= 200 \text{ W}$$

Active power $\rightarrow P_{Z_{BN}} = |V_{BN}| |i_{BN}| \cos \theta$

$$= \frac{100}{3} \times 3 \times \frac{1}{2}$$

$$= 50 \text{ W}$$

Reactive power $\rightarrow P'_{Z_{AN}} = |V_{AN}| |i_{AN}| \sin \theta = \frac{200}{3} \times 6 \times \frac{\sqrt{3}}{2}$

$$= 346.41 \text{ VAR}$$

Reactive power $\rightarrow P'_{Z_{BN}} = |V_{BN}| |i_{BN}| \sin \theta$

$$= \frac{100}{3} \times 3 \times \frac{\sqrt{3}}{2}$$

$$= 86.6 \text{ VAR}$$

As $V_{BN} = V_{CN}$, and $i_{BN} = i_{CN}$, $Z_{BN} = Z_{CN} = Z$

By symmetry,

Active power $\rightarrow P_{Z_{CN}} = P_{Z_{BN}} = 50 \text{ W}$

Reactive power $\rightarrow P'_{Z_{CN}} = P'_{Z_{BN}} = 86.6 \text{ VAR}$

Active $\rightarrow P$

$$P_{\text{source}} = -|v||i| \cos \theta$$

$$= -100 \times 6 \times \frac{1}{2}$$

$$= -300 \text{ W}$$

Reactive $\rightarrow P'_s$

$$P'_s = -|v||i| \sin \theta$$

$$= -100 \times 6 \times \frac{\sqrt{3}}{2}$$

$$= -519.62 \text{ VAR}$$

(d)

$$i_c = \frac{v}{Z_c} = j\omega C V$$

$$= j(2\pi \times 50) C \times 100 \angle -10^\circ$$

$$= 31415.93 C \angle 80^\circ \text{ A}$$

By phasor

$$\sin 60^\circ = \frac{|i_c|}{|i|}$$

$$\frac{\sqrt{3}}{2} = \frac{31415.93 C}{6}$$

$$C = 165.4 \mu\text{F}$$

