

Question 2: Merge sort

8. Sorting

For this question, suppose you have a `linkedList` class that includes methods. ‘split’ and ‘merge’, already implemented (exactly as was done in the homework):

```
class linkedList
{
private:
    class node
    {
    public:
        double data;
        node * next;
        node * prev;
    };
    node * head; // A pointer to the first node in the list
    node * tail; // A pointer to the last node in the list

public:
    // Splits the contents of list A evenly into the two given (initially empty) lists.
    // If the number of items in the list is odd, puts the extra item in the first list.
    // Runs in O(n) time, where n is the total number of items in the list.
    void split(linkedList &A, linkedList &B);

    // Merge takes 2 sorted lists and merges them into one (initially empty) list to create one
    // sorted list.
    // Runs in O(n) time, where n is the total number of items in the two given lists.
    void merge(linkedList &A, linkedList &B);
};
```

- a. Given this linked list class and the methods ‘split’ and ‘merge’, add a method ‘sort()’ to the `linkedList` class that sorts the items of the list into ascending order (with a fast run time). You may use the methods ‘split’ and ‘merge’ to help achieve this.



```
void sort() { // O(1)
    // if (nullptr) → false
    if (!head || !head->next)
        return; // O(1)

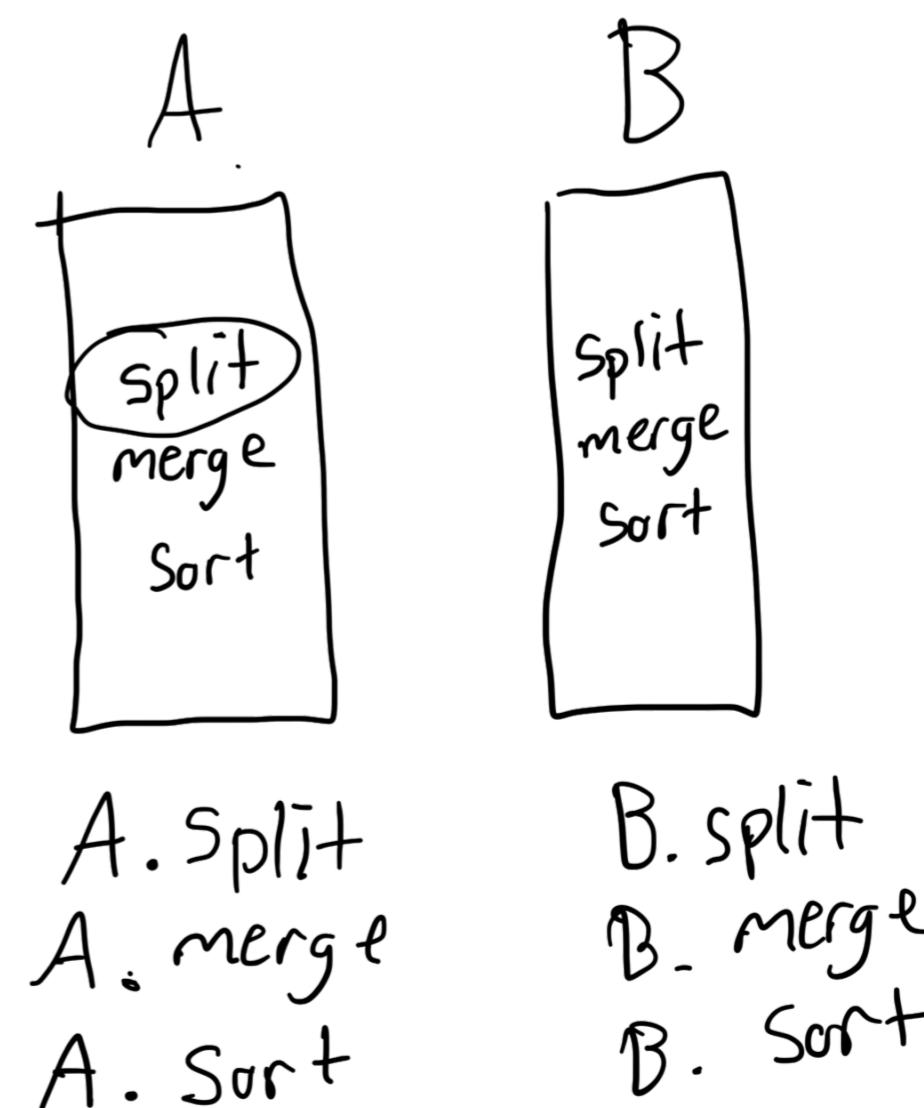
    linkedList < T > A, B;
    split(A, B); // O(n)

    A.sort(); // 2T(n/2)
    B.sort(); // O(n)

    merge(A, B); // O(n)
}
```

Steps of merge sort

1. Split ✓
2. Merge Sort left] recursively ✓
3. Merge Sort right ✓
4. Merge ✓



$$T(n) = 2T\left(\frac{n}{2}\right) + cn$$

$$\Theta(n \log n)$$