# Model-Based Quantification of Induced Gene Expression Time Courses



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#### **INTRODUCTION**

We model gene expression time courses following induction of a glucocorticoid receptor-bound transcription factor into the nucleus following exposure to dexamethasone in Arabidopsis thaliana.

In contrast to measurement of of induced expression at a single time, resulting in a single fold-change value typically long after the induction event, we model the dynamics of TF import into the nucleus followed by the transcriptional dynamics of its direct and indirect targets.

The model quantifies an observed time course with two rate coefficients:

- 1.  $\hat{\eta}_p$  = the normalized initial rate of rise (+) or fall (-) of target mRNA levels
- 2.  $\gamma_n$  = the mRNA loss rate

These two processes compete to determine the final transcript fold change: a highly-induced transcript may saturate at a low fold change if it also decays quickly, while weakly-induced transcripts may rise to a high level if they have very low loss.

In addition, some targets exhibit "turn-off", or auto-regulation. These time courses require a turn-off time,  $t_{off}$ , after which the mRNA level decays exponentially at  $\gamma_p$ .

We present analysis of experiments with GR-TFs involved in leaf regulation: *SHOOT MERISTEMLESS/STM* (AT1G65620); *ASYMMETRIC LEAVES 2/AS2/LBD6* (AT1G65620); *KANADI 1/KAN1* (AT5G16560); *REVOLUTA/REV* (AT5G60690); and *TINY* (AT5G25810).

Our experiments measure expression time courses for up to two hours after DEX exposure with both RNA-seq and microarray assays. Since secondary targets of the induced transcription factor are expected to rise after some delay, during which the primary transcript's protein level rises, we explore the use of our model to distinguish between primary and secondary targets.

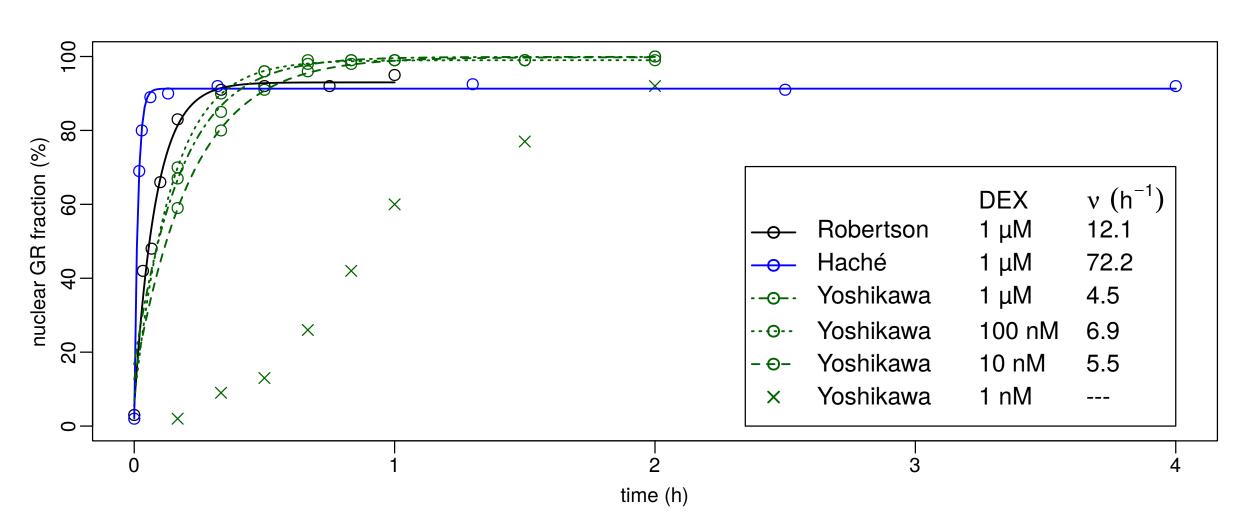
#### **OBJECTIVES**

- 1. Model the import of the GR-TF into the nucleus after DEX exposure
- 2. Model the modified transcription of GR-TF primary targets (subscript p)
- 3. Model the modified transcription of GR-TF secondary targets (subscript s), which are primary targets of GR-TF primary targets
- 4. Compare the model-fitted rate coefficients with standard fold-change analysis

#### MODEL AND EXPERIMENTAL METHOD

#### **Nuclear import model**

Transport of a glucocorticoid receptor (GR) into the nucleus after DEX application has been measured in animal tissue by several groups.



**Figure 1:** The measured nuclear GR concentration follows a saturated exponential time course, except at very low DEX concentration. Data sources in References.

The measured time courses are well described by a pair of linear ODEs:

$$\dot{\rho_c} = -\nu \rho_c + \gamma_e \rho_n$$

$$\dot{\rho_n} = \nu \rho_c - \gamma_e \rho_n - \gamma_n \rho_n$$

 $\rho_c = \text{cytoplasmic GR protein concentration}$ 

 $\rho_n$  = nuclear GR protein concentration

 $\nu = \text{nuclear import rate}$ 

 $\gamma_e$  = nuclear export rate

 $\gamma_n=$  rate of loss of GR-TF from other causes

We neglect nuclear export and loss setting  $\gamma_e=0$  and  $\gamma_n=0$  since those rates are slow compared to our two-hour measurement span. We assume that import of chimeric GR-TF is similar to the published GR import data.

### **Transcription model**

We model altered transcription of target mRNA due to DEX-induced import of the GR-TF with a set of coupled ODEs:

$$\dot{
ho_p} = \eta_p 
ho_n - \gamma_p 
ho_p$$
 $\dot{
ho_s} = \eta_s 
ho_p - \gamma_s 
ho_s$ 

 $\rho_p = {\sf expressed mRNA/protein of a primary target of the GR-TF}$ 

 $\rho_s = \text{expressed mRNA/protein of a secondary target of the GR-TF}$ 

 $\gamma_p = {\sf loss}$  rate of primary mRNA/protein

 $\gamma_s = loss rate of secondary mRNA/protein$ 

 $\eta_p=$  transcription rate between the GR-TF and primary target

 $\eta_s = \text{transcription rate between the primary and secondary targets}$ 

We assume that mRNA and protein concentrations are in fixed proportion, so that  $\rho_p$  and  $\rho_s$  represent measured mRNA levels as well as protein concentration. (This avoids two more equations and four more fit parameters accounting for translation.)  $\gamma_p$  and  $\gamma_s$  represent loss of mRNA.

These equations can be solved analytically, and set  $\nu = 10 h^{-1}$  based on the animal tissue studies (we need to measure it!).

#### Primary target expression time course metrics

The model provides two useful, independent time course metrics:

- $\hat{\eta}_p = \eta_p \rho_n(0)/\rho_p(0)$  characterizes the initial change of mRNA level
- ullet  $\gamma_p$  characterizes the loss of mRNA

In addition, we can calculate an asymptotic ( $t \to \infty$ ) fold change:

$$\mathsf{logFC}_{\infty} \equiv \lim_{t \to \infty} \mathsf{log}_2 \frac{\rho_p(t)}{\rho_p(0)} = \mathsf{log}_2 \left( 1 + \frac{\hat{\eta}_p}{\gamma_p} \frac{\rho_c(0)}{\rho_n(0)} \right)$$

The ratio  $\hat{\eta_p}/\gamma_p$  therefore determines the asymptotic fold change of a transcript: **mRNA** transcription and loss play equal roles in the final transcript level.

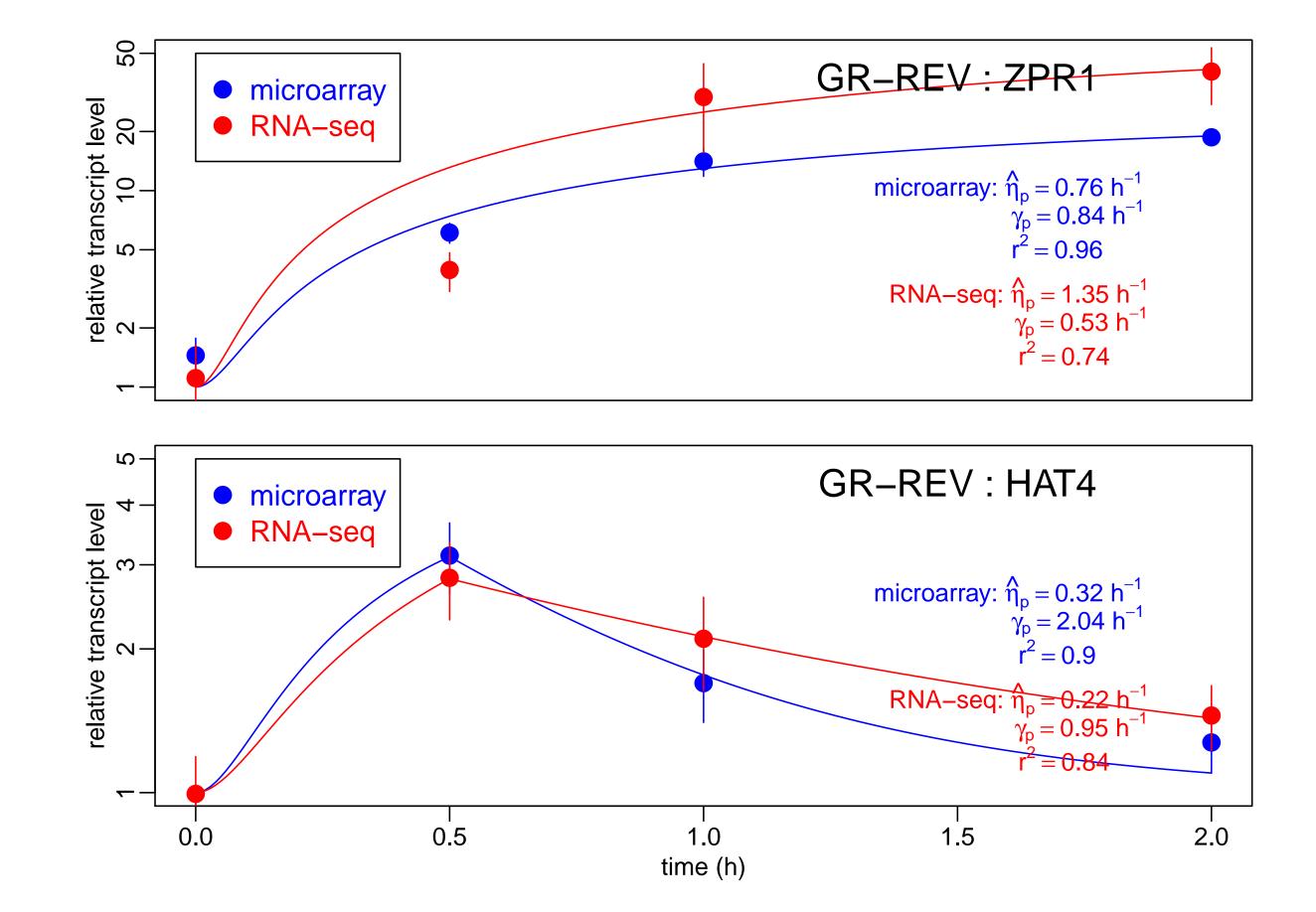
#### Time-course expression measurements in Arabidopsis thaliana

The five GR-TF plant lines plus WT plants (all Col-0) were grown to seedlings, and tissue was exposed to 50  $\mu$ M of DEX and then flash frozen 0, 0.5, 1 and 2 hours later. Almost all samples had at least three biological replicates per time. RNA was extracted and assayed with the Affymetrix ATH1 microarray and Illumina HiSeq RNA-seq. The microarray data were analyzed using the R packages affy and limma; the RNA-seq data were analyzed using TopHat2, Cufflinks and Cuffdiff. Sequences were mapped to the TAIR10 reference genome.

### **RESULTS**

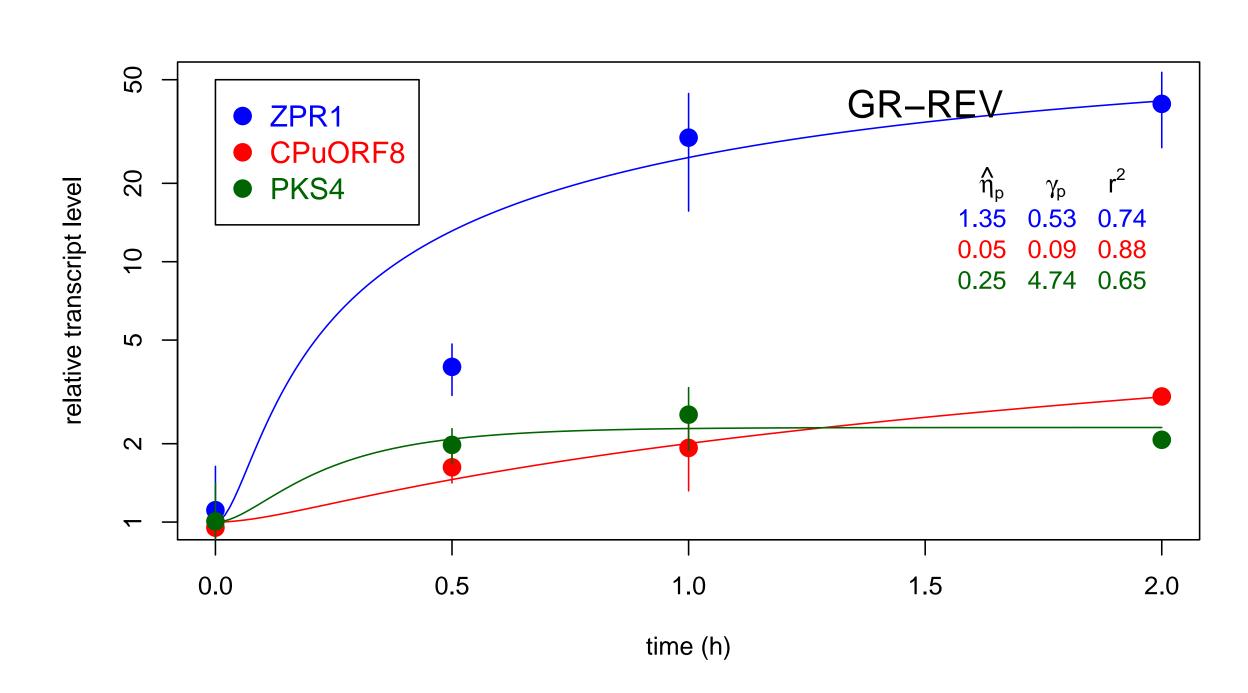
#### **Expression time courses exhibit qualitative variation**

When you measure DE in an induced expression experiment is important!



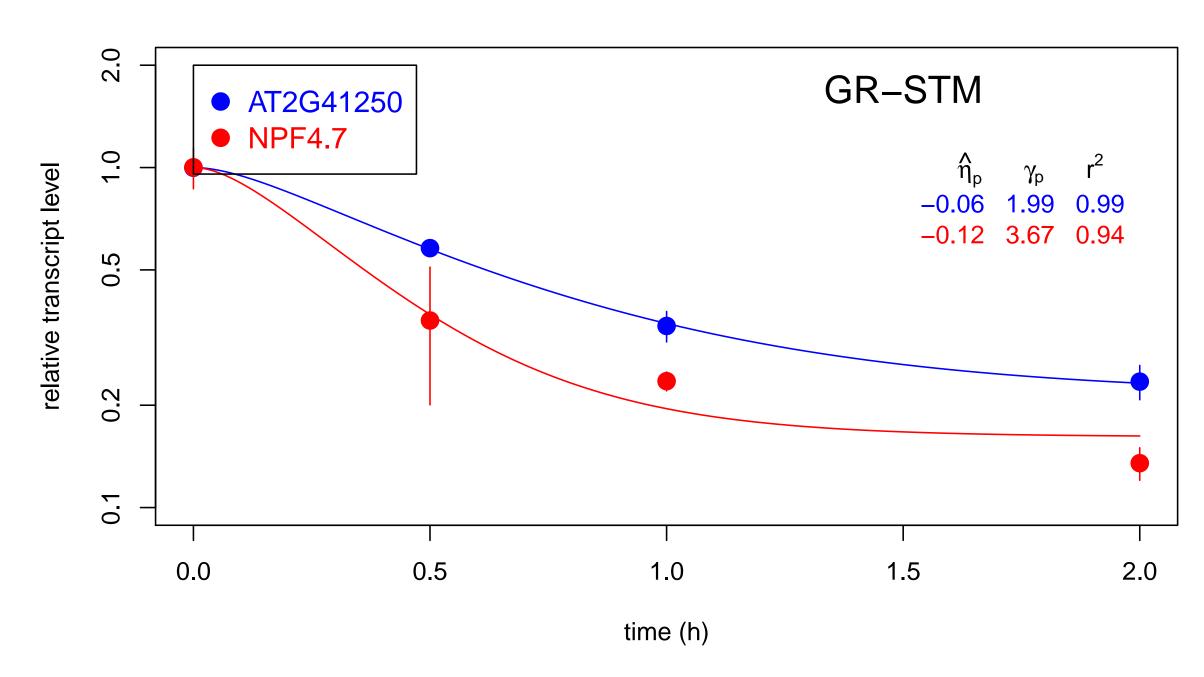
**Figure 2:** Expression time courses vary greatly, from strong GR-REV monotonic risers like *ZPR1* to HD-ZIPII self-regulators like *HAT4*. Lines represent primary target model fits with transcription turned off at t=30 mins for *HAT4*. (*HAT4* turn-off occurs some time between t=15 and 45 mins.)

Model parameters  $\hat{\eta}_p$  and  $\gamma_p$  distinguish expression time course shapes



**Figure 3:** Distinct time course shapes result from different transcription strength vs. loss rate for these GR-REV targets: high  $\hat{\eta}_p$ , low  $\gamma_p$  for *ZPR1*, the most strongly regulated GR-REV target; low  $\hat{\eta}_p$ , low  $\gamma_p$  for *CPuORF8*, which reaches a significant fold-change due to low loss; and high  $\hat{\eta}_p$ , high  $\gamma_p$  for *PKS4*, which saturates quickly due to high loss. (RNA-seq data.)

#### Down-regulation time courses are also well fit by the model



**Figure 4:** STM has a number of strongly down-regulated targets; these two GR-STM targets are particularly well fit by the model. (RNA-seq data.)

Three examples that exhibit very different transcriptional responses to DEX application:

- ZPR1 is the most strongly up-regulated target of GR-REV a strong, steady riser with a strong initial transition ( $\kappa$  is large) leading to a large asymptotic DE level (logFC $_{\infty}$  is large).
- CRK30 is the most strongly down-regulated target of GR-KAN in the RNA-seq series it is predicted to reach a larger DE level further out in time.
- HAT22 is a strong autoregulating GR-REV target an early rise with a large  $\kappa$  value is followed by "turn-off" after t=0.5 h; without turn-off, the model predicts it would reach logFC $_{\infty}=1.8$ .

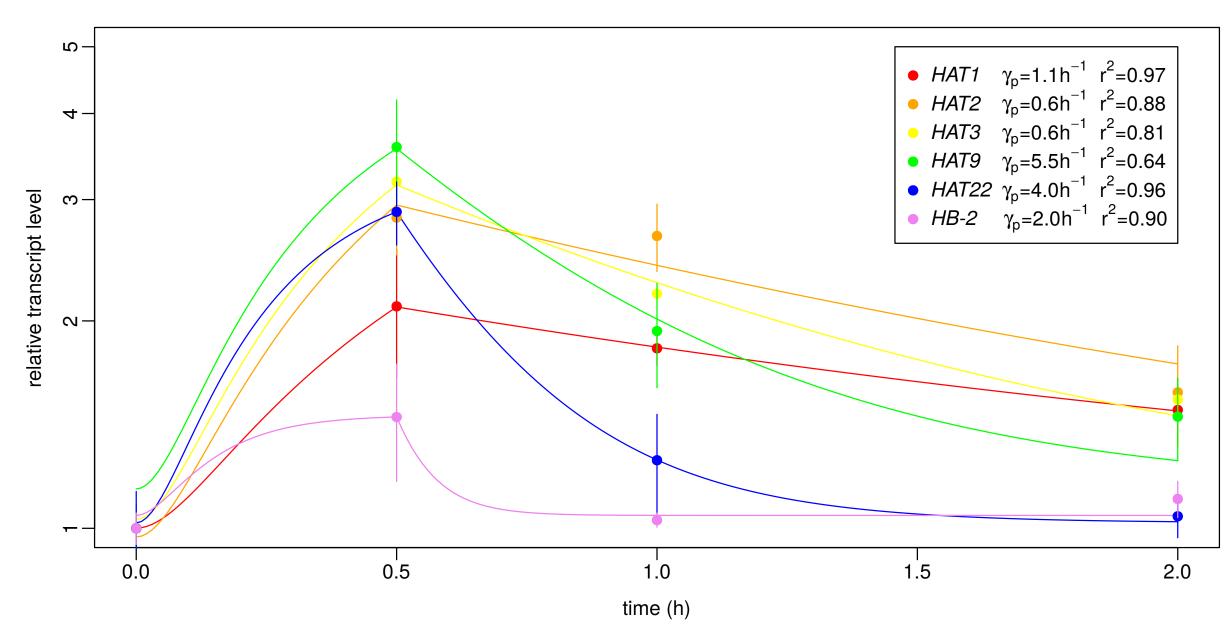
	logFC			model	
gene (assay)	0.5h	1.0h	2.0h	$\kappa$	$logFC_{\infty}$
ZPR1 (microarray)					
CRK30 (RNA-seq)	-0.72	-1.93	-2.51	$-15 h^{-2}$	-3.01
HAT22 (microarray)	1.53	×	×	$96 h^{-2}$	1.77

**Table 1:** limma and Cuffdiff DE levels along with model-derived metrics  $\kappa$  and logFC $_{\infty}$ .

Intermediate DE values, given by logFC, depend on the time of measurement while  $\kappa$  and logFC $_{\infty}$  characterize the entire time course.

## Early-peaking primary transcripts are well fit by mid-course transcription turn-off in the model

When  $\gamma_n=0$ , only group L time courses can be fit by the model with constant  $\eta_p$ . Group E and M genes appear to exhibit transcription "turn-off" — after a certain amount of time (or beyond a certain level of expression) transcription of those genes' mRNA "turns off" and the subsequent transcript level drops as  $e^{-\gamma_p t}$ . We model transcription turn-off by setting  $\eta_p=0$  at t=0.5h for E time courses and t=1.0h for M time courses.



**Figure 5:** Many early turn-off genes are found in the HD-ZIP family, especially in the HD-ZIPII class, shown here.

The rapidity of turn-off of *HAT9* and *HAT22* may indicate that they play a leading role in the HD-ZIPII autoregulatory network [Ohgishi. et al.].

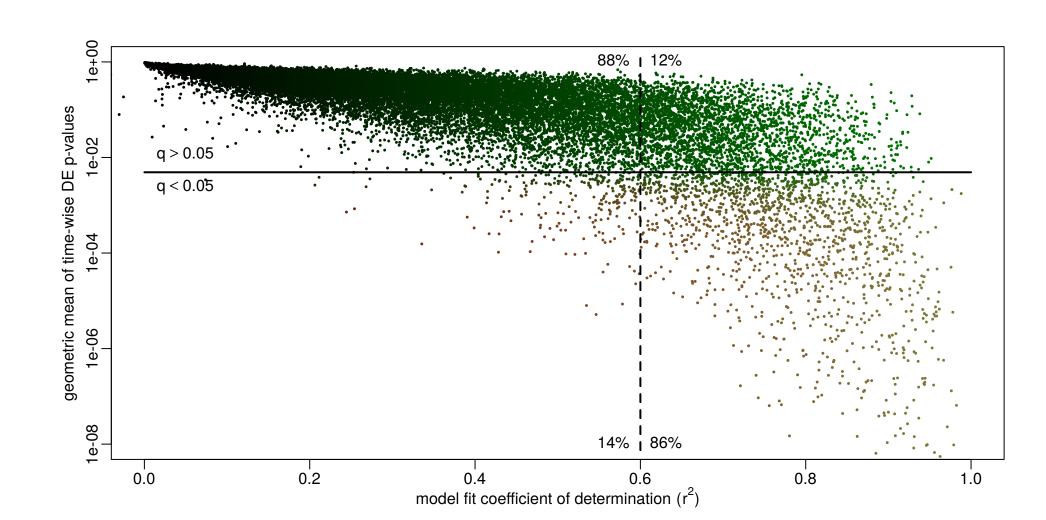
#### Conventional DE and model fit confidence measures are correlated

For microrarray/limma and RNA-seq/Cuffdiff DE measurements, p-values and FDR-adjusted q-values are the standard measures of confidence. One typically assumes that q < 0.05 represents a 95% probability that the measured DE is real and not a chance occurrence.

In our model fits, the experimental data points, one per sample (3 reps  $\times$  4 times = 12 total), are individually fit, without weighting, by minimizing the variance between data and model values using the core R nonlinear minimization routine nlm. We then compute the standard  $r^2$  coefficient of determination to quantify the quality of the fit.

- ullet DE measurements are taken at a single time relative to the t=0 base: three independent logFC, p and q values result for t=0.5, 1 and 2 h, using six data per measurement, reusing the t=0 base data each time.
- The model fits one solution to all twelve data, and is therefore subject to variation of all, not half, of the data
- The model counts the t=0 data equally with the other data.

The model fit  $r^2$  value, therefore, provides an independent measure of DE significance which spans the entire time course in a statistically balanced fashion.



**Figure 6:** Model  $r^2$  values correlate with the geometric mean of the three p-values from limma DE analysis of the 22,585 GR-REV microarray transcripts which result in a model fit of any quality. The horizontal line shows the geometric mean of p-values for which q=0.05, representing the boundary of significant limma-determined DE at the q<0.05 level.

The microarray  $\liminf p$  and model-fit  $r^2$  values correlate, and we have chosen  $r^2>0.6$  as the significance level for the model fits, covering 86% of the q<0.05 transcripts. A majority of significant DE time courses meet this model fit level in both microarray and RNA-seq series, boosting confidence in the validity of the model.

# Secondary targets are suggested by model fits and transcriptional response across four GR-TF lines

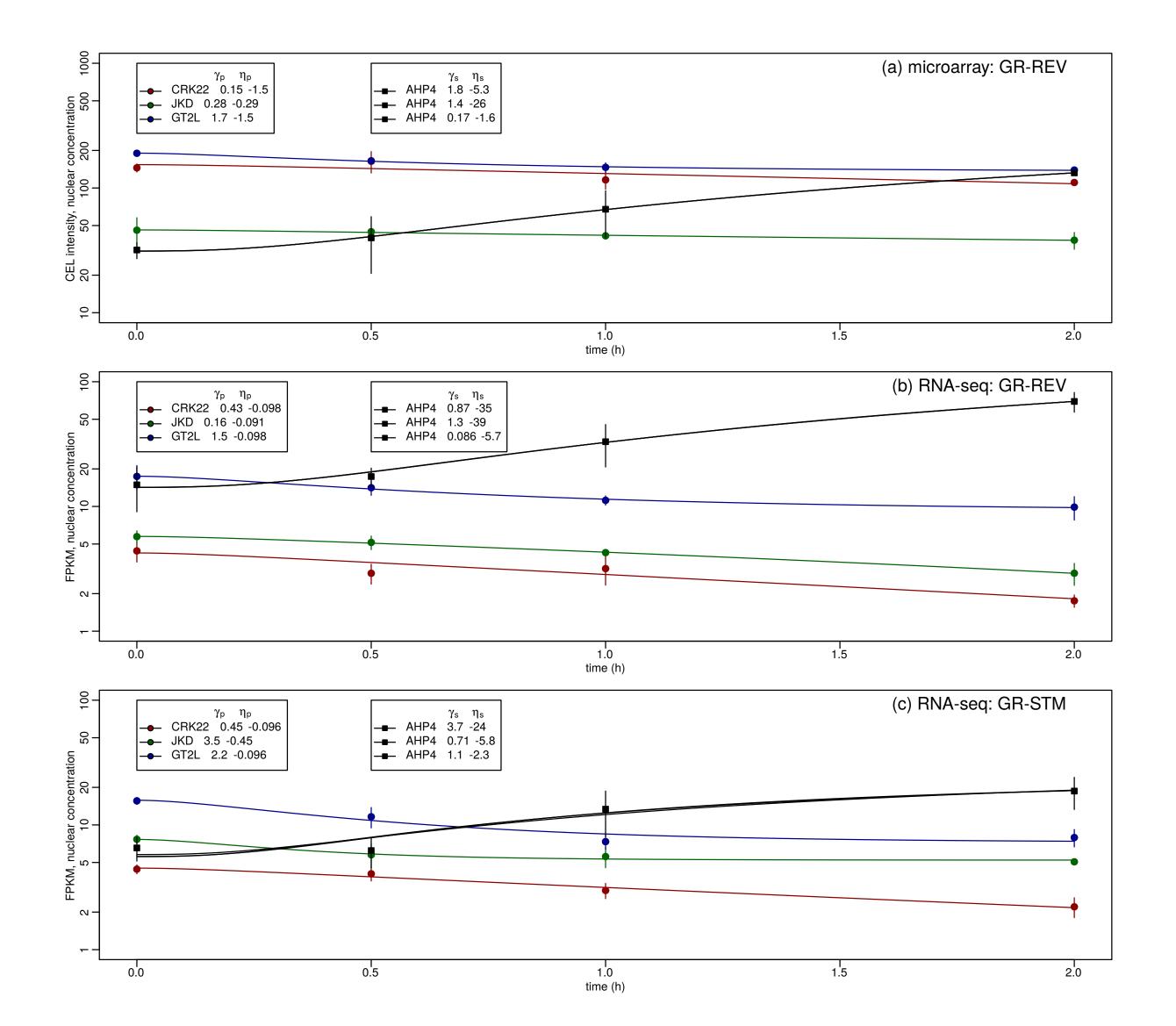
GR-REV:AHP4 rises very slowly, requiring  $\gamma_p < 0$  in the model, which is unphysical. We model the time course of AHP4 as a secondary target with  $\gamma_s > 0$ , and search for candidate primary targets in the four GR-TF lines which regulate it. If AHP4 is strictly a secondary target in the GR-TF lines in which it exhibits differential expression, then the corresponding primary target should also exhibit DE in those and only those lines. AHP4 is an up-regulated group L gene in GR-KAN, GR-REV and GR-STM, further suggesting that it is a secondary, or farther downstream target.

From the RNA-seq series: 44 other genes show all up- or all down-DE in GR-KAN, GR-REV and GR-STM and none in GR-AS2. Of these, model fits using AHP4 as the secondary target lead to:

- 10 genes as primary targets of GR-REV with  $r^2>0.6$  and  $\gamma_p,\gamma_s>0$
- 9 genes as primary targets of GR-STM with  $r^2>0.6$  and  $\gamma_p,\gamma_s>0$
- 5 genes common to the above GR-REV and GR-STM selections

The RNA-seq GR-KAN:AHP4 data variance is too high to produce good model fits.

From the microarray series, model fits to the five genes above as primaries which target AHP4 result in three candidates with  $r^2>0.6$  and  $\gamma_p,\gamma_s>0$ : CRK22, JKD and GT2L (At5g28300).



**Figure 7:** Three genes are well simulated as down-regulated targets of *KAN*, *REV* and *STM*, which in turn down-regulate *AHP4*.

We regard these three genes as candidate primary targets of *KAN*, *REV* and *STM*, which, in turn, target *AHP4*. (One of these three, *GT2L*, is a member of the Trihelix TF family, but *AHP4* has not been reported as a target.) Also note that the three candidate primary targets are *down*-regulated in GR-KAN, GR-REV and GR-STM lines. This suggests that they *repress AHP4*, which then overexpresses its mRNA as their expression is reduced by the induced TF.

#### **CONCLUSIONS**

- 1. DEX-induced GR-TF transcription time courses can be modeled with a set of linear ODEs with parameters  $(\gamma_p, \eta_p)$  describing the primary target response and  $(\gamma_s, \eta_s)$  describing the secondary target response.
- 2. Model fits use data in a balanced fashion, rather than the overemphasis of t=0 data in time-wise DE measurements.
- 3. Model-determined metrics  $\kappa$  and logFC $_{\infty}$  characterize the primary target response in a time-independent manner, as opposed to misleading single-time DE measurements.
- 4. The model simulates transcription turn-off by setting  $\eta_p$  or  $\eta_s$  to 0 at an appropriate time, matching autoregulated genes in the HD-ZIPII family.
- 5. The model simulates primary and secondary transcriptional responses, supporting target discovery and inference of gene regulatory networks.

### **Forthcoming Research**

- 1. Improve model to make robust fits for "black box" analysis, perhaps in a Web application, with data and fit diagnostics
- 2. Measure tighter time course of selected GR-TFs and targets using qPCR
- 3. Measure GR-TF nuclear import and mRNA accumulation using flourescent probes
- 4. Measure mRNA induction in real time with CRISPRi activation?

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