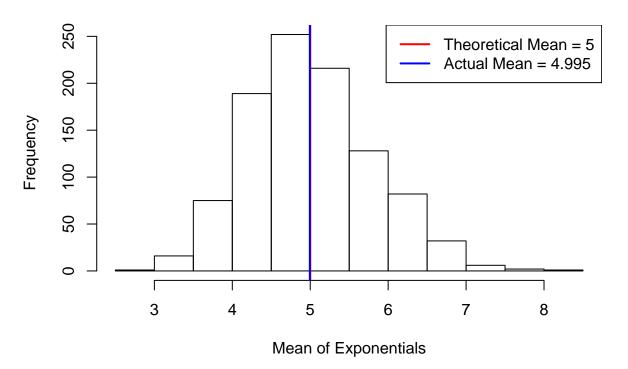
A simulation exercise

This is a study to show how close it is between the simulated centered value and the theoretical one in an exponentials distribution under the Central Limit Theorem (CLT).

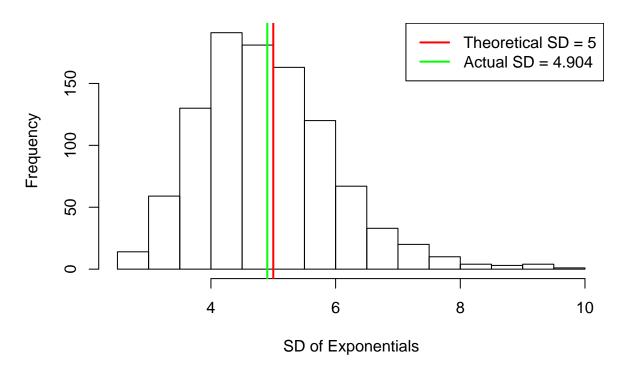
Please note that in theory, both the mean and the standard deviation of an exponential distribution is 1/lambda, where lambda is the rate parameter.

Here we generate three distributions for random exponentials in mean, standard deviation (SD) and variance. We set the lambda to be 0.2 and generate 40 random exponentials. And then we get the average for the variable (e.g. SD) in which we are interested. We repeat this process 1000 times. Three histograms are plotted below to show the distributions.

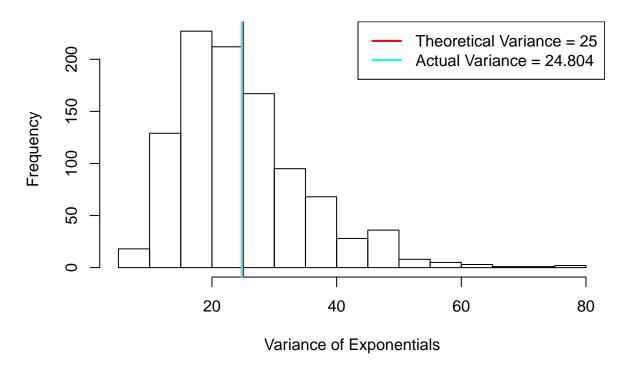
Histogram of the Means of Simulated Exponentials



Histogram of the Standard Deviations of Simulated Exponentials



Histogram of the Variances of Simulated Exponentials



Conclustion:

As you can see, the distributions (means, standard deviations and variances) are approximately normal; and the centered values is very close to the theoretical ones. If we increase the sample size from 40 to like 1000, the distributions would be more normal.