

Merge Sort	Bubble Sort
0.012416669	0.024820014
0.029710162	0.602095816
0.047838508	1.747998642
0.062429669	3.675540067
0.080597402	5.905458108
0.134090918	9.077735948
0.096029407	13.39447895
0.10484465	17.87273916
0.11094068	23.15028187
0.107481135	28.45430052
0.110450346	35.79852062
	0.012416669 0.029710162 0.047838508 0.062429669 0.080597402 0.134090918 0.096029407 0.10484465 0.11094068 0.107481135

As seen in the graph above, you can barely see a change in the mergesort line or time (which is at the bottom and looks almost like a horizontal line). The time for bubble sort increases at a large rate for each input size while as the input size of merge sort increases, there is barely an increase in the time in seconds. This shows how the big O notation of bubble sort represents quadratic growth or $O(n^2)$ since it is growing at a rapid rate and the worst case scenario for it is n^2 . The time complexity represented by merge sort is $O(\log n)$ because it's worst case is logn. This is because the loop variable is being divided. This is clearly more efficient than bubble sort because no matter the input size, the time complexity will remain relatively low while with bubble sort, it increases dramatically.