

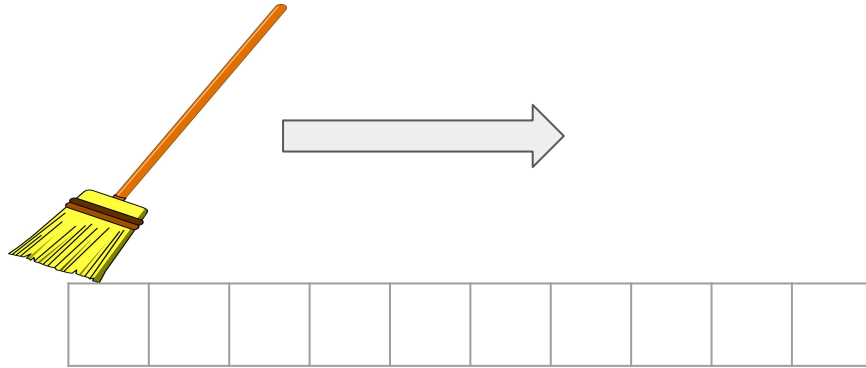
Greedy Sweeps

Sweep

Goal: start at one end of the data move across and build up the answer as we go.

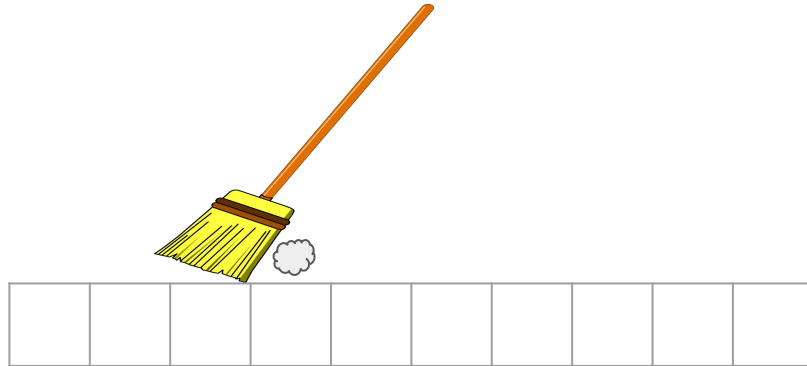
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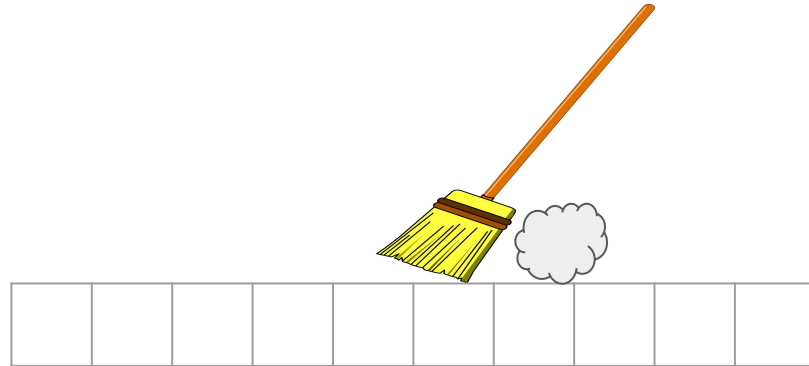
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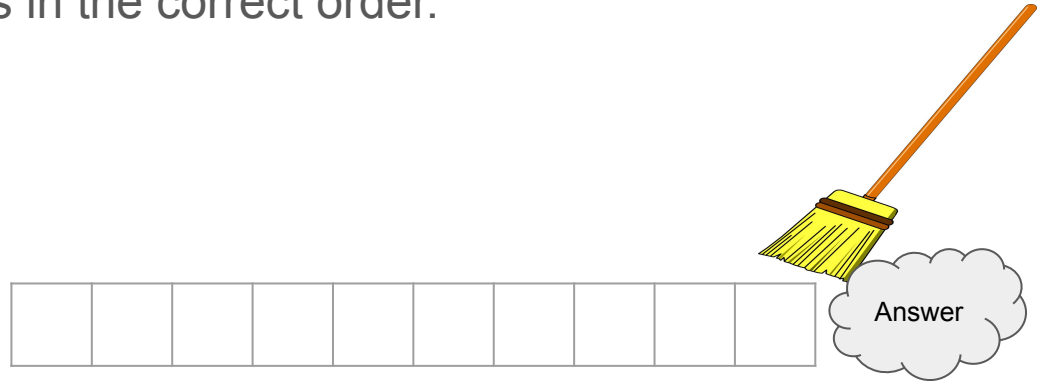
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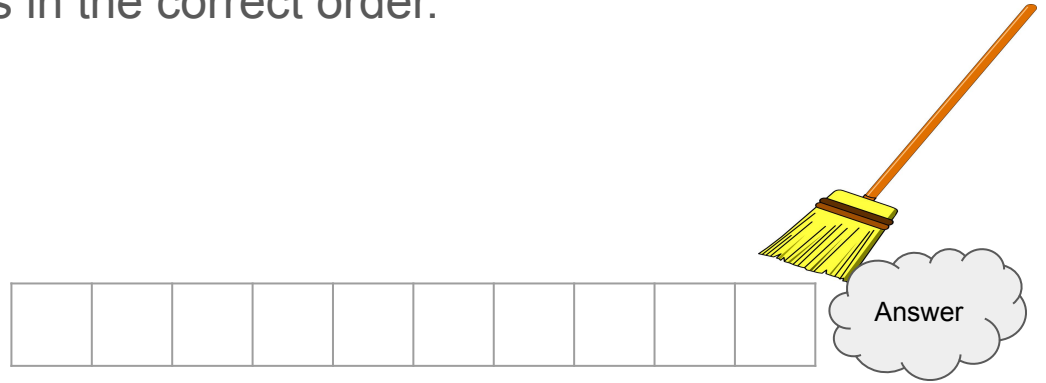


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The data needs to “sorted”



Example Problem

I need to tell all my students about some deadline

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T_T

I know when each student will enter and leave the meeting (assume no student will re-enter)

What is the minimum number of times I need to mention the deadline to ensure all students are aware?

Observations/Ideas

Working with an array of students could be challenging

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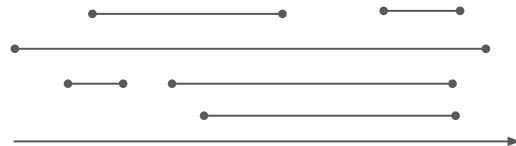
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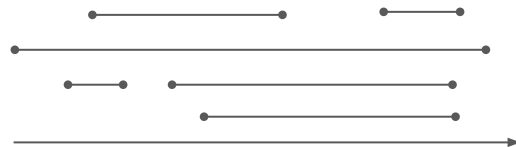
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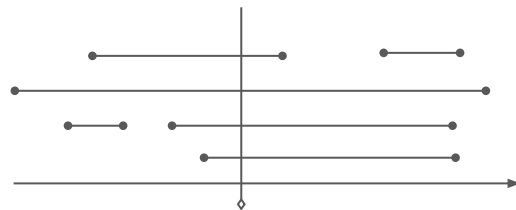
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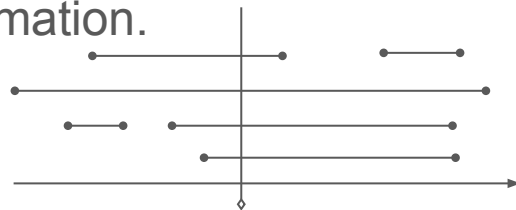
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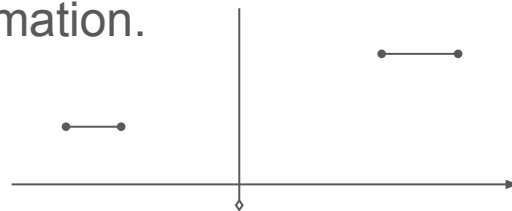
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Largest overlap?

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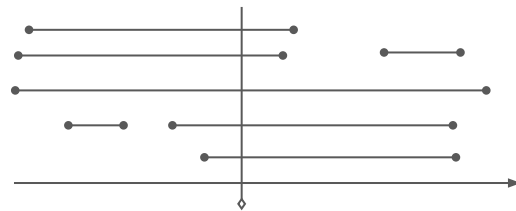
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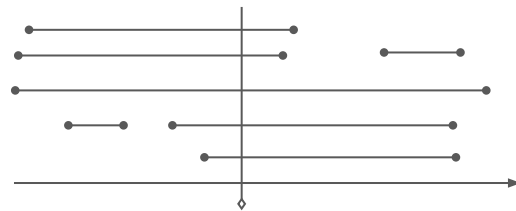


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Consider the following,



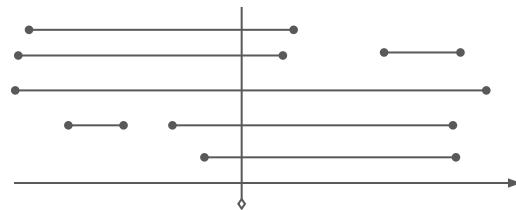
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Consider the following,

When a student leaves we must have informed them beforehand.

Be lazy

Wait until an uninformed student is just about to leave, and then hit everyone with some knowledge

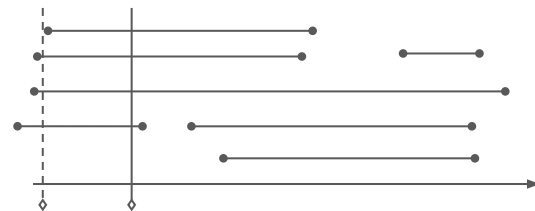
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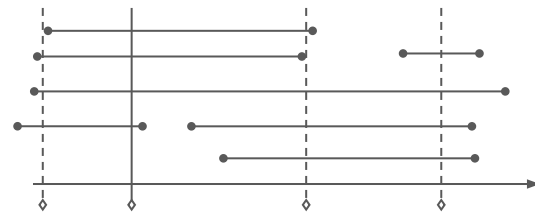
- “FTSOC Suppose an ideal solution performed a knowledge sesh earlier”



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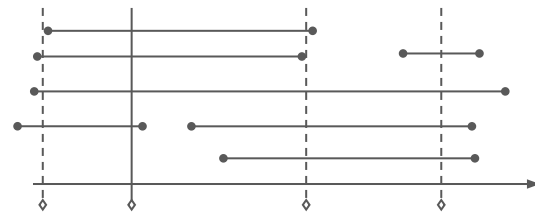
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Proving This is Correct

We need to perform an exchange argument.

- “FTSOC Suppose an ideal solution performed a knowledge sesh earlier”
- We would show that we have an ideal solution could exists by moving forward the time by patchworking with the ideal solution.
- Thus the ideal solution should do a later knowledge session.



Another Problem: Food Display Arrangement

Your friend works at a local grocery store and has the task of arranging produce. At the end of the day your friend needs to fix the order of the food. All the customers move the produce around (without buying it those jerks), and some lazy coworkers dumped all the new food in one spot.

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Another Problem: Food Display Arrangement (cont.)

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What is the least number of passes required by your friend?

FDA Strategy

How could we solve this greedily?

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Turn each food type into an interval!

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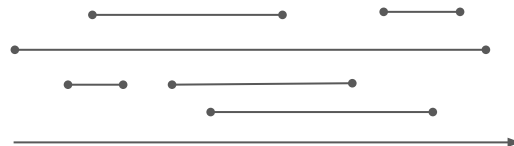
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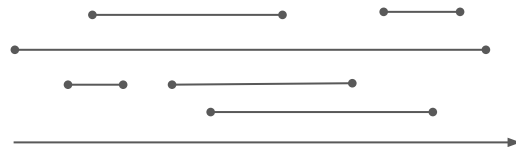
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Food that will be left alone cannot overlap with other left alone food.



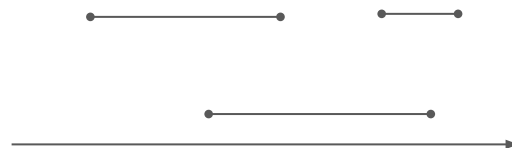
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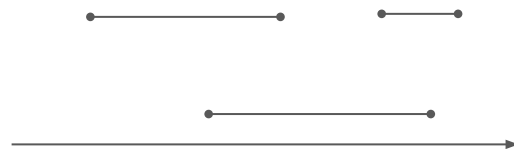
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INVALID =>



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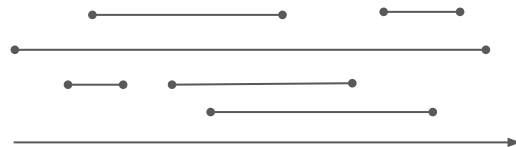
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The more intervals left,
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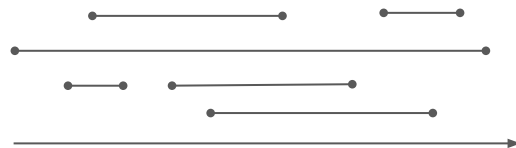
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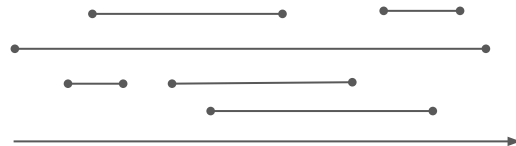
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Find maximum non-overlapping subset.

Non-Overlapping Subset Strategy

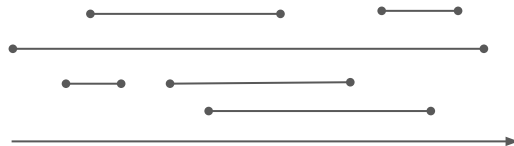
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Non-Overlapping Subset Strategy

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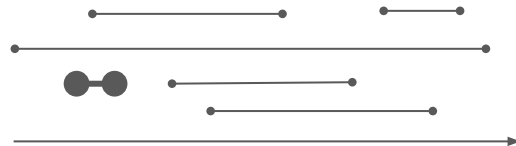
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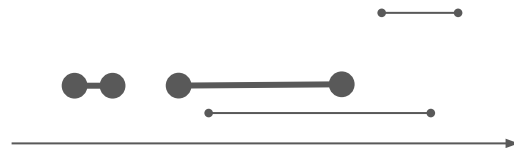


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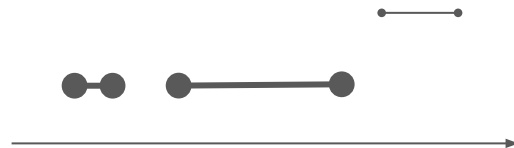


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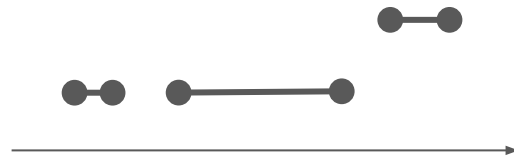


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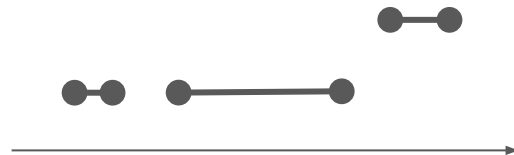
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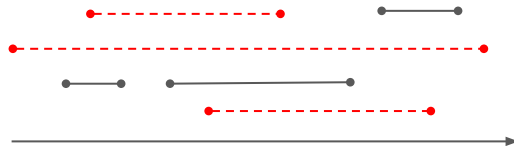
How do we do this?

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Repeat...

3 food types can be left alone.

3 types had to move



High-Level

Convert to intervals

Sort by End Points (smallest first)

Make the Last End Point Used (LEPU) be $-\infty$

Let movedIntervals be 0

Loop through sorted intervals

 If the `currentInterval.start` is after the LEPU

 Update LEPU to `currentInterval.end`

 Else

 Increment movedIntervals by 1

 End If

End Loop

Return movedIntervals