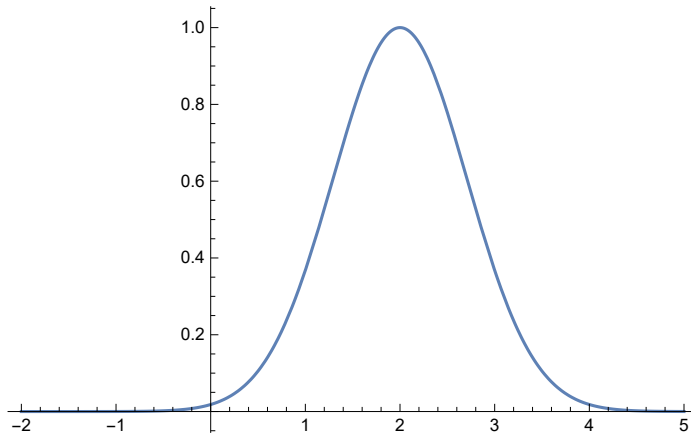


```

In[1]:= f[x_] := Exp[- (x - a) ^2];
a = 2;
Plot[f[x], {x, -2, 5}, PlotRange -> Full, PlotLegends -> "Expressions"]
NIntegrate[f[x], {x, -∞, ∞}]

```

Out[3]=



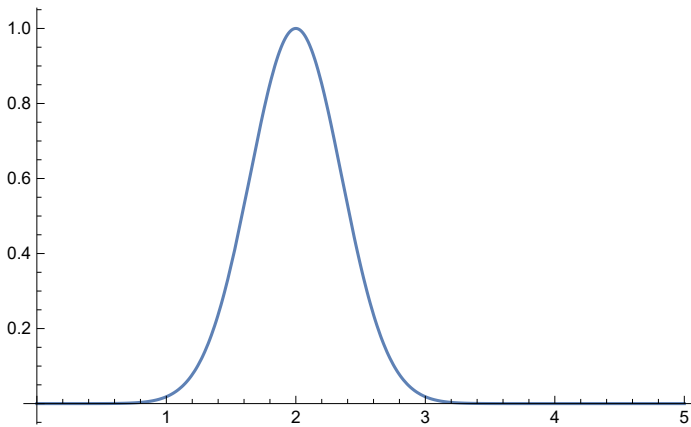
Out[4]= 1.77245

```

In[5]:= f[x_, k_] := Exp[- (x - a) ^2] / k^2;
a = 2;
Plot[f[x, k = 0.5], {x, 0, 5}, PlotRange -> Full, PlotLegends -> "Expressions"]
NIntegrate[f[x, k = 0.5], {x, -∞, ∞}]
2 * NIntegrate[f[x, k = 0.5], {x, -∞, ∞}]

```

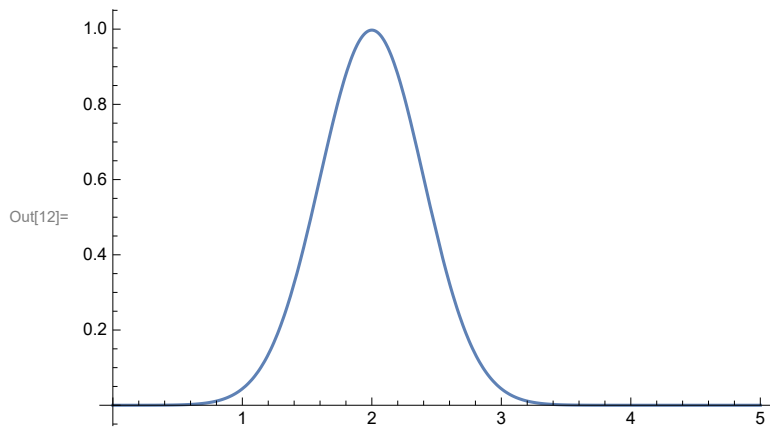
Out[7]=



Out[8]= 0.886227

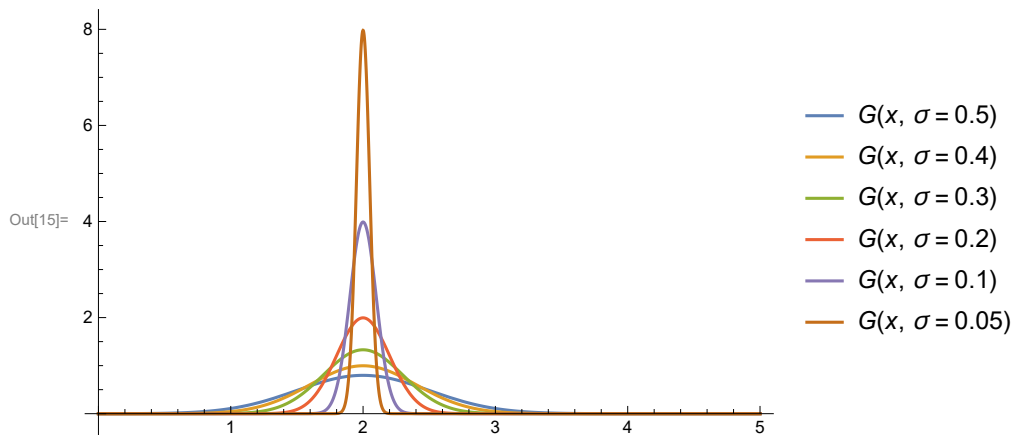
Out[9]= 1.77245

```
In[10]:= G[x_] := (1 / (σ * Sqrt[2 Pi])) Exp[- (x - a)^2 / (2 σ^2)];
a = 2; σ = 0.4;
Plot[G[x], {x, 0, 5}]
```



```
In[13]:= G[x_, σ_] := (1 / (σ * Sqrt[2 Pi])) Exp[- (x - a)^2 / (2 σ^2)];
a = 2;
Plot[{G[x, σ = 0.5], G[x, σ = 0.4], G[x, σ = 0.3], G[x, σ = 0.2], G[x, σ = 0.1],
      G[x, σ = 0.05]}, {x, 0, 5}, PlotRange -> Full, PlotLegends -> "Expressions"]
NIntegrate[G[x, σ = 0.5], {x, -∞, ∞}]
NIntegrate[G[x, σ = 0.05], {x, -∞, ∞}]
```

General: Exp[-799.918] is too small to represent as a normalized machine number; precision may be lost.



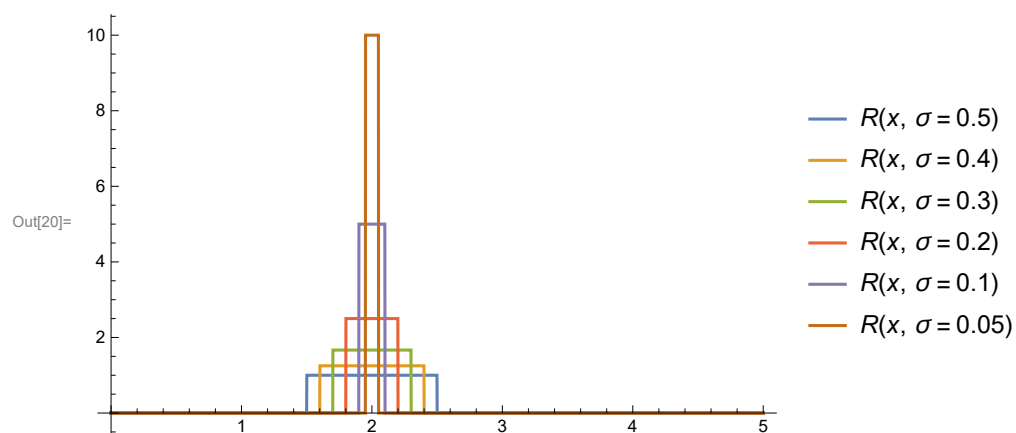
Out[16]= 1.

Out[17]= 1.

```

In[18]:= R[x_, σ_] := Piecewise[{{1/(2 σ), -σ < x - a < σ}, {0, Modulus[x - a] > σ}}];
a = 2;
Plot[{R[x, σ = 0.5], R[x, σ = 0.4], R[x, σ = 0.3], R[x, σ = 0.2], R[x, σ = 0.1],
      R[x, σ = 0.05]}, {x, 0, 5}, PlotRange -> Full, PlotLegends -> "Expressions"]
NIntegrate[R[x, σ = 0.5], {x, -∞, ∞}]
NIntegrate[R[x, σ = 0.05], {x, -∞, ∞}]

```



Out[21]= 1.

Out[22]= 1.

In[23]:=