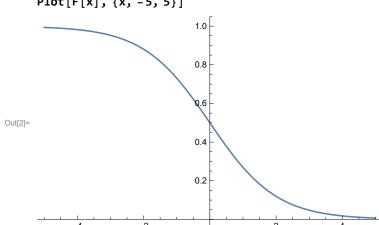
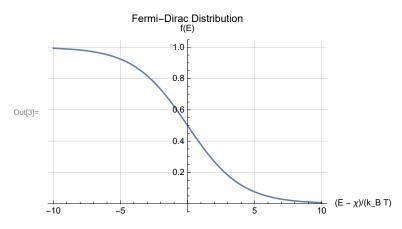
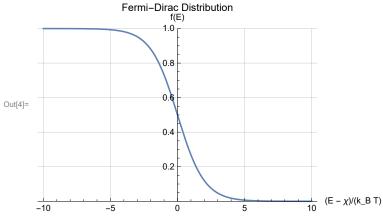
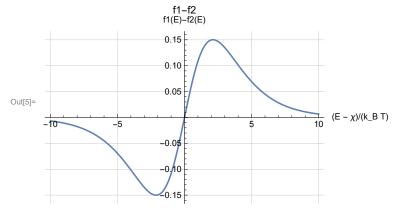
In[1]:= $F[x_] := 1/(1 + Exp[x]);$ Plot[F[x], {x, -5, 5}]



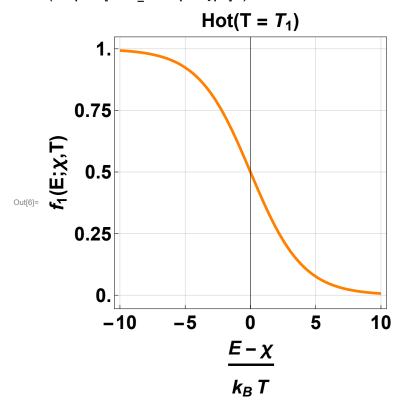
```
\begin{split} & \text{Plot} \Big[ 1 \Big/ \left( \text{Exp} \Big[ \text{x} \Big/ 2 \Big] + 1 \right), \, \{ \text{x}, -10, \, 10 \}, \, \text{AxesLabel} \rightarrow \{ \text{"} (\text{E} - \chi) / (\text{k}\_\text{B} \, \text{T}) \text{"}, \, \text{"} f(\text{E}) \text{"} \}, \\ & \text{PlotLabel} \rightarrow \text{"Fermi-Dirac Distribution", GridLines} \rightarrow \text{Automatic} \Big] \\ & \text{Plot} \Big[ 1 \Big/ \left( \text{Exp} \big[ \text{x} \big] + 1 \right), \, \{ \text{x}, -10, \, 10 \}, \, \text{PlotRange} \rightarrow \{ 0, \, 1 \}, \\ & \text{AxesLabel} \rightarrow \{ \text{"} (\text{E} - \chi) / (\text{k}\_\text{B} \, \text{T}) \text{"}, \, \text{"} f(\text{E}) \text{"} \}, \\ & \text{PlotLabel} \rightarrow \text{"Fermi-Dirac Distribution", GridLines} \rightarrow \text{Automatic} \Big] \\ & \text{Plot} \Big[ \left( 1 \Big/ \left( \text{Exp} \big[ \text{x} \Big/ 2 \big] + 1 \right) \right) - \left( 1 \Big/ \left( \text{Exp} \big[ \text{x} \big] + 1 \right) \right), \, \{ \text{x}, -10, \, 10 \}, \\ & \text{AxesLabel} \rightarrow \{ \text{"} (\text{E} - \chi) / (\text{k}\_\text{B} \, \text{T}) \text{"}, \, \text{"} f1 (\text{E}) - f2 (\text{E}) \text{"} \}, \\ & \text{PlotLabel} \rightarrow \text{"} f1 - f2 \text{"}, \, \text{GridLines} \rightarrow \text{Automatic} \Big] \end{aligned}
```



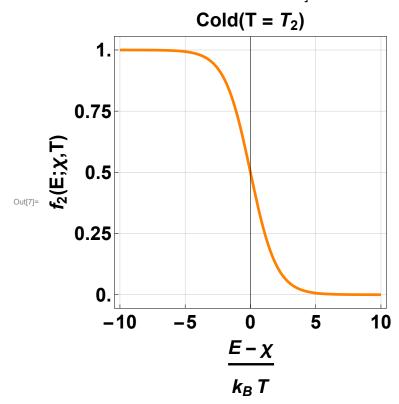




```
ln[6] = p1 = Plot[1/(Exp[x/2] + 1), \{x, -10, 10\}, AspectRatio <math>\rightarrow 1, (*AxesOrigin \rightarrow \{0, 0.5\}, *)]
          Axes \rightarrow True, GridLines \rightarrow {{-10, -5, 0, 5, 10}, {0.00, .25, 0.50, 0.75, 1.00}},
          PlotTheme \rightarrow "Scientific", FrameLabel \rightarrow {HoldForm["f<sub>1</sub>(E;\chi,T)"], None},
             \left\{ \text{HoldForm}\left[ \left\| \frac{\mathsf{E} - \chi}{\mathsf{k}_{\mathsf{B}} \mathsf{T}} \right\| \right], \, \text{HoldForm}\left[ \left\| \text{Hot}\left(\mathsf{T} = \mathsf{T}_{\mathsf{1}}\right) \right\| \right] \right\} \right\}, \, \text{AxesStyle} \rightarrow \text{Black},
          LabelStyle → {14, GrayLevel[0], Bold}, FrameStyle → Directive[Black, 20],
          FrameTicks \rightarrow {{\{0.00, .25, 0.50, 0.75, 1.00\}, None}, {{-10, -5, 0, 5, 10\}, None}},
          PlotStyle → {Orange, Thickness[0.01]}
       (*Export["hot_f-22.png",p1,ImageResolution→500]*)
       (*Export["hot_f-22.pdf",p1]*)
```

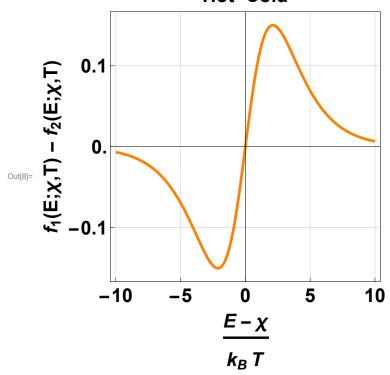


```
\begin{split} & \text{In}[T] \coloneqq \text{Plot} \Big[ 1 \Big/ \left( \text{Exp}[x] + 1 \right), \, \{x, -10, \, 10\}, \, \text{AspectRatio} \to 1, \, (\star \text{AxesOrigin} \to \{0, 0.5\}, \star) \\ & \text{Axes} \to \text{True, GridLines} \to \{\{-10, -5, 0, 5, \, 10\}, \, \{0.00, \, .25, \, 0.50, \, 0.75, \, 1.00\}\}, \\ & \text{PlotTheme} \to \text{"Scientific", FrameLabel} \to \\ & \Big\{ \{\text{HoldForm}[\text{"f}_2(E;\chi,T)\text{"}], \, \text{None}\}, \, \Big\{ \text{HoldForm}\big[\text{"}\frac{E-\chi}{k_B\,T}\text{"}\big], \, \text{HoldForm}\big[\text{"Cold}\,(T=T_2)\text{"}\big] \Big\} \Big\}, \\ & \text{AxesStyle} \to \text{Black, LabelStyle} \to \{14, \, \text{GrayLevel}[0], \, \text{Bold}\}, \\ & \text{FrameStyle} \to \text{Directive}[\text{Black, 20}], \\ & \text{FrameTicks} \to \{\{\{0.00, .25, \, 0.50, \, 0.75, \, 1.00\}, \, \text{None}\}, \, \{\{-10, -5, \, 0, \, 5, \, 10\}, \, \text{None}\}\}, \\ & \text{PlotStyle} \to \{\text{Orange, Thickness}[0.01]\} \Big] \end{split}
```

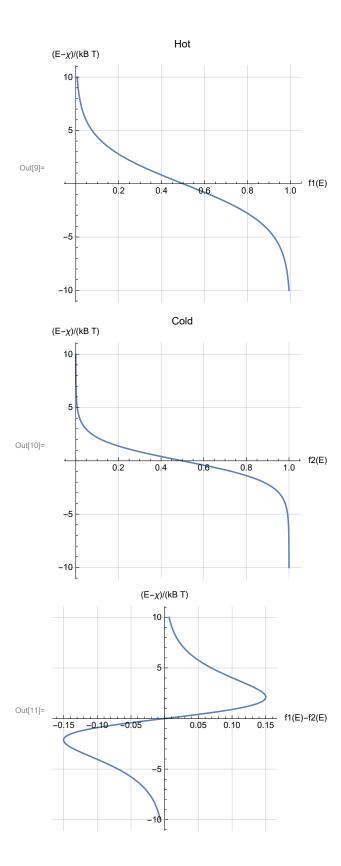


```
log_{[x]} = Plot((1/(Exp[x/2]+1)) - (1/(Exp[x]+1)), \{x, -10, 10\}, AspectRatio \rightarrow 1, Axes \rightarrow True,
     \left\{\{\text{HoldForm}[\text{"}f_1(E;\chi,T) - f_2(E;\chi,T)\text{"}], \text{None}\}, \left\{\text{HoldForm}[\text{"}\frac{E-\chi}{k_RT}\text{"}], \text{HoldForm}[\text{"Hot-Cold"}]\right\}\right\},
     AxesStyle → Black, LabelStyle → {14, GrayLevel[0], Bold},
     FrameStyle → Directive[Black, 20],
      FrameTicks \rightarrow {{{-0.1, 0.0, 0.1}, None}, {{-10, -5, 0, 5, 10}, None}},
     PlotStyle → {Orange, Thickness[0.01]}
```

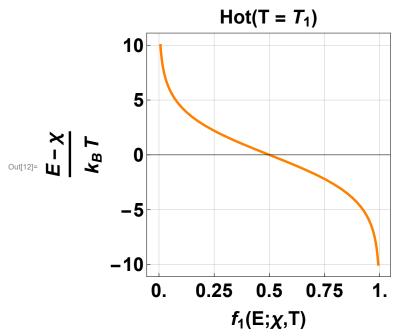
Hot-Cold



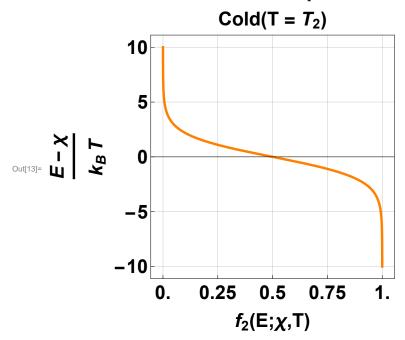
In[9]:= ParametricPlot[$\{1/(1 + Exp[x/2]), x\}$, $\{x, -10, 10\}$, AspectRatio $\rightarrow 1$, AxesLabel \rightarrow {"f1(E)", "(E- χ) / (kB T)"}, PlotLabel \rightarrow "Hot", GridLines \rightarrow Automatic] ParametricPlot $[\{1/(1 + Exp[x]), x\}, \{x, -10, 10\}, AspectRatio \rightarrow 1,$ AxesLabel \rightarrow {"f2(E)", "(E- χ) / (kB T)"}, PlotLabel \rightarrow "Cold", GridLines \rightarrow Automatic] ParametricPlot[$\{(1/(1+Exp[x/2]))-(1/(1+Exp[x])),x\},\{x,-10,10\},$ AspectRatio \rightarrow 1, AxesLabel \rightarrow {"f1(E) -f2(E)", "(E- χ) / (kB T)"}, GridLines \rightarrow Automatic]



```
ln[12]:= p1 = ParametricPlot[{1/(1 + Exp[x/2]), x},
           \{x, -10, 10\}, AspectRatio \rightarrow 1, (*AxesOrigin\rightarrow {0.5,0},*) Axes \rightarrow True,
           GridLines \rightarrow {{0.00, .25, 0.50, 0.75, 1.00}, {-10, -5, 0, 5, 10}},
           \label{eq:plotTheme} \textbf{PlotTheme} \rightarrow \texttt{"Scientific", FrameLabel} \rightarrow \left\{ \left\{ \texttt{HoldForm} \left[ \texttt{"} \frac{\texttt{E} - \chi}{\texttt{k}_B \, \texttt{T}} \texttt{"} \right] \text{, None} \right\} \text{,} \right.
               \{HoldForm["f_1(E;\chi,T)"], HoldForm["Hot(T = T_1)"]\}\}, AxesStyle \rightarrow Black,
           LabelStyle → {14, GrayLevel[0], Bold}, FrameStyle → Directive[Black, 20],
           FrameTicks \rightarrow {{{-10, -5, 0, 5, 10}, None}, {{0.00, .25, 0.50, 0.75, 1.00}, None}},
           PlotStyle → {Orange, Thickness[0.01]}
```

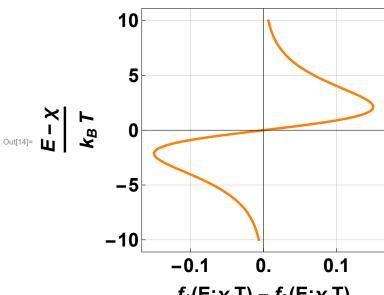


```
ln[13]:= ParametricPlot[\{1/(1+Exp[x]), x\}, \{x, -10, 10\},
         AspectRatio → 1, (*AxesOrigin→{0.5,0},*)Axes → True,
         GridLines \rightarrow {{0.00, .25, 0.50, 0.75, 1.00}, {-10, -5, 0, 5, 10}},
        \label{eq:plotTheme} \textit{PlotTheme} \rightarrow \textit{"Scientific", FrameLabel} \rightarrow \left\{ \left\{ \textit{HoldForm} \left[ "\frac{\textit{E} - \chi}{\textit{k}_{B} \; \textit{T}} " \right] \text{, None} \right\} \text{,} \right.
            \{HoldForm["f_2(E;\chi,T)"], HoldForm["Cold(T = T_2)"]\}\}, AxesStyle \rightarrow Black,
         LabelStyle → {14, GrayLevel[0], Bold}, FrameStyle → Directive[Black, 20],
         FrameTicks \rightarrow {{{-10, -5, 0, 5, 10}, None}, {{0.00, .25, 0.50, 0.75, 1.00}, None}},
         PlotStyle → {Orange, Thickness[0.01]}
```



$$\begin{split} & \text{In} [14] = \text{ParametricPlot} \Big[\Big\{ \Big(1 \, \Big/ \, \Big(1 + \text{Exp} \big[x \, \Big/ \, 2 \big] \Big) \Big) - \Big(1 \, \Big/ \, \Big(1 + \text{Exp} \big[x \, \Big) \Big) \Big), \, x \Big\}, \, \{x, -10, 10\}, \\ & \text{AspectRatio} \to 1, \, \text{Axes} \to \text{True}, \, \text{GridLines} \to \big\{ \big\{ -0.1, \, 0.0, \, 0.1 \big\}, \, \big\{ -10, \, -5, \, 0, \, 5, \, 10 \big\} \big\}, \\ & \text{PlotTheme} \to \text{"Scientific", FrameLabel} \to \Big\{ \Big\{ \text{HoldForm} \big["\frac{\mathsf{E} - \chi}{\mathsf{k_B} \, \mathsf{T}} " \big], \, \text{None} \Big\}, \\ & \big\{ \text{HoldForm} \big["f_1 (\mathsf{E}; \chi, \mathsf{T}) \, - \, f_2 (\mathsf{E}; \chi, \mathsf{T}) \, " \big], \, \text{HoldForm} \big["\text{Hot-Cold"} \big] \big\} \Big\}, \, \text{AxesStyle} \to \text{Black}, \\ & \text{LabelStyle} \to \big\{ 14, \, \text{GrayLevel} \big[0 \big], \, \text{Bold} \big\}, \, \text{FrameStyle} \to \text{Directive} \big[\text{Black}, \, 20 \big], \\ & \text{FrameTicks} \to \big\{ \big\{ \{ -10, \, -5, \, 0, \, 5, \, 10 \}, \, \text{None} \big\}, \, \big\{ \{ -0.1, \, 0.0, \, 0.1 \}, \, \text{None} \big\} \big\}, \\ \end{aligned}$$

Hot-Cold



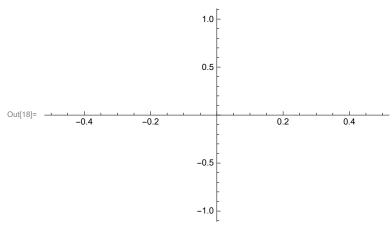
PlotStyle → {Orange, Thickness[0.01]}

 $f_1(\mathsf{E};\chi,\mathsf{T}) - f_2(\mathsf{E};\chi,\mathsf{T})$

In[15]:=
$$F[x_{-}] := 1/(1 + Exp[x]);$$

 $x[E_{-}] := \frac{E - \chi}{k_{B} * T};$

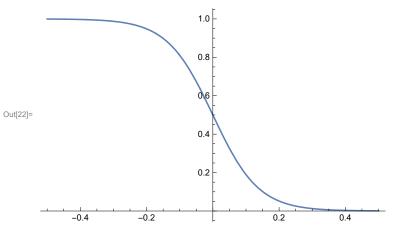
 $\mu = 0$; $k_B = 8.6 * 10^{-5}$; T = 300; Plot[F[x[E]], {E, -0.5, 0.5}]



In[19]:=
$$F[x_{]} := 1/(1 + Exp[x]);$$

$$x[E_{]} := \frac{E - \chi}{k_{B} * T};$$

 $\chi = 0$; $k_B = 8.6 * 10^{-5}$; T = 800; $Plot[F[X[E]], \{E, -0.5, 0.5\}]$



In[23]:=
$$F[E_{-}] := 1 / (1 + Exp[\frac{E - \chi}{k * T}]);$$

 $\chi = 0; k = 8.6 * 10^{-5}; T = 300;$
 $Plot[F[E], \{E, -0.5, 0.5\}]$

