

CODEBOOSTERS TECH - LeetCode Training

Time Complexity 🕒:

O(1) - Constant Time:

🔍 Explanation: In an $O(1)$ operation, the time it takes to complete the task does not depend on the size of the input. Whether the input has 1 item or 1 million items, the time taken remains the same.

💡 Real-world analogy: Think of a microwave. No matter how much food is in the microwave, the time it takes to start is the same. You're not waiting for it to "warm up" based on the amount of food inside.

💻 Example Code:

```
python

def get_first_element(arr):
    return arr[0] # O(1)
```

🔑 Code Explanation: The function `get_first_element` always returns the first element of the array `arr`. No matter how large the array is, accessing the first item takes constant time.

O(n) - Linear Time:

🔍 Explanation: In an $O(n)$ operation, the time it takes is directly proportional to the size of the input. If the input size doubles, the time taken will also double.

💡 Real-world analogy: Imagine you're checking every car in a parking lot to find the one with a flat tire. If the parking lot has 10 cars, it takes 10 minutes. If the lot has 100 cars, it takes 100 minutes.

💻 Example Code:

python

```
def print_all_elements(arr):  
    for item in arr: #  $O(n)$   
        print(item)
```

🔑 Code Explanation: Here, `print_all_elements` loops over every item in the list `arr` and prints it. The number of iterations grows with the size of `arr`. So, if `arr` has 10 items, it loops 10 times, and if `arr` has 100 items, it loops 100 times.

$O(n^2)$ - Quadratic Time:

🔍 Explanation: In $O(n^2)$, the time grows much faster because you're performing an operation inside another operation (nested loops). The time increases with the square of the input size.

💡 Real-world analogy: If you're organizing a party and calling every guest, and then for every guest, you call their +1 (a second guest), the number of calls is proportional to the square of the number of guests.

💻 Example Code:

python

```
def print_all_pairs(arr):  
    for i in arr:      #  $O(n)$   
        for j in arr:  #  $O(n)$   
            print(i, j) #  $O(n^2)$ 
```

🔑 Code Explanation: The function `print_all_pairs` contains two nested loops. The outer loop iterates over every item in `arr`, and for each item, the inner loop iterates over every item again. So, if the array has `n` elements, this code runs `n * n` times, resulting in $O(n^2)$.

$O(\log n)$ - Logarithmic Time:

🔍 Explanation: $O(\log n)$ is more efficient because each operation cuts the input size in half, making the task faster than linear or quadratic time. Binary search is a classic example where we divide the data into two parts each time.

💡 Real-world analogy: It's like a library with sorted books. Instead of going through each book, you open the book in the middle and decide if you need to go left or right. Every decision eliminates half of the books.

💻 Example Code:

```
python

def binary_search(arr, target):
    left, right = 0, len(arr) - 1
    while left <= right:
        mid = (left + right) // 2
        if arr[mid] == target:
            return mid    # O(log n)
        elif arr[mid] < target:
            left = mid + 1
        else:
            right = mid - 1
    return -1
```

🔑 Code Explanation: The `binary_search` function splits the input array in half during each iteration. Instead of checking every element like in linear search, you eliminate half the list with each step. This leads to a much faster search in larger lists, resulting in $O(\log n)$ time complexity.

$O(n \log n)$ - Log-linear Time:

🔍 Explanation: $O(n \log n)$ is more efficient than $O(n^2)$ but still slower than $O(n)$ or $O(\log n)$. It's often seen in efficient sorting algorithms like Merge Sort or Quick Sort, where the input is divided and sorted in parts.

💡 Real-world analogy: Imagine you're sorting a deck of cards. You split the deck into smaller piles ($\log n$), then merge those piles back together (n). The complexity grows as the input size grows, but it's more efficient than squaring the number of steps.

💻 Example Code:

```
python

def merge_sort(arr):
    if len(arr) > 1:
```

```
mid = len(arr) // 2
left = arr[:mid]
right = arr[mid:]

merge_sort(left)    # O(n log n)
merge_sort(right)

# Merge logic...
```

🔑 Code Explanation: `merge_sort` is a divide and conquer algorithm that splits the array into two halves ($O(\log n)$ steps) and sorts them ($O(n)$ for each step). So, in total, the time complexity is $O(n \log n)$.

Space Complexity 📁:

$O(1)$ - Constant Space:

🔍 Explanation: In $O(1)$ space complexity, you only need a fixed amount of space regardless of the input size. The amount of memory used doesn't change with the input.

💡 Real-world analogy: Think of a fixed-size bag. Whether you're packing one item or 100 items, the bag is still the same size.

💻 Example Code:

```
python

def multiply(x, y):
    return x * y    # O(1) space complexity
```

🔑 Code Explanation: This function only requires constant space because it's only storing the two variables `x` and `y` to perform the multiplication. No matter how large the numbers are, the space needed stays constant.

$O(n)$ - Linear Space:

🔍 Explanation: In $O(n)$ space complexity, the amount of memory used increases directly with the input size. More input means more space required.

💡 Real-world analogy: Think of packing a bag where you put one item per input. If there are 10 items, you need 10 bags. If there are 100 items, you need 100 bags.

💻 Example Code:

```
python

def store_elements(arr):
    result = []
    for element in arr:
        result.append(element)    #  $O(n)$  space complexity
    return result
```

🔑 Code Explanation: The function `store_elements` creates a new list `result` and appends every element from the input list `arr`. The space complexity grows with the size of the input, hence $O(n)$ space.

Wrap-up END:

Time Complexity shows us how fast an algorithm works, depending on input size.

Space Complexity tells us how much memory is needed, again depending on input size.

By analyzing both, you can choose the best algorithm based on performance constraints (e.g., large data sets, memory limitations).

Key Tip :

Always try to break down the code into real-life examples that are familiar to you. This will help you internalize the complexity and avoid getting overwhelmed with abstract definitions.



Engaging Real-Life Scenarios & Understanding Time and Space Complexity 🔍

Searching for a Book in a Library 📖:

- Time Complexity: If you search for a book in a disorganized library, it takes $O(n)$ time because you have to go shelf by shelf. But in an organized library (sorted books), you use $O(\log n)$ time.
 - Space Complexity: The space complexity is $O(1)$ because you don't need any extra space, just a memory of where you've already looked.
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Organizing a Birthday Party 🎉:

- Time Complexity: If you send one invitation to each friend individually, it's $O(n)$. But, if you send an email to a group of friends, it could be $O(1)$.
 - Space Complexity: If you keep a list of who accepted the invite, it's $O(n)$. But if you don't keep any list, it's $O(1)$.
-

Building a Shopping List 🛒:

- Time Complexity: If you go through each store and pick the items one by one, it's $O(n)$. If you use a catalog and jump straight to the items (like binary search), it's $O(\log n)$.
 - Space Complexity: If you keep your shopping list in your phone ($O(n)$), you need space for each item. If you don't store anything, it's $O(1)$.
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Running a Marathon:

Time Complexity:

- **$O(n)$:** Imagine you're running a marathon, and you need to reach each checkpoint one by one. The time it takes to complete the marathon is proportional to the number of checkpoints you pass. If there are 20 checkpoints, you spend time at 20 places; if there are 100, you pass 100 times. So, $O(n)$ time complexity, where "n" is the number of checkpoints.
- **$O(1)$:** If there was a checkpoint in the middle where you automatically teleport to the finish line, that would be $O(1)$ —the time doesn't change based on the number of checkpoints. 🏁

Space Complexity:

- **$O(1)$:** If you're running with just a water bottle, you don't need more space no matter how long the race is. Your space requirement is $O(1)$ because it doesn't depend on the race length.
 - **$O(n)$:** If you need to carry a separate bag for each checkpoint, where you store items for each checkpoint along the way, the space complexity increases with each checkpoint, making it $O(n)$.
-

Building a House:

Time Complexity:

- **$O(n)$:** Think about building a house, where you need to lay down one brick at a time. The more bricks you need to place, the more time you will spend. If you're placing 100 bricks, it takes longer than placing 10. This represents $O(n)$.
- **$O(n^2)$:** Now, imagine if you needed to place two types of bricks in a pattern, so for every brick you place, you need to place another one in a specific order. This increases the total work much faster and could be represented as $O(n^2)$.

Space Complexity:

- **$O(1)$:** If you're building a house with only a hammer, nails, and a small toolbox, you only need a fixed amount of space.

- **$O(n)$:** However, if you need to store every type of tool and material for each step of the house, your storage needs increase as the house gets bigger, which would be $O(n)$ space.
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Cooking a Meal:

Time Complexity:

- **$O(1)$:** You only need to boil water for a specific amount of time, no matter how many cups you want to make. Whether you make 1 cup of tea or 100 cups, the time remains constant.
- **$O(n)$:** On the other hand, if you're chopping vegetables and you chop 1 vegetable at a time, the time increases linearly with the number of vegetables. If you chop 10, it takes 10 minutes; if you chop 100, it takes 100 minutes.

Space Complexity:

- **$O(1)$:** If you're cooking a meal with just a pot and a spoon, the space needed remains constant regardless of the ingredients.
 - **$O(n)$:** But if you're cooking a large feast and you need multiple pots, pans, and bowls to hold each dish separately, the space required grows with the number of dishes you're preparing. This would be $O(n)$.
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Playing a Video Game:

Time Complexity:

- **$O(1)$:** If you press a button to jump in a game, no matter how many obstacles or levels there are, the action itself (jumping) takes the same amount of time. That's $O(1)$ time complexity.
- **$O(n)$:** If you need to defeat a monster at each level, and the time it takes to defeat each monster increases with each level, the time complexity would be $O(n)$, because you need to face each monster one by one as the levels increase.

Space Complexity:

- **$O(1)$:** The game's map might require constant space because no matter how many levels or zones exist, the space needed to load the game itself remains the same.
 - **$O(n)$:** If you store each level's progress in a separate save file, your storage needs will grow with each level you unlock, which results in $O(n)$ space complexity.
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Packing for a Trip:

Time Complexity:

- $O(1)$: If you already know exactly what you need to pack for your trip (a shirt, socks, and toothpaste), then the time it takes to pack is $O(1)$.
- $O(n)$: But if you need to check every item in your closet and pack them one by one, the time it takes to pack is $O(n)$, where "n" is the number of items.

Space Complexity:

- $O(1)$: If you have a fixed-size suitcase that doesn't change, you'll always need the same amount of space regardless of the items you're packing.
 - $O(n)$: If you use multiple suitcases for each item (one for shoes, one for clothes, etc.), the space needed grows with the number of items you're packing. This is $O(n)$ space complexity.
-



Organizing a Closet:

Time Complexity:

- $O(n)$: If you're organizing clothes, and you need to check each piece of clothing to decide where it goes, the time it takes depends on how many clothes you have. If you have 100 items, it takes longer than organizing just 10.
- $O(\log n)$: But if you organize your closet by categories and can immediately know where to place an item based on where it belongs (using binary search), the time it takes to organize is much more efficient and follows $O(\log n)$ time complexity.

Space Complexity:

- $O(1)$: If you just need one shelf to place all your clothes in an organized way, the space remains constant regardless of the number of clothes.
 - $O(n)$: If you need a different drawer for each category (pants, shirts, jackets, etc.), the space required grows with the number of categories, making it $O(n)$.
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Road Trip (Driving Between Cities):

Time Complexity:

- $O(1)$: If you're going to stop at only one place during the road trip (say a gas station) and don't need to worry about additional stops, the time complexity remains constant, regardless of how many cities you pass.
- $O(n)$: If you stop at each city to explore, the time increases with each stop, resulting in $O(n)$ time complexity, where "n" is the number of cities you pass.

Space Complexity:

- $O(1)$: If you're only packing for the essentials (like your wallet and phone), your space remains constant.
 - $O(n)$: But if you need to carry large bags for each stop, your space needs grow with the number of cities you visit, making it $O(n)$ space complexity.
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Making a Pizza:

Time Complexity:

- $O(1)$: If the dough is pre-made and all you have to do is put the toppings and bake it, the time remains constant, no matter the size of the pizza.
- $O(n)$: If you're making dough from scratch and it takes longer to knead and roll out the dough for each extra large pizza, then your time complexity increases with the size of the pizza, represented as $O(n)$.

Space Complexity:

- $O(1)$: If you're making one pizza, you'll need a fixed amount of space for your dough and ingredients.
 - $O(n)$: If you're making a variety of pizzas with different sizes and toppings, your space complexity increases with each pizza.
-

Wrap-up 💡:

Time Complexity 🕒:

- **$O(1)$: Constant time** — the operation takes the same amount of time regardless of input size.
- **$O(n)$: Linear time** — the time taken grows directly with the size of the input.
- **$O(n^2)$: Quadratic time** — the time taken grows exponentially with the input size due to nested operations.
- **$O(\log n)$: Logarithmic time** — the time taken grows slowly as the input size increases, often halving the problem size each step (e.g., binary search).
- **$O(n \log n)$: Log-linear time** — typically seen in efficient sorting algorithms where input is divided and processed recursively.
- **$O(2^n)$: Exponential time** — the time grows extremely fast as the input size increases, doubling with each step.
- **$O(n!)$: Factorial time** — the time grows so quickly that it becomes impractical even for small input sizes, common in problems involving permutations.

Space Complexity 📁:

- **$O(1)$: Constant space** — the memory required doesn't change with input size.
- **$O(n)$: Linear space** — the memory grows directly with the size of the input.
- **$O(n^2)$: Quadratic space** — the memory requirement grows with the square of the input size, often due to nested data structures.
- **$O(\log n)$: Logarithmic space** — the memory requirement grows slowly with input size, often seen in recursive algorithms with minimal space usage.
- **$O(n \log n)$: Log-linear space** — space grows based on a combination of linear and logarithmic factors, common in divide-and-conquer algorithms.
- **$O(2^n)$: Exponential space** — the memory usage grows rapidly with the input size, often seen in recursive algorithms that generate a large number of states.
- **$O(n!)$: Factorial space** — memory usage increases extremely quickly, typically found in algorithms dealing with permutations or combinations of input.