

Lab Question: Genetic Algorithm

Code:

```
import numpy as np

# Objective: Calculate the total distance for a given set of routes
def objective(routes, distance_matrix):
    total_distance = 0
    for route in routes:
        # Add the distance from depot to the first location
        total_distance += distance_matrix[0][route[0]]
        # Add the distances between consecutive locations in the route
        for i in range(len(route) - 1):
            total_distance += distance_matrix[route[i]][route[i + 1]]
        # Add the distance from the last location back to depot
        total_distance += distance_matrix[route[-1]][0]
    return total_distance

# Generate an initial population with more diverse routes
def initialize_population(n_pop, n_locations, n_vehicles):
    population = []
    for _ in range(n_pop):
        # Randomly generate routes (random permutations of locations)
        routes = []
        remaining_locations = list(range(1, n_locations)) # Exclude depot (location 0)
        for _ in range(n_vehicles):
            route_size = len(remaining_locations) // (n_vehicles - len(routes))
            route = np.random.choice(remaining_locations, size=route_size, replace=False).tolist()
            for loc in route:
                remaining_locations.remove(loc)
            routes.append(route)
        population.append(routes)
    return population

# Evaluate fitness of the population (lower is better)
def evaluate_fitness(population, distance_matrix):
    return [objective(routes, distance_matrix) for routes in population]

# Tournament selection
def tournament_selection(population, scores, k=3):
    selected = np.random.choice(len(population), k, replace=False)
    best = selected[np.argmin([scores[i] for i in selected])]
    return population[best]
```

Order Crossover (OX)

```
def crossover(p1, p2):
    size = len(p1)
    child = [None] * size
    start, end = sorted(np.random.choice(range(size), 2, replace=False))
    child[start:end+1] = p1[start:end+1]
```

Fill remaining positions

```
p2_idx = 0
for i in range(size):
    if child[i] is None:
        while p2[p2_idx] in child:
            p2_idx += 1
        child[i] = p2[p2_idx]
return child
```

Swap mutation (increased mutation rate)

```
def mutation(routes, n_locations):
    route = routes[np.random.randint(len(routes))] # Select a random route to mutate
    if len(route) > 1:
        i, j = np.random.choice(len(route), 2, replace=False)
        route[i], route[j] = route[j], route[i] # Swap two locations in the route
    return routes
```

Genetic algorithm for solving VRP

```
def genetic_algorithm(distance_matrix, n_iter, n_pop, n_vehicles, r_mut, r_cross, elitism=True):
    n_locations = len(distance_matrix) # Including depot (location 0)
    population = initialize_population(n_pop, n_locations, n_vehicles)
    best, best_eval = population[0], objective(population[0], distance_matrix)
```

```
for gen in range(n_iter):
    scores = evaluate_fitness(population, distance_matrix)
```

Track and print the best fitness score

```
for i in range(n_pop):
    if scores[i] < best_eval:
        best, best_eval = population[i], scores[i]
        print(f'Generation {gen}: New best solution with distance {scores[i]:.2f}')
```

Create next generation

```
children = []
for _ in range(n_pop):
    p1 = tournament_selection(population, scores)
    p2 = tournament_selection(population, scores)
```

```

        offspring = crossover(p1, p2) if np.random.rand() < r_cross else p1
        offspring = mutation(offspring, n_locations) if np.random.rand() < r_mut else offspring
        children.append(offspring)

    # Elitism: carry the best solution to the next generation
    if elitism:
        children[np.argmax([objective(child, distance_matrix) for child in children])] = best

    population = children

return best, best_eval

# Example distance matrix with 10 locations (including the depot at location 0)
distance_matrix = np.array([
    [0, 10, 15, 20, 25, 30, 35, 40, 45, 50], # Depot (location 0)
    [10, 0, 35, 25, 30, 10, 15, 20, 25, 30], # Location 1
    [15, 35, 0, 20, 10, 15, 20, 25, 30, 35], # Location 2
    [20, 25, 20, 0, 15, 20, 25, 30, 35, 40], # Location 3
    [25, 30, 10, 15, 0, 10, 15, 20, 25, 30], # Location 4
    [30, 10, 15, 20, 10, 0, 5, 10, 15, 20], # Location 5
    [35, 15, 20, 25, 15, 5, 0, 5, 10, 15], # Location 6
    [40, 20, 25, 30, 20, 10, 5, 0, 5, 10], # Location 7
    [45, 25, 30, 35, 25, 15, 10, 5, 0, 5], # Location 8
    [50, 30, 35, 40, 30, 20, 15, 10, 5, 0] # Location 9
])

# Parameters
n_iter = 100 # Number of generations
n_pop = 50 # Population size
n_vehicles = 3 # Number of vehicles
r_mut = 0.2 # Mutation rate
r_cross = 0.7 # Crossover rate

best_routes, best_score = genetic_algorithm(distance_matrix, n_iter, n_pop, n_vehicles, r_mut,
r_cross)
print("Optimal routes:", best_routes)
print(f"Total distance: {best_score:.2f}")

```

Output:

```
➡ Generation 0: New best solution with distance 245.00  
Generation 0: New best solution with distance 240.00  
Generation 1: New best solution with distance 225.00  
Generation 1: New best solution with distance 220.00  
Generation 2: New best solution with distance 210.00  
Generation 2: New best solution with distance 205.00  
Generation 6: New best solution with distance 200.00  
Generation 10: New best solution with distance 185.00  
Optimal routes: [[4, 5, 2], [3, 5, 1], [2, 3, 4]]  
Total distance: 185.00
```