

Algorithm 1: Genetic Algorithm for Optimization Problems

Code:

```
import numpy as np

# Objective function:  $f(x) = x^2$ 
def objective(x):
    return x[0] ** 2 + 2*x[0] + 1

# Initialization: generate initial population
def initialize_population(bounds, n_pop):
    return [np.random.uniform(bounds[0], bounds[1], 1).tolist() for _ in range(n_pop)]

# Fitness evaluation
def evaluate_fitness(pop):
    return [objective(ind) for ind in pop]

# Roulette wheel selection
def roulette_wheel_selection(pop, scores):
    total_fitness = sum(scores)
    probabilities = [1 - (score / total_fitness) for score in scores]
    selection_ix = np.random.choice(len(pop), p=np.array(probabilities) / sum(probabilities))
    return pop[selection_ix]

# Crossover: linear combination of parents
def crossover(p1, p2, alpha=0.5):
    offspring = alpha * p1[0] + (1 - alpha) * p2[0]
    return [offspring] # Ensure offspring is a list

# Mutation: random value within bounds
def mutation(individual, bounds, r_mut):
    if np.random.rand() < r_mut:
        return [np.random.uniform(bounds[0], bounds[1])]
    return individual

# Genetic algorithm
def genetic_algorithm(bounds, n_iter, n_pop, r_mut):
    # Initialize population
    pop = initialize_population(bounds, n_pop)
    best, best_eval = pop[0], objective(pop[0])
```

```
for gen in range(n_iter):
    # Evaluate fitness
    scores = evaluate_fitness(pop)

    # Check for new best solution
    for i in range(n_pop):
        if scores[i] < best_eval:
            best, best_eval = pop[i], scores[i]
            print(f">{gen}, new best f({pop[i]}) = {scores[i]:.6f}")

    # Select parents and create offspring
    children = []
    for _ in range(n_pop):
        p1 = roulette_wheel_selection(pop, scores)
        p2 = roulette_wheel_selection(pop, scores)
        offspring = crossover(p1, p2)
        offspring = mutation(offspring, bounds, r_mut) # Pass as list
        children.append(offspring)

    # Replace population with new offspring
    pop = children

    return [best, best_eval]

# Define range for input
bounds = [-10.0, 10.0]
# Define the total iterations
n_iter = 50
# Define the population size
n_pop = 100
# Mutation rate
r_mut = 0.1

# Perform the genetic algorithm search
best, score = genetic_algorithm(bounds, n_iter, n_pop, r_mut)
print('Done!')
print(f'f({best}) = {score:.6f}')
```

Output:

```
>0, new best f([-5.666534385599229]) = 21.776543
>0, new best f([1.080175298094792]) = 4.327129
>0, new best f([-1.5931328574092856]) = 0.351807
>0, new best f([-1.5653111777364508]) = 0.319577
>0, new best f([-0.8482241989814483]) = 0.023036
>0, new best f([-1.0705269641866977]) = 0.004974
>1, new best f([-0.9332442167834278]) = 0.004456
>1, new best f([-1.022829583444282]) = 0.000521
>6, new best f([-0.9958642058435989]) = 0.000017
>14, new best f([-0.9989132354583119]) = 0.000001
>40, new best f([-0.999748411998941]) = 0.000000
Done!
f([-0.999748411998941]) = 0.000000
```