## Max Entropy Theorems

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**Theorem 1 (Epstein)** Let  $(X \times Y, \mu \times \nu)$  be a product computable measure space. Let  $A : \mathbb{N} \to X$ ,  $B : \mathbb{N} \to Y$  be injective functions with  $\mathbf{I}(\langle A, B \rangle : \mathcal{H}) < \infty$ . For  $s \in \mathbb{N}$ , m < s, there exists  $2^{s-m}$  indices  $t < 2^s$  with  $\max\{\mathbf{G}_{\mu}(A(t)), \mathbf{G}_{\nu}(B(t))\} < -m + O(\log s)$ .

**Theorem 2 (Epstein)** Let L be the Lebesgue measure over  $\mathbb{R}$ ,  $(\mathcal{X}, \mu)$ ,  $(\mathcal{Y}, \nu)$  be non-atomic computable measure spaces. Let  $A:[0,1]\to\mathcal{X}$  and  $B:[0,1]\to\mathcal{Y}$  be continuous. Let  $\mathbf{I}(\langle A,B\rangle:\mathcal{H})<\infty$ . There is a constant c with  $L\{t\in[0,1]:\max\{\mathbf{G}_{\mu}(A(t)),\mathbf{G}_{\nu}(B(t))\}<\log\mu(X)-n\}>2^{-n-\mathbf{K}(n)-c}$ .