

# Maximum Entropy Theorem

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**Theorem 1 (Epstein)** *Let  $(X \times Y, \mu \times \nu)$  be a product computable measure space. Let  $A : \mathbb{N} \rightarrow X$ ,  $B : \mathbb{N} \rightarrow Y$  be injective functions with  $\mathbf{I}(\langle A, B \rangle : \mathcal{H}) < \infty$ . For  $s \in \mathbb{N}$ ,  $m < s$ , there exists  $2^{s-m}$  indices  $t < 2^s$  with  $\max\{\mathbf{G}_\mu(A(t)), \mathbf{G}_\nu(B(t))\} < -m + O(\log s)$ .*