Cincinnati Reds

Assessment 2.5

Sam Rizzuto

 $7~{\rm February}~2022$

Load Necessary Libraries

```
library(dplyr)
library(mgcv)
library(parallel)
library(visreg)
library(ggplot2)
library(randomForest)
library(e1071)
library(caret)
library(flexclust)
library(factoextra)
library(knitr)
#set working directory
setwd("~/Desktop/22-ds")
#load in datasets
trainDF <- read.csv("train.csv")</pre>
testDF <- read.csv("test.csv")</pre>
```

Filtering Data and Removing Outliers Through IQR

```
Q1_Angle <- quantile(trainDF$ANGLE, .25)
Q3_Angle <- quantile(trainDF$ANGLE, .75)
IQR Angle <- IQR(trainDF$ANGLE)</pre>
Q1_EXIT_SPEED <- quantile(trainDF$EXIT_SPEED, .25)
Q3_EXIT_SPEED <- quantile(trainDF$EXIT_SPEED, .75)
IQR_EXIT_SPEED <- IQR(trainDF$EXIT_SPEED)</pre>
Q1_DIRECTION <- quantile(trainDF$DIRECTION, .25)
Q3 DIRECTION <- quantile(trainDF$DIRECTION, .75)
IQR_DIRECTION <- IQR(trainDF$DIRECTION)</pre>
Q1_ReleaseSpeed <- quantile(trainDF$RELEASE_SPEED, .25)
Q3_ReleaseSpeed <- quantile(trainDF$RELEASE_SPEED, .75)
IQR_ReleaseSpeed <- IQR(trainDF$RELEASE_SPEED)</pre>
Q1_PlateX <- quantile(trainDF$PLATE_X, .25)
Q3_PlateX <- quantile(trainDF$PLATE_X, .75)
IQR_PlateX <- IQR(trainDF$PLATE_X)</pre>
Q1_PlateZ <- quantile(trainDF$PLATE_Z, .25)
Q3_PlateZ <- quantile(trainDF$PLATE_Z, .75)
IQR_PlateZ <- IQR(trainDF$PLATE_Z)</pre>
Q1_InducedVertBreak <- quantile(trainDF$INDUCED_VERTICAL_BREAK, .25)
Q3_InducedVertBreak <- quantile(trainDF$INDUCED_VERTICAL_BREAK, .75)
IQR_InducedVertBreak <- IQR(trainDF$INDUCED_VERTICAL_BREAK)</pre>
Q1_HorizontalBreak <- quantile(trainDF$HORIZONTAL_BREAK, .25)
Q3_HorizontalBreak <- quantile(trainDF$HORIZONTAL_BREAK, .75)
IQR_HorizontalBreak <- IQR(trainDF$HORIZONTAL_BREAK)</pre>
Q1_VertApproachAngle <- quantile(trainDF$VERTICAL_APPROACH_ANGLE, .25)
Q3_VertApproachAngle <- quantile(trainDF$VERTICAL_APPROACH_ANGLE, .75)
IQR_VertApproachAngle <- IQR(trainDF$VERTICAL_APPROACH_ANGLE)</pre>
```

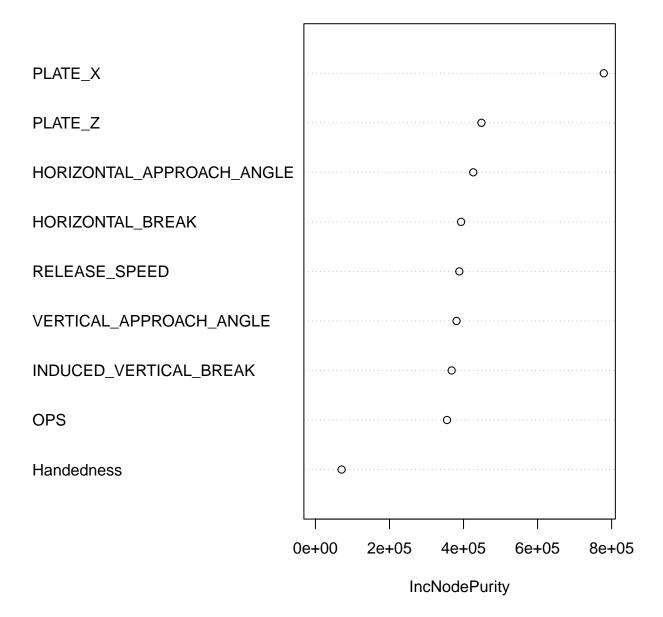
```
Q1_HorizApproachAngle <- quantile(trainDF$HORIZONTAL_APPROACH_ANGLE, .25)
Q3_HorizApproachAngle <- quantile(trainDF$HORIZONTAL_APPROACH_ANGLE, .75)
IQR HorizApproachAngle <- IQR(trainDF$HORIZONTAL APPROACH ANGLE)
trainDF <- subset(trainDF, trainDF$ANGLE > (Q1_Angle - 1.5*IQR_Angle) &
                   trainDF$ANGLE < (Q3_Angle + 1.5*IQR_Angle))</pre>
trainDF <- subset(trainDF, trainDF$EXIT SPEED > (Q1 EXIT SPEED - 1.5*IQR EXIT SPEED) &
                   trainDF$EXIT_SPEED < (Q3_EXIT_SPEED + 1.5*IQR_EXIT_SPEED))</pre>
trainDF <- subset(trainDF, trainDF$DIRECTION > (Q1_DIRECTION - 1.5*IQR_DIRECTION) &
                   trainDF$DIRECTION < (Q3_DIRECTION + 1.5*IQR_DIRECTION))
trainDF <- subset(trainDF, trainDF$RELEASE_SPEED > (Q1_ReleaseSpeed - 1.5*IQR_ReleaseSpeed) &
                   trainDF$RELEASE_SPEED < (Q3_ReleaseSpeed + 1.5*IQR_ReleaseSpeed))
trainDF <- subset(trainDF, trainDF$PLATE_X > (Q1_PlateX - 1.5*IQR_PlateX) &
                   trainDF$PLATE_X < (Q3_PlateX + 1.5*IQR_PlateX))</pre>
trainDF <- subset(trainDF, trainDF$PLATE_Z > (Q1_PlateZ - 1.5*IQR_PlateZ) &
                   trainDF$PLATE_Z < (Q3_PlateZ + 1.5*IQR_PlateZ))</pre>
trainDF <- subset(trainDF, trainDF$INDUCED_VERTICAL_BREAK > (Q1_InducedVertBreak - 1.5*IQR_InducedVertBreak) &
                   trainDF$INDUCED_VERTICAL_BREAK < (Q3_InducedVertBreak + 1.5*IQR_InducedVertBreak))
trainDF <- subset(trainDF, trainDF$HORIZONTAL_BREAK > (Q1_HorizontalBreak - 1.5*IQR_HorizontalBreak) &
                   trainDF$HORIZONTAL_BREAK < (Q3_HorizontalBreak + 1.5*IQR_HorizontalBreak))
trainDF <- subset(trainDF, trainDF$VERTICAL_APPROACH_ANGLE > (Q1_VertApproachAngle - 1.5*IQR_VertApproachAngle
                   trainDF$VERTICAL_APPROACH_ANGLE < (Q3_VertApproachAngle + 1.5*IQR_VertApproachAngle))
trainDF <- subset(trainDF, trainDF$HORIZONTAL_APPROACH_ANGLE >
                   (Q1_HorizApproachAngle - 1.5*IQR_HorizApproachAngle) &
                   trainDF$HORIZONTAL_APPROACH_ANGLE < (Q3_HorizApproachAngle + 1.5*IQR_HorizApproachAngle))
#disregard strikeouts, hbp, walks
trainDF <- trainDF %>% filter(PITCH_RESULT_KEY == "InPlay")
#goes from original 26417 rows to 24510 after cleaning
summary(trainDF)
                     AVG
                                      OBP
                                                      SLG
   BATTER_UID
 Min. : 2.00
                 Min. :0.1850 Min. :0.2570 Min. :0.2880
 1st Qu.: 36.00 1st Qu.:0.2523 1st Qu.:0.3210 1st Qu.:0.3770
 Median: 77.00 Median: 0.2670 Median: 0.3380 Median: 0.4125
 Mean: 76.96 Mean: 0.2665 Mean: 0.3387 Mean: 0.4216
 3rd Qu.:118.00
                 3rd Qu.:0.2860 3rd Qu.:0.3580 3rd Qu.:0.4545
                Max. :0.3330 Max. :0.4440 Max. :0.6130
 Max. :157.00
  VENUE KEY
                   OUTS
                                 BALLS
                                                 STRIKES
 Min. :2528 Min. :0.0000 Min. :0.000 Min. :0.000
 1st Qu.:2745    1st Qu.:0.0000    1st Qu.:0.000    1st Qu.:0.000
 Median: 2843 Median: 1.0000 Median: 1.000 Median: 1.000
 Mean :3510 Mean :0.9632 Mean :1.106 Mean :1.076
 3rd Qu.:4669 3rd Qu.:2.0000 3rd Qu.:2.000
                                              3rd Qu.:2.000
 Max. :5472 Max. :2.0000 Max. :4.000 Max.
                                                     :2.000
  BATS_LEFT
               THROWS_LEFT
                                PITCH_NUMBER RELEASE_SPEED
 Min. :0.0000 Min. :0.0000 Min. : 1.000 Min. : 70.69
 1st Qu.:0.0000 1st Qu.:0.0000 1st Qu.: 2.000 1st Qu.: 84.41
                 Median: 0.0000 Median: 3.000 Median: 89.41
 Median :0.0000
 Mean :0.4092
                 Mean :0.2502
                                Mean : 3.369
                                                 Mean : 88.48
 3rd Qu.:1.0000
                 3rd Qu.:1.0000
                                 3rd Qu.: 5.000
                                                 3rd Qu.: 92.82
 Max. :1.0000
                 Max. :1.0000 Max. :14.000
                                                 Max. :102.25
                      PLATE Z
                               INDUCED_VERTICAL_BREAK HORIZONTAL_BREAK
   PLATE X
 Min. :-1.526430 Min.
                         :0.8597 Min. :-14.609
                                                        Min.
                                                                :-26.017
 1st Qu.:-0.379685 1st Qu.:2.0195 1st Qu.: 3.729
                                                        1st Qu.:-10.609
 Median: 0.004996 Median: 2.3900 Median: 9.928
                                                        Median : -3.428
```

```
Mean :-0.001254 Mean :2.3965 Mean : 8.933
                                                      Mean : -2.280
 3rd Qu.: 0.372303 3rd Qu.:2.7676 3rd Qu.: 15.245
                                                      3rd Qu.: 5.561
 Max. : 1.518160 Max. :3.9181 Max. : 32.694
                                                      Max. : 25.943
 VERTICAL APPROACH ANGLE HORIZONTAL APPROACH ANGLE EXIT SPEED
Min. :-10.290 Min. :-4.1542
                                            Min. : 51.29
                                            1st Qu.: 81.23
 1st Qu.: -7.252
                     1st Qu.:-0.3791
 Median : -6.208
                                            Median : 91.49
                    Median : 0.8640
                      Mean : 0.7543
 Mean : -6.371
                                            Mean : 89.32
 3rd Qu.: -5.376
                      3rd Qu.: 2.0378
                                             3rd Qu.: 98.98
 Max. : -2.787
                     Max. : 5.7566
                                             Max. :118.64
    ANGLE
                DIRECTION
                                 EVENT_RESULT_KEY PITCH_RESULT_KEY
Min. :-58.917 Min. :-68.576 Length:24510
                                                  Length: 24510
 Class : character
 Median: 13.619 Median: -1.480 Mode: character
                                                  Mode : character
 Mean : 13.177 Mean : -1.374
 3rd Qu.: 29.796 3rd Qu.: 14.795
 Max. : 82.393 Max. : 65.317
      PA
                               X2B
                X1B
                                               ХЗВ
 Min. :1 Min. :0.0000 Min. :0.00000 Min. :0.000000
 1st Qu.:1 1st Qu.:0.0000 1st Qu.:0.00000 1st Qu.:0.000000
 Median: 1 Median: 0.0000 Median: 0.00000 Median: 0.000000
 Mean :1 Mean :0.2225 Mean :0.08156 Mean :0.008772
 3rd Qu.:1 3rd Qu.:0.0000 3rd Qu.:0.00000 3rd Qu.:0.000000
 Max. :1 Max. :1.0000 Max. :1.00000 Max. :1.000000
     HR
 Min. :0.00000
 1st Qu.:0.00000
 Median :0.00000
 Mean :0.05859
 3rd Qu.:0.00000
 Max. :1.00000
#######################
#create ops and handedness variables
trainDF <- trainDF %>% mutate(OPS = OBP + SLG)
testDF <- testDF %>% mutate(OPS = OBP + SLG)
trainDF <- trainDF %>% mutate(Handedness = if_else(THROWS_LEFT == BATS_LEFT, 0, 1))
testDF <- testDF %>% mutate(Handedness = if_else(THROWS_LEFT == BATS_LEFT, 0, 1))
#0 if same hands facing eachother, 1 if opposite
Random Forest Model
#running random forest on 3 prediction variables
rfTrainExitVelo <- randomForest(EXIT_SPEED ~ RELEASE_SPEED + PLATE_X + PLATE_Z +
                              INDUCED_VERTICAL_BREAK + HORIZONTAL_BREAK +
                              VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE +
                              OPS + Handedness, data = trainDF)
rfTrainAngle <- randomForest(ANGLE ~ RELEASE_SPEED + PLATE_X + PLATE_Z +
                            INDUCED_VERTICAL_BREAK + HORIZONTAL_BREAK +
                            VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE +
                            OPS + Handedness, data = trainDF)
rfTrainDirection <- randomForest(DIRECTION ~ RELEASE_SPEED + PLATE_X + PLATE_Z +
                               INDUCED_VERTICAL_BREAK + HORIZONTAL_BREAK +
                               VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE +
                               OPS + Handedness, data = trainDF)
```

#viewing importance plots of each model type to determine most significant vars in model

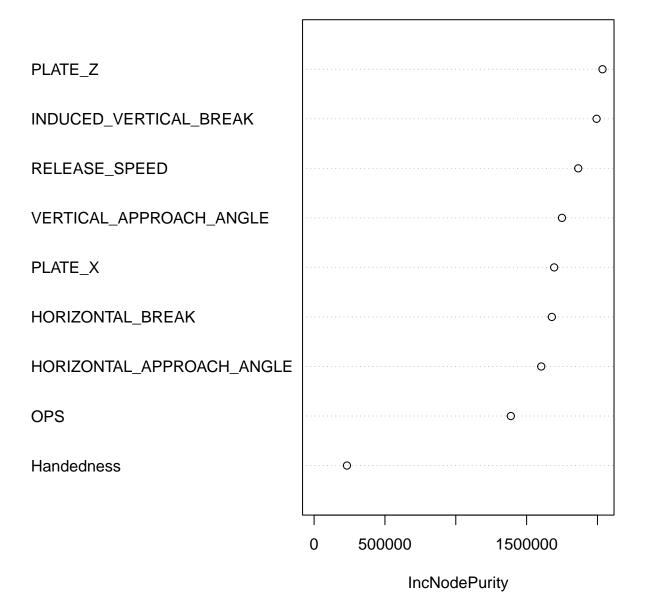
varImpPlot(rfTrainExitVelo) #drop handedness

rfTrainExitVelo



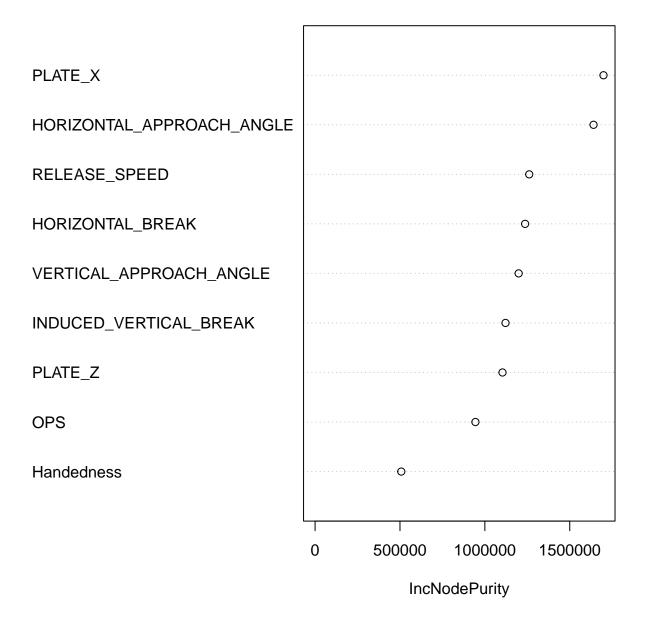
varImpPlot(rfTrainAngle) #drop ops, handedness

rfTrainAngle



varImpPlot(rfTrainDirection) #drop handedness

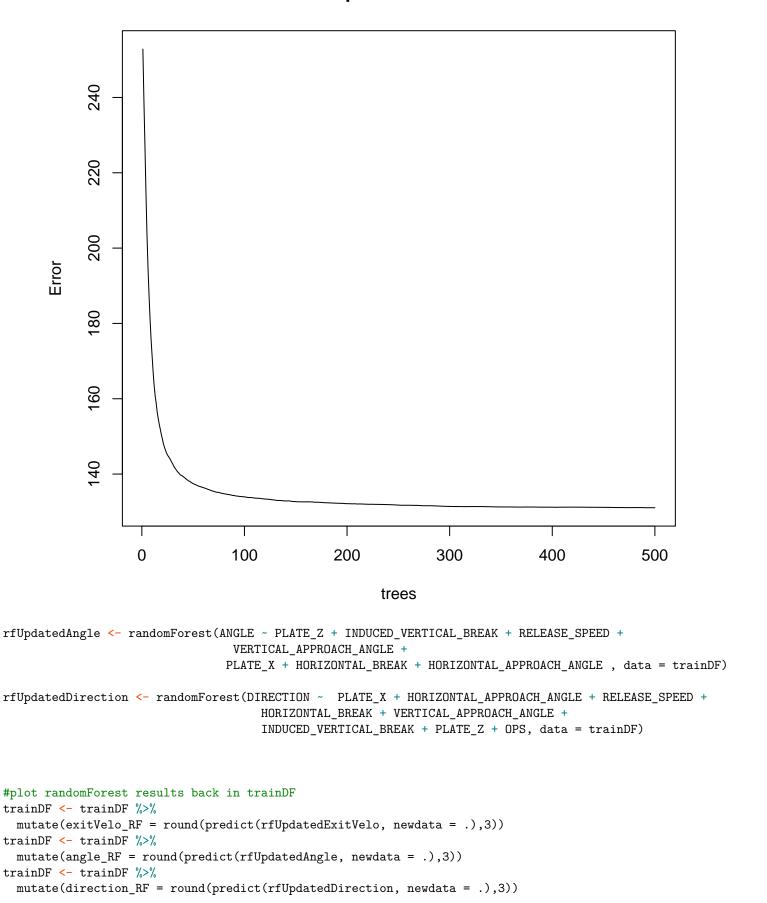
rfTrainDirection



	IncNodePurity
PLATE_X	757661.5
PLATE_Z	444438.7
HORIZONTAL_APPROACH_ANGLE	433829.5
HORIZONTAL_BREAK	396574.2
RELEASE_SPEED	394198.0
VERTICAL_APPROACH_ANGLE	392711.0
INDUCED_VERTICAL_BREAK	382078.9
OPS	364389.8

plot(rfUpdatedExitVelo) #error of rf exit velo model

rfUpdatedExitVelo



SVM Model

```
#running svm on exit velo
svmExitVelo <- svm(EXIT_SPEED ~ RELEASE_SPEED + PLATE_X + PLATE_Z +</pre>
                     INDUCED_VERTICAL_BREAK + HORIZONTAL_BREAK +
                     VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE +
                     OPS + Handedness, data = trainDF, cost = 100, gamma = 1)
#removing predictor variable of exit velo
svmExitVelo_Pred <- round(predict(svmExitVelo, trainDF[,-19]), 3)</pre>
#add svm exit velo into training df
trainDF <- trainDF %>% mutate(exitVelo_SVM = svmExitVelo_Pred)
#running svm on angle
svmAngle <- svm(ANGLE ~ RELEASE_SPEED + PLATE_X + PLATE_Z +</pre>
                  INDUCED_VERTICAL_BREAK + HORIZONTAL_BREAK +
                  VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE +
                  OPS + Handedness, data = trainDF, cost = 100, gamma = 1)
#removing predictor variable of angle
svmAngle_Pred <- round(predict(svmAngle, trainDF[,-20]), 3)</pre>
#adding prob of angle into training df
trainDF <- trainDF %>% mutate(angle_SVM = svmAngle_Pred)
#running svm model on direction
symDirection <- sym(DIRECTION ~ RELEASE SPEED + PLATE X + PLATE Z +
                      INDUCED VERTICAL BREAK + HORIZONTAL BREAK +
                      VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE +
                      OPS + Handedness, data = trainDF, cost = 100, gamma = 1)
#removing predictor variable of direction
svmDirection_Pred <- round(predict(svmDirection, trainDF[,-21]), 3)</pre>
#adding direction into training df
trainDF <- trainDF %>% mutate(direction_SVM = svmDirection_Pred)
Running GAM Model
####generalized additive model to include most important variables in training dataset
options(mc.cores = parallel::detectCores())#run model in parallel
gam_EV <- bam(EXIT_SPEED ~ RELEASE_SPEED + PLATE_X + PLATE_Z + INDUCED_VERTICAL_BREAK +
              HORIZONTAL BREAK + VERTICAL APPROACH ANGLE + HORIZONTAL APPROACH ANGLE + OPS + Handedness,
            data = trainDF, family = gaussian, method = "GCV.Cp")
summary(gam_EV) #drop platex, platez, vert approach angle
Family: gaussian
Link function: identity
Formula:
EXIT SPEED ~ RELEASE SPEED + PLATE X + PLATE Z + INDUCED VERTICAL BREAK +
    HORIZONTAL_BREAK + VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE +
    OPS + Handedness
Parametric coefficients:
                          Estimate Std. Error t value Pr(>|t|)
                          62.49285 3.30876 18.887 < 2e-16 ***
(Intercept)
                                      0.02492 7.398 1.42e-13 ***
RELEASE_SPEED
                           0.18434
```

```
0.17082 0.435 0.6635
PLATE_X
                       0.07433
PLATE Z
                       0.06586 0.21768 0.303 0.7622
INDUCED_VERTICAL_BREAK
                     0.03296 0.01815 1.816 0.0694 .
                      HORIZONTAL BREAK
VERTICAL_APPROACH_ANGLE -0.06991 0.15320 -0.456 0.6482
HORIZONTAL_APPROACH_ANGLE -0.08299 0.04914 -1.689 0.0912 .
                      12.22985 0.99085 12.343 < 2e-16 ***
OPS
Handedness
                       Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
R-sq.(adj) = 0.0163 Deviance explained = 1.67%
GCV = 154.34 Scale est. = 154.28
                               n = 24510
gam_EV_Upd <- bam(EXIT_SPEED ~ RELEASE_SPEED + INDUCED_VERTICAL_BREAK +</pre>
             HORIZONTAL_BREAK + HORIZONTAL_APPROACH_ANGLE + OPS + Handedness,
            data = trainDF, family = gaussian, method = "GCV.Cp")
gam_Ang <- bam(ANGLE ~ RELEASE_SPEED + PLATE_X + PLATE_Z + INDUCED_VERTICAL_BREAK +
            HORIZONTAL_BREAK + VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE + OPS + Handedness,
          data = trainDF, family = gaussian, method = "GCV.Cp")
summary(gam_Ang) #no drop
Family: gaussian
Link function: identity
Formula:
ANGLE ~ RELEASE_SPEED + PLATE_X + PLATE_Z + INDUCED_VERTICAL_BREAK +
   HORIZONTAL BREAK + VERTICAL APPROACH ANGLE + HORIZONTAL APPROACH ANGLE +
   OPS + Handedness
Parametric coefficients:
                     Estimate Std. Error t value Pr(>|t|)
                     80.24128 6.36217 12.612 < 2e-16 ***
(Intercept)
                     -1.09556 0.04791 -22.867 < 2e-16 ***
RELEASE SPEED
{\tt PLATE\_X}
                     -1.21579 0.32846 -3.702 0.000215 ***
PLATE_Z
                      INDUCED_VERTICAL_BREAK
                      HORIZONTAL_BREAK
VERTICAL_APPROACH_ANGLE
                       HORIZONTAL_APPROACH_ANGLE 0.75715 0.09448 8.014 1.16e-15 ***
                       7.73271 1.90523 4.059 4.95e-05 ***
OPS
                       Handedness
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
R-sq.(adj) = 0.0814 Deviance explained = 8.17%
                             n = 24510
GCV = 570.63 Scale est. = 570.4
gam_Ang_Upd <- gam_Ang</pre>
gam_Dir <- bam(DIRECTION ~ RELEASE_SPEED + PLATE_X + PLATE_Z + INDUCED_VERTICAL_BREAK +</pre>
            HORIZONTAL_BREAK + VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE + OPS + Handedness,
          data = trainDF, family = gaussian, method = "GCV.Cp")
summary(gam_Dir) #drop platez
```

Family: gaussian

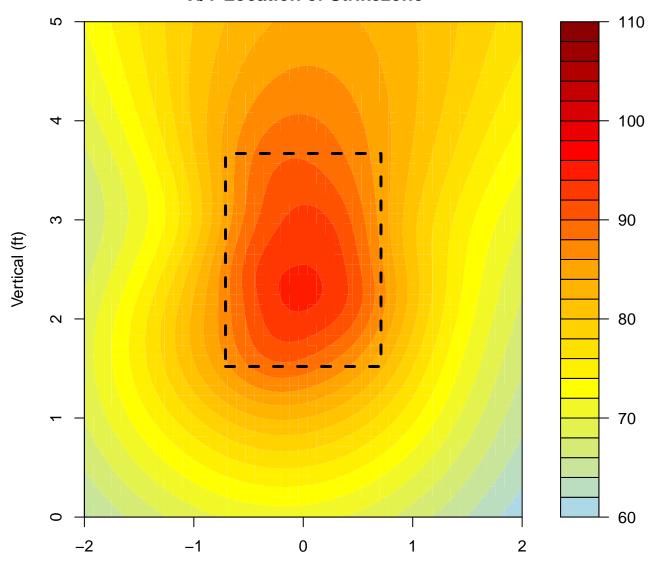
```
Link function: identity
Formula:
DIRECTION ~ RELEASE SPEED + PLATE X + PLATE Z + INDUCED VERTICAL BREAK +
   HORIZONTAL BREAK + VERTICAL APPROACH ANGLE + HORIZONTAL APPROACH ANGLE +
   OPS + Handedness
Parametric coefficients:
                       Estimate Std. Error t value Pr(>|t|)
(Intercept)
                       -8.41722 5.44751 -1.545 0.122323
                        RELEASE_SPEED
                        9.80451 0.28124 34.862 < 2e-16 ***
PLATE_X
PLATE_Z
                        INDUCED_VERTICAL_BREAK
                       HORIZONTAL_BREAK
VERTICAL_APPROACH_ANGLE
                        0.48057 0.25223 1.905 0.056760 .
HORIZONTAL_APPROACH_ANGLE 0.68024 0.08090 8.408 < 2e-16 ***
                       -9.65788 1.63132 -5.920 3.26e-09 ***
NPS
                        Handedness
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
R-sq.(adj) = 0.098
                   Deviance explained = 9.83%
GCV = 418.35 Scale est. = 418.18
gam_Dir_Upd <- bam(DIRECTION ~ RELEASE_SPEED + PLATE_X + INDUCED_VERTICAL_BREAK +
               HORIZONTAL BREAK + VERTICAL APPROACH ANGLE + HORIZONTAL APPROACH ANGLE + OPS + Handedness,
             data = trainDF, family = gaussian, method = "GCV.Cp")
#coefficients of each model to use in prediciting values
gamEV <- gam_EV_Upd$coefficients</pre>
gamAng <- gam_Ang_Upd$coefficients</pre>
gamDir <- gam_Dir_Upd$coefficients</pre>
trainDF <- trainDF %>%
 mutate(exitVelo_GAM = round(gamEV[1] + gamEV[2]*RELEASE_SPEED + gamEV[3]*INDUCED_VERTICAL_BREAK +
                             gamEV[4]*HORIZONTAL_BREAK + gamEV[5]*HORIZONTAL_APPROACH_ANGLE +
                             gamEV[6]*OPS + gamEV[7]*Handedness, 3))
trainDF <- trainDF %>%
 mutate(angle_GAM = round(gamAng[1] + gamAng[2]*RELEASE_SPEED + gamAng[3]*PLATE_X +
                          gamAng[4]*PLATE_Z + gamAng[5]*INDUCED_VERTICAL_BREAK +
                          gamAng[6] *HORIZONTAL_BREAK + gamAng[7] *VERTICAL_APPROACH_ANGLE +
                          gamAng[8]*HORIZONTAL_APPROACH_ANGLE +
                          gamAng[9]*OPS + gamAng[10]*Handedness, 3))
trainDF <- trainDF %>%
 mutate(direction_GAM = round(gamDir[1] + gamDir[2]*RELEASE_SPEED + gamDir[3]*PLATE_X +
                              gamDir[4]*INDUCED_VERTICAL_BREAK +gamDir[5]*HORIZONTAL_BREAK +
                              gamDir[6]*VERTICAL_APPROACH_ANGLE +
                              gamDir[7]*HORIZONTAL_APPROACH_ANGLE + gamDir[8]*OPS +
                              gamDir[9]*Handedness, 3))
```

Smaller GAM Model to Create Visuals

```
###smaller gam
#exit speed just on x and y location
```

```
gam_Small <- bam(EXIT_SPEED ~ s(PLATE_X, PLATE_Z),</pre>
            data = trainDF, family = gaussian, method = "GCV.Cp")
xs <- matrix(data=seq(from=-2, to=2, length=50), nrow=50, ncol=50)
ys <- t(matrix(data=seq(from=0,to=5, length=50), nrow=50, ncol=50))
gamSmallFit <- data.frame(PLATE_X = as.vector(xs), PLATE_Z = as.vector(ys))</pre>
exitVeloPred <- predict(gam_Small, gamSmallFit, types = "response")</pre>
exitVeloPred <- matrix(exitVeloPred, nrow = 50, ncol = 50)</pre>
density(exitVeloPred)
Call:
    density.default(x = exitVeloPred)
Data: exitVeloPred (2500 obs.); Bandwidth 'bw' = 1.451
       Х
                       У
 Min.
      :56.32 Min.
                       :2.710e-06
 1st Qu.:66.96 1st Qu.:5.796e-03
 Median :77.59 Median :2.556e-02
 Mean
      :77.59 Mean
                       :2.349e-02
 3rd Qu.:88.22 3rd Qu.:3.826e-02
 Max.
       :98.85 Max. :4.460e-02
summary(trainDF$EXIT_SPEED)
   Min. 1st Qu. Median
                        Mean 3rd Qu.
                                           Max.
  51.29 81.23 91.49
                        89.32 98.98 118.64
summary(trainDF$PLATE_X) #-1.5min to 1.5max, so round to -2 and 2 for x
            1st Qu.
                       Median
                                   Mean 3rd Qu.
     Min.
-1.526430 -0.379685 0.004996 -0.001254 0.372303 1.518160
summary(trainDF$PLATE_Z) #0.8 to 4.9, so round to 0 and 5
   Min. 1st Qu. Median
                           Mean 3rd Qu.
 0.8597 2.0195 2.3900 2.3965 2.7676 3.9181
#range of 60-110 to get full exit velo based on iqr
#width of HP is 23in
#height of strikezone is 25.79in based on baseball prospectus,
#with the bottom starting at 18.29in above the ground, which is 1.52ft
#to get the top of the zone, add 1.52ft plus the height (25.79in) to get 44.08in, or 3.67ft
#To create width of strikezone (17in), divide by 2 = 8.5in on each side from the middle
#and convert to ft = 0.71ft from the center
#so now when drawing strikezone, it has width -0.71 to 0.71 and height 1.52 to 3.67
filled.contour(x=seq(from=-2, to=2, length=50), y=seq(from=0, to=5, length=50), z = exitVeloPred,
               zlim=c(60,110),
               color.palette = colorRampPalette(c("lightblue", "yellow", "orange", "red", "darkred")),
               plot.axes = { rect(-0.71, 1.52, 0.71, 3.67, border="black", lty="dashed", lwd=3)
                 axis(1, at=c(-2,-1,0,1,2), pos=0, labels=c(-2,-1,0,1,2), las=0, col="black")
                 axis(2, at=c(0,1,2,3,4,5), pos=-2, labels=c(0,1,2,3,4,5), las=0, col="black")
                 },
               main = "Heat Map for Exit Velo Based on \n X/Y Location of Strikezone",
               ylab = "Vertical (ft)",
               xlab = "Horizontal Location of Pitch at Plate (ft)")
```

Heat Map for Exit Velo Based on X/Y Location of Strikezone

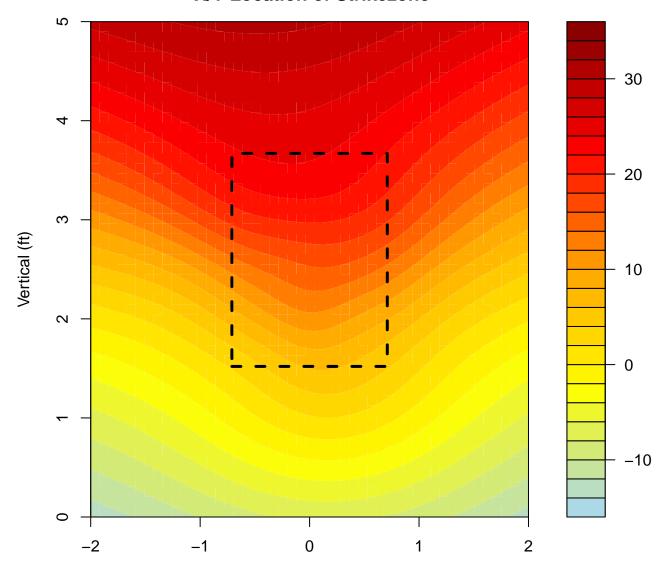


Horizontal Location of Pitch at Plate (ft)

```
#launch angle
gam_Small2 <- bam(ANGLE ~ s(PLATE_X, PLATE_Z),</pre>
                 data = trainDF, family = gaussian, method = "GCV.Cp")
gamSmallFit2 <- data.frame(PLATE_X = as.vector(xs), PLATE_Z = as.vector(ys))</pre>
anglePred <- predict(gam_Small2, gamSmallFit2, types = "response")</pre>
anglePred <- matrix(anglePred, nrow = 50, ncol = 50)</pre>
summary(trainDF$ANGLE)
                           Mean 3rd Qu.
  Min. 1st Qu. Median
                                            Max.
-58.917 -4.377 13.619 13.177 29.796 82.393
filled.contour(x=seq(from=-2, to=2, length=50), y=seq(from=0, to=5, length=50), z = anglePred,
               zlim=c(-15,35),
               color.palette = colorRampPalette(c("lightblue","yellow","orange", "red", "darkred")),
               plot.axes = { rect(-0.71, 1.52, 0.71, 3.67, border="black", lty="dashed", lwd=3)
                 axis(1, at=c(-2,-1,0,1,2), pos=0, labels=c(-2,-1,0,1,2), las=0, col="black")
                 axis(2, at=c(0,1,2,3,4,5), pos=-2, labels=c(0,1,2,3,4,5), las=0, col="black")
               },
               main = "Heat Map for Launch Angle Based on \n X/Y Location of Strikezone",
```

```
ylab = "Vertical (ft)",
xlab = "Horizontal Location of Pitch at Plate (ft)")
```

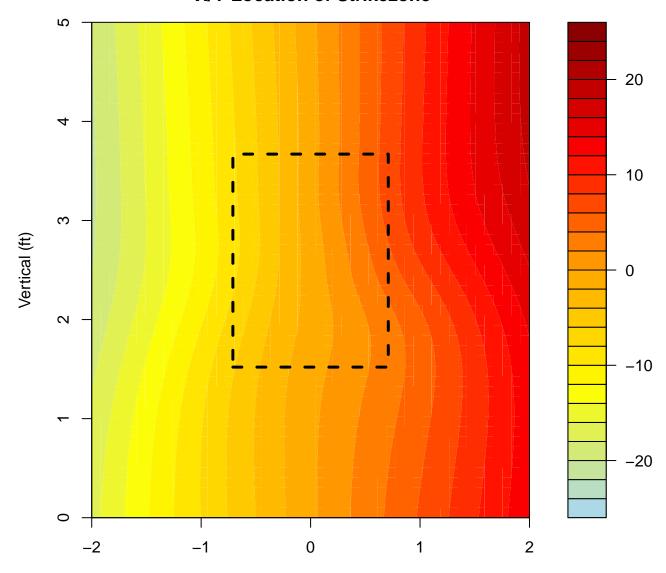
Heat Map for Launch Angle Based on X/Y Location of Strikezone



Horizontal Location of Pitch at Plate (ft)

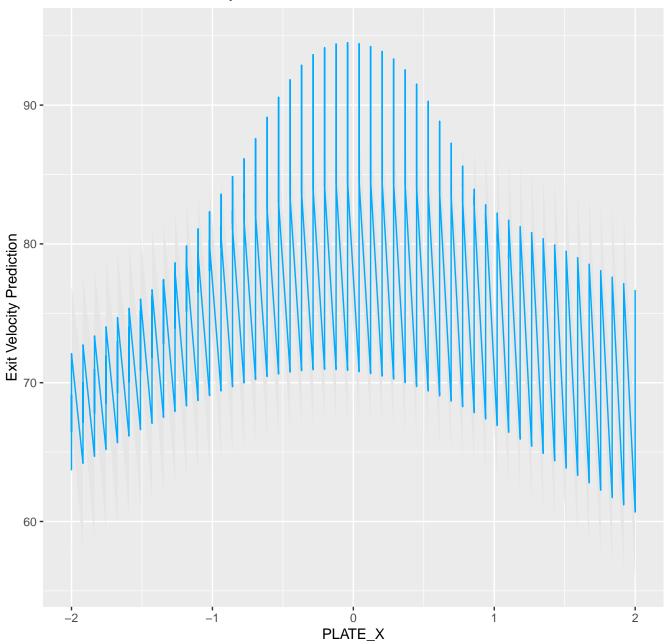
```
plot.axes = { rect(-0.71, 1.52, 0.71, 3.67, border="black", lty="dashed", lwd=3)
   axis(1, at=c(-2,-1,0,1,2), pos=0, labels=c(-2,-1,0,1,2), las=0, col="black")
   axis(2, at=c(0,1,2,3,4,5), pos=-2, labels=c(0,1,2,3,4,5), las=0, col="black")
},
main = "Heat Map for Direction Based on \n X/Y Location of Strikezone",
ylab = "Vertical (ft)",
xlab = "Horizontal Location of Pitch at Plate (ft)")
```

Heat Map for Direction Based on X/Y Location of Strikezone



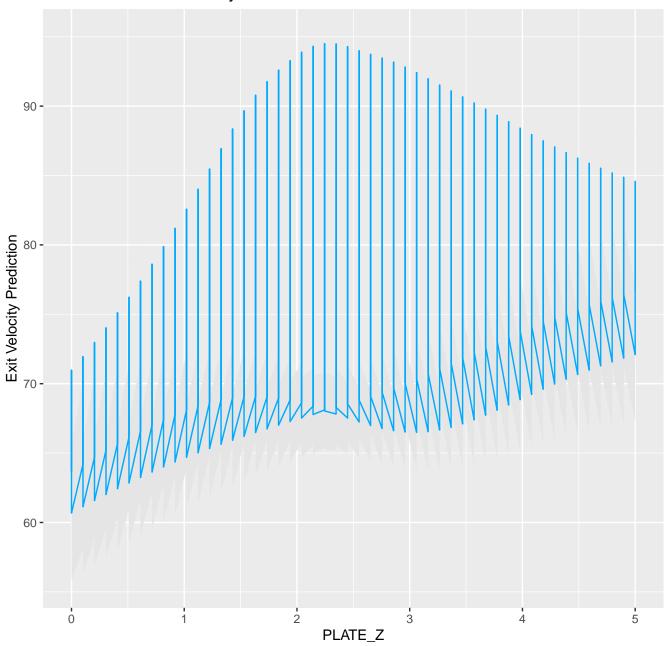
Horizontal Location of Pitch at Plate (ft)

Prediction of Exit Velocity Based on Horizontal Location of Pitch



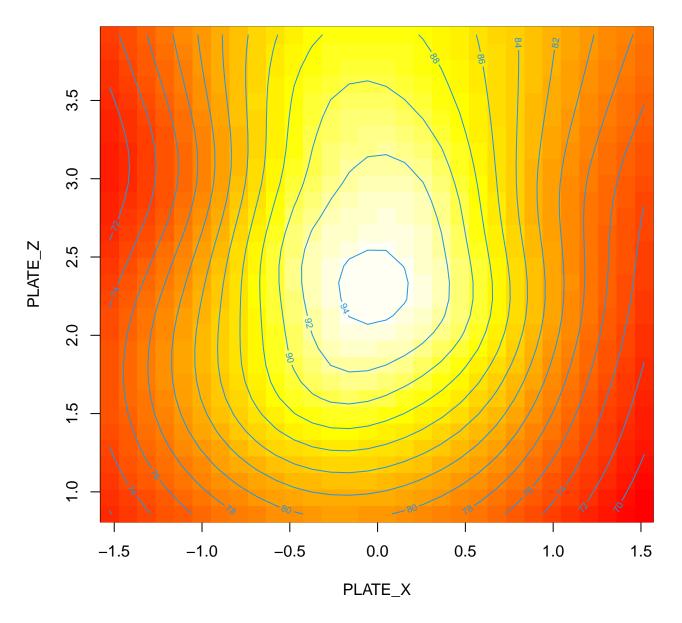
```
ggplot(aes(x=PLATE_Z,y=exitVeloPredConf$fit), data=predVals) +
  geom_ribbon(aes(ymin = lower, ymax=upper), fill='gray90') +
  geom_line(color='#00aaff') + ylab("Exit Velocity Prediction") +
  ggtitle("Prediction of Exit Velocity Based on Vertical Location of Pitch")
```

Prediction of Exit Velocity Based on Vertical Location of Pitch



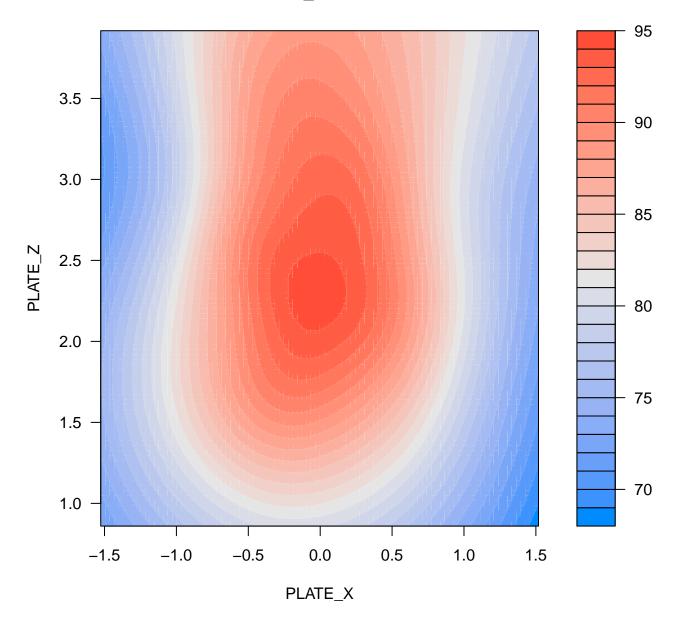
#both plots show where the highest exit velo is based on x and y location of pitch
vis.gam(gam_Small, type='response', plot.type='contour', main = "Exit Velo")

Exit Velo



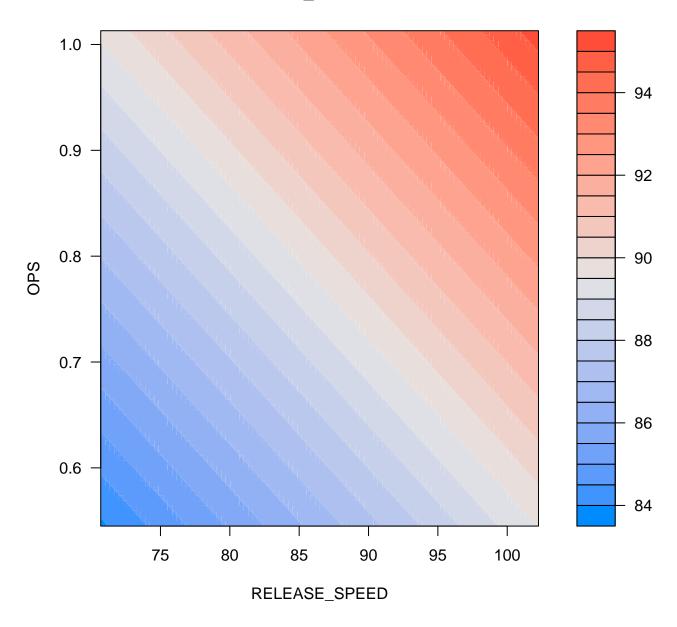
visreg2d(gam_Small, xvar='PLATE_X', yvar='PLATE_Z', scale='response')

EXIT_SPEED



visreg2d(gam_EV_Upd, xvar='RELEASE_SPEED', yvar='OPS', scale='response')

EXIT_SPEED



```
anova(gam_EV_Upd, gam_Small, test="Chisq")
Analysis of Deviance Table
```

anova(gam_EV_Upd)

Family: gaussian

Link function: identity

Formula:

```
EXIT_SPEED ~ RELEASE_SPEED + INDUCED_VERTICAL_BREAK + HORIZONTAL_BREAK +
    HORIZONTAL_APPROACH_ANGLE + OPS + Handedness
Parametric Terms:
                         df
                                    F p-value
RELEASE SPEED
                          1 74.264 < 2e-16
INDUCED_VERTICAL_BREAK 1 3.892 0.0485
HORIZONTAL_BREAK 1 6.122 0.0134
HORIZONTAL APPROACH ANGLE 1 2.810 0.0937
OPS
                         1 152.669 < 2e-16
Handedness
                           1 17.063 3.63e-05
anova(gam_Ang_Upd)
Family: gaussian
Link function: identity
Formula:
ANGLE ~ RELEASE_SPEED + PLATE_X + PLATE_Z + INDUCED_VERTICAL_BREAK +
    HORIZONTAL_BREAK + VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE +
    OPS + Handedness
Parametric Terms:
                         df
                                    F p-value
RELEASE_SPEED
                         1 522.915 < 2e-16
                          1 13.701 0.000215
PLATE_X
PLATE_Z 1 378.906 < 2e-16
INDUCED_VERTICAL_BREAK 1 507.219 < 2e-16
HORIZONTAL_BREAK 1 13.454 0.000245
VERTICAL_APPROACH_ANGLE 1 3.563 0.059084
HORIZONTAL_APPROACH_ANGLE 1 64.218 1.16e-15
OPS
                          1 16.473 4.95e-05
Handedness
                          1 12.370 0.000437
anova(gam_Dir_Upd)
Family: gaussian
Link function: identity
Formula:
DIRECTION ~ RELEASE_SPEED + PLATE_X + INDUCED_VERTICAL_BREAK +
    HORIZONTAL_BREAK + VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE +
    OPS + Handedness
Parametric Terms:
                          df
                                    F p-value
RELEASE_SPEED
                          1 13.982 0.000185
PLATE X
                          1 1216.430 < 2e-16
INDUCED_VERTICAL_BREAK 1 7.122 0.007618
HORIZONTAL_BREAK 1 286.490 < 2e-16
VERTICAL_APPROACH_ANGLE 1 8.440 0.003674
HORIZONTAL_APPROACH_ANGLE 1 70.704 < 2e-16
```

GLM model

OPS

Handedness

```
###########exit velo
exitVeloCalc <- glm(EXIT_SPEED ~ RELEASE_SPEED + PLATE_X + PLATE_Z + INDUCED_VERTICAL_BREAK +
```

1 35.056 3.25e-09

1 915.549 < 2e-16

```
HORIZONTAL_BREAK +
                   VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE + OPS + Handedness,
               data = trainDF,
               family = gaussian)
summary(exitVeloCalc)
Call:
glm(formula = EXIT_SPEED ~ RELEASE_SPEED + PLATE_X + PLATE_Z +
   INDUCED_VERTICAL_BREAK + HORIZONTAL_BREAK + VERTICAL_APPROACH_ANGLE +
   HORIZONTAL_APPROACH_ANGLE + OPS + Handedness, family = gaussian,
   data = trainDF)
Deviance Residuals:
   Min 1Q Median 3Q Max
-40.874 -7.901 2.099 9.573 31.016
Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
(Intercept)
                     62.49285 3.30876 18.887 < 2e-16 ***
RELEASE_SPEED
                     0.07433 0.17082 0.435 0.6635
PLATE_X
                     0.06586 0.21768 0.303 0.7622
PLATE_Z
-0.02235 0.00887 -2.520 0.0118 *
HORIZONTAL_BREAK
VERTICAL_APPROACH_ANGLE -0.06991 0.15320 -0.456 0.6482
HORIZONTAL_APPROACH_ANGLE -0.08299 0.04914 -1.689 0.0912 .
OPS
                     12.22985 0.99085 12.343 < 2e-16 ***
                       Handedness
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for gaussian family taken to be 154.2758)
   Null deviance: 3843946 on 24509 degrees of freedom
Residual deviance: 3779758 on 24500 degrees of freedom
AIC: 193068
Number of Fisher Scoring iterations: 2
exitVeloCalc$coefficients #coefficients used to determine exit velo
            (Intercept)
                                RELEASE SPEED
                                                            PLATE X
                                                 0.07433175
HORIZONTAL_BREAK
            62.49285293
                                   0.18433823
               PLATE_Z INDUCED_VERTICAL_BREAK
                                                     -0.02234830
             0.06586319
                                   0.03296162
 VERTICAL_APPROACH_ANGLE HORIZONTAL_APPROACH_ANGLE
                                                                OPS
            -0.06991142
                                 -0.08298921
                                                       12.22984853
            Handedness
             0.66969731
anova(exitVeloCalc, test = "Chisq")
Analysis of Deviance Table
Model: gaussian, link: identity
Response: EXIT_SPEED
```

Terms added sequentially (first to last)

```
Df Deviance Resid. Df Resid. Dev Pr(>Chi)
NULL
                                           24509 3843946
                                            24508 3808449 < 2.2e-16 ***
RELEASE SPEED
                                 35498
                            1
                                  106 24507 3808343 0.407391
PLATE_X
PLATE Z
                           1
                                   0 24506 3808342 0.964155
INDUCED_VERTICAL_BREAK 1
HORIZONTAL_BREAK 1
                                1266 24505 3807077 0.004179 **

      HORIZONTAL_BREAK
      1
      792
      24504
      3806285
      0.023460 *

      VERTICAL_APPROACH_ANGLE
      1
      29
      24503
      3806256
      0.665747

      HORIZONTAL_APPROACH_ANGLE
      1
      1088
      24502
      3805167
      0.007905 **

                            1
                                          24501 3782366 < 2.2e-16 ***
                                 22801
OPS
Handedness
                                 2608
                                            24500 3779758 3.927e-05 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
########angle
angleCalc <- glm(ANGLE ~ RELEASE_SPEED + PLATE_X + PLATE_Z + INDUCED_VERTICAL_BREAK + HORIZONTAL_BREAK +
                       VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE + OPS + Handedness,
                     data = trainDF,
                     family = gaussian)
anova(angleCalc, test = "Chisq")
Analysis of Deviance Table
Model: gaussian, link: identity
Response: ANGLE
Terms added sequentially (first to last)
                           Df Deviance Resid. Df Resid. Dev Pr(>Chi)
                                           24509 15217969
NULL
RELEASE_SPEED
                          1
                               13523
                                           24508 15204446 1.121e-06 ***
PLATE_X
                          1
                                 368 24507 15204078 0.4220621
                           1 686790 24506 14517288 < 2.2e-16 ***
PLATE Z
INDUCED_VERTICAL_BREAK 1 484625 24505 14032663 < 2.2e-16 ***
                           1 7192 24504 14025471 0.0003839 ***
HORIZONTAL_BREAK
VERTICAL_APPROACH_ANGLE 1
                                 3371 24503 14022100 0.0150540 *
HORIZONTAL_APPROACH_ANGLE 1
                                            24502 13990464 9.525e-14 ***
                                 31636
                                            24501 13981824 9.941e-05 ***
OPS
                            1
                                 8640
                                  7056
                            1
                                            24500 13974768 0.0004363 ***
Handedness
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
########direction
directionCalc <- glm(DIRECTION ~ RELEASE_SPEED + PLATE_X + PLATE_Z + INDUCED_VERTICAL_BREAK +
                        HORIZONTAL_BREAK +
                       VERTICAL_APPROACH_ANGLE + HORIZONTAL_APPROACH_ANGLE + OPS + Handedness,
                     data = trainDF,
                     family = gaussian)
anova(directionCalc, test = "Chisq")
Analysis of Deviance Table
Model: gaussian, link: identity
Response: DIRECTION
```

Terms added sequentially (first to last)

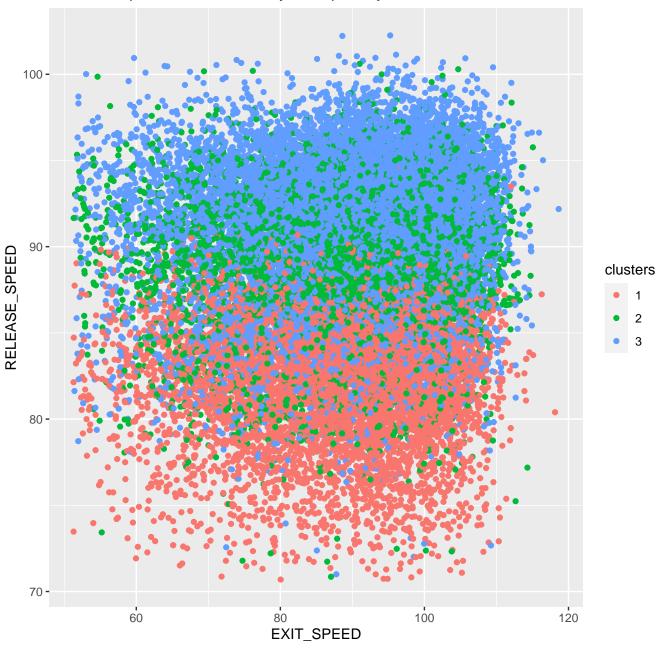
```
Df Deviance Resid. Df Resid. Dev Pr(>Chi)
NULL
                                          24509
                                                 11362518
                                          24508 11325490 < 2.2e-16 ***
RELEASE SPEED
                                37027
PLATE X
                               559080
                                          24507 10766410 < 2.2e-16 ***
                           1
                                          24506 10766003 0.323712
PLATE Z
                           1
                                  407
INDUCED_VERTICAL_BREAK
                                  378
                                          24505 10765625 0.341485
                           1
                                                 10657396 < 2.2e-16 ***
HORIZONTAL BREAK
                           1
                              108229
                                          24504
VERTICAL APPROACH ANGLE
                                          24503 10653734 0.003085 **
                           1
                                3662
HORIZONTAL_APPROACH_ANGLE 1
                                4473
                                          24502 10649261 0.001073 **
OPS
                                          24501
                                                  10626369 1.375e-13 ***
                           1
                                22892
Handedness
                               380929
                                          24500 10245440 < 2.2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
evc <- exitVeloCalc$coefficients</pre>
ac <- angleCalc$coefficients</pre>
dc <- directionCalc$coefficients</pre>
#adding new glm predicted columns to training df
trainDF <- trainDF %>%
  mutate(exitVelo_GLM = round(evc[1] + evc[2]*RELEASE_SPEED + evc[3]*PLATE_X + evc[4]*PLATE_Z +
                                evc[5]*INDUCED_VERTICAL_BREAK + evc[6]*HORIZONTAL_BREAK +
                                evc[7]*VERTICAL APPROACH ANGLE +
                                evc[8]*HORIZONTAL_APPROACH_ANGLE + evc[9]*OPS + evc[10]*Handedness, 3))
trainDF <- trainDF %>%
  mutate(angle GLM = round(ac[1] + ac[2]*RELEASE SPEED + ac[3]*PLATE X + ac[4]*PLATE Z +
                             ac[5]*INDUCED VERTICAL BREAK + ac[6]*HORIZONTAL BREAK +
                             ac[7] *VERTICAL APPROACH ANGLE +
                             ac[8]*HORIZONTAL_APPROACH_ANGLE + ac[9]*OPS + ac[10]*Handedness, 3))
trainDF <- trainDF %>%
  mutate(direction_GLM = round(dc[1] + dc[2]*RELEASE_SPEED + dc[3]*PLATE_X + dc[4]*PLATE_Z +
                                 dc[5]*INDUCED_VERTICAL_BREAK + dc[6]*HORIZONTAL_BREAK +
                                 dc[7]*VERTICAL_APPROACH_ANGLE +
                                 dc[8]*HORIZONTAL_APPROACH_ANGLE + dc[9]*OPS + dc[10]*Handedness, 3))
```

KMeans

```
subsetTrain <- trainDF[,c(19, 12:18, 29:30)]
km1 <- kmeans(subsetTrain[,2:10], 3, iter.max = 100)

clusters <- factor(km1$cluster)
ggplot(trainDF, aes(x = EXIT_SPEED, y = RELEASE_SPEED, color = clusters)) + geom_point() +
    ggtitle("Release Speed vs Exit Velocity Grouped By Clusters")</pre>
```

Release Speed vs Exit Velocity Grouped By Clusters



KMeans Plot By Clusters Based on Var Similarity



```
cords <- as.data.frame(get_pca_ind(pca)$coord)</pre>
cords$cluster1 <- factor(km2$cluster)</pre>
cords$EXIT_SPEED <- trainDF$EXIT_SPEED</pre>
head(cords) #see first few rows dimensions and clusters
        Dim.1
                      Dim.2
                                                Dim.4
                                                                         Dim.6
                                   Dim.3
                                                             Dim.5
1 \ -0.2670835 \ -0.612154122 \ -1.5278253 \ -3.0041345 \ -1.5721867 \ -0.6846484
2 -1.6181788 -0.685284226 -1.1083727 -1.5976944 -0.0713787 0.5994411
3 - 0.7583726 \quad 0.615782416 \quad 1.7885790 \quad -0.4184670 \quad 1.1029973 \quad 0.9452969
   2.1475458 \quad 2.563730676 \quad -0.3782569 \quad 0.8190211 \quad -0.5348873 \quad 0.1488507
  -1.8329566 0.005665152 -1.9021775 0.1834935 1.6097560 -0.2961044
   0.4233652 \quad 0.720917324 \quad 1.3316927 \quad -0.4232247 \quad -0.5920003 \quad -0.2493779
        Dim.7
                     Dim.8
                                    Dim.9 cluster1 EXIT_SPEED
   0.3249521 0.01195926 0.181060498
                                                   3
                                                        83.65304
  0.3777947 -0.26351196 -0.054952233
                                                        95.66794
```

pca <- prcomp(trainDF[, c(12:18, 29:30)], scale = TRUE)</pre>

Dimension reduction PCA

```
      3
      0.9258171
      0.37129333
      -0.166779325
      3
      86.94758

      4
      1.2165254
      0.42395082
      -0.032647612
      1
      76.26321

      5
      -0.2560795
      0.26898614
      0.009755342
      3
      87.25558

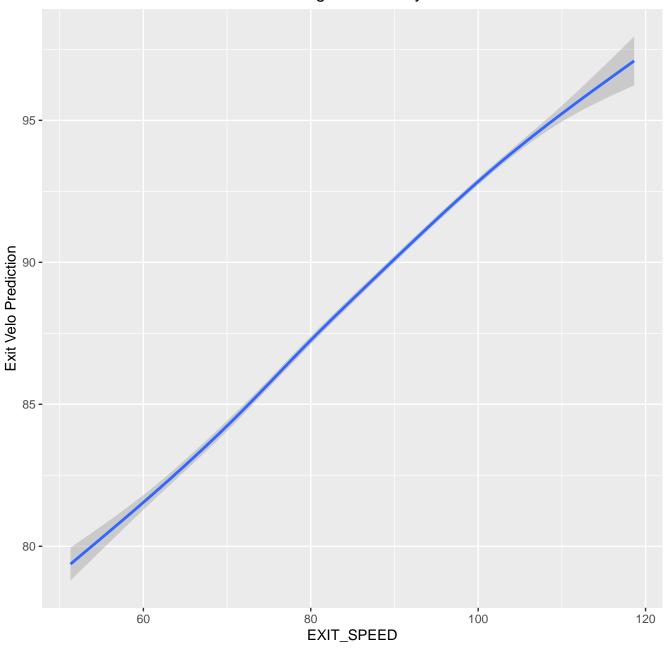
      6
      1.1292003
      -1.62054318
      0.077016925
      1
      82.83160
```

KNN

```
#######knn on exit velo
trainKNN_x_EV <- trainDF[,c(12:18,29:30)]
trainKNN_y_EV <- trainDF[,19]
knnModel_EV <- knnreg(trainKNN_x_EV, trainKNN_y_EV)
testKNN_x_EV <- testDF[,c(12:20)]

#testdf pred vals
knnpred_y_EV <- predict(knnModel_EV, data.frame(testKNN_x_EV))
knnpred_xTconf_EV <- predict(knnModel_EV, data.frame(trainKNN_x_EV), interval = "confidence", level = 0.9)
ggplot(trainDF, aes(EXIT_SPEED, knnpred_xTconf_EV)) + geom_smooth() +
    ggtitle("Error Band on KNN Model Predicting Exit Velocity") + ylab("Exit Velo Prediction")</pre>
```

Error Band on KNN Model Predicting Exit Velocity



```
mse <- mean((trainKNN_y_EV - knnpred_xTconf_EV)^2)
mae <- MAE(trainKNN_y_EV, knnpred_xTconf_EV)
rmse <- RMSE(trainKNN_y_EV, knnpred_xTconf_EV)
mse</pre>
```

[1] 109.4011

mae

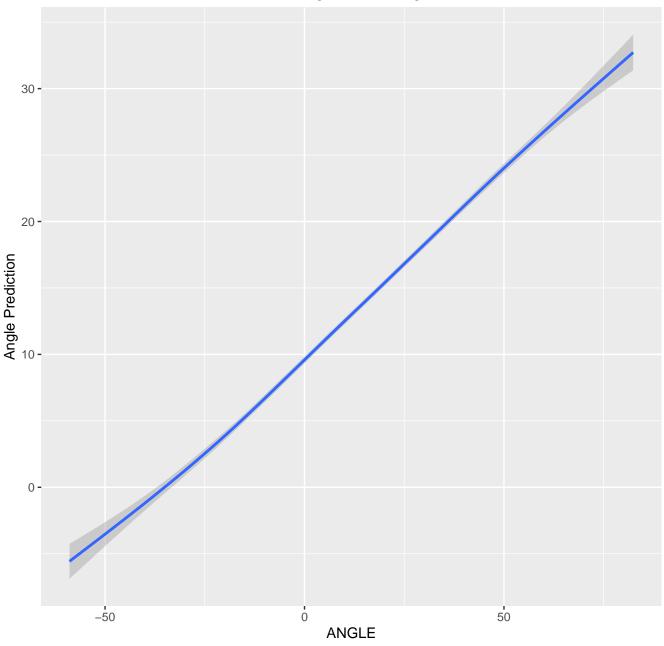
[1] 8.328806

rmse

[1] 10.4595

```
#####knn on angle
trainKNN_x_ang <- trainDF[,c(12:18,29:30)]
trainKNN_y_ang <- trainDF[,20]
knnModel_ang <- knnreg(trainKNN_x_ang, trainKNN_y_ang)
testKNN_x_ang <- testDF[,c(12:20)]
knnpred_y_ang <- predict(knnModel_ang, data.frame(testKNN_x_ang))
knnpred_xTconf_ang <- predict(knnModel_ang, data.frame(trainKNN_x_ang), interval = "confidence", level = 0.9)
ggplot(trainDF, aes(ANGLE, knnpred_xTconf_ang)) + geom_smooth() +
    ggtitle("Error Band on KNN Model Predicting Launch Angle") + ylab("Angle Prediction")</pre>
```

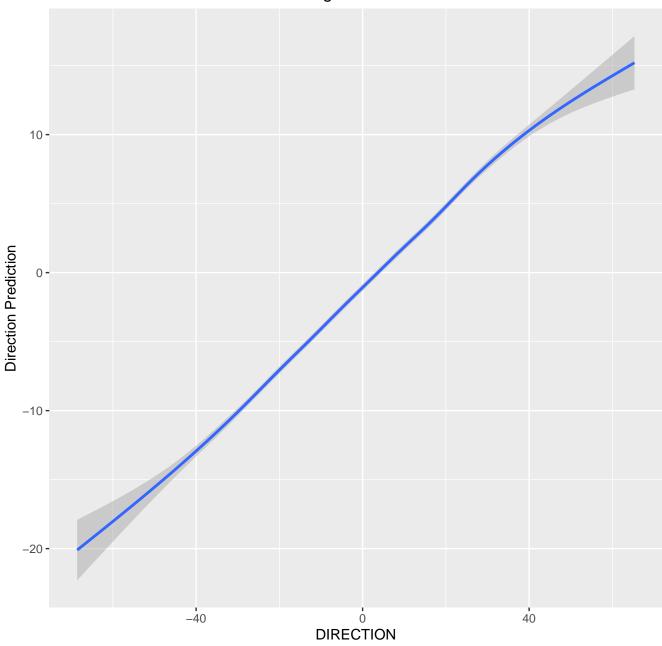
Error Band on KNN Model Predicting Launch Angle



```
####knn on direction
trainKNN_x_dir <- trainDF[,c(12:18,29:30)]
trainKNN_y_dir <- trainDF[,21]
knnModel_dir <- knnreg(trainKNN_x_dir, trainKNN_y_dir)
testKNN_x_dir <- testDF[,c(12:20)]</pre>
```

```
knnpred_y_dir <- predict(knnModel_dir, data.frame(testKNN_x_dir))
knnpred_xTconf_dir <- predict(knnModel_dir, data.frame(trainKNN_x_dir), interval = "confidence", level = 0.9)
ggplot(trainDF, aes(DIRECTION, knnpred_xTconf_dir)) + geom_smooth() +
    ggtitle("Error Band on KNN Model Predicting Direction") + ylab("Direction Prediction")</pre>
```

Error Band on KNN Model Predicting Direction



```
#add pred vals to training df
trainDF <- trainDF %>% mutate(exitVelo_KNN = round(knnpred_xTconf_EV,3))
trainDF <- trainDF %>% mutate(angle_KNN = round(knnpred_xTconf_ang,3))
trainDF <- trainDF %>% mutate(direction_KNN = round(knnpred_xTconf_dir,3))
```

Finding Absolute Errors on Training DF Models

```
[1] 4.016803
mean(abs(trainDF$EXIT_SPEED - trainDF$exitVelo_SVM))
[1] 1.266979
mean(abs(trainDF$EXIT_SPEED - trainDF$exitVelo_GAM))
[1] 10.11333
mean(abs(trainDF$EXIT_SPEED - trainDF$exitVelo_GLM))
[1] 10.11355
mean(abs(trainDF$EXIT_SPEED - trainDF$exitVelo_KNN))
[1] 8.328807
mean(abs(trainDF$ANGLE - trainDF$angle_RF))
[1] 8.196231
mean(abs(trainDF$ANGLE - trainDF$angle_SVM))
[1] 2.589948
mean(abs(trainDF$ANGLE - trainDF$angle_GAM))
[1] 19.04803
mean(abs(trainDF$ANGLE - trainDF$angle_GLM))
[1] 19.04803
mean(abs(trainDF$ANGLE - trainDF$angle_KNN))
[1] 16.74011
mean(abs(trainDF$DIRECTION - trainDF$direction_RF))
[1] 7.18387
mean(abs(trainDF$DIRECTION - trainDF$direction_SVM))
[1] 2.210109
mean(abs(trainDF$DIRECTION - trainDF$direction_GAM))
[1] 16.75261
mean(abs(trainDF$DIRECTION - trainDF$direction_GLM))
[1] 16.75257
mean(abs(trainDF$DIRECTION - trainDF$direction_KNN))
[1] 14.50776
######################
```

It can be seen that SVM has the smallest mean error rate

Testing Data

```
###########Testing Data
####gam
#adding gam predicted values to test df
testDF <- testDF %>%
  mutate(exitVelo_GAM = round(gamEV[1] + gamEV[2]*RELEASE_SPEED + gamEV[3]*INDUCED_VERTICAL_BREAK +
                                gamEV[4]*HORIZONTAL_BREAK + gamEV[5]*HORIZONTAL_APPROACH_ANGLE +
                                gamEV[6]*OPS + gamEV[7]*Handedness, 3))
testDF <- testDF %>%
  mutate(angle_GAM = round(gamAng[1] + gamAng[2]*RELEASE_SPEED + gamAng[3]*PLATE_X +
                             gamAng[4]*PLATE Z + gamAng[5]*INDUCED VERTICAL BREAK +
                             gamAng[6]*HORIZONTAL_BREAK + gamAng[7]*VERTICAL_APPROACH_ANGLE +
                             gamAng[8]*HORIZONTAL_APPROACH_ANGLE +
                             gamAng[9]*OPS + gamAng[10]*Handedness, 3))
testDF <- testDF %>%
  mutate(direction_GAM = round(gamDir[1] + gamDir[2]*RELEASE_SPEED + gamDir[3]*PLATE_X +
                                 gamDir[4]*INDUCED_VERTICAL_BREAK + gamDir[5]*HORIZONTAL_BREAK +
                                 gamDir[6]*VERTICAL_APPROACH_ANGLE +
                                 gamDir[7]*HORIZONTAL_APPROACH_ANGLE +
                                 gamDir[8]*OPS + gamDir[9]*Handedness, 3))
####glm
#adding glm predicted values to test df
testDF <- testDF %>%
  mutate(exitVelo_GLM = round(evc[1] + evc[2]*RELEASE_SPEED + evc[3]*PLATE_X + evc[4]*PLATE_Z +
                                evc[5]*INDUCED_VERTICAL_BREAK + evc[6]*HORIZONTAL_BREAK +
                                evc[7]*VERTICAL APPROACH ANGLE +
                                evc[8]*HORIZONTAL_APPROACH_ANGLE + evc[9]*OPS +
                                evc[10]*Handedness, 3))
testDF <- testDF %>%
  mutate(angle_GLM = round(ac[1] + ac[2]*RELEASE_SPEED + ac[3]*PLATE_X + ac[4]*PLATE_Z +
                             ac[5]*INDUCED_VERTICAL_BREAK + ac[6]*HORIZONTAL_BREAK +
                             ac[7]*VERTICAL_APPROACH_ANGLE +
                             ac[8]*HORIZONTAL_APPROACH_ANGLE + ac[9]*OPS +
                             ac[10]*Handedness, 3))
testDF <- testDF %>%
  mutate(direction_GLM = round(dc[1] + dc[2]*RELEASE_SPEED + dc[3]*PLATE_X + dc[4]*PLATE_Z +
                                 dc[5]*INDUCED_VERTICAL_BREAK + dc[6]*HORIZONTAL_BREAK +
                                 dc[7]*VERTICAL_APPROACH_ANGLE +
                                 dc[8]*HORIZONTAL_APPROACH_ANGLE + dc[9]*OPS +
                                 dc[10]*Handedness, 3))
###knn
#adding knn predicted values to test df
testDF <- testDF %>% mutate(exitVelo_KNN = round(knnpred_y_EV,3))
testDF <- testDF %>% mutate(angle_KNN = round(knnpred_y_ang,3))
testDF <- testDF %>% mutate(direction_KNN = round(knnpred_y_dir,3))
#View first few rows of my altered df's to see my predicted values for each model
head(trainDF)
  BATTER UID
                AVG
                       OBP
                              SLG VENUE KEY OUTS BALLS STRIKES BATS LEFT
                                       2852 1
                                                    2
1
          29 0.2320 0.2860 0.2950
                                                            1
                                                                       1
         87 0.2160 0.2820 0.3610
                                       4271 1
                                                     2
                                                                       1
```

```
3
          20 0.2695 0.3390 0.3835
                                       2528
                                                              2
                                                                        0
                                                      3
4
                                                              2
                                       4670
                                                                        0
         147 0.2895 0.3655 0.4510
                                                      1
5
          99 0.2660 0.3285 0.3560
                                       2852
                                               2
                                                      2
                                                              2
                                                                        0
                                                2
6
         110 0.2570 0.3365 0.4250
                                       2852
                                                      1
                                                                        0
  THROWS_LEFT PITCH_NUMBER RELEASE_SPEED
                                            PLATE X PLATE Z
1
                                95.11150 0.7963360 1.35507
2
                                92.76369 0.4548490 2.59344
            0
                         3
3
            0
                         6
                                88.76340 -0.3001910 3.06310
4
                         4
                              81.78240 -0.1708880 1.84865
            1
5
                         5
                                92.06150 -0.1243550 3.24001
6
                         4
                                81.60239 0.0411996 1.97743
  INDUCED_VERTICAL_BREAK HORIZONTAL_BREAK VERTICAL_APPROACH_ANGLE
1
                17.01530
                             -4.657780
                                                          -6.54525
2
                17.30840
                                -8.322809
                                                          -4.98211
3
                               -20.656200
                 2.46511
                                                          -5.81156
4
                -3.59941
                                -7.826159
                                                          -8.56734
5
                                10.426299
                15.57420
                                                          -4.67467
6
                14.52030
                               -18.717300
                                                          -7.20663
  HORIZONTAL_APPROACH_ANGLE EXIT_SPEED
                                            ANGLE DIRECTION
                   1.646740 83.65304 -14.851092 13.405146
1
2
                   1.529110
                              95.66794
                                        3.929680 21.932704
3
                   0.266562 86.94758 22.556687 15.621360
4
                  -2.952540 76.26321 -13.785541 -46.406194
5
                  -1.051080
                            87.25558
                                        1.316303 14.561501
6
                   0.059810
                              82.83160 59.353564
                                                     1.017197
           EVENT_RESULT_KEY PITCH_RESULT_KEY PA X1B X2B X3B HR
1
                                      InPlay 1
                                                           0 0 0.5810
                  field_out
2
                     single
                                      InPlay 1
                                                   1
                                                       0
                                                           0 0 0.6430
                  field_out
                                      InPlay 1
                                                  0
                                                           0 0 0.7225
  grounded_into_double_play
                                      InPlay 1
                                                  0
                                                       0
                                                             0 0.8165
                                                           0
                                      InPlay 1
5
                     single
                                                   1
                                                       0
                                                           0
                                                             0 0.6845
6
                                      InPlay 1
                                                  0
                                                       0
                                                           0
                                                             0 0.7615
                  field_out
  Handedness exitVelo_RF angle_RF direction_RF exitVelo_SVM angle_SVM
1
                  83.272
                          -6.309
                                        14.217
                                                     84.905
                                                               -12.358
2
           1
                  93.311
                            8.092
                                        15.756
                                                     94.418
                                                                 6.427
3
           0
                  88.044
                                                     88.198
                          18.882
                                        10.823
                                                                20.066
4
           1
                  80.806
                           -6.580
                                       -26.147
                                                     77.517
                                                              -16.287
5
           1
                  89.061
                           14.891
                                         8.066
                                                     88.505
                                                                 3.813
6
           0
                  85.159
                           44.449
                                         3.064
                                                     84.085
                                                                56.851
  direction_SVM exitVelo_GAM angle_GAM direction_GAM exitVelo_GLM angle_GLM
                      88.854
                                2.399
                                              13.656
                                                            88.935
                                                                      2.399
1
         15.552
2
         20.501
                      89.289
                                16.736
                                              10.981
                                                            89.309
                                                                      16.736
3
         17.778
                      88.816
                                                            88.798
                                11.520
                                              -2.975
                                                                      11.520
        -44.246
                      89.198
                                3.010
                                              -1.830
                                                            89.233
                                                                      3.010
5
         12.408
                      89.425
                                21.826
                                              -1.285
                                                            89.403
                                                                      21.826
6
         -1.138
                      88.336
                                19.072
                                                            88.377
                                              -3.264
                                                                      19.072
  direction_GLM exitVelo_KNN angle_KNN direction_KNN
1
         13.630
                      90.318
                                7.715
                                              12.695
2
         10.980
                      91.891
                                17.399
                                               4.056
3
         -2.960
                      93.822
                               17.837
                                              -7.282
4
                      72.780 -16.943
         -1.835
                                             -22.993
5
         -1.265
                      99.492
                                21.210
                                              -5.426
         -3.273
                      83.394
                                37.113
                                               9.861
head(testDF)
                       OBP
                              SLG VENUE KEY OUTS BALLS STRIKES BATS LEFT
  BATTER UID
                AVG
1
          81 0.2610 0.3285 0.3655
                                       2528
                                               2
                                                      1
                                                              2
                                                                        1
2
                                       2683
                                                1
                                                      1
                                                              1
                                                                        1
         125 0.2295 0.3255 0.4005
3
          21 0.2745 0.3365 0.4425
                                       2724
                                               2
                                                      2
                                                                        0
```

```
73 0.2890 0.3810 0.3740
4
                                         2772
                                                        0
                                                                           1
                                                  1
                                                                1
5
                                                        0
         142 0.3195 0.3605 0.4435
                                         5472
                                                  0
                                                                1
                                                                           1
6
          81 0.2610 0.3285 0.3655
                                         2843
                                                  1
                                                        0
                                                                 2
                                                                           0
  THROWS LEFT PITCH NUMBER RELEASE SPEED
                                              PLATE X PLATE Z
                          6
                                 89.33580 -0.3844000 2.530500
1
2
                          3
                                 87.97424 0.5956410 2.485661
                          3
3
            0
                                  90.37970 -0.0741844 2.732740
4
            1
                          2
                                  80.51560
                                            0.3506650 1.272440
                          2
5
            0
                                 84.06917
                                            1.0804490 1.934018
                          3
                                 90.85476 0.7055900 3.354112
6
  INDUCED_VERTICAL_BREAK HORIZONTAL_BREAK VERTICAL_APPROACH_ANGLE
1
              16.4084988
                                  -4.477510
                                                           -4.957750
2
               0.6219336
                                  -1.303324
                                                           -7.055572
3
              15.1757994
                                  -1.611590
                                                           -5.580090
4
              11.2826996
                                  13.452300
                                                           -7.813180
5
                                  11.446440
                                                           -8.635422
              -3.2285538
                                   8.335738
6
              17.5839863
                                                           -4.328052
 HORIZONTAL_APPROACH_ANGLE
                               OPS Handedness exitVelo_GAM angle_GAM
1
                    2.421590 0.694
                                             1
                                                      89.129
                                                                 21.616
2
                                             1
                                                      88.768
                    2.367589 0.726
                                                                  8.380
3
                    2.571330 0.779
                                             0
                                                      89.578
                                                                20.276
4
                                             0
                   -0.765851 0.755
                                                      87.357
                                                                12.597
5
                    3.918451 0.804
                                             1
                                                      88.532
                                                                  6.244
6
                   -1.838810 0.694
                                             1
                                                      89.488
                                                                24.187
 direction_GAM exitVelo_GLM angle_GLM direction_GLM exitVelo_KNN angle_KNN
          1.513
                       89.043
                                  21.616
                                                  1.494
                                                               92.040
1
                                                                         17.602
2
          9.906
                       88.813
                                   8.380
                                                              85.722
                                                 9.921
                                                                         10.084
3
         -5.041
                       89.568
                                  20.276
                                                -5.028
                                                             102.093
                                                                          8.851
4
         -8.883
                       87.359
                                  12.597
                                                 -8.934
                                                              88.236
                                                                         17.053
5
         10.737
                                  6.244
                                                 10.750
                                                               89.092
                                                                         16.577
                       88.617
6
          6.594
                       89.520
                                  24.187
                                                  6.612
                                                               95.074
                                                                         26.324
  direction_KNN
         16.051
1
2
         -2.762
3
          3.839
4
         -5.117
5
         -0.403
         -0.504
#writing to working directory to display final result tables
# write.csv(trainDF, "myTrainDF.csv")
# write.csv(testDF, "myTestDF.csv")
```

Another approach I though of to run a simulation (but did not get to because of time limit) is this:

Find the distribution of each of the 3 vars based on pitch type (say there are 4 pitch types) from k means and using the batting/pitch info, repeatedly generate outcome result (from model in assessment 2) for each var based on each pitch type and then randomly grab a exit velo, LA, and direction and pull the assigned outcome (out, 1b, 2b, 3b, hr) then randomly runs 1000 times, take the avg, and assign that average to be the exit velo, LA, and direction, respectively, on test data