

M2 Cheat Sheet

1 Centres of mass

1.1 How to find the centre of mass of a system of particles of given position and mass

Mass				
Distance				

$$\bar{x} = \frac{\sum m_i x_i}{\sum m_i}$$

$$\bar{y} = \frac{\sum m_i y_i}{\sum m_i}$$

1.2 How to locate centre of mass by appeal to symmetry

In some cases, centre of mass may be balanced around a point due to symmetry, this will make calculations easier.

1.3 How to find the centre of mass of a composite body

In a body with many different shapes, put the masses into the table and the associated distances and treat as normal. If all the composite shapes are the same, don't bother to find the true mass, set the mass of each shape to 1 and carry on.

1.4 How to use the position of the centre of mass in problems involving the equilibrium of a rigid body

When asked to the angle the vertical makes with a side when suspended about a point, draw the vertical from the point to the centre of mass, then use known distances to find the angle.

In a more complicated question when you are given an angle, use trig to find the ratio between the two sides that are not the hypotenuse, then solve simultaneously to find what is needed

2 Energy, work and power

2.1 How to calculate the work done by a force

$$WD = FS$$

2.2 How to calculate kinetic and gravitational potential energy

$$KE = \frac{1}{2}mv^2$$

$$GPE = mgh$$

2.3 The term mechanical energy and the work energy principle

The work energy principle - The work done by all forces on a particle equals the change in kinetic energy of the particle

Mechanical energy - The sum of the kinetic and potential energy of an object

2.4 How to apply the concept of power to the solution of problems

$$P = Fv$$

3 Equilibrium of a rigid body

$$\text{Moment} = \text{Force} \times \text{Distance}$$

4 Momentum, restitution and impulse

4.1 What momentum is and how to calculate it

$$\text{Momentum} = mv$$

Momentum is a vector quantity

Definition - The quantity of motion of a moving body

4.2 Conservation of momentum

In all collisions, momentum is conserved

$$m_1u_1 + m_2u_2 = m_1v_1 + m_2v_2$$

4.3 Coefficient of restitution

$$e = \frac{SoS}{SoA}$$

If $e=1$, the collision is perfectly elastic

If $e=0$, the collision is perfectly inelastic

4.4 Impulse

$$\text{Impulse} = Ft = m(v - u)$$

5 Projectiles

$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

$$s = \frac{u+v}{2}t$$

$$v^2 = u^2 + 2as$$

$$s = vt - \frac{1}{2}at^2$$

5.1 Forces on a projectile

Assume:

- Only force acting is gravity
- Projectile is a particle
- Projectile is not powered
- Air has no effect on the motion

There is no horizontal acceleration for the projectile

5.2 Equation for path of a projectile (don't need to know, but might be useful)

$$\ddot{x} = a = 0$$

$$\dot{x} = v = v \cos \alpha$$

$$x = vt \cos \alpha$$

$$t = \frac{x}{v \cos \alpha}$$

$$\ddot{y} = -g$$

$$\dot{y} = -gt + v \sin \alpha$$

$$y = -\frac{1}{2}gt^2 + vt \sin \alpha$$

$$y = -\frac{g}{2} \left(\frac{x}{v \cos \alpha} \right)^2 + v \left(\frac{x}{v \cos \alpha} \right) \sin \alpha$$

$$y = x^2 \left(\frac{-g}{2v^2 \cos^2 \alpha} \right) + x \left(\tan \alpha \right)$$