A Level Maths - D2 Sam Robbins 13SE

# Travelling Salesman Problem

#### 1 Definitions

The travelling salesman problem looks for a walk that gives the minimum tour.

Walk - A finite series of edges so that the end of one vertex is the start of the next

Tour - A walk that visits every vertex and returns to the starting vertex Add more information about upper and lower bounds here when you understand it more

## 2 The differences between classical and practical problems

Classical Problem - Must visit each vertex only once before returning to the start.

Practical Problem - Must visit each vertex at least once before returning to the start

### 3 Converting a network into a complete network of least distances

If a network is converted into a complete network of least distances, the classical and practical problem are the same.

To create a complete network of least distances, you must ensure the **triangle inequality** holds for all triangles in the network.

#### Triangle inequality:

The longest side of any triangle  $\leq$  The sum of the two shorter sides

In a network where the triangle inequality does not hold, replace the longest arc with the sum of the two shorter ones.