A Level Maths - S2 Sam Robbins 13SE

Continuous Distribution - Binomial - Exam Questions

1 Finding probabilities

Bhim and Joe play each other at badminton and for each game, independently of all others, the probability that Bhim loses is 0.2

Find the probability that, in 9 games:

1.1 P(X=?)

Exactly 3 of the games

1.1.1 Method 1 - Tables

Let X be the number of games lost

$$X \sim B(9, 0.2)$$

Write the question in terms of inequalities (so tables can be used)

$$P(X=3) = P(X \leqslant 3) - P(X \leqslant 2)$$

Look up the values on the tables

$$0.9144 - 0.7382 = 0.1762$$

1.1.2 Method 2 - Formula

Let X be the number of games lost

$$X \sim B(9, 0.2)$$

Write down the probability to be found:

$$P(X=3)$$

Use the formula on the data sheet:

$$\binom{n}{x}p^x(1-p)^{n-x}$$

Substitute values:

$$\binom{9}{3} \times (0.2)^3 \times (1 - 0.2)^{9-3} = 0.1762$$

1.2 P(X>?) or P(X<?)

Fewer than half the games Let X be the number of games lost

$$X \sim B(9, 0.2)$$

Write down the probability to be found

$$P(X \leq 4)$$

Look up the value on the tables

0.9804

If the inequality sign is the other way round subtract the probability from one.

If the value is not on the table, use an approximation