A Level Maths - S2 Sam Robbins 13SE

Hypothesis tests - Binomial - Exam Questions

A company claims that a quarter of the bolts sent to them are faulty. To test this claim the number of faulty bolts in a random sample of 50 is recorded.

1 Finding the critical region

Using a 5% significance level, find the critical region for a two-tailed test of the hypothesis that the probability of a bolt being faulty is $\frac{1}{4}$. The probability of rejection in either tail should be as close as possible to 0.025

Write down the distribution: $X \sim B(50, 0.25)$ For the lower value, look for the value closest to the probability of rejection

$$P(X \le 6) = 0.0194$$

To find the upper value look for the value closest to (1-probability of rejection). Then add one to this value as:

$$P(X \geqslant c) = 1 - P(X \leqslant c - 1)$$

$$P(X \le 18) = 0.9713$$

$$P(X \ge 19) = 0.0287$$

The critical values are 6 and 19

Find the actual significance

The actual significance is the true probability of rejection

$$0.0194 + 0.0287 = 0.0481$$

2 One tailed test

The machine making the bolts was reset and another sample of 50 bolts was taken. Only 5 were found to be faulty

Test at the 1% level of significance whether or not the probability of a faulty bolt has decreased. State your hypotheses clearly.

State the null and alternative hypothesis related to the $\frac{1}{4}$ probability mentioned earlier in the question

$$H_0: p = 0.25$$

$$H_1: p < 0.25$$

Write a probability based on the information given in the question

$$P(X \leq 5)$$

Look up the probability on the tables

$$P(X \leq 5) = 0.007$$

Compare this to the significance level

Write the conclusion

5 is in the critical region, reject H_0 , the test is significant, there is evidence that the probability of faulty bolts has decreased.

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3 Two tailed test

A teacher thinks that 20% of the pupils in a school read the Deano comic regularly.

 $He\ chooses\ 20\ pupils\ at\ random\ and\ finds\ 9\ of\ them\ read\ Deano.$