



Teacher-student knowledge distillation from BERT for sentence classifiers

Sam Sučík

MInf Project (Part 2) Report

Master of Informatics

School of Informatics

University of Edinburgh

2020

Abstract

TO-DO

Acknowledgements

I thank Steve Renals of University of Edinburgh and Vova Vlasov of Rasa for supervising me throughout the academic year; patiently listening to my never-ending reports and providing helpful and optimistic comments.

Many thanks also to Ralph Tang whose work inspired this project, and to Slávka Heželyová who constantly supported me and motivated me to explain all of my work in non-technical stories and metaphors.

Table of Contents

1	Introduction	7
1.1	Motivation	7
1.2	Aims	8
1.3	Contributions	8
2	Background [READY]	9
2.1	NLP before Transformers	9
2.2	Transformer-based NLP	12
2.2.1	Transformers	12
2.2.2	BERT	15
2.2.3	Newer and larger Transformer models	18
2.3	Teacher-student knowledge distillation	19
2.3.1	A brief introduction to knowledge distillation	19
2.3.2	Knowledge distillation in NLP	20
2.4	Understanding NLP models	21
3	Datasets [READY]	25
3.1	Downstream tasks	25
3.1.1	Corpus of Linguistic Acceptability	26
3.1.2	Stanford Sentiment Treebank	26
3.1.3	Sara	27
3.2	Data augmentation for larger transfer datasets	28
3.3	Probing tasks	29
4	Methods and Implementation	33
4.1	Methods and objectives	33
4.2	System overview and adapted implementations	34
4.3	Implementation details	35
4.4	Computing environment	37
5	Student tuning	39
5.1	Choosing η	40
5.2	Choosing learning rate annealing	40
5.3	Choosing batch size	40
5.4	Choosing embedding type and mode	41
5.5	Choosing task-specific parameters	41

5.5.1	CoLA	41
5.5.2	SST-2	42
5.5.3	Sara	42
6	Analysing the models	43
6.1	Analysing the models' predictions	43
6.2	Probing the models for linguistic knowledge	43
7	Overall discussion and conclusions	45
8	Future work	47
9	Plan for the rest of the semester	49
	Bibliography	51

Chapter 1

Introduction

1.1 Motivation

- After the deep learning hype started, NLP went through an era of LSTMs. Since 2017, the area has been becoming dominated by Transformer models pre-trained on large unlabelled corpora.
- As newer and bigger Transformer-based models were proposed in 2018 and 2019, improving on the SOTA, it was becoming clearer that their big size and low speed was rendering them difficult to use (both train and deploy) in practice outside of research labs.
- Recently, we've seen various early attempts at making Transformers – in particular BERT ([Devlin et al., 2018](#)) – smaller by removing attentional heads ([Michel et al., 2019](#)), quantisation and pruning ([Cheong and Daniel, 2019](#); [Sucik, 2019](#)). In terms of actually down-sizing and accelerating the models, knowledge transfer using teacher-student knowledge distillation has led to the most attractive results ([Mukherjee and Awadallah, 2019](#); [Tang et al., 2019b](#); [Jiao et al., 2019](#); [Sanh et al., 2019](#)).
- However, these studies focus only on using knowledge distillation as a tool. Important questions about the nature of this technique and how it interacts with properties of the teacher and student models remain generally unexplored.
- In line with the increasing demand for explainable AI, it is desirable that, for the beginning, at least the researchers better understand the tools they use, in this case distillation of NLP knowledge from Transformer models. Indeed, such understanding is also useful for overcoming the limitations and designing new variants of this method for smaller and better classifiers.

1.2 Aims

I aim to better understand knowledge distillation by exploring its use for knowledge transfer from BERT into different student architectures on various NLP tasks.

This can be further broken down into three aims:

- Explore the effectiveness of knowledge distillation in very different NLP tasks. To cover a broad variety of tasks, I use sentence classification datasets ranging from binary sentiment classification to 57-way intent classification to linguistic acceptability.
- Explore how distilling knowledge from a Transformer varies with different student architectures. I limit myself to using the extremely popular BERT model (Devlin et al., 2018) as the teacher architecture. As students, I use two different architectures: a BiLSTM, building on the successful work of Ralph Tang (Tang et al., 2019b,a), and a down-scaled BERT architecture.
- Explore how successfully can different types of NLP knowledge and capabilities be distilled. Since NLP tasks are often possible for humans to reason about, I analyse the models' behaviour (e.g. the mistakes they make) to learn more about knowledge distillation. I also probe the models for different linguistic capabilities, inspired by previous successful probing studies (Conneau et al., 2018; Tenney et al., 2019a).

1.3 Contributions

My actual findings. To be added later.

Chapter 2

Background [READY]

In this chapter, the Transformer models are introduced and set into the historical context; knowledge distillation is introduced, in particular its recent applications in NLP; and an overview of some relevant work in model understanding is given.

2.1 NLP before Transformers

By the very nature of the natural language, its processing has always meant processing sequences of variable length: be it written phrases or sentences, words (sequences of characters), spoken utterances, sentence pairs, or entire documents. Very often, NLP tasks boil down to making simple decisions about such sequences: classifying sentences based on their intent or language, assigning a score to a document based on its formality, deciding whether two given sentences form a meaningful question-answer pair, or predicting the next word of an unfinished sentence.

As early as 2008, artificial neural networks started playing a key role in NLP: [Collobert and Weston \(2008\)](#)¹ successfully trained a deep neural model to perform a variety of tasks from part-of-speech tagging to semantic role labelling. However, neural machine learning models are typically suited for tasks where the dimensionality of inputs is known and fixed. Thus, it comes as no surprise that NLP research has focused on developing better models that encode variable-length sequences into fixed-length representations. If any sequence (e.g. a sentence) can be embedded as a vector in a fixed-dimensionality space, a simple classification model can be learned on top of these vectors.

One key step in the development of neural sequence encoder models has been the idea of *word embeddings*: rich, dense, fixed-length numerical representations of words. When viewed as a lookup table – one vector per each supported word – such embeddings can be used to “translate” input words into vectors which are then processed further. [Mikolov et al. \(2013\)](#) introduced an efficient and improved

¹See also [Collobert et al. \(2011\)](#).

way of learning high-quality word embeddings: *word2vec*. The embeddings are learnt as part of a larger neural network, which is trained to predict the next word given several previous words, and the previous words given the current word². Such training can easily leverage large amounts of unlabelled text data and the embeddings learn to capture various properties from a word’s morphology to its semantics. Released word2vec embeddings became very popular due to their easy use and performance improvements in many NLP tasks. **TO-DO: Add a simple illustration of learning word2vec.**

While word embeddings were a breakthrough, they themselves do not address the issue of encoding a sequence of words into a fixed-size representation. This is where Recurrent neural networks (RNNs) (Rumelhart et al., 1986) and later their improved variant – Long Short-Term Memory neural networks (LSTMs) (Hochreiter and Schmidhuber, 1997) – come into play. Although originally proposed long ago, they became popular in NLP, and in text processing in particular, only later (see e.g. Mikolov et al. (2010) and Graves (2013)). These recurrent encoders process one word at a time (see Fig. 2.1) while updating an internal (“hidden”) fixed-size representation of the text seen so far. Once the entire sequence is processed, the hidden representation (also called “hidden state”) is outputted and used to make a simple prediction.

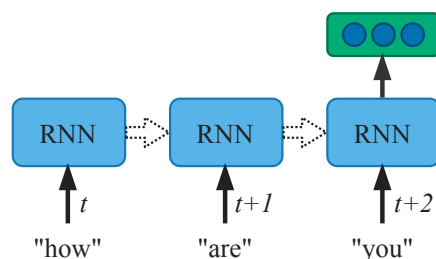


Figure 2.1. A recurrent neural network (RNN) consumes at each timestep one input word. Then, it produces a single vector representation of the inputs.

As various recurrent models started dominating NLP, one particularly influential architecture emerged, addressing tasks such as machine translation, where the output is a new sequence rather than a simple decision. This was the *encoder-decoder* architecture (Kalchbrenner and Blunsom, 2013; Sutskever et al., 2014), see Fig. 2.2. It uses a recurrent encoder to turn an input sentence into a single vector, and a recurrent decoder to generate an output sequence based on the vector.

Bahdanau et al. (2014) improved encoder-decoder models by introducing the concept of *attention*. The attention module helps the decoder produce better output by selectively focusing on the most relevant parts of the input at each decoder timestep. This is depicted in Fig. 2.3, showing the decoder just about to output the second word (“estás”). The steps (as numbered in the diagram) are:

²These are the so-called Continuous bag-of-words (CBOW) and Skip-gram (SG) tasks, respectively.

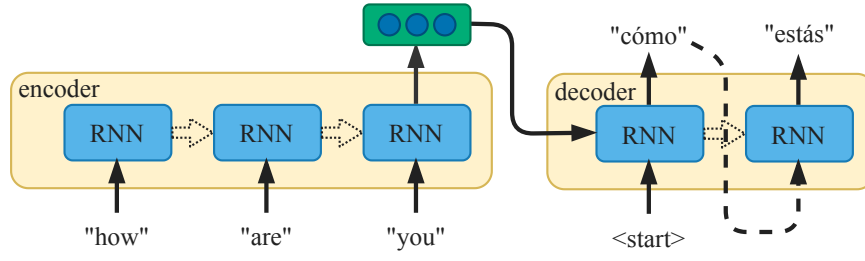


Figure 2.2. An encoder-decoder model for machine translation. Notice how the decoder initially takes as input the special $\langle \text{start} \rangle$ token and at later time consumes the previous output word.

1. the decoder's hidden state passed to the attention module,
2. the intermediate hidden states of the encoder also passed to the attention module,
3. the attention module, based on information from the decoder's state, selecting relevant information from the encoder's hidden states and combining it into the attentional *context vector*,
4. the decoder combining the last outputted word ("cómo") with the context vector and consuming this information to better decide which word to output next.

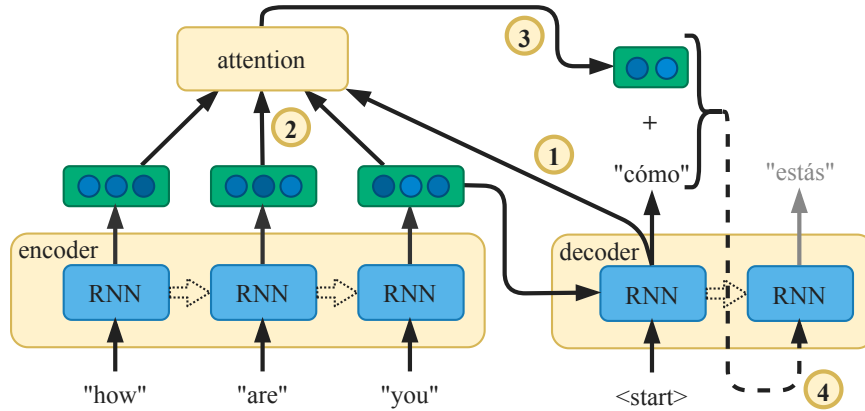


Figure 2.3. An encoder-decoder model for machine translation with added attention mechanism.

The attention can be described more formally³: First, the decoder state \mathbf{h}_D is processed into a *query* \mathbf{q} using

$$\mathbf{q} = \mathbf{h}_D \mathbf{W}_Q \quad (2.1)$$

and each encoder state $\mathbf{h}_E^{(i)}$ is used to produce the *key* and *value* vectors, $\mathbf{k}^{(i)}$ and $\mathbf{v}^{(i)}$:

$$\mathbf{k}^{(i)} = \mathbf{h}_E^{(i)} \mathbf{W}_K, \quad \mathbf{v}^{(i)} = \mathbf{h}_E^{(i)} \mathbf{W}_V. \quad (2.2)$$

³My description does not exactly follow the original works of [Bahdanau et al. \(2014\)](#) and [Luong et al. \(2015\)](#). Instead, I introduce concepts that will be useful in later sections of this work.

Then, the selective focus of the attention is computed as an *attention weight* $w^{(i)}$ for each encoder state i , by combining the query with the i -th key:

$$w^{(i)} = \mathbf{q}^\top \mathbf{k}^{(i)} . \quad (2.3)$$

The weights are normalised using softmax and used to create the context vector \mathbf{c} as a weighted average of the values:

$$\mathbf{c} = \sum_i a^{(i)} \mathbf{v}^{(i)} \quad \text{where} \quad a^{(i)} = \text{softmax}(w^{(i)}) = \frac{\exp(w^{(i)})}{\sum_j \exp(w^{(j)})} . \quad (2.4)$$

Note that W_Q , W_K , W_V are matrices of learnable parameters, optimised in training the model. This way, the attention’s “informed selectivity” improves over time.

For years, recurrent models with attention were the state of the art in many NLP tasks. However, as we will see, the potential of attention reached far beyond recurrent models.

2.2 Transformer-based NLP

2.2.1 Transformers

We saw how the attention mechanism can selectively focus on parts of a sequence to extract relevant information from it. This raises the question of whether processing the inputs in a sequential fashion with the recurrent encoder is still needed. In particular, RNN models are slow as a results of this sequentiality, with no room for parallelisation. In their influential work, [Vaswani et al. \(2017\)](#) proposed an encoder-decoder model based solely on attention and fully parallelised: the *Transformer*. The core element of the model is the *self-attention* mechanism, used to process all input words in parallel.

In particular, a Transformer model typically has multiple self-attention layers, each layer processing separate representations of all input words. Continuing with the three-word input example from [Fig. 2.3](#), a high-level diagram of the workings of a self-attention layer is shown in [Fig. 2.4](#). Importantly, the input word representations evolve from lower to higher layers such that they consider not just the one input word, but also all other words – the representation becomes *contextual* (also referred to as a *contextual embedding* of the word within the input sentence).

As for the internals of self-attention, the basic principle is very similar to standard attention. Self-attention too is used to focus on and gather relevant information from a sequence of elements, given a query. However, to produce a richer contextual embedding $\mathbf{h}_{l+1}^{(i)}$ in layer $l+1$ of the i -th input word, self-attention uses the incoming representation $\mathbf{h}_l^{(i)}$ for the query, and considers focusing on all representations in layer l , including $\mathbf{h}_l^{(i)}$ itself. [Fig. 2.5](#) shows this in detail for input

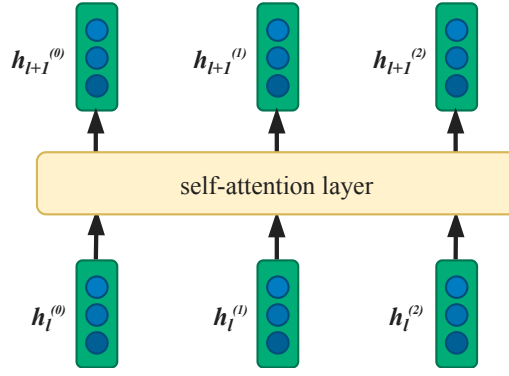


Figure 2.4. A high-level diagram of the application of self-attention in Transformer models. Three hidden states are shown for consistency with the length of the input shown in Fig. 2.3; in general, the input length can vary.

position $i = 0$. Query $q^{(0)}$ is produced and matched with every key in layer l (i.e. $k^{(0)}, \dots, k^{(2)}$) to produce the attention weights. These weights quantify how relevant each representation $h_l^{(i)}$ is with respect to position $i = 0$. Then, the new contextual embedding $h_{l+1}^{(i)}$ is constructed as a weighted sum of the values $v^{(0)}, \dots, v^{(2)}$ (same as constructing the context vector in standard attention).

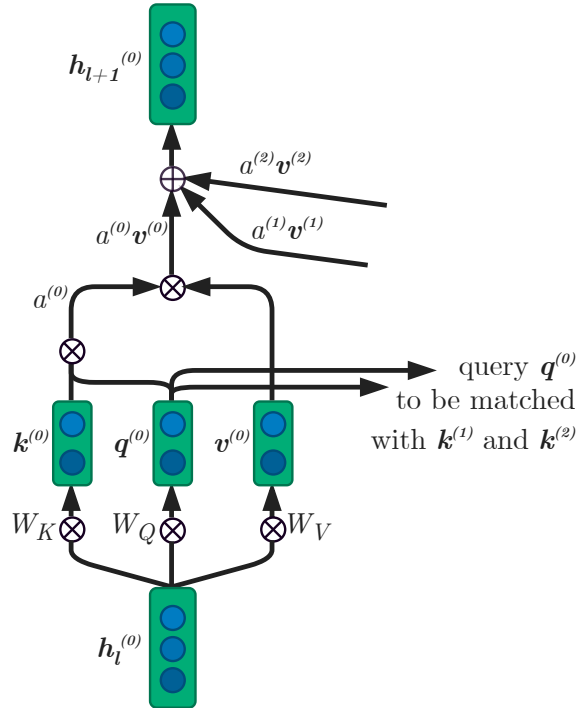


Figure 2.5. The internals of self-attention, illustrated on creating the next-layer hidden representation of the input position $i = 0$, given all representations in the current layer. Note that \otimes stands for multiplication (where the multiplication involves a learnable matrix like W_K , this is written next to the \otimes), and \oplus denotes summation.

Notice that, even though each contextual embedding considers all input positions, the next-layer contextual embeddings $h_{l+1}^{(0)}, \dots, h_{l+1}^{(2)}$ can be computed all at the

same time, in parallel: First, the keys, queries and values for all input positions are computed; then, the attention weights with respect to each position are produced; finally, all the new representations are produced. It is this parallelism that allows Transformer models to run faster. As a result, they can be much bigger (and hence create richer input representations) than recurrent models while taking the same time to train.

Due to their parallel nature, self-attentional layers have no notion of an element’s position within the input sequence. This means no sensitivity to word order. (Recurrent models sense this order quite naturally because they process input text word by word.) To alleviate this downside of self-attention, Transformers use *positional embeddings*. These are artificially created numerical vectors added to each input word, different across input positions, thus enabling the model’s layers to learn to be position- and order-sensitive.

As an additional improvement of the self-attentional mechanism, Vaswani et al. introduce the concept of multiple self-attention heads. This is very similar to having multiple instances of the self-attention module in Fig. 2.5 (each instance being one *head*). The motivation behind multiple self-attention heads is to enable each head h to learn different “focusing skills” by learning its own $W_{Q,h}$, $W_{K,h}$, $W_{V,h}$. Each head produces its own output:

$$O_{att,h} = \text{softmax}\left(\frac{\mathbf{q}\mathbf{k}^\top}{\sqrt{d_k}}\right)\mathbf{v} = \text{softmax}\left(\frac{(\mathbf{h}_l^\top W_{Q,h})^\top (\mathbf{h}_l^\top W_{K,h})}{\sqrt{d_k}}\right)(\mathbf{h}_l^\top W_{V,h}) \quad (2.5)$$

which matches Fig. 2.5 (but notice the detail of the additional scaling by $\frac{1}{\sqrt{d_k}}$, introduced by Vaswani et al., where d_k is the dimensionality of the key). The outputs of the H individual heads are then concatenated and dimensionality reduced with a trainable linear transformation W_{AO} , to produce the final output, which replaces \mathbf{h}_{l+1} in Fig. 2.5:

$$O_{att} = [O_{att,1}, \dots, O_{att,H}]W_{AO} . \quad (2.6)$$

Besides the self-attention-based architecture, there is one more important property that makes today’s Transformer models perform so well on a wide variety of NLP tasks: the way these models are trained. First used for Transformers by Radford et al. (2018)⁴, the general procedure is:

1. *Unsupervised pre-training*: The model is trained on one or more tasks, typically language modelling, using huge training corpora. For example, Radford et al. pre-train their model to do next word prediction (the standard language modelling task) on a huge corpus of over 7,000 books.
2. *Supervised fine-tuning*: The pre-trained model is trained on a concrete dataset to perform a desired downstream task, such as predicting the sentiment of a sentence, translating between languages, etc.

⁴The idea was previously used with recurrent models by Dai and Le (2015).

This two-step procedure is conceptually similar to using pre-trained word embeddings. In both cases, the aim is to learn general language knowledge and then use this as a starting point for focusing on a particular task. However, in this newer case, the word representations learned in pre-training are better tailored to the specific architecture, and they are inherently contextual – compared to pre-trained word embeddings like word2vec which are typically context-insensitive.

Importantly, pre-trained knowledge makes models more suitable for downstream tasks with limited amounts of labelled data. The model no longer needs to acquire all the desired knowledge just from the small dataset; it contains pre-trained high-quality general language knowledge which can be reused in various downstream tasks. This means that large, powerful Transformer models become more accessible: They are successfully applicable to a wider array of smaller tasks than large models that have to be trained from scratch.

2.2.2 BERT

Perhaps the most popular Transformer model today is BERT (Bidirectional Encoder Representations from Transformers), proposed by [Devlin et al. \(2018\)](#). Architecturally, it is a sequence encoder, hence suited for sequence classification tasks. While being heavily based on the original Transformer ([Vaswani et al., 2017](#)), BERT adds a few further tricks:

1. The model learns bidirectional representations: It can be trained on language modelling that is not next-word prediction (prediction given left context), but word prediction given both the left and the right context.
2. It uses two very different pre-training classification tasks:
 - (a) The *masked language modelling* (MLM) task encourages BERT to learn good contextual word embeddings. The task itself is to correctly predict the token at a given position in a sentence, given that the model can see the entire sentence with the target token(s) masked out⁵, with a different token, or left unchanged.
 - (b) The *next-sentence prediction* (NSP) task encourages BERT to learn good sentence-level representations. Given two sentences, the task is to predict whether they formed a consecutive sentence pair in the text they came from, or not.

The pre-training was carried out on text from books and from the English Wikipedia, totalling to 3,400 million words (for details see [Devlin et al. \(2018\)](#)). The MLM and NSP tasks were both used throughout the pre-training, forcing the model to learn both at the same time.

3. The inputs are processed not word by word, but are broken down using a fixed vocabulary of sub-word units (*wordpieces*, introduced by [Wu et al.](#)

⁵I.e. replaced with the special [MASK] token.

(2016)). This way, BERT can better deal with rare words. (In word-level models, words that are not found in the model’s vocabulary are replaced with a special UNKNOWN token, which means disregarding any information carried by the words.) The tokeniser module of BERT uses the wordpiece vocabulary to tokenise (segment) the input text before it is further processed. Fig. 2.6 shows an example; notice how my surname (“Sucik”) gets split into three wordpieces whereas the other, much more common words are found in the wordpiece vocabulary.

4. To enable the different pre-training tasks as well as two-sentence inputs, BERT uses a special input sequence representation, illustrated in Fig. 2.6. Given the two input sentences S_A , S_B , they are concatenated and separated by the special [SEP] token. The overall sequence is prepended with the [CLS] (classification) token. Then, for tasks like NSP, only the output representation of the [CLS] token (i.e. \mathbf{o}_0) is used, whereas for token-level tasks like MLM the output vector from the desired position is used (in Fig. 2.6, the MLM task would use \mathbf{o}_3 to predict the correct token at this position).

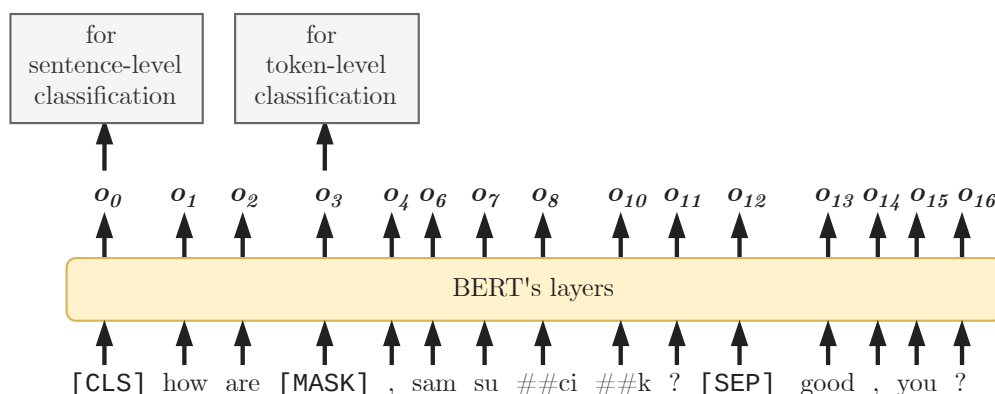


Figure 2.6. BERT’s handling of input for sentence-level and token-level tasks. The input sentences ($S_A = \text{How are you, Sam Sucik?}$ and $S_B = \text{Good, you?}$) are shown as split by BERT’s tokeniser, with the first instance of “you” masked out for MLM.

The overall architecture of BERT is shown in Fig. 2.7. The tokeniser also adds the special tokens like [CLS] and [SEP] to the input, while the trainable token embedding layer also adds positional embeddings to the tokens. The pooler takes the appropriate model output (for sequence level classification the first output \mathbf{o}_0 as discussed above) and applies a fully-connected layer with the tanh activation function. The external classifier is often another fully-connected layer with the tanh activation, producing the logits⁶. These get normalised using softmax to produce a probability distribution over all classes. The most probable class is outputted as the model’s prediction.

To complete the picture of BERT, Fig. 2.8 shows the internals of an encoder layer. Besides the multi-headed self-attention submodule, it also contains the

⁶For a classifier, the logits are the (unnormalised) predicted class probabilities.

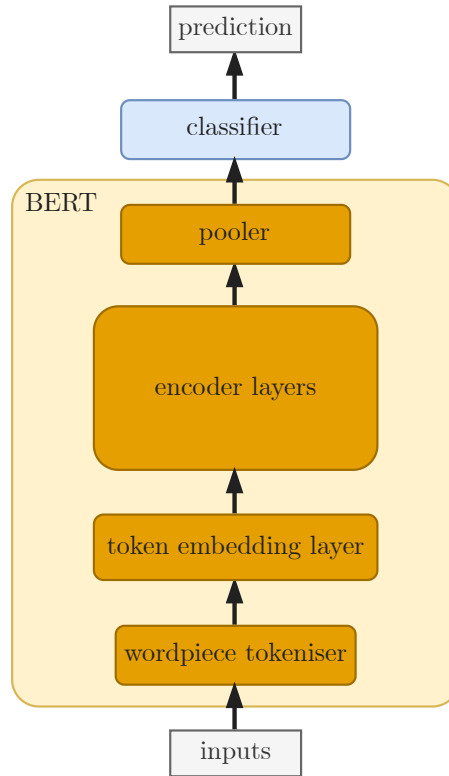


Figure 2.7. High-level overview of the modules that make up the architecture of BERT as used for sequence-level classification.

fully-connected submodule, consisting of the intermediate fully-connected transformation with parameters W_I , and the layer output fully-connected transformation with parameters W_O . Each submodule is also by-passed by a residual connection (shown with dashed lines). The residual information is summed with the submodule's output, and layer normalisation is applied to the sum. Note that this structure is not new in BERT; it was used already by the original Transformer of Vaswani et al. (2017). Conveniently, Transformers are designed such that all of the intermediate representations (especially the encoder inputs and outputs, and the self-attention layer inputs and outputs) have the same dimensionality d_h – this makes any residual by-passing and summing easy.

Originally, pre-trained BERT was released in two sizes: BERT_{Base} with 110 million parameters, 12 encoder layers and 12-head self-attention, and BERT_{Large} with 340 million parameters, 24 encoder layers and 16-head self-attention. The models quickly became popular, successfully applied to various tasks from document classification (Adhikari et al., 2019) to video captioning (Sun et al., 2019). Further pre-trained versions were released too, covering, for example, the specific domain of biomedical text (Lee et al., 2019) or multilingual text (Pires et al., 2019).

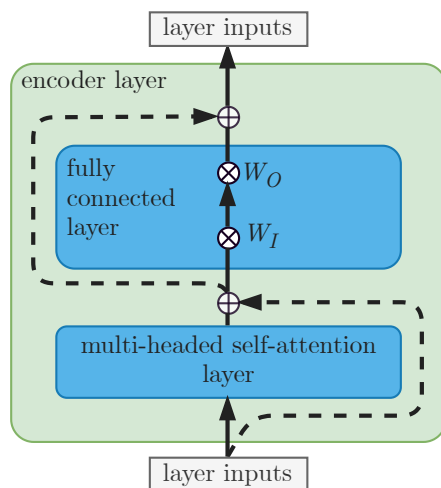


Figure 2.8. The modules making up one encoder layer in BERT; residual connections highlighted by using dashed lines.

2.2.3 Newer and larger Transformer models

Following the success of the early Transformers and BERT (Vaswani et al., 2017; Radford et al., 2018; Devlin et al., 2018), many further model variants started emerging, including:

- The OpenAI team releasing GPT-2 (Radford et al., 2019), a larger and improved version of their original, simple Transformer model GPT (Radford et al., 2018).
- Lample and Conneau (2019) introducing XLM, which uses cross-lingual pre-training and is thus better suited for downstream tasks in different languages.
- Transformer-XL (Dai et al., 2019), which features an improved self-attention that can handle very long contexts (across multiple sentences/documents).

All these open-sourced, powerful pre-trained models were a significant step towards more accessible high-quality NLP (in the context of downstream tasks with limited data). However, the model size – often in 100s of million trainable parameters – meant these models could not be applied easily in practice (outside of research): They were memory-hungry and slow.

Naturally, this inspired another stream of research: Compressing large, well-performing Transformer models (very often BERT) to make them faster and resource-efficient. I turn my focus to one compression method that worked particularly well so far: the teacher-student knowledge distillation.

2.3 Teacher-student knowledge distillation

2.3.1 A brief introduction to knowledge distillation

Knowledge distillation was introduced by (Bucila et al., 2006) as a way of knowledge transfer from large models into small ones. The aim is to end up with a smaller – and hence faster – yet well-performing model. The steps are 1) to train a big neural classifier model (also called the *teacher*), 2) to let a smaller neural classifier model (the *student*) learn from it – by learning to mimic the teacher’s behaviour. Hence also the name *teacher-student knowledge distillation*, often simply *knowledge distillation*.

There are different ways of defining the teacher’s “behaviour” which the student learns to mimic. Originally, this was realised as learning to mimic the teacher’s predictions: A dataset would be labelled by the teacher, and the student would be trained on these labels (which are in this context referred to as the *hard labels*). The dataset used for training the student (together with the teacher-generated labels) is referred to as the *transfer dataset*.

Later, Ba and Caruana (2014) introduced the idea of learning from the teacher-generated *soft labels*, which are the teacher’s logits. The idea is to provide the student with richer information about the teacher’s decisions: While hard labels only express which class had the highest predicted probability, soft labels also describe how confident the prediction was and which other classes (and to what extent) the teacher was considering for a given example.

When soft labels were first used, the student’s training loss function was the mean squared distance between the student’s and the teacher’s logits:

$$E_{MSE} = \sum_{c=1}^C (z_t^{(c)} - z_s^{(c)})^2 \quad (2.7)$$

where C is the number of classes and z_t, z_s are the teacher’s and student’s logits. Hinton et al. (2015) proposed a more general approach, addressing the issue of overconfident teachers with very sharp logit distributions. The issue with such distributions is that they carry little additional information beyond the hard label (since the winning class has a huge probability and all others have negligibly small probabilities). To “soften” such sharp distributions, Hinton et al. proposed using the *cross-entropy loss* (2.8) in combination with softmax with temperature (2.9) (instead of the standard softmax) in training both the teacher and the student.

$$E_{CE} = \sum_{c=1}^C z_t^{(c)} \log z_s^{(c)} \quad (2.8)$$

$$p_c = \frac{\exp(z^{(c)}/T)}{\sum_{c'=1}^C \exp(z^{(c')}/T)} \quad (2.9)$$

The temperature parameter T determines the extent to which the distribution will be “unsharpened” – two extremes being the completely flat, uniform distribution

(for $T \rightarrow \infty$) and the maximally sharp distribution⁷ (for $T \rightarrow 0$). When $T > 1$, the distribution gets softened and the student can extract richer information from it. Today, using soft labels with the cross-entropy loss with temperature is what many refer to simply as knowledge distillation.

Since 2015, further knowledge distillation variants have been proposed, enhancing the vanilla technique in various ways, for example:

- Papamakarios (2015, p. 13) points out that mimicking teacher outputs can be extended to mimicking mimicking the *derivatives* of the teacher’s loss with respect to the inputs. This is realised by including in the student’s loss function also the term: $\frac{\partial \mathbf{o}_s}{\partial \mathbf{x}} - \frac{\partial \mathbf{o}_t}{\partial \mathbf{x}}$ (\mathbf{x} being an input, e.g. a sentence, and \mathbf{o} being the output, e.g. the predicted class).
- Romero et al. (2015) proposed to additionally match the teacher’s internal, intermediate representations of the input. Huang and Wang (2017) achieved this by learning to align the distributions of neuron selectivity patterns between the teacher’s and the student’s hidden layers. Unlike standard knowledge distillation, this approach is no longer limited only to classifier models with softmax outputs (see the approach of Hinton et al. (2015) discussed above).
- Sau and Balasubramanian (2016) showed that learning can be more effective when noise is added to the teacher logits.
- Mirzadeh et al. (2019) showed that when the teacher is much larger than the student, knowledge distillation performs poorly, and improved on this by “multi-stage” distillation: First, knowledge is distilled from the teacher into an intermediate-size “teacher assistant” model, then from the assistant into the final student.

2.3.2 Knowledge distillation in NLP

The knowledge distillation research discussed so far was tied to the image processing domain. This is not surprising: Image processing was the first area to start taking advantage of deep learning, and bigger and bigger models had been researched ever since the revolutionary AlexNet (Krizhevsky et al., 2012).

In NLP, the (recurrent) models were moderately sized for a long time, not attracting much research in model compression. Still, one early notable work was on adapting knowledge distillation for sequence-to-sequence models (Kim and Rush, 2016), while another pioneering study (Yu et al., 2018) distilled a recurrent model into an even smaller one – to make it suitable for running on mobile devices.

Understandably, the real need for model compression started very recently, when the large pre-trained Transformer models became popular. Large size and low

⁷I.e. having the preferred class’s probability 1 and the other classes’ probabilities 0.

speed seemed to be the only downside of these – otherwise very successful and accessible – models.

Perhaps the first decision to make when distilling large pre-trained models is at which point to distill. In particular, one can distill the general knowledge from a pre-trained teacher and use such general student by fine-tuning it on downstream tasks, or one can fine-tune the pre-trained teacher on a task and then distill this specialised knowledge into a student model meant for the one task only. Each of these approaches has its advantages and disadvantages.

In the first scenario (distilling pre-trained knowledge), a major advantage is that the distillation happens once and the small student can be fine-tuned fast for various downstream tasks. Since the distillation can be done on the same data that the teacher was pre-trained on – large unlabelled text corpora –, lack of transfer data is not a concern. A possible risk is that the large amount of general pre-trained language knowledge will not “fit” into the small student, requiring the student itself to be considerably large. [Sanh et al. \(2019\)](#) took this approach and, while their student is successfully fine-tuned for a wide range of tasks, it is only 40% smaller than the BERT_{Base} teacher.

In the second scenario, only the task-specific knowledge needs to be transferred to the student – potentially allowing very small students. However, teacher fine-tuning and distillation have to be done anew for each task and this is resource-hungry. Additionally, there may be a lack of transfer data if the downstream task dataset is small. Various ways of addressing this issue by *augmenting* small datasets have been proposed, with mixed success. [Mukherjee and Awadallah \(2019\)](#) use additional unlabelled in-domain sentences with labels generated by the teacher – this is limited to cases where such in-domain data are available. [Tang et al. \(2019b\)](#) create additional sentences using simple, rule-based perturbation of existing sentences from the downstream dataset. Finally, [Jiao et al. \(2019\)](#) and [Tang et al. \(2019a\)](#) use large Transformer models generatively to create new sentences. In the first case, BERT is applied repeatedly to an existing sentence, changing words into different ones one by one and thus generating a new sentence. In the second case, new sentences are sampled token-by-token from a GPT-2 model fine-tuned on the downstream dataset with the next-token-prediction objective.

Clearly, each approach is preferred in a different situation: If the requirement is to compress the model as much as possible, and there is enough transfer data, distilling the fine-tuned teacher is more promising. If, on the other hand, one wants to make available a re-usable, small model, then distilling the broader, pre-trained knowledge is preferred.

2.4 Understanding NLP models

Neural models are by their very nature opaque or even black boxes, and (not) really understanding the models is a serious concern. Despite the typical pre-

ference of performance over transparency, recently, the demand for explainable artificial intelligence (XAI) has been increasing, as neural models become widely used.

The area of image processing has seen the most attempts at interpreting neural models, partly because reasoning about images is easy for humans. Various techniques shed light into the workings of image classifiers, e.g. creating images that maximally excite certain neurons (Simonyan et al., 2013) or highlighting those parts of an image that a particular neuron “focuses” on (Zeiler and Fergus, 2013).

In NLP, interpreting is more difficult and historically came with a delay similar to the delay with which large neural models became popular for NLP tasks. In their review, Belinkov and Glass (2018) observe that many methods for analysing and interpreting models are simply adapted from image processing, in particular the approach of visualising a single neuron’s focus, given an input. In attentional sequence-to-sequence models, the attention maps can be visualised to explore the soft alignments between input and output words (see, e.g., Strobel et al. (2018)). However, these methods are mostly qualitative and suitable for exploring individual input examples, thus not well suited for drawing statistically backed conclusions or for model comparison.

More quantitative and NLP-specific are the approaches that explore the linguistic knowledge present in a model’s internal representations. Most often, this is realised by *probing* the representations for specific linguistic knowledge: trying to automatically recover from them specific properties of the input. When such recovery works well, the representations must have contained the linguistic knowledge tied to the input property in question. First used by Shi et al. (2016) for exploring syntactic knowledge captured by machine translation models, this general approach was quickly adopted more widely. Adi et al. (2017) explored sentence encodings from recurrent models by probing for simple properties like sentence length, word content and word order. More recently, Conneau et al. (2018) curated a set of 10 probing tasks ranging from easy surface properties (e.g. sentence length) through syntactic (e.g. the depth of the syntactic parse tree) to semantic ones (e.g. identifying semantically disrupted sentences). Focusing on Transformers, Tenney et al. (2019b) proposed a set of *edge probing* tasks, examining how much contextual knowledge about an entire input sentence is captured within the contextual representation of one of its words. Their tasks correspond to the typical steps of a text processing pipeline – from part-of-speech (POS) tagging to identifying dependencies and entities to semantic role labelling. Tenney et al. (2019a) managed to localise the layers of BERT most important for each of these “skills”. They showed that the ordering of these “centres of expertise” within BERT’s encoder matches the usual low- to high-level order: from simple POS tagging in the earlier layers to the most complex semantic tasks in the last layers.

While the discussed approaches provide valuable insights, they merely help us intuitively describe or quantify the kinds of internal knowledge/expertise present in the models. Gilpin et al. (2018) call this level of model understanding *in-*

interpretability – comprehending what a model does. However, they argue that what we should strive to achieve is *explainability*: the ability to “summarize the reasons for neural network behavior, gain the trust of users, or produce insights about the causes of their decisions”. In this sense, today’s methods achieve only interpretability because they enable researchers to describe but not explain – especially in terms of causality – the internals and decisions of the models. Still, interpreting models is an important step not only towards explaining them, but also towards understanding the properties of different architectures and methods and improving them.

Chapter 3

Datasets [READY]

In this chapter, I introduce the downstream tasks and how I augmented their data to create large transfer datasets. I also introduce the probing tasks used later for analysing the teacher and student models.

3.1 Downstream tasks

The downstream task datasets I use to fine-tune the teacher model. The tasks are chosen to be diverse so that the knowledge distillation analysis later in this work is set in a wide NLP context. At the same time, all the datasets are rather small and therefore well representing the type of use case where pre-trained models like BERT are desirable due to the lack of labelled fine-tuning data.

Today, perhaps the most widely used collection of challenging NLP tasks¹ is the GLUE benchmarking collection (Wang et al., 2018). This collection comprises 11 tasks which enable model benchmarking on a wide range of NLP tasks from sentiment analysis to detecting textual similarity, all framed as single-sentence or sentence-pair classification. Each task comes with an official scoring metric (such as accuracy or F1), labelled training and evaluation datasets, and a testing dataset with labels not released publicly. The test-set score accumulated over all 11 tasks forms the basis for the popular GLUE leaderboard².

In this work, I use single-sentence classification tasks (i.e. not sentence-pair tasks). Therefore, only two GLUE tasks are suitable for my purposes – the Corpus of Linguistic Acceptability (CoLA) and the Stanford Sentiment Treebank in its binary classification variant (SST-2). As the third task, I use an intent classification dataset called Sara, which is not part of the GLUE collection.

¹Challenging by the nature of the tasks and by the small dataset size.

²gluebenchmark.com/leaderboard

3.1.1 Corpus of Linguistic Acceptability

The CoLA dataset ([Warstadt et al., 2018](#)) comprises roughly 8,500 training sentences, 1,000 evaluation and 1,000 testing sentences. The task is to predict whether a given sentence represents acceptable English or not (binary classification). All the sentences are collected from linguistic literature where they were originally hand-crafted to demonstrate various linguistic principles and their violations.

The enormous variety of principles, together with many hand-crafted sentences that comply with or violate a principle in a niche way, make this dataset very challenging even for the state-of-the-art Transformer models. As a non-native speaker, I myself struggle with some of the sentences, for instance:

- **The car honked down the road.* (unacceptable)
- *Us, we'll go together.* (acceptable)

There are many examples which are easy for humans to classify but may be challenging for models which have imperfect understanding of the real world. Sentences like “Mary revealed himself to John.” require the model to understand that “Mary”, being a typical female name, disagrees with the masculine “himself”.

The scoring metric is Matthew’s Correlation Coefficient (MCC) ([Matthews, 1975](#)), a correlation measure between two binary classifications. The coefficient is also designed to be robust against class imbalance, which is important because the dataset contains many more acceptable examples than unacceptable ones.

3.1.2 Stanford Sentiment Treebank

The SST-2 dataset ([Socher et al., 2013](#)) is considerably bigger than CoLA, with roughly 67,000 training examples, 900 evaluation and 1,800 testing examples. It contains sentences and phrases from movie reviews collected on [rottentomatoes.com](#). The main SST dataset comes with human-created sentiment annotations on the continuous scale from very negative to very positive. SST-2 is a simplified version with neutral-sentiment phrases removed, only containing binary sentiment labels (positive and negative).

Unlike the hand-crafted examples in CoLA, many examples in SST-2 are not the best-quality examples. In particular, sentences are sometimes split into somewhat arbitrary segments³, such as:

- *should have been someone else -* (negative)
- *but it could have been worse.* (negative)

The labels are also sometimes unclear, see:

³This is due to the use of an automated parser in creating the dataset.

- *american chai encourages rueful laughter at stereotypes only an indian-american would recognize.* (negative)
- *you won't like roger, but you will quickly recognize him.* (negative)

Despite the problematic examples, most are straightforward (e.g. “delightfully cheeky” or “with little logic or continuity”), making this task a relatively easy one. With accuracy being the official metric, best models in the GLUE leaderboard score over 97%, very close to the official human baseline of 97.8%⁴.

3.1.3 Sara

As the third task, I use an intent classification dataset created by Rasa, a start-up building open-source tools for conversational AI⁵.

The dataset is named Sara after the chatbot deployed on the company's website⁶. The Sara chatbot is aimed for holding conversations with the website visitors on various topics, primarily answering common questions about Rasa and the tools that it develops (the same tools were used to build Sara). To support diverse topics, Sara internally classifies each human message as one of 57 intents and then generates an appropriate response. The Sara dataset is a collection of human-generated message examples for each of the 57 intents, e.g.:

- *what's the weather like where you are?* (ask_weather)
- *what is rasa actually* (ask_what_is_rasa)
- *yes please!* (affirm)
- *i need help setting up* (install_rasa)
- *where is mexico?* (out_of_scope)

TO-DO: List of all intents with brief descriptions or representative examples? Perhaps in the appendix...

In the early days of the chatbot, it supported fewer intents, and several artificial examples per intent were first hand-crafted by Rasa employees to train the initial version of Sara's intent classifier. After Sara was deployed, more examples were collected and annotated from conversations with the website's visitors⁷. Inspired by the topics that people tended to ask about, new intent categories were added. Today, the dataset still evolves and can be found – together with the implementation of Sara – at github.com/RasaHQ/rasa-demo (accessed April 3,

⁴See the GLUE leaderboard at gluebenchmark.com/leaderboard

⁵For transparency: I did a Machine learning research internship with Rasa in the summer of 2019.

⁶See the bot in action at rasa.com/docs/getting-started/.

⁷To get a consent for such use of the conversations, each visitor was shown the following before starting a conversation with Sara: “Hi, I'm Sara! By chatting to me you agree to our privacy policy.”, with a link to rasa.com/privacy-policy/

2020). It contains both the original hand-crafted examples as well as the (much more abundant) “real” examples.

The Sara dataset version I use dates back to October 2019, when I obtained it from Rasa and pseudonymised the data⁸. In particular, I removed any names of persons and e-mail addresses in any of the examples, replacing them with the special tokens `__PERSON_NAME__` and `__EMAIL_ADDRESS__`, respectively. The dataset comprises roughly 4,800 examples overall, and was originally split into 1,000 testing examples and 3,800 training examples. I further split the training partition into training and evaluation, with roughly 2,800 and 1,000 examples, respectively. All three partitions have the same class distribution.

In line with how the dataset is used for research at Rasa, I use as the main scoring metric the multi-class micro-averaged F_1 score. This variant of multi-class F_1 considers all examples combined and is computed from the overall precision P and recall R in the usual way: $F_{1micro} = \frac{2PR}{P+R}$. Here, the overall P and R are calculated from the overall true-positives TP , false-positives FP and false-negatives FN :

$$P = TP/(TP + FP), \quad R = TP/(TP + FN) \quad (3.1)$$

where TP is in this case the total number of correctly predicted examples (hits H), and both FN and FP equal the number of incorrect predictions (misses M). Hence:

$$F_{1micro} = H/(H + M) = P = R = accuracy. \quad (3.2)$$

Compared to another popular multi-class metric – the macro-averaged F_1 , the F_{1micro} score takes into account the sizes of different classes by looking at all examples in combination. This way, the overall score cannot be harshly pulled down just because of low recall or precision on some small, rare class.

3.2 Data augmentation for larger transfer datasets

As discussed in [Section 2.3.2](#), the transfer datasets in knowledge distillation often need to be augmented; if they are too small, they don’t provide enough opportunity for the teacher to “demonstrate its knowledge” to the student, and the student learns little.

[Tang et al. \(2019a\)](#) demonstrated on several GLUE tasks that using an augmented training portion for distillation leads to much better student performance than using just the original small training portion. For CoLA in particular, using just the small training set led to very poor student performance (see Table 1 in [Tang et al.](#)).

I take the augmentation approach that [Tang et al.](#) found to work the best: Generating additional sentences using a GPT-2 model ([Radford et al., 2019](#))

⁸As a former employee (intern) of Rasa, I got access to the data under the NDA I had signed with the company.

fine-tuned on the training set⁹. The steps for creating the transfer dataset from the training portion are:

1. Fine-tune the pre-trained GPT-2 model (the 345-million-parameter version) on the training portion for 1 epoch with the language-modelling objective (i.e. predicting the next subword token given the sequence of tokens so far).
2. Sample from the model a large number of tokens to be used as the beginnings (*prefixes*) of the augmentation sentences. This sampling can be done as one-step next-token prediction given the special **SOS** (start-of-sentence) token.
3. Starting from each sampled prefix, generate an entire sentence token by token by repeatedly predicting the next token using the GPT-2 model. The generation of a sentence stops when the special **EOS** (end-of-sentence) token is generated or when the desired maximum sequence length is reached (in this case 128 tokens).
4. Add the generated augmentation sentences to the original training data, and generate the teacher logits for each sentence.

For consistency with Tang et al. (2019a), I added 800,000 augmentation sentences to the training data of each of the three downstream tasks, resulting in the transfer datasets comprising roughly 808,500, 867,000, and 802,800 sentences for CoLA, SST-2, and Sara, respectively.

3.3 Probing tasks

The probing tasks (discussed in Section 2.4) I use after knowledge distillation to analyse the linguistic capabilities of the students and the teacher. In particular, I use the probing suite curated by Conneau et al. (2018), consisting of 10 tasks¹⁰.

Each probing task is a collection of 120,000 labelled sentences, split into training (100,000), evaluation (10,000) and test (10,000) set. The label refers to a property of the sentence, such as the sentence’s length. The aim is to recover the property from an encoding of the sentence, produced by the model being probed. Fig. 3.1 shows the basic workflow. First, the model is used to produce an encoding of each sentence. Then, a light-weight classifier is trained, taking the training sentences’ encodings as inputs and learning to produce the labels. The evaluation sentence encodings are used to optimise the hyperparameters of the classifier. Finally, a probing score (accuracy) is produced on the test encodings. The score quantifies how well the sentence property in question is recoverable (and thus present) in the encodings. This serves as a proxy measure of the linguistic knowledge tied

⁹I used the code for Tang et al. (2019a) which is available at github.com/castorini/d-bert (accessed April 4, 2020).

¹⁰The data, along with code for probing neural models, are publicly available as part of the SentEval toolkit for evaluating sentence representations (Conneau and Kiela, 2018) at github.com/facebookresearch/SentEval (accessed April 4, 2020).

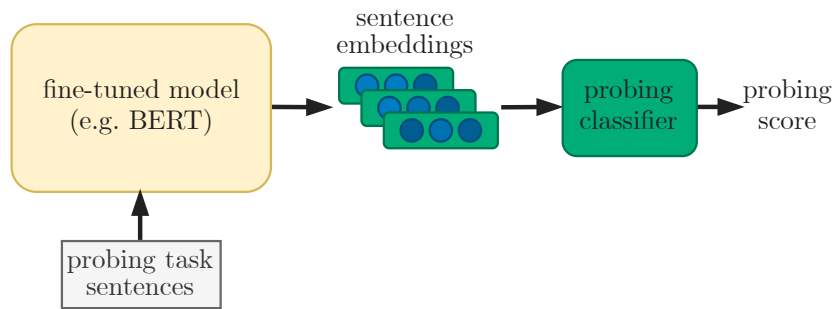


Figure 3.1. A high-level diagram of the probing process.

to the property. If, for instance, the property to be recovered is the depth of a sentence’s syntactic parse tree, the score hints at the model’s (un)capability to understand (and parse) the syntax of input sentences.

Regarding the linguistic capabilities explored by the probing suite, each task falls into one of three broad categories – surface properties, syntax, and semantics:

1. Surface information:

- **Length** is about recovering the length of the sentence. The labels are somewhat simplified: The actual sentence lengths grouped into 6 equal-width bins – making this task a 6-way classification.
- **WordContent** is about identifying which words are present in the sentence. A collection of 1000 mid-frequency words was curated, and sentences were chosen such that each contains exactly one of these words. The task is identify which one (1000-way classification).

2. Syntactic information:

- **Depth** is about classifying sentences by their syntactic parse tree depth, with depths ranging from 5 to 12 (hence 8-way classification).
- **BigramShift** is about sensitivity to (un)natural word order – identifying sentences in which the order of two randomly chosen adjacent words has been swapped (binary classification).
- **TopConstituents** is about recognising the top syntactic constituents – the nodes found in the syntactic parse tree just below the S (sentence) node. This is framed as 20-way classification, choosing from 19 most common top-constituent groups + the option of “other”.

3. Semantic information:

- **Tense** is binary classification task, identifying the tense (present or past) of the sentence – given by the main verb of the sentence (the verb in the main clause). At the first sight, this is mainly a morphological task (in English, most verbs have the past tense marked by the “-d/ed”

suffix). However, the model first has to identify the main verb within a sentence, which makes this task also semantic.

- **SubjNumber** is about determining the number (singular or plural) of the sentence’s subject (binary classification). Similar to the previous task, this one (and the next one too) is arguably about both morphology and semantics.
- **ObjNumber** is the same as SubjNumber, applied to the direct object of a sentence.
- **OddManOut** is binary classification, identifying sentences in which a randomly chosen verb or noun has been replaced with a different random verb or noun. Presumably, the random replacement in most cases makes the sentence semantically unusual or invalid (e.g. in “He reached inside his persona and pulled out a slim, rectangular black case.” the word “persona” is clearly odd). To make this task more difficult, the replacement word is chosen such that the frequency of the bigrams in the sentence stays roughly the same. (Otherwise, in many cases, the random replacement would create easy hints for the probing classifier, in the form of bigrams that are very unusual.)
- **CoordinationInversion** works with sentences that contain two coordinate clauses (typically joined by a conjunction), e.g. “I ran to my dad, but he was gone.” In half of the sentences, the order of the two clauses was swapped, producing sentences like: “He was gone, but I ran to my dad.” The task is to identify the changed sentences (which are often semantically broken).

When choosing from the existing probing suites, I considered that of [Tenney et al. \(2019a\)](#) as well. As the authors showed, their tasks and methods can effectively localise different types of linguistic knowledge in a Transformer model like BERT. However, the task data are not freely available, the tasks have a relatively narrow coverage with heavy focus on the most complex NLP tasks like entity recognition and natural language inference, and the probing is done on single-token representations. The suite of [Conneau et al.](#), on the other hand, is publicly available, better covers the easier tasks (surface and syntactic information), and examines whole-sentence representations. In the future, however, I expect the two probing suites to be combined and used frequently together, as they complement each other.

Chapter 4

Methods and Implementation

In this chapter, I re-iterate on the main objectives of this work, the approach I took, and go into detail in describing the design and implementation work underlying my experiments and analyses.

4.1 Methods and objectives

My main aim is to explore knowledge distillation by using it. In particular, I use it on three different NLP tasks (CoLA, SST-2, Sara) and with two different student architectures (a bi-directional LSTM student and a BERT student). I further analyse and compare the teacher and students on each task. I do not aim for beating someone else’s reported scores or for finding the best hyperparameter values for a model; I aim to learn more about knowledge distillation.

Because this work is heavily inspired by my internship at Rasa on *compressing BERT*¹, I aim to produce student models as small as possible. Therefore, I take the approach of first fine-tuning a teacher model and then distilling only the fine-tuned knowledge into tiny students (see the discussion back in [Section 2.3.2](#)).

The most technical and time-demanding part of my work is setting up the system’s implementation and using knowledge distillation to create small yet well-performing students for further analysis. Naturally, this involves optimisation of the student models’ hyperparameters to make the students perform at least somewhat comparably with today’s models like BERT. (There is little point in trying to get insights by analysing models that perform poorly in the first place.) However, I try to carry out only the essential optimisation, ending up with *a* well-performing student instead of *the* best one possible.

In order to reasonably constrain the amount of time and work put into optimisation of students’ hyper-parameters, I carry out a more thorough parameter exploration only on the CoLA task. Subsequently, I use the best found student

¹See blog.rasa.com/compressing-bert-for-faster-prediction-2/ and blog.rasa.com/pruning-bert-to-accelerate-inference/, accessed April 4, 2020.

parameters on the other two tasks, only adapting the most essential parameters – like the student model size – on each task separately.

Only once good students are trained, the key part of this work begins. I analyse what the students learnt well and what they did not, how they differ from their teacher and from each other. Where possible, I try to generalise across the three datasets. However, some findings are simply specific to a particular downstream task, and each task can provide different insights.

As the first step of the analysis, I probe all models. This is relatively straightforward and produces clear, quantitative results. (Indeed, it may not be easy to draw clear conclusions from the results.)

As the second step, I carry out a (mostly qualitative) analysis of the models’ predictions on concrete sentences. This analysis is much more time-consuming and is not widely used. However, I still believe that it can provide some useful insights. In particular, I look at predictions both through correctness – e.g. manually analysing sentences which were classified correctly by one model but not by another – and through confidence – which models are more confident, on what sentences are they (un)confident, how this relates to their (in)correctness...

Finally, I try to combine the probing and prediction analysis results into overall conclusions, seeing whether the two methods agree or disagree with each other and whether they help to describe the same or different aspects of the models and of knowledge distillation.

Because of the unavailability of test labels in CoLA and SST-2, I carry out the prediction analysis on all three tasks on the evaluation sentences. This can be understood as shedding light on the model qualities being optimised when one tunes a model’s hyper-parameters on the evaluation portion. Another option would be to carry out the analysis on a held-out set not used in training.

4.2 System overview and adapted implementations

Because a lot of research around Transformers is open-sourced, I make use of existing works and implementations. Fig. 4.1 shows the high-level pipeline of my work. It is inspired by the best pipeline of Tang et al. (2019a), with the exception that they only used the recurrent bi-directional LSTM (BiLSTM) student and did not carry out probing or prediction analysis.

For most of my implementation, I use the `transformers` open-source PyTorch library (Wolf et al., 2019)², which provides tools for working with pre-trained Transformers like BERT. For knowledge distillation, I adapt the code of Sanh et al. (2019), which is today also part of `transformers`³. (Note that they do

²github.com/huggingface/transformers, accessed April 4, 2020

³github.com/huggingface/transformers/tree/master/examples/distillation, accessed April 4, 2020

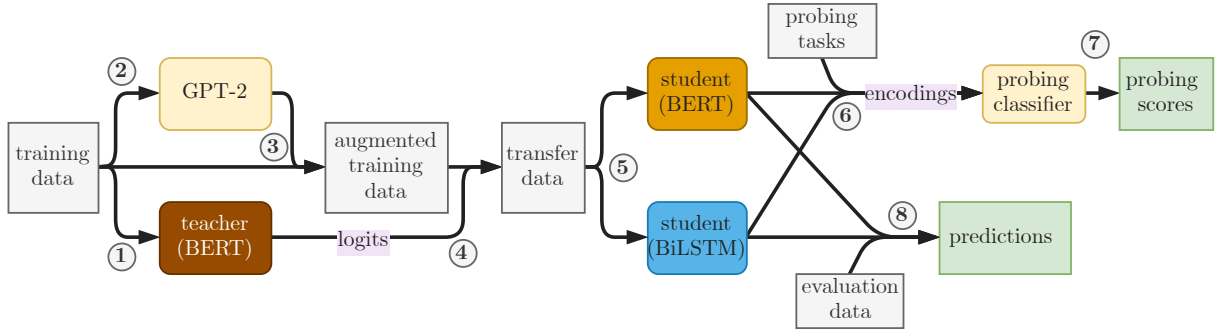


Figure 4.1. The main pipeline of this work: ① teacher fine-tuning, ② GPT-2 fine-tuning, ③ generating augmentation sentences, ④ adding teacher logits to the augmented training dataset, ⑤ knowledge distillation into students, ⑥ producing probing sentence encodings, ⑦ training the probing classifier and producing probing scores, ⑧ producing predictions on evaluation sentences.

knowledge distillation *before* downstream fine-tuning.) For augmenting the training data using GPT-2 and for knowledge distillation with the BiLSTM student, I adapt the code of Tang et al.⁴, which uses an early version of `transformers`. For probing the two students, I use the SentEval framework (Conneau and Kiela, 2018)⁵.

In terms of implementation, the most of my own work lies in adapting and integrating the different codebases into one, and in adding the possibility for optimising various student parameters (see the next section). I also make the code more general compared to the original codebases, which in many cases contained hard-coded decisions relating to the respective studies (be it Sanh et al. or Tang et al.). The core of my implementation can be found in my forked version of `transformers` at github.com/samsucik/pytorch-transformers/, with code for running experiment and analyses, as well as results and reporting, found in the project-specific repository at github.com/samsucik/knowledge-distil-bert.

4.3 Implementation details

Following Tang et al. (2019a), I use the case-insensitive pre-trained BERT_{Large} (340 million parameters) as the teacher. From now, I will refer to this model as BERT_T. The large BERT generally performs better than the 110-million-parameter BERT_{Base} variant and is therefore more desirable, but also slower, with a greater incentive for compression (in this case using knowledge distillation). For teacher fine-tuning on each downstream task, I also use the procedure of Tang et al.: 3-epoch training with batch size $B = 36$ on the training set, using the cross-entropy loss and the Adam optimizer with $\eta = 5 \times 10^{-5}$ and the usual β values ($\beta_1 = 0.9$, $\beta_2 = 0.999$). The learning rate η was linearly “warmed up” (annealed

⁴github.com/castorini/d-bert, accessed April 4, 2020

⁵github.com/facebookresearch/SentEval

from 0 to the target value) over the first 10% of the total training steps, and decayed linearly to 0 over the remaining steps. Somewhat surprisingly, while the performance of BERT_T converged (plateaued) within the 3-epoch budget on CoLA and SST-2 (as measured by the task-relevant metric on the evaluation set), the convergence was much slower for Sara. Hence, I empirically found a more suitable number of epochs within which the teacher would converge on Sara: 10.

TO-DO: add dev score plots

In fine-tuning the GPT-2 model, I again repeat the procedure of Tang et al.. In particular, the model is trained over 1 epoch using the cross-entropy loss, the AdamW learning algorithm (Adam with weight decay, see Loshchilov and Hutter (2019)) with learning rate $\eta = 5 \times 10^{-5}$, weight decay $\lambda = 1 \times 10^{-3}$, and the usual β values. The same linear scheduling is used as the one for fine-tuning BERT_T. The only parameter I choose differently from Tang et al. is the batch size B : They used batches of 48 whereas I use smaller batches of 16 examples to make the fine-tuning possible with my limited memory resource. **TO-DO: report the bpc or other scores**

As the first student, I use the bi-directional LSTM from Tang et al., comprising one hidden LSTM layer with 300 units. The last hidden states for either of the two processing directions are concatenated and passed to a fully connected layer with output 400 units⁶, the ReLU activation function and dropout. A final (linear) layer follows, projecting to the number of target classes, i.e. producing the logits. The model is topped with a softmax classifier for normalising the logits. **TO-DO: add a diagram** The original model was built to process sentences word by word, encoding each word using the pre-trained word2vec embeddings⁷ before passing it to the LSTM layer. Words for which there is no embedding (*out-of-vocabulary* (OOV) words) are embedded using a vector initialised with random numbers drawn uniformly from $[-0.25, 0.25]$. The embedding layer supports three *embedding modes*, based on Kim (2014):

1. **Static**: the embedding parameters are frozen and do not change during training.
2. **Non-static**: the embedding parameters are allowed to be further changed (fine-tuned) during training.
3. **Multichannel**: two embedding instances are used in parallel, one is frozen, the other one is allowed to be fine-tuned. For each input word, the two embeddings produced are concatenated together for further processing. The multichannel mode is the one used by Tang et al..

One significant change I made to this model is enabling the use of wordpiece embeddings (instead of word-level ones). This way, the fine-tuned embedding layer from BERT_T can be plugged into the student, giving it some of the teacher's

⁶Even though Tang et al. tried also other, slightly different layer dimensions, these are the ones that worked the best on CoLA.

⁷The 300-dimensional version trained on Google News, see code.google.com/archive/p/word2vec/.

knowledge even before knowledge distillation begins. In total, this model – from now referred to as $LSTM_S$ – has 2.41 million trainable parameters (excluding the embedding layer), making it 140x smaller than $BERT_T$.

For the second student, I use a smaller version of the teacher BERT model, with all dimensions down-scaled 5x to roughly match the number of trainable non-embedding parameters: with 5 transformer layers, hidden dimension of 204, intermediate layers of size 750, and 3 attentional heads (amounting to 2.42M parameters). I will refer to this model as $BERT_S$.

$LSTM_S$ was trained to minimise the mean squared loss (MSE) between the teacher-generated logits and student’s logits. While the cross-entropy loss with configurable temperature is more popular and in essence a generalisation of the MSE loss (see [Hinton et al. \(2015\)](#)), [Tang et al. \(2019a\)](#) report that the MSE loss led to slightly better performance in their experiments. For $BERT_S$, I use the traditional cross-entropy loss with temperature set to $T = 3$ following the findings of [Tsai et al. \(2019\)](#) who experimented with different temperatures (note that $T = 3$ was used as the default also in the experiments of [Tang et al. \(2019a\)](#)).

Following preliminary experiments, I limited the number of training epochs to 30 for $LSTM_S$ (same budget was used by [Tang et al. \(2019a\)](#)) and to 60 for $BERT_S$ as it was converging much slower than the recurrent student. I stick to this training budget throughout my experiments.

As for the probing classifier that [Conneau et al.](#) propose to use with their probing suite, it is a simple neural network with one hidden layer with the sigmoid activation function and dropout, followed by a linear layer projecting to the desired number of classes. The cross-entropy training loss is used, with the Adam learning algorithm with $\eta = 0.001$, $\beta_1 = 0.9$ and $\beta_2 = 0.999$. Training uses minibatches of 64 examples and uses early stopping for when the accuracy does not improve over 5 consecutive iterations. For consistency with the exact method of [Conneau et al.](#), I tune the dropout rate (choosing from [0.0, 0.1, 0.2]) and the hidden layer width (choosing from [50, 100, 200]) using the evaluation set.

4.4 Computing environment

Chapter 5

Student tuning

Importantly, extensive tuning of the students' hyperparameters is certainly not the main objective of this work. However, my aim is to carry out an analysis of the teacher and student models and the distillation process. For such analysis to be of some value, it should be done using well-performing models which themselves are of practical value.

I tune a number of hyperparameters for the 2.4M-parameter students using the CoLA task. Afterwards, I tune a smaller number of parameters – which are the most likely to be task-dependent – separately for each downstream task, trying to obtain $LSTM_S$ and $BERT_S$ that would achieve 90% of the teacher's performance while being as small as possible. These student are then used for further analysis.

For both students, I first tune the following, in this order (for more details, see the next sections):

1. learning rate η
2. learning rate scheduling, more concretely the warm-up and decay of η
3. batch size B
4. embedding type (wordpiece vs word) and mode

Afterwards, I tune on each task separately the embedding type and the student size.

The starting configuration (which I change as I tune the different parameters) is:

- $BERT_S$: Adam with $\eta = 5e - 5$, $B = 256$, learning rate warm-up over the first 10 epochs, followed by linear decay, and wordpiece embedding layer
- $LSTM_S$: Adadelata with $\eta = 1.0$, $B = 50$, no learning rate annealing, and word embedding layer in the multichannel mode, using word2vec

Initially, $LSTM_S$ had its embedding layer initialised with word2vec embeddings, but $BERT_S$ was initialised entirely from scratch. Naturally, this was posing a disadvantage for $BERT_S$ as it was starting with no knowledge. Hence, I added

the option to initialise the embedding layer with wordpiece embeddings from the corresponding finetuned $BERT_T$. I report results of parameter tuning for both of these variants of $BERT_S$.

5.1 Choosing η

Because [Tang et al. \(2019a\)](#) report not tuning their hyperparameters, I acknowledge their parameter choices but challenge many of them. In particular, they use Adadelata with $\eta = 1.0$ and $\rho = 0.95$ as the learning algorithm. I attempt to use the Adam algorithm as it is a generalised, improved version of Adadelata. Hence, for both students, I compare values of η from $[5e-3, 1.5e-3, 5e-4, 1.5e-4, 5e-5, 1.5e-5, 5e-6]$ for the Adam optimizer, with betas fixed to 0.9 and 0.98.

TO-DO: add graphs

The best value was found to be $\eta = 5e-4$ for $LSTM_S$ and bth variants of $BERT_S$. For $BLSTM_S$, I abandoned the Adadelata optimizer as it performed worse than Adam.

5.2 Choosing learning rate annealing

I tried linear warm-up of η (starting from 0) over $[0, 5, 10, 15, 20]$ epochs E_{WP} for $BERT_S$ and over $[0, 5, 10, 15]$ epochs for $LSTM_S$.

TO-DO: add graphs

For $BERT_S$ initialised from scratch, $E_{WP} = 20$ and no decay worked the best. For the other students, decay was improving the performance slightly, with the best E_{WP} being 0 for $LSTM_S$ and 15 for $BERT_S$.

5.3 Choosing batch size

Note that for $LSTM_S$ this was done prior to exploring the learnign rate annealing, as my aim was to merely verify that $B = 50$ reported by [Tang et al. \(2019a\)](#) was the best value. For $BERT_S$, I had much less intuition about suitable batch sizes. The explored values were $[32, 64, 128, 256, 512]$ for $BERT_S$ and $[32, 50, 128, 256, 512]$ for $LSTM_S$.

TO-DO: add graphs

Interestingly, while $LSTM_S$ preferred the smalles batch size $B = 32$, $BERT_S$ preferred much bigger batches: 256 when initialised from scratch and 128 with wordpiece embeddings initialised from $BERT_T$.

5.4 Choosing embedding type and mode

After observing that the best $LSTM_S$ consistently outperforms its counterpart $BERT_S$, I turned to exploring the effect of pre-trained knowledge present in the student before distillation. In $LSTM_S$, this lies in the word2vec embeddings. Additionally, the embedding layer is used in the *multichannel mode*: two parallel embedding layers are initialised from word2vec, with one being frozen during distillation and the other one allowed to be finetuned. In $BERT_S$, there is no pre-trained knowledge or there is the knowledge from the teacher’s wordpiece embeddings (dimensionality reduced by a trainable linear layer to match the smaller hidden size of $BERT_S$).

I was interested to see whether the effect of different type of embeddings – word2vec pre-trained on general language modelling vs wordpiece pre-trained on language modelling and finetuned on the particular downstream task – could explain some of the performance gap between $BERT_S$ and $LSTM_S$. Hence, I tried each of the 2 students with each of the 2 embedding types, combined with each of the following 2 modes: the multichannel mode described above, and the simple (*non-static*) mode where only one embedding instance is created, which is unfrozen and allowed to further train during distillation.

TO-DO: add graphs

Turns out $LSTM_S$ strongly prefers word embeddings in the multichannel mode, while $BERT_S$ is less decisive, with only slight preference for word embeddings and the multichannel mode. This also shows that the different embedding properties don’t explain the worse performance of $BERT_S$.

5.5 Choosing task-specific parameters

For each dataset, I first tried different embedding types and modes, and then for the best-performing combination I tried up-scaling the students to get as close to 90% of $BERT_T$ ’s performance as possible, while keeping the size of each student reasonably smaller than the teacher.

5.5.1 CoLA

Here I had the optimal embedding type/mode already.

I tried expanding $LSTM_S$ by increasing the number of LSTM layers from 1 to [2, 3, 4, 5] and the width of the LSTM and fully-connected layers from the original 300 and 400 by 2x, 3x, 4x and 5x. In case of $BERT_S$, I tried increasing the number of layers from the original 5 to 10 and 15, and the other parameters (# of attentional heads, hidden and intermediate size) by 2x, 3x and 4x.

TO-DO: add graphs

For $LSTM_S$, the results are indecisive, without clear correlation between student size and performance. The best student was 2x deeper and 2x wider than the initial configuration.

For $BERT_S$, I soon observed that bigger models started dying after the first few epochs. TO-DO: add diagnostic graphs. This dying surfaced as the dev-set score flattening out and then decreasing towards 0, at which point the gradients in the model would explode. I identified the cause of this to be too big learning rate (thanks to the warm-up, the model was experiencing η starting from 0 and increasing towards the target value). Hence, by comparing the graphs for the linearly increasing η and the dev-set performance, I tried to manually identify η values as big as possible that were still enabling the model to improve fast (without making it plateau or die). These values were in the range from the originally chosen $5e-4$ down to $8e-5$ (generally lower η for bigger models). After this modification, all students trained normally, without dying. TO-DO: add graphs and conclusions once all of these have finished training.

5.5.2 SST-2

TO-DO: run experiments and report

5.5.3 Sara

TO-DO: run experiments and report

Chapter 6

Analysing the models

6.1 Analysing the models' predictions

This will involve for each downstream task:

1. gathering dev-set predictions made by the two best students and the teacher
2. looking at the mistakes made by each model (most confident mistakes and least confident mistakes first, maybe taking first 10-20 mistakes from each end), trying to describe them in intuitive terms if possible
3. comparing the mistakes made by different models, again trying to describe what I observe
4. looking at how confident the predictions were in general for each model (maybe the distribution of confidences?) and if possible, comparing this across models

My aim is to make at least some observations describable in human-understandable terms about how the models compare: how the 2 architecturally different students compare, and how their predicting behaviour compares to that of their teacher. Ideally, I will be also able to form some (even if weak) hypotheses that are further testable using probing tasks.

6.2 Probing the models for linguistic knowledge

Here, I will for each downstream task:

- probe each of the 3 models in different layers (e.g. the 24-layer $BERT_T$ in layers 1, 6, 12, 18, 24) to see how much linguistic knowledge and where is present in each model
- probe also the pre-trained BERT (not finetuned on any downstream task) and look at how knowledge is preserved/thrown away when the teacher gets

finetuned vs when students with little prior knowledge are trained during distillation

- compare how knowledge is present in the two architecturally different students, try to relate this to other differences noticed when analysing the students' predictions

For now, I have one graph summarising the results of probing just the teacher models, see [Fig. 6.1](#).

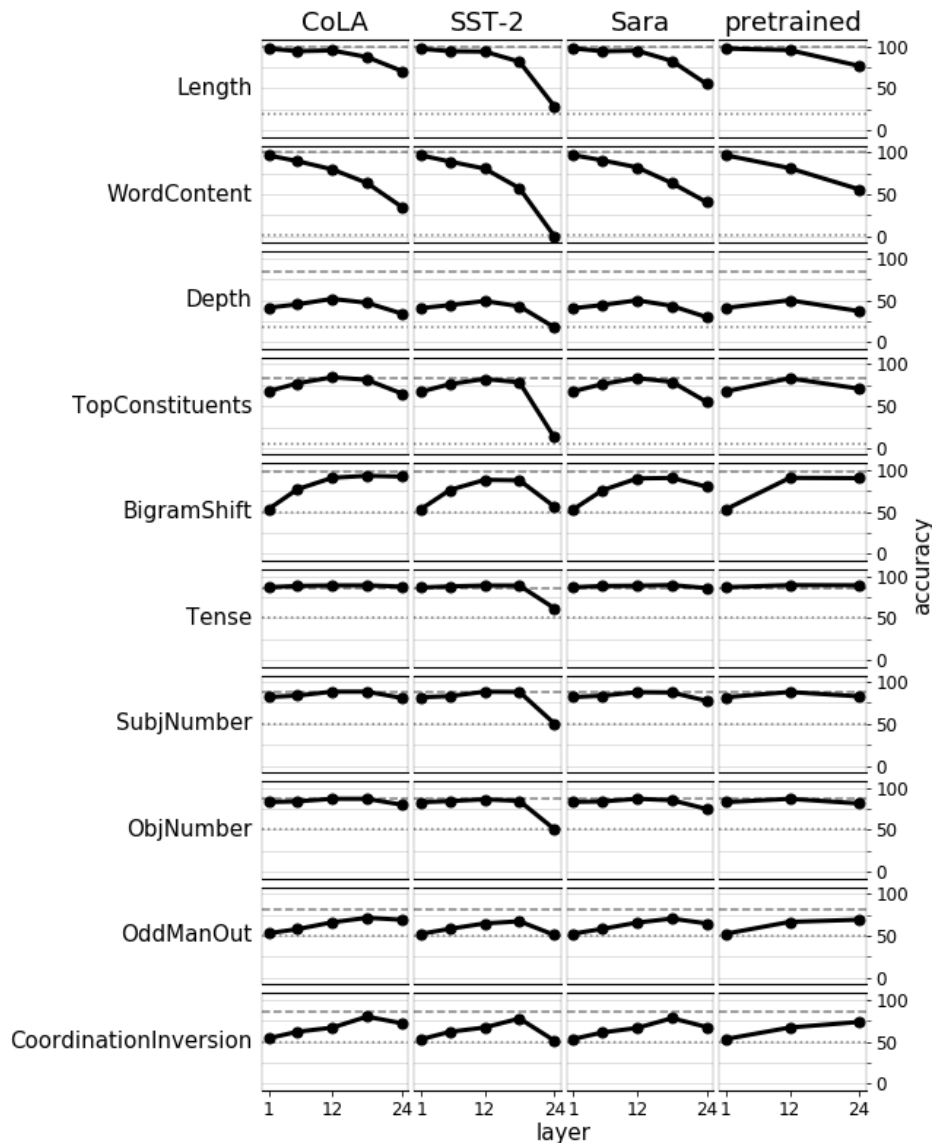


Figure 6.1. Probing the 3 finetuned teachers and the pre-trained one. The dotted line shows baseline accuracy levels achieved by majority-class guessing, the dashed line shows human performance.

Chapter 7

Overall discussion and conclusions

Chapter 8

Future work

Chapter 9

Plan for the rest of the semester

Work finished:

- implementing everything related to distillation (incl. teacher finetuning and generating augmentation data with GPT-2)
- creating augmented transfer sets and finetuning the BERT teacher for each task
- exploring the model parameters shared across tasks (i.e. doesn't include embedding type and student size)
- implementing everything needed for probing
- implementing everything needed for gathering predictions for mistake/confidence analysis

Work to be done:

- now-Feb 10: finishing size exploration for SST-2 and Sara (ending up with best students for each downstream task)
- Feb 11-23: analysing the predictions of all models (includes Inovative Learning Week Feb 17-21 when I won't get terribly much done)
- Feb 11-16: probing the best students
- Feb 24-Mar 1: putting together overall analysis and conclusions
- Mar 2-Apr 2: buffer time and writing the report (a lot of coursework in this period as well)

Bibliography

- Adhikari, A., Ram, A., Tang, R., and Lin, J. (2019). DocBERT: BERT for document classification.
- Adi, Y., Kermany, E., Belinkov, Y., Lavi, O., and Goldberg, Y. (2017). Fine-grained analysis of sentence embeddings using auxiliary prediction tasks. *ICLR*, abs/1608.04207.
- Ba, J. and Caruana, R. (2014). Do deep nets really need to be deep? In *NIPS*.
- Bahdanau, D., Cho, K., and Bengio, Y. (2014). Neural machine translation by jointly learning to align and translate.
- Belinkov, Y. and Glass, J. R. (2018). Analysis methods in neural language processing: A survey. *Transactions of the Association for Computational Linguistics*, 7:49–72.
- Bucila, C., Caruana, R., and Niculescu-Mizil, A. (2006). Model compression. In *KDD '06*.
- Cheong, R. and Daniel, R. (2019). transformers.zip: Compressing transformers with pruning and quantization.
- Collobert, R. and Weston, J. (2008). A unified architecture for natural language processing: Deep neural networks with multitask learning. In *Proceedings of the 25th International Conference on Machine Learning, ICML 2008*, page 160–167, New York, NY, USA. Association for Computing Machinery.
- Collobert, R., Weston, J., Bottou, L., Karlen, M., Kavukcuoglu, K., and Kuksa, P. (2011). Natural language processing (almost) from scratch. *J. Mach. Learn. Res.*, 12(null):2493–2537.
- Conneau, A. and Kiela, D. (2018). SentEval: An evaluation toolkit for universal sentence representations. *arXiv*, abs/1803.05449.
- Conneau, A., Kruszewski, G., Lample, G., Barrault, L., and Baroni, M. (2018). What you can cram into a single $\&\!*\&\!$ vector: Probing sentence embeddings for linguistic properties. In *ACL*.
- Dai, A. M. and Le, Q. V. (2015). Semi-supervised sequence learning. In Cortes, C., Lawrence, N. D., Lee, D. D., Sugiyama, M., and Garnett, R., editors, *Ad-*

- vances in Neural Information Processing Systems 28*, pages 3079–3087. Curran Associates, Inc.
- Dai, Z., Yang, Z., Yang, Y., Carbonell, J. G., Le, Q. V., and Salakhutdinov, R. (2019). Transformer-XL: Attentive language models beyond a fixed-length context. In *ACL*.
- Devlin, J., Chang, M.-W., Lee, K., and Toutanova, K. (2018). BERT: Pre-training of deep bidirectional transformers for language understanding.
- Gilpin, L. H., Bau, D., Yuan, B. Z., Bajwa, A., Specter, M., and Kagal, L. (2018). Explaining explanations: An overview of interpretability of machine learning.
- Graves, A. (2013). Generating sequences with recurrent neural networks.
- Hinton, G. E., Vinyals, O., and Dean, J. (2015). Distilling the knowledge in a neural network. *ArXiv*, abs/1503.02531.
- Hochreiter, S. and Schmidhuber, J. (1997). Long short-term memory. *Neural Comput.*, 9(8):1735–1780.
- Huang, Z. and Wang, N. (2017). Like what you like: Knowledge distill via neuron selectivity transfer. *arXiv*, abs/1707.01219.
- Jiao, X., Yin, Y., Shang, L., Jiang, X., Chen, X., Li, L., Wang, F., and Liu, Q. (2019). TinyBERT: Distilling BERT for natural language understanding.
- Kalchbrenner, N. and Blunsom, P. (2013). Recurrent continuous translation models. In *Proceedings of the 2013 Conference on Empirical Methods in Natural Language Processing*, pages 1700–1709.
- Kim, Y. (2014). Convolutional neural networks for sentence classification. In *Proceedings of the 2014 Conference on Empirical Methods in Natural Language Processing (EMNLP)*, pages 1746–1751, Doha, Qatar. Association for Computational Linguistics.
- Kim, Y. and Rush, A. M. (2016). Sequence-level knowledge distillation. *arXiv*, abs/1606.07947.
- Krizhevsky, A., Sutskever, I., and Hinton, G. E. (2012). ImageNet classification with deep convolutional neural networks. In *NIPS*.
- Lample, G. and Conneau, A. (2019). Cross-lingual language model pretraining. *arXiv preprint arXiv:1901.07291*.
- Lee, J., Yoon, W., Kim, S., Kim, D., Kim, S., So, C. H., and Kang, J. (2019). BioBERT: a pre-trained biomedical language representation model for biomedical text mining. *Bioinformatics*.
- Loshchilov, I. and Hutter, F. (2019). Decoupled weight decay regularization. In *ICLR*.
- Luong, T., Pham, H., and Manning, C. D. (2015). Effective approaches to attention-based neural machine translation. In *Proceedings of the 2015 Confer-*

- ence on *Empirical Methods in Natural Language Processing*, pages 1412–1421, Lisbon, Portugal. Association for Computational Linguistics.
- Matthews, B. W. (1975). Comparison of the predicted and observed secondary structure of T4 phage lysozyme. *Biochimica et Biophysica Acta (BBA)-Protein Structure*, 405(2):442–451.
- Michel, P., Levy, O., and Neubig, G. (2019). Are sixteen heads really better than one?
- Mikolov, T., Chen, K., Corrado, G., and Dean, J. (2013). Efficient estimation of word representations in vector space. In Bengio, Y. and LeCun, Y., editors, *1st International Conference on Learning Representations, ICLR 2013, Scottsdale, Arizona, USA, May 2-4, 2013, Workshop Track Proceedings*.
- Mikolov, T., Karafiát, M., Burget, L., Černocký, J., and Khudanpur, S. (2010). Recurrent neural network based language model. In *INTERSPEECH*.
- Mirzadeh, S., Farajtabar, M., Li, A., and Ghasemzadeh, H. (2019). Improved knowledge distillation via teacher assistant: Bridging the gap between student and teacher. *CoRR*, abs/1902.03393.
- Mukherjee, S. and Awadallah, A. H. (2019). Distilling transformers into simple neural networks with unlabeled transfer data.
- Papamakarios, G. (2015). Distilling model knowledge (MSc thesis). *arXiv*, abs/1510.02437v1.
- Pires, T., Schlinger, E., and Garrette, D. (2019). How multilingual is multilingual BERT?
- Radford, A., Narasimhan, K., Salimans, T., and Sutskever, I. (2018). Improving language understanding by generative pre-training. URL <https://s3-us-west-2.amazonaws.com/openai-assets/researchcovers/languageunsupervised/languageunderstandingpaper.pdf>.
- Radford, A., Wu, J., Child, R., Luan, D., Amodei, D., and Sutskever, I. (2019). Language models are unsupervised multitask learners. *OpenAI Blog*, 1(8):9.
- Romero, A., Ballas, N., Kahou, S. E., Chassang, A., Gatta, C., and Bengio, Y. (2015). FitNets: Hints for thin deep nets. In *In Proceedings of ICLR*.
- Rumelhart, D. E., Hinton, G. E., and Williams, R. J. (1986). *Learning Internal Representations by Error Propagation*, page 318–362. MIT Press, Cambridge, MA, USA.
- Sanh, V., Debut, L., Chaumond, J., and Wolf, T. (2019). DistilBERT, a distilled version of BERT: smaller, faster, cheaper and lighter. In *NeurIPS EMC² Workshop*.
- Sau, B. B. and Balasubramanian, V. N. (2016). Deep model compression: Distilling knowledge from noisy teachers. *arXiv*, abs/1610.09650.

- Shi, X., Padhi, I., and Knight, K. (2016). Does string-based neural MT learn source syntax? In *Proceedings of the 2016 Conference on Empirical Methods in Natural Language Processing*, pages 1526–1534, Austin, Texas. Association for Computational Linguistics.
- Simonyan, K., Vedaldi, A., and Zisserman, A. (2013). Deep inside convolutional networks: Visualising image classification models and saliency maps.
- Socher, R., Perelygin, A., Wu, J., Chuang, J., Manning, C. D., Ng, A. Y., and Potts, C. (2013). Recursive deep models for semantic compositionality over a sentiment treebank. In *EMNLP*.
- Strobelt, H., Gehrmann, S., Behrisch, M., Perer, A., Pfister, H., and Rush, A. M. (2018). Seq2seq-vis: A visual debugging tool for sequence-to-sequence models.
- Sucik, S. (2019). Pruning BERT to accelerate inference. <https://blog.rasa.com/pruning-bert-to-accelerate-inference/>.
- Sun, C., Myers, A., Vondrick, C., Murphy, K., and Schmid, C. (2019). VideoBERT: A joint model for video and language representation learning.
- Sutskever, I., Vinyals, O., and Le, Q. V. (2014). Sequence to sequence learning with neural networks. In *Advances in neural information processing systems*, pages 3104–3112.
- Tang, R., Lu, Y., and Lin, J. (2019a). Natural language generation for effective knowledge distillation. In *Proceedings of the 2nd Workshop on Deep Learning Approaches for Low-Resource NLP (DeepLo 2019)*, pages 202–208, Hong Kong, China. Association for Computational Linguistics.
- Tang, R., Lu, Y., Liu, L., Mou, L., Vechtomova, O., and Lin, J. (2019b). Distilling task-specific knowledge from BERT into simple neural networks. *arXiv*, abs/1903.12136.
- Tenney, I., Das, D., and Pavlick, E. (2019a). BERT rediscovers the classical NLP pipeline. In *ACL*.
- Tenney, I., Xia, P., Chen, B., Wang, A., Poliak, A., McCoy, R. T., Kim, N., Van Durme, B., Bowman, S., Das, D., et al. (2019b). What do you learn from context? probing for sentence structure in contextualized word representations. In *7th International Conference on Learning Representations, ICLR 2019*.
- Tsai, H., Riesa, J., Johnson, M., Arivazhagan, N., Li, X., and Archer, A. (2019). Small and practical BERT models for sequence labeling. In *EMNLP/IJCNLP*.
- Vaswani, A., Shazeer, N., Parmar, N., Uszkoreit, J., Jones, L., Gomez, A. N., Kaiser, L., and Polosukhin, I. (2017). Attention is all you need. In *Advances in neural information processing systems*, pages 5998–6008.
- Wang, A., Singh, A., Michael, J., Hill, F., Levy, O., and Bowman, S. (2018). GLUE: A multi-task benchmark and analysis platform for natural language understanding. In *Proceedings of the 2018 EMNLP Workshop BlackboxNLP*:

- Analyzing and Interpreting Neural Networks for NLP*, pages 353–355, Brussels, Belgium. Association for Computational Linguistics.
- Warstadt, A., Singh, A., and Bowman, S. R. (2018). Neural network acceptability judgments. *arXiv*, abs/1805.12471.
- Wolf, T., Debut, L., Sanh, V., Chaumond, J., Delangue, C., Moi, A., Cistac, P., Rault, T., Louf, R., Funtowicz, M., and Brew, J. (2019). HuggingFace’s Transformers: State-of-the-art natural language processing. *ArXiv*, abs/1910.03771.
- Wu, Y., Schuster, M., Chen, Z., Le, Q. V., Norouzi, M., Macherey, W., Krikun, M., Cao, Y., Gao, Q., Macherey, K., Klingner, J., Shah, A., Johnson, M., Liu, X., Łukasz Kaiser, Gouws, S., Kato, Y., Kudo, T., Kazawa, H., Stevens, K., Kurian, G., Patil, N., Wang, W., Young, C., Smith, J., Riesa, J., Rudnick, A., Vinyals, O., Corrado, G., Hughes, M., and Dean, J. (2016). Google’s neural machine translation system: Bridging the gap between human and machine translation.
- Yu, S., Kulkarni, N., Lee, H., and Kim, J. (2018). On-device neural language model based word prediction. In *Proceedings of the 27th International Conference on Computational Linguistics: System Demonstrations*, pages 128–131, Santa Fe, New Mexico. Association for Computational Linguistics.
- Zeiler, M. D. and Fergus, R. (2013). Visualizing and understanding convolutional networks.