MSiA-413 Introduction to Databases and Information Retrieval

Homework 1: Number representations

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Instructions

You should submit this homework assignment via Canvas. Acceptable formats are word files, text files, and pdf files. Paper submissions are not allowed and they will receive an automatic zero.

As explained during lecture and in the syllabus, assignments are done in groups. The groups have been created and assigned. Each group needs to submit only one assignment (i.e., there is no need for both partners to submit individually the same homework assignment).

Each group can submit solutions multiple times (for example, you may discover an error in your earlier submission and choose to submit a new solution set). We will grade only the last submission and ignore earlier ones.

Make sure you submit your solutions before the deadline. The policies governing academic integrity, tardiness and penalties are detailed in the syllabus.

Question 1. Unsigned Integer Representation (10 points – 1 point per row)

Please fill out the blank parts of the table below to (i) express the following numbers in binary, (ii) calculate their hexadecimal representation (as shown in class), and (iii) calculate their decimal value as a sum of powers of two.

For example: $52_{10} = 0011\ 0100_2 = 0x34 = 1*2^5 + 1*2^4 + 0*2^3 + 1*2^2 + 0*2^1 + 0*2^0 = 32 + 16 + 4$

	DECIMAL NUMBER	BINARY	HEXADECIMAL	SUM OF POWERS OF TWO
EXAMPLE	52	0011 0100	0x34	32 + 16 + 4
1A)	6	00000110	0x6	4 + 2 = 6
1B)	19	00010011	0x13	16 + 2 + 1 = 19
1C)	22	00010110	0x16	16 + 4 + 2 = 22
1D)	38	00100110	0x26	32 + 4 + 2 = 38
1E)	42	00101010	0x2A	32 + 8 + 2 = 42
1F)	155	10011011	0x9B	128 + 16 + 8 + 2 + 1 = 155
1G)	612	1001100100	0x264	512 + 64 + 32 + 4 = 612
1H)	1819	11100011011	0x71B	1024 + 512 + 256 + 16 + 8 + 2 + 1 = 1819
1I)	2293	100011110101	0x8F5	2048 + 128 + 64 + 32 + 16 + 4 + 1 = 2293
1J)	3176	110001101000	0xC68	2048 + 1024 + 64 + 32 + 8 = 3176

Question 2. Signed Integer Representation (10 points – 1 point per row)

Please fill out the blank parts of the table below as needed to calculate the 8-bit two's complement binary representation of the following signed decimal numbers. |x| denotes the absolute value of x. If particular number(s) below cannot be represented as 8-bit signed binary integer(s), please indicate which one(s) and explain why. The explanation will then carry the points of the corresponding row(s). Please remember that:

- You may need to add zeros to the left of the number to make it an 8-bit binary number.
- In two's complement signed integer representation, for every (positive or negative) integer x, it holds: -x = -x + 1, where -x is the complement of x (calculated by flipping the bits of x).
- If you don't need a column to calculate the 8-bit signed integer binary representation of a number, you can leave that column blank (as in example 1).

For example: $82_{10} = 0101 \ 0010_2$. Note that we added a zero at the front to make it an 8-bit binary number. The sign bit (most significant bit of its 8-bit binary representation) is 0, indicating a positive integer, so the 8-bit signed integer binary representation of 82_{10} is $0101 \ 0010_2$.

However, to calculate the 8-bit signed integer representation of -82 we need to calculate its two's complement. We have $|-82_{10}| = 82_{10} = 0101\ 0010_2$. Flipping the bits gives 1010 1101₂. Finally, adding one gives 1010 1110₂. Thus, the 8-bit signed binary representation of -82₁₀ is 1010 1110₂.

	VALUE OF	X	~ X	8-BIT SIGNED
	INTEGER	IN 8-BIT BINARY	IF NEEDED	INTEGER
	X			REPRESENTATION
EXAMPLE 1	82	$0101\ 0010 = 82_{10}$		$0101\ 0010 = 82_{10}$
EXAMPLE 2	-82	$0101\ 0010 = 82_{10}$	1010 1101	$1010\ 1110 = -82_{10}$
2A)	-1	0000 0001	1111 1110	$111111111 = -1_{10}$
2B)	-19	0001 0011	1110 1100	$1110\ 1101 = -19_{10}$
2C)	22	0001 0110		$00010110 = 22_{10}$
2D)	-38	0010 0110	1101 1001	$1101\ 1010 = -38_{10}$
2E)	-42	0010 1010	1101 0101	$1101\ 0110 = -42_{10}$
2F)	68	0100 0100		$01000100 = 68_{10}$
2G)	-100	0110 0100	1001 1011	$1001\ 1100 = -100_{10}$
2H)	127	0111 1111		$0111\ 1111 = 127_{10}$
2I)	128	-	-	-
2J)	-129	-	-	-

If you found any numbers that you cannot represent as 8-bit signed integers, indicate which ones and why they cannot be represented in the space below.

Question 3. Binary Pattern Representation (10 points)

BIT PATTERN 1

BIT PATTERN 2

What value does bit pattern 1 represent when interpreted as a

3a) (2 points) 32-bit signed integer in two's complement arithmetic?

-559038737

3b) (2 points) 32-bit <u>unsigned</u> integer?

3735928559

3c) (1 point) write the value in question 3b as a hexadecimal number

0xDEADBEEF

What value does bit pattern 2 represent when interpreted as a 3d) (2 points) 32-bit signed integer in two's complement arithmetic?

1280265249

3e) (2 points) 32-bit <u>unsigned</u> integer?

1280265249

3f) **(1 point)** UTF-8 text?

LOL!

Question 4. Accuracy of Integer and Floating Point Representations (20 points – 1 per row)

In the table below, answer "exactly," "approximately," or "no way" to indicate how the following (base ten) numbers can be represented as 32-bit signed integers, 64-bit signed integers, single precision (32-bit) floats, and double precision (64-bit) floats. If the number can be rounded to a value that is representable and the relative error is less than 10⁻³, then the best answer is "approximately." For example, I would say that 2.5 is "no way" 3, but 2.9999999 is "approximately" 3. The relative error definition is in the reading material and was explained in the lab session.

You can use online floating-point conversion tools (e.g., http://www.binaryconvert.com/convert_float.html).

BASE TEN NUMBER		32-BIT <i>SIGNED</i> INTEGER	64-BIT <i>SIGNED</i> INTEGER	32-BIT FLOATING POINT	64-BIT FLOATING POINT
EXAMPLE	1.0×10^{20}	no way	no way	approximately	exactly
4 A	-0.5	no way	no way	exactly	exactly
4B	1/3 (one third)	no way	no way	approximately	approximately
4C	0.1	no way	no way	approximately	approximately
4D	1/16 (one sixteenth)	no way	no way	exactly	exactly
4E	17.5	no way	no way	exactly	exactly
4F	4,000,000,000	no way	exactly	exactly	exactly
4 G	-4,000,000,001	no way	exactly	approximately	exactly
4H	$\sqrt{2}$	no way	no way	approximately	approximately
4I	2,000,000,000	exactly	exactly	exactly	exactly
4 J	2,000,000,001	exactly	exactly	approximately	exactly
4K	20,000,000	exactly	exactly	exactly	exactly
4L	20,000,000.25	approximately	approximately	approximately	exactly
4M	33,554,432.25	approximately	approximately	approximately	exactly
4N	33,554,432.9	approximately	approximately	approximately	approximately
4O	9,123,000,000,000,000,000	no way	exactly	approximately	exactly
4 P	-9,123,123,123,000,000,000	no way	exactly	approximately	approximately
4Q	9,123,123,123,123,123,123	no way	exactly	approximately	approximately
4R	pi	no way	no way	approximately	approximately
4S	infinity	no way	no way	exactly	exactly
4T	zero	exactly	exactly	exactly	exactly