



# DEEP LEARNING

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## Deep Neural Networks

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# Lecture Outline

1. DNN
2. DNN Design
3. TensorFlow

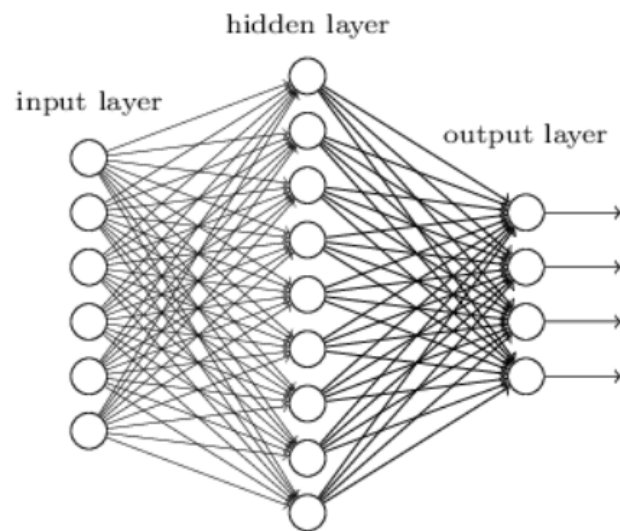
# DNN

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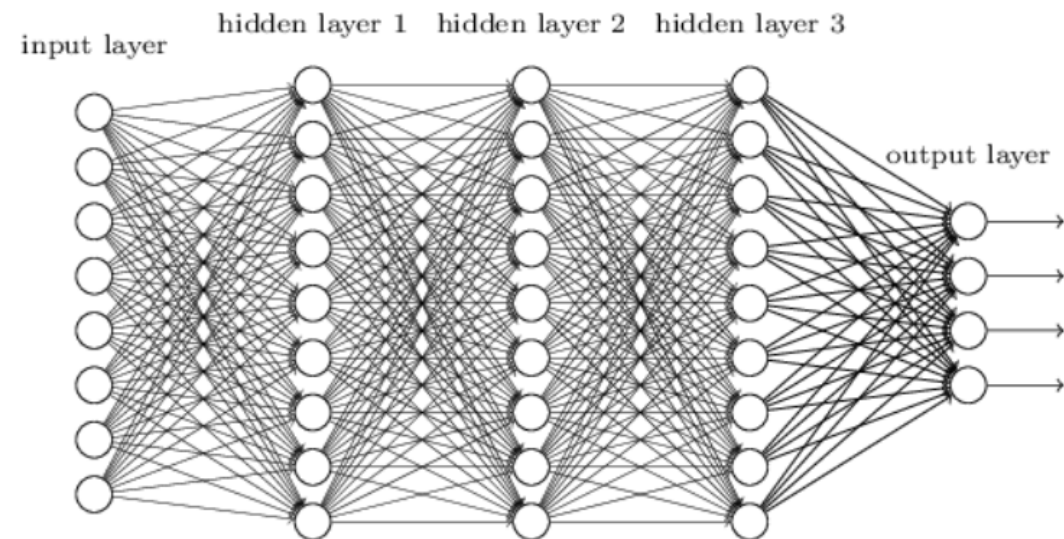
Deep Neural Networks

# Deep Neural Networks (DNNs)

- DNNs contain many more hidden layers or neurons in different configurations
- Known to generalize better on high dimensional data and cognitive problems



Artificial Neural Network



Deep Neural Network

# DNN Architectures

- FFN: Feed forward Network
- CNN : Convolutional Neural Networks
- RNN: Recurrent Neural Networks
- LSTM: Long Short-Term Memory
- DBN: Deep Belief Networks

# Benefits of Depth

- Highly nonlinear functions are even better function approximators
- Learning representations makes them highly flexible to various problems and domains
- Training can be parallelized using powerful multicore CPUs and GPUs

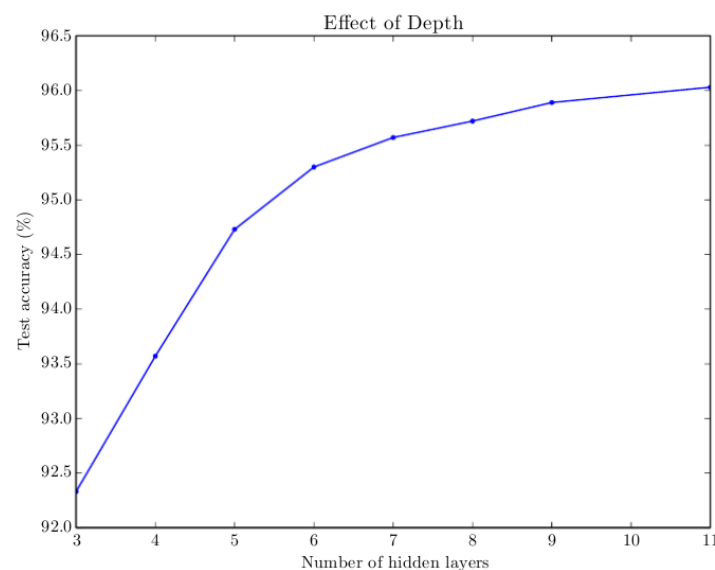
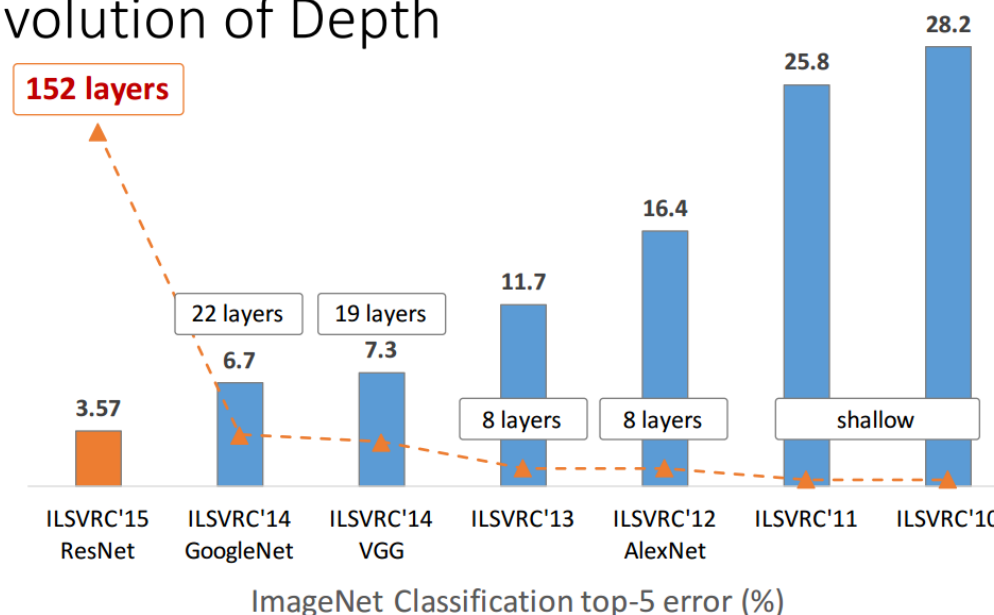


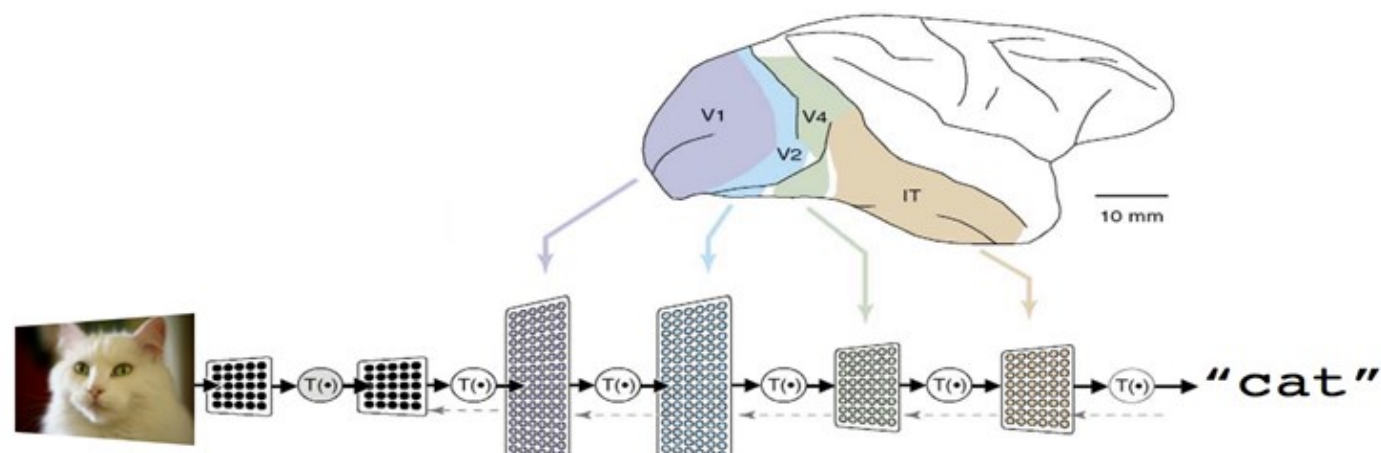
Figure 6.6: Empirical results showing that deeper networks generalize better when used to transcribe multi-digit numbers from photographs of addresses. Data from [Goodfellow et al. \(2014d\)](#). The test set accuracy consistently increases with increasing depth. See Fig. 6.7 for a control experiment demonstrating that other increases to the model size do not yield the same effect.

## Revolution of Depth



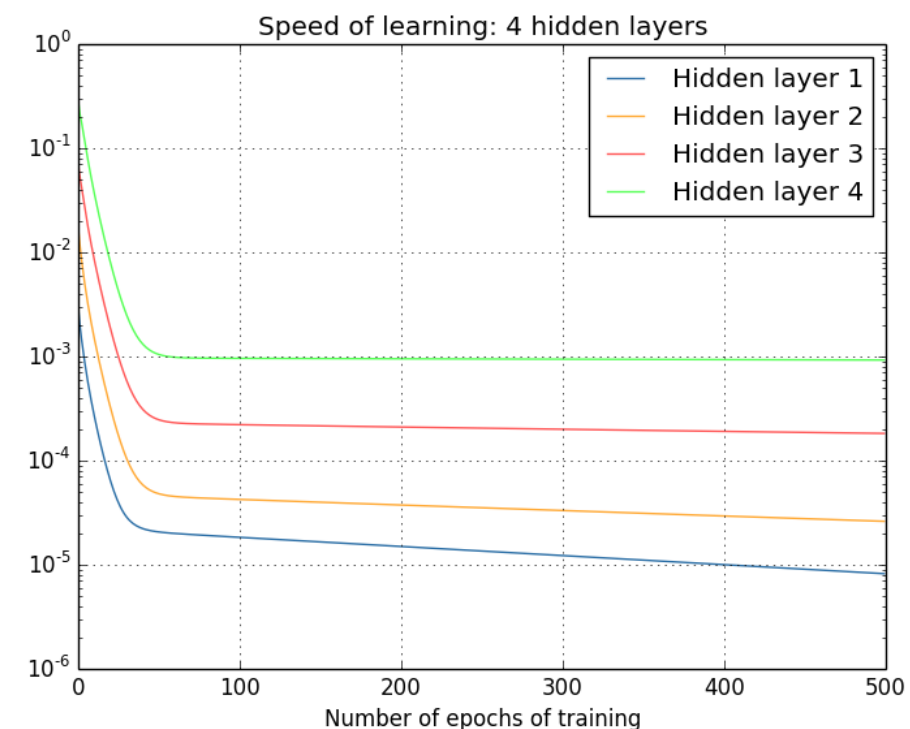
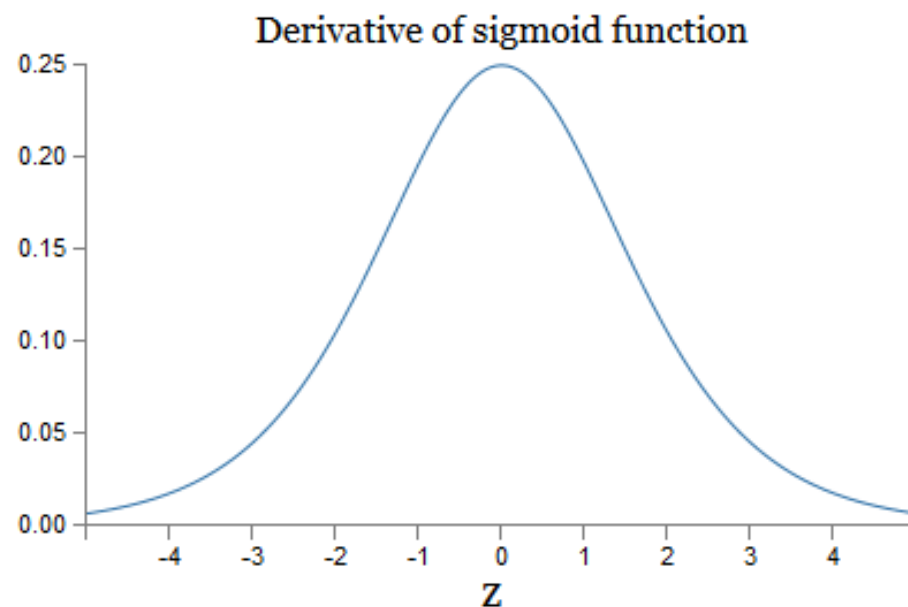
# DNN Challenges

- Significant compute and infrastructure requirements
- Vanishing and exploding gradients
- Long train and test times
- Requirement for big labelled datasets
- Black-box/opaque approach



# Vanishing and Exploding Gradients

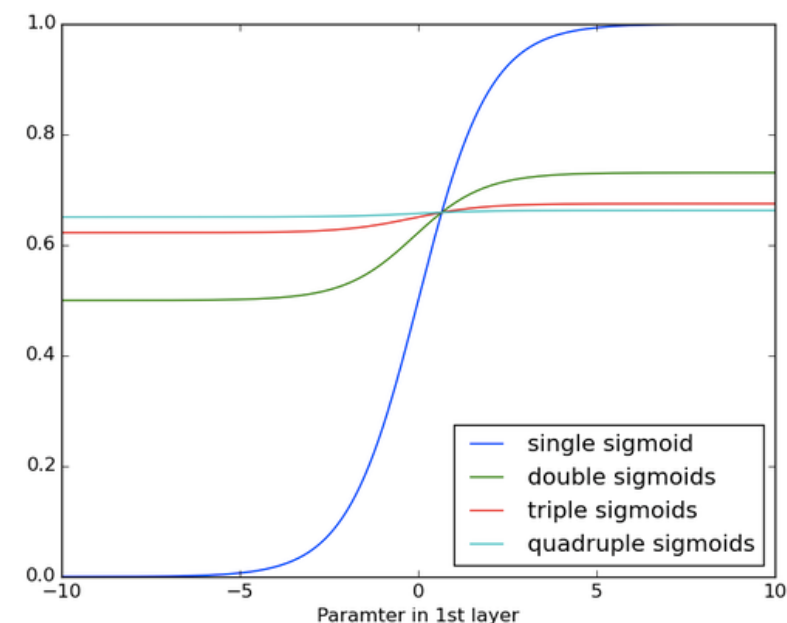
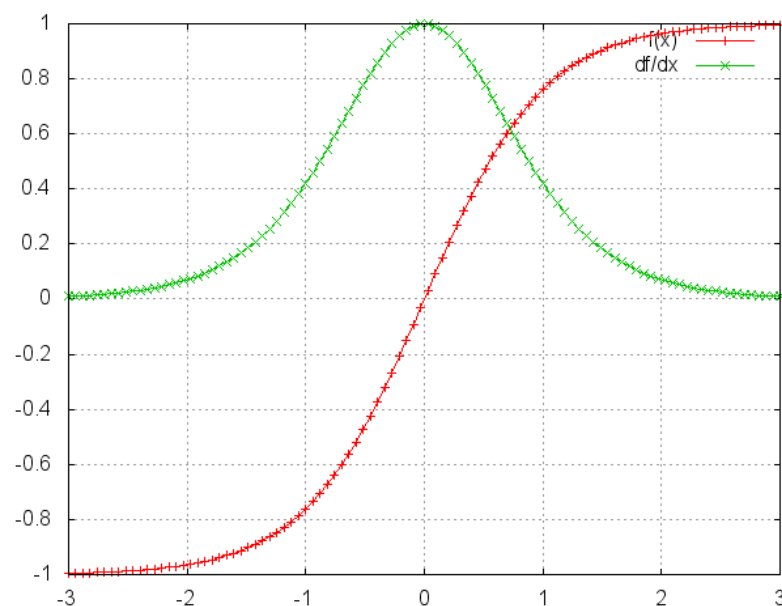
- Saturating nonlinearities (like tanh or sigmoid) can not be used for deep networks as they tend to get stuck in the saturation region as the network grows deeper





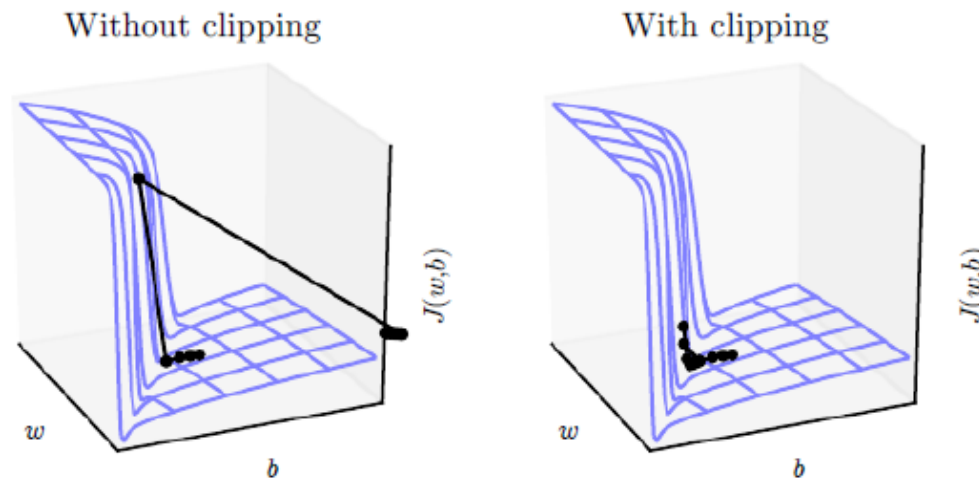
# Vanishing Gradients

- Gradients for the lower layers (closer to the input) can become very small. With small values in the matrix and multiple matrix multiplications, the gradient values shrink exponentially fast, eventually vanishing completely
- The ReLU activation function can help prevent vanishing gradients



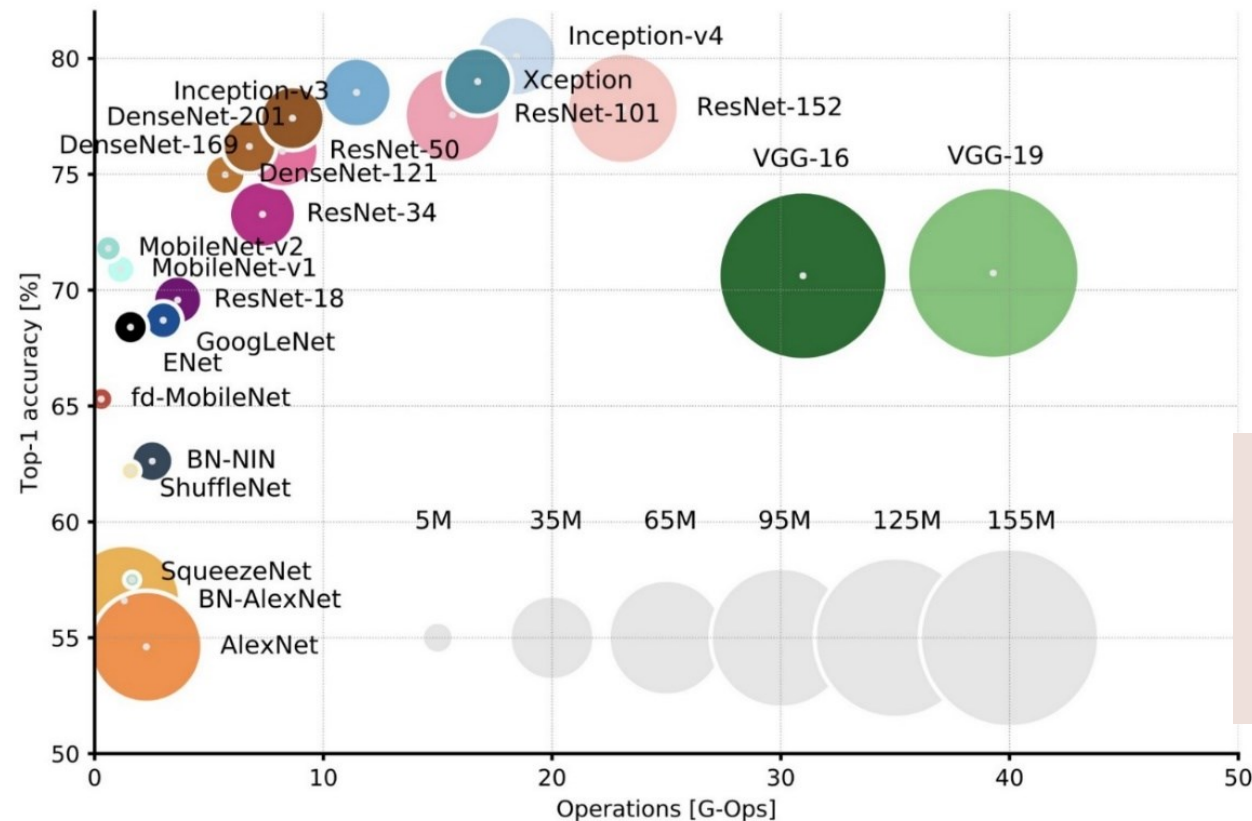
# Exploding Gradient

- Solved relatively easily because gradients can be truncated or squashed:
  - Gradient Clipping
  - Weight Regularization



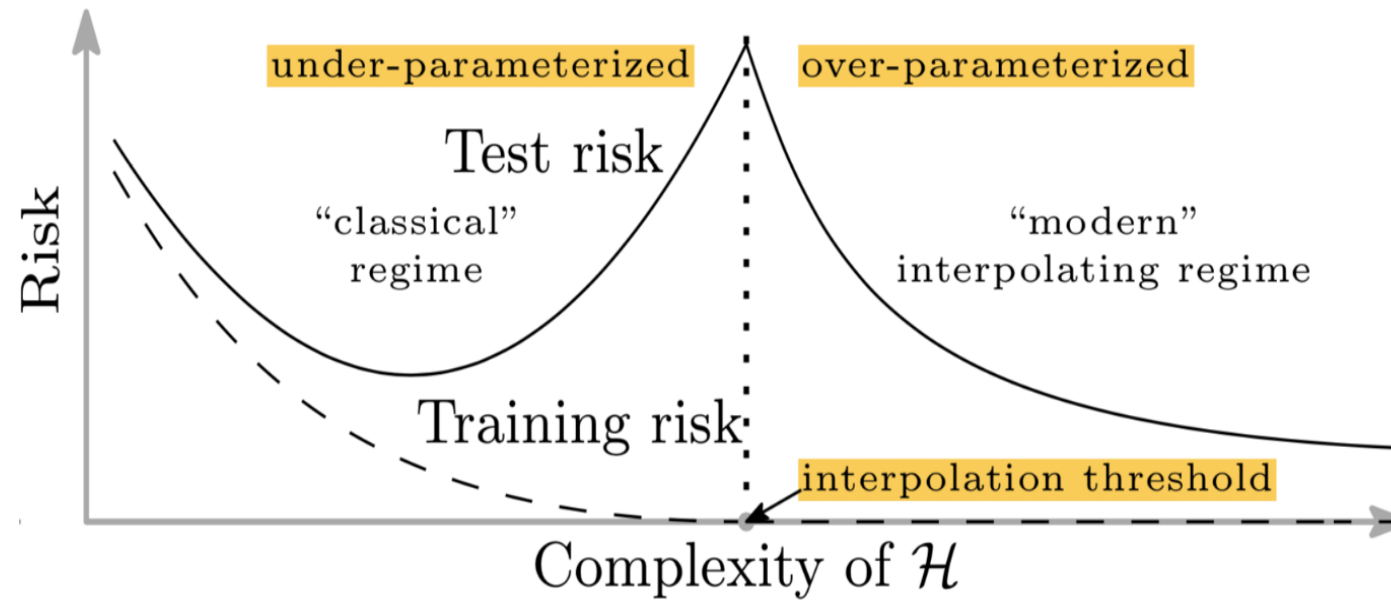
# Overparameterization

- Models where the number of parameters is significantly larger than the sample size
- Despite massive sizes, DNNs have exhibited remarkable generalization performance



Top-1 one-crop accuracy versus the number of operations required for a single forward pass. The size of the blobs is proportional to the number of network parameters

# Double Descent



“Double descent” risk curve that extends the traditional U-shaped bias-variance curve beyond the point of interpolation

<https://arxiv.org/abs/1812.11118>

<https://openai.com/research/deep-double-descent>

# DNN DESIGN

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Preprocessing, Regularization, Hyperparameters

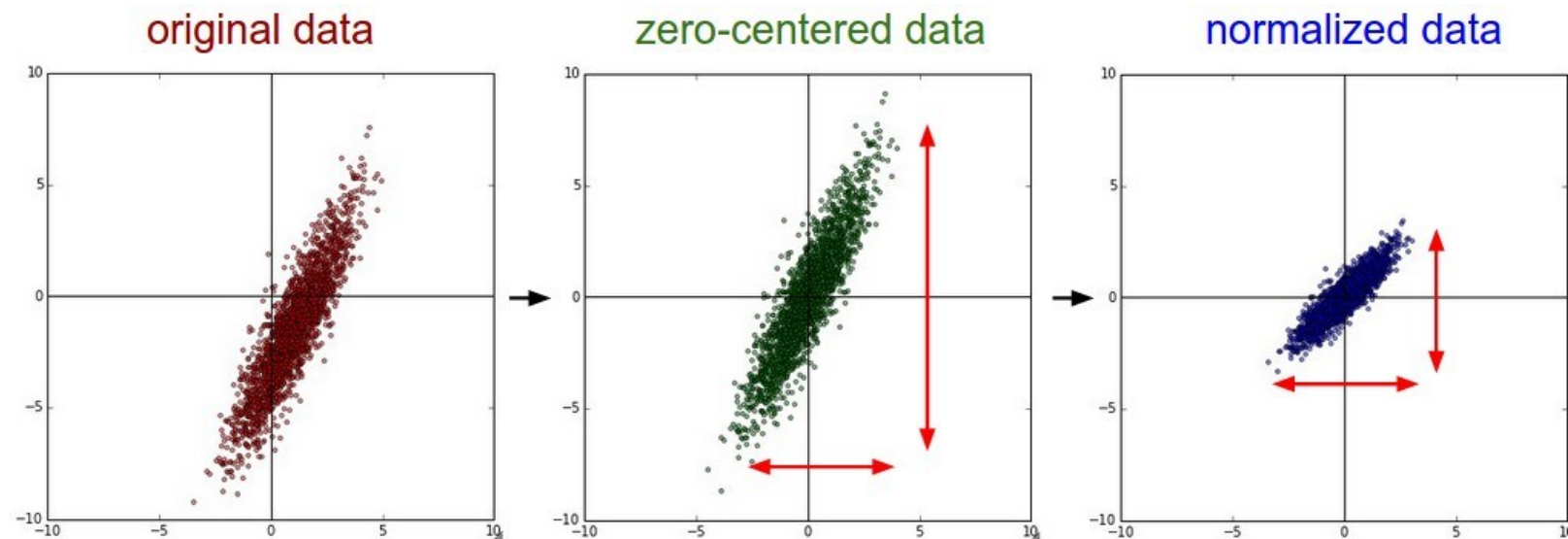
# Data Preprocessing: Normalization

- Mean subtraction - centering the data around origin

```
X -= np.mean(X, axis = 0)
```

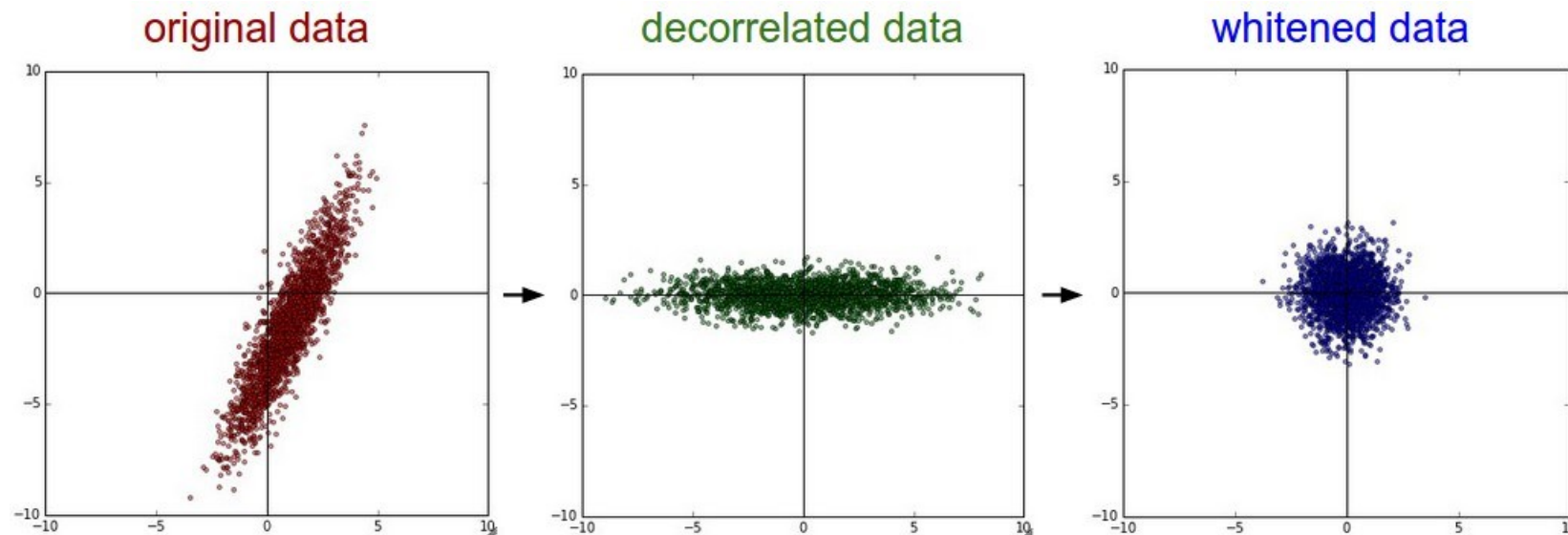
- Normalization - dimensions approximately at same scale

```
X /= np.std(X, axis = 0)
```



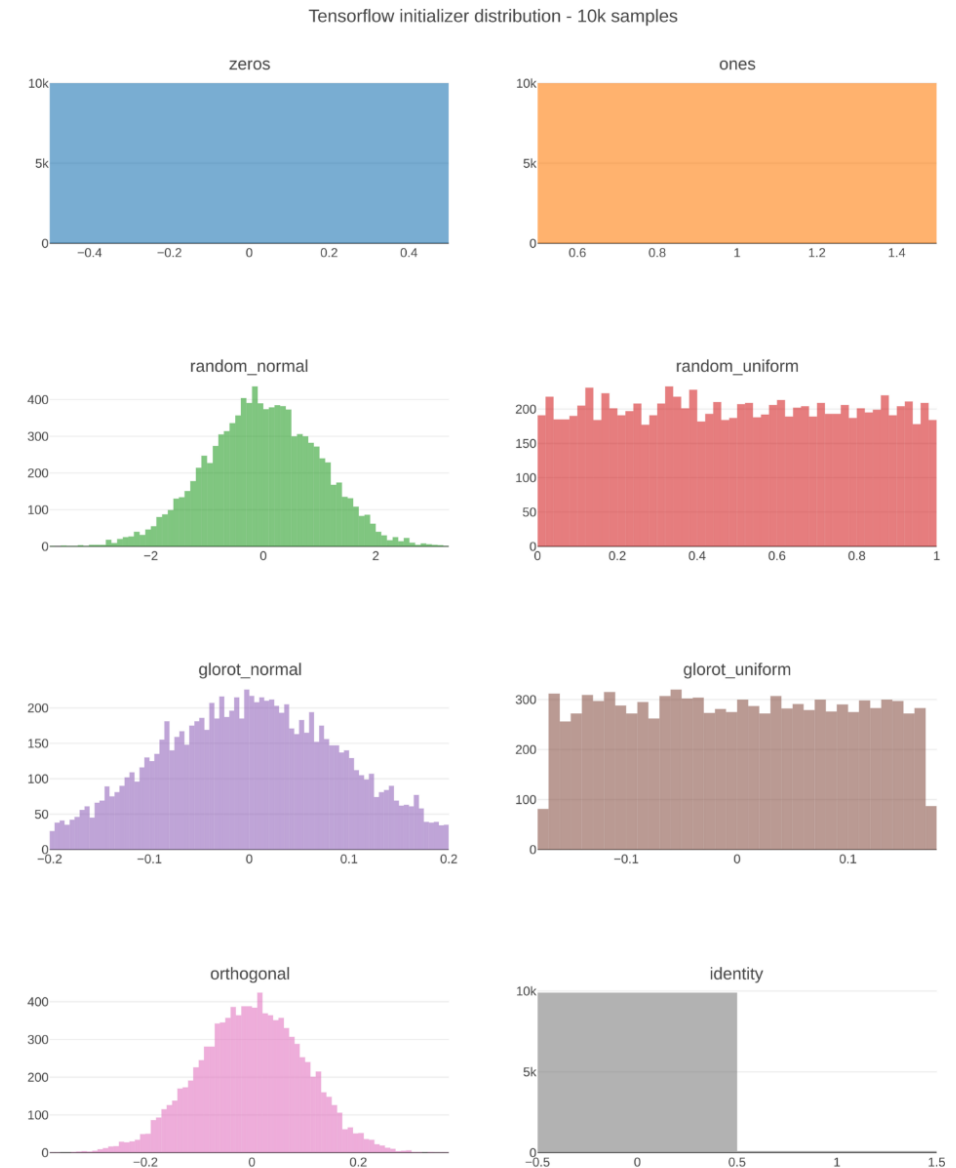
# Data Preprocessing: PCA, Whitening

1. Center data , calculate co-variance matrix
2. SVD factorization, decorrelation
3. PCA - dimensionality reduction
4. Whitening - stretching data into an isotropic gaussian blob to normalize the scale



# Weight Initialization

- Normalized Data
  - Weights expected to be centered at 0, small positive/negative
  - Asymmetry between neurons facilitates learning
  - Same valued or 0 weights very hard to learn.
- Random Initialization
  - From Gaussian or Uniform distribution





# Weight Initialization: Glorot

- Allows for scaling the weight distribution on a layer-by-layer basis.
- Draws from a normal or uniform distribution with centered mean and standard deviation scaled to the layer's number of input and output neurons



<https://becominghuman.ai/priming-neural-networks-with-an-appropriate-initializer-7b163990ead>

# Regularization

- Prevents overfitting by modifying the loss function by adding additional terms that penalize large weights
- L2 regularization is usually preferred over L1 due to empirical performance results

$$\text{L1: } R(\theta) = \|\theta\|_1 = \sum_{i=1}^n |\theta_i|$$

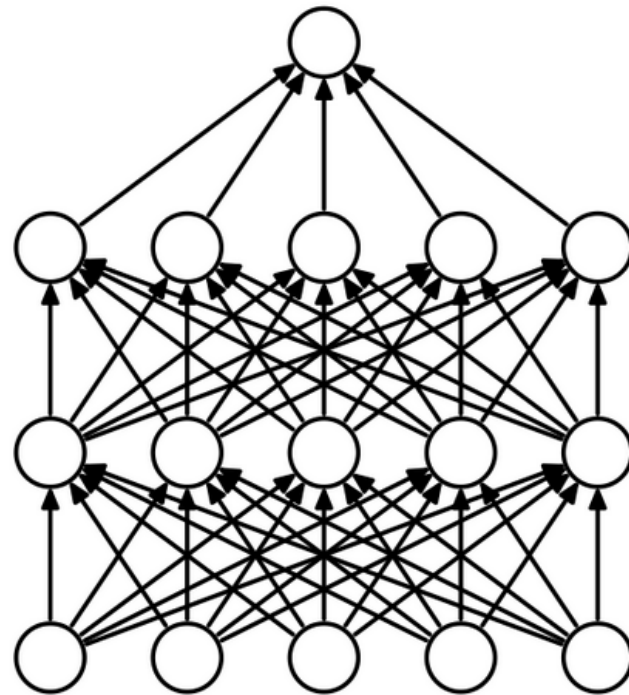
Error function + magnitude of all weights in the neural network

$$\text{L2: } R(\theta) = \|\theta\|_2^2 = \sum_{i=1}^n \theta_i^2$$

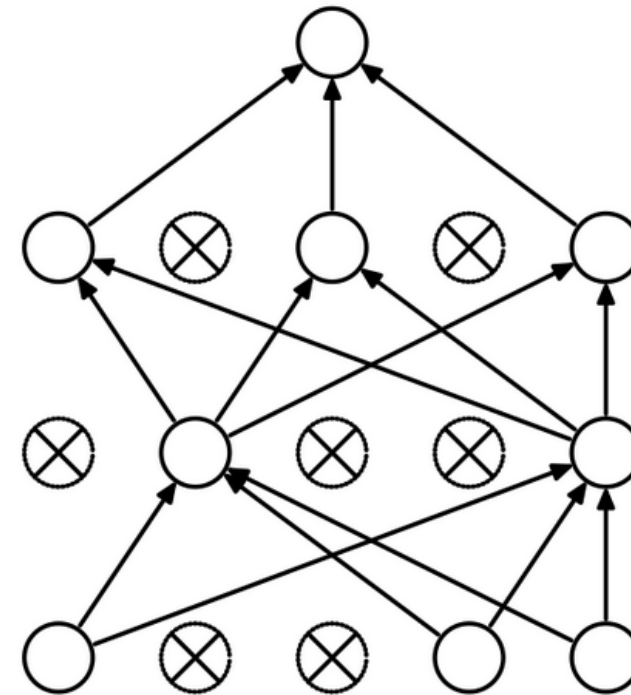
Error function + squared magnitude of all weights in the neural network

# Dropout

- Randomly drop weights from a layer such that at each layer neurons are forced to learn the multiple characteristics of the network



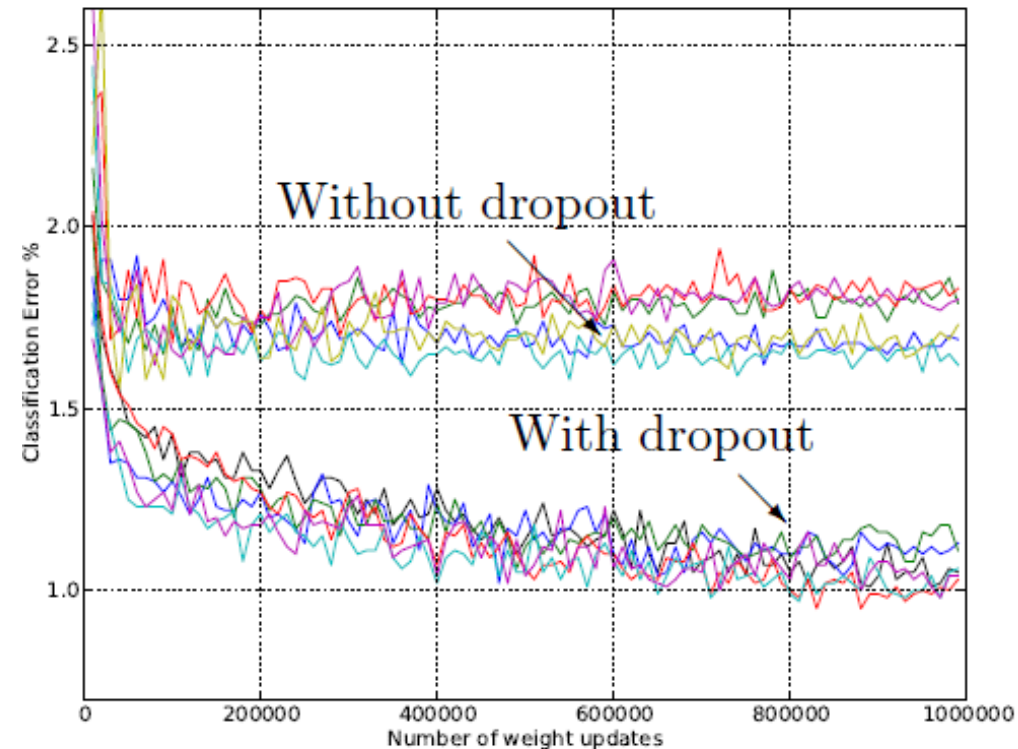
(a) Standard Neural Net



(b) After applying dropout.

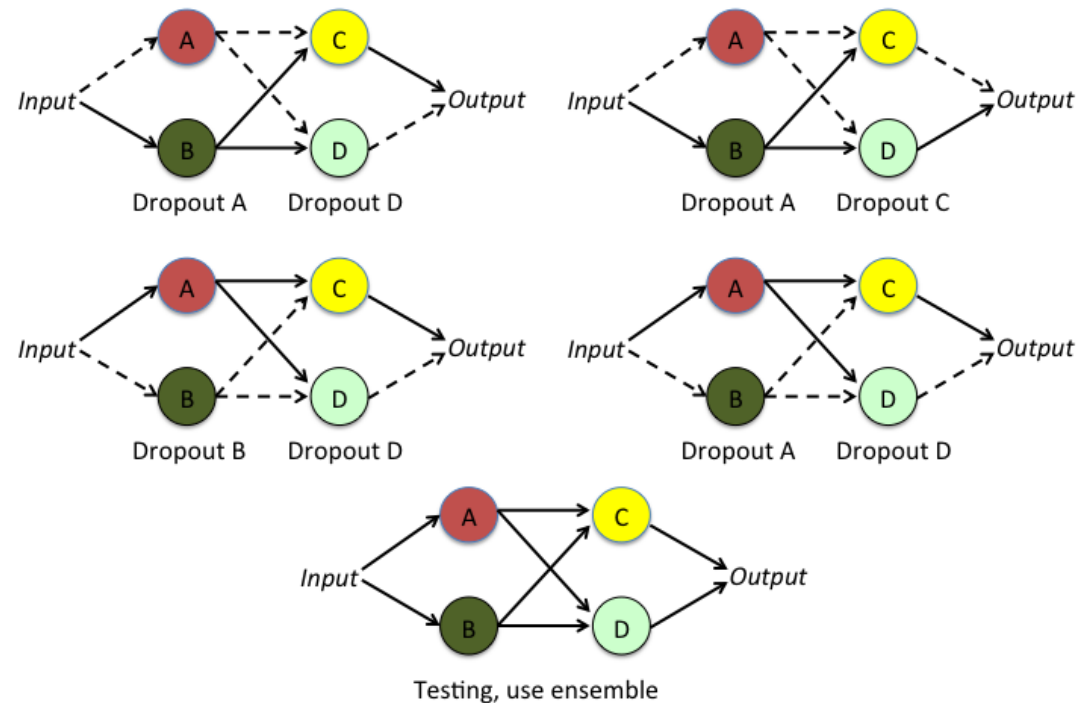
# Dropout

- Prevents overfitting by combining exponentially many different ANN architectures efficiently



# Dropout: Ensemble Effect

- Effect of taking ensemble over  $\binom{N}{\frac{N}{2}}^h$  models.

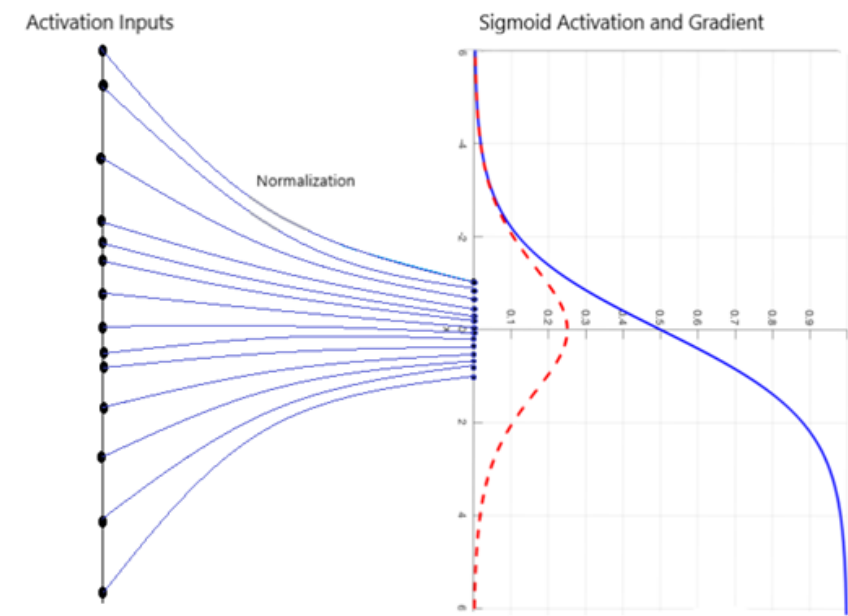
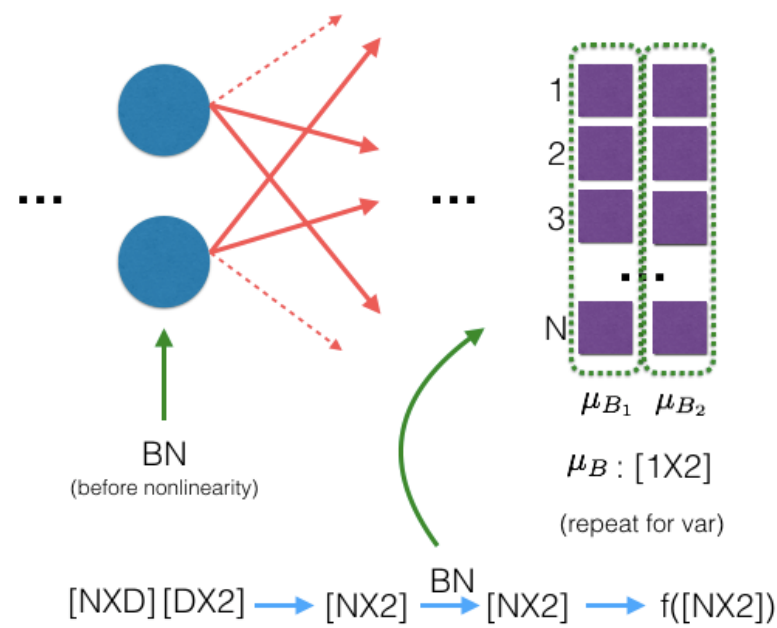


2 layers and 4 neurons in each layer,  ${}^4C_2 \times {}^4C_2 = 36$  ; takes average over 36 models.

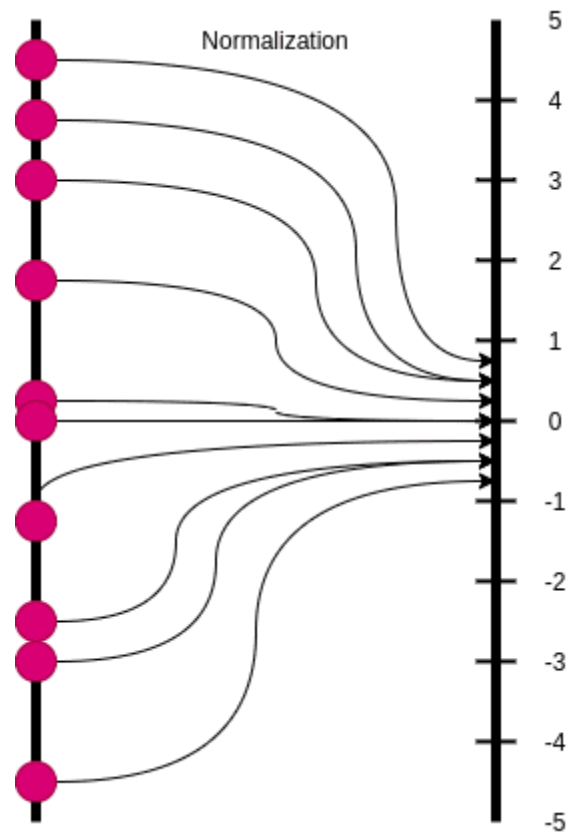
2 layers with 100 neurons in each layer, takes average over 24502500 possible models

# Batch Normalization

- Method to normalize the inputs of each layer, in order to fight the internal covariate shift problem.
- Reduces vanishing gradient during training and can decrease training time and result in better performance



# Batch Normalization



$$\mu_{\mathcal{B}} = \frac{1}{m} \sum_{i=1}^m x_i$$

Input

Mini-batch mean

$$\sigma_{\mathcal{B}}^2 = \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2$$

Mini-batch variance

$$\hat{x}_i = \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}}$$

Normalize

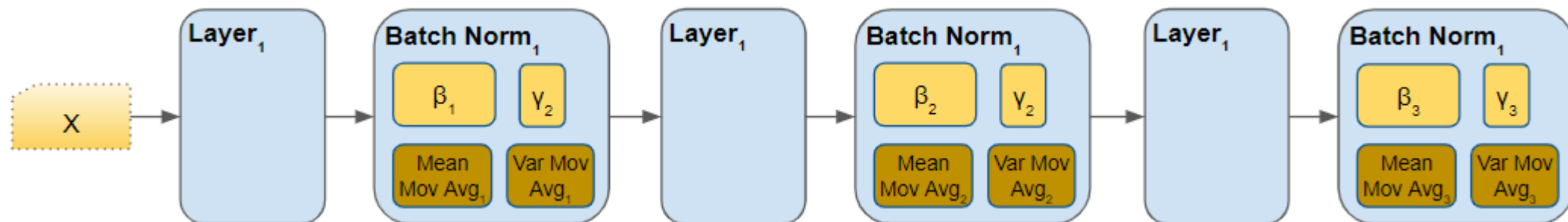
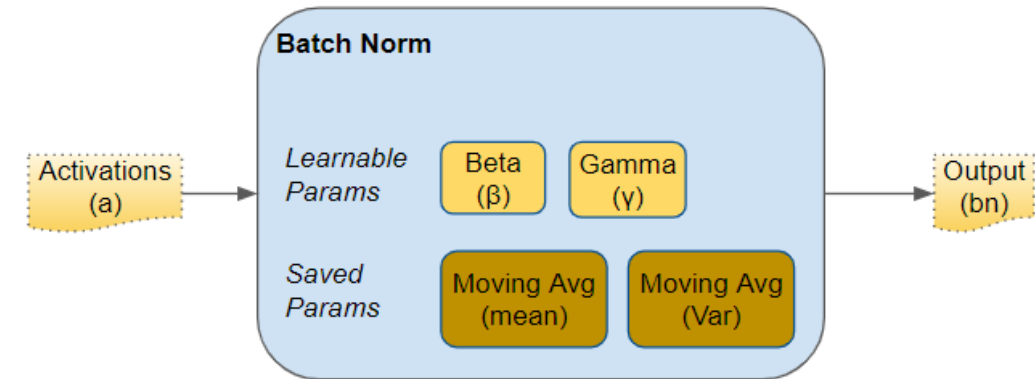
$$y_i = \gamma \hat{x}_i + \beta = \text{BN}_{\gamma, \beta}(x_i)$$

Scale and Shift

Output

# Batch Normalization: Parameters

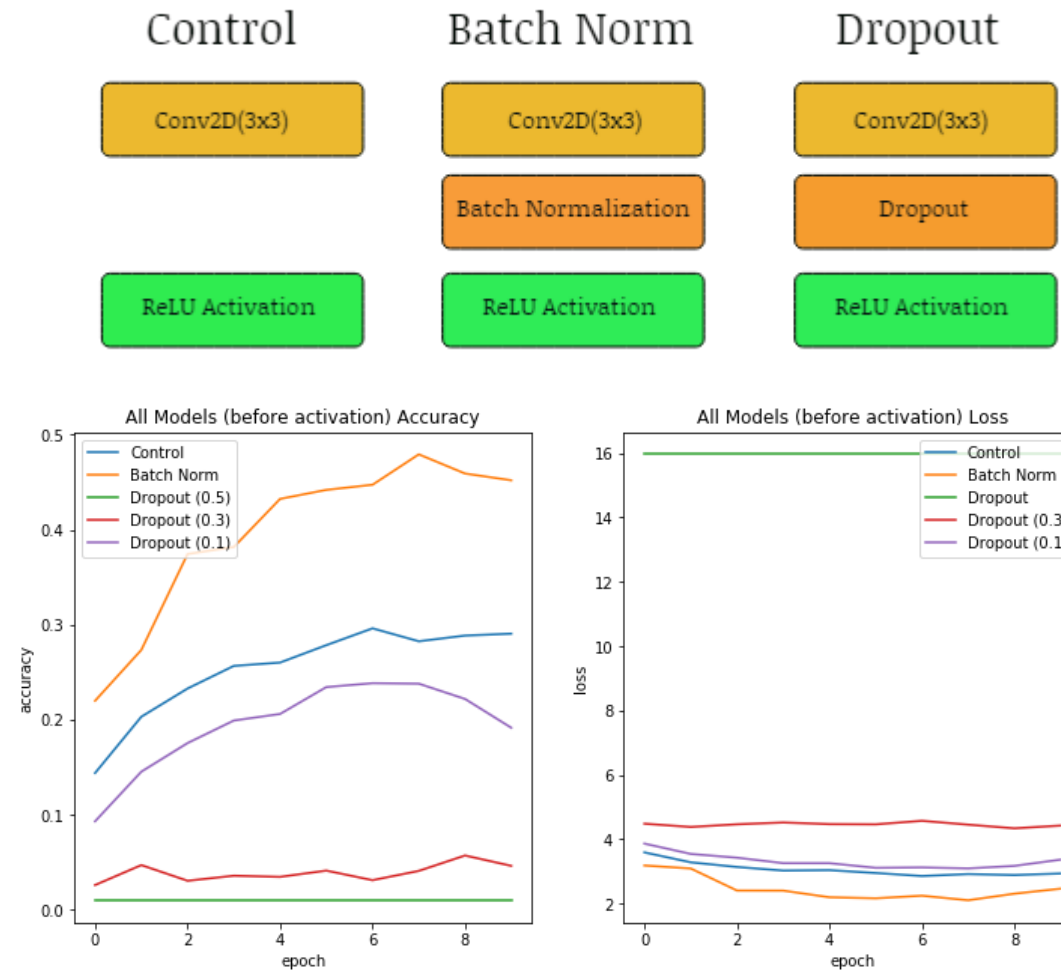
- BN layer has parameters of its own:
  - Two learnable parameters beta and gamma.
  - Two non-learnable parameters (Mean Moving Average and Variance Moving Average) are saved as part of the 'state' of the Batch Norm layer.



3 hidden layers and 3 BN layers in a network, would have three learnable beta and gamma parameters for the three layers



# Dropout vs Batch Normalization



# Hyperparameter Tuning

## Architecture

- Architecture
- No of hidden layers
- No of hidden units in each layer
- Activation function
- Batch Normalization
- Dropout

## Optimization

- Weights Initialization
- Learning Rate
- Loss Function
- Batch size
- Momentum
- Number of epochs

# Hyperparameters - Optimizers, Learning Rate, Gradient

## Optimizers

- `tf.train.GradientDescentOptimizer`
- `tf.train.AdadeltaOptimizer`
- `tf.train.AdagradOptimizer`
- `tf.train.AdagradDAOptimizer`
- `tf.train.MomentumOptimizer`
- `tf.train.AdamOptimizer`
- `tf.train.FtrlOptimizer`
- `tf.train.ProximalGradientDescentOptimizer`
- `tf.train.ProximalAdagradOptimizer`
- `tf.train.RMSPropOptimizer`

## Decaying the learning rate

- `tf.train.exponential_decay`
- `tf.train.inverse_time_decay`
- `tf.train.natural_exp_decay`
- `tf.train.piecewise_constant`
- `tf.train.polynomial_decay`

## Gradient Clipping

- `tf.clip_by_value`
- `tf.clip_by_norm`
- `tf.clip_by_average_norm`
- `tf.clip_by_global_norm`
- `tf.global_norm`

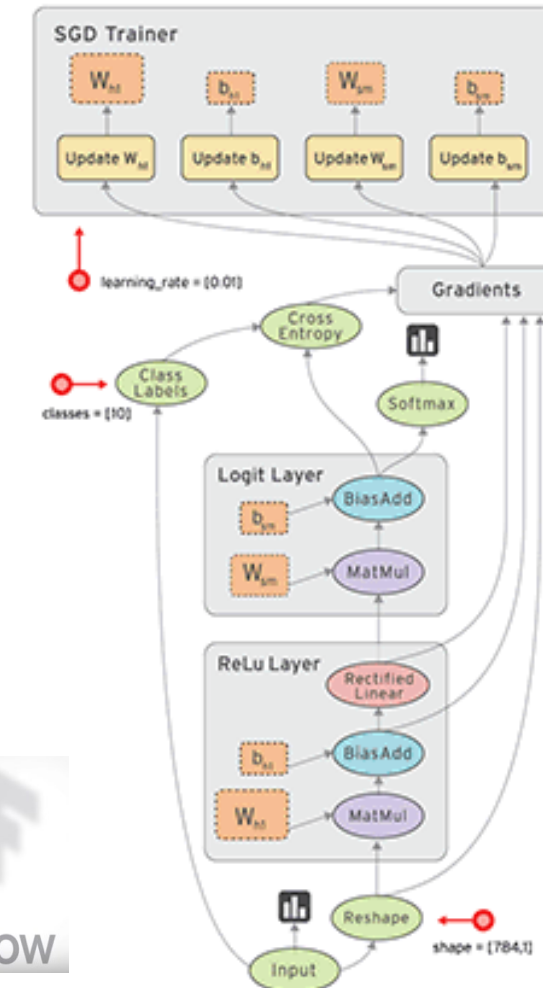
# Best Practices

- Normalize all data and/or use batch normalization
- Use small initial random weights
- Reduce learning rate when weights oscillate
- Keep derivatives from going to zero by choosing non-saturating activations
- Use momentum to speed learning
- Use mini-batches for stabilizing gradients
- Avoid overfitting - L2 regularization, Dropouts, Early stopping of training
- Use neural network ensembles

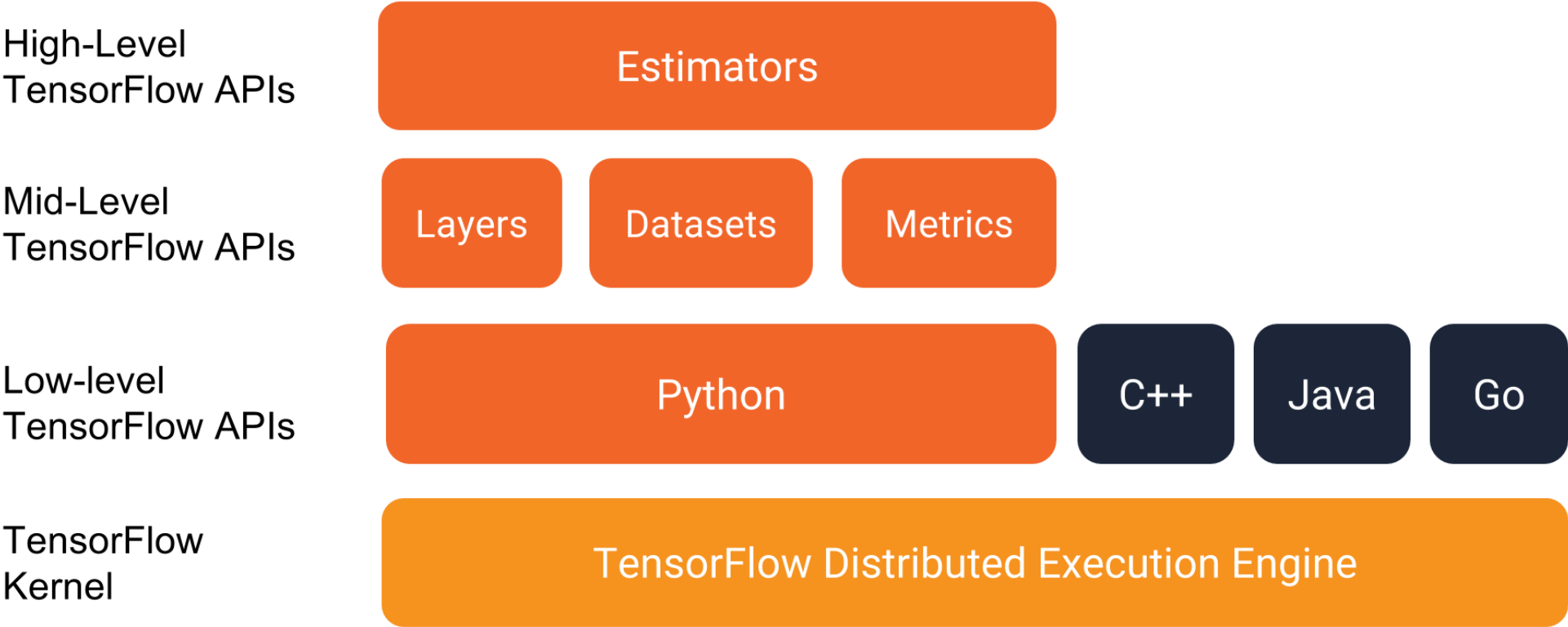


# TensorFlow

- TensorFlow expresses a numeric computation as a directed graph
- Tensor is the central unit of data which consists of a set of primitive values shaped into a multi-dimensional array
- A tensor's rank is its number of dimensions, while its shape is a tuple of integers specifying the array's length along each dimension.

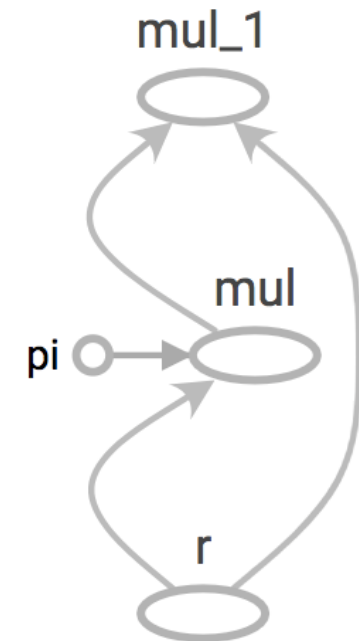


# TensorFlow Architecture



# Graph

- A computational graph is a series of TensorFlow operations arranged into a graph.
- The graph is composed of two types of objects:
  - Operations (or "ops"): The nodes of the graph. Operations describe calculations that consume and produce tensors.
  - Tensors : The edges in the graph. These represent the values that will flow through the graph. Most TensorFlow functions return `tf.Tensors`. `tf.Tensors` do not have values, they are handles to elements in the computation graph.





# Advantages of Graphs

- Parallelism
- Distributed execution
- Compilation
- Portability

# TensorBoard

