

MSiA

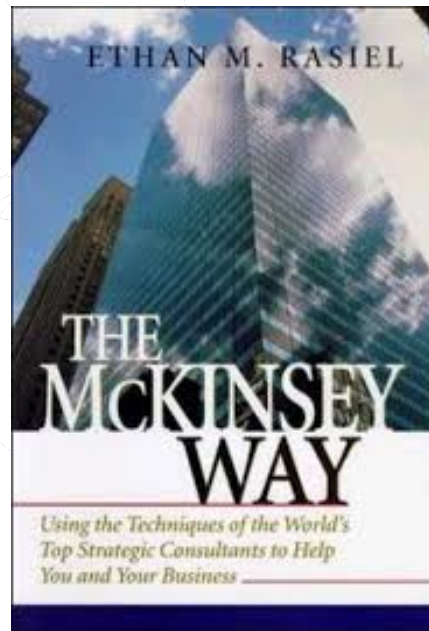
CLASS 2: MODELS FOR DECISION-MAKING

Joel Shapiro
Clinical Associate Professor, MEDS

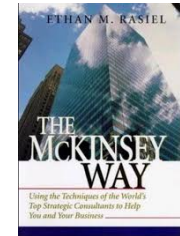
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A FRAMEWORK FOR RIGOROUS DECISION-MAKING IS NOT NEW

**Q: What did YOU
find helpful (or not)
about this reading?**



WHY DID WE READ THIS?



Many analytics tools are new, many concepts are not.

There are exceptions - being able to craft accurate predictions enables us to do some things differently.

Plus, automation offers lots of cool opportunities to implement analytics at scale.

Your success as a data scientist depends on your ability to do good work, but also to recognize that many analytics concepts are not new to the business world.

The marketing team at your company has a big database of prospective customers, and can predict the likelihood that each customer will convert.

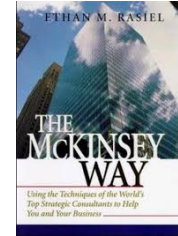
Prospect A is 1% likely to convert

Prospect B is 50% likely to convert

Prospect C is 99% likely to convert

If you have the resources to send only ONE prospect to the sales team, which one should it be?

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E.g., a business leader wanting to deploy resources in a way that maximizes marginal benefit is not new. But using prediction with experimentation as a method may be novel.

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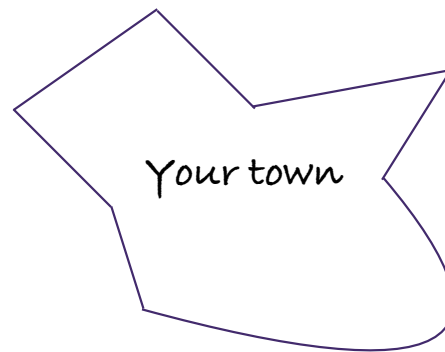
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YOUR TURN... TO HELP DETERMINE WHERE TO PUT EMS SERVICES

You are a council member for a small town in the early 1900s (pre-computers)

Your town has long been using the emergency management services (fire, law enforcement, etc.) of a neighboring town. You feel like you are finally at the point where you can and should build your own.

Q: Where to put it?



ADVISING ON THESE DECISIONS REQUIRES **PRECISION**

What's important?

What are the goals?

What are the options?

How do you balance the pros and cons of each option?

As data professionals, we build **MODELS** to generate answers.

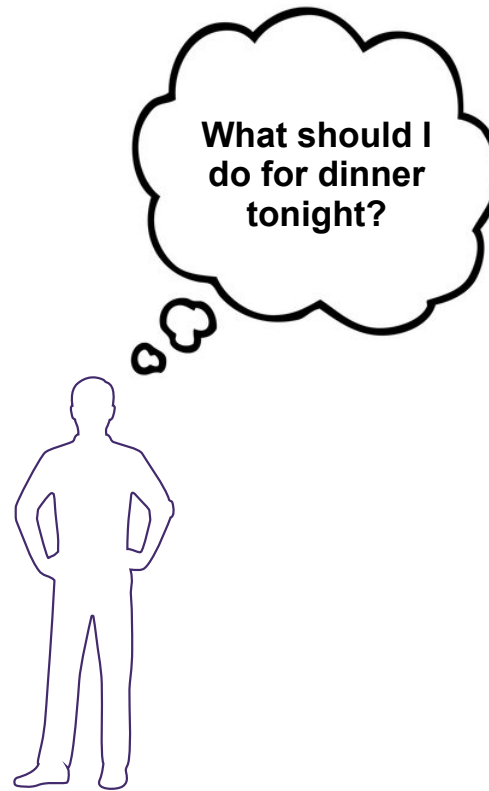
MODELS ENABLE DECISION-MAKING

1. Identify universe of options
2. Generate an evaluation mechanism
3. Prioritize among those evaluations

$$\begin{array}{l} \text{maximize} \\ \text{minimize} \end{array} \quad f(x,y,z\dots) \quad \text{s.t. constraints}$$

**You might know these as
“constrained optimization” problems.**

I WANT TO HELP YOU FIGURE OUT DINNER TONIGHT!



CONSTRAINED OPTIMIZATION IS A GOOD WAY TO THINK ABOUT WHY YOU BUILD MODELS AND HOW THEY WILL BE USED

**Where should I go for
dinner tonight?**

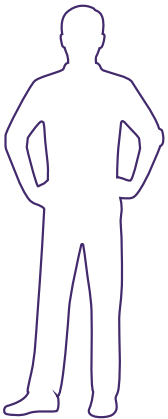
What are my options?

How much value does each have? (taste, fullness, health)

What's my objective?

What's the most I'll spend, farthest I'll drive, etc.?

$$\begin{array}{ll} \text{maximize} & f(x,y,z,\dots) \\ \text{minimize} & \end{array} \quad \text{s.t. constraints}$$



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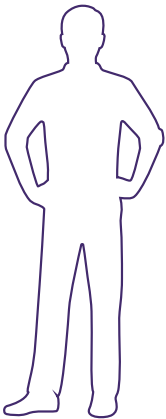
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Things you care about can be expressed as objectives OR constraints.

What's the difference here?

Maximize fullness, s.t. <\$15

Minimize cost, s.t. must feel full

CONSTRAINED OPTIMIZATION FORCES PRECISION

I like thinking of problems as constrained optimization problems bc they force decision-makers to articulate **what they care about** and the **relative value of each thing they care about**.

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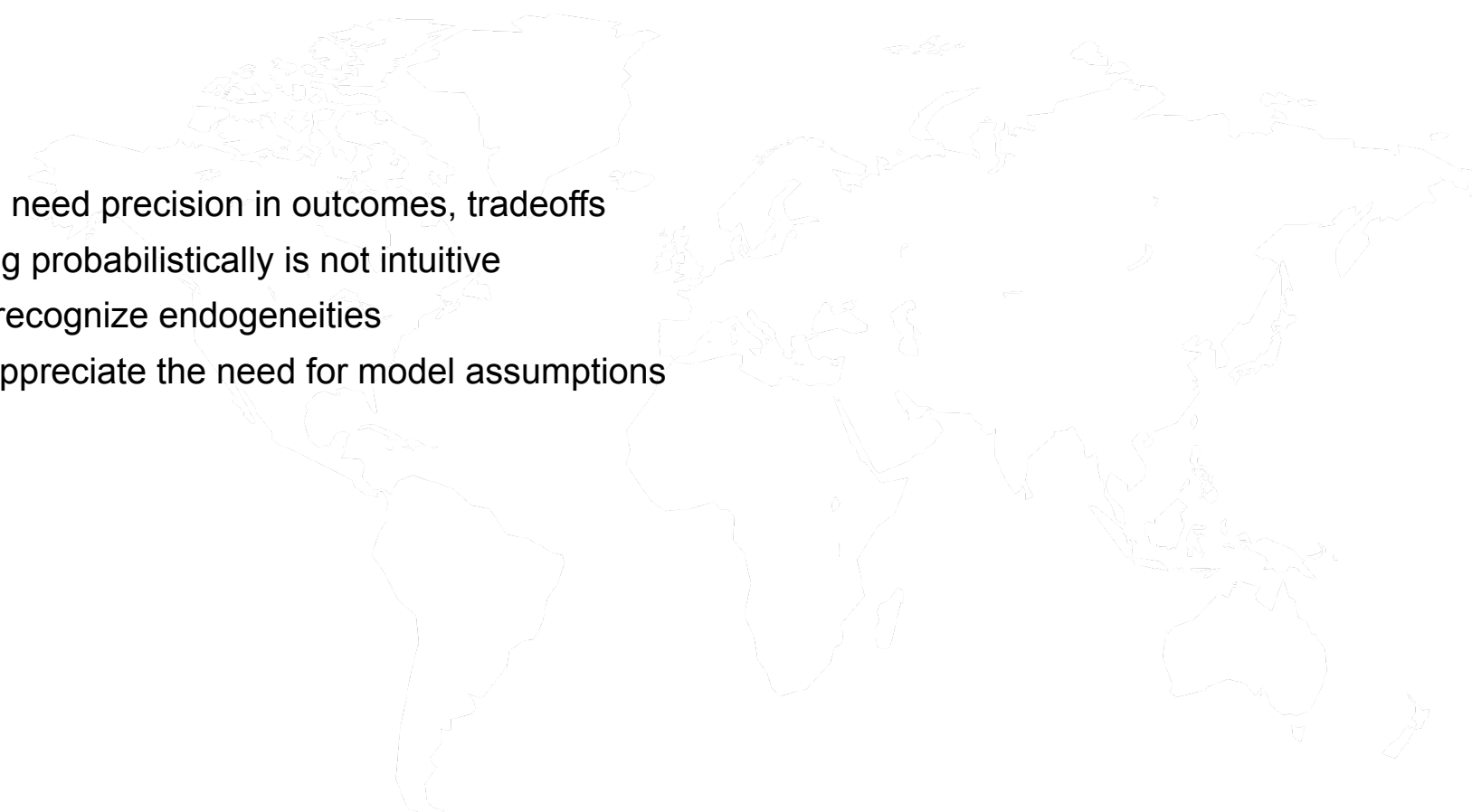
“Advise me on where to go for dinner.”

“Help me figure out which customers I should target.”

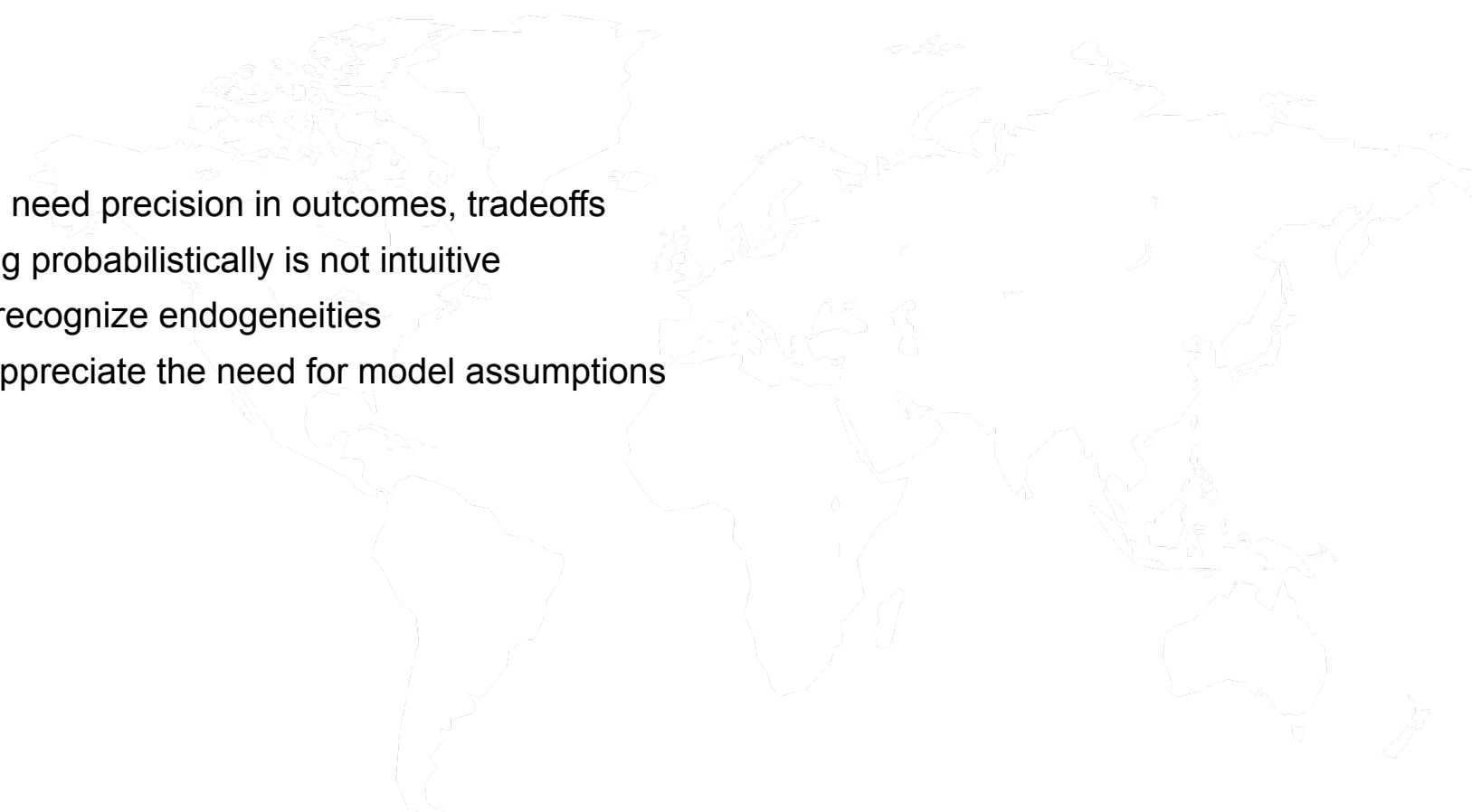
“We have one COVID vaccine left.
Should we give it to an elderly person with many health problems?
Or a healthy 25 year old?”

And **precision** means I can provide **better solutions**.

SO WHY DO BIZ LEADERS STRUGGLE WITH MODELS?

- 
- ✓ 1. Models need precision in outcomes, tradeoffs
 - 2. Thinking probabilistically is not intuitive
 - 3. Fail to recognize endogeneities
 - 4. Don't appreciate the need for model assumptions

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Was this model wrong?

- with three models
- ☐ Polls-plus forecast
What polls, the economy and historical data tell us about Nov. 8
 - ☒ Polls-only forecast
What polls alone tell us about Nov. 8
 - ☐ Now-cast
Who would win the election if it were held today

National overview

Updates
National polls

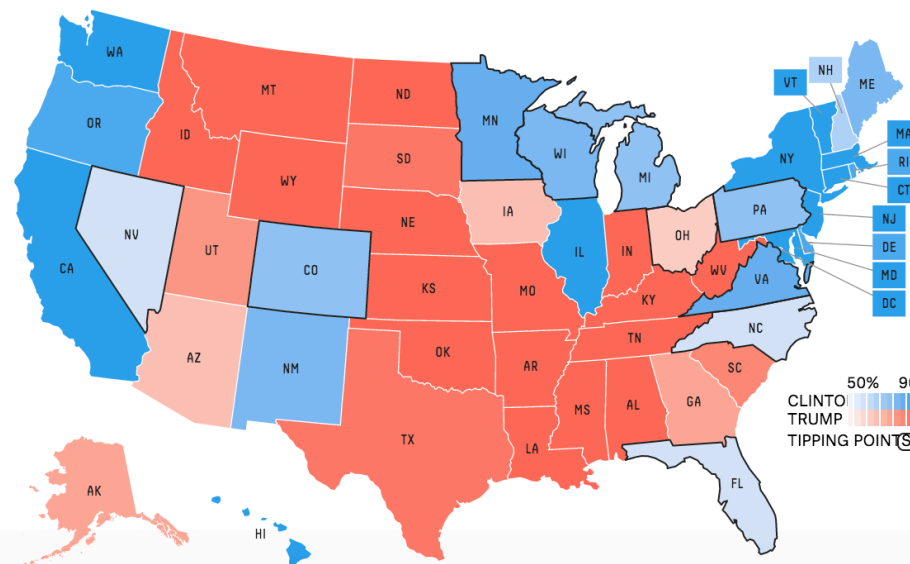
States to watch

Arizona
Colorado
Florida
Georgia
Iowa
Maine
Michigan
Minnesota
Nevada
New Hampshire
New Mexico
North Carolina
Ohio
Pennsylvania
Utah

Who will win the presidency?



Chance of winning



CONSIDER THIS EXAMPLE

Cell Block A houses 25 violent criminals, 24 of whom, acting together in the prison yard, kill one of the guards. The 25th prisoner does not participate but cannot be identified by video cameras. An investigation fails to yield additional information because none of the prisoners will talk.

Nevertheless, the District Attorney selects one prisoner (“P”) at random and charges him with murder. At trial, the DA presents uncontroverted evidence that:

- P was in the prison yard at that time and
- All but one prisoner participated in the killing.

Would you convict P?

Thanks to Jonathan Koehler, NU Law evidence professor for this example

AND THIS ONE...

Imagine that I've built a new diagnostic predictive tool to help the MSiA admissions team identify which prospective students have lied on their application. The test has a 97% true positive rate and a 97% true negative rate.

In the next round of admissions, the tool identifies someone as a liar.

Should MSiA reject that applicant? What are the chances that person lied?

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BAYES THEOREM

$$P(\text{Liar} \mid +) = \frac{P(+ \mid \text{Liar}) * P(\text{Liar})}{P(+)} = \frac{P(+ \mid \text{Liar}) * P(\text{Liar})}{P(+ \mid \text{Liar}) * P(\text{Liar}) + P(+ \mid \text{NotLiar}) * P(\text{NotLiar})}$$

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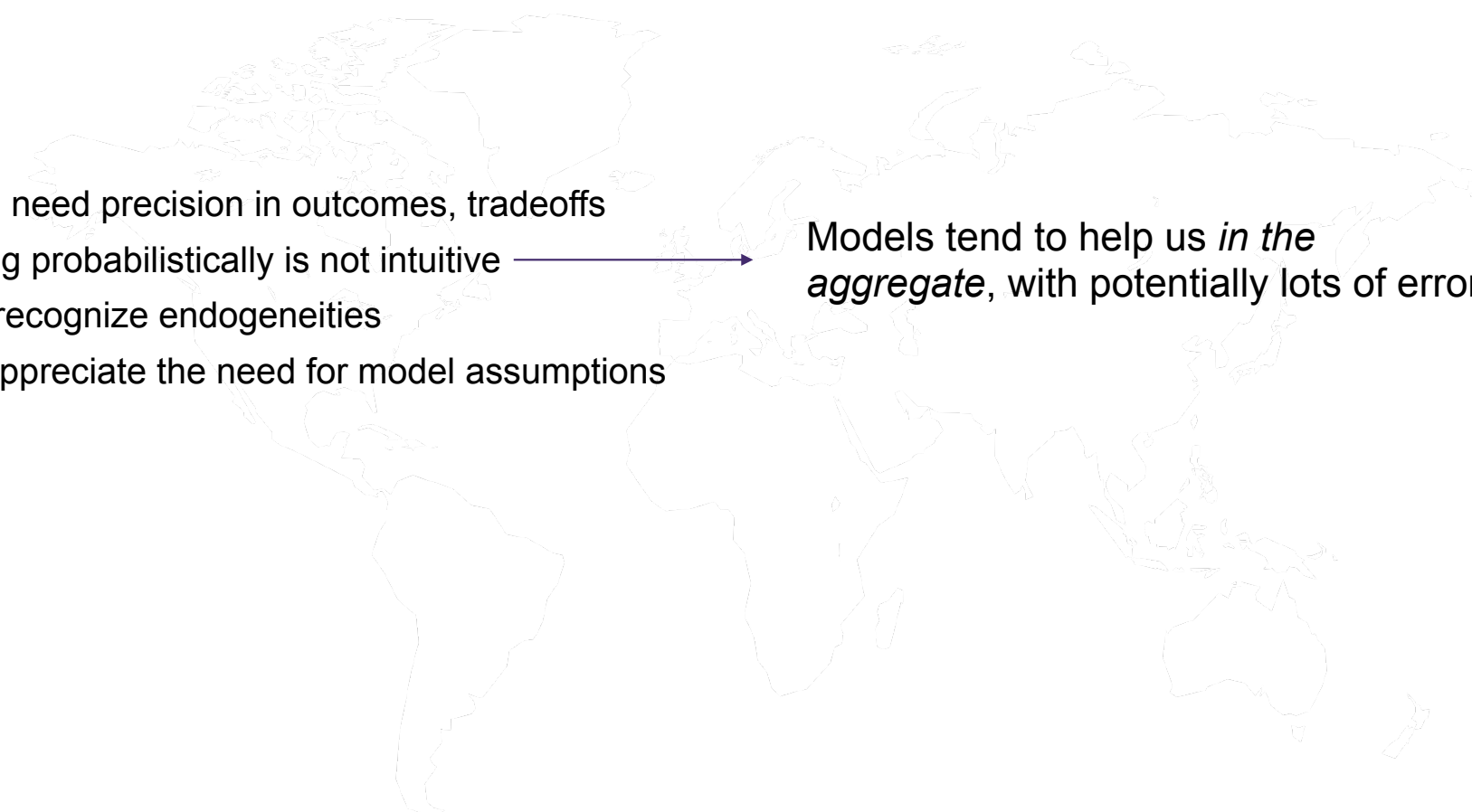
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If $p(\text{Liar}) = 1\%$, then $p(\text{Liar} \mid +) = 25\%$

If $p(\text{Liar}) = 10\%$, then $p(\text{Liar} \mid +) = 78\%$

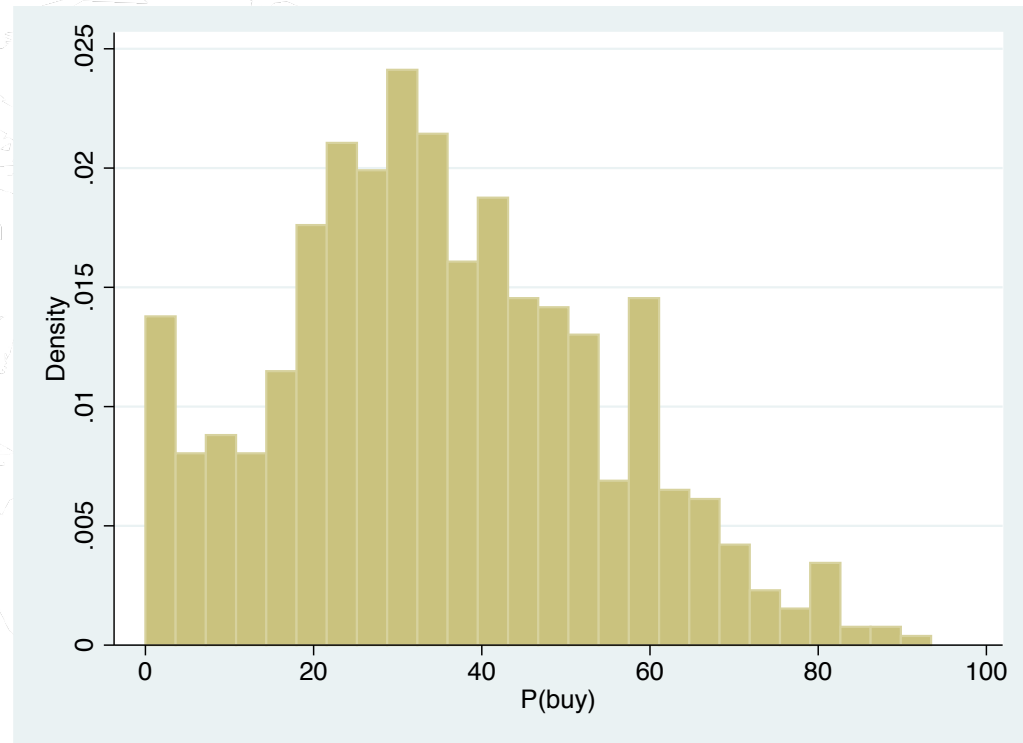
If $p(\text{Liar}) = 30\%$, then $p(\text{Liar} \mid +) = 93\%$

WHAT'S THE POINT HERE?

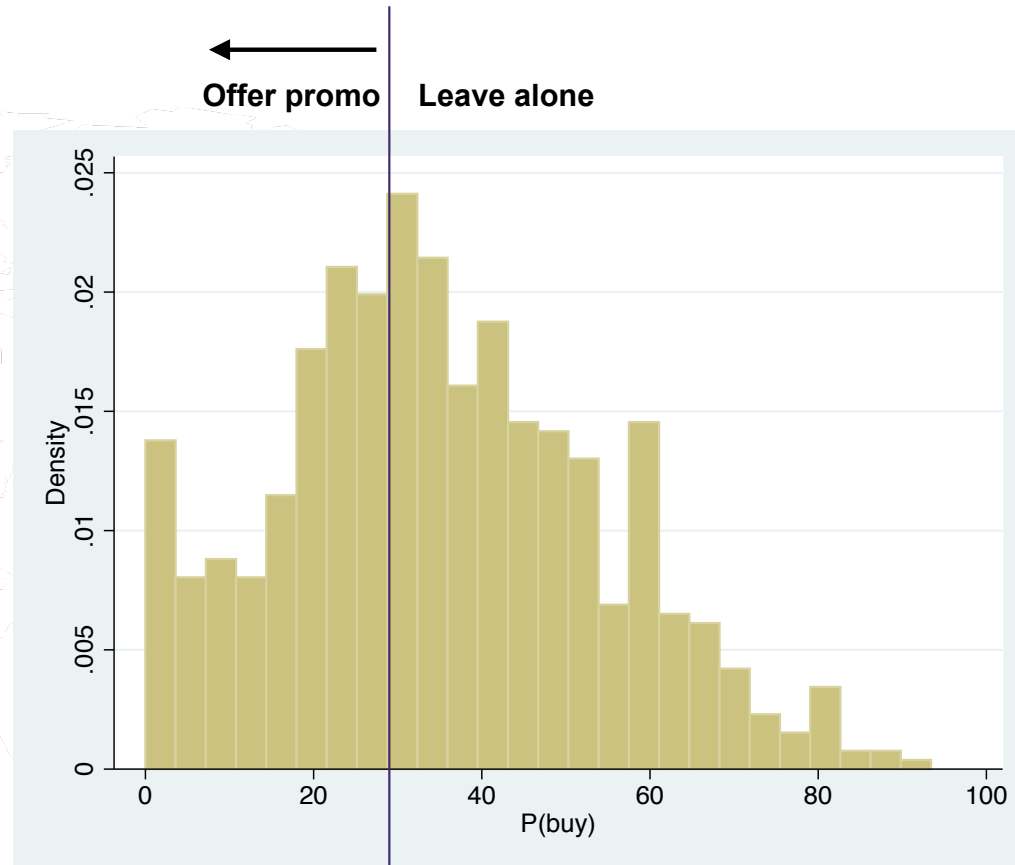
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Models tend to help us *in the aggregate*, with potentially lots of error

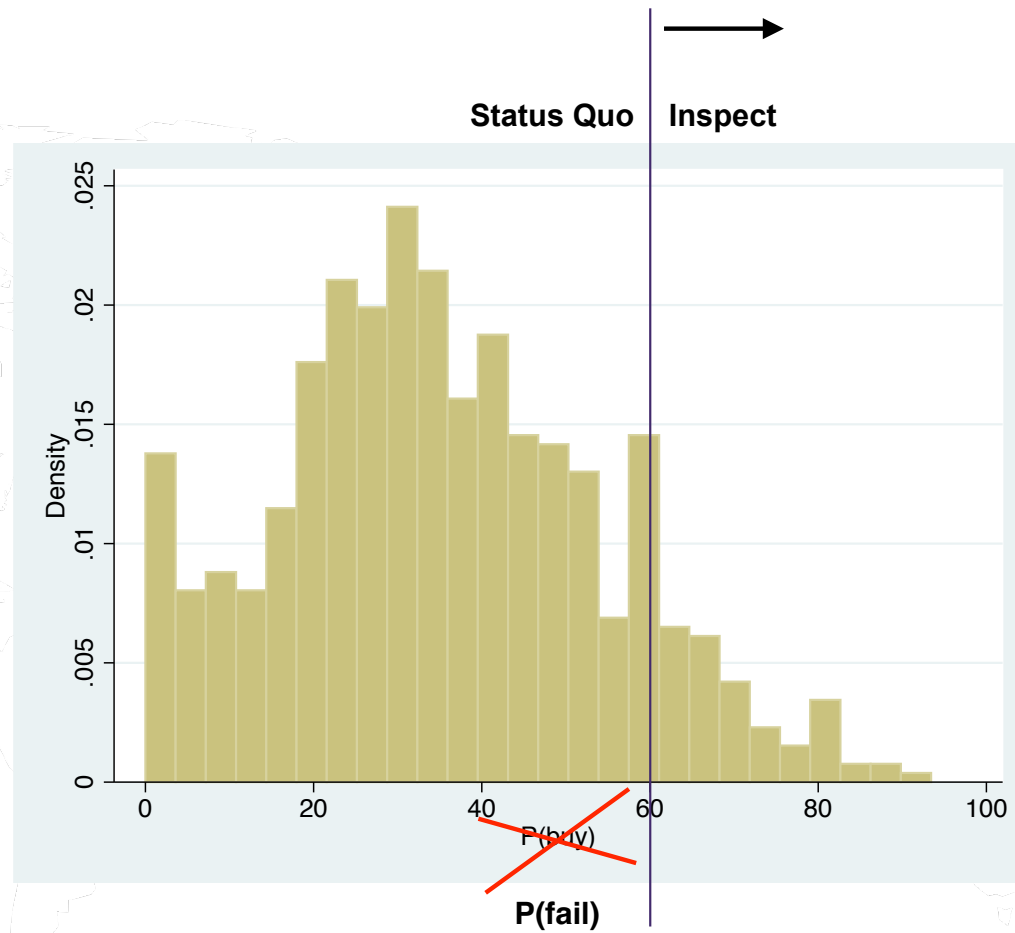
CustomerID	P(buy)
2805341	0.678
6291929	0.297
4560378	0.015
1379279	0.499
2422622	0.673
3571303	0.336
7500176	0.515
7437015	0.041
1245047	0.884
2283893	0.886
1901072	0.686
7263443	0.452
6244271	0.247
9966029	0.382
5391105	0.562
8419109	0.955
2544554	0.382
4706292	0.899



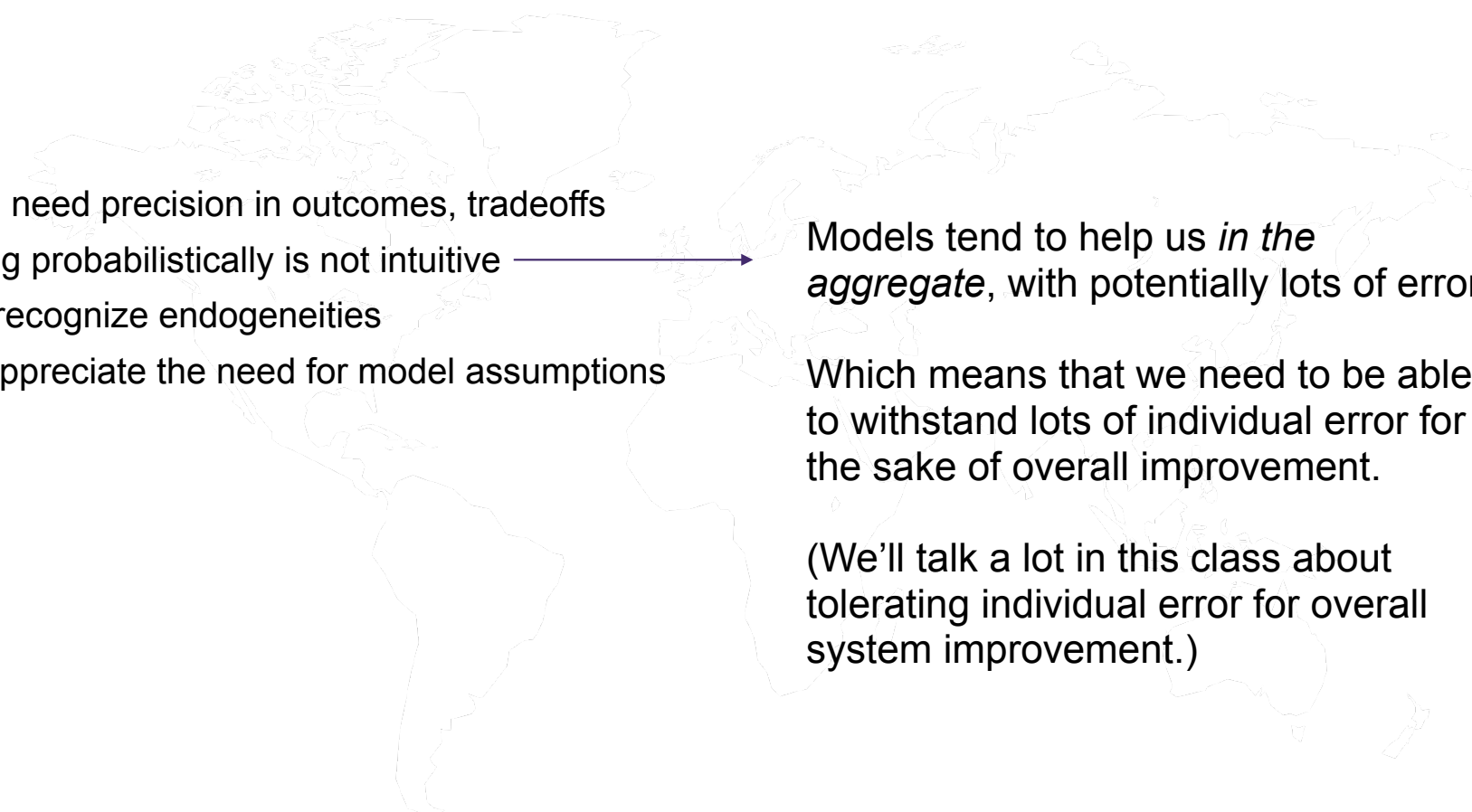
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MachineID	P(fail)
CustomerID	P(buy)
2805341	0.678
6291929	0.297
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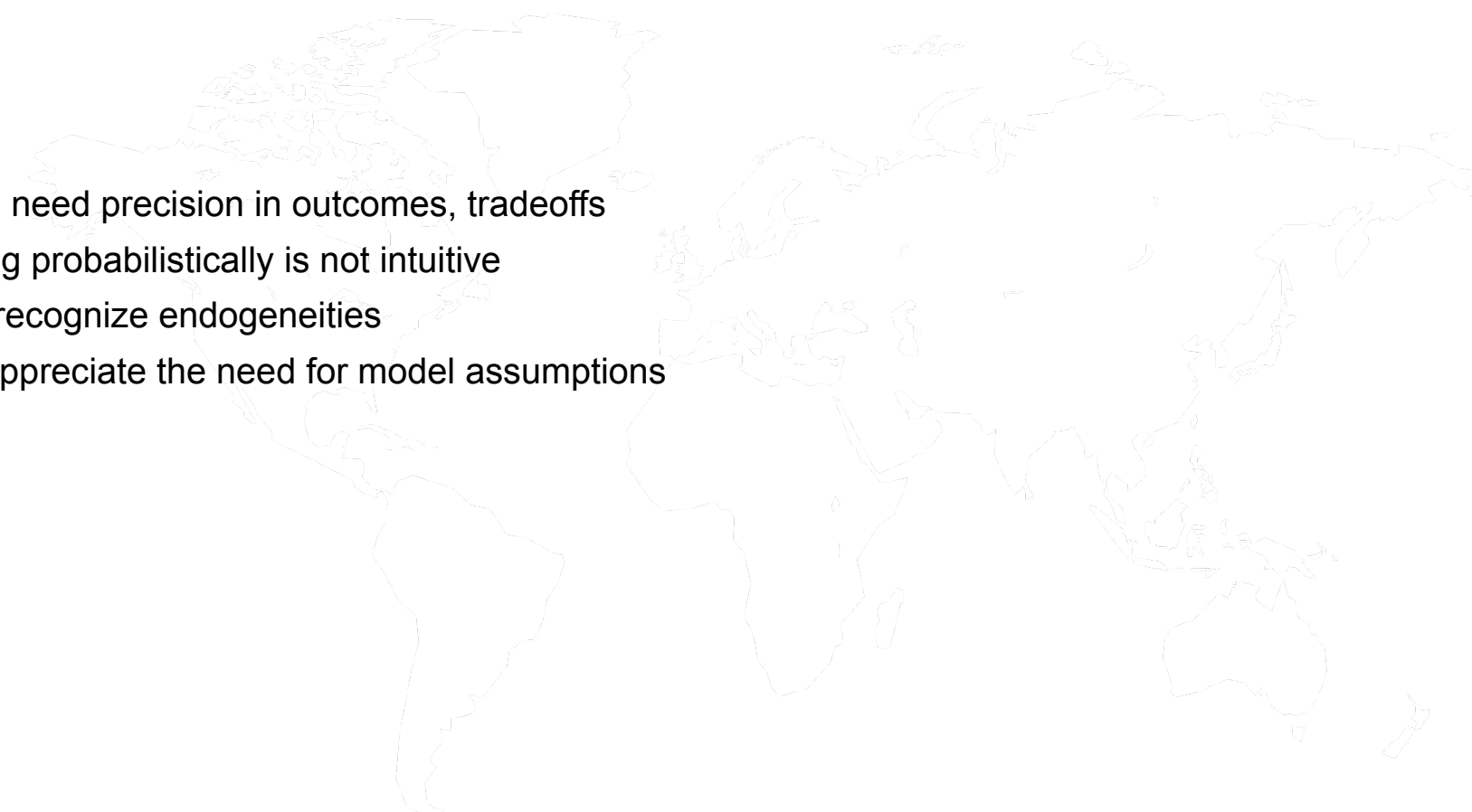
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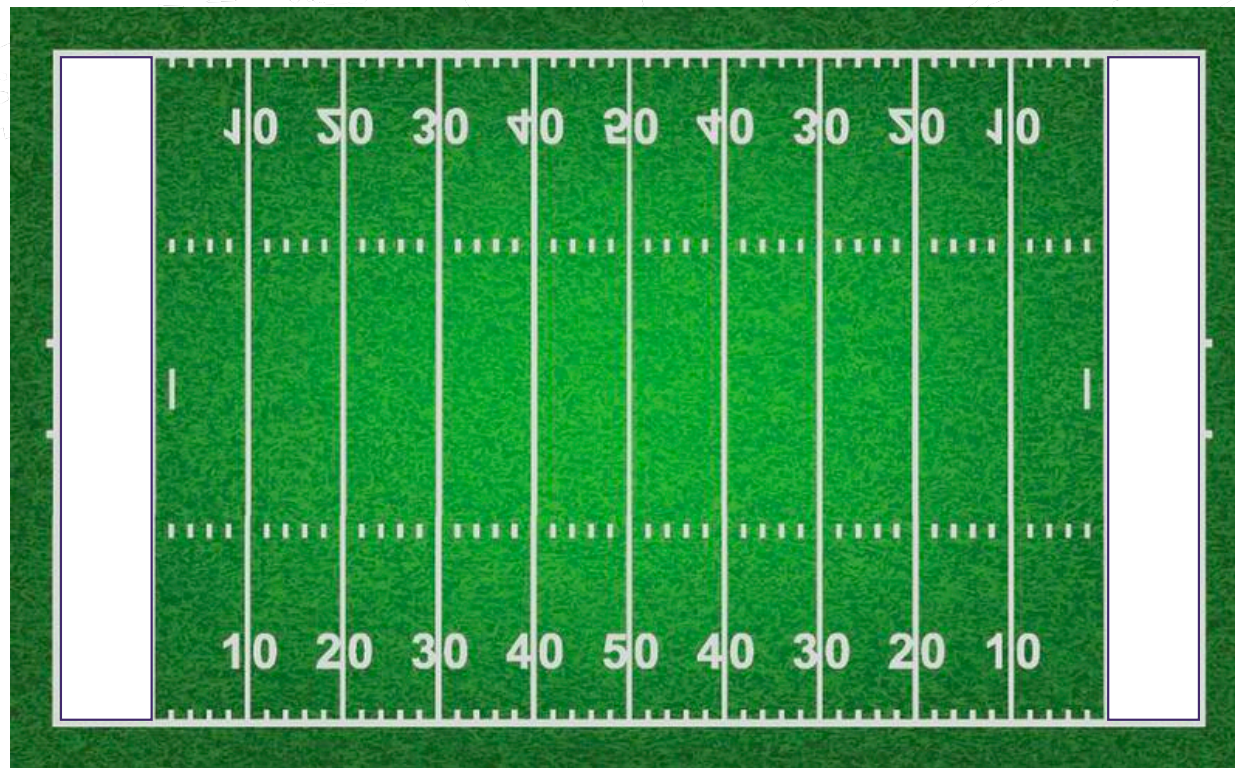
Which means that we need to be able to withstand lots of individual error for the sake of overall improvement.

(We'll talk a lot in this class about tolerating individual error for overall system improvement.)

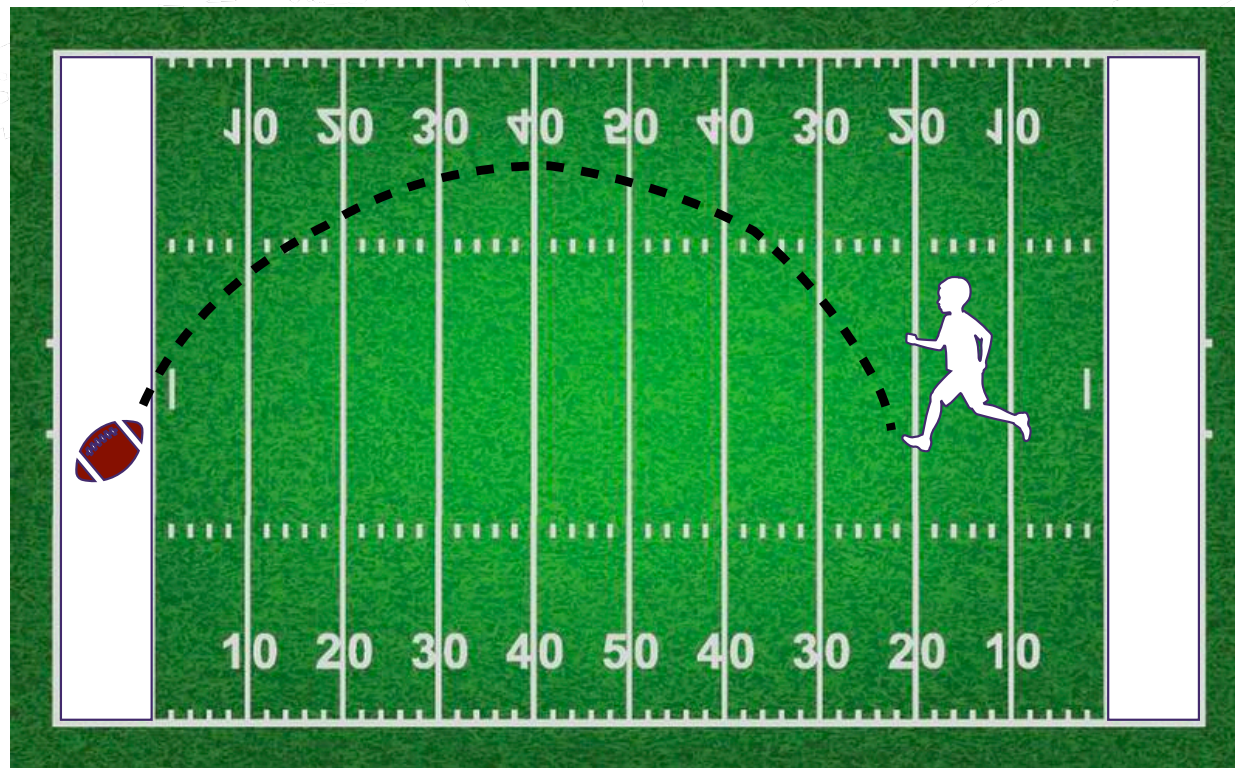
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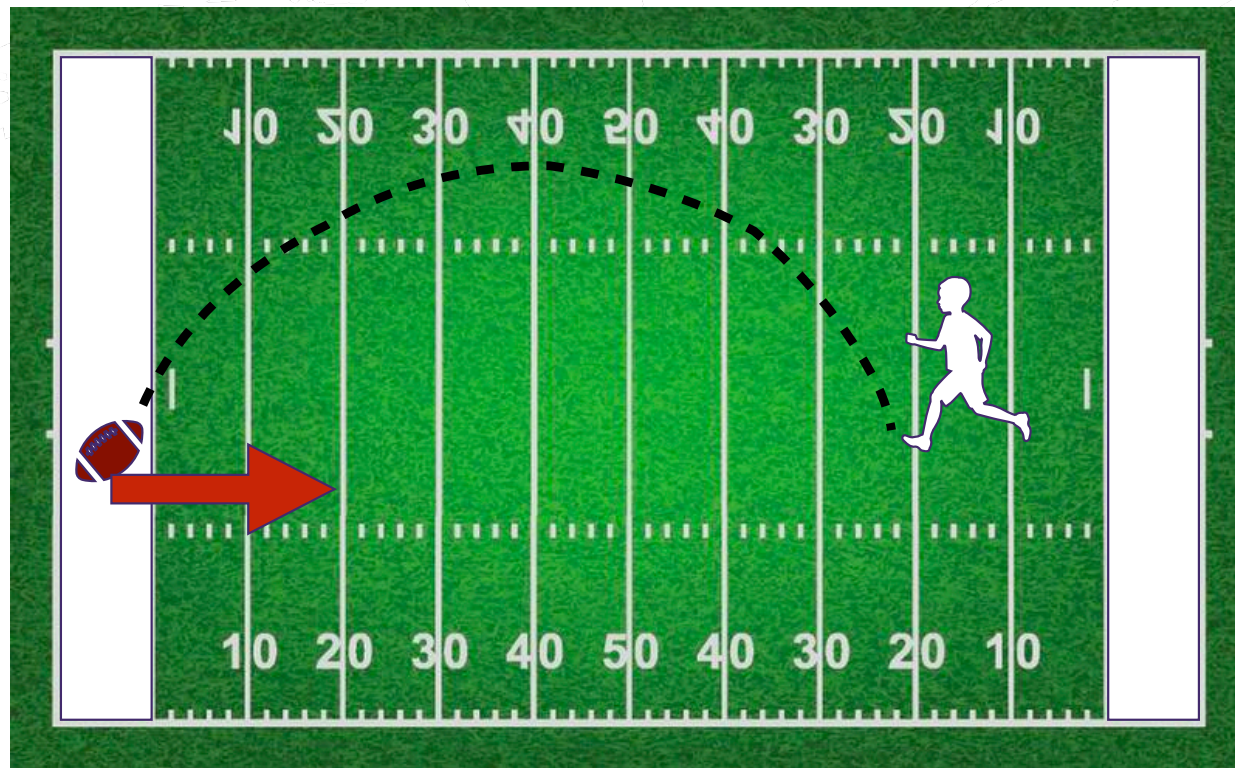
CONSIDER THIS ENDOGENEITY IN AMERICAN FOOTBALL



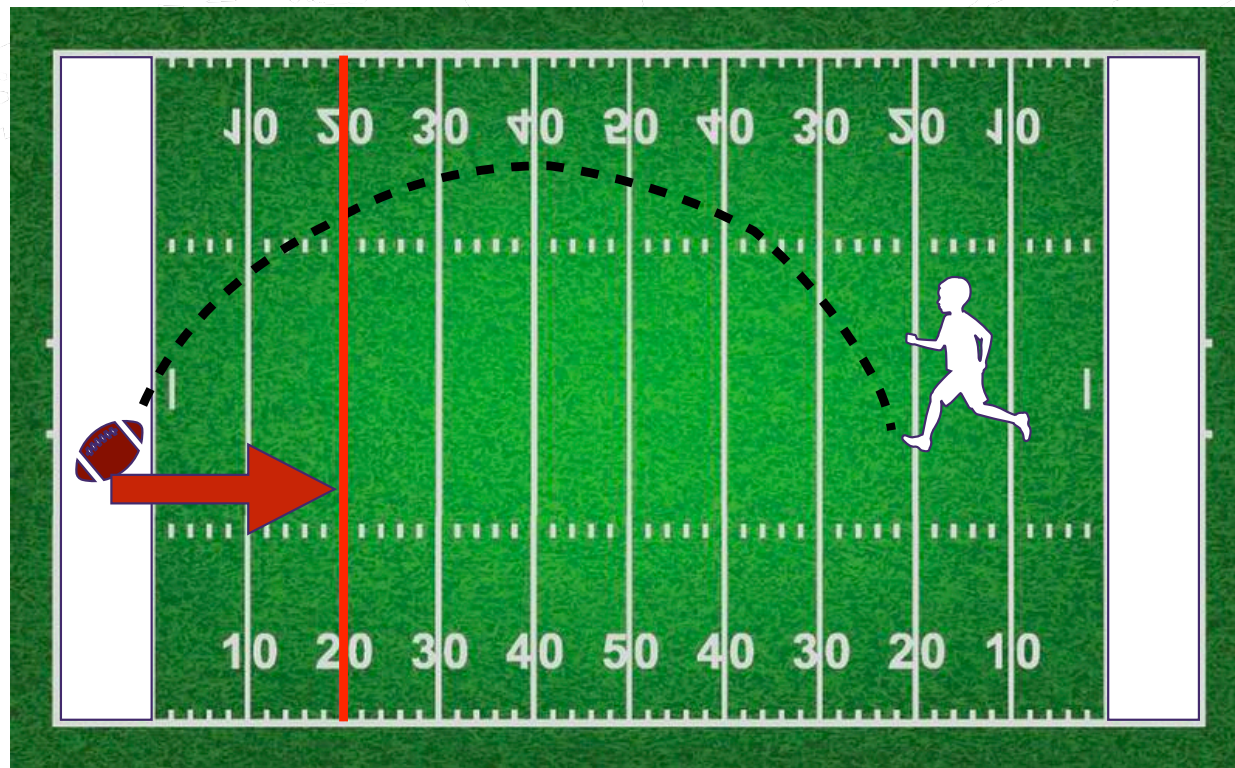
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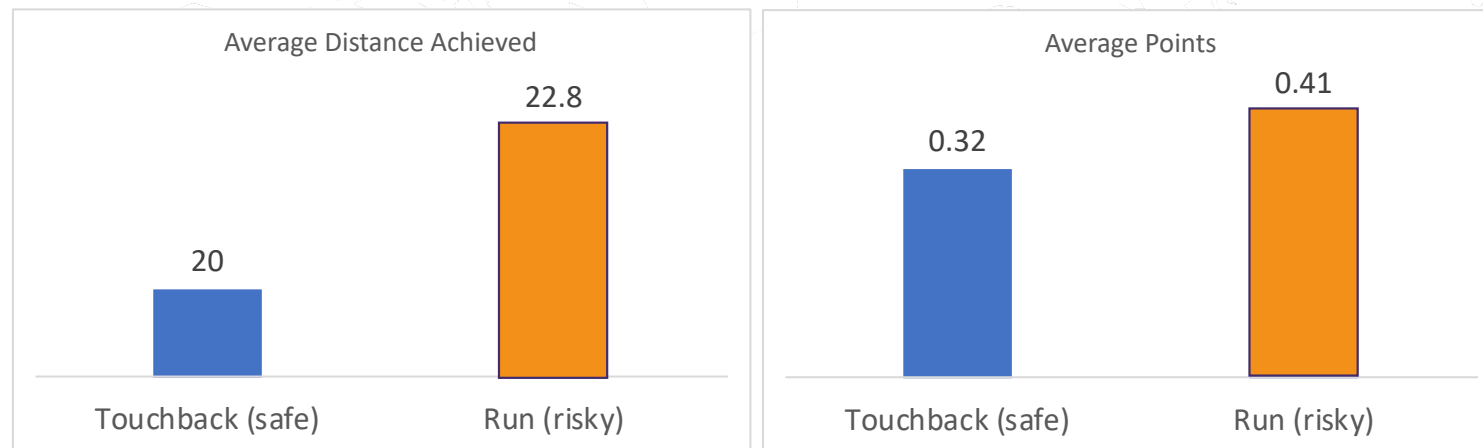
CONSIDER THIS ENDOGENEITY IN AMERICAN FOOTBALL



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CONSIDER THIS ENDOGENEITY IN AMERICAN FOOTBALL



The “high risk” decision is consistently better than the safe play.

CONSIDER THIS ENDOGENEITY IN AMERICAN FOOTBALL

We DO know:

Conditions = great!
Decision = run back (risky)



Conditions = not great!
Decision = touchback (safe)



We DON'T know:

Conditions = not great!
Decision = run back (risky)



Thus, it isn't reasonable to tell more players to make risky decision!

UNRECOGNIZED ENDOGENEITIES / OVB = BIGGEST RISK TO GOOD CRITICAL THINKING WITH DATA & MODELS

You've encountered endogeneities with statistics:

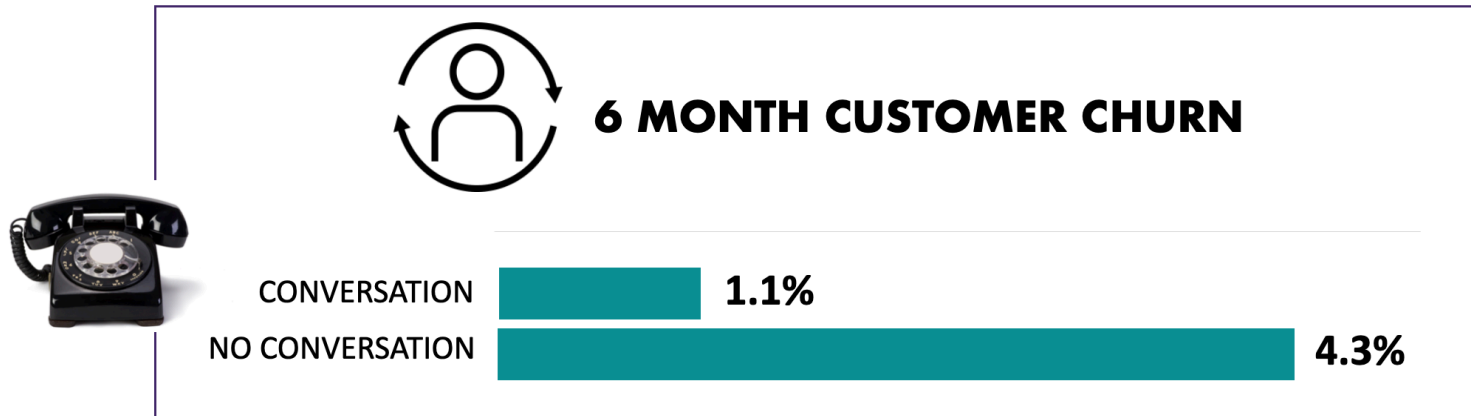
$$y = b_0 + b_1x + e$$

Endogeneity if these
aren't independent

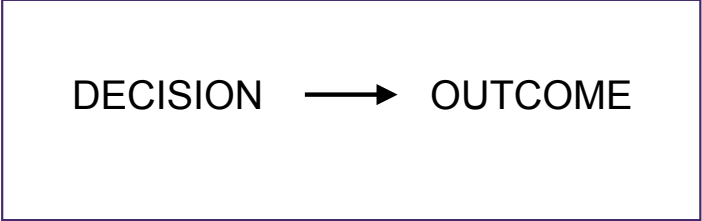
$$\text{Points} = b_0 + b_1\text{Touchback?} + e$$

The conditions in which you make
a decision influence your decision
AND the outcome, independent of
your decision

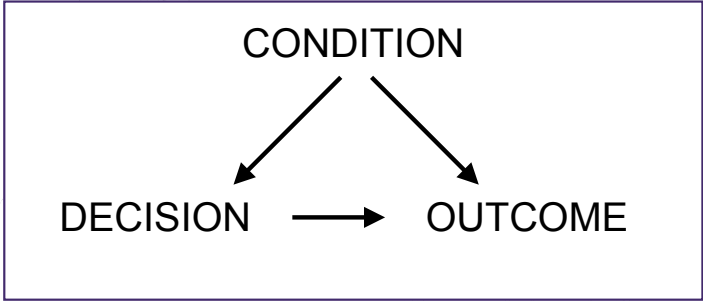
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DECISION → OUTCOME

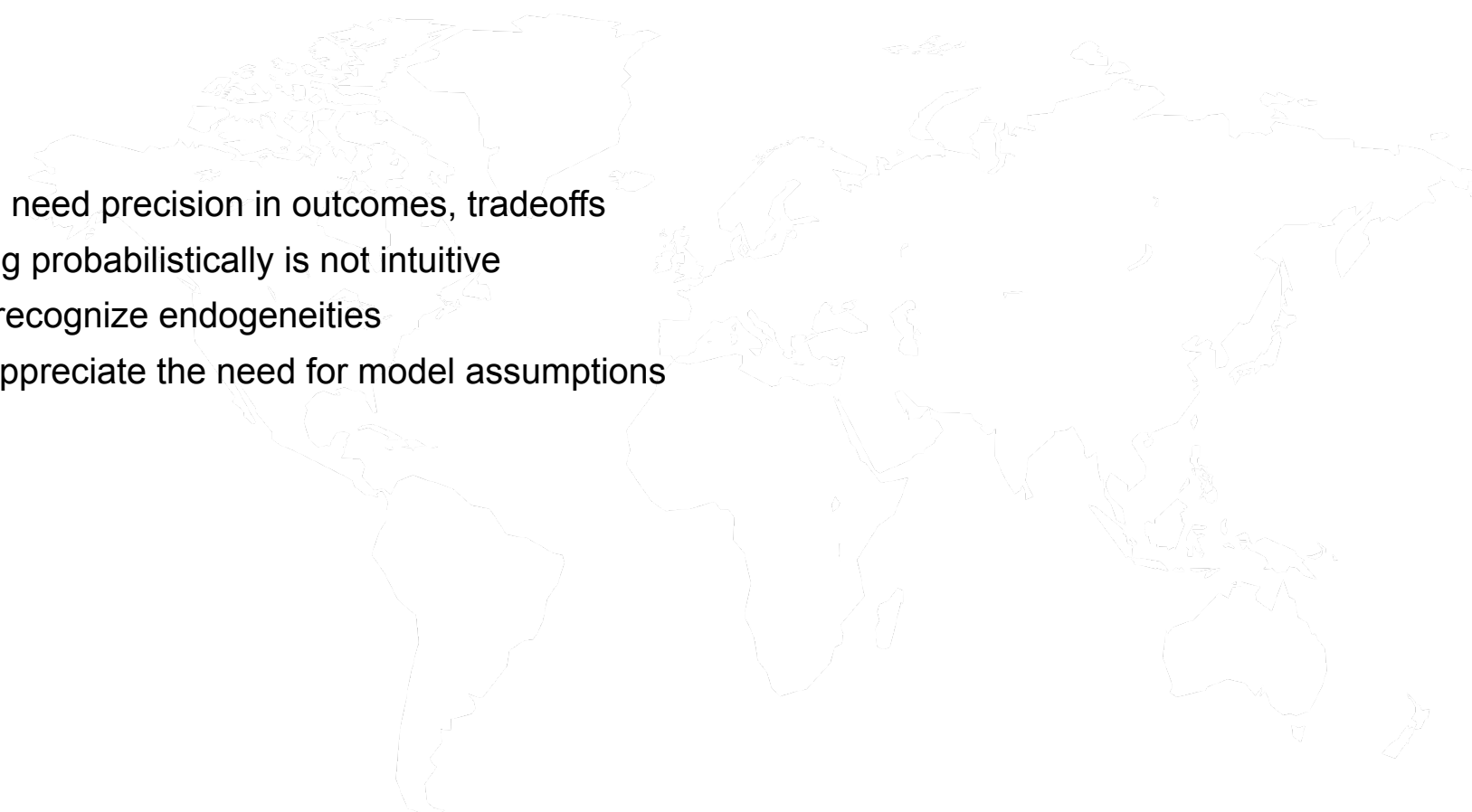


CONDITION
↓ ↓
DECISION → OUTCOME

Did decision cause the outcome?
Or was outcome a byproduct of the condition,
which caused the outcome?

But this happens ALL THE TIME. Business decision-makers try to make decisions in the conditions where they are most likely to be successful!

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YOUR HOMEWORK

Northwestern | Kellogg School of Management

JOEL SHAPIRO

Fly or Drive?

Your job in Chicago has required that that you go to Milwaukee, WI for a meeting at the Milwaukee airport. Is it safer for you to fly or drive?

Assume the following:

- You live very near Chicago's O'Hare airport
- You always wear a seatbelt and are sober while driving
- The distance to Milwaukee is 71 miles
- Last year, there were 40,100 auto traffic deaths in the U.S.
- 90% of plane accidents occur during the takeoff or landing phase
- There are approximately 0.2 deaths per 10 billion miles flown
- The risk of being in a fatal car crash while sober and wearing a seatbelt is only 20% of the risk for the general population

Provide a complete answer to "is it safer to drive or fly?" by doing the following: 1) clearly answer the question and support your answer with the appropriate calculations 2)

SAMPLE ANSWER

RISK OF DEATH, DRIVING

General Risk

(12,000 mi) x (300M people)
= 3.6×10^{12} total miles driven

(40,100 deaths/yr) / (3.6×10^{12} mile/yr)
= 1.114×10^{-8} deaths/mi

Chi:Mil

(1.114×10^{-8} deaths/mi) x 71 mi x 0.2
= **1.581×10^{-7} deaths / trip**

For this 1 trip, I expect 0.0000001581 deaths

RISK OF DEATH, FLYING

General Risk

0.2 deaths / 1×10^{10} mi
= 2×10^{-11} deaths / mi

Chi:Mil

(2×10^{-11} deaths / mi) x 71 mi =
= **1.4×10^{-9} deaths / trip**

For this 1 trip, I expect 0.0000000014 deaths

$$p(\text{driving death}) = 113 * p(\text{flying death})$$

ASSUMPTIONS THAT CONCERN ME

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Overestimate by factor of 2? 4?

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Is flight risk linearly related to distance?

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$p(\text{driving death}) = 1000 * p(\text{flying death})$

