



Software Contracts: Semantics Verification Optimization

Sam Tobin-Hochstadt
Indiana University

Not in this talk

Gradual Types

Metaprogramming

Refinement Types

Concurrent Systems

Performance Tools

Contracts

R. Morris
Editor

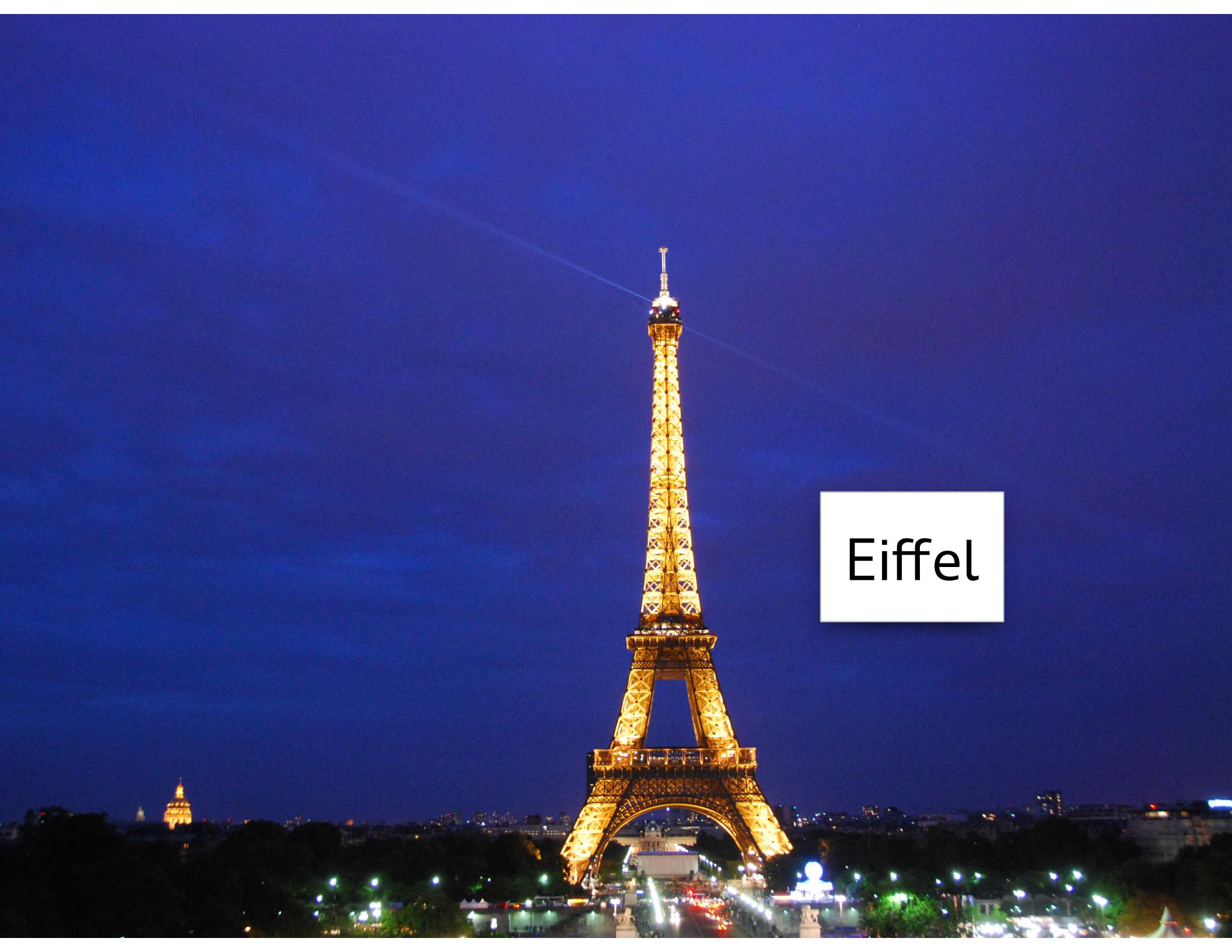
On the Criteria To Be Used in Decomposing Systems into Modules

D.L. Parnas
Carnegie-Mellon University

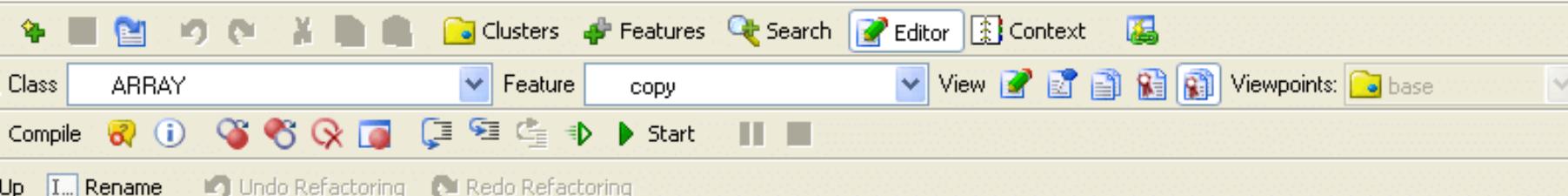
s modularization as a mechanism
bility and comprehensibility of a
the shortening of its development

Introduction

A lucid statement of the philosophy of mod

A photograph of the Eiffel Tower in Paris, France, taken at night. The tower is illuminated from within, casting a warm glow against the dark blue sky. A single beam of light extends from the top of the tower towards the upper left. In the foreground, the Seine River and the Champs de Mars are visible, with various lights reflecting on the water and trees. In the background, the city of Paris is visible under a clear sky.

Eiffel



```

feature -- Element change

    enter (v: like item; i: INTEGER_32)
        -- Replace 'i'-th entry, if in index interval, by 'v'.
        require
            valid_index (i)

    fill (other: CONTAINER [G])
        -- Fill with as many items of 'other' as possible.
        -- The representations of 'other' and current structure
        -- need not be the same.
        -- (from COLLECTION)
        require -- from COLLECTION
            other_not_void: other /= Void
            extendible: extendible

    force (v: like item; i: INTEGER_32)
        -- Assign item 'v' to 'i'-th entry.
        -- Always applicable: resize the array if 'i' falls out of
        -- currently defined bounds; preserve existing items.
        ensure
            inserted: item (i) = v
            higher_count: count >= old count

    put (v: like item; i: INTEGER_32)
        -- Replace 'i'-th entry, if in index interval, by 'v'.
        require -- from TABLE
            valid_index (i)
        require -- from TO_SPECIAL
            valid_index: valid_index (i)
        ensure then -- from INDEXABLE
            insertion_done: item (i) = v
        ensure -- from TO_SPECIAL
            inserted: item (i) = v

    subcopy (other: ARRAY [like item]; start_pos, end_pos, index_pos: INTEGER_32)
        -- Copy items of 'other' within bounds 'start_pos' and 'end_pos'

```

Eiffel

Now available in

- Python
- JavaScript
- Ruby
- C#
- Java
- ...

point-in-module

```
(provide point-in?)  
  
(define (point-in? p x y)  
  (define p-dot  
    (pin-under p x y (disk 1)))  
  (equal?  
    (pict->argb-pixels p-dot)  
    (pict->argb-pixels p)))
```

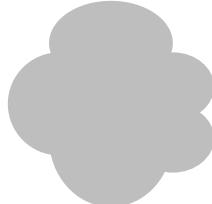
point-in-module

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    (pict->argb-pixels p)))
```

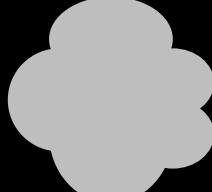
```
(point-in? (cloud 100 100) 0 0)
```

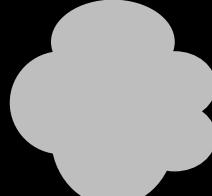
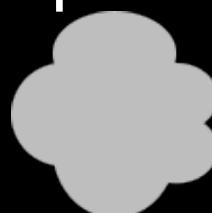
point-in-module

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(define (point-in? p x y)  
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  (equal?  
    (pict->argb-pixels p-dot)  
    (pict->argb-pixels p)))
```

(point-in?  0 0)

```
(define (point-in? p x y)
  (define p-dot
    (pin-under p x y (disk 1)))
  (equal?
    (pict->argb-pixels p-dot)
    (pict->argb-pixels p)))
```

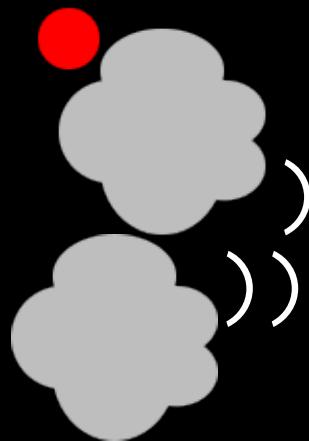
(point-in?  0 0)

```
(define p-dot
  (pin-under  0 0 (disk 1)))
(equal?
  (pict->argb-pixels p-dot)
  (pict->argb-pixels )))
```

```
(define p-dot  
  (lambda (pict)  
    (let ([dot (pict->dot pict)])  
      (if (empty? dot)  
          (pict->empty-pict pict)  
          (let ([x (dot->x dot)]  
                [y (dot->y dot)]  
                [r (dot->r dot)])  
            (pict->empty-pict pict)  
            (dot-set! (pict->empty-pict pict)  
                     (dot-make (dot-x dot)  
                             (dot-y dot)  
                             (dot-r dot)))))))
```



```
(equal?  
  (pict->argb-pixels  
   (pict->argb-pixels
```

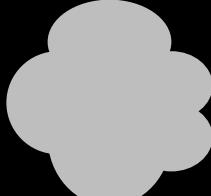


```
(equal?
#"\"0\377\377\377\0\3...")  
#"\"377\377\0\0\377\3..."))
```

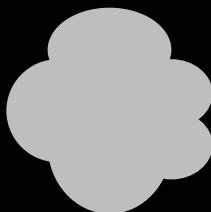
point-in-module

```
(provide point-in?)  
  
(define (point-in? p x y)  
  (define p-dot  
    (pin-under p x y (disk 1)))  
  (equal?  
    (pict->argb-pixels p-dot)  
    (pict->argb-pixels p)))
```

```
(point-in? (cloud 100 100) 50 50)
```

```
(define p-dot
  (pin-under  50 50 (disk 1)))
(equal?
  (pict->argb-pixels p-dot)
  (pict->argb-pixels )))
```

```
(define p-dot  
  (lambda (p1 p2)  
    (equal?  
      (pict->argb-pixels p1)  
      (pict->argb-pixels p2))))
```



(equal?
(pict->argb-pixels
(pict->argb-pixels



```
(equal?
#"\"0\377\377\377\0\3...")  
#"\"0\377\377\377\0\3..."))
```

```
> (point-in? (cloud 100 100) #f #f)
```

```
> (point-in? (cloud 100 100) #f #f)
pin-under: contract violation
  expected: (or/c real? pict-path?)
  given: #f
  in: the dx/fp argument of
    (->i
      ((base pict-convertible?))
      (dx/fp (or/c real? pict-path?)))
      (dy/f
        (dx/fp)
        (if (real? dx/fp)
            real?
            (->
              pict-convertible?
              pict-path?
              (values real? real?))))
      (pict pict-convertible?))
      (result pict?))
contract from: <pkgs>/pict-lib/pict/main.rkt
blaming: point-in-module
(assuming the contract is correct)
```

```
> (point-in? (cloud 100 100) #f #f)
pin-under: contract violation
expected: (or/c real? pict-path?)
given: #f
in: the dx/fp argument of
  (->i
    ((base pict-convertible?))
    (dx/fp (or/c real? pict-path?)))
    (dy/f
      (dx/fp)
      (if (real? dx/fp)
          real?
          (->
            pict-convertible?
            pict-path?
            (values real? real?))))))
  (pict pict-convertible?))
```

blaming: point-in-module

```
(define p-dot
  (pin-under #f #f (disk 1)))
(equal?
 (pict->argb-pixels p-dot)
 (pict->argb-pixels ))
```

(-> pict? real? real?
boolean?)

point-in-module

```
(provide/contract
[point-in? (-> pict? real? real?
                      boolean?)])
(define (point-in? p x y)
  (define p-dot
    (pin-under p x y (disk 1)))
  (equal?
    (pict->argb-pixels p-dot)
    (pict->argb-pixels p)))
```

point-in-module

```
(provide/contract
[point-in? (-> pict? real? real?
                      boolean?)])
(define (point-in? p x y)
  (define p-dot
    (pin-under p x y (disk 1)))
  (equal?
    (pict->argb-pixels p-dot)
    (pict->argb-pixels p)))
```

```
(point-in? (cloud 100 100) #f #f)
```

point-in-module

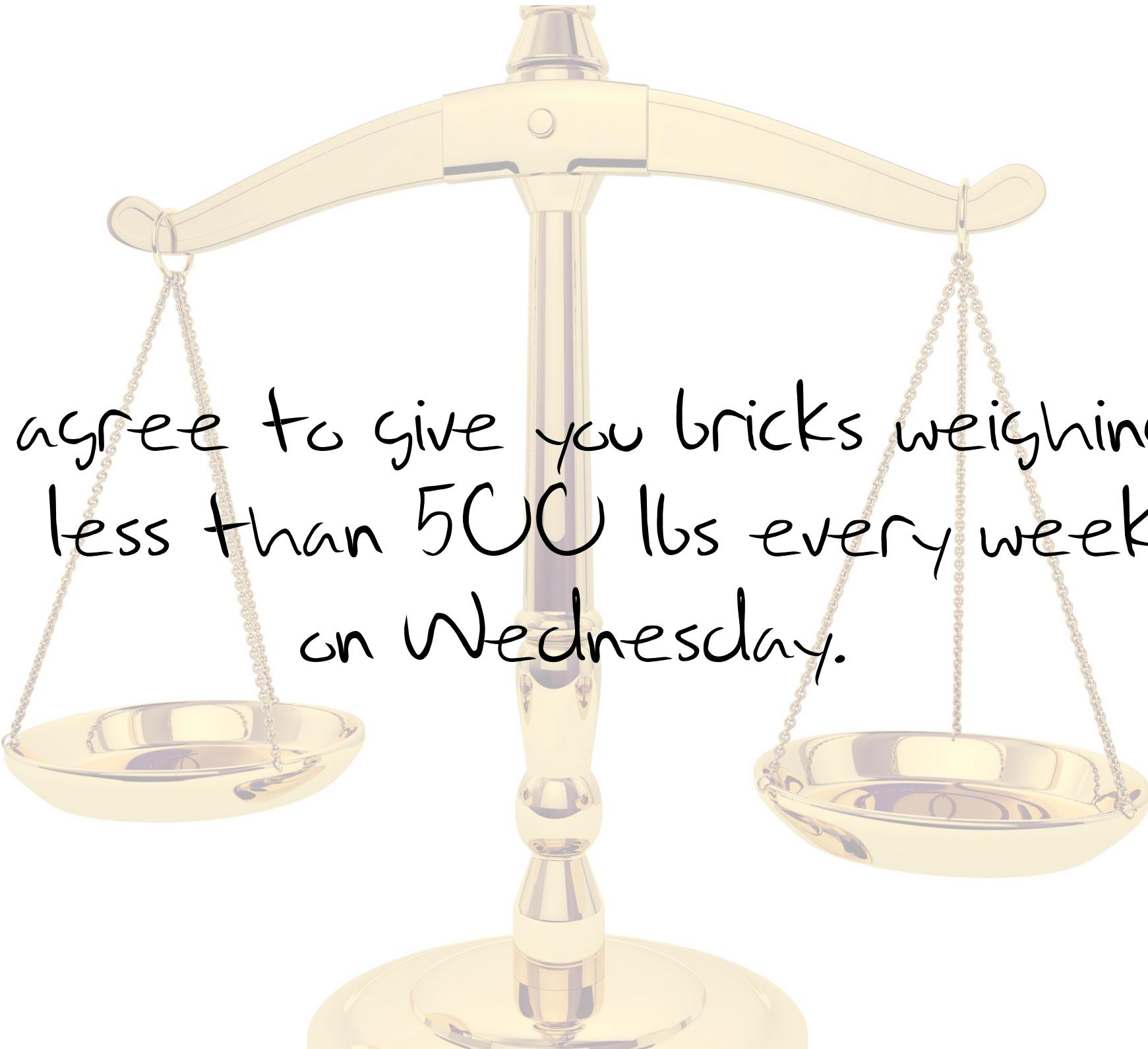
```
(provide/contract
[point-in? (-> pict? real? real?
                      boolean?)])
(define (point-in? p x y)
  (define p-dot
    (pin-under p x y (disk 1)))
  (equal?
    (pict->argb-pixels p-dot)
    (pict->argb-pixels p)))
```

(point-in?  #f #f)

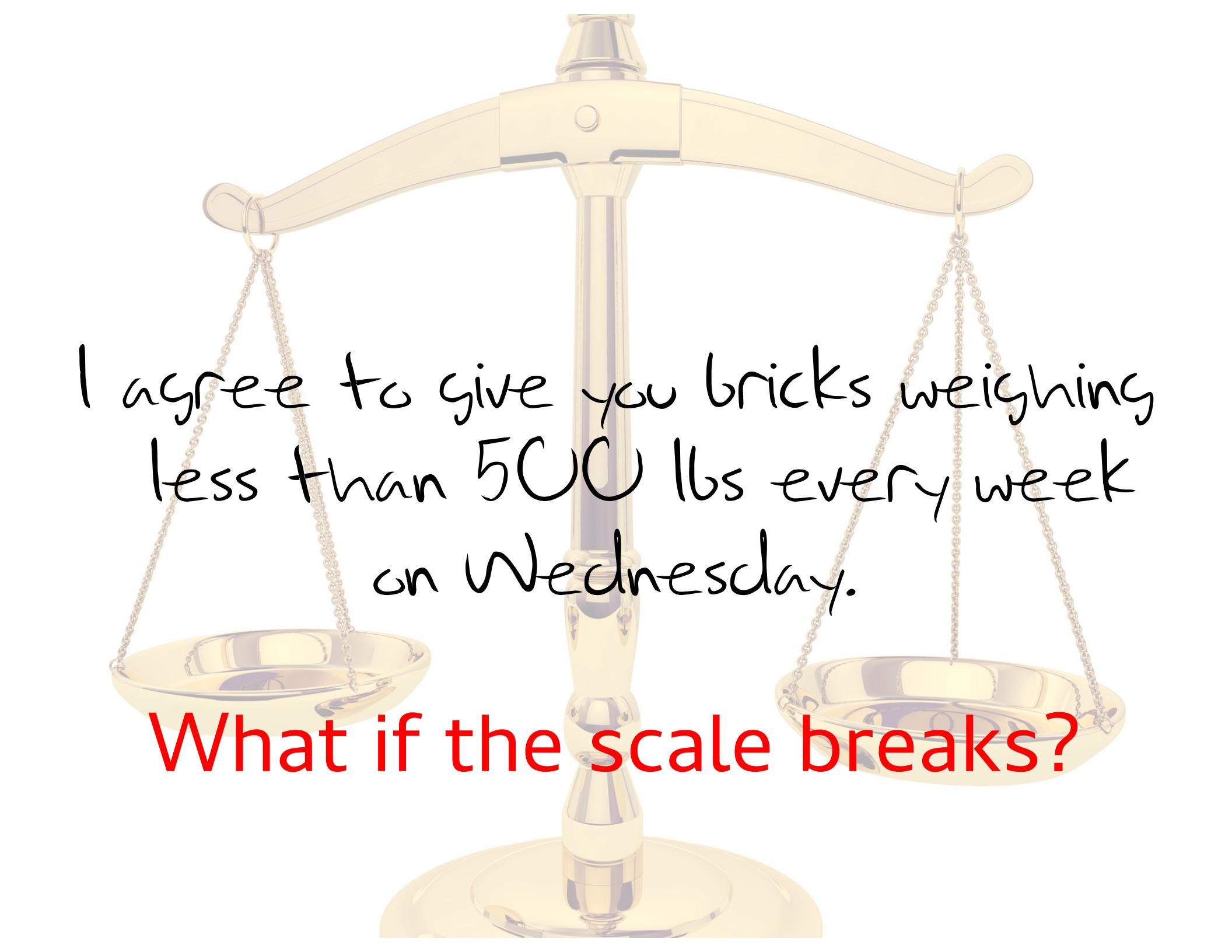
point-in?: contract violation
expected: real?
given: #f
in: the 2nd argument of
 (-> pict? real? real? boolean?)
contract from: point-in-module
blaming: top-level
(assuming the contract is correct)

Semantics

Signature



I agree to give you bricks weighing
less than 500 lbs every week
on Wednesday.



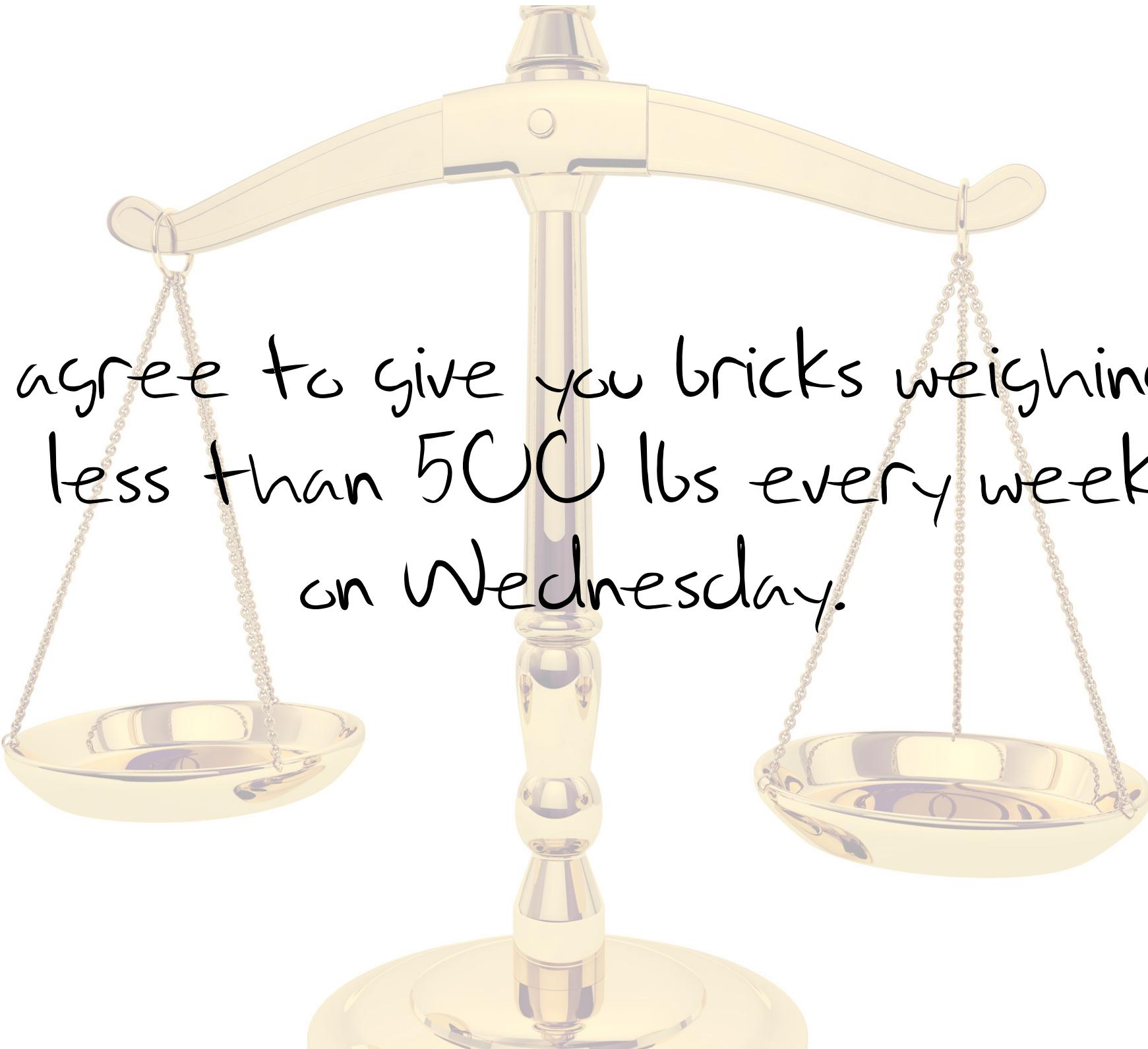
I agree to give you bricks weighing less than 500 lbs every week on Wednesday.

What if the scale breaks?

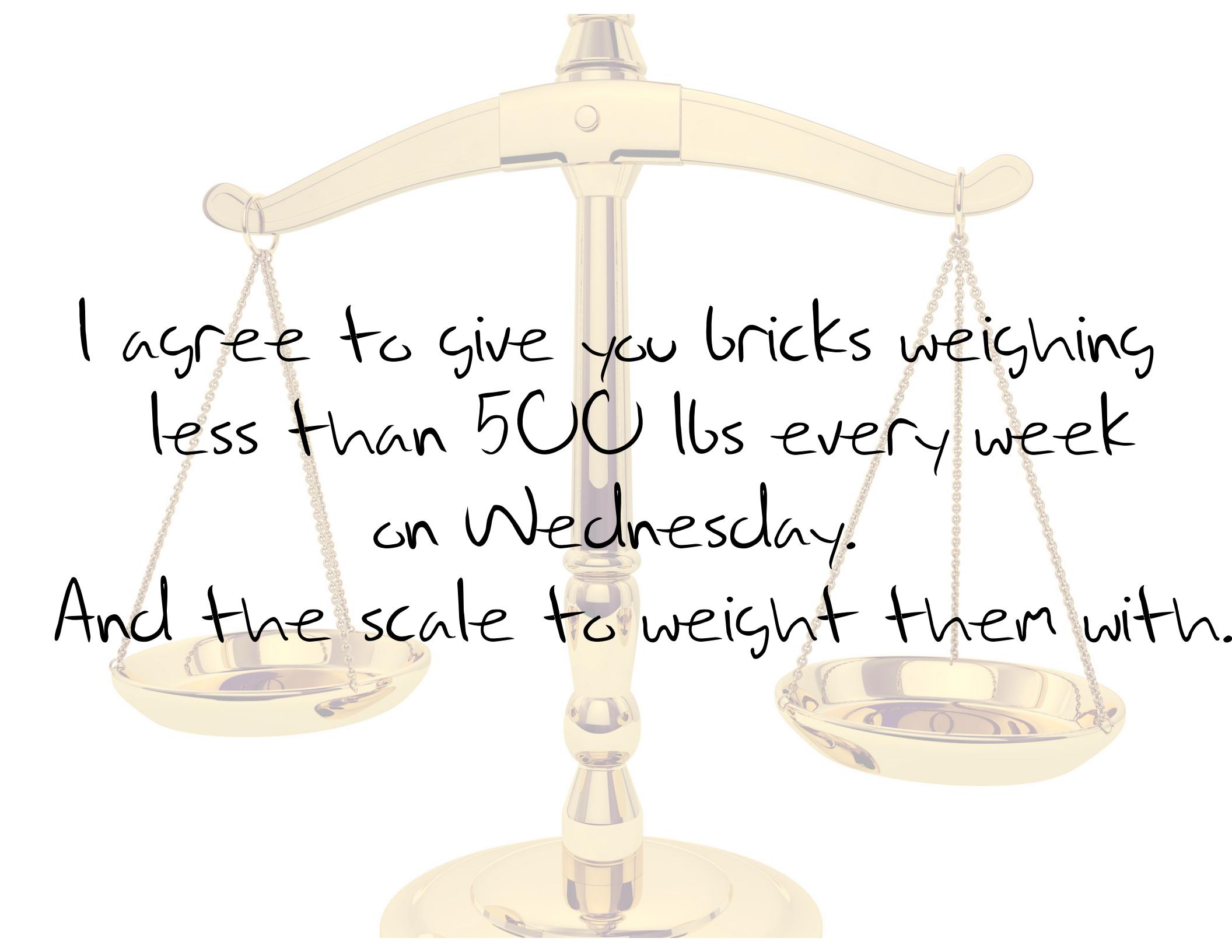
I agree to give you less than £1000 every week.

Contracts can go wrong.

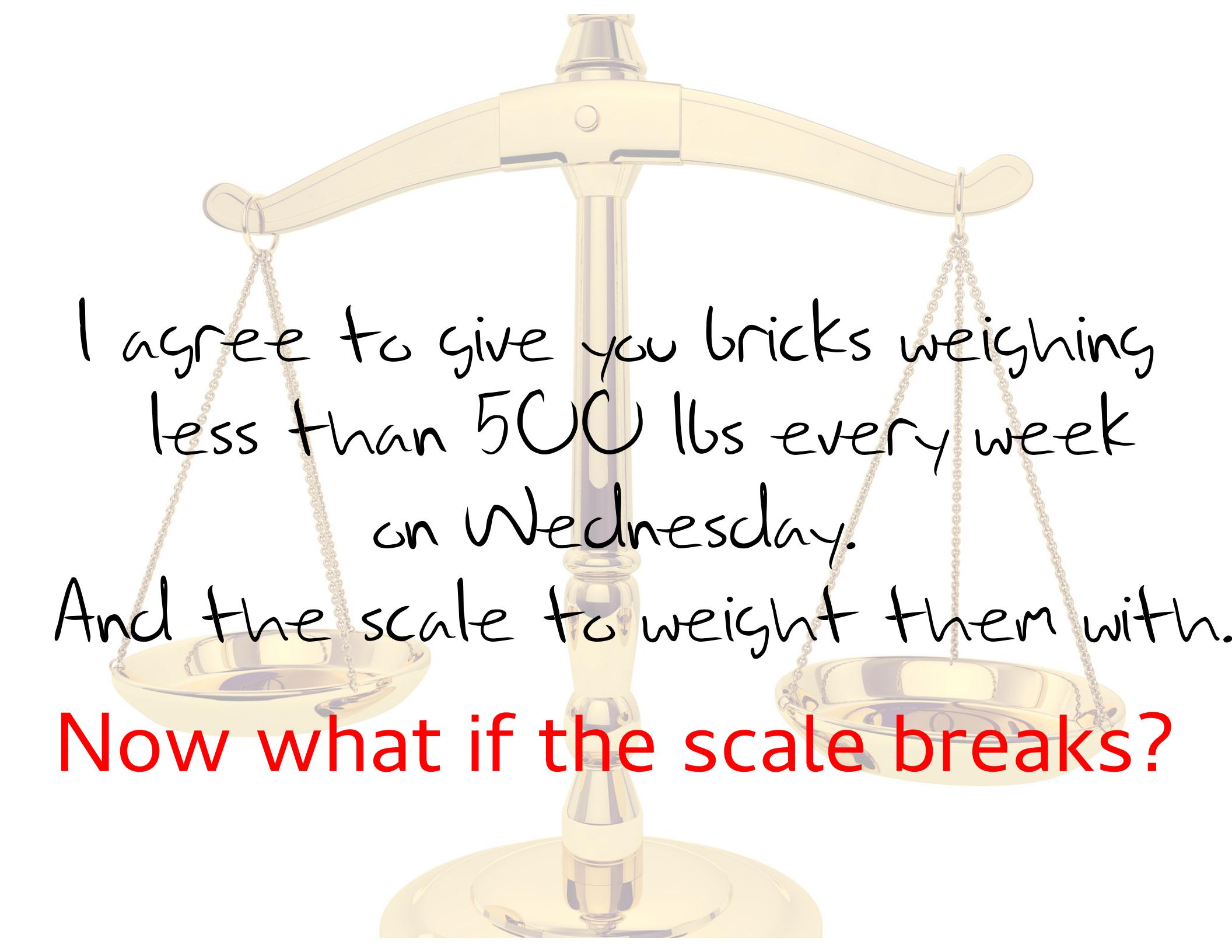
What if the scale breaks?



I agree to give you bricks weighing
less than 500 lbs every week
on Wednesday.



I agree to give you bricks weighing
less than 500 lbs every week
on Wednesday.
And the scale to weight them with.



I agree to give you bricks weighing less than 500 lbs every week on Wednesday.
And the scale to weight them with.

Now what if the scale breaks?

Dependent contracts

```
(provide
[construction
(->d [b bricks?]
      [scale (-> any/c weight)]
      #:pre (< (scale b) 500)
      any)])
(construction heavy-bricks scale)
```

Dependent contracts

```
(provide
[construction
(->d [b bricks?]
      [scale (-> <1000/c weight)]
      #:pre (< (scale b) 500)
      any)])
```

Dependent contracts

```
(provide
[construction
(->d [b bricks?]
      [scale (-> <1000/c weight)]
      #:pre (< (scale b) 500)
      any)])
(construction heavy-bricks fragile-scale)
```

Dependent contracts

```
(provide  
[construction  
(->d [b bricks?]  
[scale (->e [c weight])  
#:>pre-e b) 500)  
any . Who should be blamed?  
(construction heavy-bricks fragile-scale)
```

Solution: Complete Blame

- Says who should be blamed in tricky cases
- Ensures that contracts are complete
- Helps with gradual typing!

Semantics II

Many approaches to contracts

- Check everything now
- Check everything now, in parallel
- Check when needed
- ...

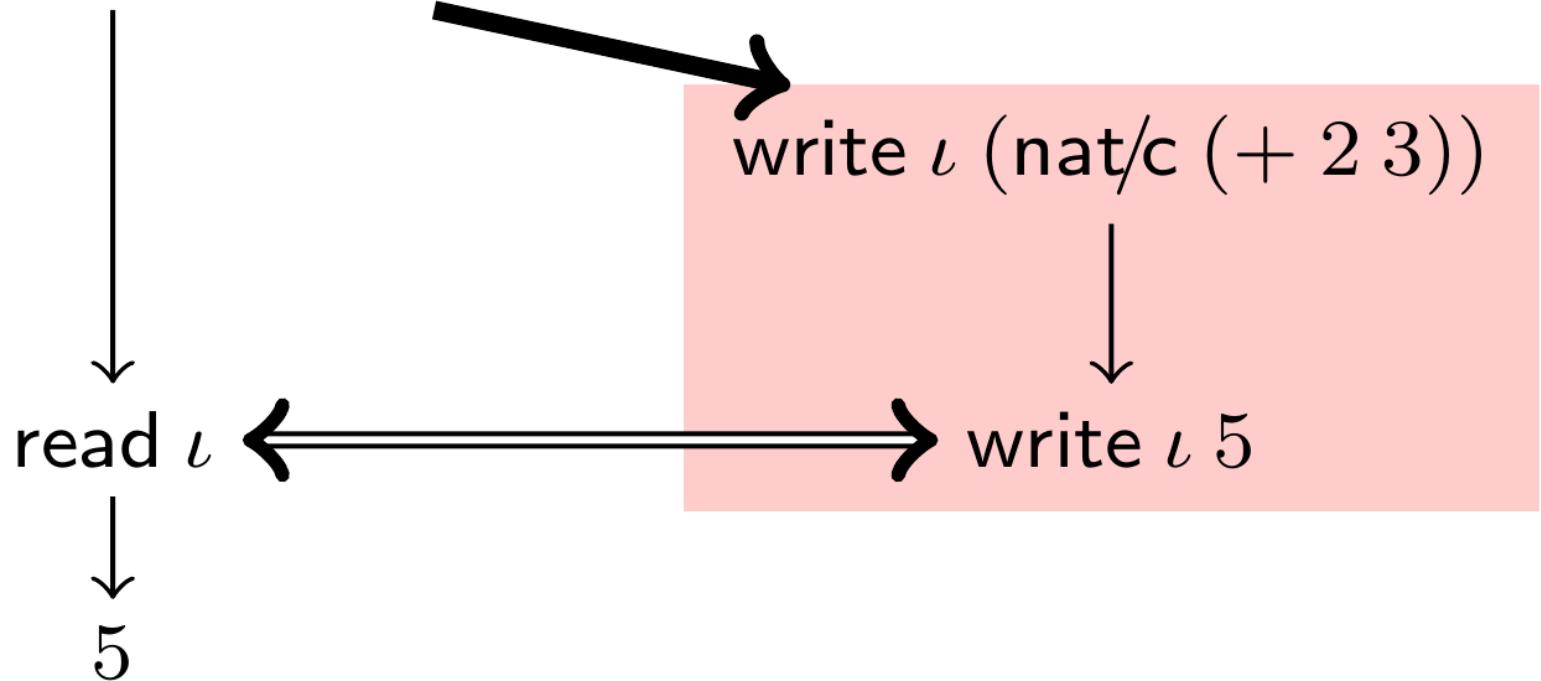
Many approaches to contracts

- Check everything now
- Check everything now
- Check when needed
- ...

Insight: communicating processes

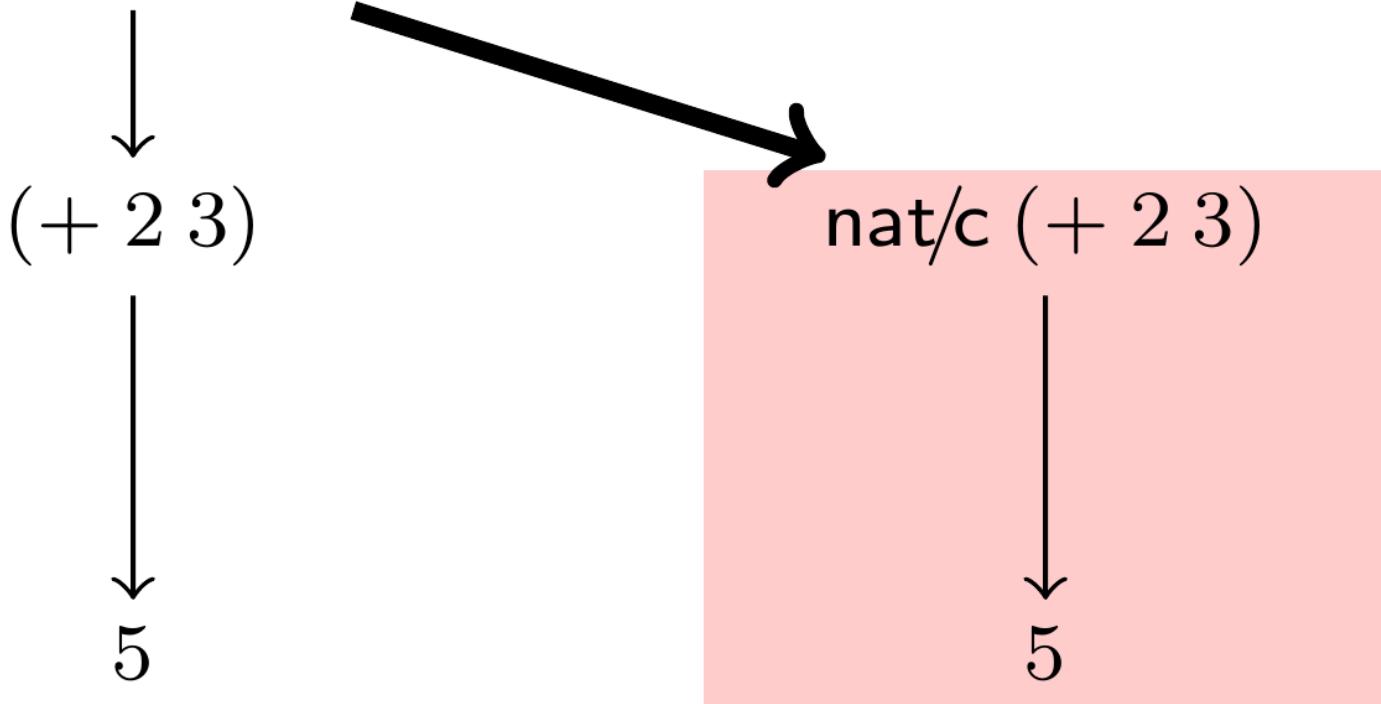
Eager Monitoring

check nat/c eager (+ 2 3)

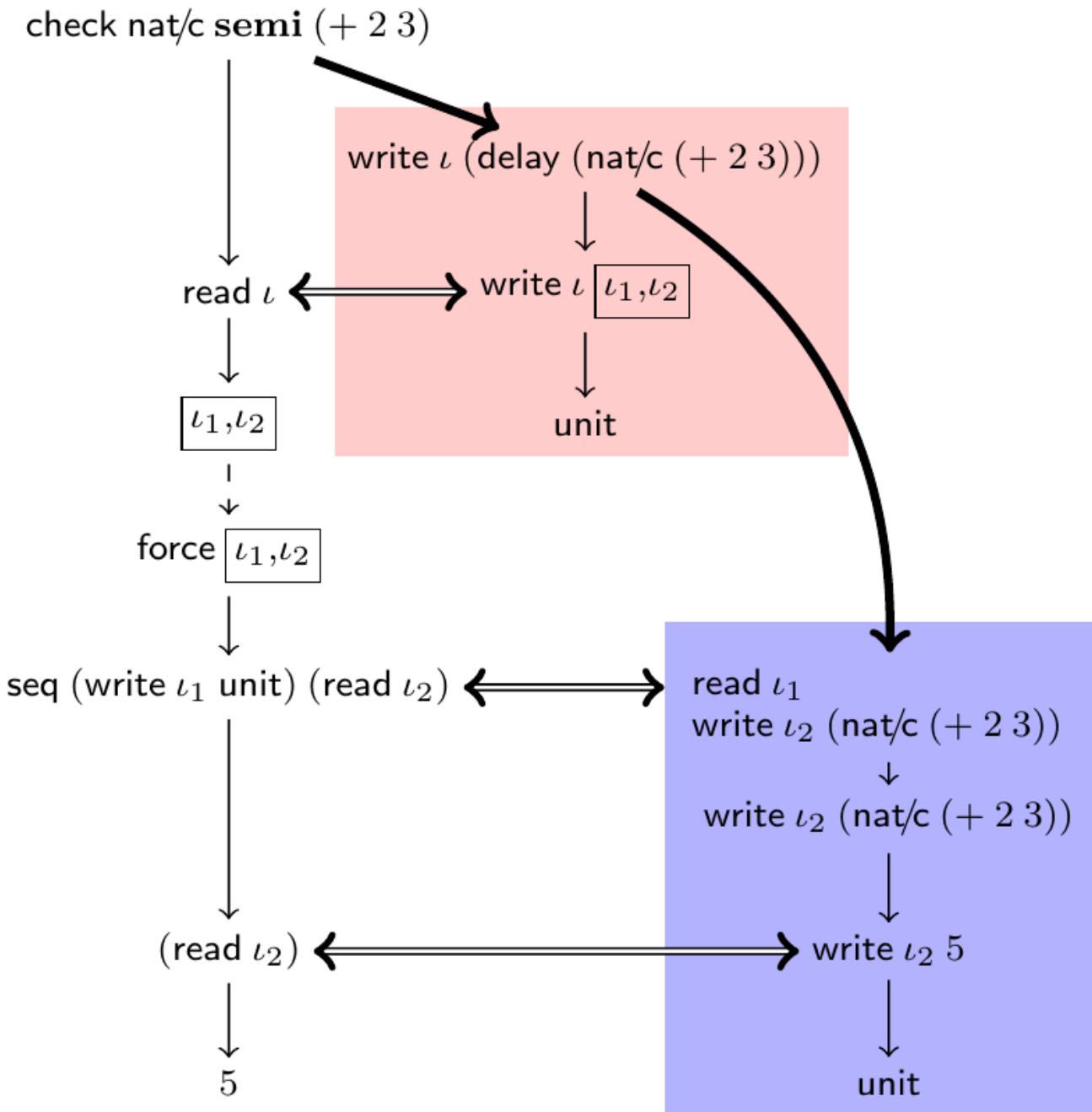


Asynchronous Monitoring

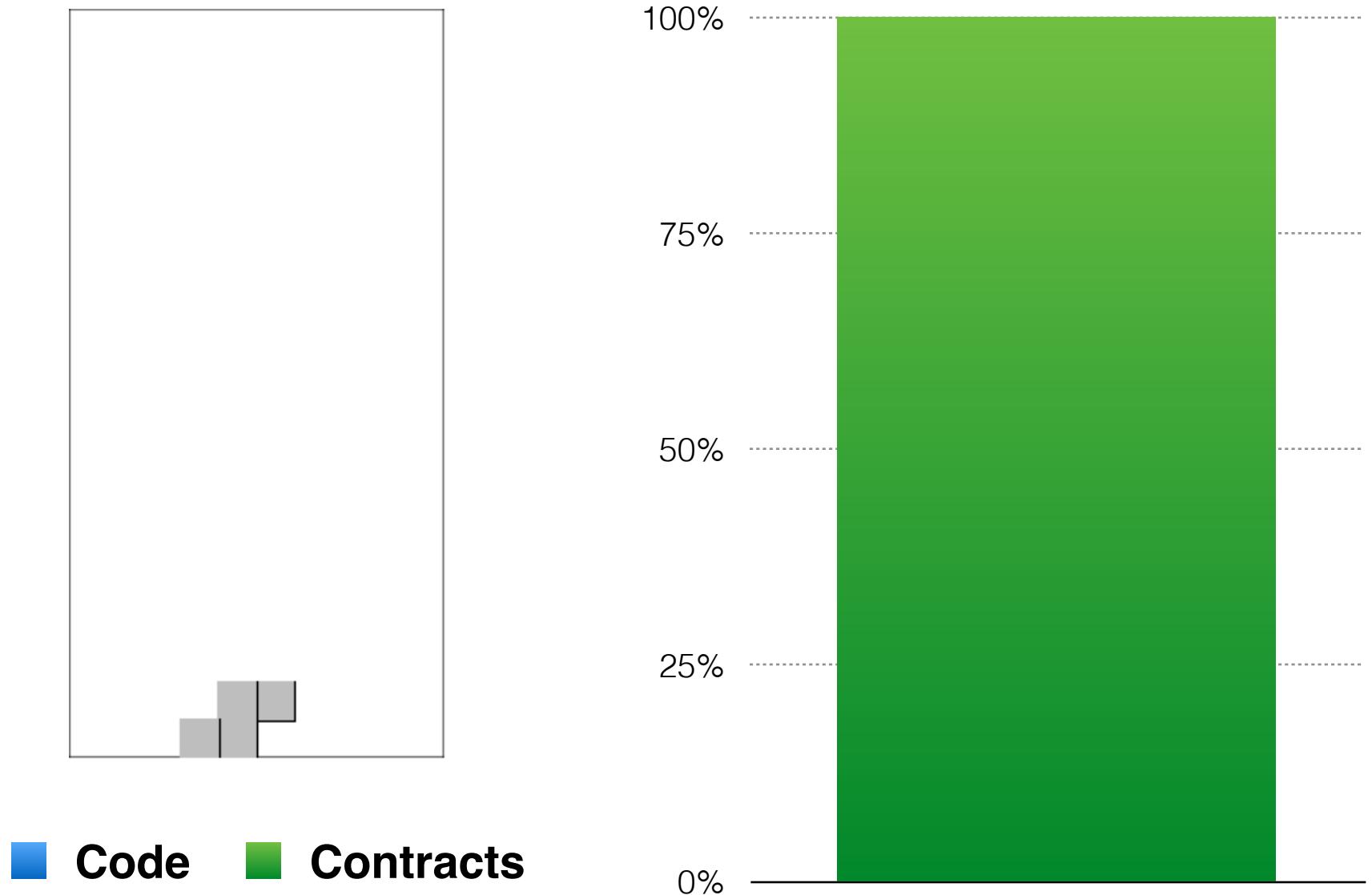
check nat/c **async** (+ 2 3)

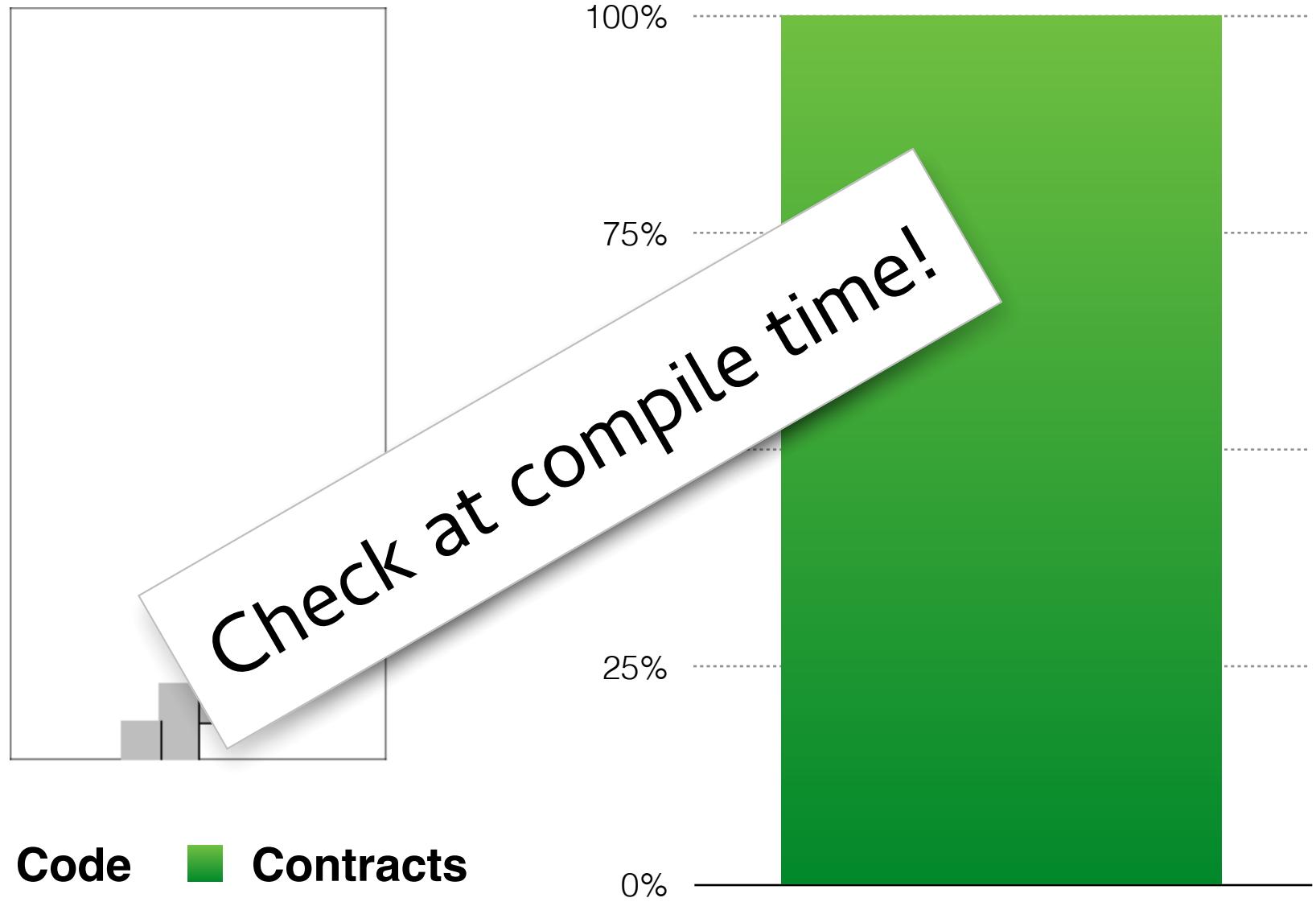


Semi-Eager Monitoring



Verification





Racket Users ›

DrRacket internal error

1 post by 2 authors



Alex Knauth

4/22/15



Other recipients: users@racket-lang.org

I'm not sure how it got into this state, but now every time I start typing something or anything like that I get a DrRacket internal error window saying:

hash-ref: contract violation

 expected: hash?

 given: #f

 argument position: 1st

 other arguments...:

 'configure-runtime

 '()

 context...:

 /Applications/Racket/April-16/Racket v6.2.0.2/share/pkgs/drracket/drracket/private/syncheck/blueboxes-gui.rkt:450:4:
 compute-tag+rng method in ...ck/blueboxes-gui.rkt:175:2

 /Applications/Racket/April-16/Racket v6.2.0.2/share/pkgs/gui-lib/framework/private/coroutine.rkt:47:20

 /Applications/Racket/April-16/Racket v6.2.0.2/share/pkgs/gui-lib/framework/private/coroutine.rkt:56:0: coroutine-run

 /Applications/Racket/April-16/Racket v6.2.0.2/collects/racket/contract/private/arrow-val-first.rkt:265:18

 /Applications/Racket/April-16/Racket v6.2.0.2/share/pkgs/drracket/drracket/private/syncheck/blueboxes-gui.rkt:414:4:
 update-the-strs method in ...ck/blueboxes-gui.rkt:175:2

 /Applications/Racket/April-16/Racket v6.2.0.2/share/pkgs/gui-lib/framework/private/logging-timer.rkt:41:0: log-
 timeline/proc

Racket Users >

DrRacket internal error

1 post by 2 authors

G+1



Alex Knauth

4/22/15



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/Applications/Racket/April-16/Racket v6.2.0.2/share/pkgs/drracket/drracket/private/syncheck/blueboxes-gui.rkt:414:4:

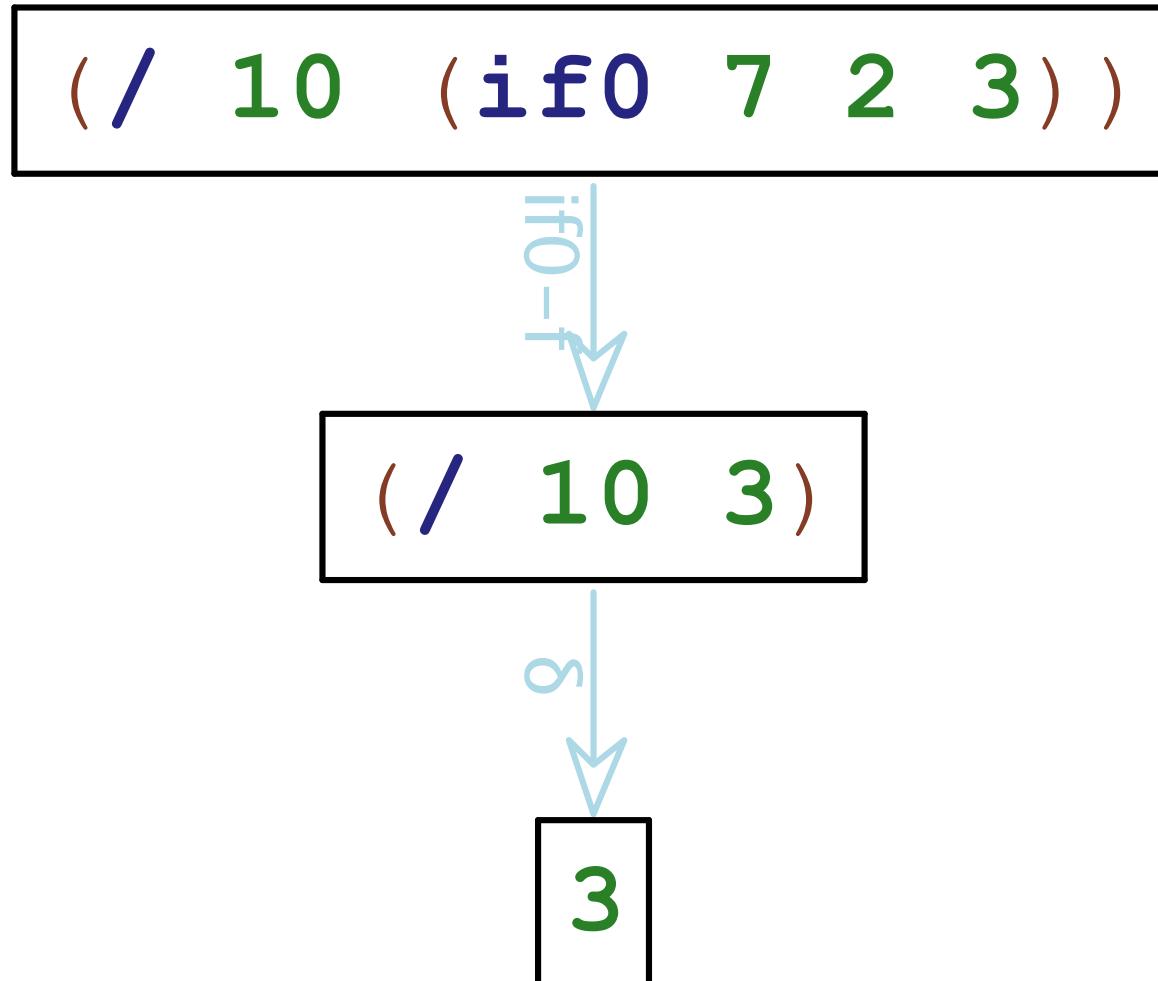
update-the-strs method in ...ck/blueboxes-gui.rkt:175:2

/Applications/Racket/April-16/Racket v6.2.0.2/share/pkgs/gui-lib/framework/private/logging-timer.rkt:41:0: log-timeline/proc

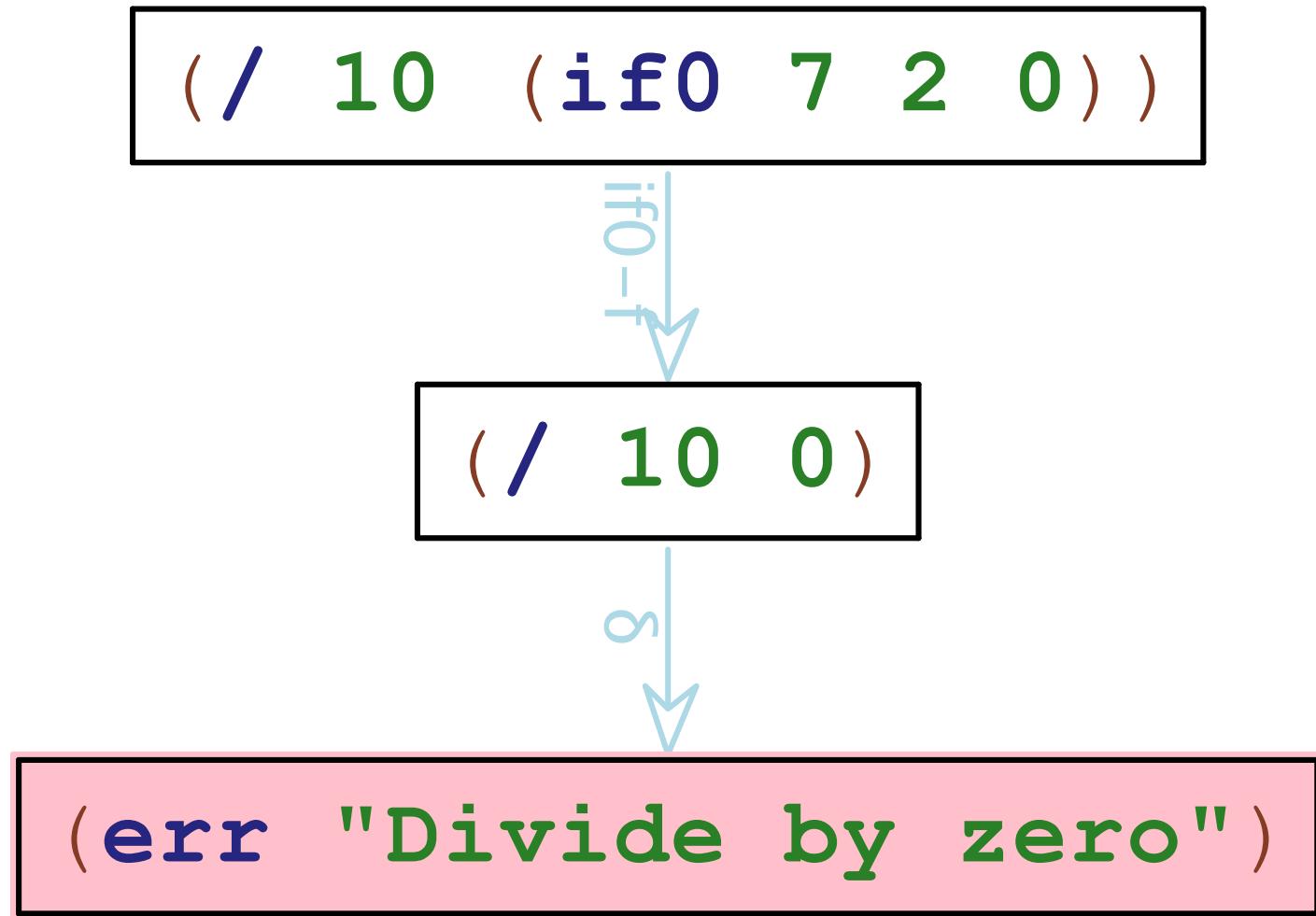
Check at compile time!

A simple language

A simple language

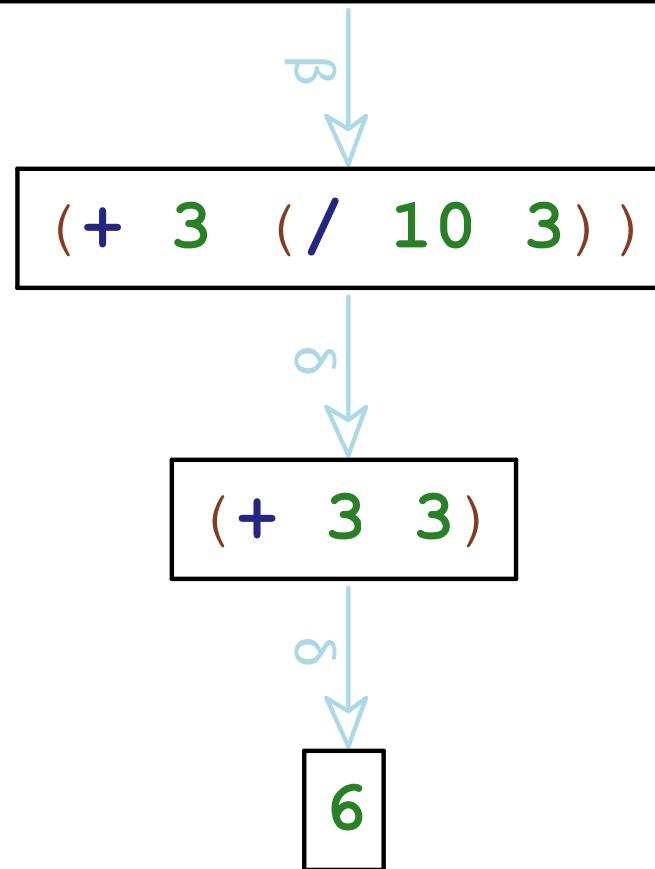


A simple language

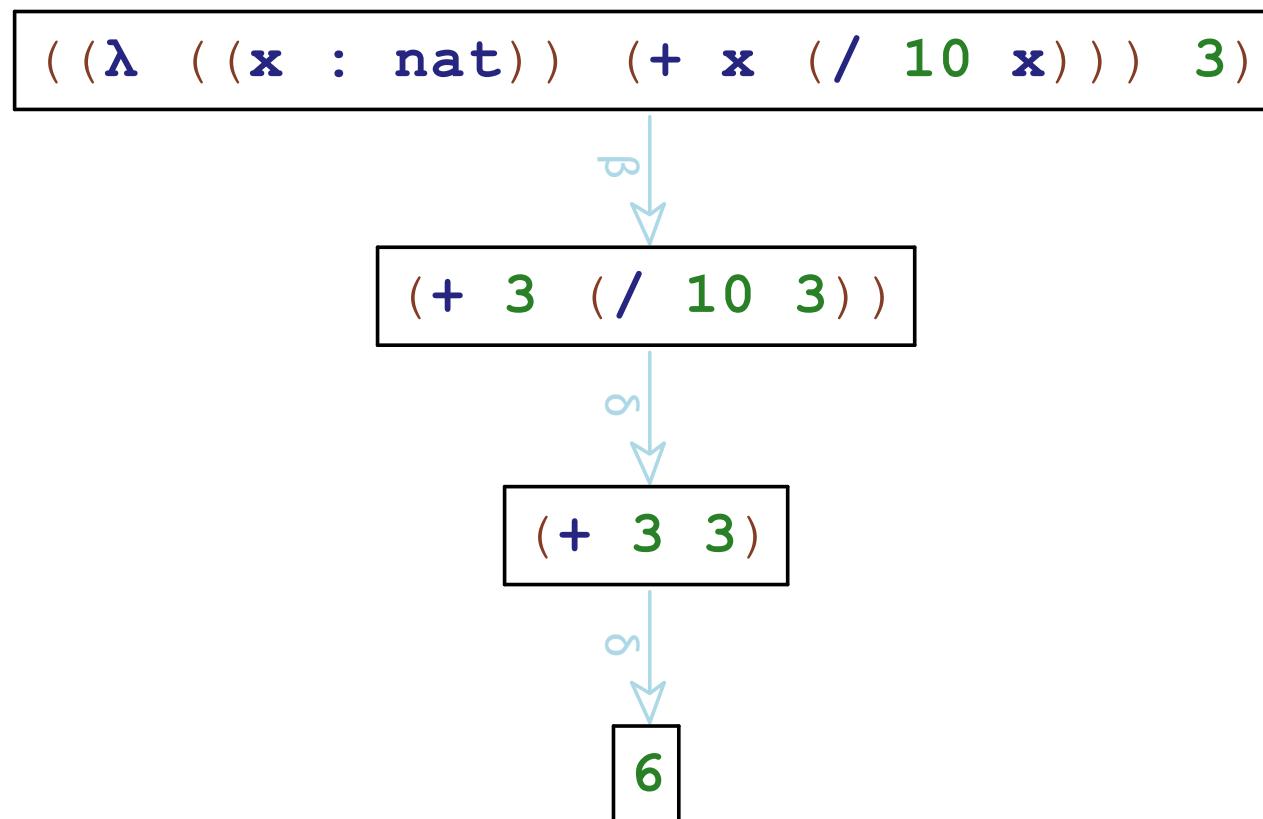


A simple language

```
( (λ ( (x : nat) ) (+ x (/ 10 x)) ) 3)
```



A simple language



A simple language

```
( (λ ( (f : (nat -> nat)) ) (f 3) )  
  (λ ( (x : nat) ) (+ x (/ 10 x)) ) )
```

β

```
( (λ ( (x : nat) ) (+ x (/ 10 x)) ) 3)
```

β

```
( + 3 (/ 10 3) )
```

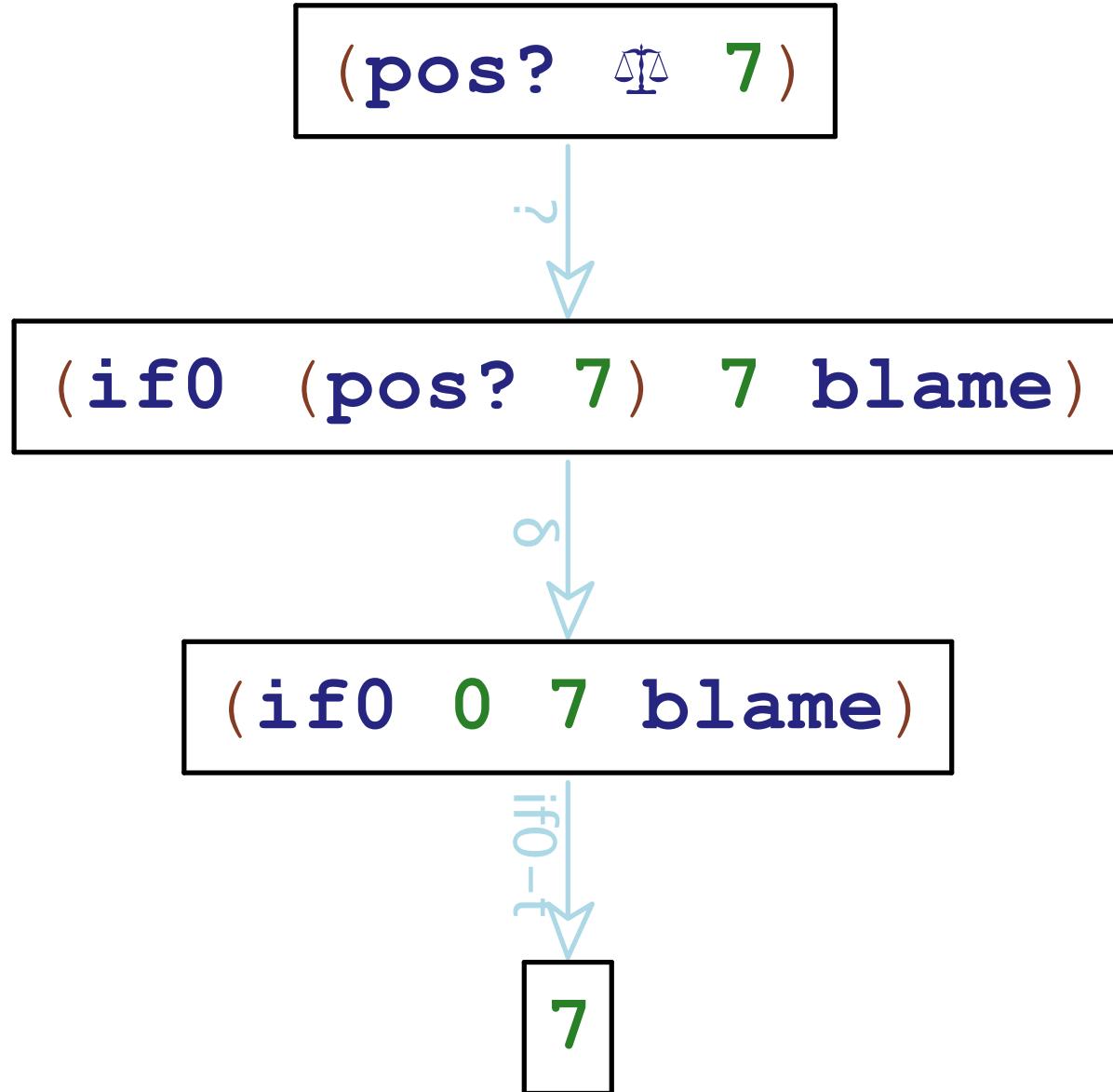
δ

```
( + 3 3 )
```

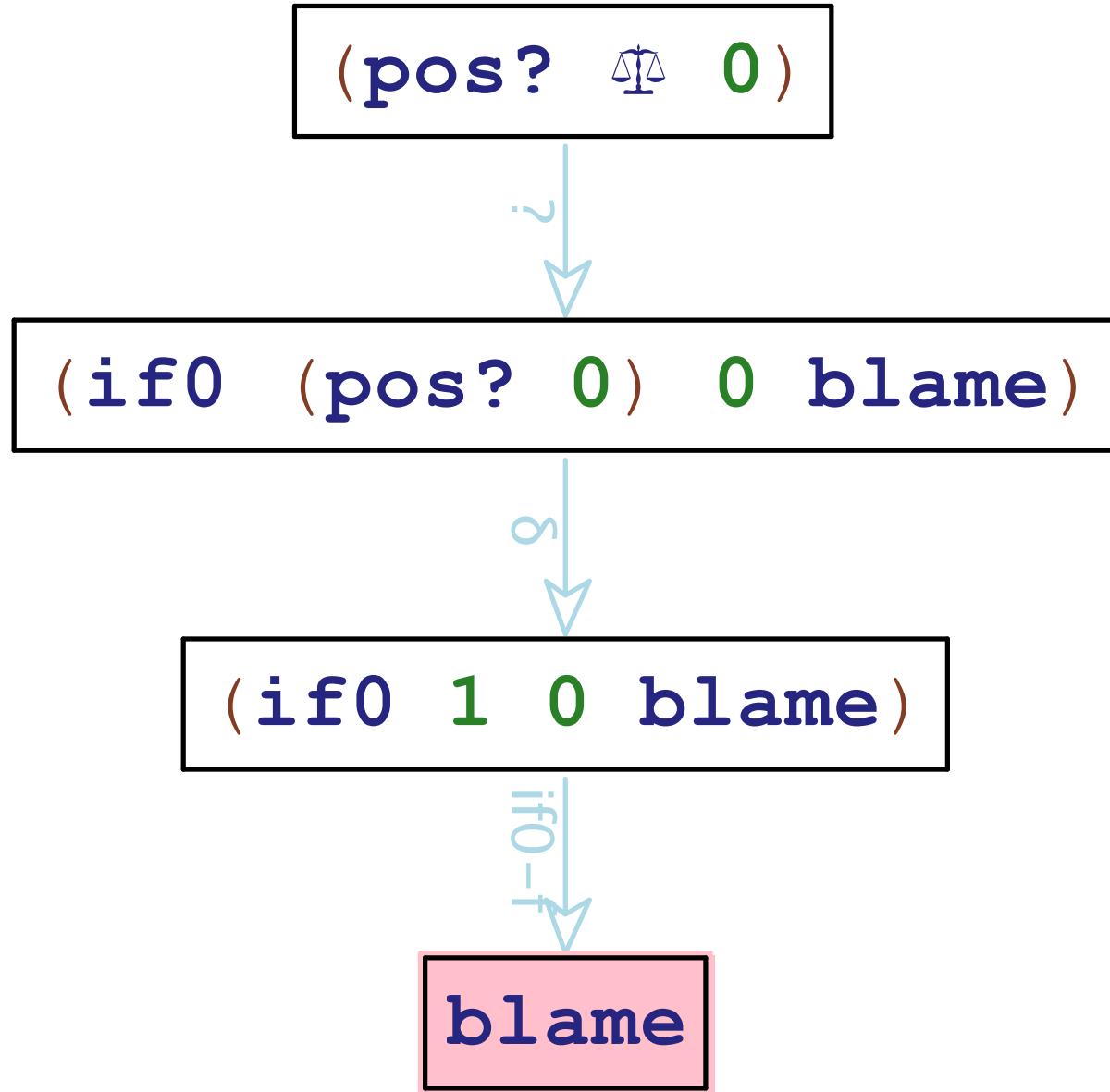
δ

6

A simple language



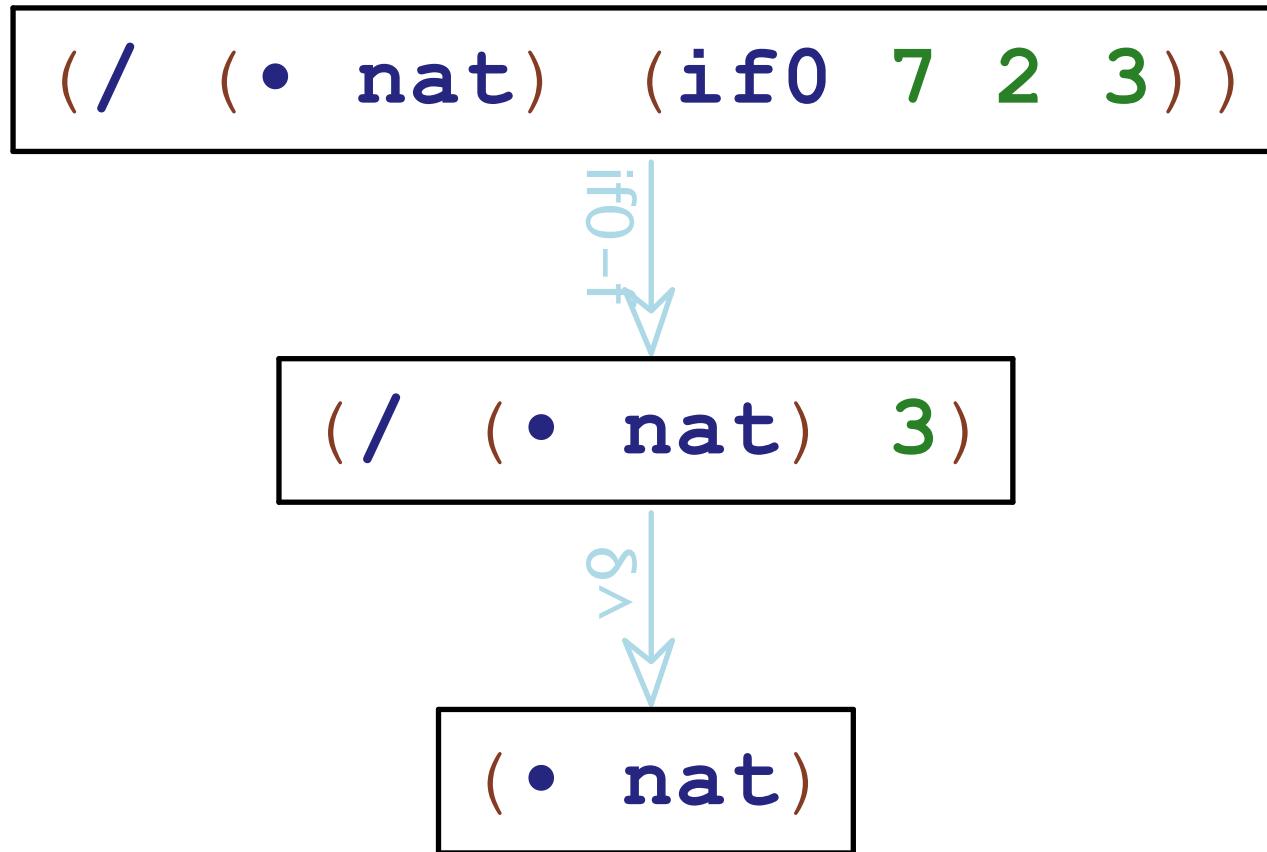
A simple language



With abstract values

```
( /  ( •  nat)  (if0 7 2 3) )
```

With abstract values



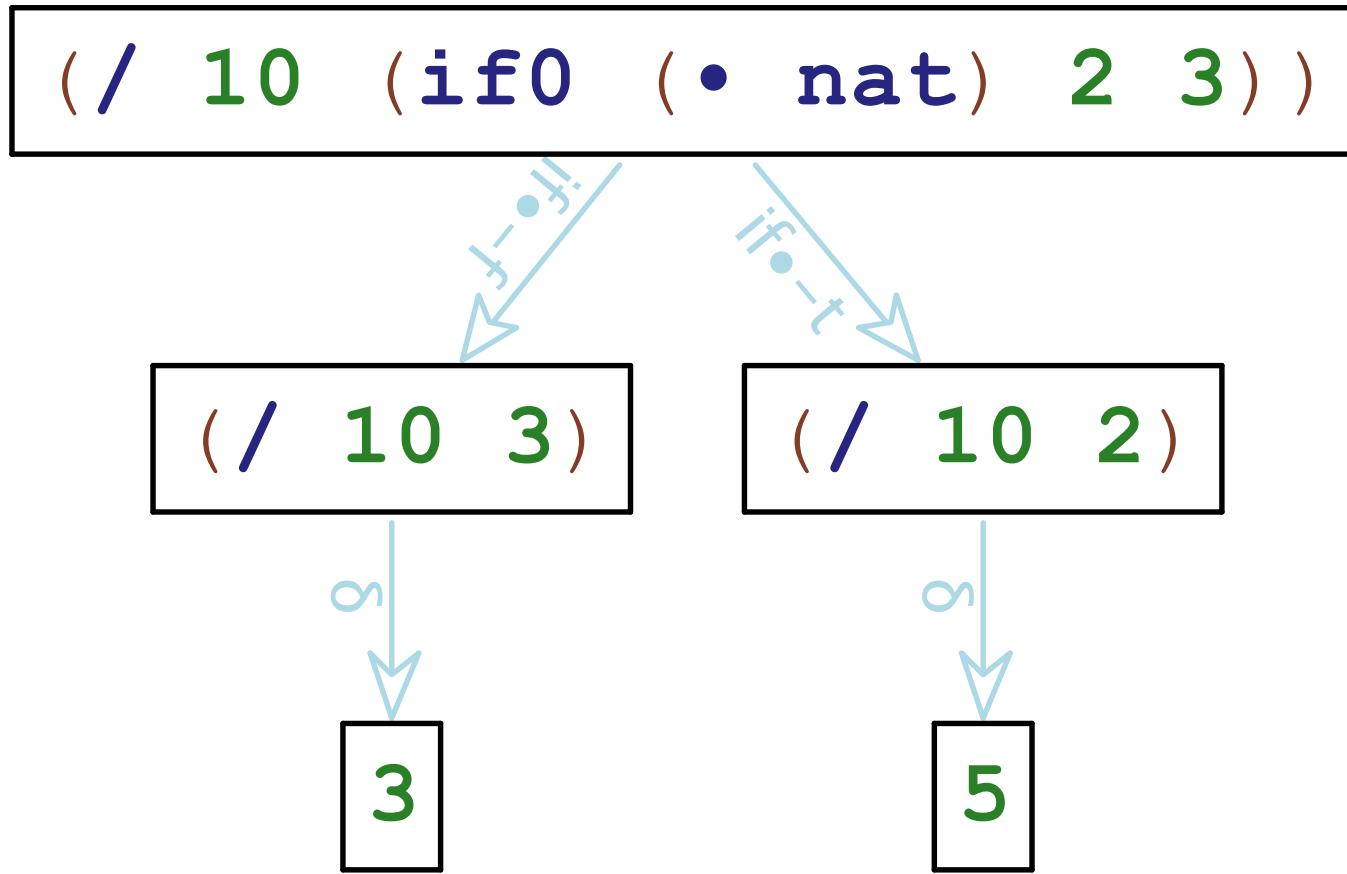
With abstract values

```
( / 10 (if0 7 2 3) )
```

With abstract values

```
( /  10  (if0  (•  nat)  2  3) )
```

With abstract values



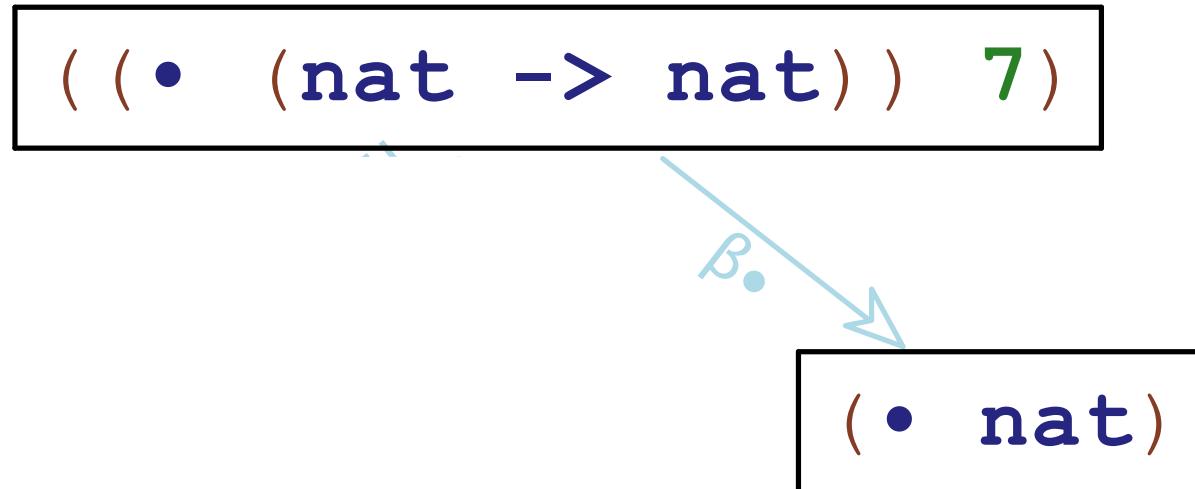
With abstract values

```
( add1 7 )
```

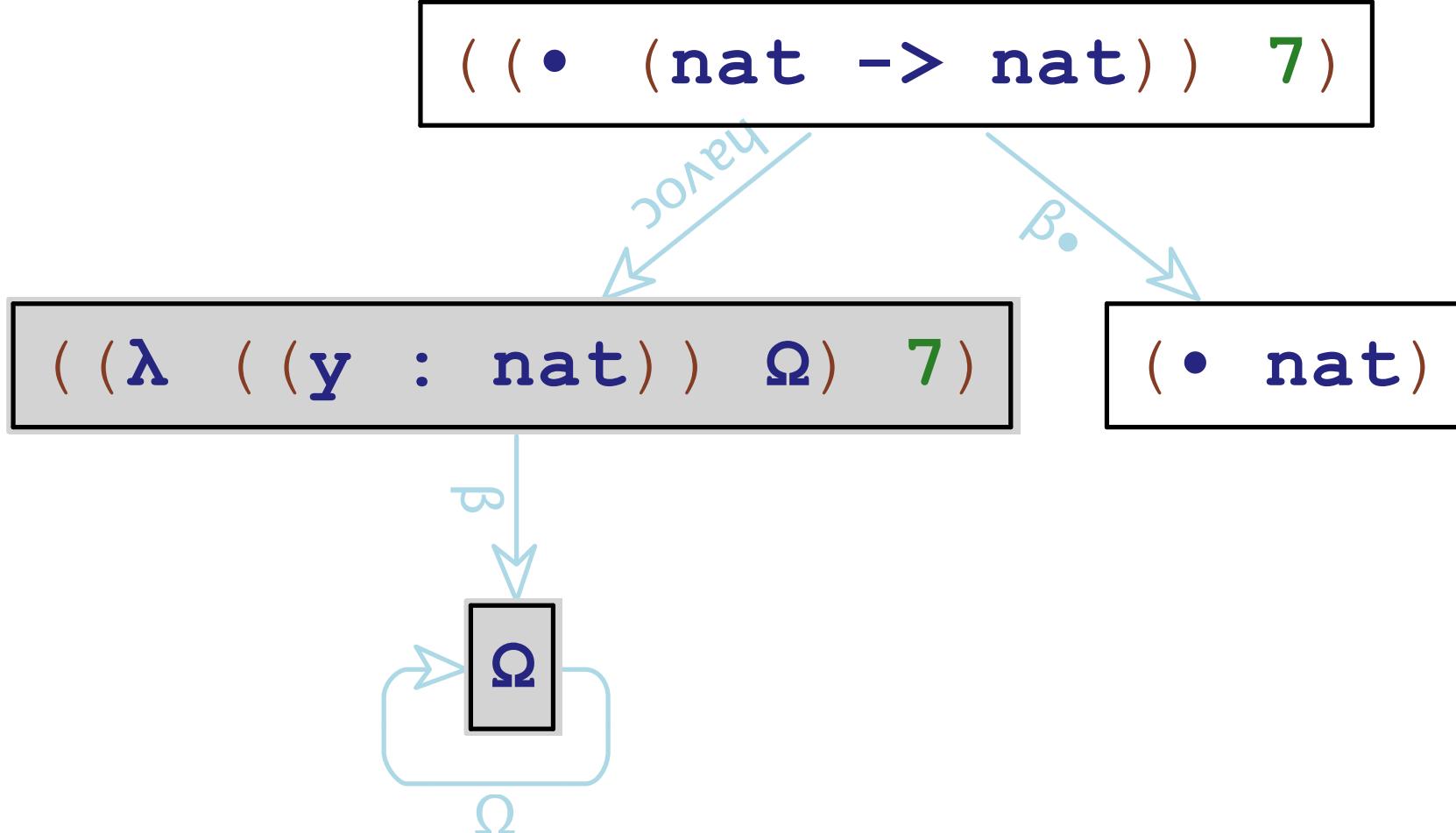
With abstract values

```
( ( •  (nat -> nat) ) 7 )
```

With abstract values



With abstract values



With abstract values

```
( (λ ( (f : (nat -> nat)) ) (f 3) )
  (λ ( (x : nat) ) (+ x (/ 10 x)) ) )
```

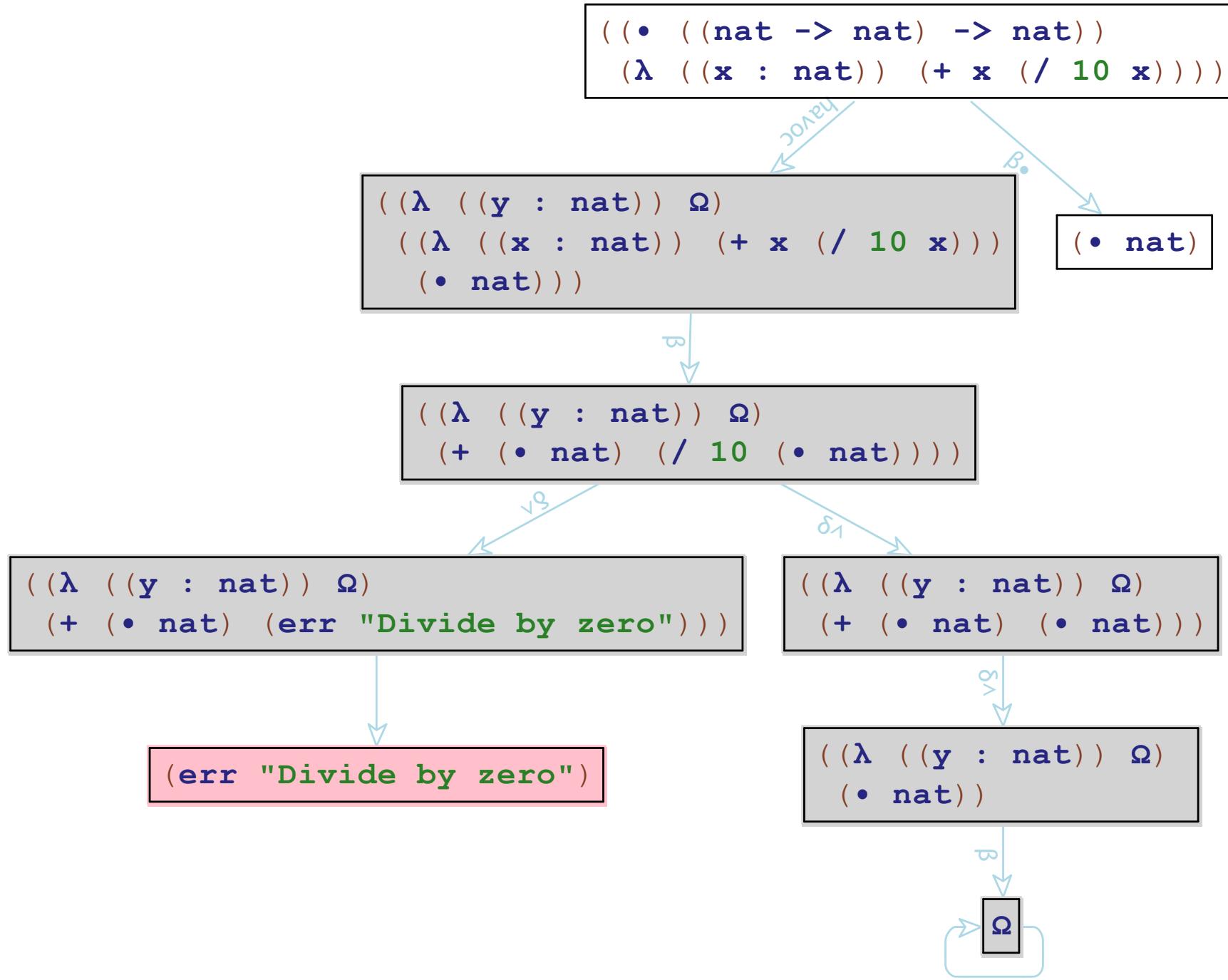
With abstract values

```
( ( •  ( (nat -> nat) -> nat) )  
  (λ  ( (x : nat) )  (+ x (/ 10 x)) ) )
```

With abstract values

```
( (• ( (nat -> nat) -> nat) )  
  (λ ( (x : nat) ) ( + x (/ 10 x) ) ) )
```

With abstract values



The higher-order case

```
( ( • ( (nat -> nat) -> nat)
      ( (pos? -> pos?) -> pos?) )
  (λ ( (x : nat) ) (+ x (/ 10 x)) ) ) )
```

The higher-order case

```
( ( • ( (nat -> nat) -> nat)
      ( (pos? -> pos?) -> pos?) )
  (λ ( (x : nat) ) (+ x (/ 10 x)) ) ) )
```

β_\bullet

```
( • nat pos?)
```

The higher-order case

```
( ( • ( (nat -> nat) -> nat)
  ( (pos? -> pos?) -> pos? ) )
  (λ ( (x : nat) ) ( + x (/ 10 x) ) ) )
```

```
( (λ ( (y : nat) ) Ω)
  ( (λ ( (x : nat) ) ( + x (/ 10 x) ) )
    ( • nat pos? ) ) )
```

```
( • nat pos?)
```

```
( (λ ( (y : nat) ) Ω)
  ( + ( • nat pos?) (/ 10 ( • nat pos? ) ) ) )
```

```
( (λ ( (y : nat) ) Ω)
  ( + ( • nat pos?) ( • nat ) ) )
```

```
( (λ ( (y : nat) ) Ω)
  ( • nat) )
```



The higher-order case

```
( ( • ( (nat -> nat) -> nat) )  
  ( (pos? -> pos?) ≈ (λ ( (x : nat) ) (+ x (/ 10 x)))))
```

The higher-order case

```
( ( • ( (nat -> nat) -> nat) )  
  ( (pos? -> pos?) ≈ (λ ( (x : nat) ) ( + x (/ 10 x) ) ) ) )
```



```
( ( • ( (nat -> nat) -> nat) )  
  (λ ( (x : nat) ) (pos? ≈ ( (λ ( (x : nat) ) ( + x (/ 10 x) ) )  
    (pos? ≈ x) ) ) ) )
```

havoc

β•

```
(nat) Ω  
nat) (pos? ≈ ( (λ ( (x : nat) ) ( + x (/ 10 x) ) )  
  (pos? ≈ x) ) ) )
```

(• nat)

The higher-order case

VQ↓

```
((λ ((y : nat)) Ω)
 (pos? ≡ (λ ((x : nat)) (+ x (/ 10 x)))
 (if0 (• nat) (• nat pos?) (blame HAVOC)))
```

```
((λ ((y : nat)) Ω)
 (pos? ≡ (λ ((x : nat)) (+ x (/ 10 x)))
 (blame HAVOC))))
```

```
((λ ((y : nat)) Ω)
 (pos? ≡ (λ ((x :
 (• nat pos?
```

if_{•-t}

if_{•-t}

blame HAVOC

```
((λ ((y : nat)) Ω)
 (pos? ≡ (+ (• nat pos?
```

D

O

The higher-order case

$((\lambda ((y : \text{nat})) \Omega)$

$(\text{pos?} \triangleq (\bullet \text{ nat pos?})))$

known

$((\lambda ((y : \text{nat})) \Omega)$

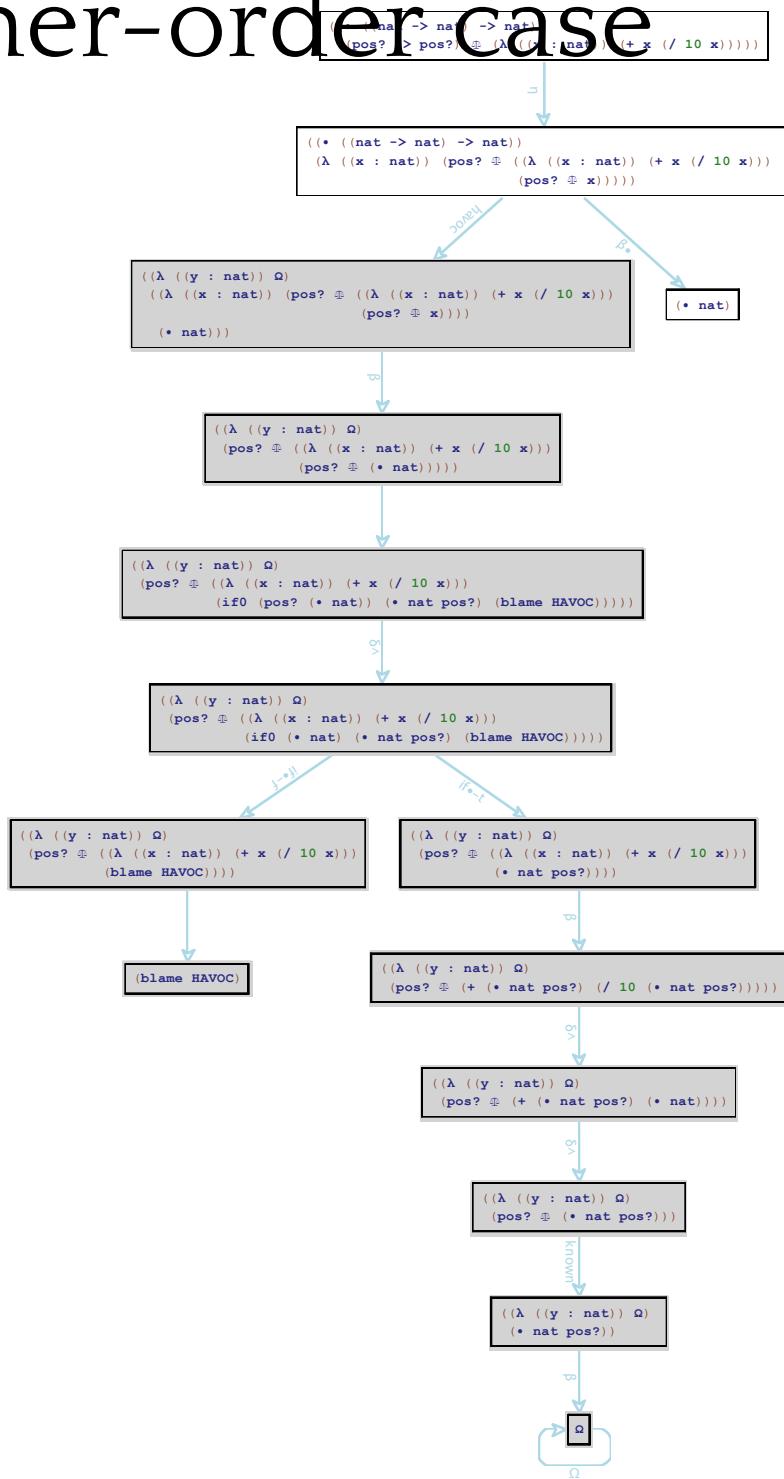
$(\bullet \text{ nat pos?}))$

β

Ω

Ω

The higher-order case



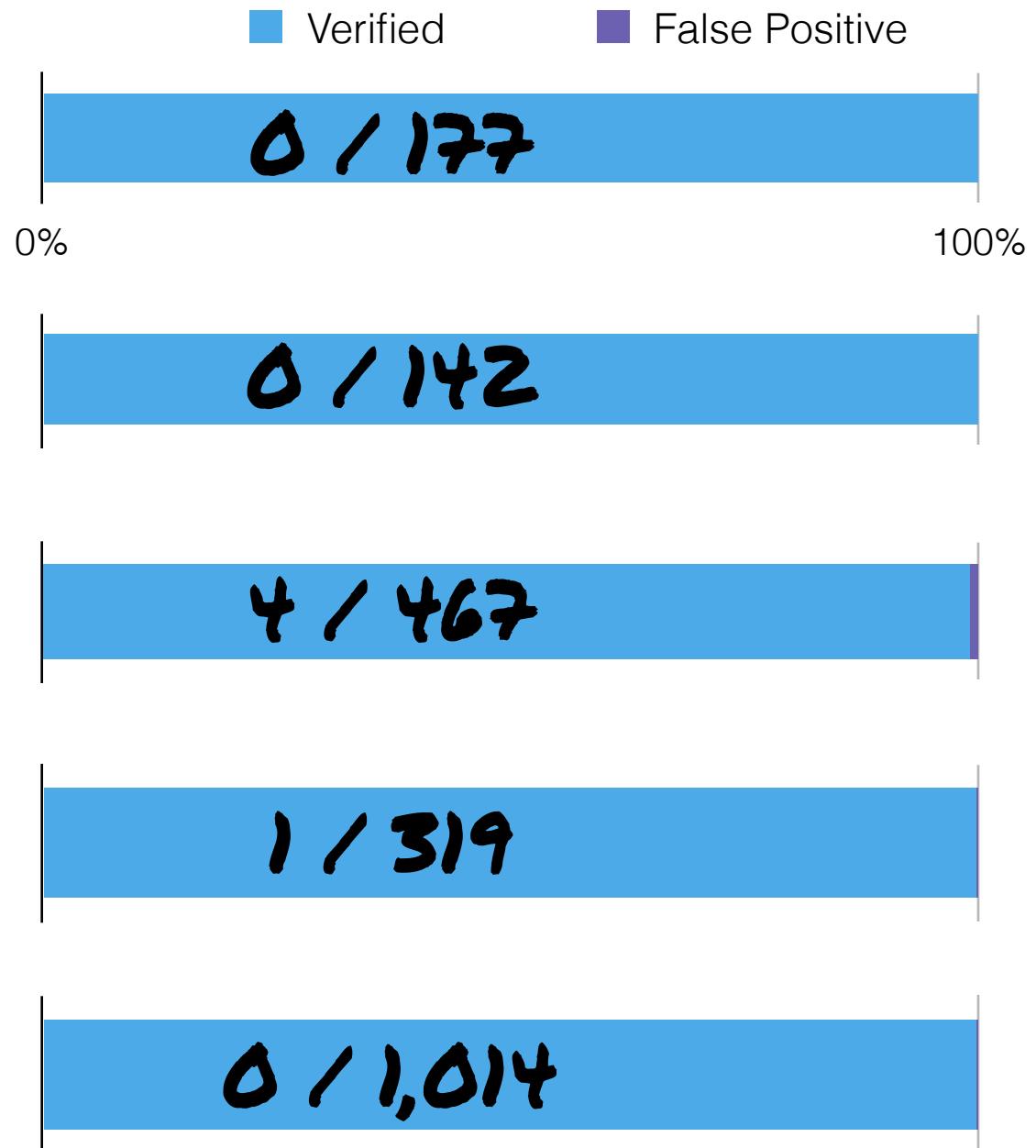
SOFT TYPING

**OCCURRENCE
TYPING**

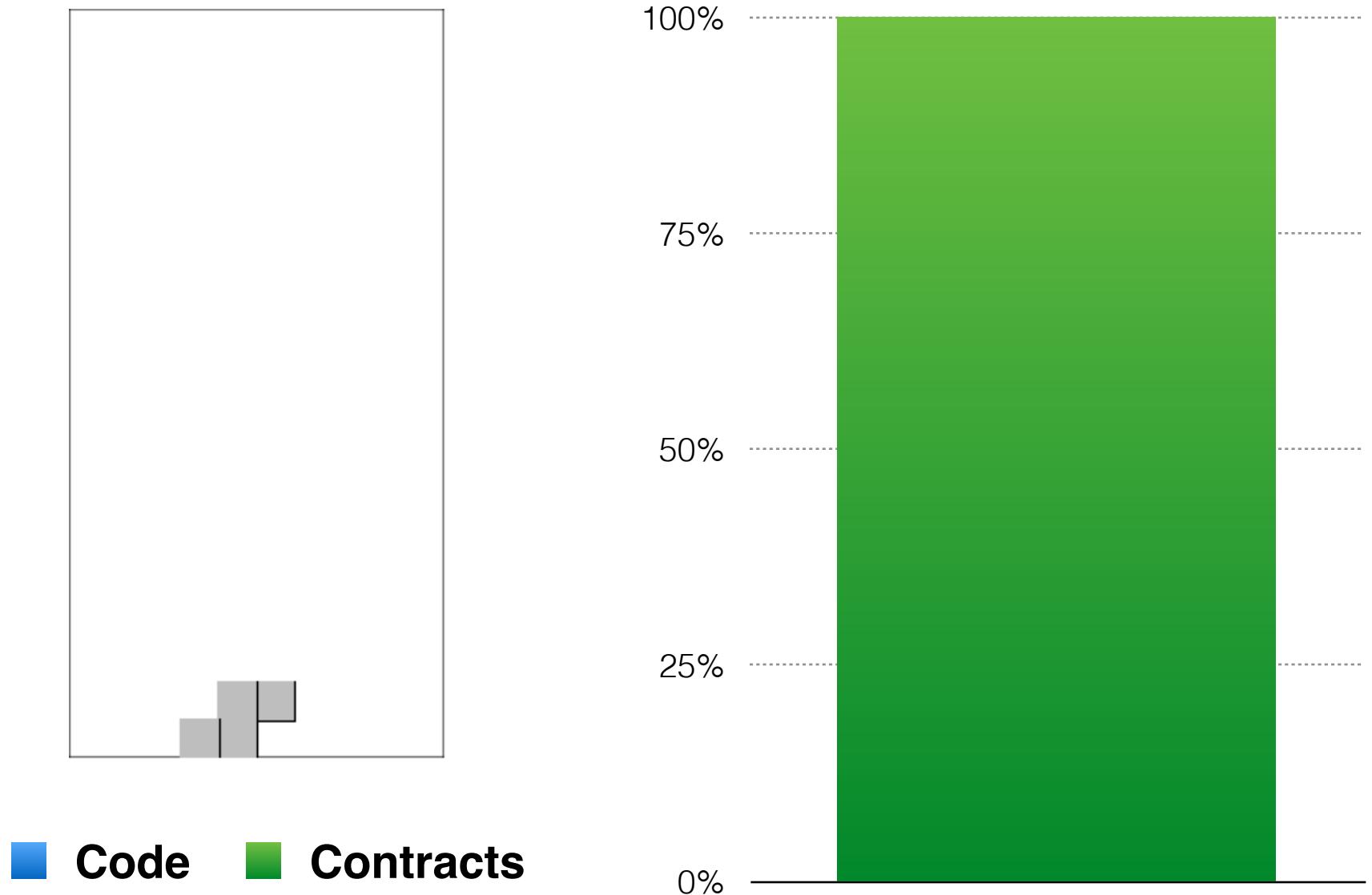
**H.O. RECURSION
SCHEMES**

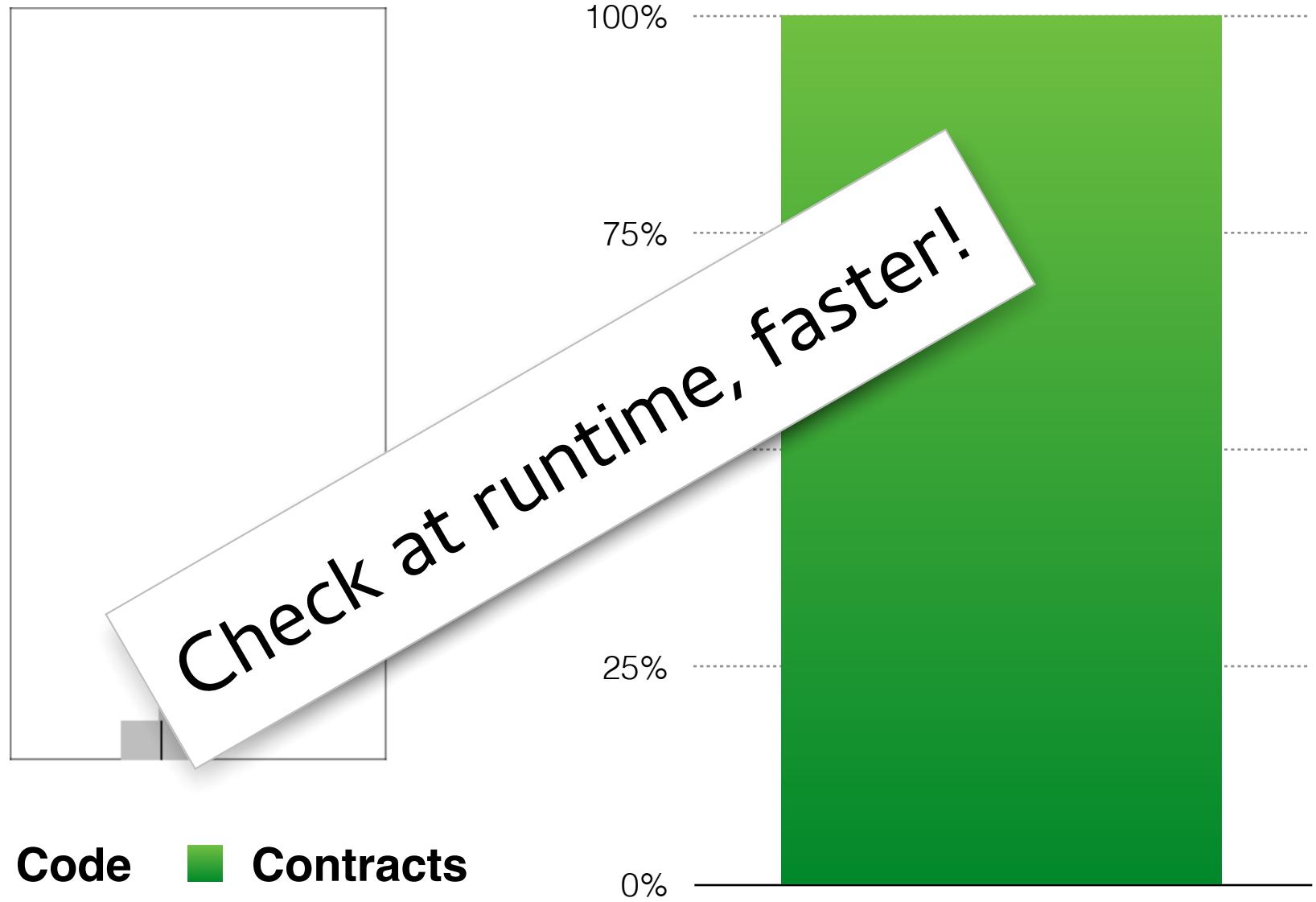
**DEPENDENT
REFINEMENT
TYPES**

VIDEO GAMES



Optimization





A simpler program

```
(define (dot u v)
  (for/sum ([x u]
            [y v])
    (* x y)))
```

A simpler program

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(define (dot u v)
  (for/sum ([x u]
            [y v])
    (* x y)))
```

506 ms (size 10000000)

A simpler program

```
(define/contract (dot u v)
  ((vectorof flonum?)
   (vectorof flonum?))
  . -> . flonum?))
(for/sum ([x u] [y v])
  (* x y)))
```

1159 ms (size 10000000)

Why are contracts hard to optimize?

```
(contract (-> integer? integer?)  
         (lambda (x) x))
```

Why are contracts hard to optimize?

```
(chaperone-procedure
  (lambda (x) x)
  (lambda (v)
    (unless (integer? v) (error 'blame))
    v)
  (lambda (v)
    (unless (integer? v) (error 'blame))
    v)))
```

MAYBE YOU CAN
HAVE YOUR CAKE
AND EAT IT TOO.

With Pycket ...

```
(define (dot u v)
  (for/sum ([x u]
            [y v])
    (* x y)))
```

12 ms (size 10000000)

With Pycket ...

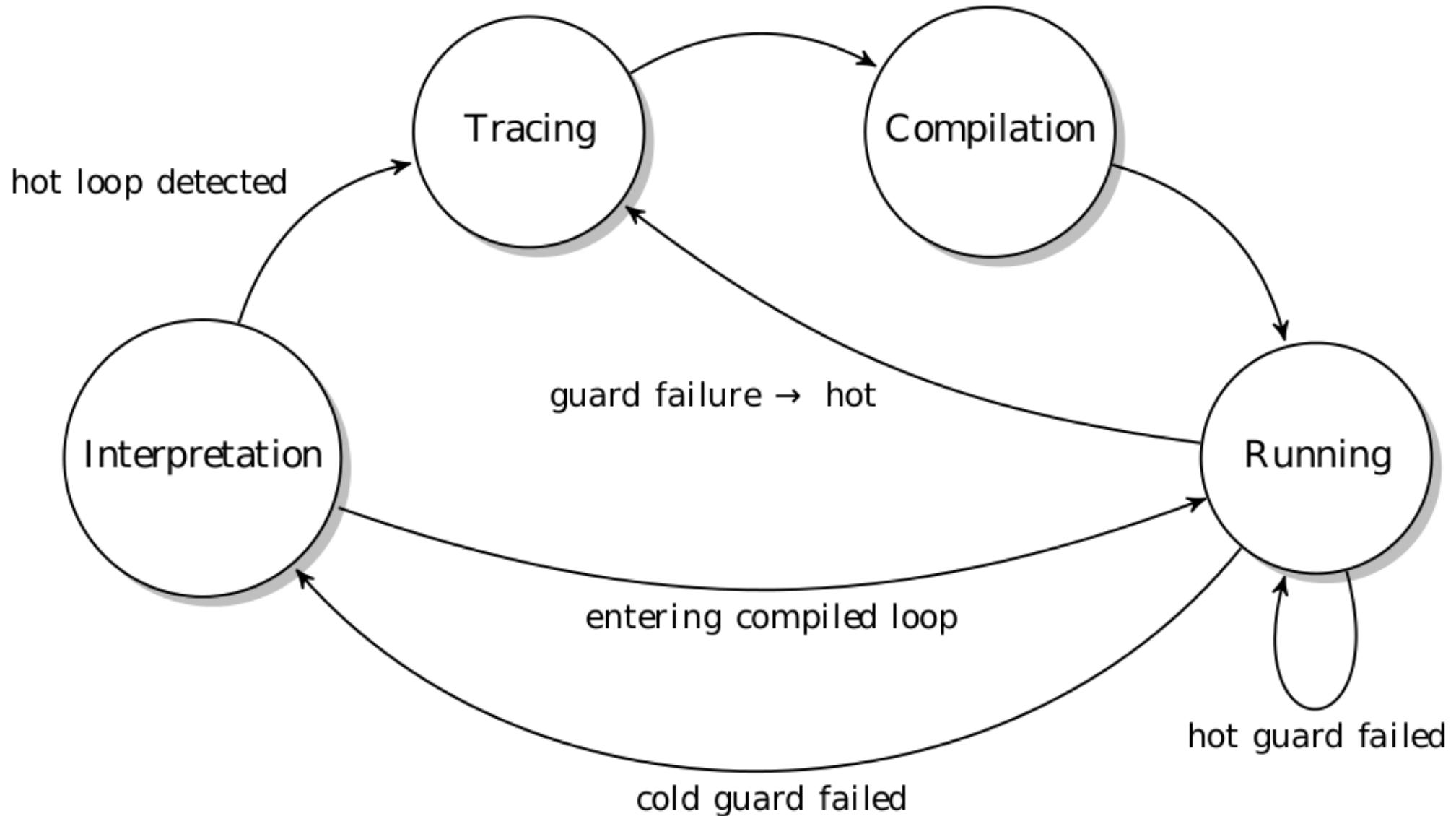
```
(define/contract (dot u v)
  ((vectorof flonum?))
  ((vectorof flonum?))
  (. -> . flonum?))
(for/sum ([x u] [y v])
  (* x y)))
```

17 ms (size 10000000)

Tracing JIT

1. Interpret Program
2. Find hot loop
3. Record operations for one iteration
4. Optimize
5. Switch to new code

Tracing JIT



(Diagram from Antonio Cuni)

Dot product Inner Loop

loop header

```
label(p3, f58, i66, i70, p1, i17, i28, p38, p48)
    guard_not_invalidated()
```

loop termination tests

```
i71 = i66 < i17
    guard(i71 is true)
i72 = i70 < i28
    guard(i72 is true)
```

vector access

```
f73 = getarrayitem_gc(p38, i66)
f74 = getarrayitem_gc(p48, i70)
```

core operations

```
f75 = f73 * f74
f76 = f58 + f75
```

increment loop counters

```
i77 = i66 + 1
i78 = i70 + 1
```

jump back to loop header

```
jump(p3, f76, i77, i78, p1, i17, i28, p38, p48)
```

Key Optimizations

Inlining (happens for free)

Constant propagation

Allocation Removal

We didn't write a JIT or an optimizer!

We didn't write a JIT or an optimizer!

RPython creates a JIT from an interpreter

CEK Machine

$$e ::= x \mid \lambda x. e \mid e\ e$$

$$\kappa ::= [] \mid \text{arg}(e, \rho) :: \kappa \mid \text{fun}(v, \rho) :: \kappa$$

$$\langle x, \rho, \kappa \rangle \longmapsto \langle \rho(x), \rho, \kappa \rangle$$

$$\langle (e_1\ e_2), \rho, \kappa \rangle \longmapsto \langle e_1, \rho, \text{arg}(e_2, \rho) :: \kappa \rangle$$

$$\langle v, \rho, \text{arg}(e, \rho') :: \kappa \rangle \longmapsto \langle e, \rho', \text{fun}(v, \rho) :: \kappa \rangle$$

$$\langle v, \rho, \text{fun}(\lambda x. e, \rho') :: \kappa \rangle \longmapsto \langle e, \rho'[x \mapsto v], \kappa \rangle$$

CEK Advantages

Fast continuations

Tail recursion

Arbitrary size stack

CEK Advantages

Fast continuations

Tail recursion

Arbitrary size stack

Allocation everywhere

From CEK to JIT

1. Whole-program type inference
2. Translation to C
3. Adding JIT based on hints

Main Interpreter Loop

```
try:  
    while True:  
        driver.jit_merge_point()  
        if isinstance(ast, App):  
            prev = ast  
            ast, env, cont = ast.interpret(env, cont)  
            if ast.should_enter:  
                driver.can_enter_jit()  
except Done, e:  
    return e.values
```

	Pycket ± Pycket* ±		Racket ±		V8 ±		PyPy ±	
Bubble								
direct	640	1	656	1	1384	4	336	0
chaperone	768	0	778	1	6668	5	105891	2579
proxy					1153	8		
unsafe	496	1	550	1	955	1		
unsafe*	495	0	508	1	726	1		
Church								
direct	714	2	705	1	1243	6	2145	18
chaperone	6079	54	8400	34	38497	66		
contract	1143	6	2310	8	10126	142	295452	1905
proxy					53953	277	95391	848
wrap	3471	7	3213	5	4214	26	8731	45
Struct								
direct	133	0	133	0	527	0	377	0
chaperone	134	0	134	1	5664	68		
proxy					26268	130	1168	38
unsafe	133	0	133	0	337	0		
unsafe*	133	0	133	0	337	0		

ODE								
direct	2158	6	2645	6	5476	91		
contract	2467	8	5099	8	12235	128		
Binomial								
direct	1439	8	6879	83	2931	24		
contract	17749	83	19288	61	52827	507		

Contracts: a useful technology and a source of research ideas

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