

# The Design and Implementation of Typed Scheme

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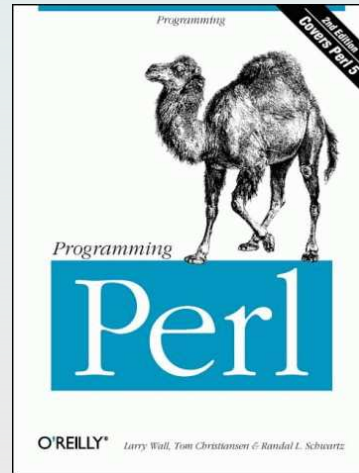
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# The PL Renaissance



# The PL Renaissance

Programming languages are flourishing



# What's good

These languages are

- interactive
- designed for rapid development
- supported by an active community
- modular
- higher-order

And they're exciting!

# What's not so good

(define (main stx trace-flag super-expr  
deserialize-id-expr name-id  
interface-exprs defn-and-exprs)

```
(let-values ([([this-id] #'this-id)
              [(the-obj) (datum->syntax (quote-syntax here) (gensym 'self))]
              [(the-finder) (datum->syntax (quote-syntax here) (gensym 'find-self))])
  (let* ([def-ctx (syntax-local-make-definition-context)]
        [localized-map (make-bound-identifier-mapping)]
        [any-localized? #f]
        [localize/set-flag (lambda (id)
                              (let ([id2 (localize id)])
                                (unless (eq? id id2)
                                  (set! any-localized? #t)
                                  id2))])
        [bind-local-id (lambda (id)
                          (let ([localize/set-flag id]
                                (syntax-local-bind-syntax (syntax-local-lookup id)
                                                             (bound-identifier-mapping-put!
                                                              localized-map
                                                              id
                                                              1))))])
        [lookup-localize (lambda (id)
                           (bound-identifier-mapping-get
                            localized-map
                            id
                            (lambda ()
                              (localize id))))])
        (let ([defn-and-exprs (expand-all-forms stx defn-and-exprs def-ctx bind-local-id)])
          [bad (lambda (msg expr)
                  (raise-syntax-error #f msg stx expr))]
          [class-name (if name-id
                          (syntax-e name-id)
                          (let ([s (syntax-local-infer-name stx)])
                            (if (syntax? s)
                                (syntax-e s)
                                s))))])
            (for-each (lambda (stx)
                        (syntax-case stx (-init -init-rest -field -init-field -inherit-field
                                           -private -public -override -augride
                                           -public-final -override-final -augment-final
                                           -pubment -overment -augment
                                           -rename-super -inherit -inherit/super -inherit/inner -rename-inner
                                           -inspect)
                          [(form orig idp ...)
                           (and (identifier? #'form)
                                (or (free-identifier=? #'form (quote-syntax -init))
                                    (free-identifier=? #'form (quote-syntax -init-field))))]))
                      defn-and-exprs)
          (and (free-identifier=? #'form (quote-syntax -init))
               (free-identifier=? #'form (quote-syntax -init-field)))))))))
```

+ 900 lines

# What's not so good

; Start here:

```
(define (main stx trace-flag super-expr  
        deserialize-id-expr name-id  
        interface-exprs defn-and-exprs)
```

```
(let-values ([([this-id] #'this-id)  
              ([the-obj] (datum->syntax (quote-syntax here) (gensym 'self)))  
              ([the-finder] (datum->syntax (quote-syntax here) (gensym 'find-self)))  
              ([def-ctx (syntax-local-make-definition-context)]  
               [localized-map (make-bound-identifier-mapping)]  
               [any-localized? #f]  
               [localize/set-flag (lambda (id)  
                                   (let ([id2 (localize id)])  
                                     (unless (eq? id id2)  
                                       (set! any-localized? #t))  
                                     id2))]  
               [bind-local-id (lambda (id)  
                                (let ([localize/set-flag id]  
                                      (syntax-local-bind-syntax (syntax-local-lookup id)  
                                                                    (bound-identifier-mapping-put!  
                                                                      localized-map  
                                                                      id  
                                                                      1))))]  
               [lookup-localize (lambda (id)  
                                 (bound-identifier-mapping-get  
                                  localized-map  
                                  id  
                                  (lambda ()  
                                    (localize id))))])  
  (let ([defn-and-exprs (expand-all-forms stx defn-and-exprs def-ctx bind-local-id)]  
        [bad (lambda (msg expr)  
                (raise-syntax-error #f msg stx expr)]  
        [class-name (if name-id  
                        (syntax-e name-id)  
                        (let ([s (syntax-local-infer-name stx)])  
                          (if (syntax? s)  
                              (syntax-e s)  
                              s)))]])  
    (for-each (lambda (stx)  
              (syntax-case stx (-init -init-rest -field -init-field -inherit-field  
                                   private public override augride  
                                   public-final override-final augment-final  
                                   pubment overment augment  
                                   rename-super inherit inherit/super inherit/inner rename-inner  
                                   inspect)  
                [(form orig idp ...)  
                 (and (identifier? #form)  
                      (or (free-identifier=? #form (quote-syntax -init))  
                          (free-identifier=? #form (quote-syntax -init-field))))])  
              (and (identifier? #form)  
                   (or (free-identifier=? #form (quote-syntax -init))  
                       (free-identifier=? #form (quote-syntax -init-field))))))
```

+ 900 lines

# Program Evolution

How can we make our script evolve into a mature program?

By adding statically checked design information piece by piece.

# What do we need

1. Module by module migration
2. Easy integration with untyped code
3. Sound guarantees from the type system
4. Avoid rewriting code



# Typed Scheme

# Why PLT Scheme?

PLT Scheme is a scripting language.

- Untyped, Modular, Built to script libraries

We are facing the same dilemma.

- Lots of untyped code to maintain

# Why PLT Scheme?

PLT Scheme has advantages for implementing program evolution.

- Modules [Flatt 02]
- Software Contracts [Findler 02]

# Why PLT Scheme?

Lessons from PLT Scheme apply elsewhere.

# Modular migration

## 1. Module by module migration

Hello World in PLT Scheme

```
#lang scheme
```

```
print
```

```
(printf "Hello World")
```

# Modular migration

## 1. Module by module migration

Hello World in Typed Scheme

```
#lang typed-scheme
```

```
print
```

```
(printf "Hello World")
```

# Modular migration

## 1. Module by module migration

### Simple Arithmetic in PLT Scheme

```
#lang scheme
```

```
arith
```

```
(define (sq x)  
  (* x x))
```

# Modular migration

## 1. Module by module migration

### Simple Arithmetic in Typed Scheme

```
#lang typed-scheme
```

```
arith
```

```
(: sq (Num → Num))
```

```
(define (sq x)
```

```
  (* x x))
```



# Modular migration

## 1. Module by module migration

Multi-module programs

```
#lang typed-scheme
```

```
arith
```

```
(: sq (Num → Num))
```

```
(define (sq x)
```

```
  (* x x))
```

```
(provide sq)
```

```
#lang typed-scheme
```

```
run
```

```
(require arith)
```

```
(sq 11) ; => 121
```

# Integration with plain PLT Scheme

## 2. Easy integration with untyped code

Typed to Untyped

```
#lang typed-scheme
```

```
arith
```

```
(: sq (Num → Num))
```

```
(define (sq x)
```

```
  (* x x))
```

```
(provide sq)
```

```
#lang scheme
```

```
run
```

```
(require arith)
```

```
(sq 11)
```

```
(sq "eleven")
```

# Integration with plain PLT Scheme

## 3. Sound guarantees from the type system

Typed to Untyped

```
#lang typed-scheme
```

```
arith
```

```
(: sq (Num → Num))
```

```
(define (sq x)
```

```
  (* x x))
```

```
(provide sq)
```

```
#lang scheme
```

```
run
```

```
(require arith)
```

```
(sq 11)
```

```
(sq "eleven") ; => contract violation
```

# Integration with plain PLT Scheme

## 2. Easy integration with untyped code

Untyped to Typed

```
#lang scheme
```

```
arith
```

```
(define (sq x)  
  (* x x))  
(provide sq)
```

```
#lang typed-scheme
```

```
run
```

```
(require/typed sq (Num → Num) arith)  
(sq 11)  
(sq "eleven")
```

# Integration with plain PLT Scheme

## 3. Sound guarantees from the type system

Untyped to Typed

```
#lang scheme
```

```
arith
```

```
(define (sq x)  
  (* x x))  
(provide sq)
```

```
#lang typed-scheme
```

```
run
```

```
(require/typed sq (Num → Num) arith)  
(sq 11)  
(sq "eleven") ; => type error
```

# A Type System for PLT Scheme

## 4. Avoid rewriting code

PLT Scheme programmers do not write with any particular type system in mind.

So Typed Scheme must capture their informal reasoning.

# A Type System for PLT Scheme

## 4. Avoid rewriting code

How PLT Scheme programmers reason

```
#lang scheme
```

```
; Shape = Position  $\cup$  Circle  $\cup$  Rectangle  $\cup$  ...
```

```
; Shape  $\rightarrow$  Num
```

```
; what is the area of shape s?
```

```
(define (shape-area s)
```

```
  (cond
```

```
    [(position? s) 0]
```

```
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
```

```
    ...))
```

# A Type System for PLT Scheme

## 4. Avoid rewriting code

How PLT Scheme programmers reason

```
#lang scheme
```

```
; Shape = Position  $\cup$  Circle  $\cup$  Rectangle  $\cup$  ...
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; what is the area of shape s?
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  (cond
```

```
    [(position? s) 0]
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```
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
```

```
    ...))
```



# A Type System for PLT Scheme

## 4. Avoid rewriting code

How PLT Scheme programmers reason

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#lang scheme
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```
; Shape = Position  $\cup$  Circle  $\cup$  Rectangle  $\cup$  ...
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```
; Shape  $\rightarrow$  Num
```

```
; what is the area of shape s?
```

```
(define (shape-area s)
```

```
  (cond
```

```
    [(position? s) 0]
```

```
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
```

```
    ...))
```

# A Type System for PLT Scheme

## 4. Avoid rewriting code

How PLT Scheme programmers reason

```
#lang typed-scheme

(define-type-alias Shape
  (⋃ Position Circle Rectangle ...))
(: shape-area (Shape → Num))
; what is the area of shape s?
(define (shape-area s)
  (cond
    [(position? s) 0]
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
    ...))
```

# A Type System for PLT Scheme

## 4. Avoid rewriting code

### Occurrence Typing

```
#lang typed-scheme

(define-type-alias Shape
  (⋃ Position Circle Rectangle ...))
(: shape-area (Shape → Num))
; what is the area of shape s?
(define (shape-area s)
  (cond
    [(position? s) 0]
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
    ...))
```

# A Type System for PLT Scheme

## 4. Avoid rewriting code

### Occurrence Typing

```
#lang typed-scheme

(: shape-area (Shape → Num))
(define (shape-area s)
  (cond
    [(position? s) 0]
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
    ...))
```

# A Type System for PLT Scheme

## 4. Avoid rewriting code

### Occurrence Typing

```
#lang typed-scheme

(: shape-area (Shape → Num))
(define (shape-area s)
  (cond
    [(position? s) 0]
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
    ...))
```

$s : \text{Shape}$

# A Type System for PLT Scheme

## 4. Avoid rewriting code

### Occurrence Typing

```
#lang typed-scheme

(: shape-area (Shape → Num))
(define (shape-area s)
  (cond
    [(position? s) 0]
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
    ...))
```

$s : \text{Shape}$

# A Type System for PLT Scheme

## 4. Avoid rewriting code

### Occurrence Typing

```
#lang typed-scheme

(: shape-area (Shape → Num))
(define (shape-area s)
  (cond
    [(position? s) 0]
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
    ...))
```

$s : \text{Position}$

# A Type System for PLT Scheme

## 4. Avoid rewriting code

### Occurrence Typing

```
#lang typed-scheme

(: shape-area (Shape → Num))
(define (shape-area s)
  (cond
    [(position? s) 0]
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
    ...))
```

$s : \text{Shape}$



# A Type System for PLT Scheme

## 4. Avoid rewriting code

### Occurrence Typing

```
#lang typed-scheme

(: shape-area (Shape → Num))
(define (shape-area s)
  (cond
    [(position? s) 0]
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
    ...))
```

$s : \text{Circle}$

# A Type System for PLT Scheme

## 4. Avoid rewriting code

### Occurrence Typing

```
#lang typed-scheme

(: shape-area (Shape → Num))
(define (shape-area s)
  (cond
    [(position? s) 0]
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
    ...))
```

$s : \text{Circle}$

# A Type System for PLT Scheme

## 4. Avoid rewriting code

### Occurrence Typing

```
#lang typed-scheme

(: shape-area (Shape → Num))
(define (shape-area s)
  (cond
    [(position? s) 0]
    [(circle? s) (* (sqr (circle-radius s) 2) pi)]
    ...))
```

circle? : (Any → Bool : Circle)

# A Type System for PLT Scheme

## 4. Avoid rewriting code

How PLT Scheme programmers reason

```
#lang scheme
```

```
(map rectangle-area  
  (filter rectangle? list-of-shapes))
```

# A Type System for PLT Scheme

## 4. Avoid rewriting code

How PLT Scheme programmers reason

```
#lang typed-scheme
```

```
(map rectangle-area  
  (filter rectangle? list-of-shapes))
```

# A Type System for PLT Scheme

## 4. Avoid rewriting code

How PLT Scheme programmers reason

```
#lang typed-scheme
```

```
(map rectangle-area  
  (filter rectangle? list-of-shapes))
```

```
rectangle? : (Any → Boolean : Rectangle)
```

# A Type System for PLT Scheme

## 4. Avoid rewriting code

How PLT Scheme programmers reason

```
#lang typed-scheme
```

```
(map rectangle-area  
  (filter rectangle? list-of-shapes))
```

```
filter : ( $\forall$  (a b)  
          ((Listof a) (Any  $\rightarrow$  Bool : b)  
             $\rightarrow$  (Listof b)))
```

# A Type System for PLT Scheme

## 4. Avoid rewriting code

Polymorphism

Union Types

Recursive Types

Structures

Occurrence Typing



# A Type System for PLT Scheme

## 4. Avoid rewriting code

Polymorphism

Union Types

Recursive Types

Structures

Occurrence Typing

Refinement Types

# Refinement Types

Any predicate can define a type

#lang typed-scheme

SQL

```
(: sql-safe? (String → Bool))  
(define (sql-safe? s) ...)  
(: query ((Refinement sql-safe?) → Result))  
(define (query s)  
  (string-append  
    "SELECT from Data where k = " s " ;"))
```

# Refinement Types

Any predicate can define a type

```
#lang typed-scheme
```

```
SQL
```

```
(: sql-safe? (String → Bool))
```

```
(define (sql-safe? s) ...)
```

```
(: check (String → (Refinement sql-safe?)))
```

# Refinement Types

Any predicate can define a type

```
#lang typed-scheme
```

```
SQL
```

```
(: sql-safe? (String → Bool))  
(define (sql-safe? s) ...)  
(: check (String → (Refinement sql-safe?)))  
(define (check s)  
  (if (sql-safe? s)  
      s  
      (error "not safe")))
```

# Refinement Types

Any predicate can define a type

```
#lang typed-scheme
```

```
SQL
```

```
(: sql-safe? (String → Bool))  
(define (sql-safe? s) ...)  
(: check (String → (Refinement sql-safe?)))  
(define (check s)  
  (if (sql-safe? s)  
      s  
      (error "not safe")))
```

```
sql-safe? : (String -> Bool : (Refinement sql-safe?))
```

# Refinement Types

Any predicate can define a type

```
#lang typed-scheme
```

```
SQL
```

```
(: sql-safe? (String → Bool))  
(define (sql-safe? s) ...)  
(: check (String → (Refinement sql-safe?)))  
(define (check s)  
  (if (sql-safe? s)  
      s  
      (error "not safe")))
```

```
x : (String -> Bool : (Refinement x))
```

Does it work?

# Formal Validation

We have a formal model of Typed Scheme

- Enjoys standard soundness properties

We have an implementation of this model using PLT Redex

- 500 lines

We have a verified model in Isabelle/HOL

- 5000 lines



# Real Validation

## Implemented in PLT Scheme

- Support PLT Tools (Check Syntax, Debugger, etc)
- Integrates with macro and module system
- Standard libraries available

# Real Validation

Ported thousands lines of existing code

- Games, scripts, libraries, educational code
- Even parts of DrScheme
- Not by the original author
- Very few changes to the code

# Future Work

# Exploiting Soft Typing

Soft typing attempted to typecheck untyped programs without programmer help.

This project was hindered by complex type languages and unpredictable errors.

We believe that using Typed Scheme as a target will help.

# Onward to JavaScript?

Other scripting languages present new challenges.

- Object systems
- No contract systems
- Weak module systems

And new opportunities.

# Thank You

Implementation, Documentation

[`http://www.plt-scheme.org`](http://www.plt-scheme.org)

PLT Redex Model, Isabelle Model

[`http://www.ccs.neu.edu/~samth`](http://www.ccs.neu.edu/~samth)

Thanks to Ryan Culpepper, Matthew Flatt, Ivan Gazeau