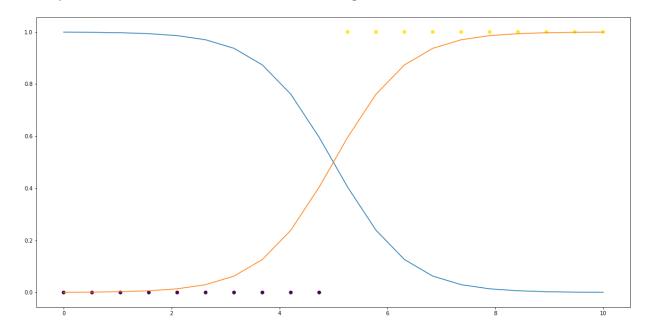
## Assignment is at the bottom!

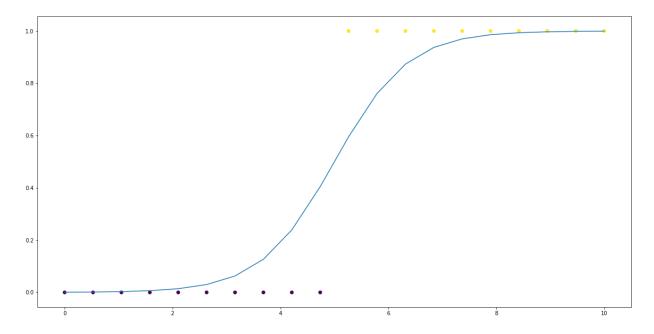
```
In [1]: | from sklearn.linear_model import LogisticRegression
        import pandas as pd
        import matplotlib.pyplot as plt
        %matplotlib inline
        import numpy as np
        from pylab import rcParams
        rcParams['figure.figsize'] = 20, 10
        from sklearn.linear_model import LogisticRegression as Model
In [2]: # creating dummy dataset with 10 datapoints of 0s and 1s to set up classification
        # will treat 0s and 1s as probabilities
        y = np.concatenate([np.zeros(10), np.ones(10)])
        x = np.linspace(0, 10, len(y))
In [3]: plt.scatter(x, y, c=y)
Out[3]: <matplotlib.collections.PathCollection at 0x1e38dd46308>
         0.8
         0.6
         0.4
         0.2
In [4]: model = LogisticRegression()
In [5]: model.fit(x.reshape(-1, 1),y)
Out[5]: LogisticRegression()
```

```
In [6]: plt.scatter(x,y, c=y)
plt.plot(x, model.predict_proba(x.reshape(-1, 1)))
```



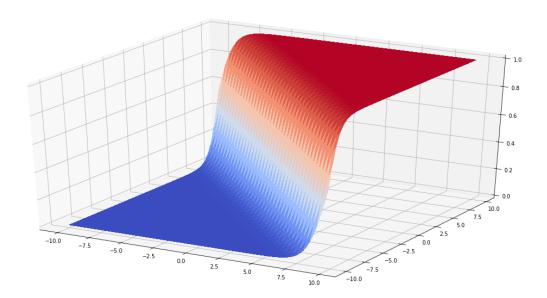
```
In [7]: # only concerned with probablity of orange line (above)
plt.scatter(x,y, c=y)
plt.plot(x, model.predict_proba(x.reshape(-1, 1))[:,1])
```

Out[7]: [<matplotlib.lines.Line2D at 0x1e38de0c588>]



```
In [8]: b, b0 = model.coef_, model.intercept_
         model.coef_, model.intercept_
 Out[8]: (array([[1.46709085]]), array([-7.33542562]))
 In [9]: # shows only half of the signoid
         plt.plot(x, 1/(1+np.exp(-x)))
 Out[9]: [<matplotlib.lines.Line2D at 0x1e38e151108>]
          1.0
          0.9
          0.8
          0.7
          0.6
          0.5
In [10]: b
Out[10]: array([[1.46709085]])
In [11]: plt.plot(x, 1/(1+np.exp(-(b[0]*x +b0))))
Out[11]: [<matplotlib.lines.Line2D at 0x1e38e745808>]
          1.0
```

```
In [12]: # 8:50 of Lecture
         from mpl toolkits.mplot3d import Axes3D # noga: F401 unused import
         import matplotlib.pyplot as plt
         from matplotlib import cm
         from matplotlib.ticker import LinearLocator, FormatStrFormatter
         import numpy as np
         fig = plt.figure()
         ax = fig.gca(projection='3d')
         # Make data.
         X = np.arange(-10, 10, 0.25)
         Y = np.arange(-10, 10, 0.25)
         X, Y = np.meshgrid(X, Y) # these are matrixes
         R = np.sqrt(X^{**2} + Y^{**2})
         \# Z = 1/(1+np.exp(-(b[0]*X +b[0]*Y +b0))) \# less steep
         \# Z = 1/(1+np.exp(-(b[0]*X +.25*b[0]*Y +b0))) \# more steep
         Z = 1/(1+np.exp(-(b[0]*X +b[0]*Y +.2*b0+2))) #moves the intercept
         surf = ax.plot_surface(X, Y, Z, cmap=cm.coolwarm,
                                 linewidth=0, antialiased=False)
```



```
In [13]: X
Out[13]: array([[-10. , -9.75, -9.5 , ...,
                                                 9.5,
                                                        9.75],
                                          9.25,
                                          9.25,
                                                 9.5,
              [-10., -9.75, -9.5, ...,
                                                        9.75],
              [-10., -9.75]
                             -9.5 , ...,
                                          9.25,
                                                 9.5,
                                                        9.75],
              [-10., -9.75, -9.5, ...,
                                                 9.5 ,
                                          9.25,
                                                        9.75],
              [-10., -9.75, -9.5, ...,
                                          9.25,
                                                 9.5,
                                                        9.75],
              [-10., -9.75, -9.5, ...,
                                          9.25,
                                                 9.5,
                                                       9.75]])
```

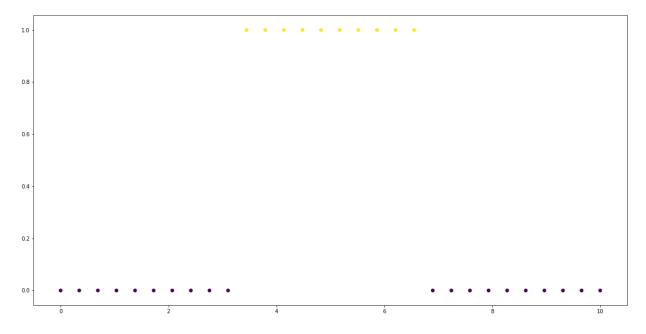
```
In [14]: Y
Out[14]: array([[-10. , -10. , -10. , ..., -10. , -10. , -10. ],
              [-9.75, -9.75, -9.75, ..., -9.75, -9.75,
                                                        -9.75],
              [ -9.5 , -9.5 , -9.5 , ..., -9.5 , -9.5 ,
                                                        -9.5],
                                                  9.25,
              9.25,
                        9.25,
                               9.25, ...,
                                           9.25,
                                                        9.25],
              [ 9.5,
                              9.5 , ...,
                       9.5,
                                           9.5,
                                                  9.5,
                                                        9.5],
              [ 9.75,
                        9.75,
                              9.75, ...,
                                           9.75,
                                                  9.75,
                                                         9.75]])
```

What if the data doesn't really fit this pattern?

```
In [15]: y = np.concatenate([np.zeros(10), np.ones(10), np.zeros(10)])
         x = np.linspace(0, 10, len(y))
```

```
In [16]: plt.scatter(x,y, c=y)
```

Out[16]: <matplotlib.collections.PathCollection at 0x1e38ed43fc8>



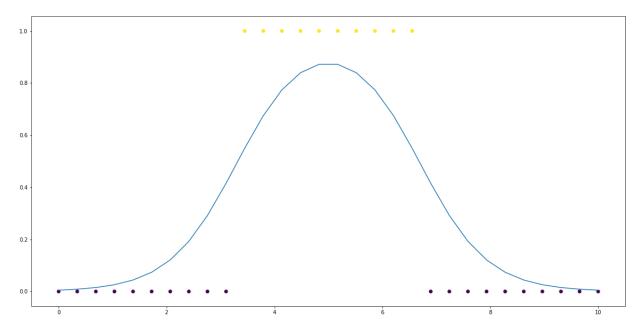
```
In [17]: model.fit(x.reshape(-1, 1),y)
```

Out[17]: LogisticRegression()

```
In [19]: model1 = LogisticRegression()
    model1.fit(x[:15].reshape(-1, 1),y[:15])
Out[19]: LogisticRegression()
In [20]: model2 = LogisticRegression()
    model2.fit(x[15:].reshape(-1, 1),y[15:])
Out[20]: LogisticRegression()
```

```
In [21]: plt.scatter(x,y, c=y)
  plt.plot(x, model1.predict_proba(x.reshape(-1, 1))[:,1] * model2.predict_proba(x.
```

#### Out[21]: [<matplotlib.lines.Line2D at 0x1e38ecfab88>]



xt[transform\_columns] = enc.transform(golden[transform\_columns])

```
In [26]: df.salary.unique()
Out[26]: array([' <=50K', ' >50K'], dtype=object)
In [27]: golden.salary.replace(' <=50K.', ' <=50K').replace(' >50K.', ' >50K').unique()
Out[27]: array([' <=50K', ' >50K'], dtype=object)
In [28]: model.fit(preprocessing.scale(x.drop('salary', axis=1)), x.salary)
Out[28]: LogisticRegression()
In [29]: pred = model.predict(preprocessing.scale(x.drop('salary', axis=1)))
          pred_test = model.predict(preprocessing.scale(xt.drop('salary', axis=1)))
In [30]: |x.head()
Out[30]:
                                             education-
                                                       marital-
             age workclass
                            fnlwgt education
                                                               occupation relationship race sex
                                                        status
                                                  num
                             77516
           0
              39
                        7.0
                                         9.0
                                                    13
                                                           4.0
                                                                      1.0
                                                                                 1.0
                                                                                      4.0
                                                                                           1.0
           1
              50
                        6.0
                             83311
                                         9.0
                                                    13
                                                           2.0
                                                                      4.0
                                                                                 0.0
                                                                                      4.0
                                                                                           1.0
              38
                        4.0 215646
                                        11.0
                                                    9
                                                           0.0
                                                                      6.0
                                                                                 1.0
                                                                                      4.0
                                                                                           1.0
           2
              53
                        4.0 234721
                                         1.0
                                                    7
                                                           2.0
                                                                      6.0
                                                                                      2.0
                                                                                           1.0
           3
                                                                                 0.0
              28
                        4.0 338409
                                         9.0
                                                    13
                                                           2.0
                                                                     10.0
                                                                                 5.0
                                                                                      2.0
                                                                                           0.0
In [31]: from sklearn.metrics import (
              accuracy_score,
              classification_report,
              confusion_matrix, auc, roc_curve
In [32]: | accuracy_score(x.salary, pred)
Out[32]: 0.8250360861152913
In [33]: confusion_matrix(x.salary, pred)
Out[33]: array([[23300,
                           1420],
                 [ 4277, 3564]], dtype=int64)
```

```
In [34]: |print(classification_report(x.salary, pred))
                       precision
                                    recall f1-score
                                                       support
                  0.0
                            0.84
                                      0.94
                                                0.89
                                                         24720
                            0.72
                                      0.45
                  1.0
                                                0.56
                                                          7841
             accuracy
                                                0.83
                                                         32561
                            0.78
                                      0.70
                                                0.72
                                                         32561
            macro avg
         weighted avg
                                                0.81
                            0.81
                                      0.83
                                                         32561
In [35]: print(classification_report(xt.salary, pred_test))
                                    recall f1-score
                       precision
                                                       support
                  0.0
                            0.85
                                      0.94
                                                0.89
                                                         12435
                            0.70
                                      0.45
                                                0.55
                  1.0
                                                          3846
                                                0.82
                                                         16281
             accuracy
                            0.77
                                      0.69
                                                0.72
                                                         16281
            macro avg
         weighted avg
                            0.81
                                      0.82
                                                0.81
                                                         16281
```

## **Assignment**

- 1. Use your own dataset (create a train and a test set) and build 2 models: Logistic Regression and Decision Tree (shallow (2-3)). Compare the test results.
- 2. Repeat 1. but let the Decision Tree be much deeper to allow over-fitting. Compare the two models' test results again, does the Logistic Regression have an improvement due to a lower variance?

```
In [36]: insurance = pd.read_csv('../data/insurance.csv')
insurance.head()
```

#### Out[36]:

	age	sex	bmi	children	smoker	region	charges
0	19	female	27.900	0	yes	southwest	16884.92400
1	18	male	33.770	1	no	southeast	1725.55230
2	28	male	33.000	3	no	southeast	4449.46200
3	33	male	22.705	0	no	northwest	21984.47061
4	32	male	28.880	0	no	northwest	3866.85520

```
In [37]: insurance.dtypes
Out[37]: age
                         int64
                        object
          sex
          bmi
                       float64
          children
                         int64
          smoker
                        object
          region
                        object
          charges
                       float64
          dtype: object
In [38]: from sklearn import preprocessing
          enc = preprocessing.OrdinalEncoder()
In [39]: |transform_columns = ['sex', 'smoker', 'region']
In [40]: x = insurance.copy()
          x[transform columns] = enc.fit transform(insurance[transform columns])
Out[40]:
                age sex
                            bmi children smoker region
                                                           charges
              0
                     0.0 27.900
                                      0
                                            1.0
                                                   3.0 16884.92400
                 19
              1
                 18
                     1.0 33.770
                                      1
                                            0.0
                                                   2.0
                                                        1725.55230
                     1.0 33.000
              2
                 28
                                      3
                                            0.0
                                                   2.0
                                                        4449.46200
              3
                 33
                     1.0 22.705
                                      0
                                            0.0
                                                   1.0 21984.47061
                 32
                     1.0 28.880
                                      0
                                            0.0
                                                   1.0
                                                        3866.85520
                     1.0 30.970
                                                   1.0 10600.54830
           1333
                 50
                                      3
                                            0.0
                     0.0 31.920
                                            0.0
                                                        2205.98080
           1334
                 18
                                      0
                                                   0.0
                                                        1629.83350
           1335
                 18
                    0.0 36.850
                                      0
                                            0.0
                                                   2.0
           1336
                 21
                     0.0 25.800
                                      0
                                            0.0
                                                   3.0
                                                        2007.94500
           1337
                 61
                     0.0 29.070
                                      0
                                            1.0
                                                   1.0 29141.36030
          1338 rows × 7 columns
In [41]: from sklearn.model selection import train test split
          x_train, x_test, y_train, y_test = train_test_split(x.drop('smoker', axis=1), x.s
In [42]: from sklearn.linear model import LogisticRegression
          model = LogisticRegression()
In [43]: model.fit(preprocessing.scale(x train), y train)
          model.coef_, model.intercept_
Out[43]: (array([[-1.07041457, 0.10937251, -1.66413989, -0.22858889, 0.08491027,
                     3.89658144]]),
           array([-3.44537705]))
```

```
In [44]: | pred = model.predict(preprocessing.scale(x_train))
         pred test = model.predict(preprocessing.scale(x test))
In [45]: from sklearn.metrics import (
             accuracy score,
             classification_report,
             confusion matrix, auc, roc curve
         )
In [46]: | accuracy_score(y_train, pred)
Out[46]: 0.9601196410767697
In [47]: |accuracy_score(y_test, pred_test)
Out[47]: 0.9522388059701492
In [48]: confusion_matrix(y_test, pred_test)
Out[48]: array([[258,
                [ 7, 61]], dtype=int64)
In [49]: | print(classification_report(y_test, pred_test))
                        precision
                                     recall f1-score
                                                        support
                             0.97
                                       0.97
                                                 0.97
                  0.0
                                                            267
                  1.0
                             0.87
                                       0.90
                                                 0.88
                                                             68
                                                 0.95
                                                            335
             accuracy
                                                 0.93
            macro avg
                            0.92
                                       0.93
                                                            335
         weighted avg
                            0.95
                                       0.95
                                                 0.95
                                                            335
```

#### **Decision Tree at 2 levels**

```
In [50]: from sklearn.tree import DecisionTreeClassifier
In [51]: model = DecisionTreeClassifier(criterion='entropy', max_depth=2)
    model.fit(x_train, y_train)
Out[51]: DecisionTreeClassifier(criterion='entropy', max_depth=2)
In [52]: model.tree_.node_count
Out[52]: 7
In [53]: pred = model.predict(x_train)
    pred_test = model.predict(x_test)
```

```
In [54]: | accuracy_score(y_train, pred)
Out[54]: 0.9292123629112662
In [55]: |accuracy_score(y_test, pred_test)
Out[55]: 0.9104477611940298
In [56]: print(classification_report(y_test, pred_test))
                       precision
                                    recall f1-score
                                                      support
                            1.00
                                     0.89
                                               0.94
                  0.0
                                                          267
                           0.69
                                     1.00
                                               0.82
                  1.0
                                                           68
                                               0.91
                                                          335
             accuracy
                         0.85 0.94
0.94 0.91
            macro avg
                                               0.88
                                                          335
                                               0.92
         weighted avg
                           0.94
                                     0.91
                                                          335
```

#### Comparison

The logistic model is more accurate, however, the two level decision tree successful predicts true positives and true negatives but poorly predicts false positives.

# 2. Repeat 1. but let the Decision Tree be much deeper to allow over-fitting. Compare the two models' test results again, does the Logistic Regression have an improvement due to a lower variance?

```
In [57]: model = DecisionTreeClassifier(criterion='entropy', max_depth=10)
    model.fit(x_train, y_train)

Out[57]: DecisionTreeClassifier(criterion='entropy', max_depth=10)

In [58]: model.tree_.node_count

Out[58]: 61

In [59]: pred = model.predict(x_train)
    pred_test = model.predict(x_test)

In [60]: accuracy_score(y_train, pred)

Out[60]: 0.9920239282153539

In [61]: accuracy_score(y_test, pred_test)

Out[61]: 0.9582089552238806
```

In [62]: print(classification\_report(y\_test, pred\_test))

	precision	recall	f1-score	support
0.0	0.97	0.98	0.97	267
1.0	0.92	0.87	0.89	68
accuracy			0.96	335
macro avg	0.94	0.92	0.93	335
weighted avg	0.96	0.96	0.96	335

### Comparison

The 10 level decision tree performs better that prior logistic and two level decision tree, with higher accuracy, precision, and recall. However, the deeper model likely over-fits and may not perform well on new data.