

## Problem 1

In this problem, we are asked to do out the N-queens problem by hand with N=9.

Below is a table containing our solution.

For each queen we have assigned a color as follows:

queen 1 — red  
 queen 2 — blue  
 queen 3 — green  
 queen 4 — yellow  
 queen 5 — cyan  
 queen 6 — teal  
 queen 7 — magenta  
 queen 8 — olive

.	.	Q <sub>1</sub>	.	.	.	.	.	.
.	x <sub>1</sub>	x <sub>1</sub>	x <sub>1</sub>	.	.	.	.	Q <sub>2</sub>
x <sub>1</sub>	Q <sub>3</sub>	x <sub>1</sub>	.	x <sub>1</sub>	.	.	x <sub>2</sub>	x <sub>2</sub>
x <sub>3</sub>	x <sub>3</sub>	x <sub>1</sub>	.	.	x <sub>1</sub>	x <sub>2</sub>	Q <sub>4</sub>	x <sub>2</sub>
Q <sub>5</sub>	x <sub>3</sub>	x <sub>1</sub>	x <sub>3</sub>	.	x <sub>2</sub>	x <sub>1</sub>	x <sub>4</sub>	x <sub>2</sub>
x <sub>5</sub>	x <sub>3</sub>	x <sub>1</sub>	Q <sub>6</sub>	x <sub>2</sub>	x <sub>4</sub>	.	x <sub>1</sub>	x <sub>2</sub>
x <sub>5</sub>	x <sub>3</sub>	x <sub>1</sub>	x <sub>2</sub>	x <sub>4</sub>	x <sub>3</sub>	Q <sub>7</sub>	x <sub>4</sub>	x <sub>1</sub>
x <sub>5</sub>	x <sub>3</sub>	x <sub>1</sub>	x <sub>4</sub>	Q <sub>8</sub>	x <sub>6</sub>	x <sub>3</sub>	x <sub>4</sub>	x <sub>2</sub>
x <sub>5</sub>	x <sub>2</sub>	x <sub>1</sub>	x <sub>6</sub>	x <sub>5</sub>	x <sub>8</sub>	x <sub>6</sub>	x <sub>3</sub>	x <sub>2</sub>

In the above table we demonstrate the use of the Monte Carlo approach to generate an estimate of the total cost to solve the N-queens problem with N=9. In the below table we give the row sums for all of the options, and then the total sum which represents the overall cost to solve the problem:

Row #	Choices	Cost
1	9	9
2	6	9 · 6
3	4	9 · 6 · 4
4	3	9 · 6 · 4 · 3
5	2	9 · 6 · 4 · 3 · 2
6	2	9 · 6 · 4 · 3 · 2 · 2
7	1	9 · 6 · 4 · 3 · 2 · 2 · 1
8	1	9 · 6 · 4 · 3 · 2 · 2 · 1 · 1
9	0	0
<b>Total</b>		<b>9999</b>