COMP1002 DATA STRUCTURES AND ALGORITHMS

LECTURE 6: GRAPHS



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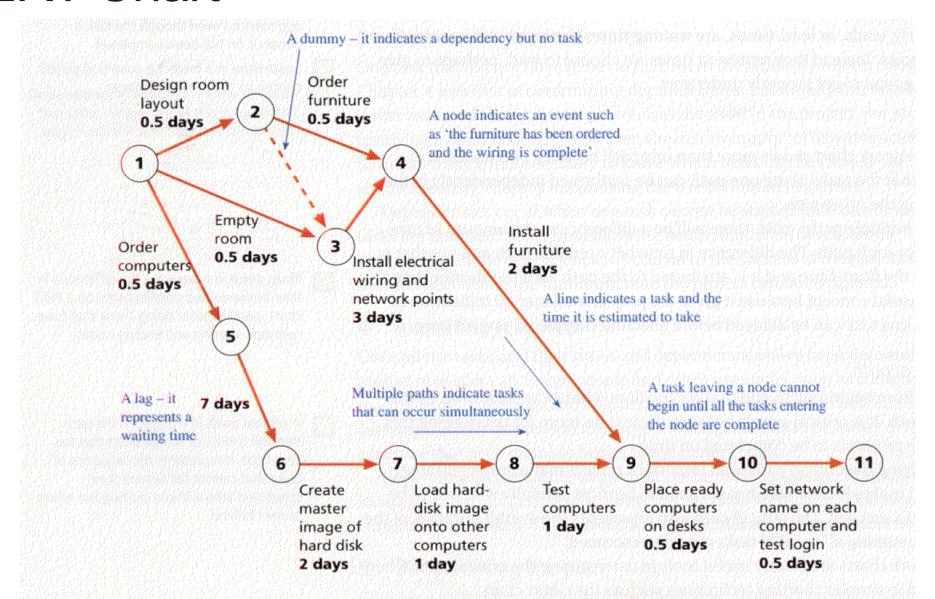
This Week

- Graph Terminology
- Graph Representation
- Graph Algorithms
 - Conceptual
- Big-O time complexity analysis

What is a Graph?

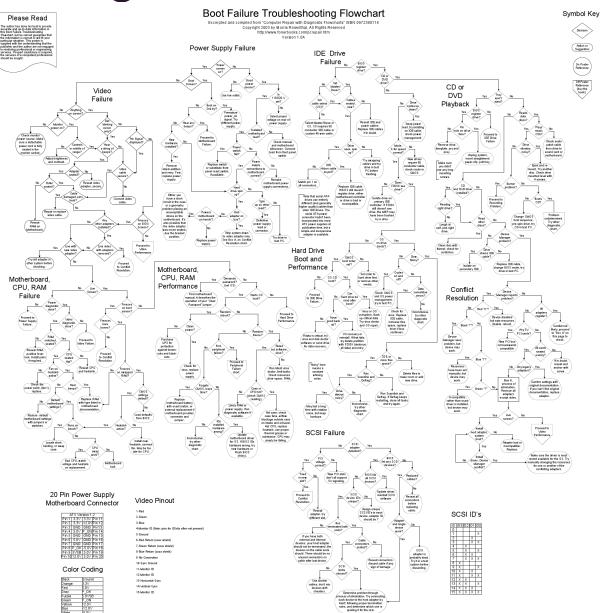
- A graph is a data structure representing connections between items
 - We're storing values with the potential for connections between any or all elements
- Examples of graphs in everyday life:
 - PERT charts
 - Flow charts
- Examples in computer science
 - Networks
 - Social Network diagrams
 - Executing a makefile

PERT Chart



[8.19] A PERT chart shows tasks on the lines. These are also known as CPM and PERT/CPM charts.

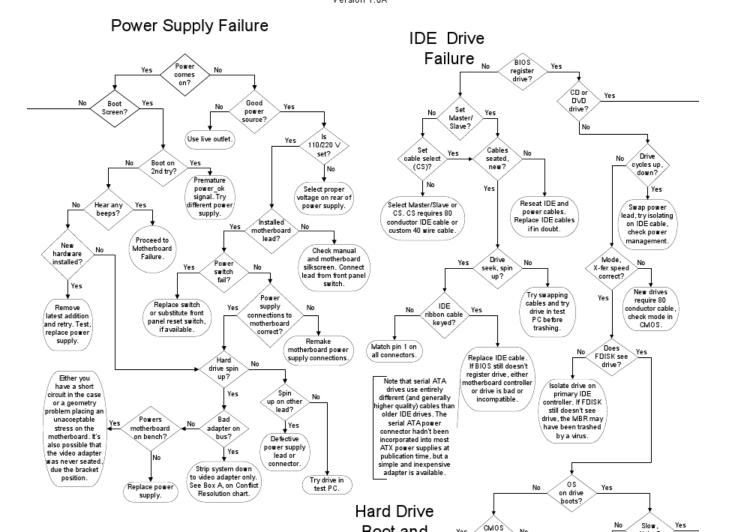
Troubleshooting Flowcharts



Troubleshooting Flowcharts

Boot Failure Troubleshooting Flowchart

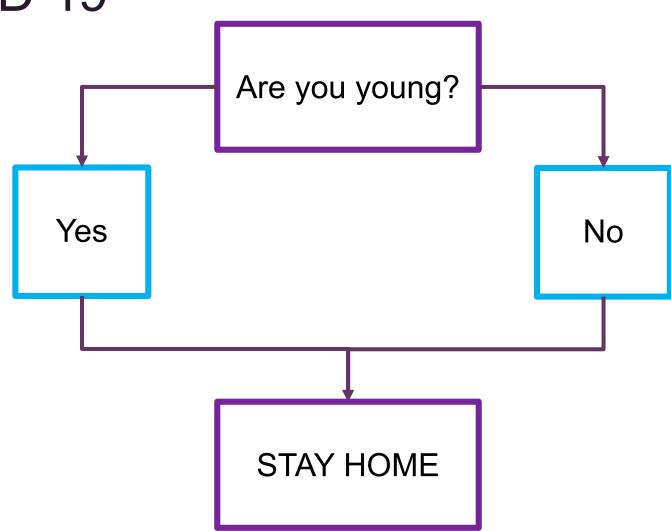
Excerpted and compiled from "Computer Repair with Diagnostic Flowcharts" ISBN 0972380116
Copyright 2003 by Morris Rosenthal, All Rights Reserved
http://www.fonerbooks.com/pcrepair.htm
Version 1.0A



Troubleshooting Flowcharts

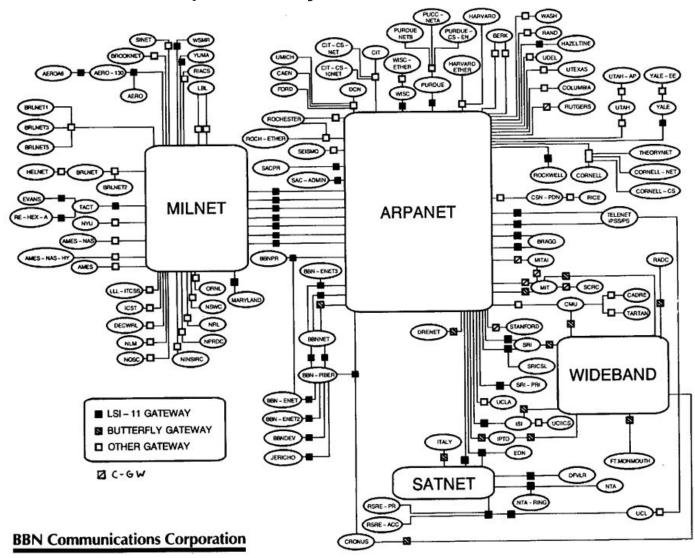


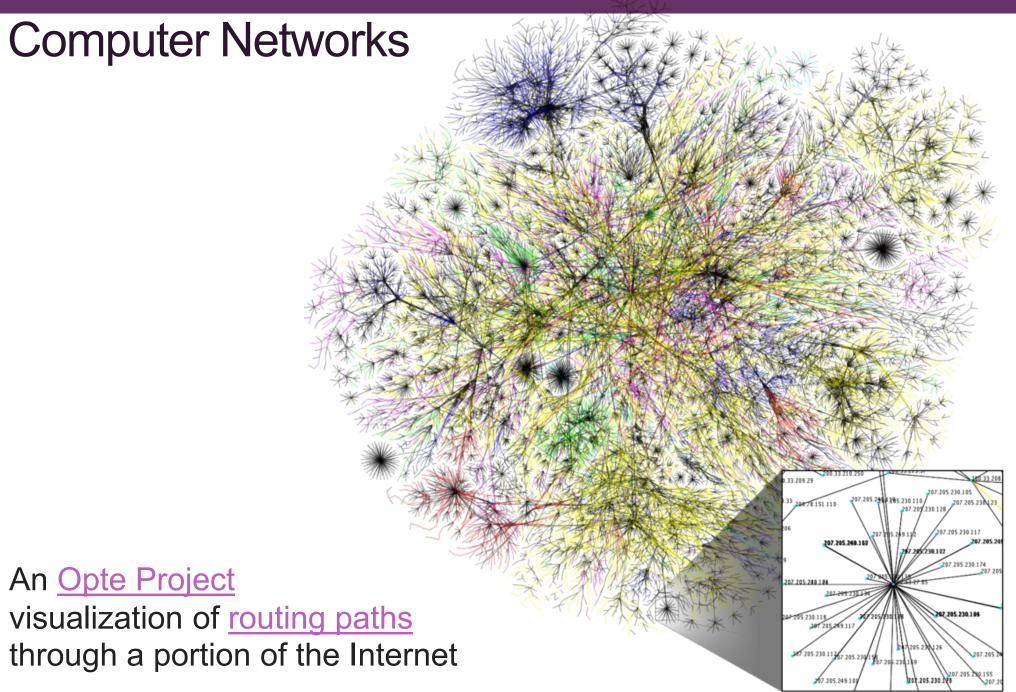
COVID-19



Computer Networks

TCP/IP Internet map of early 1986.

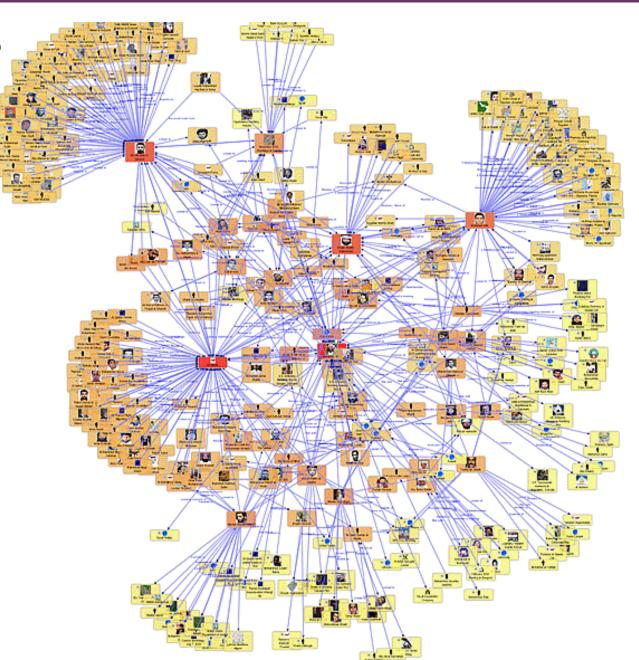




Social Networks

Using Social Network Analysis, you can answer:

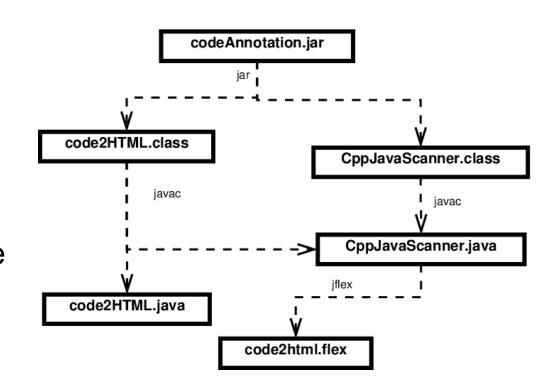
- •How highly connected is an entity within a network?
- •What is an entity's overall importance in a network?
- •How central is an entity within a network?
- •How does information flow within a network?



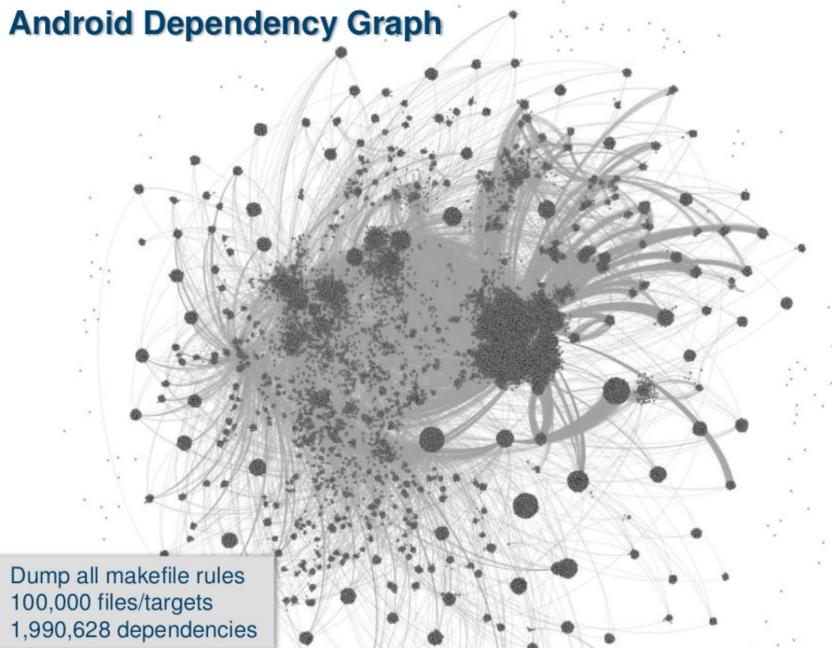
Makefiles

How make Works

- Construct the dependency graph from the target and dependency entries in the makefile
- •Do a topological sort to determine an order in which to construct targets.
- •For each target visited, invoke the commands if the target file does not exist or if any dependency file is newer
 - Relies on file modification dates



Makefile Rules

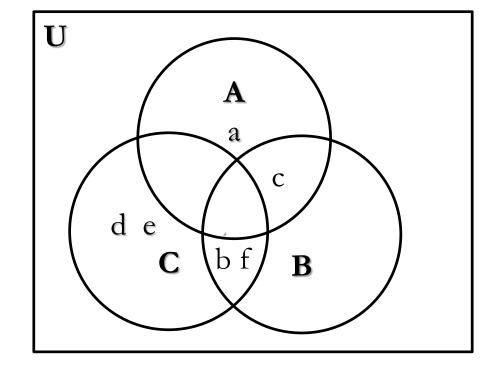


Set Theory

- A set is any collection of objects, e.g. a set of vertices
- The objects in a set are called the elements of the set
- Repetition and order are not important
 - $\{2, 3, 5\} = \{5, 2, 3\} = \{5, 2, 3, 2, 2, 3\}$
- Sets can be written in predicate form:
 - $\{1, 2, 3, 4\} = \{x : x \text{ is a positive integer less than 5}\}$
 - Read the colon as "such that", also {x|x is a....}
- The empty set is $\{\} = \emptyset$, all empty sets are equal

Elements and Subsets

- $x \in A$ means "x is an element of A"
- A ⊆ B means "A is a subset of B"



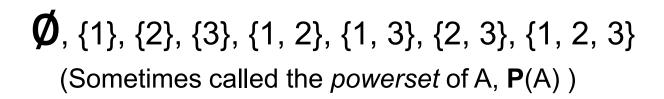
- If A ⊆ B and A ≠ B...
 A is a proper subset of B and we write A ⊂ B
- A ⊆ A for every set A
 - Every set is a subset of itself

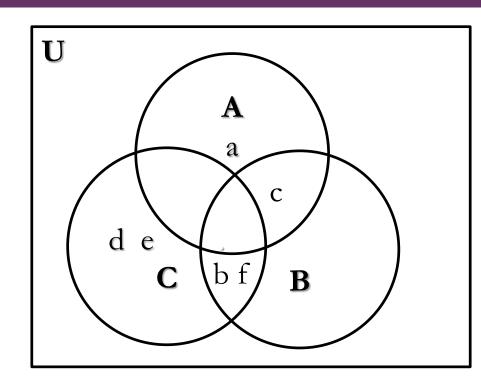
Subsets

- If $A \subseteq B$ and $B \subseteq C$ then $A \subseteq C$
- If $A \subseteq B$ and $B \subseteq A$ then A = B
- The empty set is a subset of every set:

$$\emptyset \subseteq A$$
 for any A

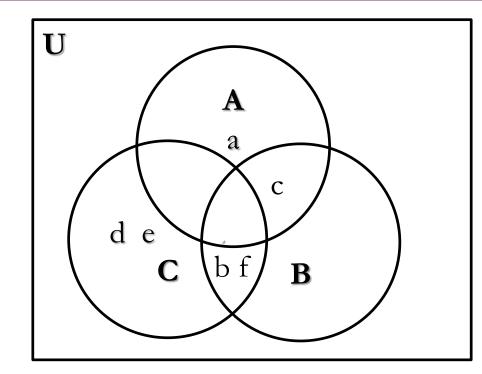






Operations on Sets

- Union
 - $A \cup B = \{ x : x \in A \text{ or } x \in B \}$
- Intersection
 - $A \cap B = \{ x : x \in A \text{ and } x \in B \}$



- Universal Set
 - All sets under consideration will be subsets of a background set, called the Universal Set, U
- Complement
 - A' = $\{x : x \in U \text{ and } x \in A'\}$

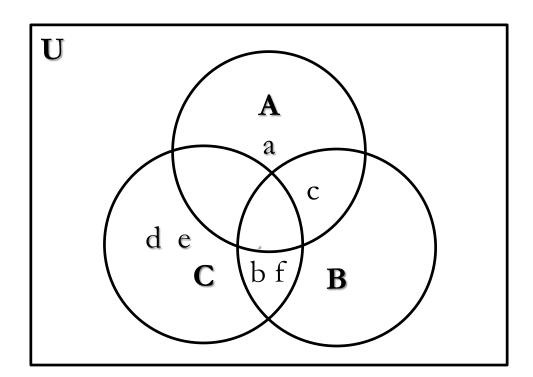
Example

• Let:

- U = {a, b, c, d, e, f}
- $A = \{a, c\}$
- $B = \{b, c, f\}$
- $C = \{b, d, e, f\}$

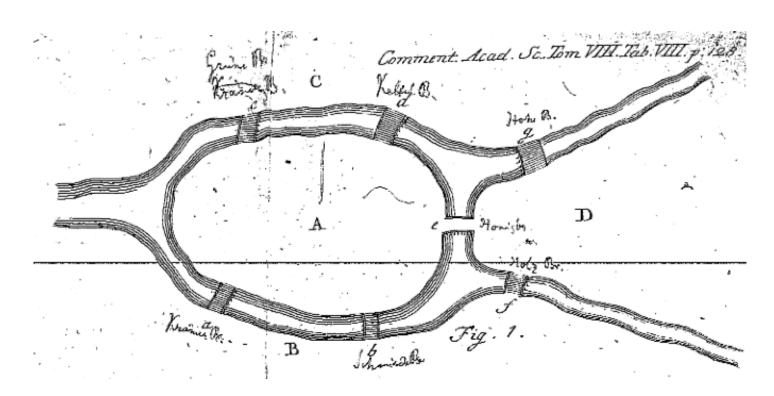
• Then:

- $B \cup C = \{b, c, d, e, f\}$
- $A \cap (B \cup C) = \{c\}$
- A' = {b, d, e, f} = C
- A' \cap (B \cup C) = C \cap (B \cup C) = {b, d, e, f} = C



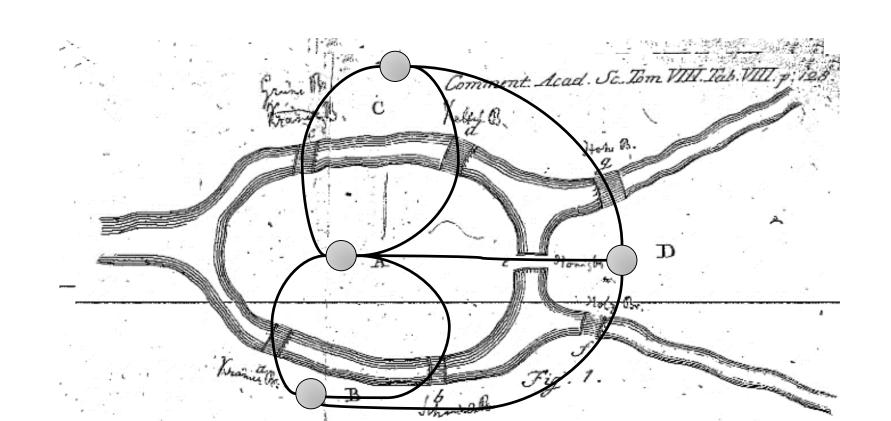
Graph Theory - History

- The town of Konigsberg (now Kaliningrad) is on the banks of the Pregel River, and two islands connected by 7 bridges
- The locals puzzled over whether they could walk across all of the bridges exactly once and return to their starting point



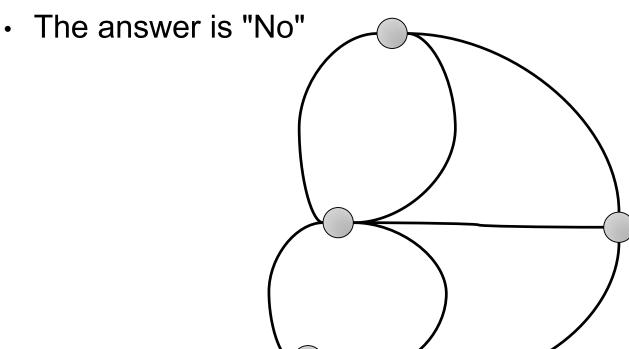
Graph Theory - History

- In 1735, Leonhard Euler (1707-1783) published a paper with a solution to the problem – proving it was not possible
- He abstracted the problem into what became graph theory, based on an idea by Leibniz (1646-1716)



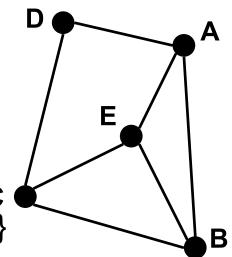
Graph Theory - History

- The solution:
 - "If a connected graph has more than two vertices of odd degree, then it cannot contain an Eulerian path", proved by Euler
 - "If a connected graph has no vertices of odd degree, or two such vertices, then it contains an Eulerian path", Carl Hierholzer, 1873



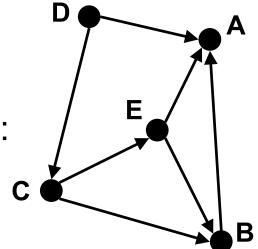
Graph Terminology

- Vertex: A labelled node in the graph
 - A, B, C, D, E
- Edge: An arc joining two vertices
 - {A, B}, {A, D}, {A, E}, {B, C}, {B, E},{C, D}, {C, E}
 - Edges can have weight, direction and labels
 - The two vertices in an edge are the endpoints
- Graph: made up of a set V of vertices and a set
 E of edges
 - $V = \{A, B, C, D, E\}$
 - $E = \{\{A, B\}, \{A, D\}, \{A, E\}, \{B, C\}, \{B, E\}, \{C, D\}, \{C, E\}\}\}$



Graph Terminology - Direction

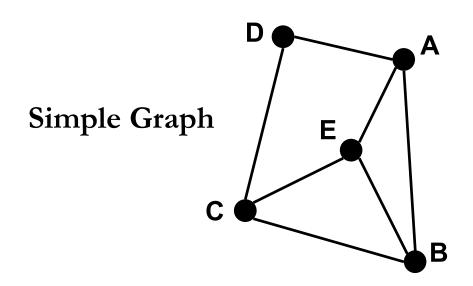
- A graph can be directed or undirected
- Undirected edges in the previous slide were:
 - {A, B}, {A, D}, {A, E}, {B, C}, {B, E}{C, D}, {C, E}

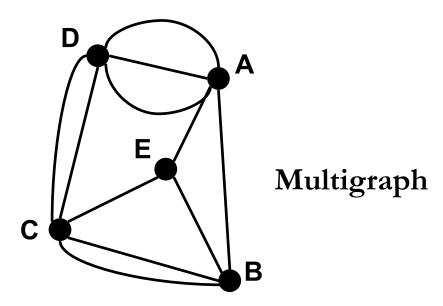


- The directed edge linking A and B is (B,A)
 - Order is important
 - B is the source, A is the sink
- Directed edges in this graph are:
 - $E = \{(D,A), (D,C), (B,A), (C,B), (C,E), (E,A), (E,B)\}$

Multigraphs

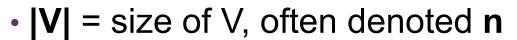
- Multigraphs allow multiple edges between the same pair of vertices
- Graphs that are not multigraphs are referred to as simple graphs



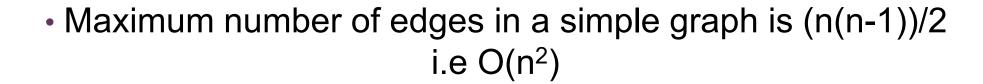


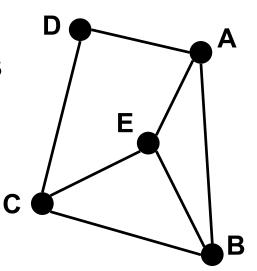
Graph Size

- Given the graph with V vertices and E edges
 - V = {A, B, C, D, E}
 - $E = \{\{A, B\}, \{A, D\}, \{A, E\}, \{B, C\}, \{B, E\}, \{C, D\}, \{C, E\}\}\}$



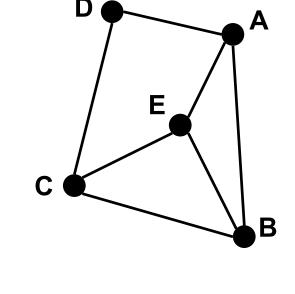
- |E| = size of E, often denoted m
 - |V|= 5
 - |E|= 7

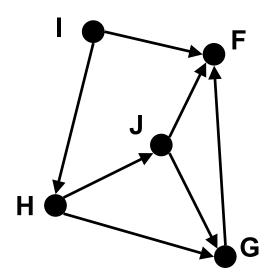




Vertex Adjacency and Degree

- Two vertices are adjacent if they are connected by an edge
 - D is adjacent to A
- The **degree** of a vertex, d(v), is the number of edges for which it is an endpoint
 - d(D) = 2, d(A) = 3





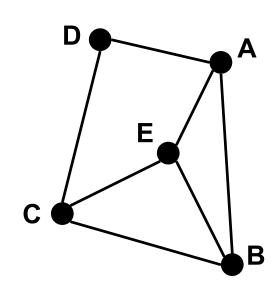
- If the graph is directed...
 - Outdegree of a vertex: the number of edges for which it is the source
 - Indegree of a vertex: the number of edges for which it is the sink
 - ideg(I)=0, odeg(I)=2, d(I)=2
 - ideg(F) = 3, odeg(F) = 0, d(F) = 3

Paths and Cycles

- A path from vertex v_1 to v_2 is a sequence of vertices $v_1, v_2, ..., v_k$, that are connected by edges (v_1, v_2) , (v_2, v_3) ... (v_{k-1}, v_k)
 - Path from D to E: (D, A, B, E)
 - Edges in the path: (D,A), (A,B), (B,E)

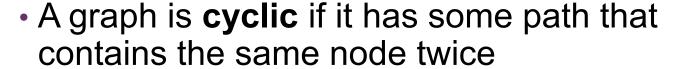


- Vertex u is reachable from v if there is a path for u to v
- A circuit is a path whose first and last vertices are the same

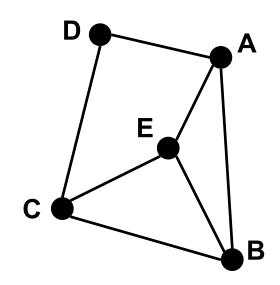


Paths and Cycles

- A simple circuit is a cycle if, except for the first (and last) vertex, no other vertex appears twice
 - e.g. (A,B,E,A) or (D,A,B,E,C,D)

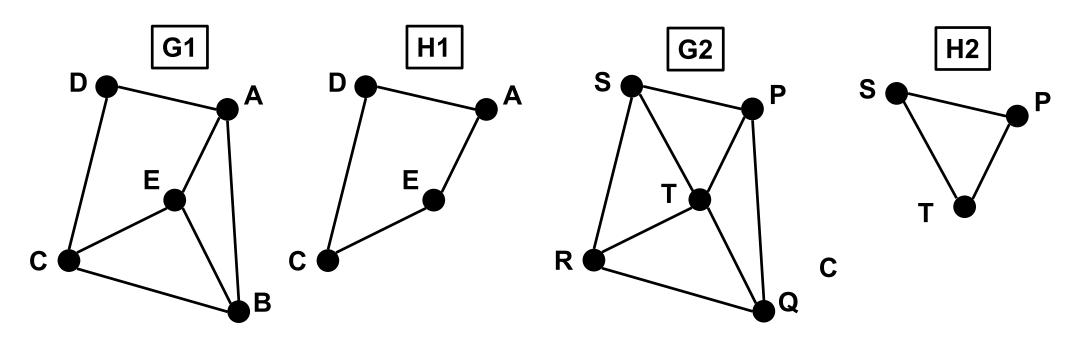


- Otherwise acyclic or non-cyclic
- Trees and linked lists are acyclic
- A Hamiltonian cycle of graph G is a cycle that contains all the vertices of G:
 - (D,A,B,E,C,D)



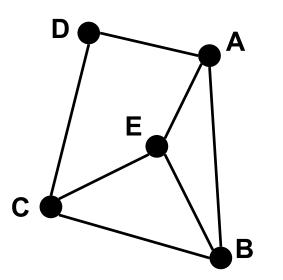
Subgraphs

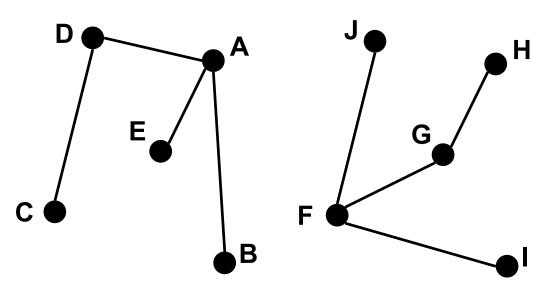
- A subgraph of a graph G = (V, E) is a graph H = (U, F) such that U ⊆ V and F ⊆ E.
 - H1={ [U1: A, E, C, D], [F1: (A, E),(E, C),(C, D),(D, A)] } is subgraph of G1
 - H2={ [U2:S, P, T], [F2: (S, P),(S, T),(T, P)] } is a subgraph of G2A



Graph Connectivity

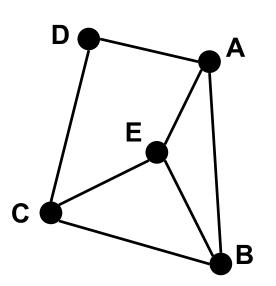
- A graph is said to be connected if there is a path from any vertex to any other vertex in the graph
- A forest is a graph that does not contain a cycle
- A tree is a connected forest
- A spanning forest of an undirected graph G is a subgraph of G that is a forest and contains all the vertices of G.

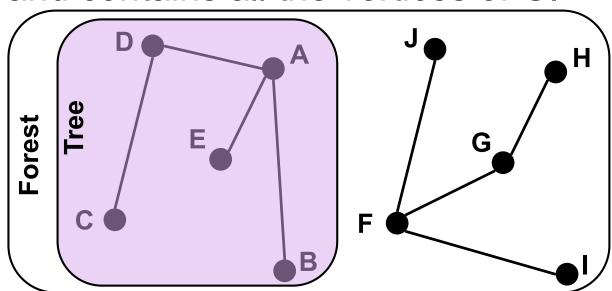




Graph Connectivity

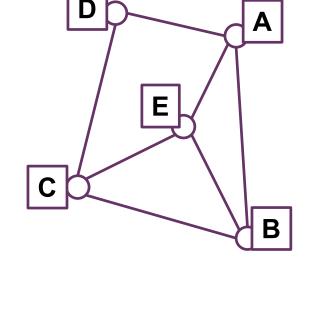
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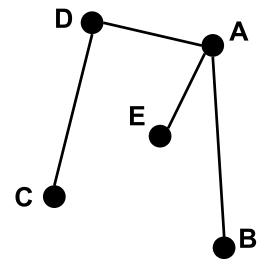


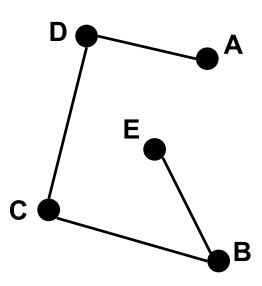


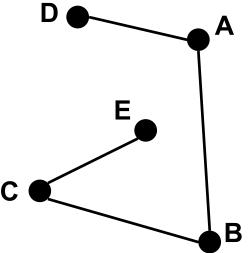
Spanning Trees

- A spanning tree of a graph G is a subgraph of G that is a tree and contains all the vertices of G
- Some spanning trees of this graph → are below:



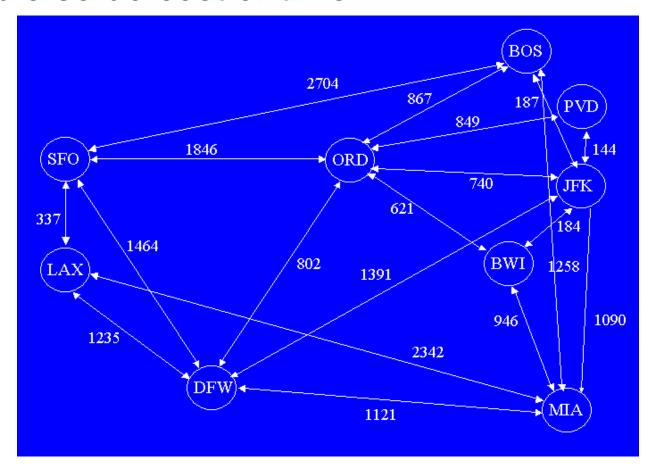






Example: Airport distances

- Nodes represent airports, edges represent flights
- Edge values represent the distance for each flight
- Could also do cost or time



Goodrich and Tamassia,
"Data Structures and
Algorithms in Java"

GRAPH REPRESENTATION AND IMPLEMENTATION

Adjacency Matrix

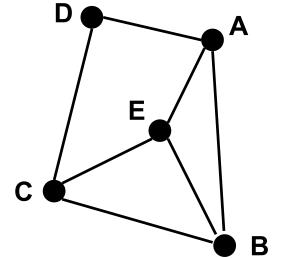
Adjacency List (options: links, nodes, edges)

Graph Representations

- Two main approaches:
 - Adjacency Lists
 - Adjacency Matrices
- Undirected Graphs examples:

Adjacency List

Α	В	D	E
В	Α	С	E
С	В	D	E
D	Α	С	
E	Α	В	С

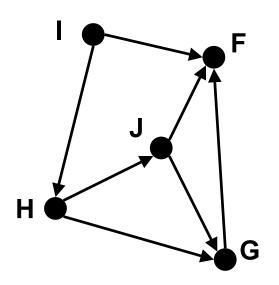


Adjacency Matrix

	Α	В	С	D	E
Α	0	1	0	1	1
В	1	0	1	0	1
С	0	1	0	1	1
D	1	0	1	0	0
Е	1	1	1	0	0

Graph Representations

Directed Graphs - examples:

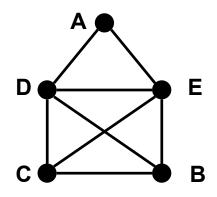


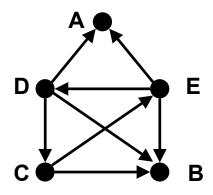
Adjacency List

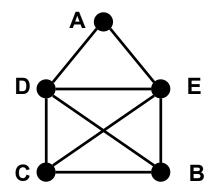
F			
G	F		
Н	J	G	
I	F	Н	
J	F	G	

	F	G	Н	I	J
F	0	0	0	0	0
G	1	0	0	0	0
Н	0	1	0	0	1
I	1	0	1	0	0
J	1	1	0	0	0

PRACTICING GRAPH REPRESENTATIONS

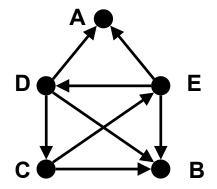






Α	D	Е		
В	С	D	Е	
С	В	D	E	
D	Α	В	С	Е
E	Α	В	С	D

	Α	В	С	D	E
Α	0	0	0	1	1
В	0	0	1	1	1
С	0	1	0	1	1
D	1	1	1	0	1
E	1	1	1	1	0



Α			
В			
С	В	E	
D	Α	В	С
E	Α	В	D

	Α	В	С	D	E
Α	0	0	0	0	0
В	0	0	0	0	0
С	0	1	0	0	1
D	1	1	1	0	0
E	1	1	0	1	0

Graph Implementation

- Graphs can be put together much like trees
 - i.e., a set of nodes linking to other nodes
 - Note: Depending on the application, may not need to implement the nodes just work with adjacency list or matrix
 - Each node has zero or more links
 - We won't know how many when we are building the graph
 - Adjacency List:
 - Use a linked list within each node to connect to other nodes
 - Adjacency Matrix:
 - Use an n x n matrix of Boolean or ones and zeroes (or values to represent weights)

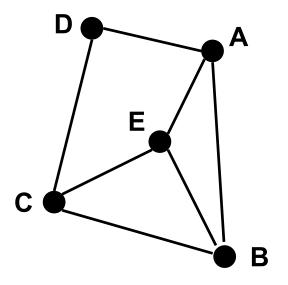
Implementation Analysis

Operation/Space (n vertices & m edges)	Adjacency List	Adjacency Matrix
Contains edge (v _i , v _j)	O(# edges out of v _i)	O(1)
Iterate out-edges of v _i	O(# edges out of v _i)	O(n)
Iterate over all edges	O(n+m)	O(n ²)
Space	O(n+m)	O(n ²)

- Undirected or directed
- Maintain array to lookup labels (O(1))
- Adding vertex means increasing size of array, or start with default capacity and track size (like original stack/queue)...

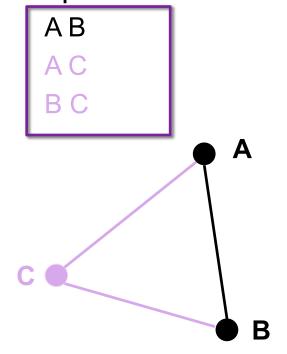
Label Lookup

0	А
1	В
2	С
3	D
4	E



	0	1	2	3	4
0	0	1	0	1	1
1	1	0	1	0	1
2	0	1	0	1	1
3	1	0	1	0	0
4	1	1	1	0	0

- Building a Graph:
 - May have list of vertices, then list of connections (edges)
 - Can also just have list of connections, if label not in list, add vertex before adding edge
- Input file:

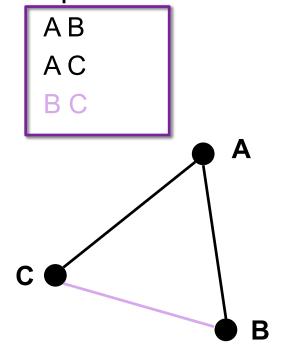


Lookup

0	Α
1	В
2	
3	
4	

	0	1	2	3	4
0	0	1			
1	1	0			
2					
3					
4					

- Building a Graph:
 - May have list of vertices, then list of connections (edges)
 - Can also just have list of connections, if label not in list, add vertex before adding edge
- Input file:

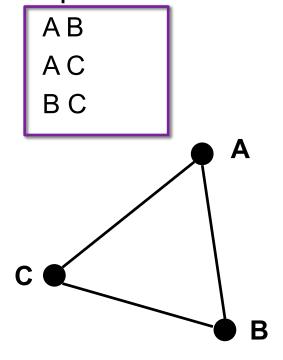


Lookup

0	Α
1	В
2	С
3	
4	

	0	1	2	3	4
0	0	1	1		
1	1	0	0		
2	1	0	0		
3					
4					

- Building a Graph:
 - May have list of vertices, then list of connections (edges)
 - Can also just have list of connections, if label not in list, add vertex before adding edge
- Input file:



Lookup

0	Α
1	В
2	С
3	
4	

	0	1	2	3	4
0	0	1	1		
1	1	0	1		
2	1	1	0		
3					
4					

DSAGraph Class – Adjacency Matrix

 Holds Vertices in 2D array, numbers in matrix are number of edges or a weight between two vertices

```
CLASS DSAGraph
FIELDS: matrix(n x n array), labels (lookup for labels, if needed)
CONSTRUCTOR DSAGraph IMPORTS NONE // could import n, number of vertices
MUTATOR addVertex IMPORTS label[, value] EXPORTS NONE
MUTATOR addEdge IMPORTS label1, label2 EXPORTS NONE
                                                                [brackets]
              // if undirected, add in both directions
                                                                indicate
ACCESSOR has Vertex IMPORTS label EXPORTS boolean
                                                                optional
ACCESSOR getVertexCount IMPORTS NONE EXPORTS int
ACCESSOR getEdgeCount IMPORTS NONE EXPORTS int
ACCESSOR isAdjacent IMPORTS label1, label2 EXPORTS boolean
ACCESSOR getAdjacent IMPORTS label EXPORTS vertexList
ACCESSOR displayAsList IMPORTS NONE EXPORTS NONE
ACCESSOR displayAsMatrix IMPORTS NONE EXPORTS NONE
```

DSAGraph Class – Adjacency Matrix

 Holds Vertices in 2D array, numbers in matrix are number of edges or a weight between two vertices

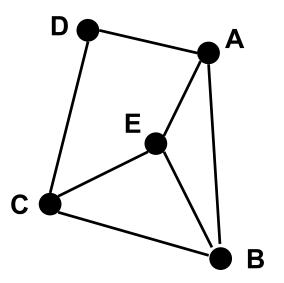
```
DSAGraph
matrix(n x n matrix)
labels
      () or DSAGraph()
+ addVertex(label)
+ addEdge(label1, label2)
+ hasVertex(label): boolean
+ getVertexCount(): int
+ getEdgeCount(): int
+ isAdjacent (label1, label2): boolean
+ getAdjacent (label): vertexList
+ displayAsList()
+ displayAsMatrix()
```

Graph as Adjacency List

- Complexity of implementation depends on program needs:
 - Lists and links (no data)
 - Lists of GraphNodes (data in nodes)
 - Lists of GraphNodes and Lists of Edges

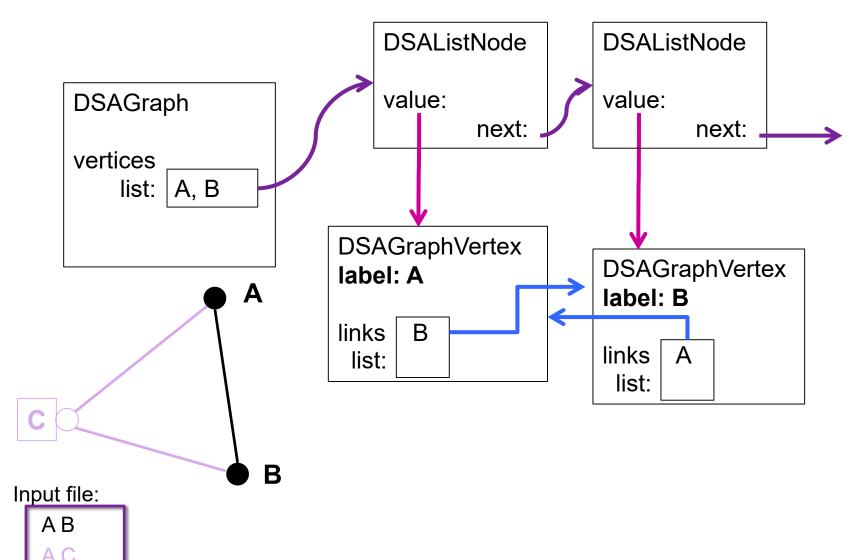
Adjacency List

Α	В	D	E
В	Α	С	E
С	В	D	E
D	Α	С	
E	Α	В	С

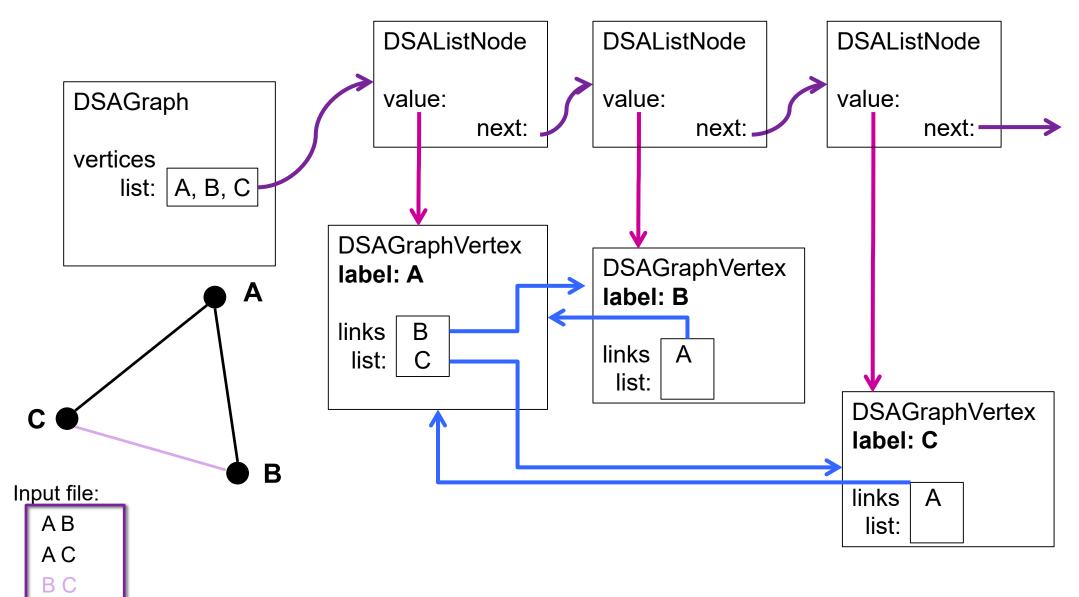


- If you only need to store the links, a very simple structure is possible:
 - Just a linked list of vertices
 - Link up by referencing itself
- We will use a List of GraphNodes to store the information for each vertex

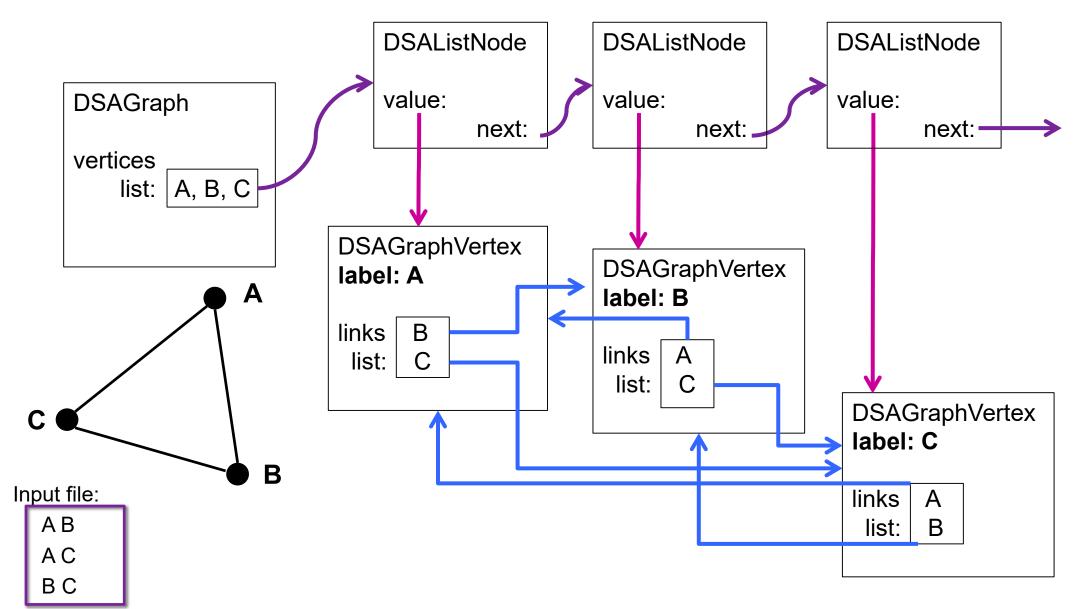
Graph as Adjacency List (use for Pracs)



Graph as Adjacency List (use for Pracs)



Graph as Adjacency List (use for Pracs)



DSAGraph Class – Adjacency List

- Holds Vertices in linked list
- Each Vertex has a label, a possible value and a linked list of neighbours

```
CLASS DSAGraph
FIELDS: vertices (DSALinkedList)
CONSTRUCTOR DSAGraph IMPORTS NONE
MUTATOR addVertex IMPORTS label [, value] EXPORTS NONE
MUTATOR addEdge IMPORTS label1, label2 EXPORTS NONE
              // if undirected, add in both directions
ACCESSOR has Vertex IMPORTS label EXPORTS boolean
ACCESSOR getVertexCount IMPORTS NONE EXPORTS int
ACCESSOR getEdgeCount IMPORTS NONE EXPORTS int
ACCESSOR getVertex IMPORTS label EXPORTS vertex
ACCESSOR getAdjacent IMPORTS label EXPORTS vertexList
ACCESSOR isAdjacent IMPORTS label1, label2 EXPORTS boolean
ACCESSOR displayAsList IMPORTS NONE EXPORTS NONE
ACCESSOR displayAsMatrix IMPORTS NONE EXPORTS NONE
```

Vertices are set up similarly to nodes in linked lists

DSAGraphVertex Class – Adjacency List

- Label is usually a String or an int
- Optional value could be an Object

```
CLASS DSAGraphVertex
FIELDS: label, [value,] links, visited
CONSTRUCTOR DSAGraphVertex IMPORTS inLabel[, inValue]
ACCESSOR getLabel IMPORTS NONE EXPORTS label
ACCESSOR getValue IMPORTS NONE EXPORTS value
ACCESSOR getAdjacent IMPORTS NONE EXPORTS vertexList
MUTATOR addEdge IMPORTS vertex EXPORTS NONE
MUTATOR setVisited IMPORTS NONE EXPORTS NONE //for searching (later)
MUTATOR clearVisited IMPORTS NONE EXPORTS NONE
ACCESSOR getVisited IMPORTS NONE EXPORTS Boolean
ACCESSOR toString IMPORTS NONE EXPORTS string
```

DSAGraph Class – with Edges

- Most complex version
- Has Vertex and Edge objects in lists

```
CLASS DSAGraph
FIELDS: vertices, edges (DSALinkedList) // edges have their own class
CONSTRUCTOR DSAGraph IMPORTS NONE
MUTATOR addVertex IMPORTS label, value EXPORTS NONE
MUTATOR addEdge IMPORTS label1, label2 [edgeLabel, value] EXPORTS NONE
ACCESSOR has Vertex IMPORTS label EXPORTS boolean
ACCESSOR getVertexCount IMPORTS NONE EXPORTS int
ACCESSOR getEdgeCount IMPORTS NONE EXPORTS int
ACCESSOR getVertex IMPORTS label EXPORTS vertex
ACCESSOR getEdge IMPORTS label EXPORTS edge
ACCESSOR getAdjacent IMPORTS label EXPORTS vertexList
ACCESSOR getAdjacentE IMPORTS label EXPORTS edgeList
```

DSAGraphVertex Class

```
CLASS DSAGraphVertex
FIELDS: label, value, [links,] visited
   # edges may be sole keepers of connections -> no "links" in vertex
CONSTRUCTOR DSAGraphVertex IMPORTS inLabel, inValue
ACCESSOR getLabel IMPORTS NONE EXPORTS label
ACCESSOR getValue IMPORTS NONE EXPORTS value
ACCESSOR getAdjacent IMPORTS NONE EXPORTS vertexList
[ACCESSOR getAdjacentE IMPORTS NONE EXPORTS edgeList]
[MUTATOR addEdge IMPORTS edge/vertex EXPORTS NONE]
MUTATOR setVisited IMPORTS NONE EXPORTS NONE //later
MUTATOR clearVisited IMPORTS NONE EXPORTS NONE
ACCESSOR getVisited IMPORTS NONE EXPORTS Boolean
ACCESSOR toString IMPORTS NONE EXPORTS string
```

DSAGraphEdge Class

- May be required if storing weights or other information
- Label is usually a String or an int
 - e.g., weight or relationship are useful labels (uniqueness not important)
- Value can be an int or a more complex Object

```
CLASS DSAGraphEdge
FIELDS: from, to, label, value  # can have label and/or value

CONSTRUCTOR DSAGraphEdge IMPORTS fromVertex, toVertex, inLabel, inValue

ACCESSOR getLabel IMPORTS NONE EXPORTS label
ACCESSOR getValue IMPORTS NONE EXPORTS value

ACCESSOR getFrom IMPORTS NONE EXPORTS vertex
ACCESSOR getTo IMPORTS NONE EXPORTS vertex

ACCESSOR isDirected IMPORTS NONE EXPORTS boolean

ACCESSOR toString IMPORTS NONE EXPORTS string
```

Adding Vertices and Edges

Adding vertices

- Adjacency lists is trivial they don't need to be connected to the rest of the graph straight away
- With adjacency matrix, add to label list (resize matrix if needed)

Adding edges

- Adding edges to an adjacency matrix is trivial (change a value)
- When using adjacency lists means finding both vertices, and adding the vertex or edge to the adjacency list (both directions, if undirected)

DSAGraph Class – optional & additional methods

<may be added as needed, could vary imports/exports, some should be private>

```
ACCESSOR degree IMPORTS vertex EXPORTS int
ACCESSOR hasValue IMPORTS value EXPORTS boolean
ACCESSOR isAdjacent IMPORTS label1, label2 EXPORTS boolean
```

ACCESSOR nextVertex IMPORTS NONE EXPORTS vertex

- can use iterator to go through vertices
- may need to sort them to have a consistent order...

ACCESSOR sort IMPORTS NONE EXPORTS none

- often alphabetical or numeric
- can include sort as part of insert to do incrementally

ACCESSOR display IMPORTS NONE EXPORTS string

Need at least one display method Variations:

- as adjacency lists
- as adjacency matrices
- traverse using DFS or BFS and convert

SEARCHING AND TRAVERSING

Now you have your graph, what are you going to do with it...?

Finding in a Graph

- More tricky than trees and lists as no leaf nodes or tail
- May have cycles, so could go on forever
- Need to keep track of vertices visited
- Approach:
 - Move through the graph, marking vertices as visited
 - On each step, continue through the not visited vertices until all vertices have been visited
- Two basic graph traversal algorithms:
 - Depth-First Search
 - Breadth-First Search
- Later units will cover other graph algorithms

Graph Traversal

- To find a value in a graph, you need to traverse the entire graph in an orderly way
- You may also want to display or store all values in the graph
- Depth-first search is similar to a pre-order traversal of a tree go as deep along each path as possible before returning
- Breadth-first search goes level by level as you move away from the starting point
- Need to mark vertices as visited for algorithms to work

Depth-first Search

depthFirstSearch()

Uses: G = (V, E) in adjacency list format
 v = node on top of stack S
 L[v] refers to the adjacency list of v

Output: The DFS tree T

Could be a queue of objects, or string of labels or a new graph (that's a tree)...

Depth-first Search - Algorithm

 $T = T \cup (v, w)$

mark w as old

push (S, w)

V = W

v = pop S

6.

7.

8.

9.

10.

```
    mark all vertices new and set T = {}
    mark any one vertex v to old // Alpha order preferred
    push (S, v) // push v onto stack S
    while S is nonempty do
    while exists a new vertex w in L[v] do
```

// add to traversal tree

// set visited flag to true

// move along branch...

// store for later...

// backtracking...

Depth-first Search

1

new = {A,B,C,D,E} old = {} T = {} A

new = {B,C,D,E} old = {A} L[A] = {B,D,E} T = {}

2

new={C,D,E}

 $L[B] = \{A,C,E\}$ old = $\{A,B\}$ $T = \{(A,B)\}$ 3

new= $\{D,E\}$ 4

C B

 $L[C] = \{B,D,E\}$ old = $\{A,B,C\}$ $T = \{(A,B),(B,C)\}$

D New ={E}CBA

L[D] ={A,C} old = {A,B,C,D} T={(A,B),(B,C),(C,D)} new ={E}

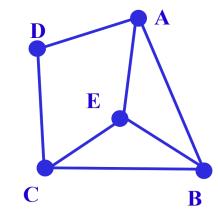
B A

L[C] = {B,D,E} old = {A,B,C,D} T={(A,B),(B,C),(C,D), (C,E)}

E new = {}

B A

L[E]={A,B,C} old = {A,B,C,D,E} T = {(A,B),(B,C), (C,D),(C,E)}



Breadth-first Search

breadthFirstSearch()

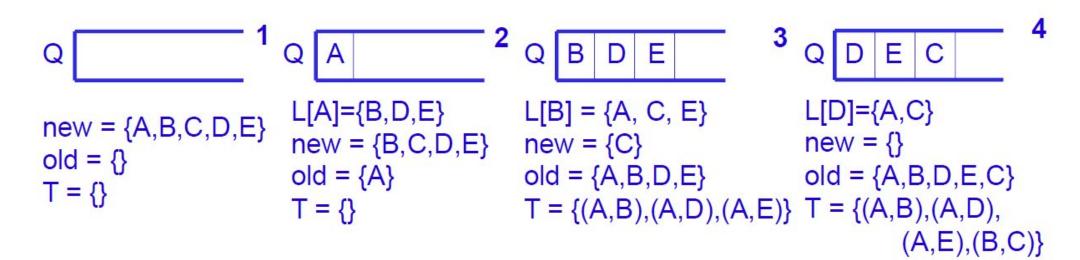
Uses: G = (V, E)
 v = value at front of queue Q
 L[v] refers to the adjacency list of v

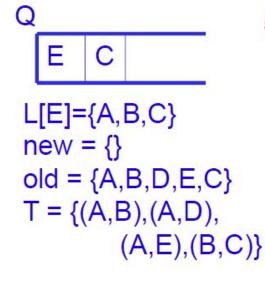
Output: The BFS tree T

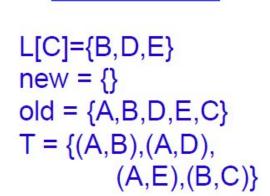
Breadth-first Search – Algorithm

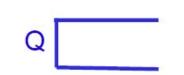
- 1. Mark all vertices new and set T = { }
- 2. Mark the start vertex v = old
- 3. insert (Q, v) // Q is a queue
- 4. while Q is nonempty do
- 5. v = dequeue(Q)
- 6. **for each** vertex w in L[v] marked new do
- 7. $T = T \cup \{v,w\}$
- 8. mark w = old
- 9. insert (Q,w)

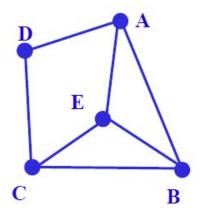
Breadth-first Search











MOTIVATIONAL SLIDES

Graph-based Assignments in DSA...

Graph Applications from Previous Semesters

Assignment Semester 2, 2017

- You are tasked with developing a program to hold information about locations and distances/times by various modes of transportation.
- You will be calculating the shortest path between locations, taking into consideration the transportation options the user requests, and any weather or traffic conditions that exist.
- For each pair of locations, there may be multiple distances and times for a range of travel types: walk, cycle, drive, bus, train, plane etc. Users can select which modes they are interested in travel times for.
- There will also be peak and offpeak times which will be selected based on the indicated mode.

Graph Applications from Previous Semesters

Assignment Semester 1, 2018

- It is 2050. A team of planetary scientists have discovered that there is a network of tunnels underneath the surface of Phoebe, one of the more unusual moons of Saturn.
- They have sent a team of identical robotic probes to Phoebe to map this network of tunnels. Each robot lands at a random point on the surface of Phoebe, drills down through the surface until it hits the tunnel network, then randomly moves through the network building a map. Each robot has sensors that detect various characteristics of the tunnels and their intersections. Oddly enough, they cannot detect each other. The robots regularly upload their maps to Earth for the scientists to process. It is your job to write the program that will process the data from this team of robots and merge it all together.

Graph Applications from Previous Semesters

Assignment Semester 2, 2018

- It is election time 2016. Australia is voting for a new government and Prime Minister to take us through the next 3 years...
- The campaign management team need to get overall information about their position in the lead-up to the election (we will use the 2016 election results as the "poll data")
- They also need to know which divisions should be visited to get maximum impact, and provide an itinerary based on the distances/time between the locations.

Graph Application

Assignment Semester 2, 2019

- You are developing a model to support research into the spread of information through a social network
- The model will need to load in data for a network from a file
- Your program will then simulate the spread of "news" over time, outputting statistics for each run
- Applications could include:
 - Fake news in social media
 - Measles / Ebola outbreaks
 - Zombie apocalyse modelling
- This scenario should allow you to reuse parts of many of your practicals, which you must self-cite

Graph Application

Assignment Semester 1, 2020

- Was going to be "A Day in the Life"
- Given the current pandemic, we will now model spread of disease
- You will need to base it on established models, e.g. SIR
- More complex models will get more marks (see Shiflet ref.)
- These are often "systems models", whereas this assignment requires a graph-based model of population connectedness
- Your code will need to take in parameters including:
 - # Susceptible, Infected population size/proportion (for SIR model)
 - Infectiousness of disease
 - Recovery rate
 - Interventions in place e.g. social distancing, isolation, travel restrictions
- This scenario should allow you to reuse parts of many of your practicals, which you must self-cite

The End

- Helpful website: https://algorithms.tutorialhorizon.com/graph-representation-adjacency-matrix-and-adjacency-list/
- Next Week Hash Tables, then week free, both pracs due after break
- This is when we used to have the mid-semester test.
- Test yourself on past papers ask tutors or Piazza for feedback





