

# Ejercicios de Funcion de Transferencia

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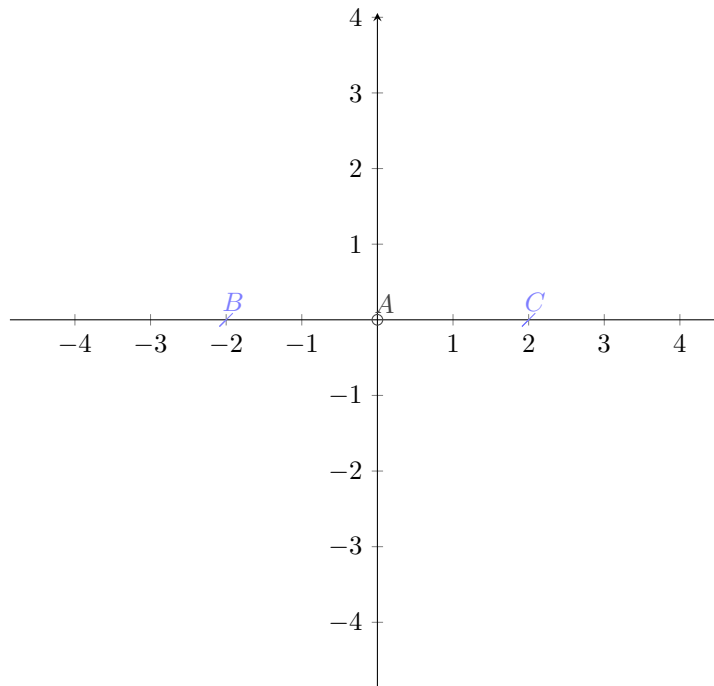
Determinar los ceros y los polos de las siguientes funciones de transferencia y graficarlos en el plano complejo ,decir s el sistema es *estable* o *inestable*

1. La funcion  $F(s) = \frac{(s+3)}{s^2+4}$  Determinar si el sistema es estable o inestable

$$F(s) = \frac{(s+3)}{s^2+4} \quad s^2 + 4 = 0 \quad s = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$s = 0 \pm \frac{\sqrt{0^2 - 4(1)(4)}}{2(1)} \quad s = \pm \frac{\sqrt{-16}}{2}$$

$$s = \pm \frac{\sqrt{-1\sqrt{16}}}{2} \quad s = \pm 2j \quad s_1 = s_2 \text{ \& } s_2 = -2j$$

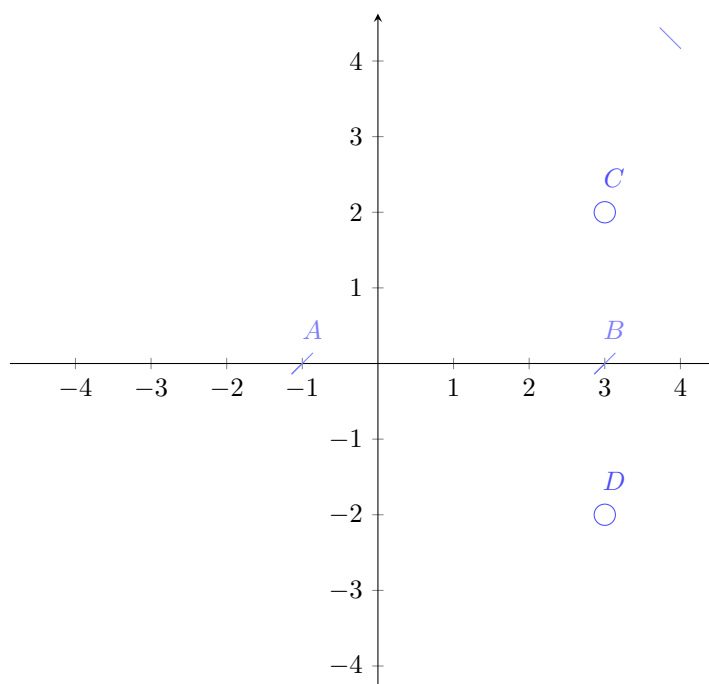


*No es estable*

2. La funcion  $Ft = \frac{s+3}{s^3+2s^2-s-2}$  Determina el estado del sistema.

$$Ft = \frac{s+3}{s^3+2s^2-s-2} \quad s = 0 \pm \frac{\sqrt{0^2-4(1)(1)}}{2(1)}$$

$$= \pm \frac{\sqrt{-4}}{2} = \pm 2j$$



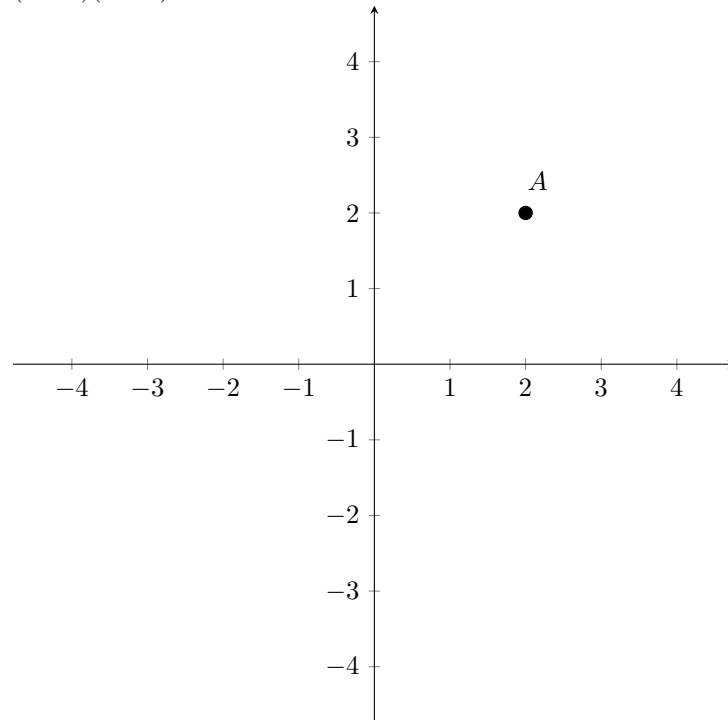
*Es estable*

3.  $Ft = \frac{s-1}{s^2-4s+4}$

$$s^2 - 4s + 4$$

$$s^2 - 4s + 4 = 0$$

$$(s - 2)(s - 2) = 0 \quad s = 2 \text{ \& } s = 2$$



*Es inestable y (estable) al borde*

$$4. Ft = \frac{1}{s^2+s+1}$$

$$s^2 + s + 1 = 0$$

$$s^2 + s + 1 =$$

$$(1)(1)(1)$$

$$s = -1 \pm \frac{\sqrt{1-4(1)(1)}}{2(1)}$$

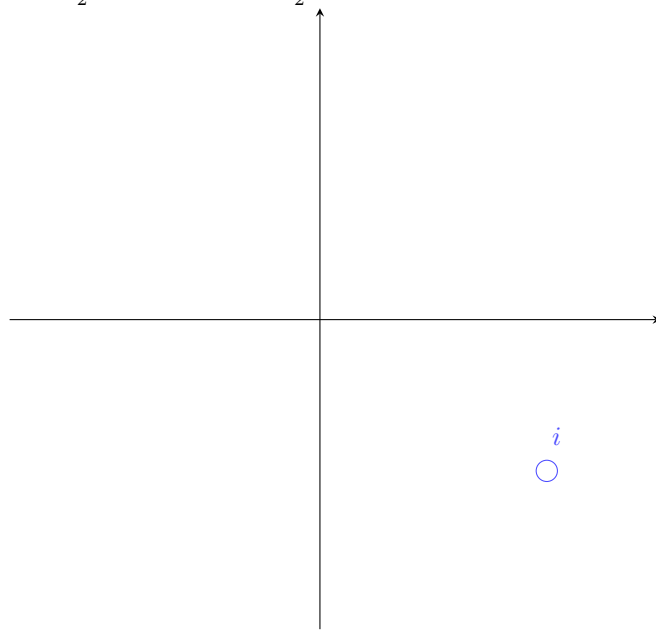
$$= \frac{-1 \pm \sqrt{-3}}{2}$$

$$\frac{1 \pm \sqrt{-3}}{2}$$

$$\frac{-1 \pm \sqrt{3}i}{2}$$

$$s = \frac{-1 + \sqrt{3}i}{2}$$

$$s = \frac{-1 - \sqrt{3}i}{2}$$



*es inestable*