GLMs: Validation

Models behaving badly: Part 2!

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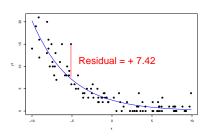
December 3, 2020

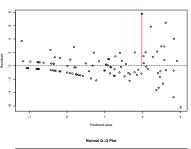
Motivation

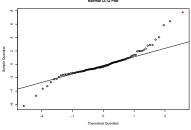
- Are my model results reliable?
 - Residual checks
 - Overdispersion
 - Zero-inflation
- Model selection which terms should I use?
 - log-likelihood, χ^2 tests, and AIC
 - ML vs REML
- Other things
 - Binomial GLMs with >1 trial
 - Offsets in count models
 - R² for GLMs
- Show-and-tell!

Problem 1: Residual checks

- In LMs, residual checks are used to make sure that:
- 1 Terms are linearly related
- ② Generating process is valid
- Variance is constant
- "Regular" residuals don't work this way for GLMs!







There are many kinds of residuals!

In addition to response (regular) residuals there are:

- Working residuals
- Pearson residuals
- Deviance residuals

Deviance residuals use likelihood:

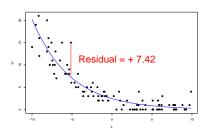
$$r_{dev} = sign(y - \hat{y})\sqrt{2(log(L(y|\theta_s)) - log(L(y|\theta))))}$$

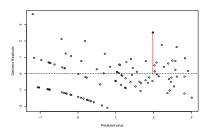
- This may look scary, but R does this all for you!
- These are analogous to regular residuals in LMs
- For more about the different kinds of residuals, see here

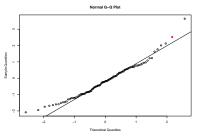
Solution: use deviance residuals for GLMs

Keep in mind:

- Residuals from GLMs will never be as "pretty" as those from LMs
- Especially true for:
 - Binomial GLMs
 - Poisson/Negative Binomial GLMs with many zeros

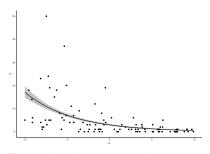






Problem 2: Overdispersion

- Binomial and Poisson families have **no** variance term (e.g. SD).
- Sometimes this assumption doesn't work!
- This is very common for Poisson models



Example: data are much more variable than the predictions from the model

Problem: Overdispersion

```
##
## Call:
## glm(formula = v1 ~ x, family = "poisson", data = d1)
##
## Deviance Residuals:
      Min
                10 Median
                                         Max
## -2.0843 -0.9460 -0.1897 0.5333 3.6416
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.89455 0.07818 11.44 <2e-16 ***
              -0.21145 0.01174 -18.01 <2e-16 ***
## x
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
      Null deviance: 564.27 on 99 degrees of freedom
## Residual deviance: 106.20 on 98 degrees of freedom
## ATC: 362.01
## Number of Fisher Scoring iterations: 5
```

- In a regular Poisson or Binomial model, Residual deviance \div Degrees of Freedom should be ~ 1
- Residual deviance is the sum of all deviance from the model
- This model looks OK (106.2 \div 98 = 1.08)

Problem: Overdispersion

```
##
## Call:
## glm(formula = v2 ~ x, family = "poisson", data = d1)
## Deviance Residuals:
      Min
                1Q Median
                                         Max
## -4 1009 -1 7543 -0 8805 0 4796 8 6102
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 1.07897 0.06871 15.70 <2e-16 ***
              -0.17581 0.01069 -16.44 <2e-16 ***
## x
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
      Null deviance: 851.96 on 99 degrees of freedom
## Residual deviance: 501.98 on 98 degrees of freedom
## ATC: 735.46
##
## Number of Fisher Scoring iterations: 5
```

- This model does **not** look OK (501.98 \div 98 = 5.12)
- Generated using Negative Binomial, but fit to Poisson

Causes

Overdispersion can be caused by different things:

- Using the wrong probability distribution
 - e.g. Poisson, but should be Negative Binomial
- Lots of zeros in count data
 - e.g. Very short observation period
- Leaving out an important term
 - e.g. An important interaction term was omitted
- Random effects¹ not accounted for
 - e.g. Data collected at different sites, but ignored

¹Random effects discussed later

Solutions for overdispersion

Try the following (in this order):

- 1 Consider terms that may have been left out
 - Fixed effects
 - 2 Random effects
- 2 Try distributions that account for overdispersion
 - 1 Negative Binomial, Beta Binomial, Zero-inflated Poisson²
 - 2 Quasi-binomial² and quasi-poisson²
 - 3 Transform counts to presence/absence
- 3 Lower your expectations, and use a lower critical p-value (e.g. 0.01 instead of 0.05)
- 4 Design a better study :(

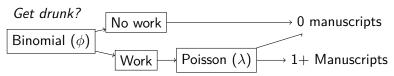
²These can be annoying to deal with, so avoid if possible

Zero-inflation: drunk monks

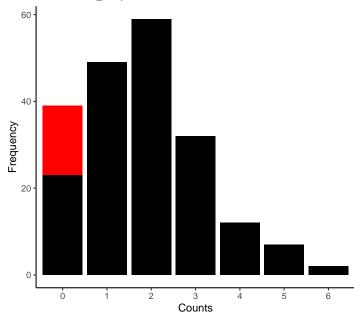
An analogy:

- 1 Monks at a monastary make copies of manuscripts. Most days they make very few (0 or 1), but occasionally they make many (2-5)
- Some days they decide to try out the beer that's been brewing in the cellar! No manuscripts get made on those days.
- 3 The number of manuscripts made (per day) follows a zero-inflated Poisson distribution

This is *mixture* of a Poisson and a Binomial:

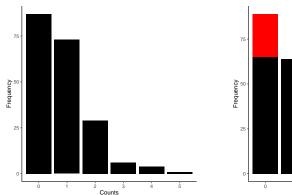


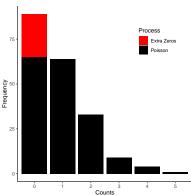
Zero-inflation: graphical model



Problem: hard to fit

- Hard for R to tell the difference between ZIP/ZINB, and a Poisson/NB with a low mean (λ).
- This needs a lot of data in order to work! Consider longer sampling periods in order to reduce zeros





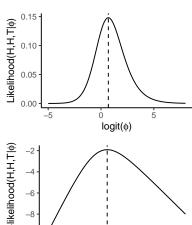
Model selection

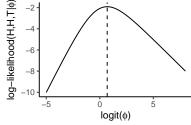
How many terms should be in my model?

- Same principle as in regular linear models: what do you think the process is? (see Lecture 4)
- Perhaps some terms should always be included on principal?
- To test whether terms are important in predicting your data, use likelihood-ratio tests
 - AIC tests usually say the same thing as LR tests
 - drop1(model,test='Chisq')

log likelihood

- Probabilities multiplied together quickly become very small
- Computers can't distinguish between extremely big or small numbers
- Therefore, it uses log-likelihoods (also easier to calculate)





ML vs REML

- Maximum likelihood (ML) estimates of variance (e.g. SD) are always smaller than the actual variance (biased)
- Restricted maximum likelihood (REML) uses a mathematical trick to get around this, but...
- This means that models with different numbers of terms don't have the same REML estimates
- Likelihood between these models technically can't be compared!

Solution = Use ML if comparing between models with different fixed effects, then re-fit with REML once you've decided on a model

Other things!

- Binomial GLMs with >1 trial
- Offsets in count models
- R^2 for GLMs

Binomial GLMs with >1 trial

- If you're measuring single "success/failures", 1s and 0s are used
- If multiple trials occur, R requires counts of successes and failures
- Example: "I counted male and female critters at different sites. How do I tell if temperature affects sex ratios?"

```
#Number of females and males are in 2 separate columns in d1
glm(cbind(females,males) ~ temperature, family='binomial',data = d1)
```

This will correctly account for different numbers of critters ("trials") at each site

Offsets in count models

- Poisson/NB models assume that counts occur over the same period of time
- Count models use integers only, so you can't just do: counts ÷ hours
- Solution: use *offsets* to deal with different observation times
 - Predictor with a slope fixed at 1
- Example: "I counted critters for different lengths of time at each site. How do I tell if temperature affect counts?"

```
#hours = observation time at each site, and
# must be log-transformed before being used in an offset
#
glm(counts ~ offset(log(hours)) + temp, family='poisson',data = d1)
```

This will return estimates that have been scaled to a 1-hour observation time

R-squared for GLMs

- Bad news: there isn't really any good way to get R² (explained variance) for non-1m models
- OK news: there are many $pseudo-R^2$ measures that are sort of like R^2 , but nobody really agrees on which one is best
- Good news: ecologists tend to not know or care about this

Solution: pick a single type of \mathbb{R}^2 and use that, or omit it completely 3

- See here, here or here for more info on R^2
- Try rsquaredglmm() from piecewiseSEM or r.squaredGLMM() from MuMIn

³But be prepared to argue with supervisors, committee members, or reviewers! They will want some kind of measure of how well your model predicted your data.

Show-and-tell!

