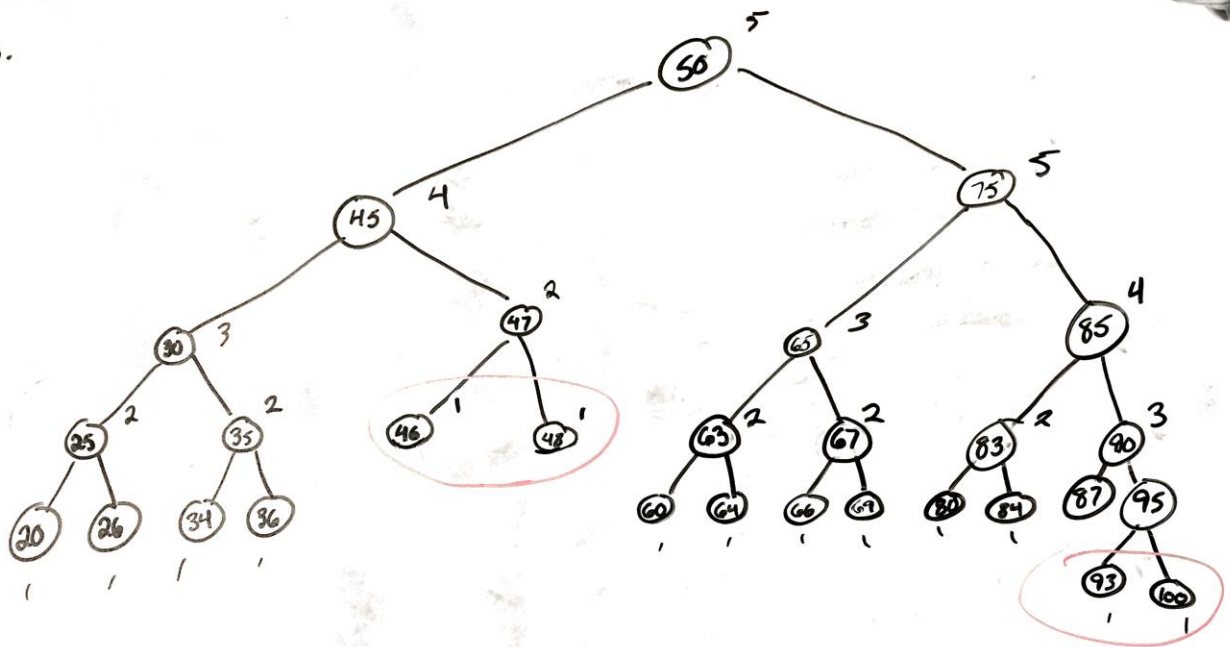


1a. the depth of the shallowest leaf can be no less than the depth of the deepest leaf minus 1 ($d_{max} - 1$)

1b.



2. Max tree height, both red and black nodes, w/ black-depth of 3?

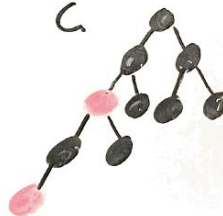
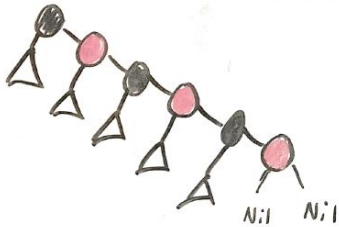
of edges

∝. Max depth of 5

6.

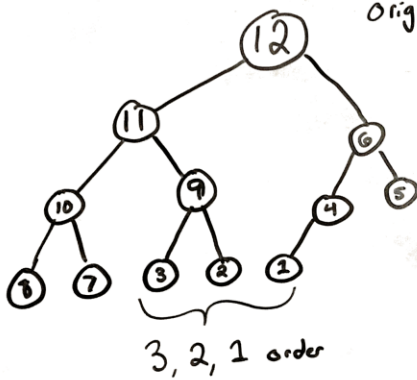
Min # of internal
Nodes to produce in a.?

10 internal Nodes

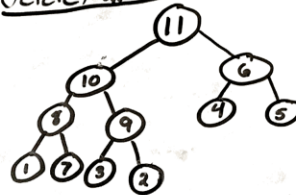


3.

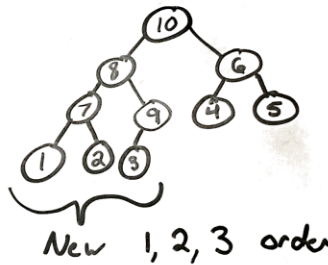
original heap



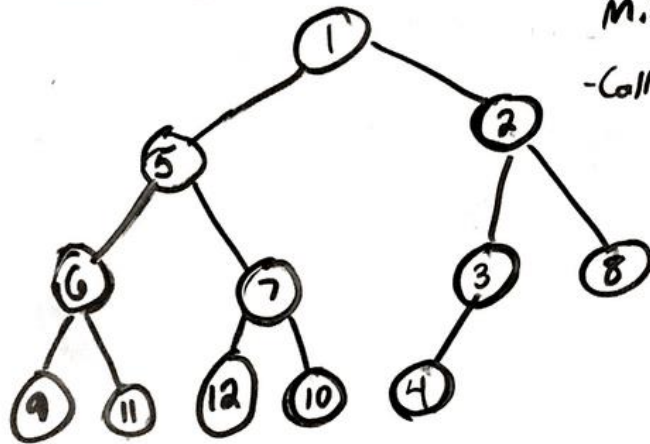
delete Max call



deleteMax call



4a.



min heap

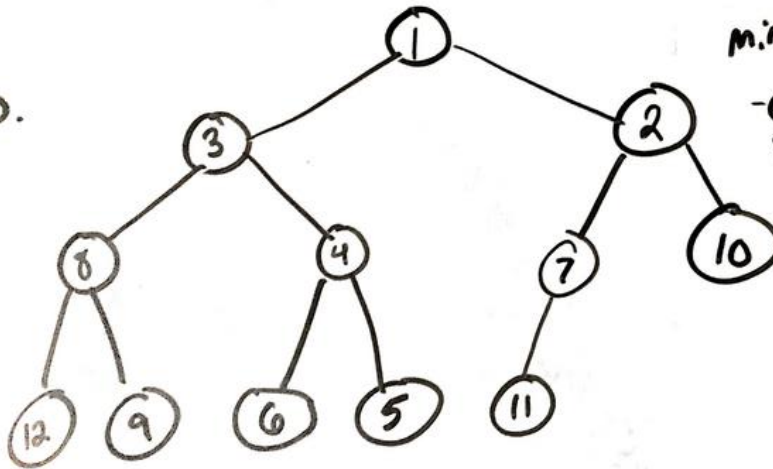
-Calling delete on

6 will cause

4 to replace and

it will bubble up

4b.



min heap

-Calling delete on

8 will cause 11

to replace and it

will trickle down

4c. It is not possible to construct a heap that will fit the parameters. The reason being is if we construct a heap we will have the same replacement value for both cases. In order for us to replace a value for 6 in a heap and have that value bubble up to the top, that value needs to be 5 or lower. By contrast, in order for us to replace the value 8 and have it trickle down the heap, it must be 9 or greater. Since there is no overlap for these number sets, therefore it is impossible to have the parameters met.