

## **Two classes of multi-model candidate management procedures for Atlantic bluefin tuna.**

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### **Abstract**

We developed two classes of management procedures for Atlantic bluefin tuna based on multi-model inference. The basis of the procedures were estimation methods tuned to five operating models from the reference OM grid. For the empirical class, we used OM catchability and a stationary stock mixing distribution to estimate area biomass from the larval indices. For model-based class of MPs, we tuned 5 delay difference assessment models to each of the 5 operating models, matching stock recruit steepness and biomass for the recent historical period from 1965 - 2016. At each time step, estimates of current (empirical) or projected (model-based) biomass were generated from approved management indices. These estimates were used in harvest control rules to generate area-specific TACs, and the five TACs were averaged to produce harvest advice for the East and West area. Multiple MPs were then defined based on varying precautionary TAC caps, maximum target harvest rates, and HCR control points. We found that MPs with lower caps, lower maximum harvest rates and control points avoided overfishing on the reference grid more often. We also found that the subset of OMs that our AMs were tuned to managed to capture the uncertainty well.

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## 1 Introduction

The International Commission for the Conservation of Atlantic Tunas (ICCAT) is currently conducting a management strategy evaluation (MSE) for Atlantic bluefin tuna (ref ICCAT 2019). The technical core of an MSE is closed loop simulation testing of candidate management procedures (CMPs) that provide harvest advice in the presence of uncertainty. Uncertainty is captured by a set of operating models, which represent a plausible range of states for the management system.

The operating models for Atlantic bluefin tuna are based on different hypotheses (fits) of a multi-stock, multi-area, age- and length-structured model known as the Modifiable Multi-stock Model (M3), with 4 fishing seasons per year, that allow for mixing of fish from both stocks in each area in a given season (**REF TSD**). Given the inherent complexity of such a model, it is impossible to use the same structure within a management procedure, as management procedures must be able to be tested within simulations in a timely manner. Therefore, management procedures must be designed that are of lower levels of complexity than the operating model.

In this paper, we develop and test two classes of CMPs that use multi-model inference to provide harvest advice in the MSE framework. The first class is based on an empirical index-based method of estimating spawning stock biomass, and the second replaces the empirical method with a multi-stock state-space delay difference stock assessment model. Both classes are made up of five biomass estimation and harvest control rules that are tuned to one of five reference grid operating models. Catch advice from each sub-procedure is then combined to produce area-specific TACs.

## 2 Methods

Our candidate management procedures were based on multi-model inference [rossi2019inferring], combining estimates of biomass and associated catch advice from sub-procedures tuned to a subset of the reference grid of multi-stock operating models. This multi-model formulation allowed us to capture the biological uncertainty represented by the reference grid of operating models.

We defined two classes of MP: empirical and model based. The empirical MPs scale larval indices by OM estimates of catchability, while the model-based MPs fit state space delay difference assessment model to management indices.

### 2.1 Choice of operating models

Some of the following can be moved to the subsections...

We chose a tuning subset of five reference grid operating models to tune our estimation procedures. These five OMs were chosen to span the three main axes of operating model uncertainties (stock-recruit steepness, natural mortality/maturity, and stock mixing), as well as the range of spawning stock biomass scales and dynamics (Figure 1).

### 2.2 Empirical Estimation Procedure

The empirical estimation procedure used a simple moving average of the two spawning stock larval survey indices. For each time step  $t$ , and stock  $s \in \{GOM, MED\}$  the current average larval index is calculated as

$$\bar{I}_{s,t} = \frac{\sum_{t'=t-3}^t I_{s,t'}}{4}, \quad (1)$$

where  $I_{s,t}$  is the larval index for stock  $s$  at time  $t$ . We then scaled the smoothed survey indices to multiple biomass estimates, one for every operating model in the tuning subset, by using the appropriate larval survey

catchability parameter, e.g

$$\hat{B}_{s,t,k} = \frac{\bar{I}_{s,t}}{q_{s,k}}, \quad (2)$$

where  $q_{s,k}$  is the stock larval index catchability parameter from the tuning operating model  $k \in \{1, 2, 4, 7, 11\}$ .

Spawning stock biomass was then translated to area biomass using an assumed constant distribution of biomass for stock mixing

$$P = (p_{s,a}) = \begin{pmatrix} .898 & .102 \\ .1 & .9 \end{pmatrix}, \quad (3)$$

found by averaging the proportion of stock biomass in each area over the historical period in the tuning set of OMs. The rows of matrix  $P$  are indexed by spawning stocks  $\{MED, GOM\}$ , and the columns are indexed by management area  $\{E, W\}$ . This generates an area specific biomass

$$B_a = \sum_s p_{s,a} B_s, \quad (4)$$

where  $s \in \{MED, GOM\}$ ,  $a \in \{E, W\}$ .

## 2.3 Delay Difference Model

For the model-based class of procedures, the simple index scaling method of the empirical procedure is replaced by a state-space multi-stock delay difference assessment model. The two spawning stocks are assumed to be distinct spawning stocks for the larval surveys, but are mixed using the distribution  $P$  for the other management indices and the observed catches.

### 2.3.1 Equilibria

Because there is no mixing of spawners, each stock has the simple Delay Difference equilibrium states, which can be expressed as a function of long-term fishing mortality  $f = F_s$ . The equations for equilibria in Table 1 were used to initialise the model at a fished equilibrium in 1965, as well as estimate biological reference points for use in the harvest control rules.

### 2.3.2 Biomass time series reconstruction

Each assessment model was initialised in a fished state in 1965. To do so, we estimated an initial fishing mortality rate  $F(s, 0)$ , and assumed that the stock was at the fished equilibrium defined in Table 1. Other free parameters were unfished biomass  $B_{s,0}$ , catchability  $q_g$  and observation error uncertainty  $\tau_g$  for biomass and abundance indices, and recruitment process error deviations  $\omega_{s,t}$  for  $t \in 1966, \dots, 2014$  (Table 2).

We assumed the that proportion  $p_{s,a}$  of stock  $s \in \{MED, GOM\}$  in area  $a \in \{E, W\}$  was constant, allowing the fluctuations in stock biomass to account for the mixing dynamics. We also assumed that the stocks were homogeneously mixed in each area, so that total stock specific catch was the sum of the area specific catches, split according to the proportion to the stock biomass in each area (eqn ref).

We used a numerical Newton-Rhapon method to solve for instantaneous fishing mortality at all time steps  $t \geq 1$ , which were used in the survival calculation to progress numbers and biomass to the next time step.

Random walk in process errors...

Because this is a model-based MP and the time-series of approved management indices are rather short, we included two additional indices. These indices were the M3 model yearly spawning stock biomass estimates for the East and West stocks. These biomass time series were assumed to be observed with catchability  $q = 1$  and an observation error CV of 5%. This allowed our AMs to estimate catchability for the approved indices and scale them to the spawning stock biomass, which was required for extending the fit to the approved indices in the projections, as well as making sensible estimates of biological parameters despite the complexity difference between the operating model and the assesment models.

### 2.3.3 Reference Points

Reference points for each stock were estimated from the equilibrium values in (Table 1). The optimal fishing mortality rate  $F_{MSY}$  was found by numerically solving for the stationary point of the yield curve, and was in turn used to estimate the optimal equilibrium biomass  $B_{MSY}$  associated with that mortality rate.

We estimated area based reference points for use in harvest control rules, which were the stock-area biomass weighted averages of the stock-specific reference points, i.e.

$$B_{MSY,a} = \sum_s \frac{B_{s,a}}{B_a} B_{MSY,s}, \quad (5)$$

$$F_{MSY,a} = \sum_s \frac{B_{s,a}}{B_a} F_{MSY,s}, \quad (6)$$

where  $B_{s,a} = p_{s,a} B_s$ .

## 2.4 Harvest Control Rules

SAM: make a table of HCR design dimensions (UCPs, Umax, Caps)

For each of the five sub-procedures we defined a ramped harvest control rule with upper and lower control points and a maximum harvest rate. The control points and maximum harvest rates for these rules were based

either based on the associated operating model's biological reference points, or the , and a precautionary TAC cap was used to limit removals in cases of bias in projected biomass or reference point estimates.

Our ramped harvest control rule was based off the rules used for albacore tuna [ref]. These rules requires an upper control point ( $UCP$ ), a lower control point ( $LCP$ ) and a maximum target harvest rate  $U_{max}$ . The general form of the rules (ignoring AM, area, and stock indices):

$$U_{targ} = \begin{cases} 0.1 \cdot U_{max} & B \leq LCP \\ U_{max} * (0.1 + 0.9 \frac{B}{UCP-LCP}) & LCP \leq B \leq UCP \\ U_{max} & UCP \leq B \end{cases} \quad (7)$$

For all HCRs, we set  $LCP = .4UCP$ , and tested two options for the upper control point:  $UCP = B_{MSY}$  or  $UCP = .4B_0$ . We also tested two options for the maximum target harvest rate at  $U_{max} = F_{MSY}$  and  $U_{max} = \frac{2 \cdot M}{3}$ . Under the empirical management procedures, control points were taken from the tuning grid of operating models, while under the model-based MPs, control points were taken as the delay difference model equilibria.

Both home-stock- and area-based harvest control rules were applied for East and West area TACs. For example, in the East area, HCRs were applied based on East (MED) spawning stock biomass compared to the East stock control points and harvest rates, and East area biomass compared to mixed stock control points and harvest rates. Mixed area based control points and harvest rates were averaged over the two stocks present in the area, weighted by the proportion of stock specific biomass in that area (e.g. see area-based reference points calcs in previous section), and the lower of the two TACs was chosen. From this, the West TAC would almost always be managed according to the Gulf of Mexico spawning stock harvest control rules, and the East TAC would almost always be managed according to the mixed East Area harvest control rule, as this includes the weaker stock.

We applied a TAC cap in each area to make the HCRs more precautionary. This extra precaution is required to guard against optimistic assessment errors and biases in reference point calculations, both of which are

caused by the complexity mismatch between the AMs and the OMs. We tested three kinds of caps: a high cap of 25 kt in the East, and 4 kt in the West; a low cap of 20 kt in the East, and 2.5 kt in West; and a cap of the stock and area based MSY, which was derived from assessment model equilibria (Table 1).

## 2.5 Providing catch advice by area

To provide a single TAC at each time step we averaged over the TAC advice from the 5 sub-procedures for both the empirical and model-based MPs. For the model-based MP, we tested two weightings for the averaging: equal weighting (standard mean), and weighting by Akaike’s Information Criterion (AIC). For the empirical MPs, we fully tested only a simple average weighting, but started development on a stochastic approximation method to tune the weighting to specific biomass objectives.

To calculate the AIC weighting across the tuning grid, we used only the observation model likelihood components for the approved management indices. This is because the approved management indices were data that were common among the tuning grid AMs, while the included OM spawning stock biomass indices differed between AMs, invalidating the assumptions of AIC.

Final TACs were then smoothed with respect to the previous management interval’s TAC. This smoothing allowed a maximum increase of 20%, and a maximum decrease of 50%, compared to the previous management interval.

## 3 Results

### 3.1 Fits of Delay Difference AMs to historical data

The addition of spawning stock biomass as absolute stock indices allowed the delay difference models to fit to historical biomass well.

### 3.2 Performance in projections

#### 3.2.1 Empirical MPs

#### 3.2.2 Delay Difference Model-based MPs

## 4 Discussion

## 5 Tables

Table 1: Unfished and fished equilibrium quantities for the delay-difference population dynamics.

Description	Equation
Survivorship	$S^{(f)} = e^{-M-f}$

Description	Equation
Average Weight	$\bar{w}^{(f)} = \frac{S^{(f)}\alpha + w^{(k)}(1-S^{(f)})}{1-\rho S^{(f)}}$
Unfished Numbers	$N = B_0/\bar{w}^{(f=0)}$
Unfished Recruitment	$R_0 = (1 - S^{(f=0)})N_0$
Stock-Recruit	$a = \frac{4hR_0}{B_0(1-h)}, b = \frac{5h-1}{B_0(1-h)}$
Biomass	$B^{(f)} = \frac{S^{(f)}(\alpha + \rho\bar{w}^{(f)}) + \bar{w}^{(f)}(aw^{(k)} - 1)}{b(\bar{w}^{(f)} - \rho S^{(f)}\bar{w}^{(f)}) - \alpha S^{(f)}}$
Recruitment	$R^{(f)} = \frac{aB^{(f)}}{1+bB^{(f)}}$
Yield	$Y^{(f)} = \frac{f}{M+f}(1 - e^{-M-f})B^{(f)}$



Table 2: Process and observation model components of the delay difference stock assessment model used in BC Sablefish management procedures. Initialisation values for biomass, numbers, and recruitment are equilibrium unfished values from Table 2.

No.	Equation
<b>Model Free Parameters</b>	
A2.1	$\theta_s = \{\log F_{s,0}, \log B_{s,0}, q_g, \tau_g, \vec{\omega}_{s,t}\}.$
<b>Initialisation (<math>t = 1</math>)</b>	
A2.2	$B_{s,1} = B_s^{(f=F_{s,0})}$
A2.3	$N_{s,1} = N_s^{(f=F_{s,0})}$
A2.4	$R_{s,1} = R_s^{(f=F_{s,0})}$
<b>Mixed Area Biomass</b>	
A2.5	$B_{s,a,t} = p_{s,a} \cdot B_{s,t}$
A2.6	$B_{a,t} = \sum_s B_{s,a,t}$
<b>Stock Specific Catch</b>	
A2.7	$C_{s,t} = \sum_a \frac{B_{s,a,t}}{B_{a,t}} C_{a,t}$
<b>Time series Reconstruction (<math>2 \leq t \leq T</math>)</b>	
A2.8	$R_{s,t} = \begin{cases} R_{s,1} e^{\omega_{s,t-k} - \sigma^2/2} & t \leq k \\ \frac{aB_{s,t-k}}{1+bB_{s,t-k}} e^{\omega_{s,t-k} - \sigma^2/2} & t > k \end{cases}$
A2.9	$Z_{s,t-1} = M_s + F_{s,t-1}$
A2.10	$N_{s,t} = e^{-Z_{s,t-1}} N_{s,t-1} + R_{s,t}$
A2.11	$B_{s,t} = e^{-Z_{s,t-1}} (\alpha N_{s,t-1} + \rho B_{s,t-1}) + w_s^{(k)} R_{s,t}$
<b>Statistical Model</b>	
A2.12	$\hat{I}_{g,t} = q_g \cdot B_{s,t}$
A2.13	$\hat{I}_{g,t} = q_g \cdot B_{a,t}$
A2.14	$\log I_{g,t} \sim N(\log \hat{I}_{g,t}, \tau_g)$
A2.15	$\omega_{s,t} \sim N(0, \sigma)$

Table 3: Delay difference assessment model estimates of unfished biomass, natural mortality, and biological reference points, when fit to the tuning grid of operating models 1, 2, 4, 7, and 11.

AM	Mediterranean Spawners					Gulf of Mexico Spawners				
	$B_{0,MED}$	$B_{MSY,MED}$	$F_{MSY,MED}$	$MSY_{MED}$	$M_{MED}$	$B_{0,GOM}$	$B_{MSY,GOM}$	$F_{MSY,GOM}$	$MSY_{GOM}$	$M_{GOM}$
1	739.66	119.87	0.25	29.99	0.10	167.77	35.88	0.18	6.40	0.10
2	1469.22	404.73	0.10	39.21	0.11	223.48	68.75	0.08	5.29	0.10
4	805.82	130.62	0.25	32.38	0.10	121.13	37.31	0.08	2.92	0.11
7	743.87	120.56	0.25	30.03	0.10	254.15	54.38	0.18	9.77	0.10
11	2143.18	589.91	0.10	56.66	0.10	470.27	144.77	0.08	11.22	0.10

## 6 Figures

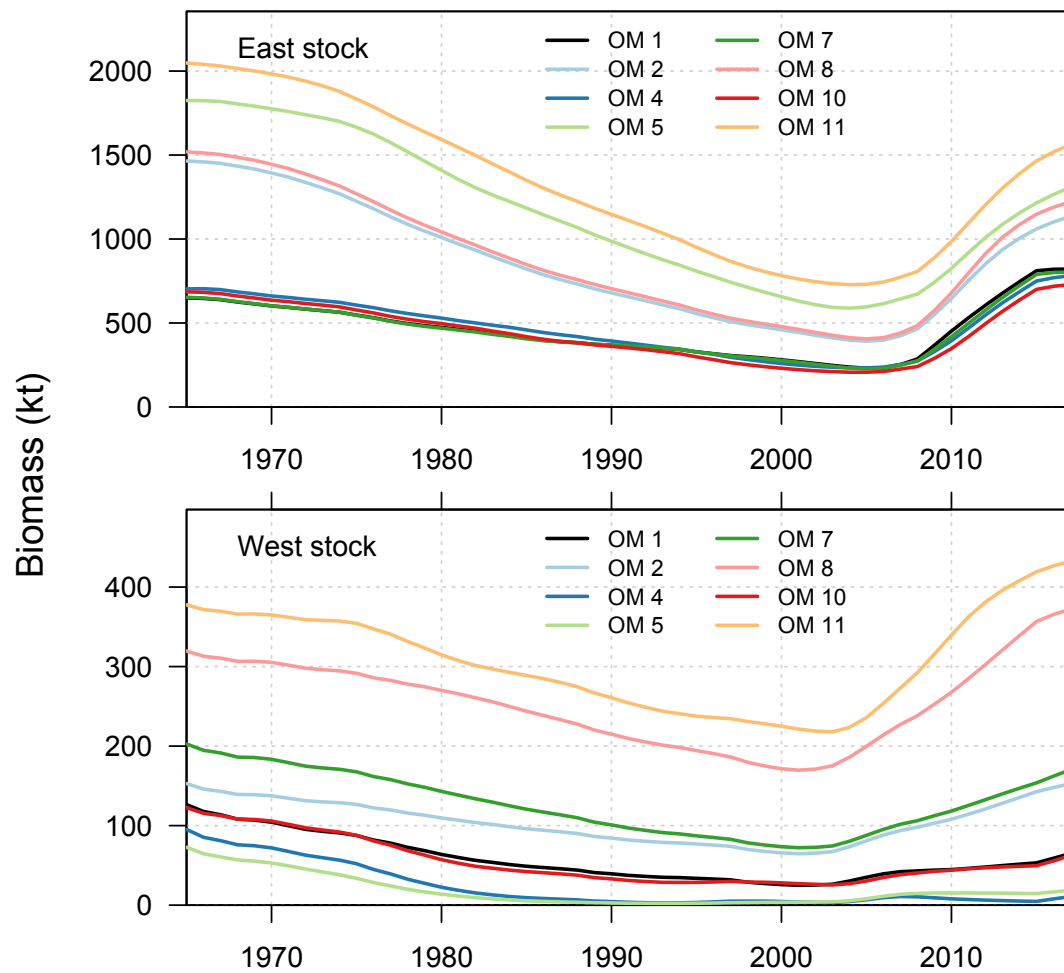


Figure 1: Operating model spawning stock biomasses for the full reference grid for both the Mediterranean stock (East) and Gulf of Mexico stock (West). Each colour corresponds to a different OM from the reference grid.

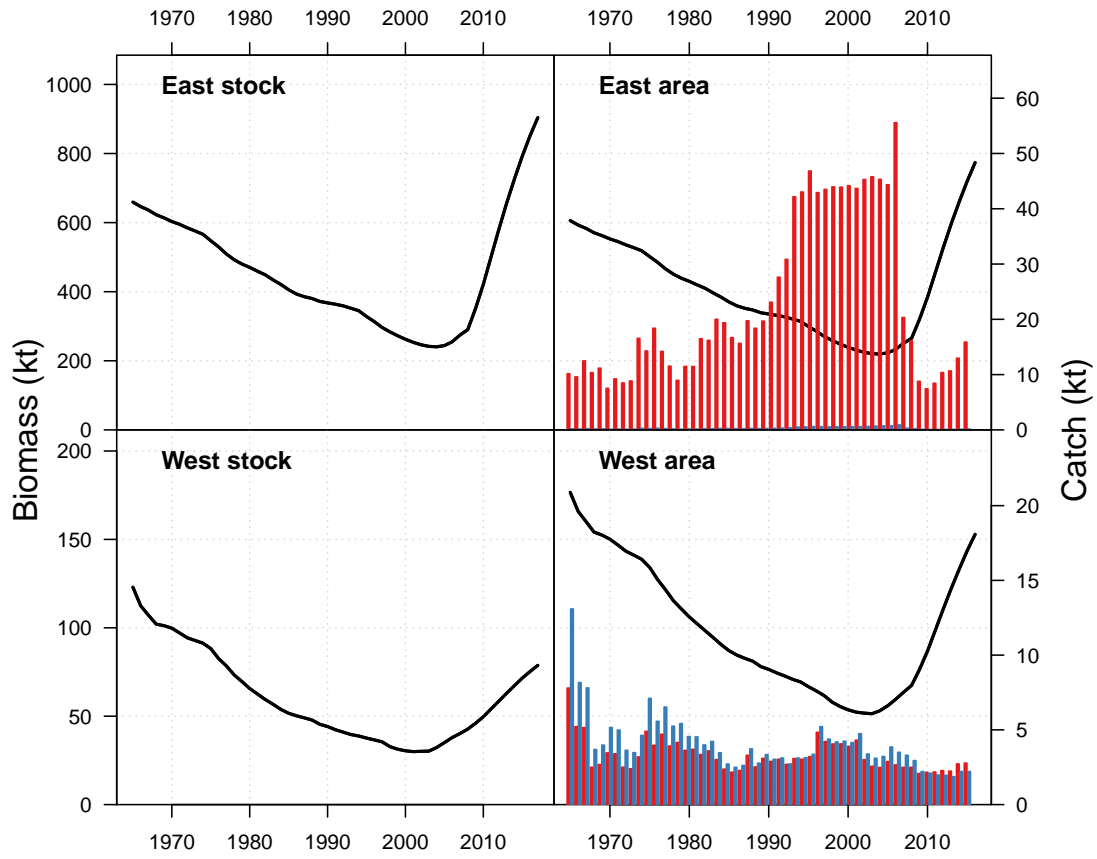


Figure 2: Spawning stock biomass estimates by stock (left hand column) and area (right hand column) from the delay difference stock assessment model fit to OM 1. Total area catch is shown split into East stock (red bars) and West stock (blue bars).

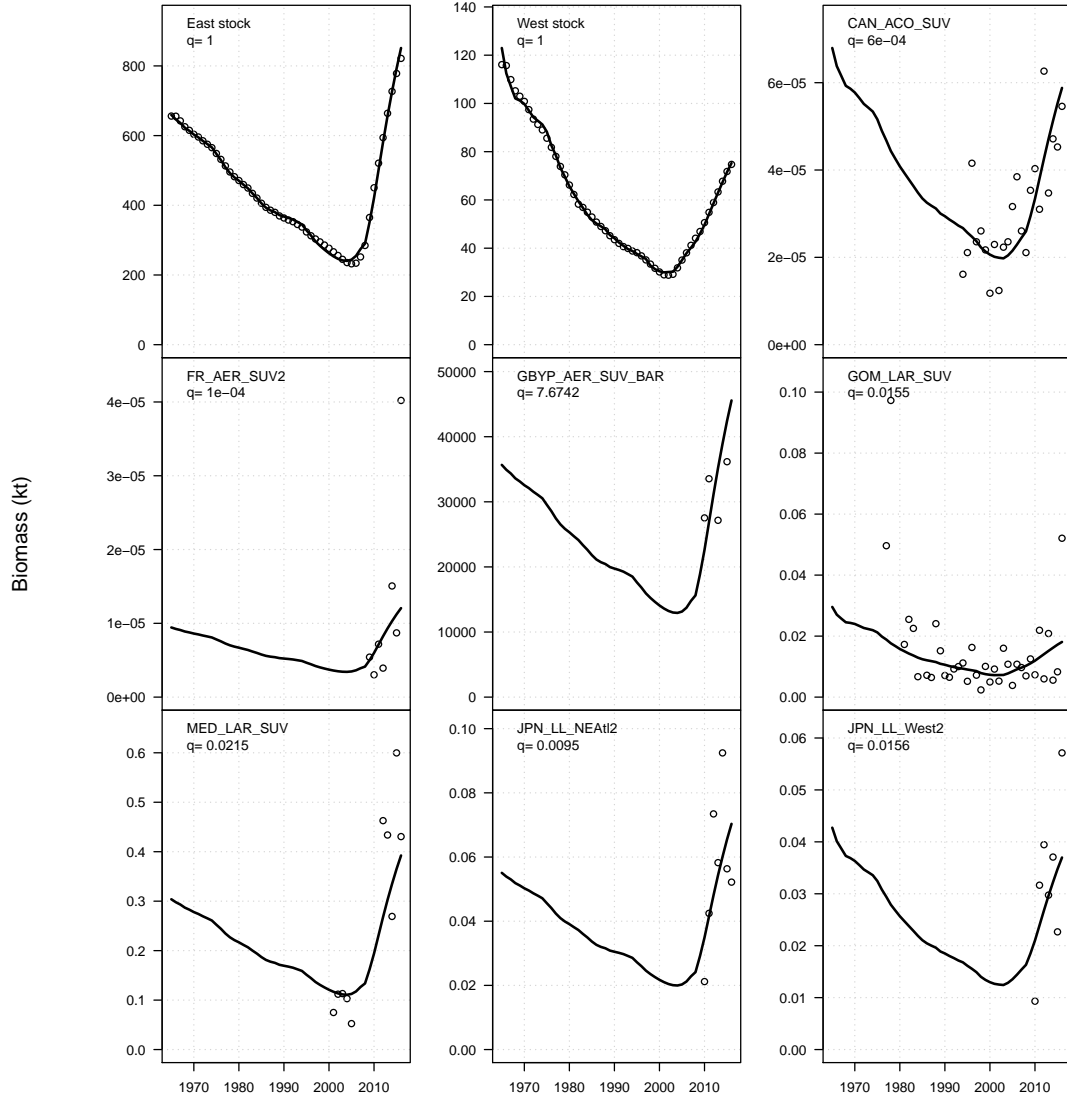


Figure 3: Fits of the delay difference stock assessment model to stock and area management indices, with the associated catchability estimates. Data are shown as circles, while the lines indicate the model biomass scaled by catchability. East Stock and West Stock indices are the spawning stock biomass estimates from operating model 1.

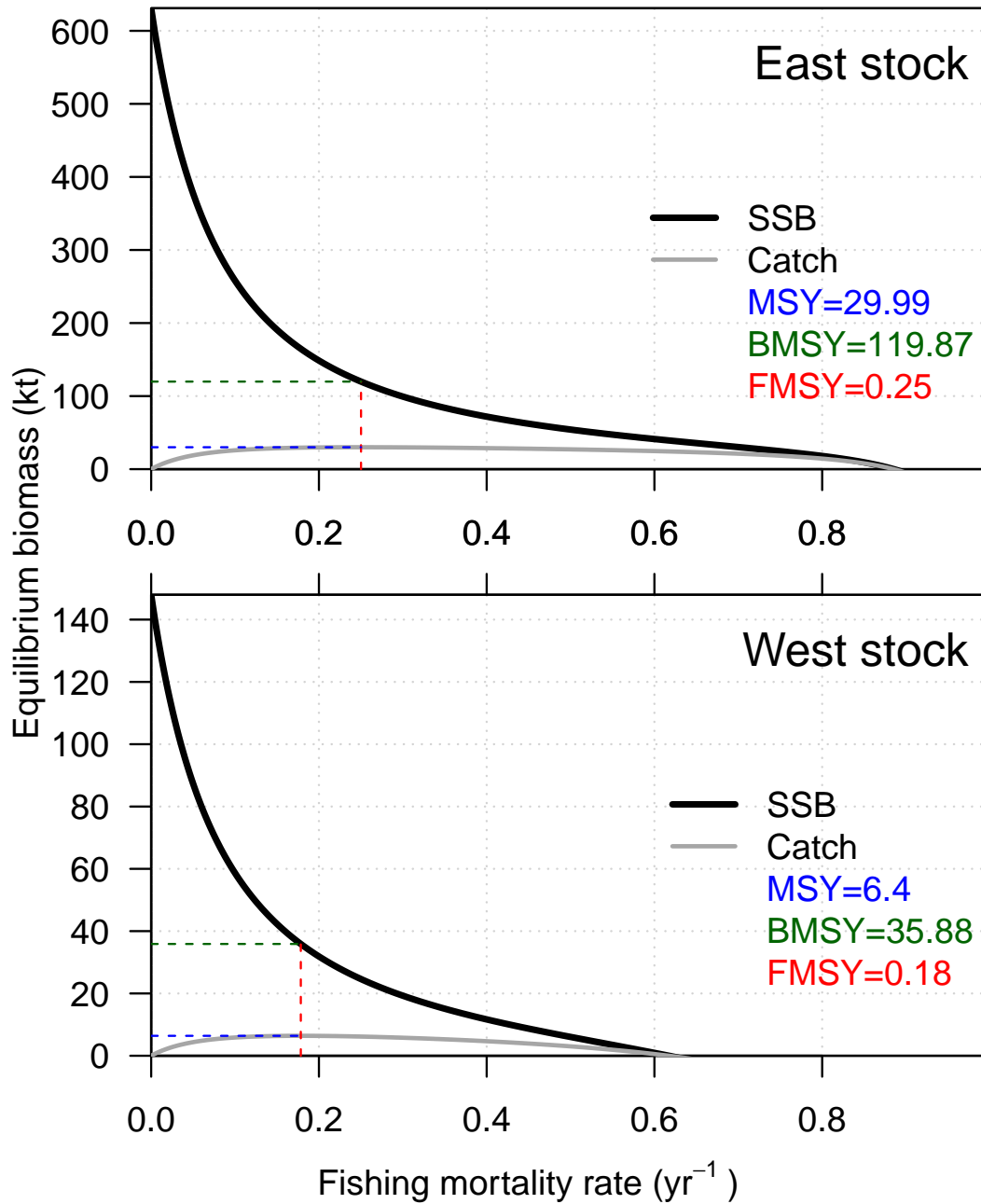


Figure 4: Equilibrium biomass (black) and yield (grey) curves as a function of fishing mortality estimated by the delay difference model fits to the management indices and operating model 1 spawning stock biomass.