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a) for class $y=0$ $E[x_1] = (1+1+2+3+3)/5 = 2$ $E[x_2] = (1+1+2+2+3)/5 = 1.8$ $\text{cov}(x_1, x_2) = E[x_1 x_2] - E[x_1]E[x_2] = (3+6+6+1+2)/5 - 3.6 = 0$ for class $y=1$ $E[x_1] = (1+2+4+5+5)/5 = 3.4$ $E[x_2] = (4+5+6+6+7)/5 = 5.6$ $\text{cov}(x_1, x_2) = E[x_1 x_2] - E[x_1]E[x_2] = (30+24+20+10+7)/5 - 19.04 = 18.2 - 19.04 = -0.84$ b) $\bar{x}^T = (3.5, 2)$ $\Sigma = \text{covariance matrix for } y=0$ $\text{var}(x_1) = E[x_1^2] - E[x_1]^2 = (1 + 1 + 4 + 9 + 9)/5 - 4 = 0.8$ $\text{var}(x_2) = (1 + 1 + 4 + 4 + 9)/5 - 3.6 = 0.2$ $\text{for } y = 1$ $\text{var}(x_1) = (1 + 4 + 16 + 25 + 25)/5 - 11.56 = 14.2 - 11.56 = 2.64$ $\text{var}(x_2) = (16 + 25 + 36 + 36 + 49)/5 - 31.36 = 32.4 - 31.36 = 1.04$ $\Sigma_{\text{for } y = 0} = \begin{pmatrix} 0.8 & 0 \\ 0 & 0.2 \end{pmatrix}$ $\Sigma_{\text{for } y = 1} = \begin{pmatrix} 2.64 & -0.84 \\ -0.84 & 1.04 \end{pmatrix}$

μ = vector of expected values

c) LDA assumes that the classes have different means and shared variance, while with QDA each class can have a different variance

d) ???

e) LDA is a much less flexible classifier than QDA. therefore LDA usually makes better predictions when there are relatively few training observations and reducing variance is crucial. QDA can be used with a bigger sample size, when the variance of the classifier is not a huge concern.

number of features??