$\label{eq:Quiz #9, 3/30} \text{Math 157 (Calculus II), Spring 2023}$

Problem 1 is worth 5 points (2.5 pts each part), and Problem 2 is worth 5 points (1 pt each part), for a total of 10 points. Remember to *show your work* on all problems!

1. For each of the following sequence limits, compute the limit or explain why it does not exist.

(a)
$$\lim_{n \to \infty} \frac{3n^2 + 4}{2n^2 + 5n + 1}$$

(b)
$$\lim_{n \to \infty} \sin\left(\frac{\pi}{2} + \frac{\pi}{n}\right)$$

2. For each of the following sequences $\{a_n\}_{n=1}^{\infty}$, state whether it is: (i) increasing, decreasing, or neither; (ii) bounded, or unbounded; (iii) convergent or divergent.

(a)
$$a_n = n^2$$

(b)
$$a_n = (-1)^n \cdot n^2$$

(c)
$$a_n = \frac{1}{n}$$

(d)
$$a_n = \frac{(-1)^n}{n}$$

(e)
$$a_n = (-1)^n$$