Quiz #6, Due: 10/12 Math 181 (Discrete Structures), Fall 2022

Problem 1 is worth 5 points and Problem 2 is worth 5 points, for a total of 10 points. Remember to show your work and explain your answers on all problems!

- 1. Prove the following: "For any two positive real numbers x and y, if $xy \ge 2$ then $x \ge \sqrt{2}$ or $y \ge \sqrt{2}$." **Hint**: Use a proof by contradiction or a proof by contrapositive.
- 2. Prove the following: "There exist irrational numbers a and b such that a^b is rational." Do this by employing the following **proof strategy**. Show that either
 - $a = \sqrt{2}$ and $b = \sqrt{2}$ satisfy the statement;
 - or, $a = \sqrt{2}^{\sqrt{2}}$ and $b = \sqrt{2}$ do.

Your proof does not have to show which of these two possibilities hold. You may use the fact we proved in class that $\sqrt{2}$ is irrational. You may also use the law of exponents $(x^y)^z = x^{yz}$.