

Quiz #10, Due: 11/8
Math 181 (Discrete Structures), Fall 2022

Problem 1 is worth 4 points (2 pts each part), and Problem 2 is worth 6 points (1.5 pts each part), for a total of 10 points. Remember to *show your work* and *explain your answers* on all problems!

1. Let $X = \{1, 2, 3\}$ and define a relation R on $X \times X = \{(a, b) : a, b \in X\}$ where $(a, b) R (c, d)$ if and only if $a + b = c + d$. (For example, we have $(2, 2) R (1, 3)$ since $2 + 2 = 4 = 1 + 3$.)
 - (a) Explain why R is an equivalence relation.
 - (b) List one element of each equivalence class of R .
2. Let $X = \{a, b, c\}$. Let $S \subseteq X^*$ be the set of strings on X of length 4. (For example, $abbc \in S$.)
 - (a) What is $\#S$ (the number of elements in S)?
 - (b) Let $S_1 \subseteq S$ be the subset of strings in S that begin with “a.” What is $\#S_1$?
 - (c) Let $S_2 \subseteq S$ be the subset of strings in S that end with “bb.” What is $\#S_2$?
 - (d) Let $S_3 \subseteq S$ be the subset of strings in S that either begin with “a” or end with “bb” (or both). What is $\#S_3$? [**Hint:** use the Principle of Inclusion and Exclusion!]