

Quiz #10, 4/6  
Math 157 (Calculus II), Spring 2023

Problem 1 is worth 5 points (2.5 pts each part), and Problem 2 is worth 5 points (2.5 pts each part), for a total of 10 points. Remember to *show your work* on all problems!

1. Consider the series  $s = \sum_{n=1}^{\infty} \frac{1}{n^3}$ . Let  $s_n = \sum_{k=1}^n \frac{1}{k^3}$  be the  $n$ th partial sum for this series.
  - (a) Compute  $s_2$ , the second partial sum, as an estimate for the true value  $s$  of the series.
  - (b) Let  $R_2 = s - s_2$  denote the error of your estimate. Compute bounds on this error using integrals. **Hint:** recall that  $\int_{n+1}^{\infty} f(x) dx \leq R_n \leq \int_n^{\infty} f(x) dx$  for the appropriate  $f(x)$ .

2. For the following series, decide whether they converge or diverge. Do this by using a comparison (either direct or limit) to a series whose convergence/divergence we showed in class.

(a)  $\sum_{n=1}^{\infty} \frac{2}{2n-1}$

(b)  $\sum_{n=1}^{\infty} \frac{1}{3^n - 2}$