## Quiz #10, 4/11 Math 157 (Calculus II), Spring 2024

Problem 1 is worth 6 points, and Problem 2 is worth 4 points, for a total of 10 points. Remember to  $show\ your\ work$  on all problems!

- 1. Consider the series  $s = \sum_{n=1}^{\infty} \frac{1}{n^3}$ . Let  $s_n = \sum_{k=1}^n \frac{1}{k^3}$  be the *n*th partial sum for this series.
  - (a) Compute  $s_2$ , the second partial sum, as an estimate for the true value s of the series.
  - (b) Let  $R_2 = s s_2$  denote the error of your estimate. Compute upper and lower bounds on this error. **Hint**: recall that  $\int_{n+1}^{\infty} f(x) dx \le R_n \le \int_n^{\infty} f(x) dx$  for the appropriate f(x).

2. For the following series, decide whether they converge or diverge. Explain your answers.

(a) 
$$\sum_{n=1}^{\infty} \frac{4n^2 - n + 4}{3n^2 + 3n - 1}$$

(Hint: look at the limit of the terms.)

(b) 
$$\sum_{n=1}^{\infty} \frac{1}{3^n + 1}$$

(Hint: compare to a series you know.)

$$(c) \sum_{n=1}^{\infty} \frac{2}{2n-1}$$

(Hint: compare to a series you know.)

(d) 
$$\sum_{n=1}^{\infty} \frac{2}{2n^2 - 1}$$

(Hint: compare to a series you know.)