## Midterm #2, 11/15Math 156 (Calculus I), Fall 2022

Each problem is worth 10 points, for a total of 50 points. You have 50 minutes to do the exam. Remember to *show your work* on all problems!

1. Compute the derivative f'(x) for the following functions f(x):

(a) 
$$f(x) = \sqrt{x^3}$$

(b) 
$$f(x) = xe^x$$

(c) 
$$f(x) = \cos(2x)$$

(d) 
$$f(x) = \ln(x^2)$$

- 2. Consider the curve in the x, y-plane defined by the implicit equation  $x^2 + xy + y^2 = 1$ . Compute the slope of the tangent to this curve at the point (x, y) = (1, 0).
- 3. Let  $f: \mathbb{R} \to \mathbb{R}$  be given by  $f(x) = xe^x$ . Find all the critical points of f. For each critical point: is it a local minimum, a local maximum, or neither?
- 4. As in the previous problem, let  $f(x) = xe^x$ . Compute the second derivative f''(x). Then find the intervals where the graph of f(x) is concave up, and where it is concave down.
- 5. Use L'Hôpital's rule to compute the following limits:

(a) 
$$\lim_{x \to 0} \frac{\sin(x)}{e^x - 1}$$

(b) 
$$\lim_{x \to 0^+} \frac{\ln(x)}{x^{-1}}$$