

# **TUGAS AKHIR**

## **MENGIKUTI MAYORITAS: SEBUAH ALGORITMA BARU UNTUK MENGHITUNG MEDIAN TRAJECTORY**



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2002**



# FINAL PROJECT

## FOLLOWING THE MAJORITY: A NEW ALGORITHM FOR COMPUTING A MEDIAN TRAJECTORY



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2002



# LEMBAR PENGESAHAN

## MENGIKUTI MAYORITAS: SEBUAH ALGORITMA BARU UNTUK MENGHITUNG MEDIAN TRAJECTORY

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### **MENGIKUTI MAYORITAS: SEBUAH ALGORITMA BARU UNTUK MENGHITUNG MEDIAN TRAJECTORY**

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## ABSTRAK

Kami mengembangkan dua algoritma baru untuk menghitung lintasan dari median set lintasan. Algoritma pertama adalah  $O(1.2108^m + m^5 n^5)$  terburuk waktu algoritma, dengan menggunakan konsep Jarak Fréchet. Algoritma kedua menggunakan metode penyangga. Dalam situasi praktis, algoritma ini dapat menghitung median lintasan di  $O((mn)^2 \log mn)$  waktu. Untuk kedua algoritma,  $m$  adalah jumlah lintasan dalam mengatur dan lintasan masing-masing memiliki segmen  $n$ . Kami membandingkan algoritma buffer dengan dua algoritma lain, salah satu dari mereka menggunakan konsep homotopy. Hasil kami menunjukkan bahwa algoritma penyangga melakukan agak lebih baik.

**Kata-kata kunci:** Lintasan, Homotopy, Fréchet, Lintasan Median, Penyangga



## ABSTRACT

We develop two new algorithms to compute a median trajectory from a set of trajectories. The first algorithm is an  $O(1.2108^m + m^5 n^5)$  worst-case time algorithm, using the concept of Fréchet Distance. The second algorithm uses a buffer method. In practical situations, this algorithm can compute the median trajectory in  $O((mn)^2 \log mn)$  time. For both algorithms,  $m$  is the number of trajectories in the set and each trajectory has  $n$  segments. We compare the buffer algorithm with two other algorithms, one of them using the homotopy concept. Our results suggest that the buffer algorithm performs somewhat better.

**Keywords:** Trajectory, Homotopy, Fréchet, Median Trajectory, Buffer



*Dipersembahkan untuk diri sendiri*



## KATA PENGANTAR

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Bandung, Juli 2002

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## BAB 1

### INTRODUCTION

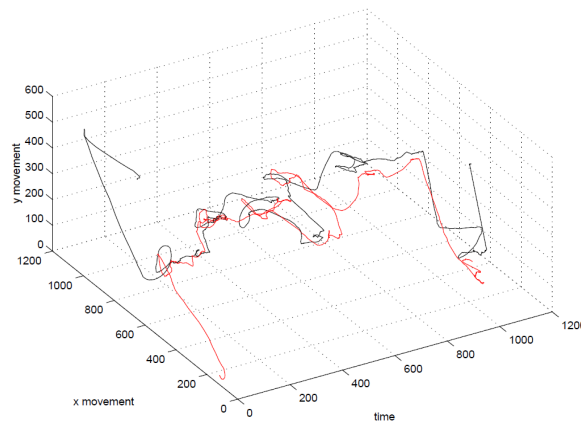
#### 1.1 Motivation

A trajectory is the motion path of a moving object. Various moving objects such as animals (probably in a wildlife area), hurricanes, or customers in a shopping area have trajectories that can provide valuable information. For example, trajectory data can be used to predict the movement of the same type of object in similar situation in the future.

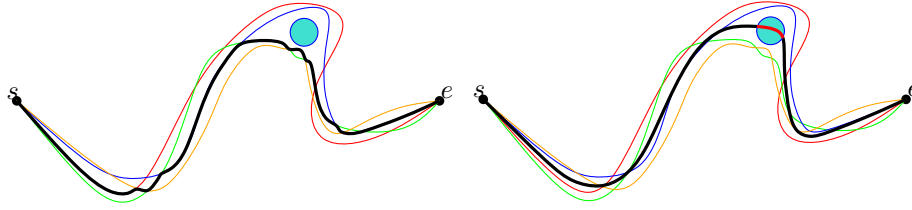
During a tracking procedure, the location of these moving objects can be obtained using various location detection devices (e.g: RFID, GPS devices and mobile phones). Later, this information will be sent to a database using any communication network (usually a wireless network). Because typical trajectory data is obtained during a specific interval, then trajectory data also has a temporal component, besides its spatial component.

The trajectory of a moving object is typically modeled as a sequence of consecutive locations in a multi-dimensional (generally two or three dimensional) Euclidean space [1]. Figure 1.1 shows an example of two trajectories from two objects which are moving in a 2D plane. With their temporal component, we can see that these trajectories are represented as polylines in a 3D space.

Nowadays, with the rapid development of technologies in mobile computing and wireless communication, many devices with location acquisition capabilities make it possible to obtain huge volumes of trajectory data from various moving objects. Furthermore, analysis of trajectory data is an important task for many applications that contain processing and managing moving objects,



Gambar 1.1: Example of 2D trajectories with time component, from [1]



Gambar 1.2: Example of the median (left) and the mean (right) trajectory [2]

such as animal movements [3, 4, 5, 6], traffic and transport analysis [7], defense and surveillance areas [8], oceanographic observations<sup>1</sup>, weather and natural phenomena [9], people behavior [10] and sports [11, 12].

Previous work on trajectory data analysis shows that there are several ways to analyze sets of trajectories. For example, similarity between trajectories can be determined [13, 14, 15]. Trajectories can also be clustered into groups with similar characteristics [16, 17, 18, 19]. Other examples are common data mining tasks such as classification [20, 21] and outlier detection [22]. Furthermore, interesting movement patterns such as flocking can also be computed from a set of trajectories [23, 24, 25, 26].

Even though analysis and research on trajectories has expanded in recent years, several basic concepts still need to be studied further. Some of them are the median and the mean trajectory for a collection/set of trajectories. The median and the mean trajectory share some common properties: they should be similar to other trajectories in the set and all parts of them should be located roughly in the middle of the set. However, there are several important differences between them: Firstly, the median trajectory must use only parts of trajectories in the set. It uses only parts of one trajectory or combines parts from many different trajectories. This property might be a disadvantage for the median because some parts of it can be located not in the middle of the set, but in several situations this might be useful.

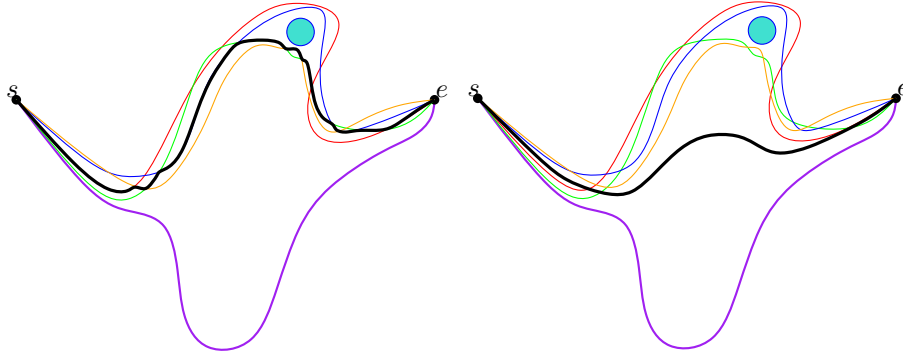
Figure 1.2 shows a set of four trajectories which avoid the light-blue obstacle. The possible mean trajectory (the black trajectory in the right-hand side of the figure) will pass through the obstacle because the mean must lie in the middle of all trajectories in the set. In this case, it is clear that the mean trajectory is not suitable for a path of a moving object.

The median trajectory (black trajectory in the left-hand side of the figure) gives a more suitable path because it always uses parts of other trajectories. In parts near the obstacle, the median is not really in the middle of other trajectories.

Secondly, the median trajectory is more robust against outliers than the mean trajectory. Figure 1.3 shows this situation: we add one trajectory (with purple color) which can be categorized as an outlier compared to other trajectories. While the median trajectory only needs to be modified a little bit, the mean trajectory has to be changed a lot (comparing to the mean trajectory in Figure 1.2), to keep it in the middle of other trajectories.

In this thesis, we will not cover the mean trajectory and only discuss the median trajectory and algorithms to compute it. We also ignore the temporal component of the trajectory because it is not clear yet how to take it into account when computing the median trajectory. However, some

<sup>1</sup>W.S. Kessler, "Argo work in the coral sea." [http://faculty.washington.edu/kessler/noumea/gliders/argo\\_coral\\_sea.html](http://faculty.washington.edu/kessler/noumea/gliders/argo_coral_sea.html), March 2010.



Gambar 1.3: Robustness of the median trajectory

research on motion and kinetic data structures contains a temporal component and are related to the median/mean trajectory [27, 28].

For other types of data, a median has a clear definition. The median from a population (or a sample) of integer numbers is the number that separates the population into two halves, where at most half of the population have a smaller value and the other half of the population have a larger value than the median.

For geometric data types, the concept of median also exist. A *center point* of a set  $P$  of  $n$  points in the plane is a point such that any closed half-plane whose bounding line contains the center point, contains at least  $n/3$  points of  $P$  [29]. If we force the center point to be one of the points from  $P$ , then we obtain a 2-dimensional version of the median, although the “quality” of this median can be bad.

The median trajectory does not have any formal definition yet. Based on several properties that we mention earlier, such as its similarity with other trajectories and lying approximately in the middle of the set, we can determine a possible median, which can useful in several ways:

### 1.1.1 Determine the most typical trajectory

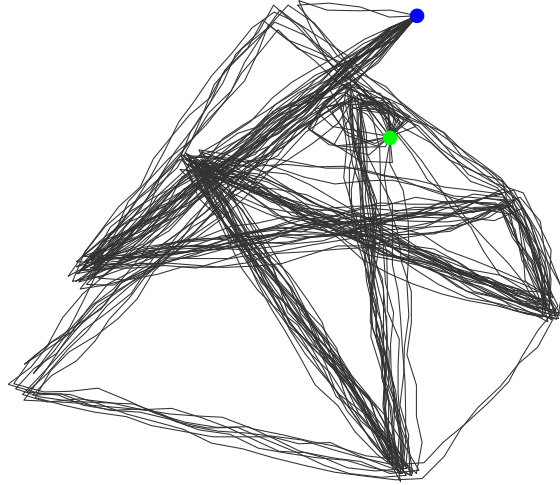
The property of the median trajectory makes it suitable to analyze the movement behavior or movement pattern from a group of same objects because the median somehow represents the whole trajectories in the set/collection. The median trajectory properties, such as the length, the direction or the average speed (if we include the temporal component), could give valuable information.

Example applications include the detection of outliers, which can be done by analyzing the length and the similarity of the shape of the median with other trajectories. Analyzing the average speed together with the shape of the median trajectory might be useful to understand the behavior and the movement pattern of people walking around in an area which has several interesting places to be visited (e.g., a zoo or an amusement park).

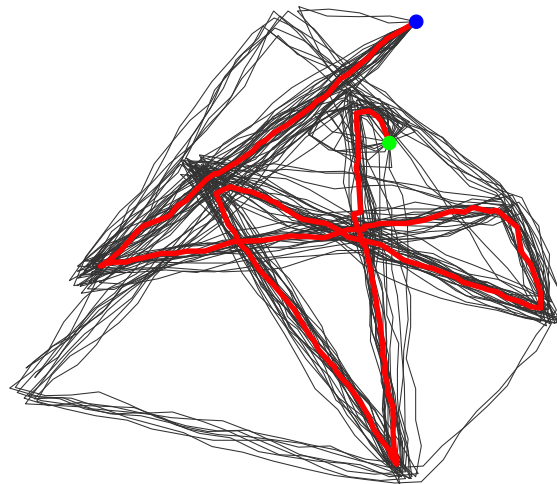
### 1.1.2 Better visualization for a set of trajectories

Visualization of the median trajectory, together with its set of trajectories, might give the viewer a better interpretation and information about the set of trajectories.

We give an example in Figure 1.4, where a set has 30 trajectories, which is paths of 30 objects moving from the blue point to the green point. From this figure, we can hardly tell anything



Gambar 1.4: The set of 30 trajectories, starting at the blue point & ending at the green point



Gambar 1.5: A set of 30 trajectories with its possible median trajectory



about the general behavior or the direction of these trajectories. However, we know that several trajectories are different than others and probably can predict what the majority does, but it is still difficult to visualize what the majority of these trajectories does.

In the following figure (Figure 1.5), we present a possible median trajectory as the red and thick trajectory. From this visualization, it is clear what the majority of trajectories does. Moreover, we can identify what parts of some trajectories are completely different from others.

The visualization of the median trajectory could be useful in some real-life applications: The median trajectory from trajectories of visitors in a national park can be used to see the most common path taken by visitors, which is probably the path that is preferred by future visitors. This information might be useful if we want to create a map that can help those visitors by providing valuable information about a path and direction on that national park in the map, so that he/she can decide which path that he/she will take.

### 1.1.3 $k$ -medoid clustering

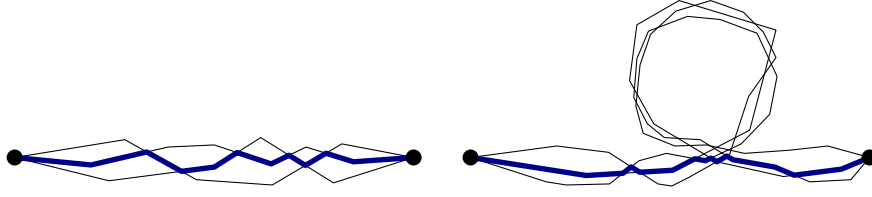
Another application that could use the median trajectory is the  $k$ -medoid algorithm, which is used in cluster analysis. The  $k$ -medoid clustering algorithm is related to the  $k$ -means algorithm, a method to partition/group a set of objects into  $k$  different clusters containing similar objects.

In general, each cluster in both algorithms has one object act as a *central object* and other members of the cluster should be similar or having a small distance to this object. The similarity or the distance between objects can be measured using different distance functions (e.g. Euclidean distance, Minkowski distance, etc), depending on the type of objects and the purpose of the clustering.

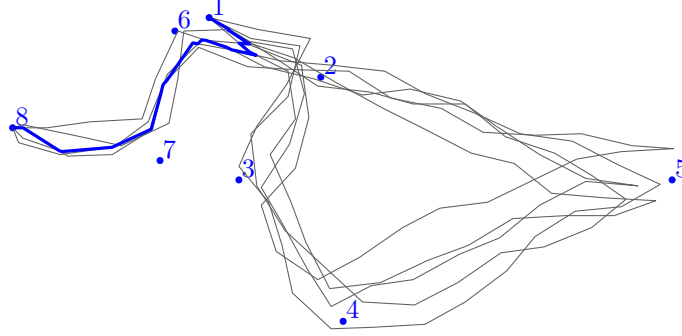
The main difference between the two algorithms is on the selection of the central object for each cluster. While the  $k$ -means simply uses the mean of objects, the  $k$ -medoid must use the medoid (an object which has the smallest average of dissimilarity/distance to all other objects in the set, but it must be a member of the set). This implies that  $k$ -means could create a new object to be the central object whereas the  $k$ -medoid must use one of the objects from the set. Thus, the  $k$ -medoid algorithm is more suitable for spatial clustering purposes and less sensitive against noise and outliers.

Partitioning Around Medoids (PAM) [30] is a basic  $k$ -medoid clustering algorithm. It works as follow:

1. Define a value  $k$  and choose  $k$  objects as a set of medoids.
2. Assign every object to its closest/similar medoid and after that, compute the cost for the whole configuration.
3. Find another configuration by selecting a pair of medoid and non-medoid objects which have the smallest distance cost and swapping them temporarily. Then, we assign all other objects to this temporary set of medoids and obtain a new configuration.
4. If the new configuration has smaller cost than the last configuration, then we change the set of medoids and return to step 3
5. Otherwise, stop and we find the set of medoids with their non-overlapping set of clusters.



Gambar 1.6: Illustration of the simple idea using switching



Gambar 1.7: The median trajectory makes a shortcut [2]

In case we want to cluster a set of trajectories, we can use the median trajectory as a medoid in this algorithm. However, some changes probably should be made. For example, finding another configuration is not done by simply swapping the median with other trajectory, instead we can choose to swap part of them (with the requirement that both trajectories intersect one another).

## 1.2 Basic Idea of the Research

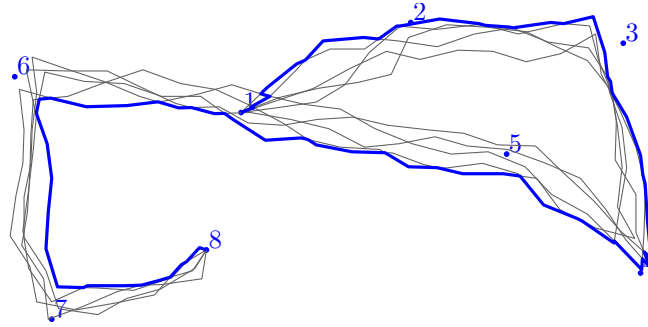
Consider a set  $T$  of  $m$  trajectories. We want to compute the median trajectory of  $T$ . In this set, all trajectories have the same start and end points. The median trajectory of  $T$  must be built using parts of trajectories in  $T$  and somehow must follow what other trajectories in  $T$  do, while staying in the “middle” of other trajectories.

### 1.2.1 The Simple Switching Method

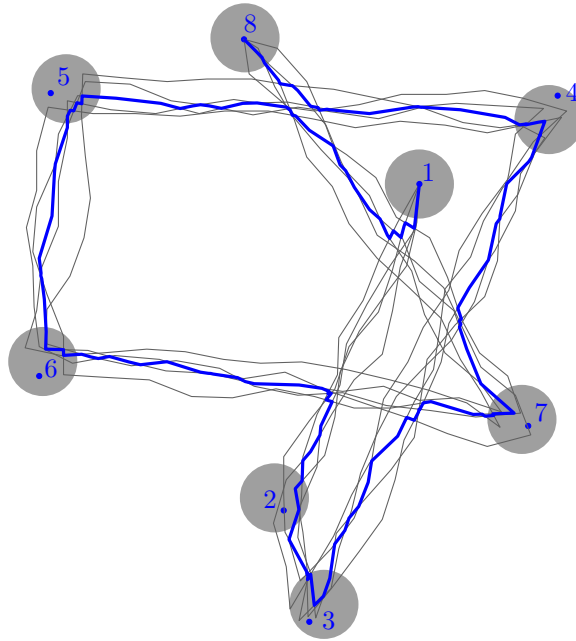
A simple idea to obtain a median trajectory from  $T$  is to start from the “middle” trajectory, which is the  $(m + 1)/2$ -level of arrangement formed by all trajectories in  $T$  (we assume  $m$  is odd). At every intersection point, the median trajectory will switch to another trajectory and keep  $(m + 1)/2$  trajectories above and below the median [31].

Figure 1.6 shows the result (the median trajectory is the thick-blue trajectory) of this approach for two different types of set of trajectories, one of them contains trajectories with self intersection. From the right-hand side of the figure in Figure 1.6, we can see that this method cannot produce suitable median trajectory because the median does not follow the loop created by the three trajectories.

In general, this method will not give a suitable median if a set of trajectories contains self-intersecting trajectories. More examples from [2] show several “incorrect” median trajectories obtained by using this simple switching method. The blue median trajectory in Figure 1.7 makes a



Gambar 1.8: The median trajectory does not stay in the middle [2]



Gambar 1.9: The median trajectory does not follow the correct sequence of regions [2]

shortcut path to the end point.

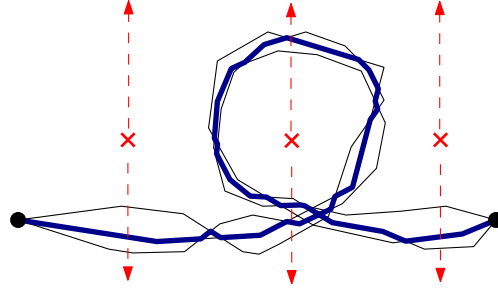
The median trajectory in Figure 1.8 does not stay in the "middle" of other trajectories. Finally, in Figure 1.9, the median trajectory does not follow the sequence of regions as the other trajectories. The correct sequence of regions is 1 – 2 – 3 – 4 – 5 – 6 – 7 – 8.

### 1.2.2 The Algorithm Using the Concept of Homotopy

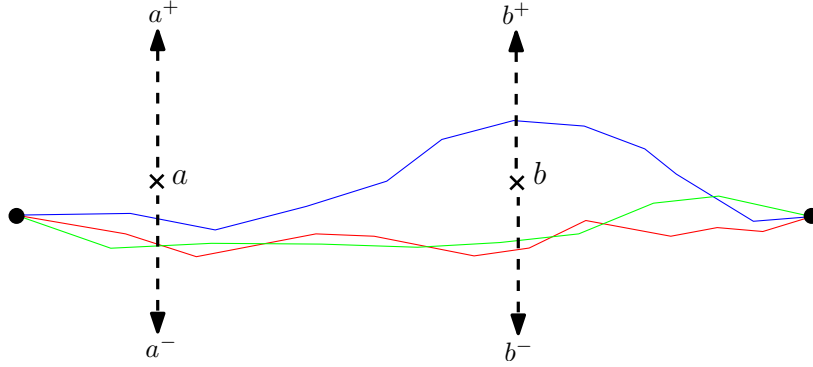
Another algorithm to compute the median trajectory uses the concept of homotopy (along with the modified simple switching method) [31]. This algorithm works by placing cross in a relatively large face bounded by segments from a set of trajectories. Figure 1.10 shows an example where cross is placed in the relatively large bounded face and two crosses are placed in the outer face.

Based on the location of these crosses, each trajectory in  $T$  will be assigned a *signature*. Figure 1.11 shows three trajectories and two crosses  $a$  and  $b$ . From these two crosses, four half-lines are created:  $a^+$  and  $a^-$  are half-lines above and below  $a$ , while  $b^+$  and  $b^-$  are half-lines above and below  $b$ , respectively.

For all trajectories in  $T$ , we give them a signature based on how they intersect with the half-



Gambar 1.10: Illustration of the algorithm using homotopy concept



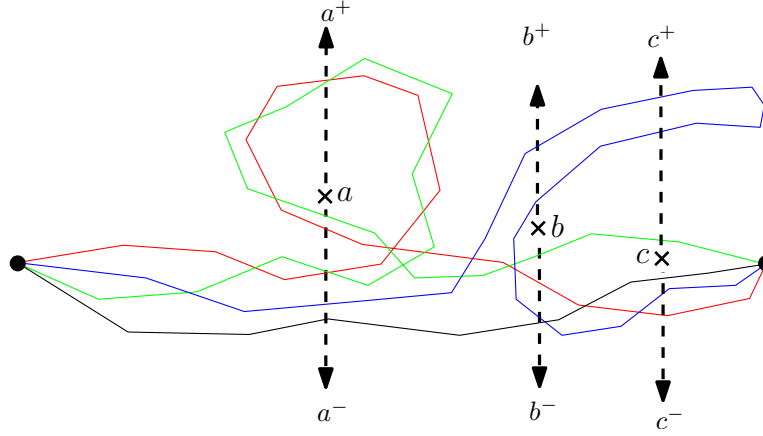
Gambar 1.11: Trajectories and crosses

line(s) from the crosses. Note that each trajectory might have a different signature, because it depends on the position of the trajectory with respect to all crosses in the plane. In Figure 1.11, the blue trajectory intersect with  $a^-$  and  $b^+$ , thus its signature will be  $a^-b^+$  (the order is following the direction of the trajectory). In the same way, the signature of the red trajectory will be the same as the green trajectory:  $a^-b^-$ .

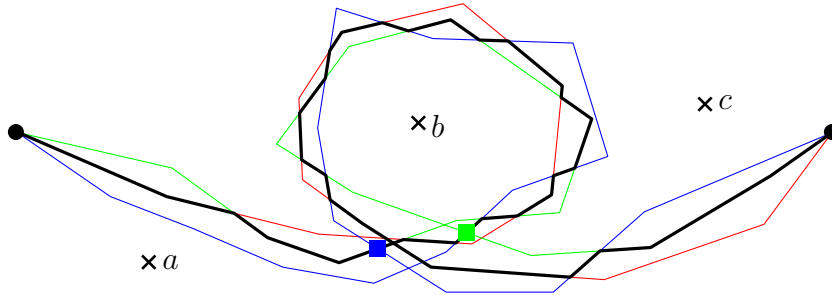
Two different trajectories are homotopic if one trajectory can be deformed continuously into the other one without passing through any crosses, while the start and end point are not moved. Naturally, two trajectories are homotopically equivalent if their signatures are exactly the same. However, two homotopic trajectories do not always have the same signatures. We shown an example in Figure 1.12 where the blue and the black trajectory are homotopic, but their signatures are different.

To determine whether two trajectories with different signature are homotopic or not, we perform a *reduce* operation. This *reduce* operation works by eliminating two exact same signs, if their position is next to each other in the signature. In Figure 1.12, the signature of the blue trajectory is  $a^-b^+c^+c^+b^+b^-c^-$ . Notice that it has two  $c^+$  that we can eliminate. This will change the signature of the blue trajectory into  $a^-b^+b^+b^-c^-$ . Once again, we can identify that two  $b^+$  are positioned directly to each other. Performing the reduce operation again, we will get the final signature of the blue trajectory:  $a^-b^-c^-$ . At this point, we cannot apply the reduce operation again to this signature, and we say that the signature has been *maximally reduced*. Finally, we conclude that if two trajectories have the same maximally reduced signature, then the two trajectories are homotopically equivalent.

The next step of the algorithm is to create a subset  $T'$  of  $T$ , and then find the median trajectory by using only parts of trajectories from  $T'$ . Creating  $T'$  is straightforward, we only need to compute



Gambar 1.12: The blue and black trajectory are homotopically equivalent [2]



Gambar 1.13: Modified switching method [2]

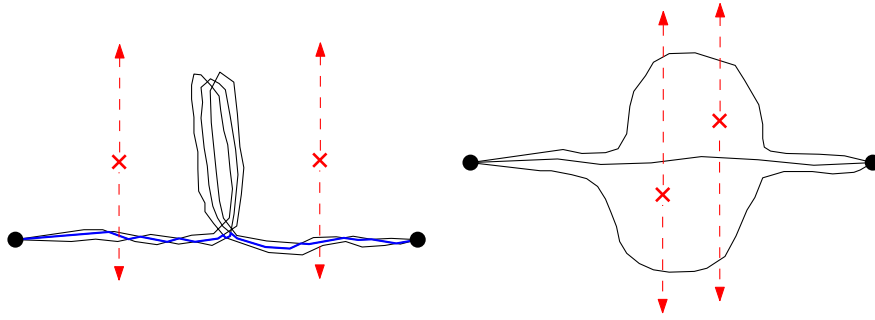
maximally reduced signature for all trajectories and choose a subset with the largest number of trajectories which have the same signature.

To create the median trajectory from  $T'$ , we use the modified version of the switching method. This method start at the first segment of the “middle” trajectory. We find such a segment by determine the outer face of the set of trajectories. The first segment of the “middle” trajectory is the segment where there are  $(n - 1)/2$  first segments from other trajectories (assume  $n$  is odd) between the segment and the outer face (on each side of the segment).

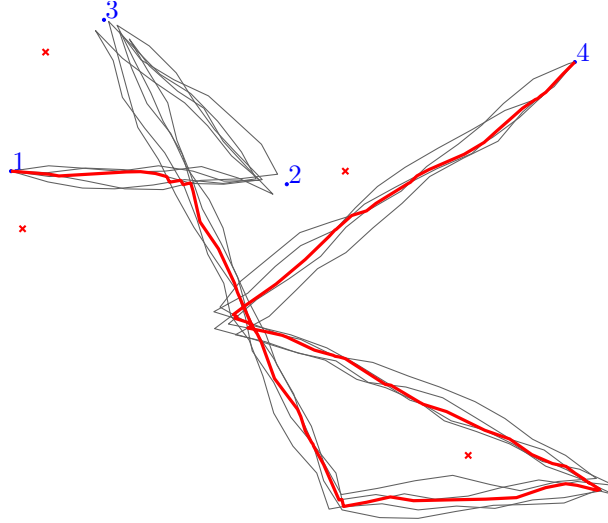
Then, at every intersection, the median will switch to another trajectory if the continuation along this trajectory (without ever switching again) gives the same signature with the signature of one trajectory from  $T'$ . Figure 1.13 shows an example of this algorithm. After starting with the red trajectory and switching to the green trajectory at the first intersection, the next intersection is with the blue trajectory (at the small blue square) and so far, the signature for the median is  $a^+$ . Although the blue trajectory is going forward, the signature after this intersection while following the blue trajectory (until the end point) is  $b^-c^-$ .

If the median switches at this intersection, the final signature will be  $a^+b^-c^-$ , which is not the signature of this set ( $a^+b^-b^+b^-c^-$ ). At this point, the median does not switch to another trajectory. Instead, it continues to move along the green trajectory. The same situation also occurs when the median (now following the blue trajectory) intersects with the green trajectory (at the small green square).

Although this algorithm can produce a more suitable median trajectory for the situation where the switching method fails, the quality of the homotopic median trajectory depends heavily on the



Gambar 1.14: Example cases where algorithm using homotopy will fail



Gambar 1.15: The median trajectory does not pass through part of trajectories in the upper left area

following factors:

- placement of the crosses
- the number of trajectories which have the same signature

Therefore, in several cases the algorithm with the homotopy concept cannot produce suitable median trajectories. We give two examples in Figure 1.14: in the left-hand side of figure, the final median trajectory (blue) does not follow other trajectories to the area with a narrow space. This problem arises because that narrow space is not large enough for a cross to be placed.

In the right-hand side of the figure, there are no two trajectories homotopically equivalent to each other. Nevertheless, by looking at their position, the median trajectory should be the one in the middle (between the two crosses). However, the algorithm with the homotopy concept does not guarantee that a suitable median trajectory will be found because there is no subset that contains the majority of trajectories in  $T$ . Figure 1.15 shows an example from [2], where the median trajectory does not completely follow what other trajectories do.

### 1.2.3 The Proposed Solutions

To solve the problems we mention in the previous section, we propose two algorithms to compute the median trajectory from a set of  $m$  trajectories (where each trajectory has  $n$  segments).

The first algorithm is an  $O(1.2108^m + m^5 n^5)$  worst-case time algorithm. This algorithm uses the Fréchet Distance [32] and works similar to the algorithm using the homotopy concept because both of them have to create the largest subset of similar trajectories and then compute the median trajectory by using parts of trajectories in that subset. By using the Fréchet Distance, we avoid the requirement to find proper places to put crosses, but still can produce suitable median trajectory in the situation where the homotopic algorithm fails (e.g. the example with a narrow space).

The second algorithm uses the combination of the buffer concept and Dijkstra's Shortest Path algorithm. Unlike all previous algorithms, this algorithm does not need to find the largest subset consisting similar trajectories. Using this algorithm, we can compute the median trajectory in  $O(h^2 \log h)$  time in the worst-case, where  $h$  is the number of all segments in  $T$  ( $h = O(mn)$ ).

We implemented the second algorithm in Java programming language and experiments have been done to determine the quality of the resulting median trajectory produced by this algorithm. To provide the test data (set of trajectories), we use a trajectories generator instead of using real-world data. This allow us to test much larger sets of trajectories

## 1.3 Outline of the Thesis

Chapter 2 describes the properties for a set of trajectories and also some properties the median trajectory should have.

The next two chapters explain in detail the two algorithms:

- Chapter 3 starts with a brief introduction of the Fréchet Distance and after that, we will explain how to use it to compute the median trajectory.
- Chapter 4 introduces the method to compute the median trajectory using the combination of the buffer concept and Dijkstra's shortest path algorithm.

We will give an explanation about our implementation, particularly on the implementation of the trajectories generator, in Chapter 5. In Chapter 6, we present the measures used to evaluate the quality of the median trajectory, the experiments set-up and the results from the experiments. This thesis will be concluded in Chapter 7 and 8, where we draw conclusions and discuss some issues and possible directions for further research.

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## BAB 2

### LANDASAN TEORI

Bab 2 ini akan dibahas mengenai dasar teori CAPTCHA, OCR, dan PHP yang akan digunakan pada penelitian kali ini.

#### 2.1 CAPTCHA

Istilah CAPTCHA (Completely Automated Public Turing test to tell Computer and Human Apart) diperkenalkan pertama kali pada tahun 2000, oleh Luis von Ahn, Manuel Blum, Nicholas Hopper dan John Langford dari Carnegie Mellon University. CAPTCHA merupakan sejenis tes untuk memastikan apakah respon yang masuk ke komputer berasal dari manusia atau bukan.

##### 2.1.1 Penerapan dari CAPTCHA

CAPTCHA memiliki beberapa penerapan untuk menjaga keamanan, diantaranya adalah :

- Mencegah komentar spam di blog. Banyak blogger mengenal program yang mengirimkan komentar bogus, terutama untuk meningkatkan peringkat mesin pencari untuk beberapa situs web. Ini disebut komentar spam. Dengan menggunakan CAPTCHA, manusia tidak perlu daftar untuk mengirimkan komentar, tetapi tetap dapat memasukkan komentar di blog.
- Melindungi proses pendaftaran pada situs web. Beberapa perusahaan (Yahoo, Google, Microsoft) menawarkan layanan email gratis. Sampai beberapa tahun lalu, layanan ini diserang oleh bots yang dapat melakukan pendaftaran hingga ribuan email per menitnya. Solusinya adalah dengan menggunakan CAPTCHA yang dapat memastikan bahwa hanya manusia yang dapat memperoleh akun gratis pada email. Sehingga pada umumnya, untuk mencegah serangan dari program otomatis, semua layanan gratis dapat dilindungi dengan CAPTCHA.
- Melindungi online pool. Pada tahun 1999, <http://www.slash.org> mengeluarkan sebuah online poll yang bertanya tentang sekolah terbaik di bidang computer science (sebuah pertanyaan yang sangat berbahaya). Pada mayoritas online poll, IP address dapat dicatat untuk mencegah pengguna yang sama melakukan voting lebih dari sekali. Tetapi, seorang pelajar dari Carnegie Mellon menemukan cara untuk melakukan voting berkali-kali dengan sebuah program, sehingga nilai CMU meningkat dengan cepat. Keesokan harinya, pelajar dari MIT menulis programnya sendiri untuk melakukan online poll sehingga poll tersebut menjadi kontes voting antara bots. Akhirnya MIT selesai dengan 21156 suara dan CMA dengan 21032 suara,

sementara sekolah lainnya tidak lebih dari 1000 suara. Apakah hasil dari online poll dapat dipercaya? Tidak, kecuali poll tersebut benar-benar dilakukan oleh manusia.

- Mencegah dictionary attack pada password. CAPTCHA dapat digunakan untuk mencegah dictionary attack pada password. Caranya sederhana, yaitu dengan menampilkan CAPTCHA setelah terjadi beberapa kesalahan login berturut-turut pada sistem.
- Mencegah bots pada mesin pencari. Kadang-kadang ada beberapa situs web yang ingin web-nya sulit ditemukan oleh orang lain. Untuk itu, ada sebuah html tag untuk mencegah search engine bots dalam membaca halaman web tersebut. Isi tag tersebut kurang lebih “Tolong, tidak ada bot “, tetapi yang tersebut tidak menjamin bahwa tidak akan ada bot yang akan membacanya. Walaupun begitu, bots mesin pencari, yang biasanya berada dimiliki perusahaan besar, akan menghargai situs web yang tidak ingin dicari tersebut. Tetapi, untuk benar-benar menjamin bahwa bot tidak akan memasuki situs web dibutuhkan CAPTCHA.
- Mencegah worm dan spam pada email. CAPTCHA juga menawarkan solusi terhadap masalah ini. Idennya seperti ini, “Saya akan menerima email, jika saya tahu bahwa di komputer pengirim benar-benar manusia “. Beberapa perusahaan besar telah mulai menggunakan ide ini.

### 2.1.2 Pedoman untuk CAPTCHA

CAPTCHA sangat direkomendasikan untuk menambah perlindungan dari penyalahgunaan suatu situs web. Terdapat banyak implementasi dari CAPTCHA namun hanya sedikit yang memiliki keunggulan. Terdapat beberapa pedoman yang sangat dianjurkan dalam mengimplementasikan CAPTCHA, berikut ini pedoman untuk setiap CAPTCHA :

- Aksesibilitas CAPTCHA yang telah diimplementasi harus dapat diakses. CAPTCHA tidak hanya sebatas pada membaca teks atau persepsi visual lainnya, tapi memungkinkan seseorang yang memiliki gangguan pada penglihatannya dapat mengakses CAPTCHA yang telah diimplementasi. Contohnya dengan menambah pilihan untuk CAPTCHA berbasis audio.
- Keamanan Gambar Gambar atau teks CAPTCHA harus didistorsi secara acak sebelum ditampilkan ke pengguna. Banyak pengimplementasian CAPTCHA yang memiliki gambar tidak aman karena menggunakan teks yang tidak terdistorsi, sehingga implementasi CAPTCHA tersebut dapat ditembus oleh program komputer. Contoh gambar CAPTCHA dengan teks yang tidak terdistorsi dapat dilihat dibawah ini.
- Keamanan Skrip Membuat CAPTCHA yang baik tidaklah mudah. Selain membuat gambar yang tidak bisa dibaca oleh program komputer, sistem CAPTCHA pun harus menjamin tidak ada cara yang mudah dalam menembusnya pada tingkat skrip. Contoh ketidakamanan skrip antara lain : Pertama, sistem untuk memberikan jawaban CAPTCHA dalam teks sederhana merupakan bagian dari form website. Kedua, sistem untuk menjawab CAPTCHA yang sama dapat digunakan berulang kali. Hal tersebut membuat CAPTCHA rentan terhadap serangan yang disebut replay attack.

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## 2.2 Teori Kombinatorial



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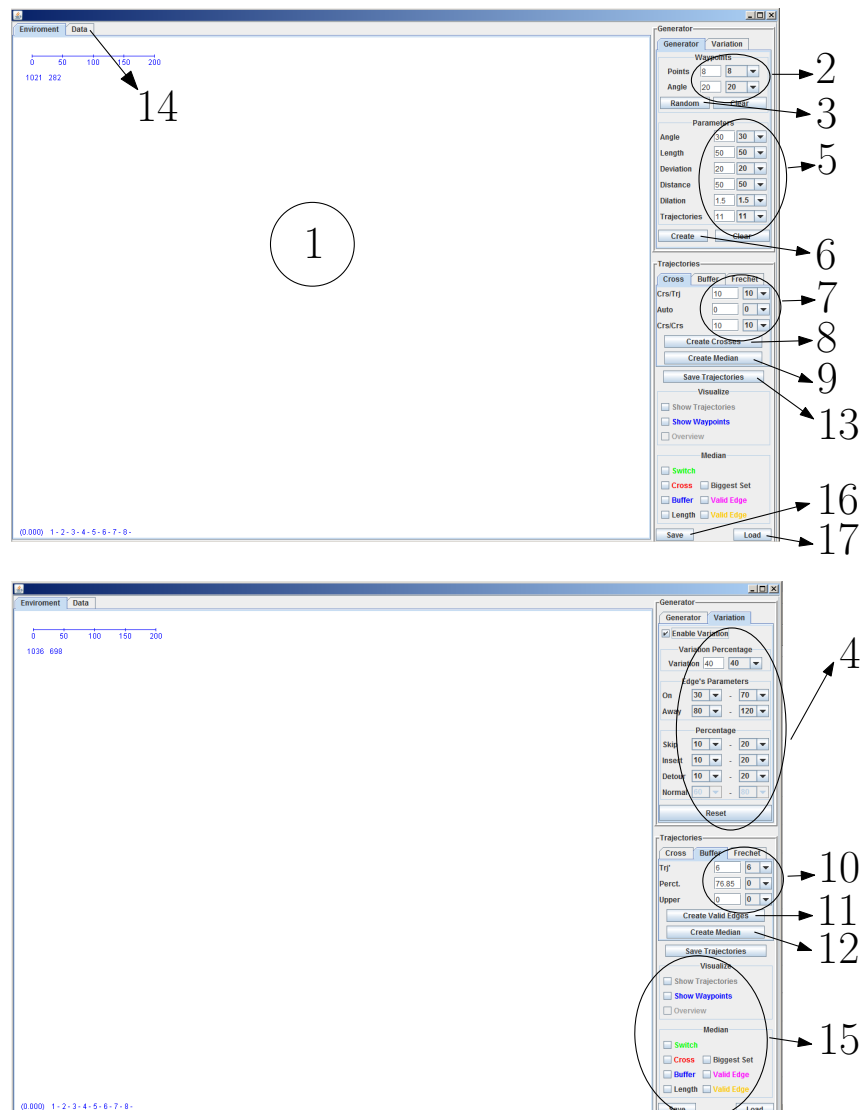
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# LAMPIRAN A

## THE PROGRAM

The interface of the program is shown in Figure A.1:



Gambar A.1: Interface of the program

Step by step to compute the median trajectory using the program:

1. Create several waypoints. Click anywhere in the “Environment” area(1) or create them automatically by setting the parameters for waypoint(2) or clicking the button “Random”(3).

2. The “Variation” tab could be used to create variations by providing values needed to make them(4).
3. Create a set of trajectories by setting all parameters(5) and clicking the button “Create”(6).
4. Compute the median using the homotopic algorithm:
  - Define all parameters needed for the homotopic algorithm(7).
  - Create crosses by clicking the “Create Crosses” button(8).
  - Compute the median by clicking the “Compute Median” button(9).
5. Compute the median using the switching method and the buffer algorithm:
  - Define all parameters needed for the buffer algorithm(10).
  - Create valid edges by clicking the “Create Valid Edges”button(11).
  - Compute the median by clicking the “Compute Median”button(12).
6. Save the resulting median by clicking the “Save Trajectories” button(13). The result is saved in the computer memory and can be seen in “Data” tab(14)
7. The set of trajectories and its median trajectories will appear in the “Environment” area(1) and the user can change what to display by selecting various choices in “Visualize” and “Median” area(15).
8. To save all data to the disk, click the “Save”(16) button. A file dialog menu will appear.
9. To load data from the disk, click the “Load”(17) button.

# LAMPIRAN B

## THE SOURCE CODE

Listing B.1: MyFurSet.java

```

1
2 import java.util.ArrayList;
3 import java.util.Collections;
4 import java.util.HashSet;
5
6 /**
7  *
8  * @author Lionov
9  */
10
11 //class for set of vertices close to furthest edge
12 public class MyFurSet {
13     protected int id; //id of the set
14     protected MyEdge FurthestEdge; //the furthest edge
15     protected HashSet<MyVertex> set; //set of vertices close to furthest edge
16     protected ArrayList<ArrayList<Integer>> ordered; //list of all vertices in the set for each
        trajectory
17     protected ArrayList<Integer> closeID; //store the ID of all vertices
18     protected ArrayList<Double> closeDist; //store the distance of all vertices
19     protected int totaltrj; //total trajectories in the set
20
21     /**
22     * Constructor
23     * @param id : id of the set
24     * @param totaltrj : total number of trajectories in the set
25     * @param FurthestEdge : the furthest edge
26     */
27     public MyFurSet(int id,int totaltrj,MyEdge FurthestEdge) {
28         this.id = id;
29         this.totaltrj = totaltrj;
30         this.FurthestEdge = FurthestEdge;
31         set = new HashSet<MyVertex>();
32         ordered = new ArrayList<ArrayList<Integer>>();
33         for (int i=0;i<totaltrj;i++) ordered.add(new ArrayList<Integer>());
34         closeID = new ArrayList<Integer>(totaltrj);
35         closeDist = new ArrayList<Double>(totaltrj);
36         for (int i = 0; i < totaltrj; i++) {
37             closeID.add(-1);
38             closeDist.add(Double.MAX_VALUE);
39         }
40     }
41
42     /**
43     * set a vertex into the set
44     * @param v : vertex to be added to the set
45     */
46     public void add(MyVertex v) {
47         set.add(v);
48     }
49
50     /**
51     * check whether vertex v is a member of the set
52     * @param v : vertex to be checked
53     * @return true if v is a member of the set, false otherwise
54     */
55     public boolean contains(MyVertex v) {
56         return this.set.contains(v);
57     }
58
59     /**
60     * create a column for table Gamma, sorted for each row
61     */
62     public void createColumn() {
63         for (MyVertex v : set) {
64             for (Integer key : v.vertexnum.keySet()) {
65                 for (Integer values : v.vertexnum.get(key)) {
66                     ordered.get(key).add(values);
67                 }
68             }
69         }
70         for (ArrayList<Integer> al : ordered) Collections.sort(al);
71     }

```

72 |  
73 |  
74 | }